

*SCHOOL ON SYNCHROTRON RADIATION AND APPLICATIONS*  
*In memory of J.C. Fuggle & L. Fonda*

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*Miramare - Trieste, Italy*

**1561/18**

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**Photoemission as a Solid State Spectroscopy:  
Many-Body Effects, Applications to Complex Materials**

**Juerg Osterwalder**

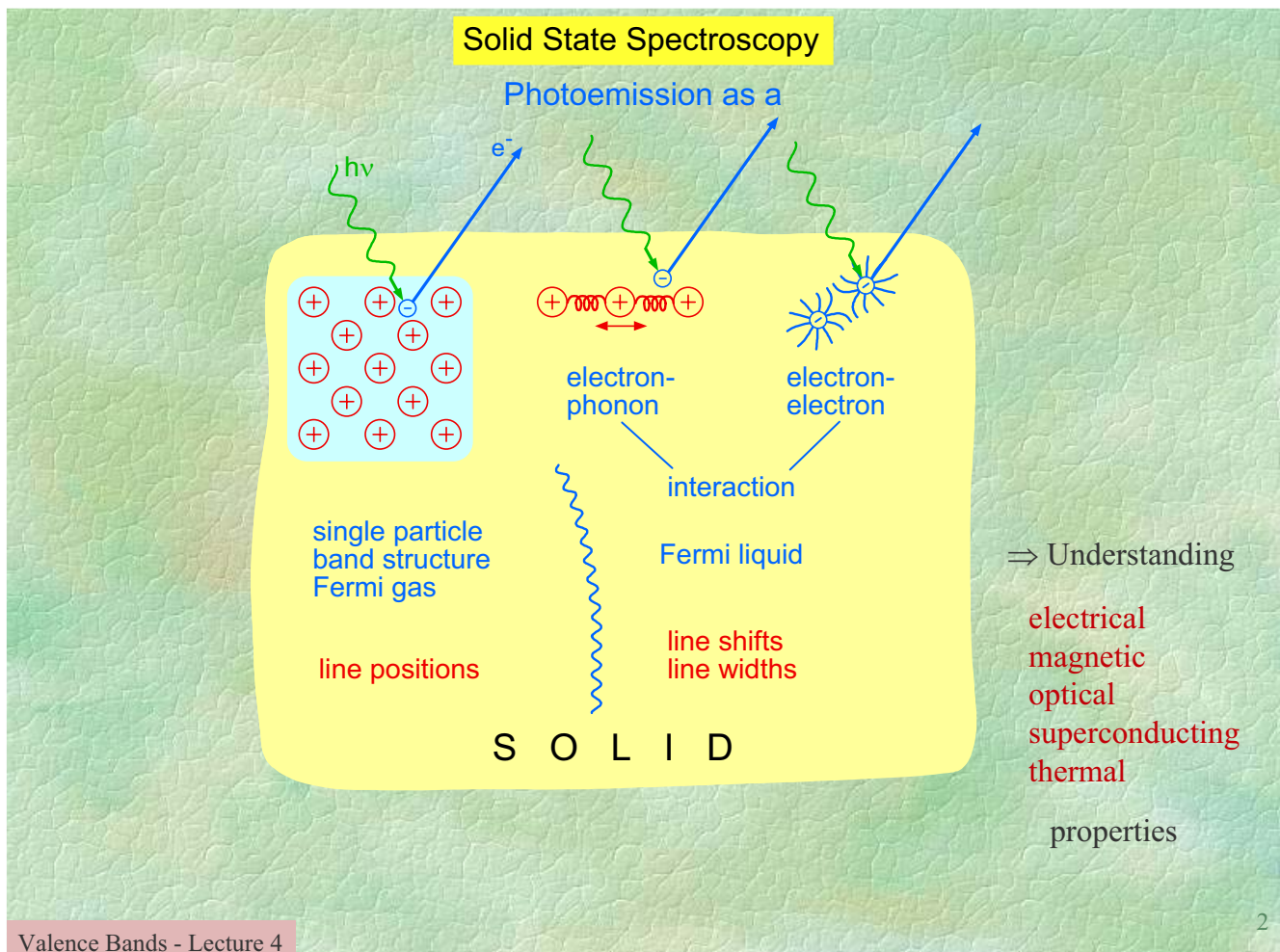
# Photoemission as a Solid State Spectroscopy: Many-Body Effects, Applications to Complex Materials

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<http://www.physik.unizh.ch/groups/grouposterwalder/>

## Lecture 4

- Many-Body Effects in Photoemission
- NiO: an Example for a Strongly Correlated System
- Theoretical Concepts: Sudden Approximation, Spectral Function
- Interpretation of Line Widths, Relation to Photoemission Experiments
- Energy Distribution Curves vs. Momentum Distribution Curves





# Manybody Effects in Photoemission

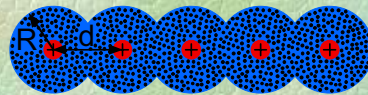
So far: one-electron picture (Fermi gas !)

But: **electrons** interact with **electrons** with phonons with ...

Two types of phenomena:

- $e^-$  - interaction in the **initial state**
  - hot topic in solid state physics (**strongly correlated materials, Fermi liquids** → **non-Fermi liquids**)
- $e^-$  - interaction during the **photoemission process**
  - **satellites, line shapes, line positions**
  - important for **interpretation of spectra** !

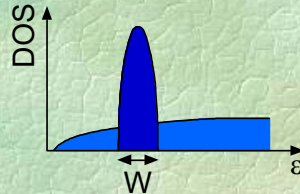
Two extreme types of states



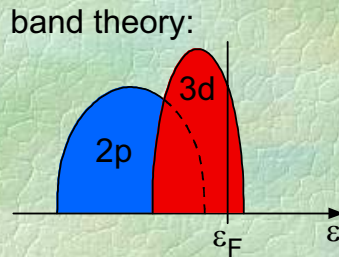
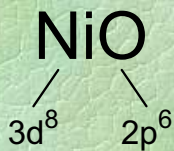
R - d : large overlap (s, p)  
large dispersion  $\epsilon(k)$   
nearly free electrons  
→ **one-electron picture** !



R << d : little overlap (d, f)  
little dispersion  
tight binding  
→ **correlation effects** !



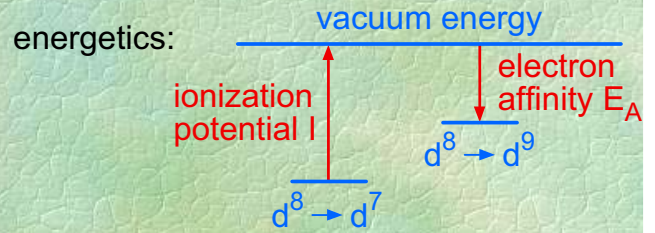
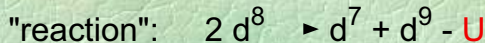
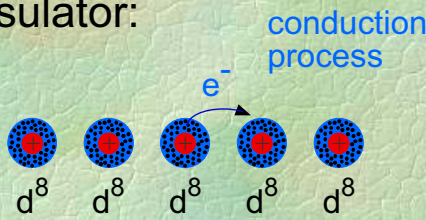
# NiO: an Example for a Strongly Correlated System



But: experiment shows insulating gap (4 eV) !

→ predicts a metal

Mott Insulator:

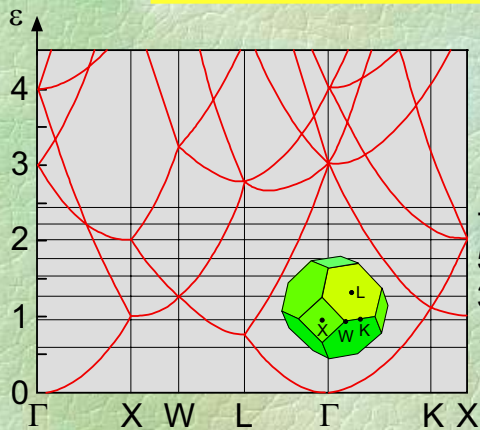


$$U = I - E_A$$

free ions : U = 18 eV  
solid state: reduced (O charge transfer)

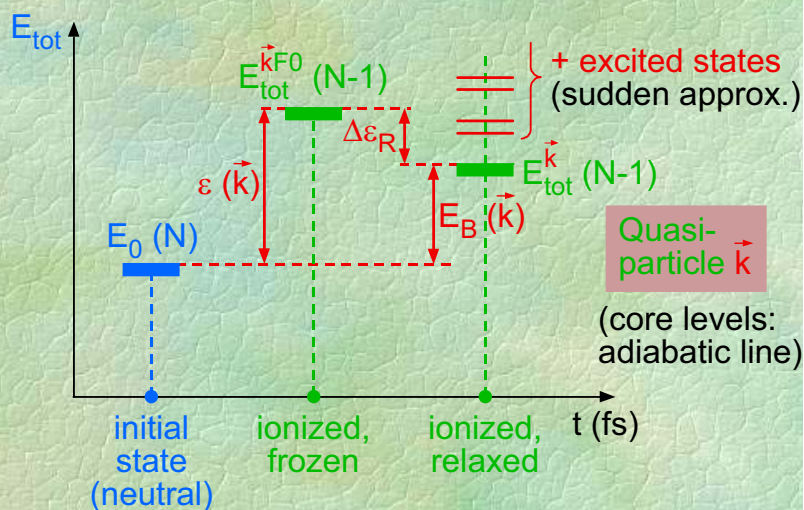


## Theoretical Concepts

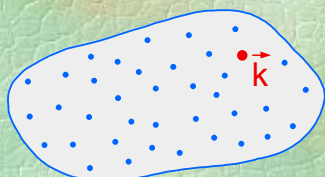


Theory:  
energy eigenvalues

## Total-Energy Diagram:



Koopman's Theorem:



N electrons

$$\varepsilon(\vec{k}) = E_{\text{tot}}^{\vec{k},\text{SCF}}(N) - E_{\text{tot}}^{\vec{k},\text{F0}}(N-1) < 0$$

"frozen orbitals"

## The Photocurrent I

Atoms, Molecules:

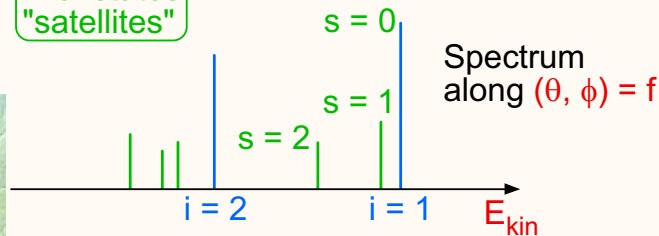
$$I \sim \left| \langle \phi_{f,E_{\text{kin}}} | \vec{r}_k \cdot \vec{\varepsilon} | \phi_{i,k}(\vec{r}_k) \rangle \right|^2 |c_s^{i,k}|^2 \delta(E_{\text{kin}} + E_s(N-1) - E_0(N) - hv)$$

various final states (angles, ...)

various orbitals

various atoms

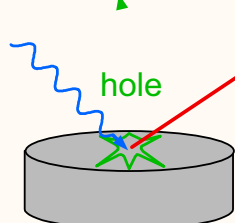
excited final states "satellites"



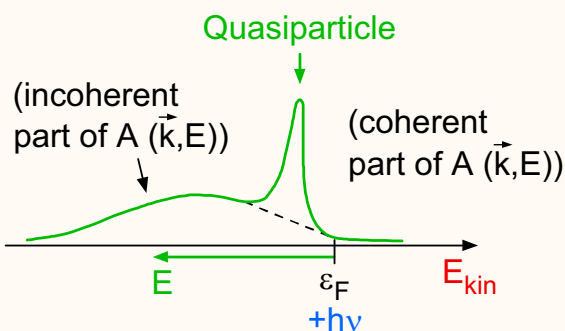
Solids:

$$I \sim \left| \langle \phi_{f,E_{\text{kin}}} | \vec{r}_k \cdot \vec{\varepsilon} | \phi_{i,\vec{k}} \rangle \right|^2 A(\vec{k}, E)$$

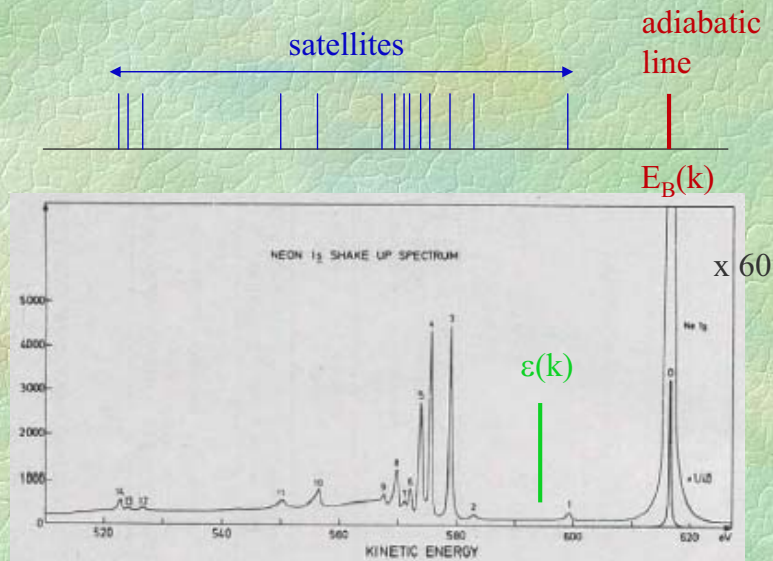
"Spectral Function"



sea of excitations



# The Photocurrent from Neon 1s



... and also Coupling to Lattice Degrees of Freedom - e.g. Adsorbate Vibrations

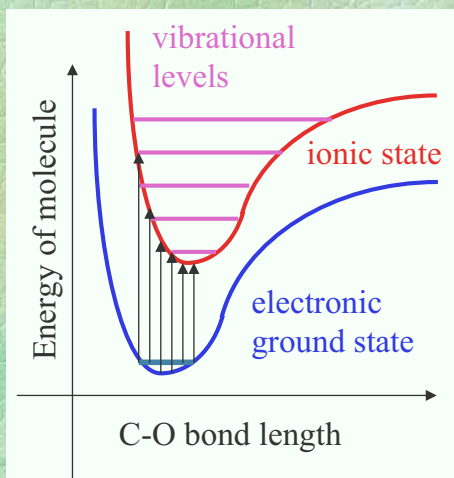
$$E_{\text{kin}} = h\nu - (E_{\text{final}} - E_{\text{initial}})$$

Photoelectron      Electronic or vibronic excitations      Ground state

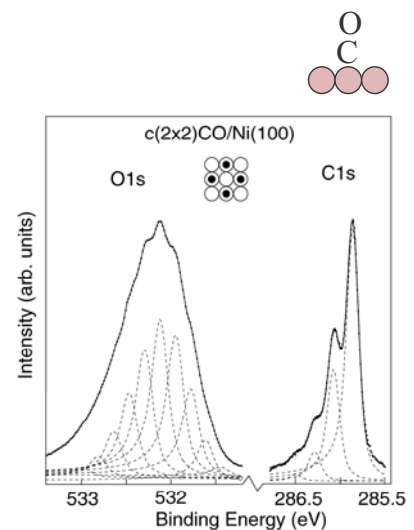
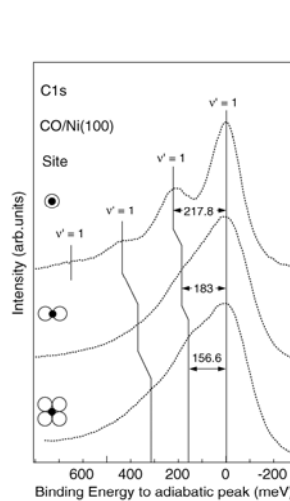
(chemical shift)

$E_{\text{final}}$  depends on ... bonding site

... where the photohole sits



=> Franck-Condon Principle



Föhlisch et. al Phys. Rev. Lett. 81 (1998) 1730



## Spectral Functions

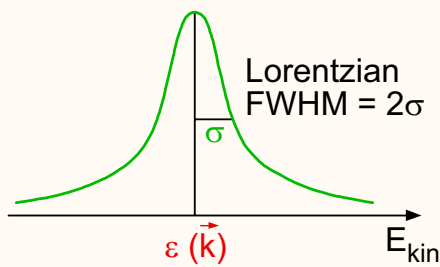
... can be calculated by **Greens Function Formalism**:

$$A(\vec{k}, E) = \frac{1}{\pi} \Im \{ G_+(\vec{k}, E) \}$$

independent particles  
(no interactions):

$$G_+^0(\vec{k}, E) = \frac{1}{E - \epsilon(\vec{k}) - i\sigma}$$

$$A(\vec{k}, E) = \frac{1}{\pi} \frac{\sigma}{(E - \epsilon(\vec{k}))^2 + \sigma^2}$$

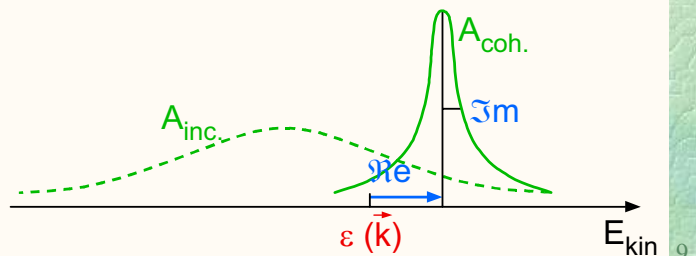


with interactions:

$$G_+(\vec{k}, E) = \frac{1}{E - \epsilon(\vec{k}) - \Sigma(\vec{k}, E)}$$

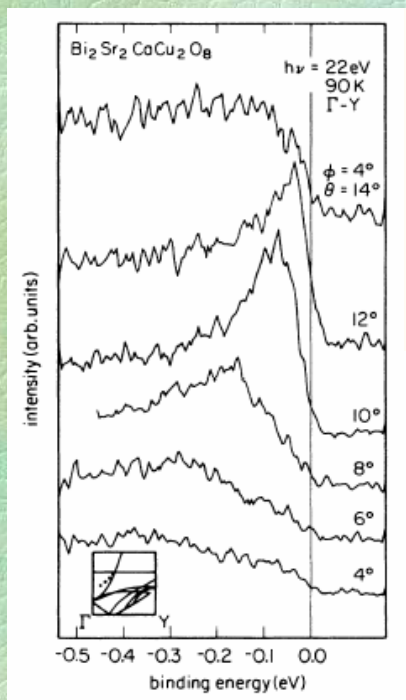
Self energy  
=> need Hamiltonian of system !

$$A(\vec{k}, E) \sim \frac{\Im \{ \Sigma(\vec{k}, E) \}}{[E - \epsilon(\vec{k}) - \Re \{ \Sigma(\vec{k}, E) \}]^2 + [\Im \{ \Sigma(\vec{k}, E) \}]^2}$$



## Experimental Situation on Line Widths

Fermi-liquid theory: Line width  $\Delta E \sim (E - E_F)^2$



Experiment on  
HTC material:

$$\Delta E \sim (E - E_F)$$

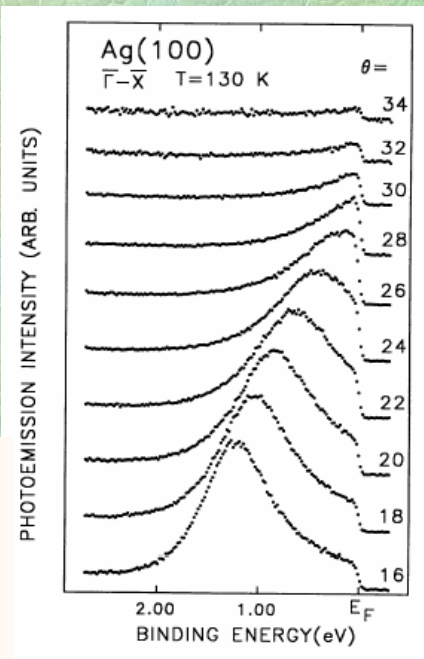
=> non-Fermi-liquid ?

C. G. Olson et al.,  
PRB 42, 381 (1990)

... but:

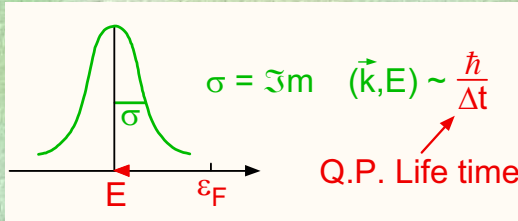
Silver (a much simpler material)  
even shows a growing line width  
towards  $E_F$  !

Y. Hwu et al.,  
PRB 45, 5438 (1992)

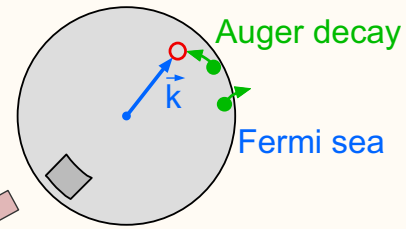


=> One needs to know  
the technique well !

## Interpretation of Line Widths



dominant hole decay processes:

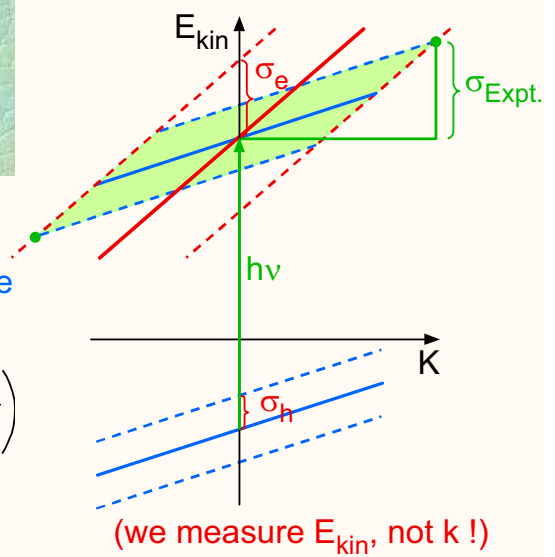


Fermi liquid theory

$$\rightarrow \Delta t \sim \frac{1}{E^2}$$

$$\rightarrow \sigma \sim E^2$$

**Caution!**



Photoemission measures

hole lifetime  $\frac{1}{\sigma_h}$   
and photoelectron lifetime

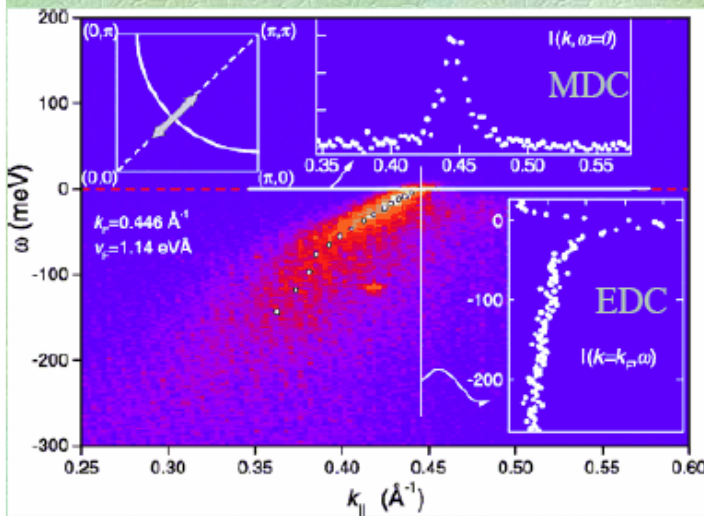
normal emission:  
(P.Thiry, 1981)

$$\sigma_{Expt.} = \frac{v_e^\perp \cdot v_h^\perp}{v_e^\perp - v_h^\perp} \cdot \left( \frac{\sigma_h}{v_h^\perp} + \frac{\sigma_e}{v_e^\perp} \right)$$

group velocities  $\frac{\partial \epsilon}{\partial k_i}$

## Energy Distribution Curves (EDCs) and Momentum Distribution Curves (MDCs)

Example: Dispersion Plot from BSCCO High Temperature Superconductor

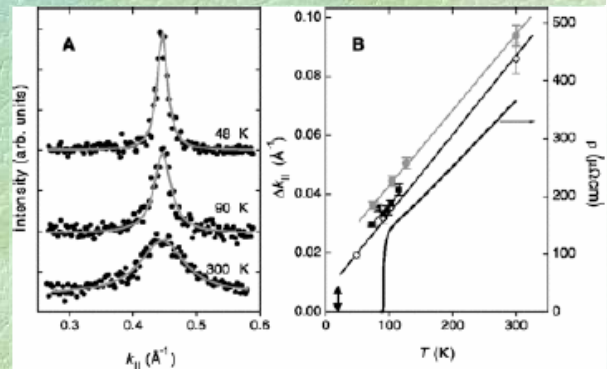


⇒ Connection between photoemission data and sample resistivity

Line Width  $\Delta k$  in MDCs is related to the mean free path  $\Lambda$  of the electrons near  $E_F$  and thus to the scattering rate:

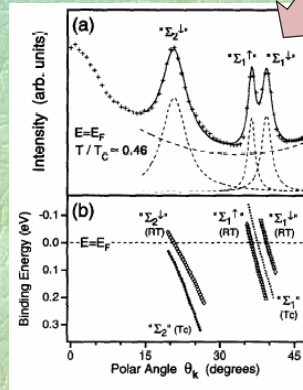
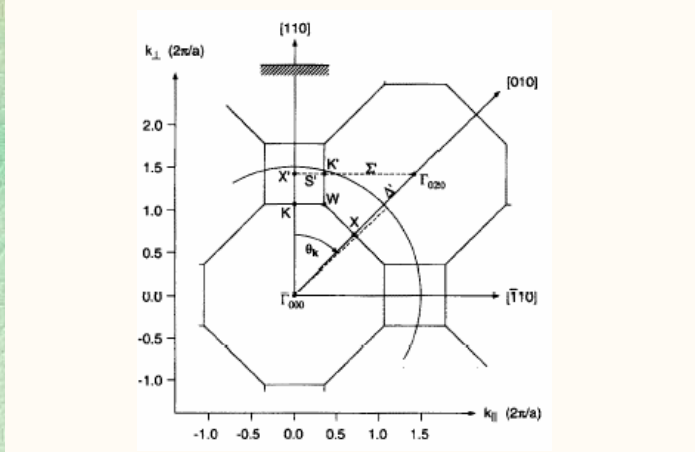
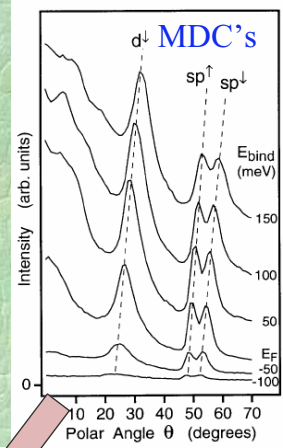
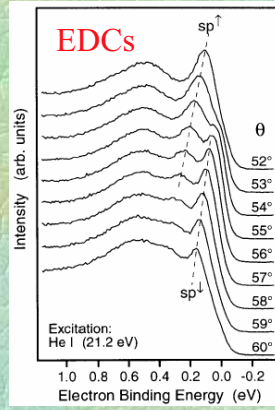
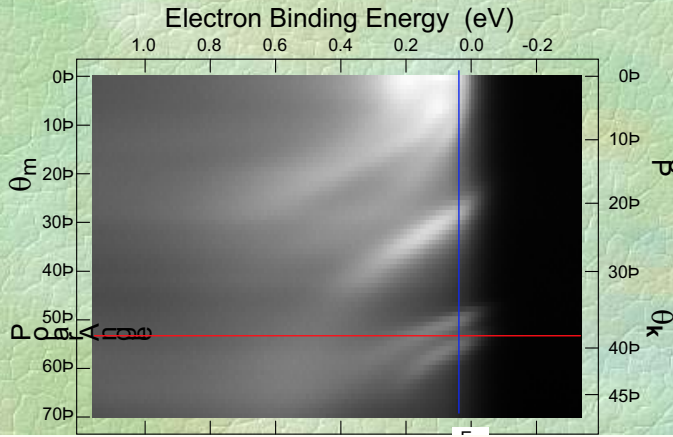
$$\hbar v_k \Delta k = \frac{\hbar v_k}{\Lambda} \approx |2\Im \Sigma(\vec{k}, \omega)|$$

( $v_k$  is the electron group velocity)





# Extracting Energy Dispersion



... often more accurately from MDCs ! (simpler line shapes)



# Photoemission as a Solid State Spectroscopy: Many-Body Effects, Applications to Complex Materials

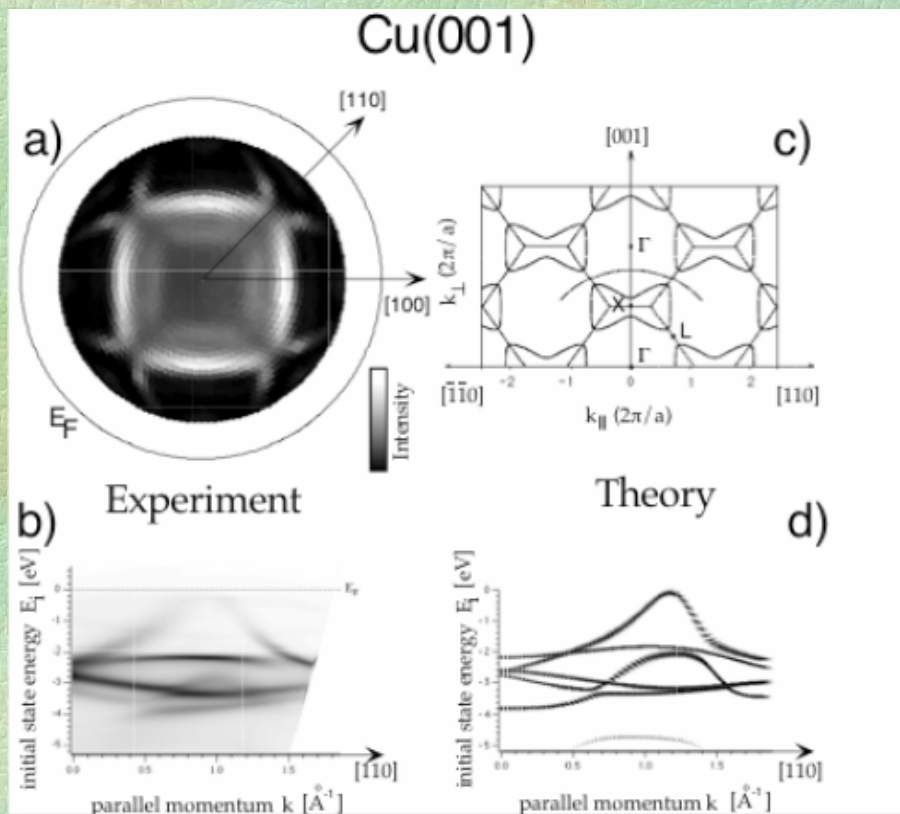
Jürg Osterwalder

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<http://www.physik.unizh.ch/groups/grouposterwalder/>

## Lecture 5

- Electron-Electron Interaction: Weak Effects in Photoemission from Cu
- Electron-Electron Interaction: Strong Effects in Photoemission from Ni and Co
- Electron-Phonon Interaction: Renormalization of Dispersion by Phonons
- Applications: Observation of a Giant Kohn Anomaly on H/Mo(110)
- Applications: Photoemission from High and Low  $T_c$  Superconductors

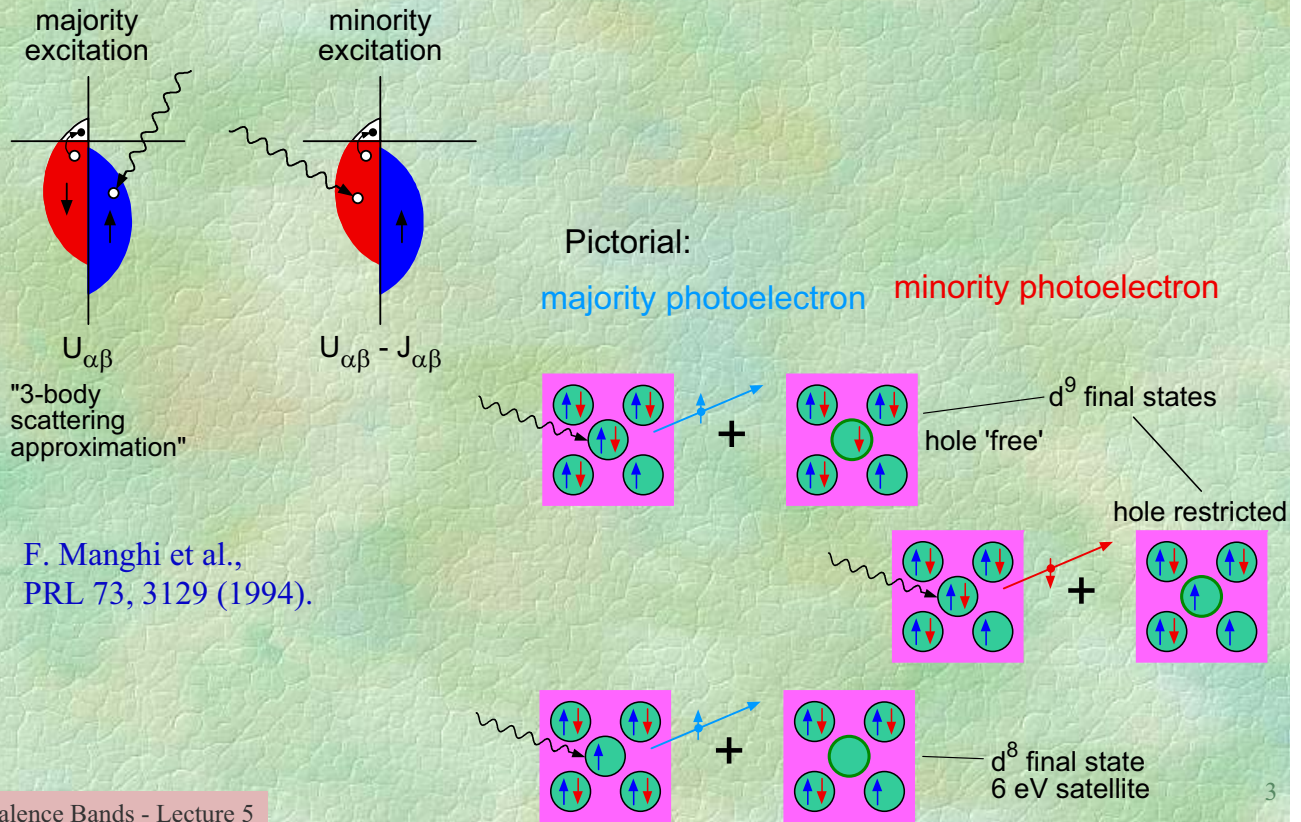
## Weak Electron-Electron Interaction Effects in Photoemission from Cu





# Valence Photoemission from Ni

$3d^{9.4} \rightarrow$  correlation effects in the 3d channel

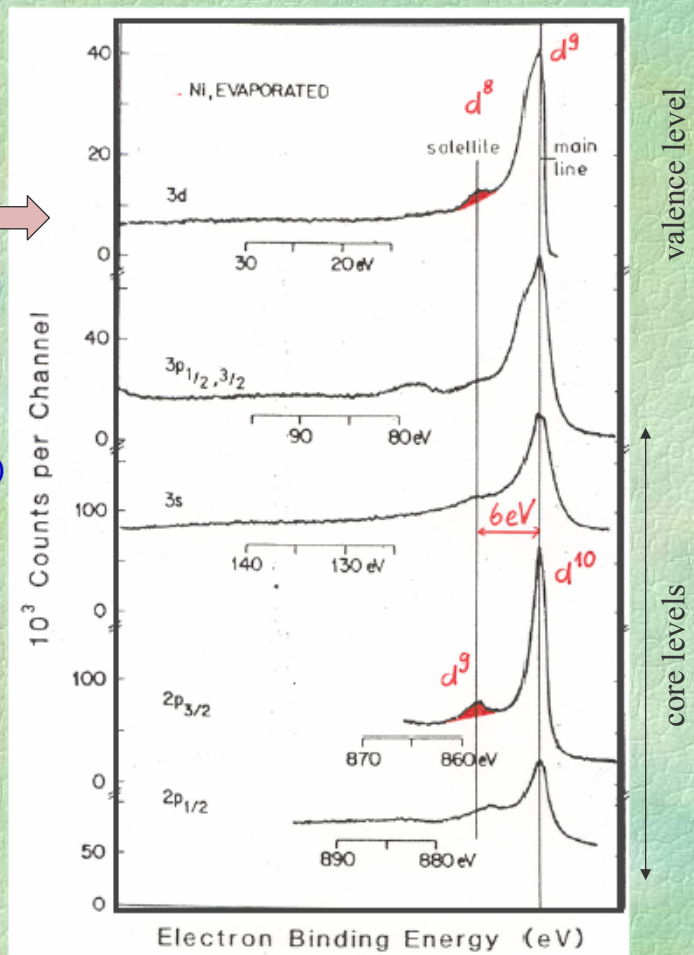
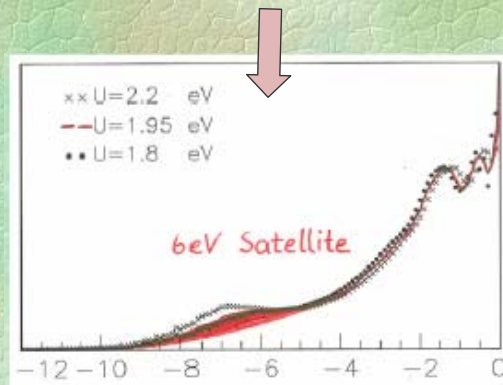


F. Manghi et al.,  
PRL 73, 3129 (1994).

## The 6 eV Satellite in Ni Metal

Experiments: Each photohole is accompanied by a 6 eV satellite  
(S. Hüfner, Photoelectron Spectroscopy (Springer, Berlin 1995))

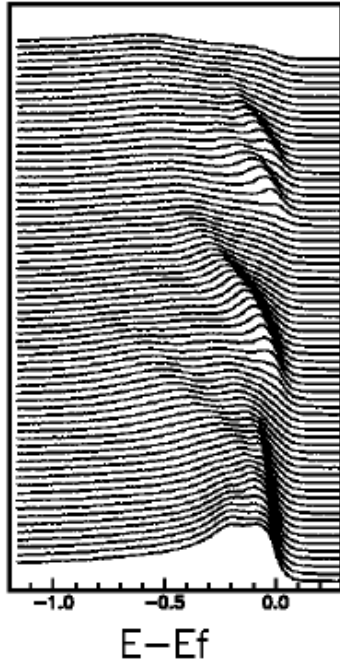
Theory: 3BS Model  
(F. Manghi et al., PRB 59, R10409 (1999))



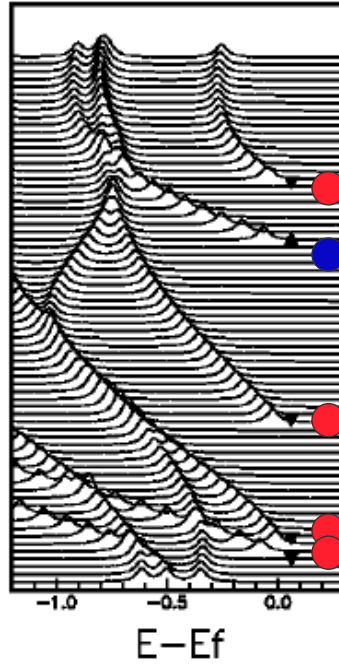


# Renormalization of Band Dispersion by e-e Interaction: Ni

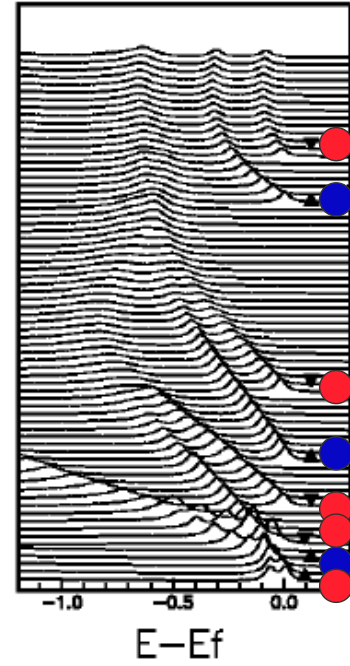
Experiment



Theory  
(single particle)



Theory  
(3BS model)

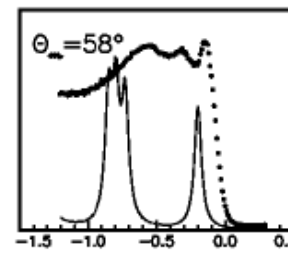
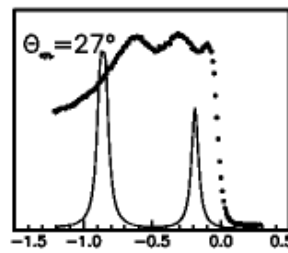
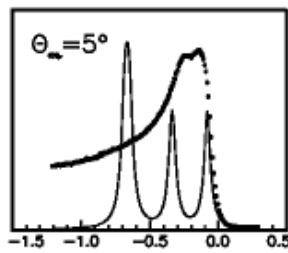


● Minority spin

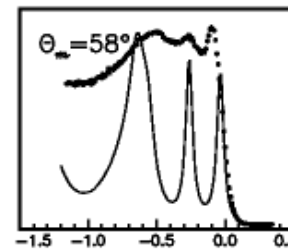
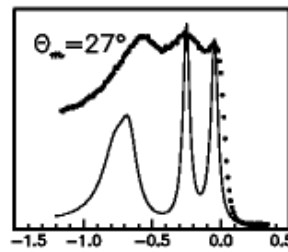
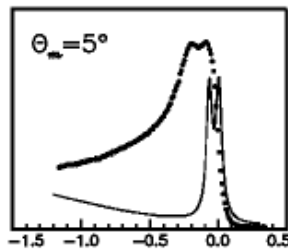
● Majority spin

# Quantitative Comparison of e-e Interaction Effects in Ni

Single particle (LDA)



Quasi particle (3BS)

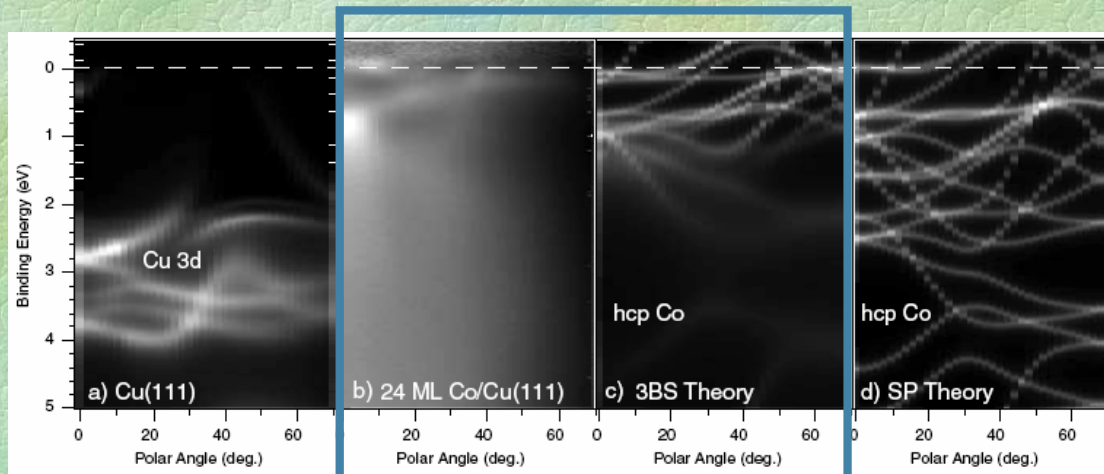


# Even Stronger Renormalization in Cobalt

Sample:

Co(0001)

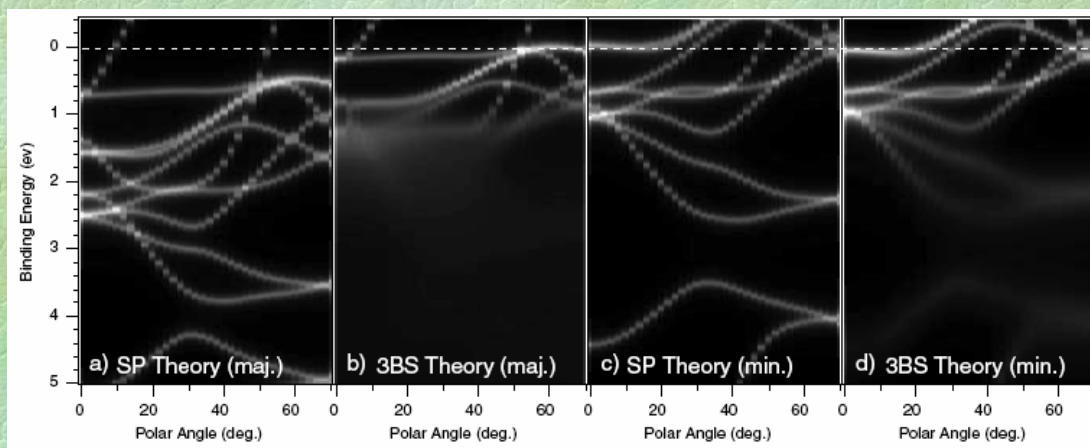
Cu(111)



Single particle

Strong many-body effects !

# Many-Body Effects are Strongly Spin Dependent



Majority spin

Minority spin



# Electron-Phonon Interaction: Renormalization of Dispersion by Phonons

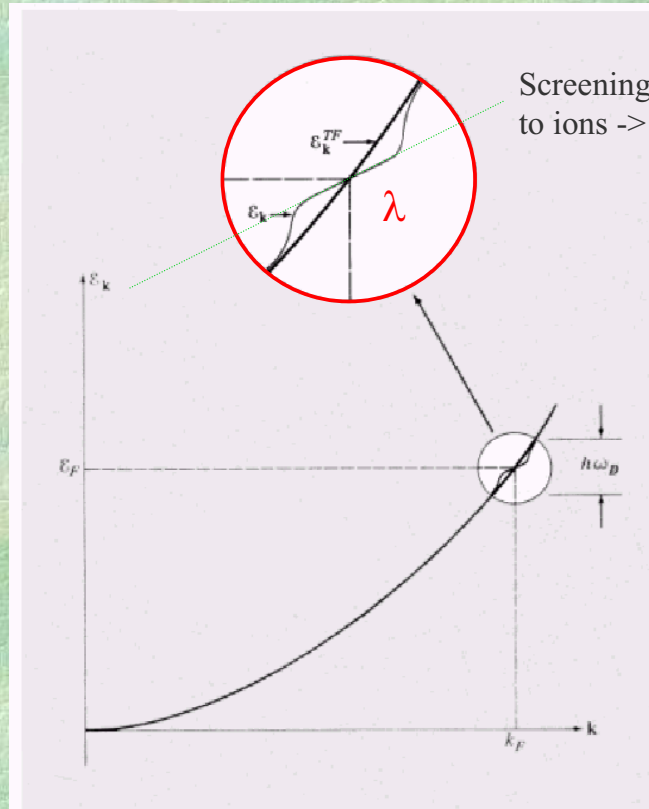
$\lambda$   
electron-mode  
coupling constant

Renormalization of  $m^*$  by

$$Z^{-1} = 1 + \lambda$$

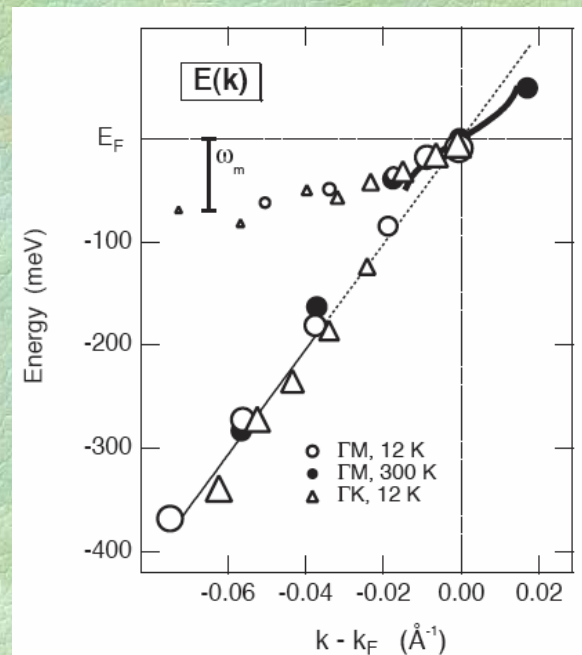
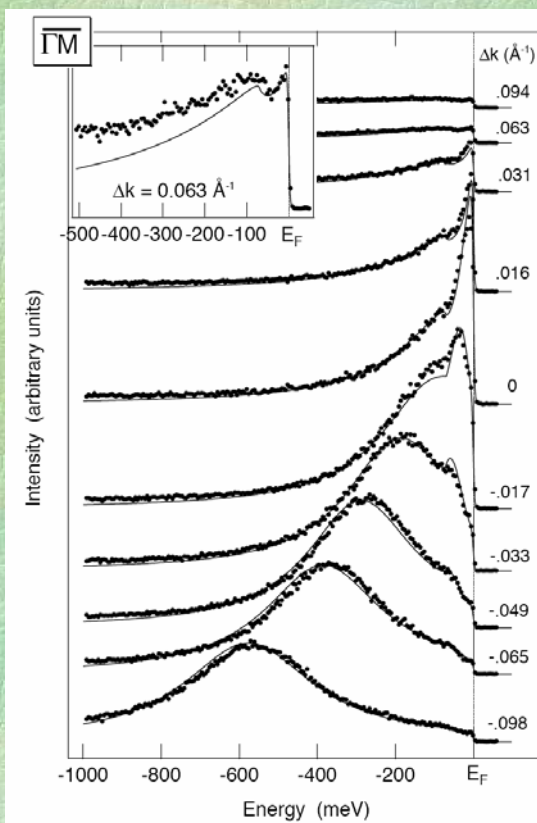
Some values for  $\lambda$ :

Cu 0.15  
Be 0.24  
Pb 1.50



Ashcroft, Mermin  
"Solid State Physics"

# Observation of $m^*$ Renormalization in Beryllium

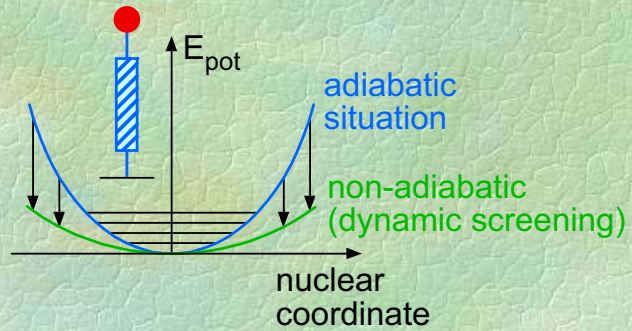
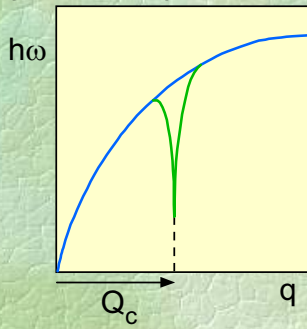


M. Hengsberger et al.,  
PRL 83, 592 (1999).



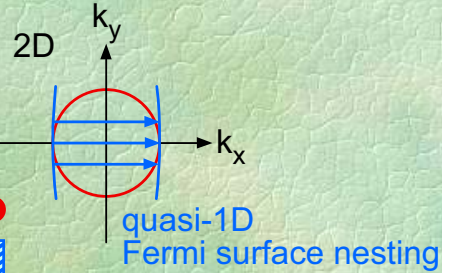
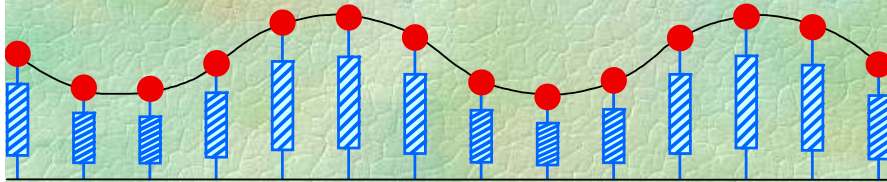
# Giant Kohn Anomaly

phonon dispersion curve



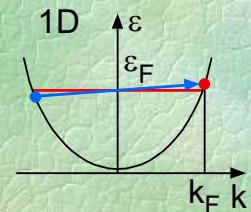
e.g. transversal mode:

$$\Lambda = \frac{2\pi}{Q_c}$$

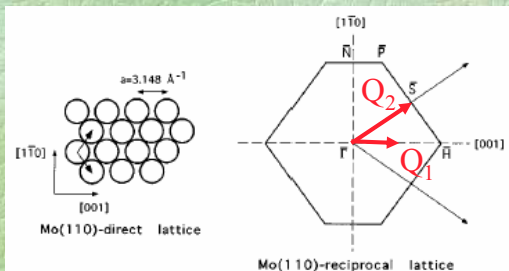


optimum screening:

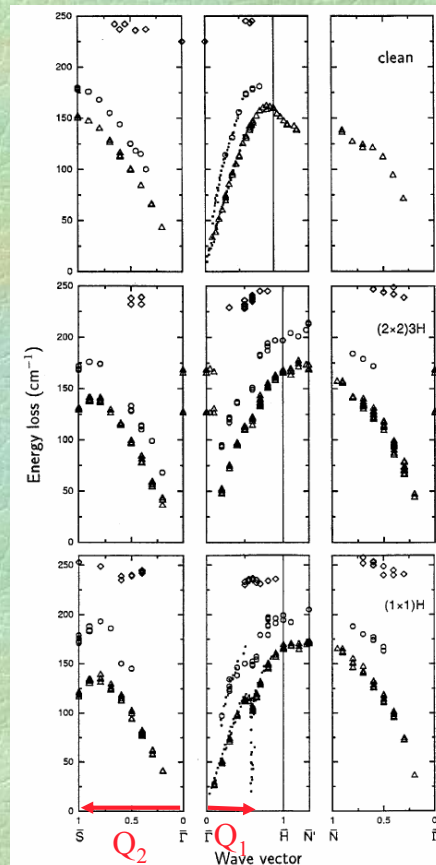
- standing wave with same wave number ( $Q_c = 2 k_F$  !)
- large phase space for  $e^-$  - hole pair excitations (low  $\epsilon$  / high  $q$ )



## Surface Phonon Modes for H/Mo(110) - A Giant Kohn Anomaly ?



HREELS Data



clean

0.75 ML

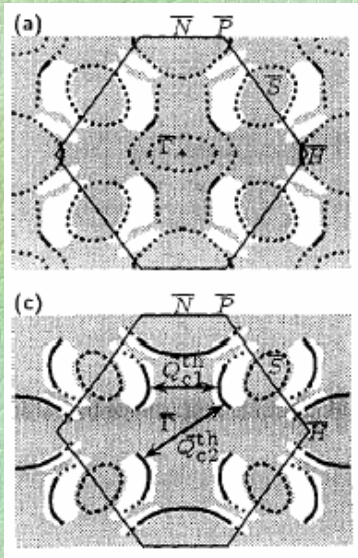
1 ML

J. Kröger et al., PRB 55, 10895 (1997)

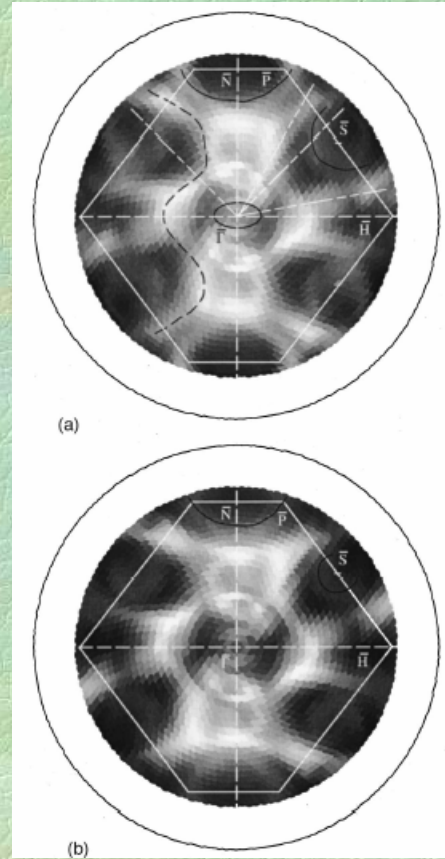


# Fermi Surface Contours of Surface States on Mo(110)

Theory:



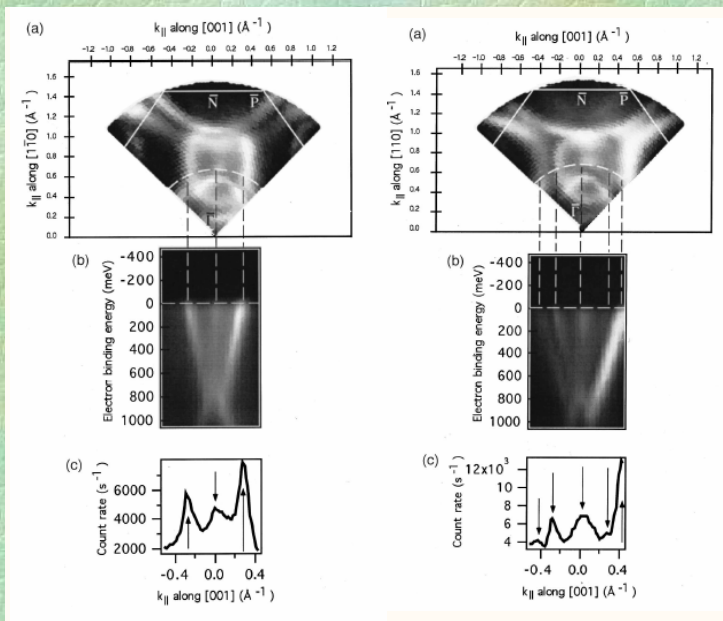
B. Kohler et al., PRL 74, 1387 (1995)



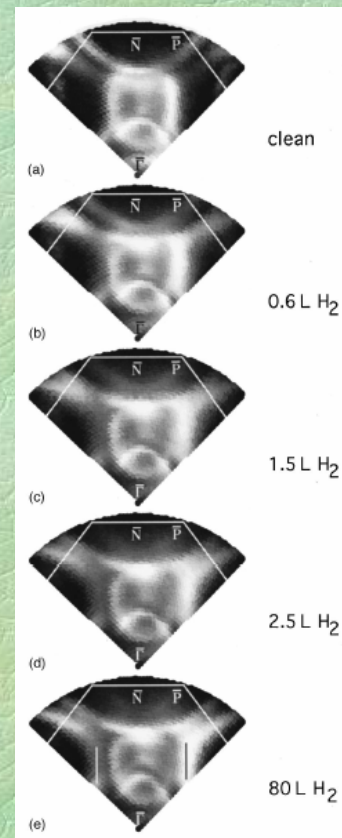
Clean Mo(110)

1 ML Hydrogen

# Evolution of Fermi Surface Contours with Hydrogen Coverage

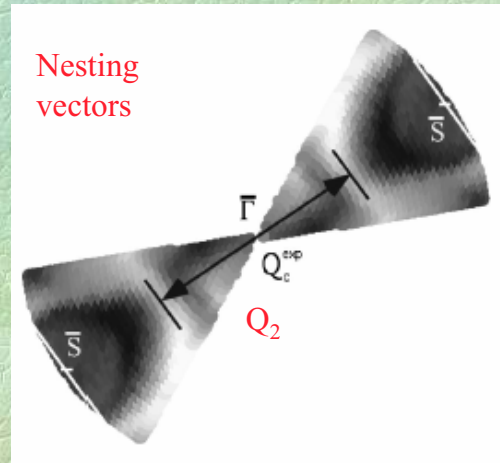
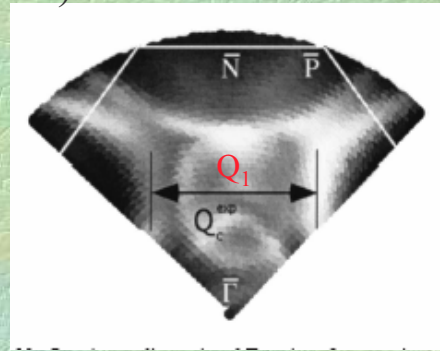
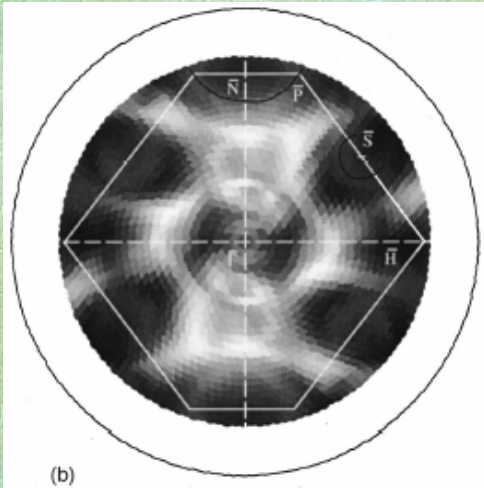


=> H-induced shift of Fermi surface contour



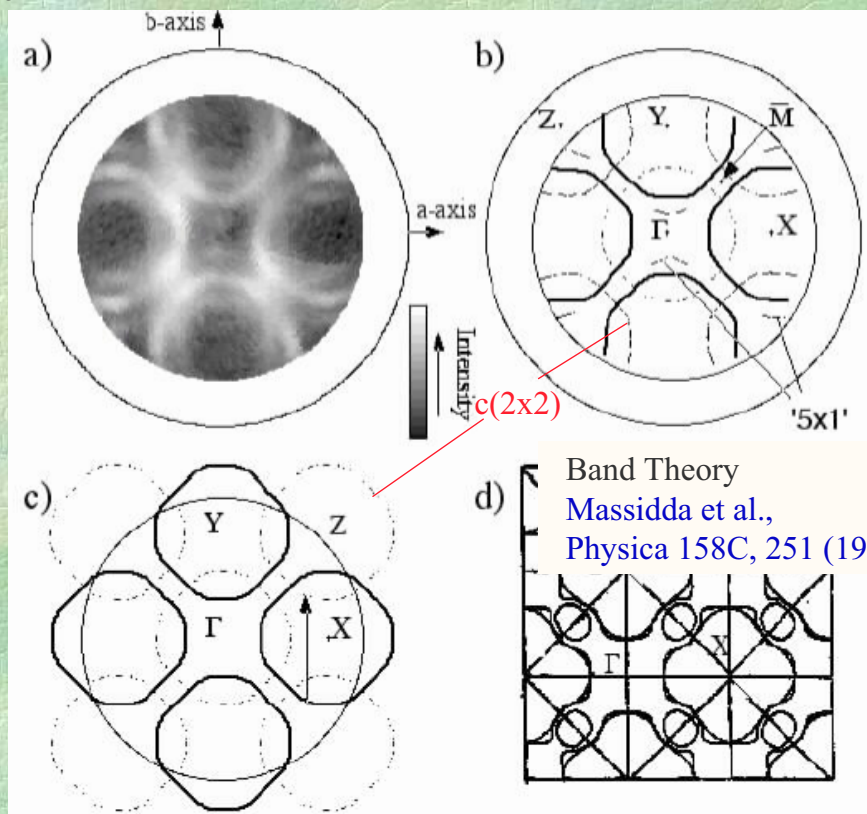


## Fermi Surface Nesting on 1 ML H/Mo(110) Seen by Photoemission



	$Q_1(\text{\AA}^{-1})$	$Q_2(\text{\AA}^{-1})$
EELS	0.90	1.22
PE	0.85	1.19
DFT	0.86	1.23

## Fermi Surface Mapping on a High Temperature Superconductor: $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ (001)



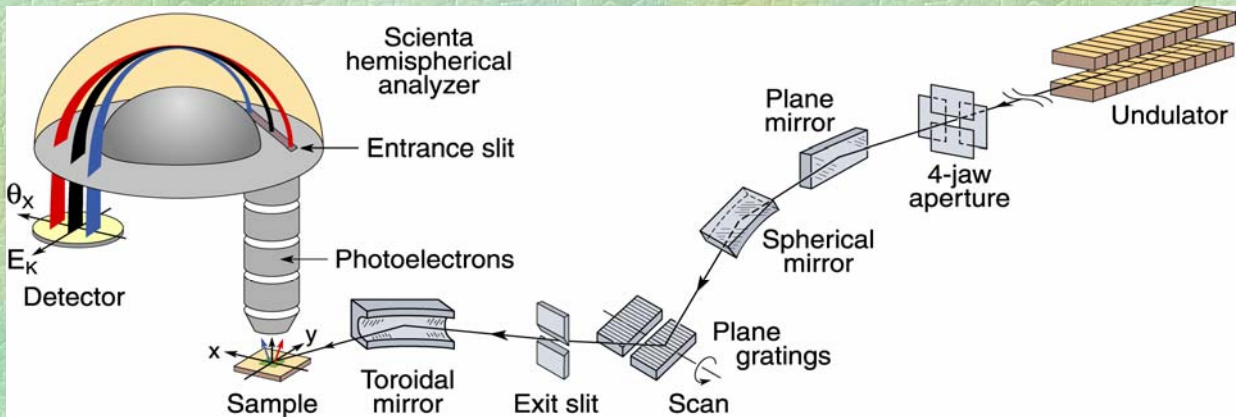
P. Aebi et al.,  
PRL 72, 2757 (1994)

Band Theory  
Massidda et al.,  
Physica 158C, 251 (1988)



# High-Resolution Photoemission

A state-of-the-art photoemission beamline at Stanford (SSRL)

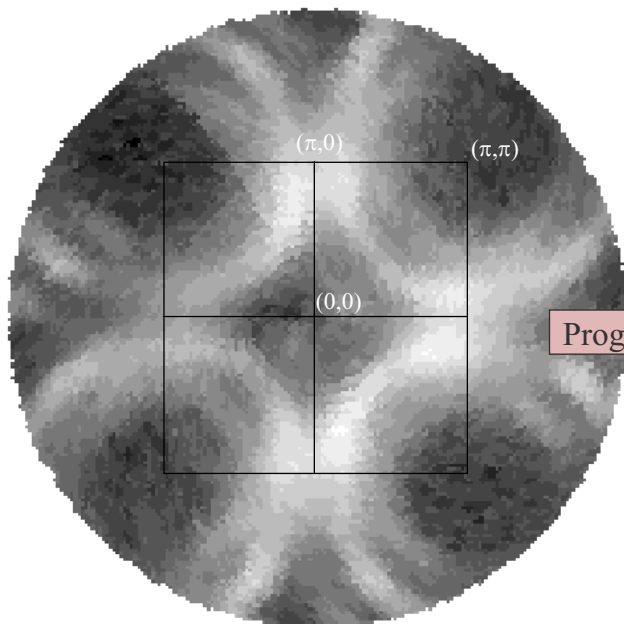


**Highest resolution in energy and momentum**

~ 2 meV in energy

~ 0.005 Å<sup>-1</sup> in momentum

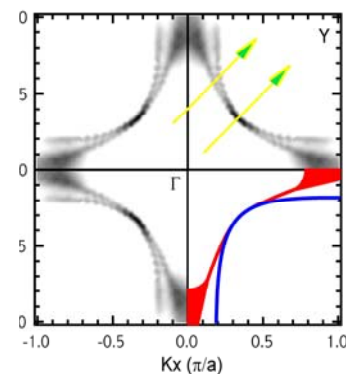
Bi2212:  
First Fermi surface mapping,  
superstructure contours



P. Aebi et al., Phys. Rev. Lett. 72, 2757 (1994).

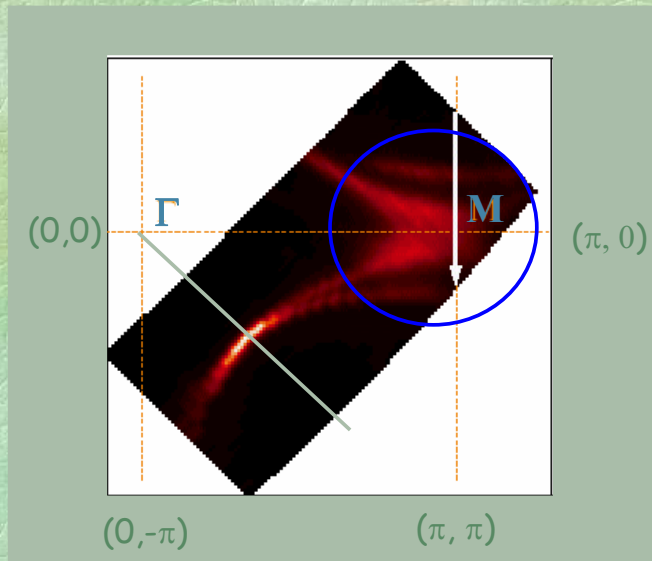
Pb-doped Bi2212:  
-layer splitting

Two CuO layers  
per unit cell



gdanov et al.,  
ys. Rev. B 64, 180505 (2001)

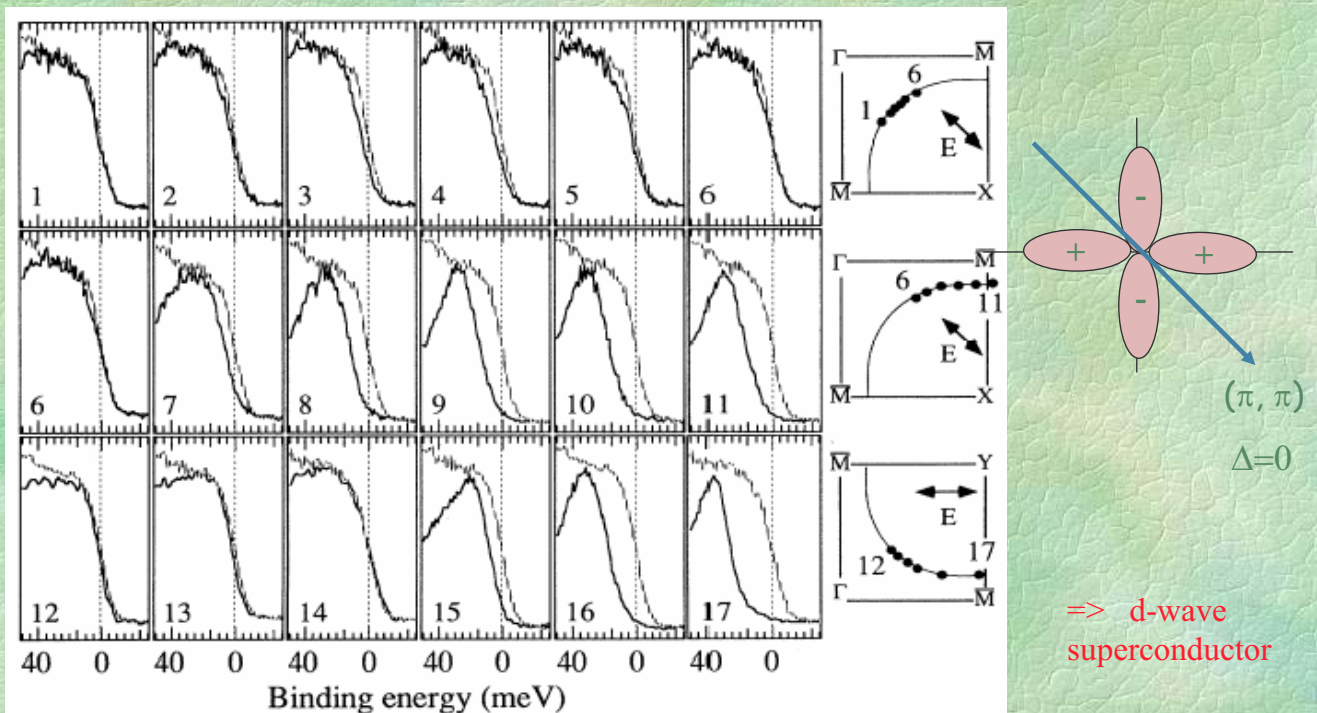
## Details on the Fermi Surface of BSCCO



- Superstructure
- Superconducting Gap
- Bilayer Splitting

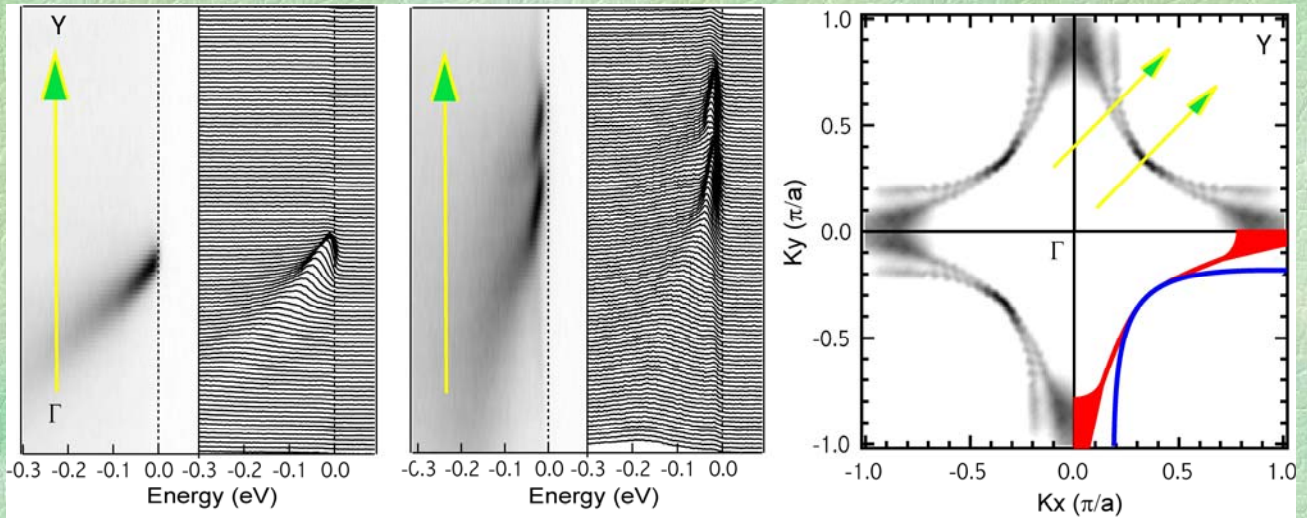
## Anisotropy of the Superconducting Gap in BSCCO

... need to measure spectra exactly on the Fermi surface !





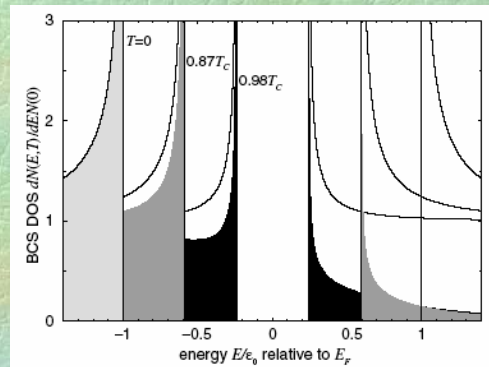
# Pb-doped Bi2212: Bi-layer splitting



High **energy and momentum** resolution combined with improved sample enables the clear observation of bilayer splitting

# In Conventional Superconductors it is Much Harder to See the Gap !

Density of states near  $E_F$  in the superconducting state: BCS model for different temperatures



Sample:

$V_3Si$

$T_c = 17 K$

$\Delta_{gap} = 5 meV$

Instr. Res. 2.9 meV !

F. Reinert et al.,  
PRL 85, 3930 (2000)

