



the  
**abdus salam**  
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*SCHOOL ON SYNCHROTRON RADIATION AND APPLICATIONS  
In memory of J.C. Fuggle & L. Fonda*

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**Computed Tomography**

**Diego Dreossi & Silvia Pani**

# Computed Tomography

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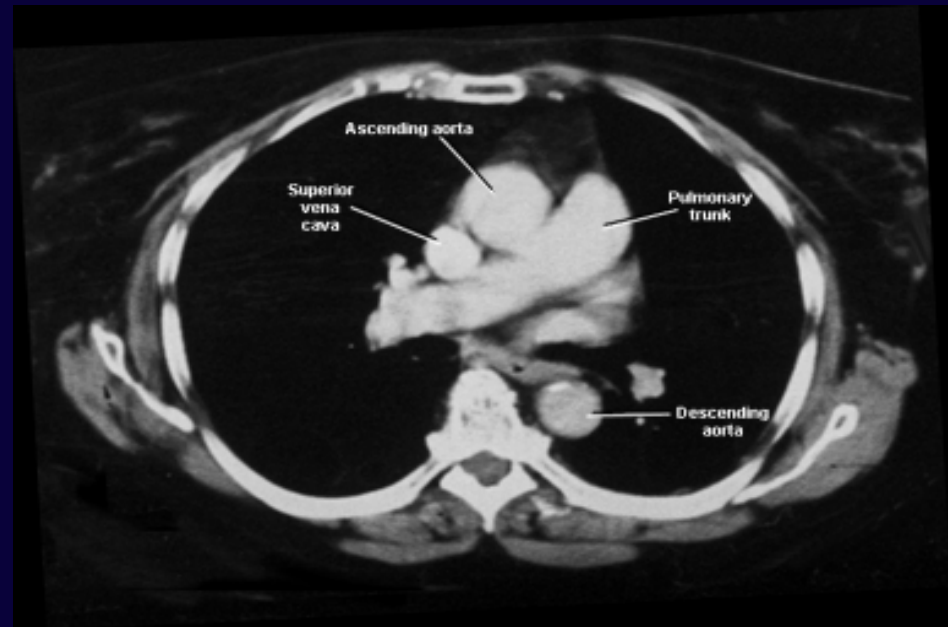
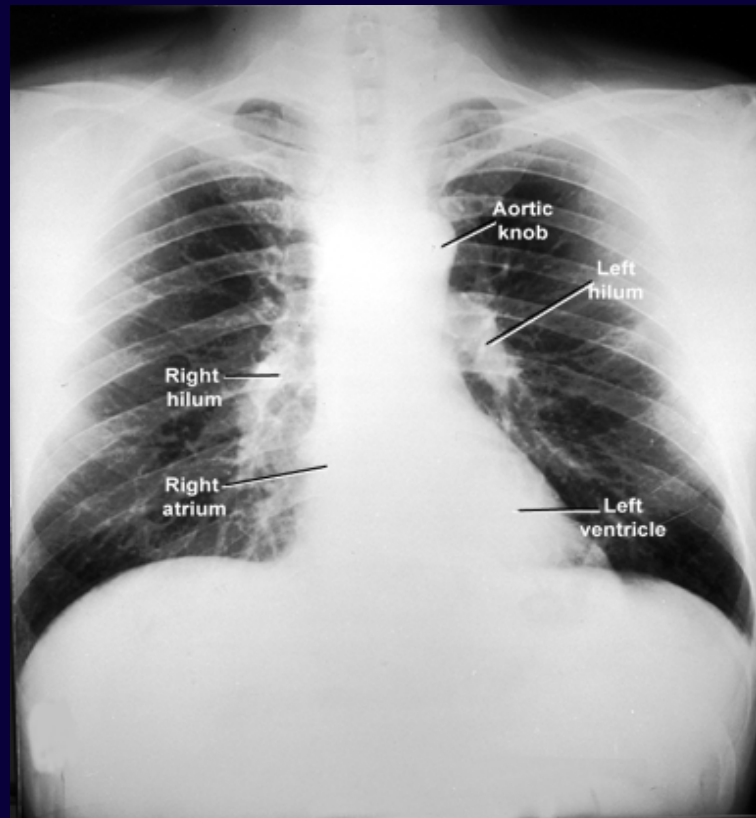
# Summary

- Computed Tomography
  - Purpose
  - How does it work?
- CT reconstruction
  - Filtered backprojection
- Synchrotron radiation CT
- MicroCT at the SYRMEP beamline
- Further applications

## The goal

- To provide a three-dimensional information (depth of the structures/organs)
- To provide information about the attenuation coefficient (tissue characterization)

## From planar imaging... to CT

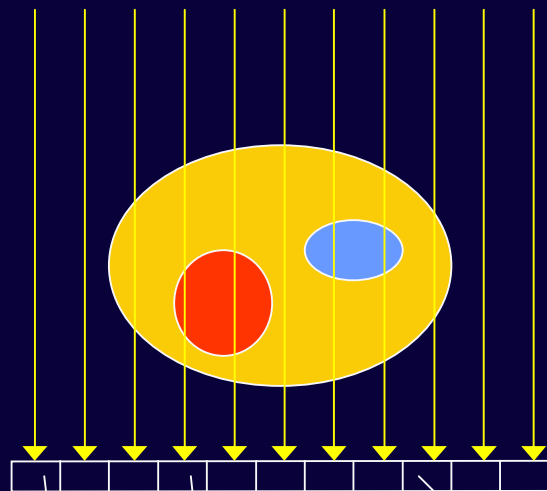


Source: University of Arkansas Medical School  
<http://anatomy.uams.edu/HTMLpages/anatomyhtml/xraythorax.html>

## How does it work?

- Laminar beam and laminar detector
- The object/patient is rotated in front of the beam
- During the rotation, planar images (projections) are acquired at different angles
- The matrix of acquired data is called SINOGRAM: each line of the sinogram corresponds to a projection at a given angle
- A map of the attenuation coefficients is reconstructed from the sinogram by means of proper algorithms

# Image acquisition

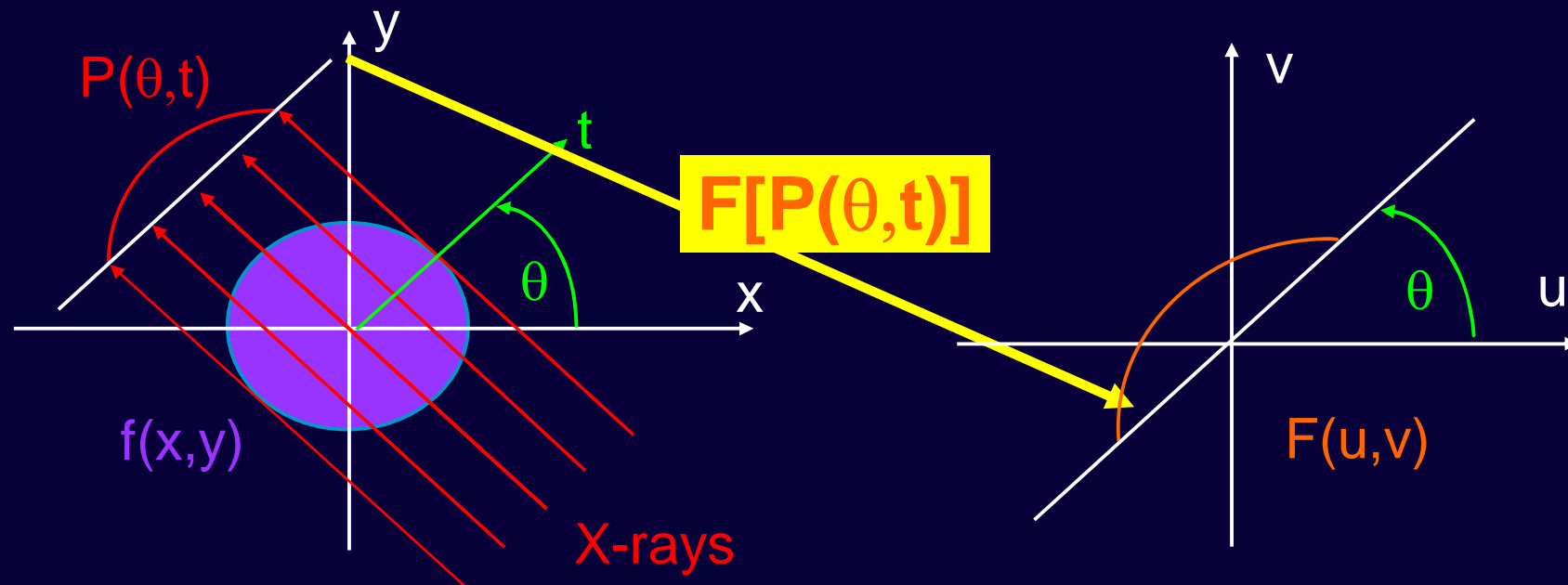


- The line integral of the attenuation coefficient determines the attenuation along each X-ray path

$$I_0$$
$$I_0 e^{-\int_{l_1} \mu dx}$$
$$I_0 e^{-\int_{l_2} \mu dx}$$

# Image reconstruction: backprojection

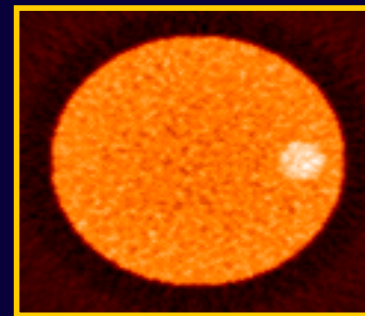
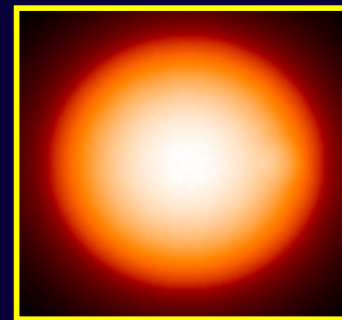
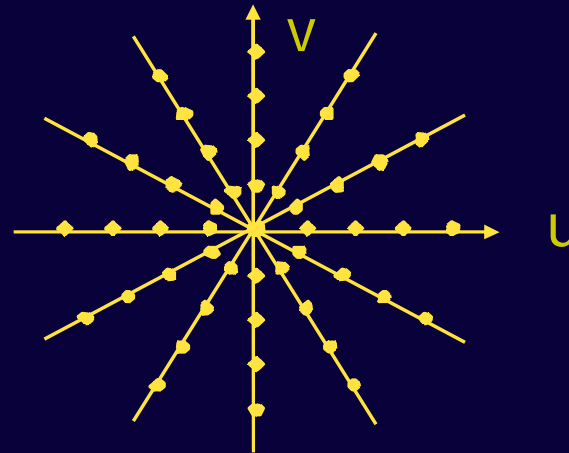
- Purpose: obtaining the distribution function  $f(x,y)$  given a complete set of projections  $P(\theta,t)$
- Fourier slice theorem: the FT of a projection  $P(\theta,t)$  corresponds to a sampling of the FT of  $f(x,y)$  along a line tilted by an angle  $\theta$





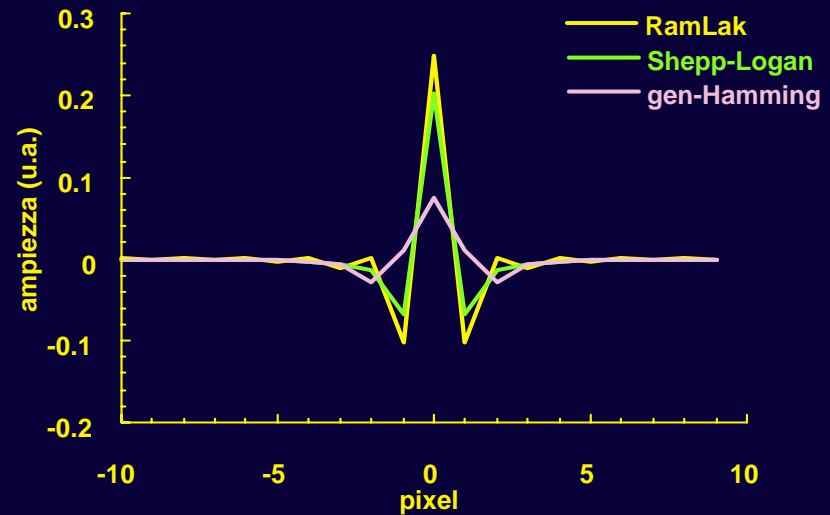
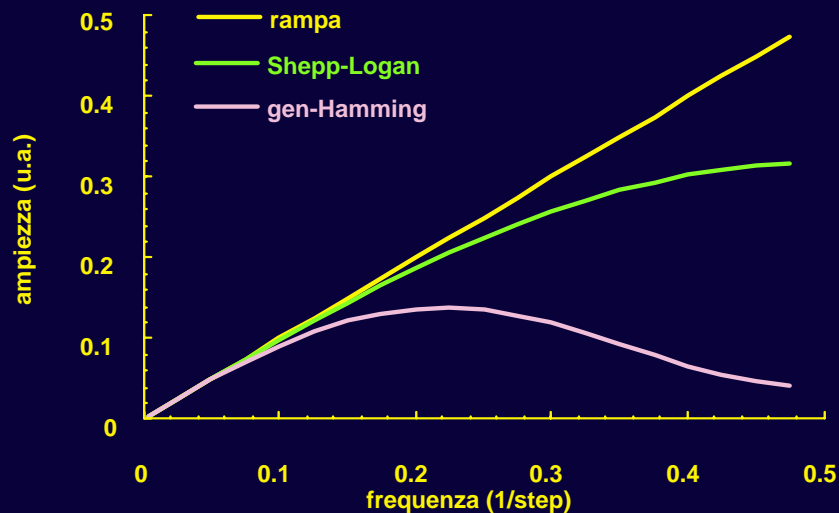
# Filtered backprojection

- Each pixel of the matrix is reconstructed by summing up all projections crossing it
- But: oversampling for low frequencies!



Filtering: each transformed projection is multiplied by a function reducing the contribution of low frequencies

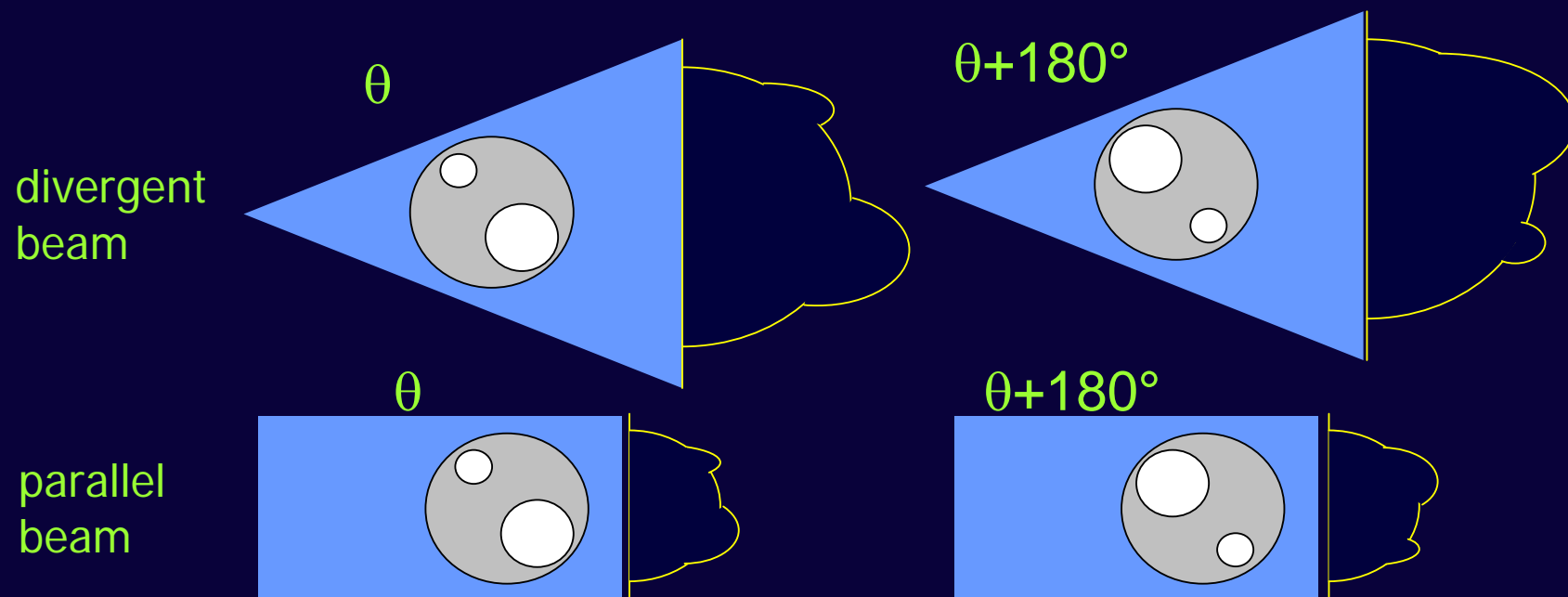
# Filtered backprojection



- Ramp filter (RamLak): enhancement of high frequencies  
→ noise
- Gen-Hamming, Shepp-Logan: enhancement of intermediate frequencies
- Convolution theorem → convolution in the direct space as an alternative to multiplication in the Fourier space

# The advantages of SR CT – I

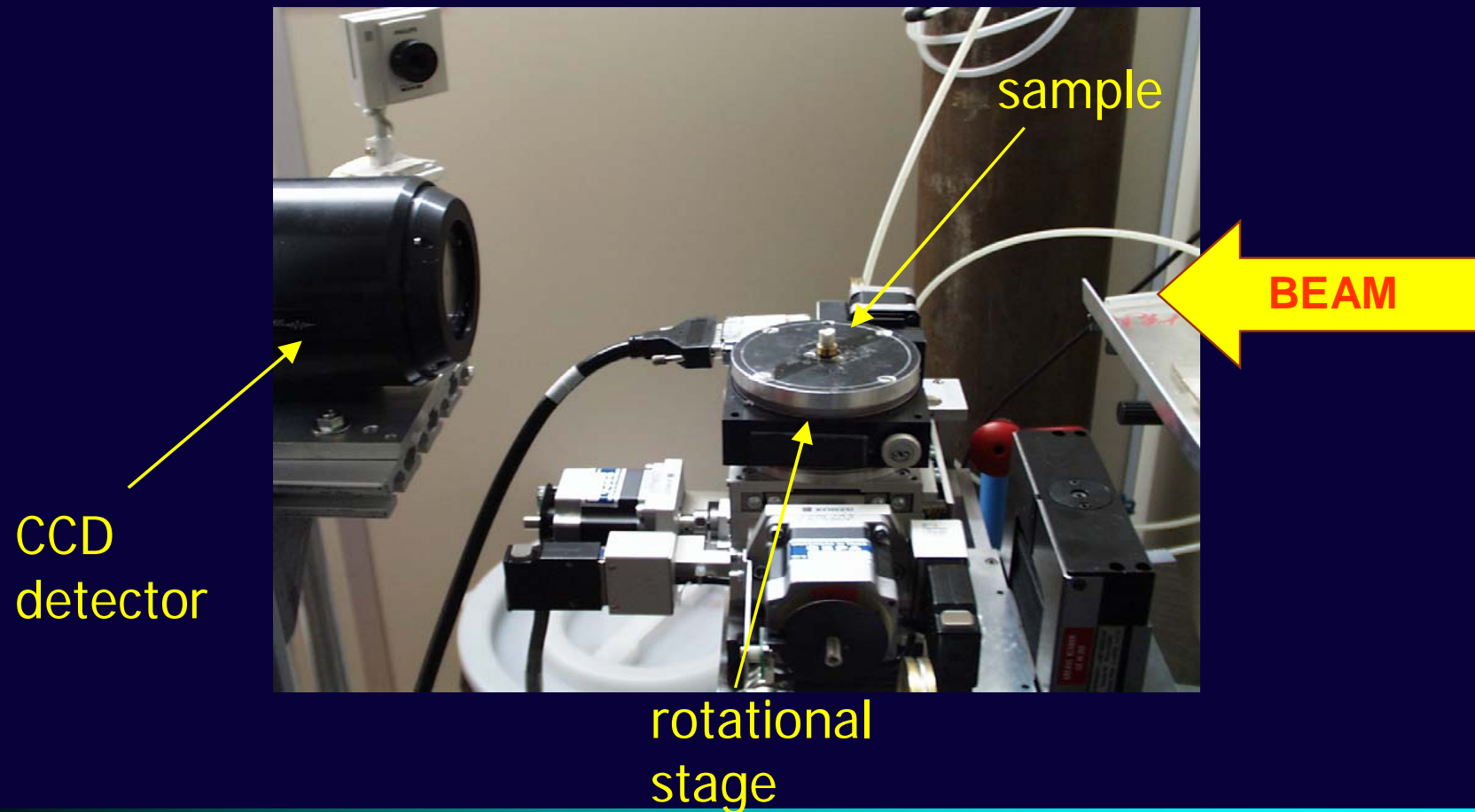
- Parallel beam:
  - an acquisition across 180 degrees provides all necessary information (lower dose – shorter acquisition time)
  - simplified reconstruction algorithms



## The advantages of SR CT – II

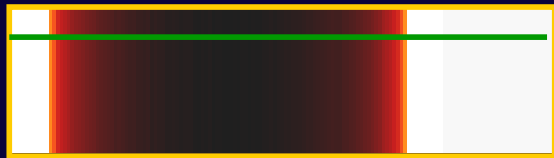
- Monochromatic beam:
  - No beam hardening artifacts
  - Possibility of reconstructing true attenuation coefficients → tissue characterization

# MicroCT at the SYRMEP beamline - I



# MicroCT at the SYRMEP beamline - II

- A projection = a  $2048 * 300$  matrix
- A height  $h$  is chosen
- A line at height  $h$  is extracted from each projection and a sinogram is formed



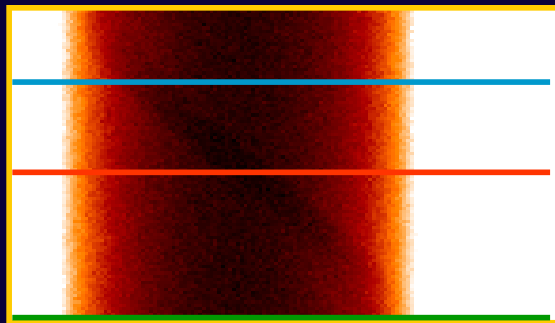
0 degrees



90 degrees

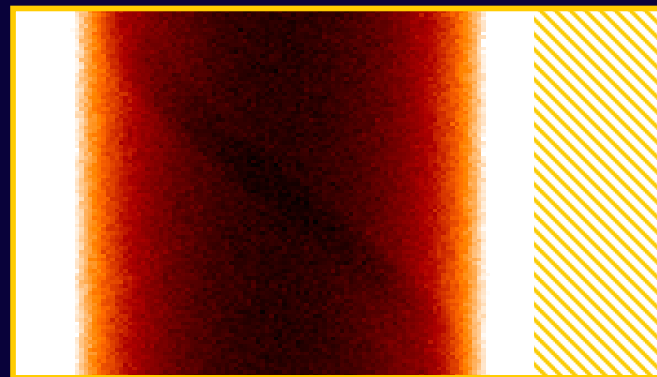


140 degrees



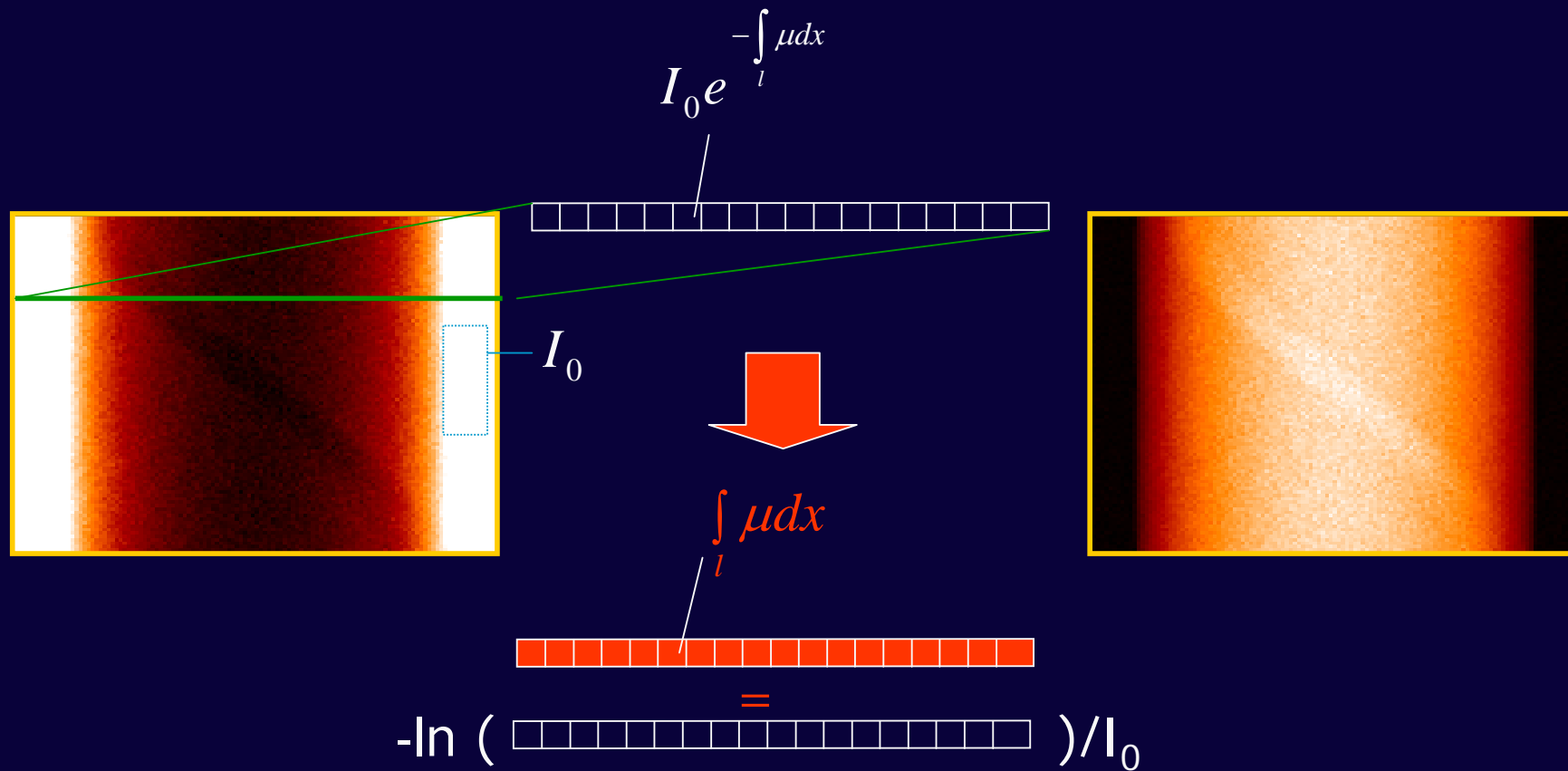
## MicroCT at the SYRMEP beamline - III

- The sinogram is trimmed in order to have the center of rotation coincident to the center of the matrix



# MicroCT at the SYRMEP beamline - IV

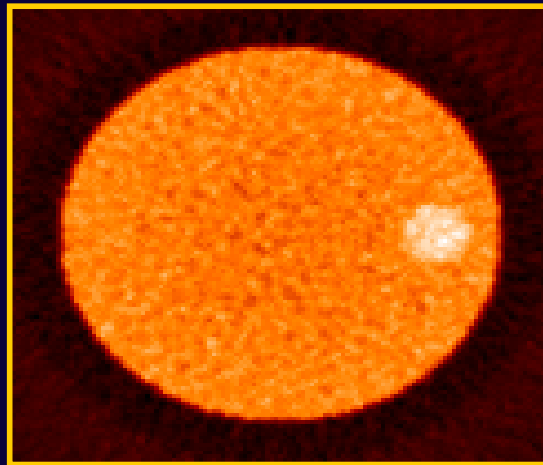
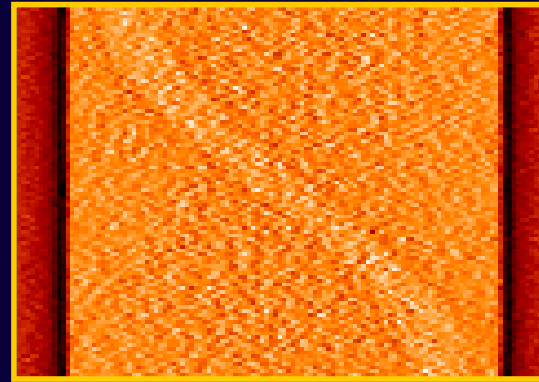
- The sinogram is transformed in order to obtain line integrals of the attenuation coefficients





# MicroCT reconstructions at the SYRMEP beamline - V

- Each line of the logarithmic sinogram is filtered



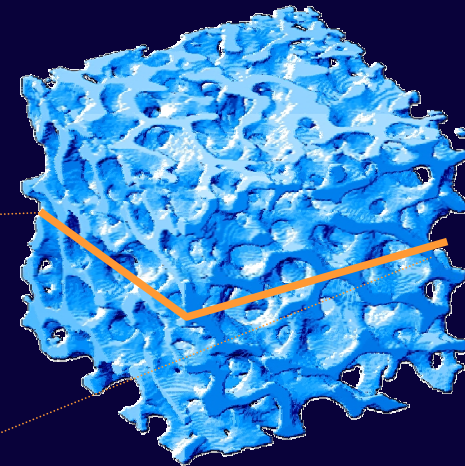
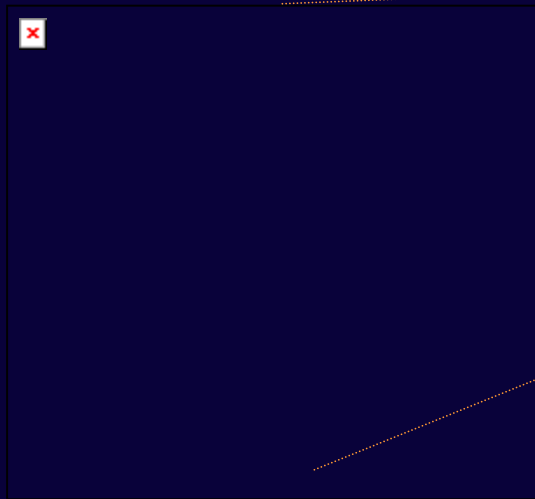
- The final image is obtained by means of a backprojection



Volume rendering

# Volume rendering

- 2-d images are stacked
- The 3-d structure of the object is visualized



# A possible application: sintered replicas of biological samples

- Why?
  - Tool for enhanced visualization
  - Used in mechanical tests to assess the bone architecture load bearing capabilities
    - Tests on biological samples cannot be repeated!
- How?
  - Built by rapid prototyping in a relatively homogeneous and well characterized material



## Selected laser sintering

- The object is defined by means of a CAD file
- Layer Manufacturing Technology (LMT)
- Parts are manufacturing layer by layer from polyamide powder with a CO<sub>2</sub> laser
- Complex structures, such as the trabecular architecture, can be built