

SCHOOL ON SYNCHROTRON RADIATION AND APPLICATIONS
In memory of J.C. Fuggle & L. Fonda

19 April - 21 May 2004

Miramare - Trieste, Italy

1561/17

**Photoemission from Valence Bands, Dispersion and Fermi
Surface Mapping**

Juerg Osterwalder

Photoemission from Valence Bands, Dispersion and Fermi Surface Mapping

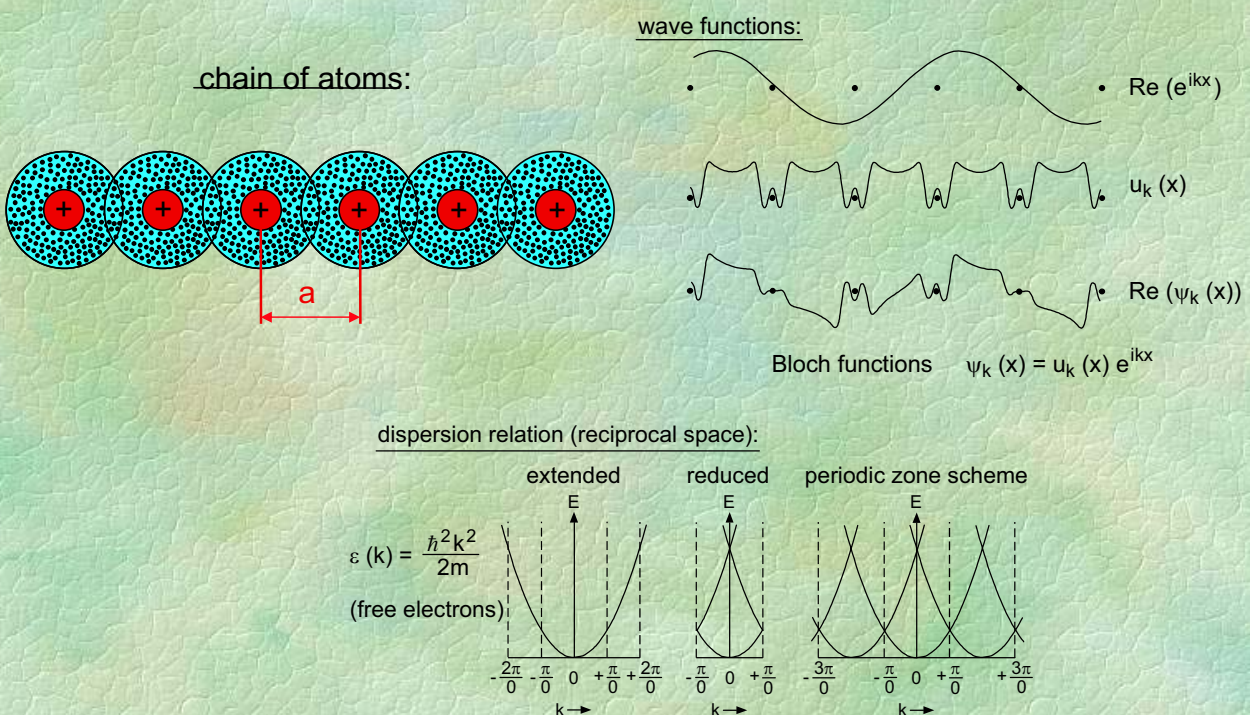
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CH-8057 Zürich, Switzerland - osterwal@physik.unizh.ch
<http://www.physik.unizh.ch/groups/grouposterwalder/>

Lecture 1

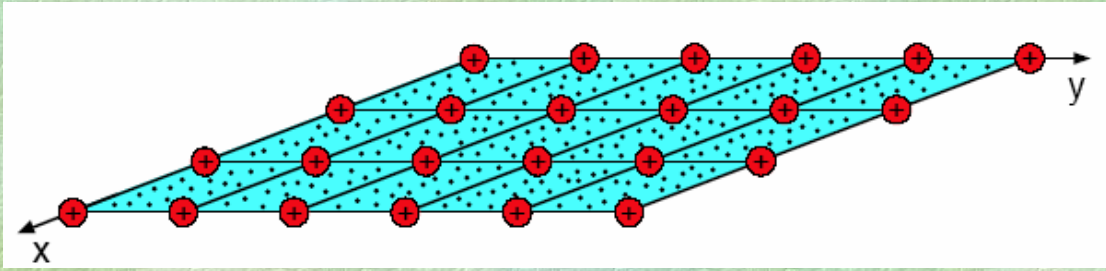
- Electronic Band Structure in 1-3 Dimensions
- Photoemission from a Periodic Potential
- The 3-Step Model
- A 1D Example: p(2x1) O-Cu(110) -> Band Mapping
- A 2D Example: The Shockley Surface State on Cu(111)
- A Few Words about Surface States in General
- Surface States on Stepped Surfaces:
A Playground for Quantum Mechanics

Electronic Bandstructure in 1 Dimension

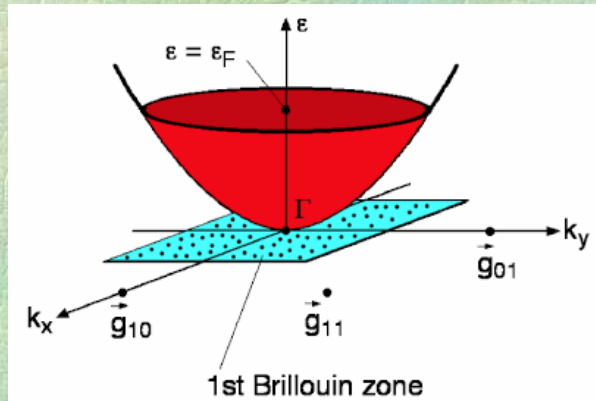


Electronic Structure in 2 Dimensions

(Plane of atoms)

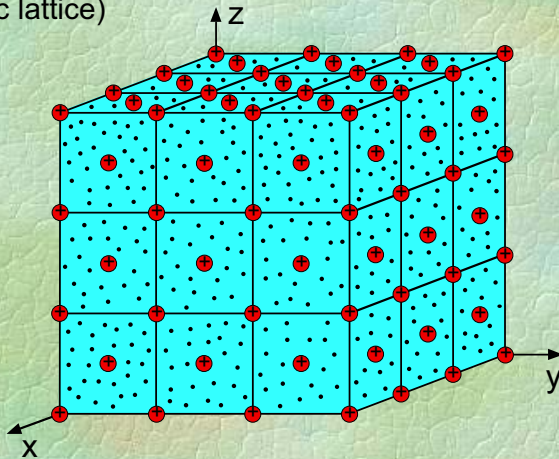


dispersion relation

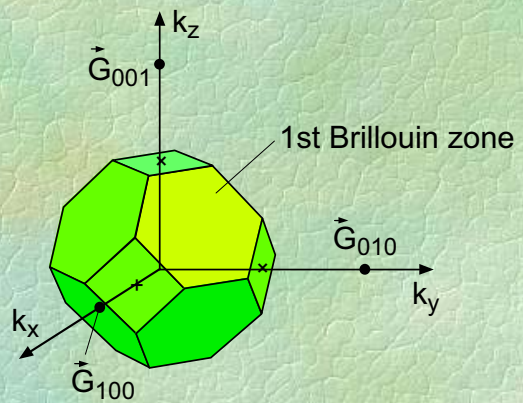


Electronic Structure in 3 Dimensions

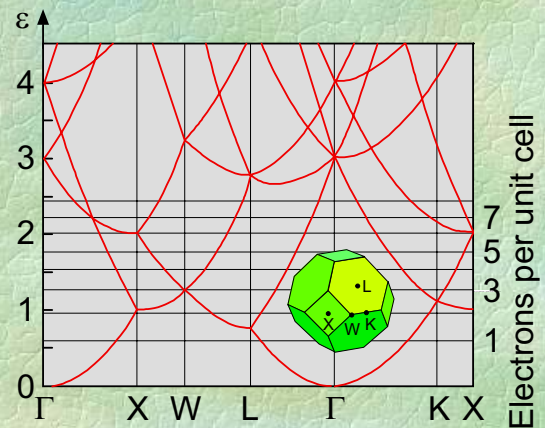
real space:
(face-centered
cubic lattice)



reciprocal space:



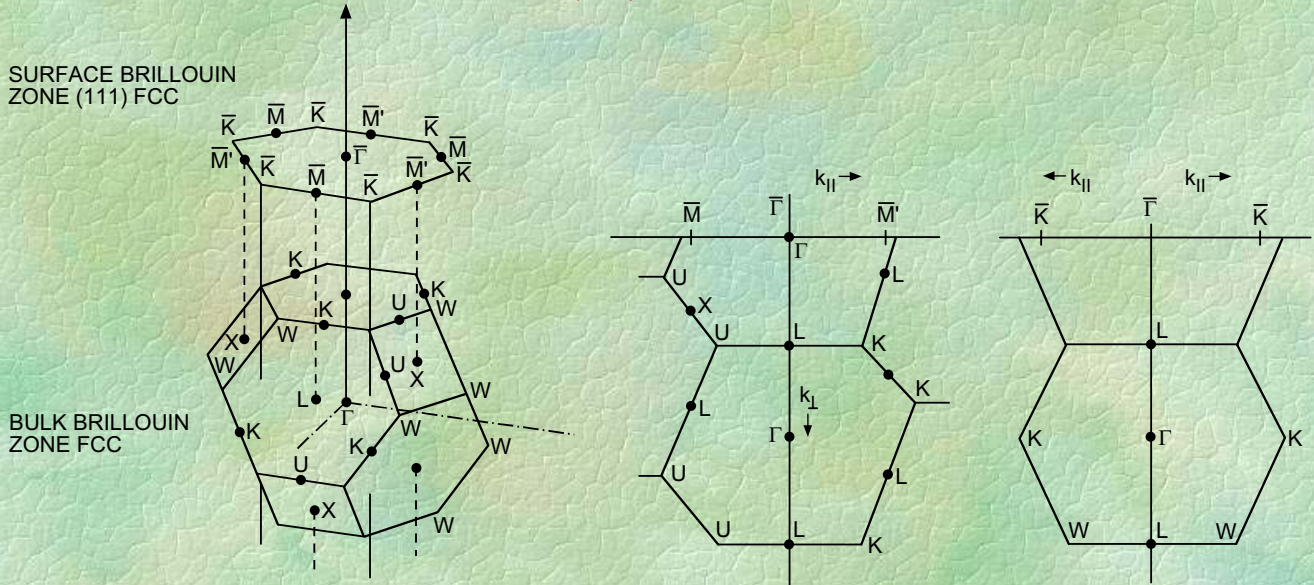
dispersion relation:



The Geography of Reciprocal Space

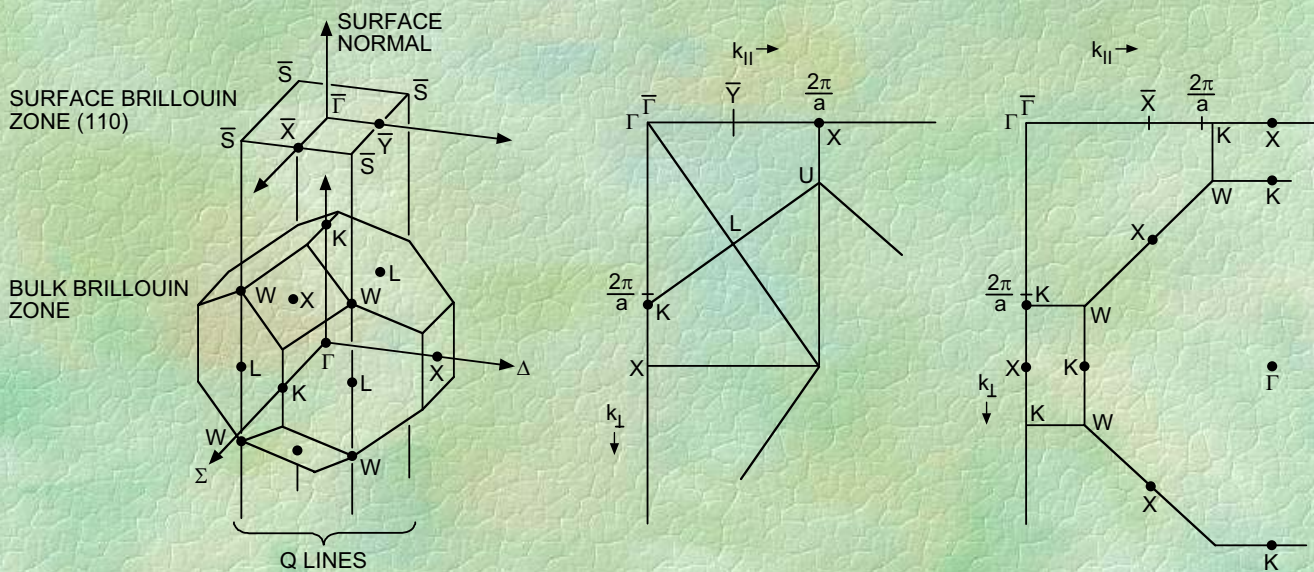
Surface and Bulk Brillouin Zones for face-centered cubic (fcc) Lattices

(111) Surface



Surface and Bulk Brillouin Zones for face-centered cubic (fcc) Lattices

(110) Surface

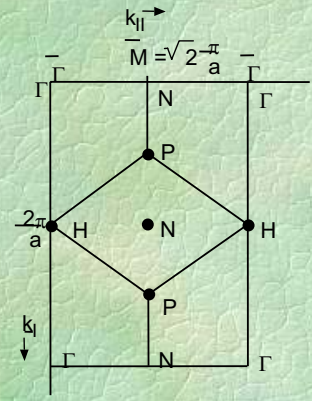
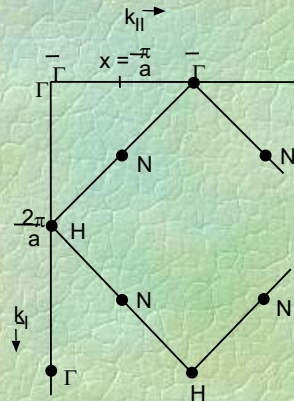
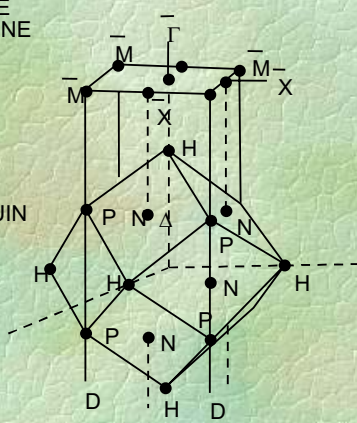


Surface and Bulk Brillouin Zones for body-centered cubic (bcc) Lattices

(001) Surface

(001) SURFACE BRILLOUIN ZONE

BULK BRILLOUIN ZONE



From E. W. Plummer, W. Eberhardt
Adv. Chem. Phys. 49, 533 (1982)

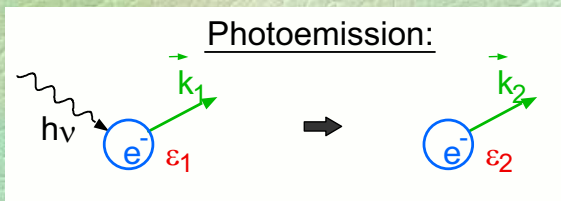
Photoemission of a free electron

	Energy	Momentum
free electron	$\epsilon(\vec{k}) = \frac{\hbar^2 k^2}{2m}$	$\hbar \vec{k}$
photon ($h\nu$)	$\epsilon(\vec{k}) = \hbar \vec{k} c$	$\hbar \vec{k}$

wave numbers k

$$e^- : k = 0.51 \sqrt{\epsilon [\text{eV}]} \text{ \AA}^{-1}$$

$$h\nu : k = 0.51 \cdot \epsilon [\text{eV}] \cdot 10^{-3} \text{ \AA}^{-1}$$



Conservation Laws:

$$\epsilon_1 + h\nu = \epsilon_2$$

$$\vec{k}_1 + \vec{k}_{h\nu} = \vec{k}_2$$

... cannot be simultaneously fulfilled!
 \Rightarrow prozess forbidden

Atoms, Molecules: Recoil
 Solids : Recoil (= reciprocal lattice vector)

Photoemission from a Periodic Potential

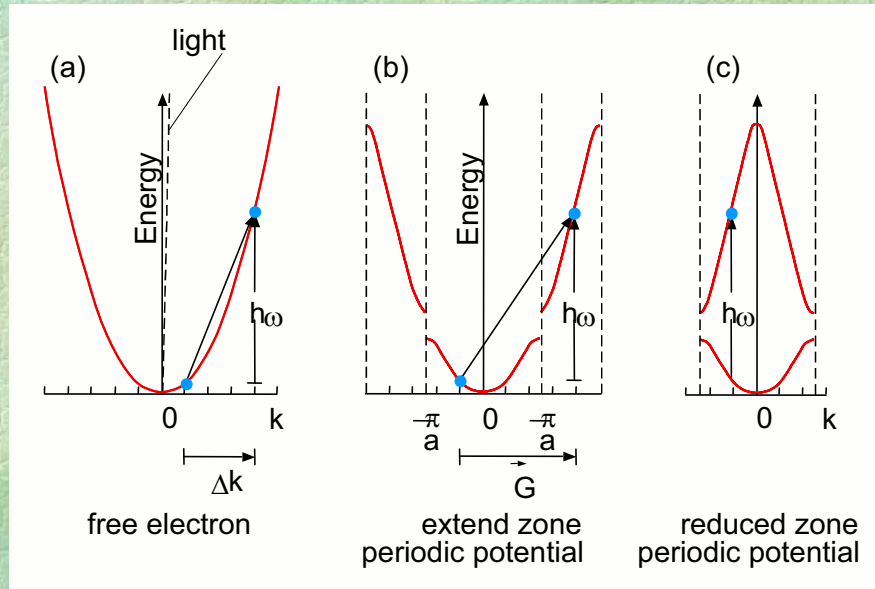
Conservation Laws:

$$\varepsilon_i(\vec{k}_i) + h\nu = \varepsilon_f(\vec{k}_f)$$

$$\vec{k}_i + \vec{k}_{h\nu} + \vec{G} + \vec{g} = \vec{k}_f$$

$$\approx 0$$

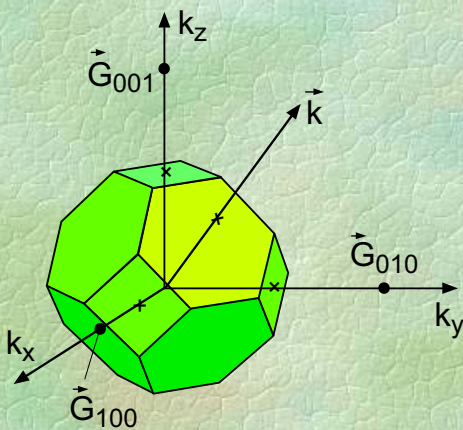
reconstructed surface



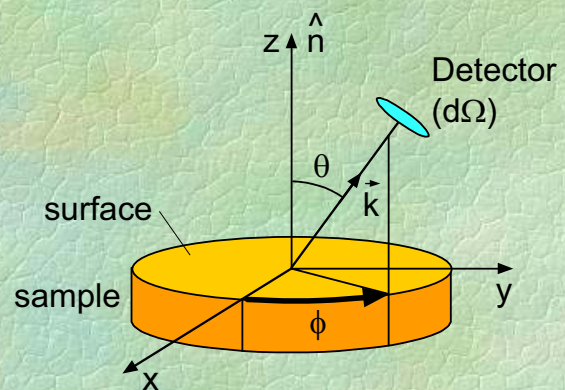
→ Direct Transitions

Measurement of the Photoelectron Momentum

reciprocal space:



real space:



direction: $\hat{k} = \theta, \phi$ (watch for refraction)

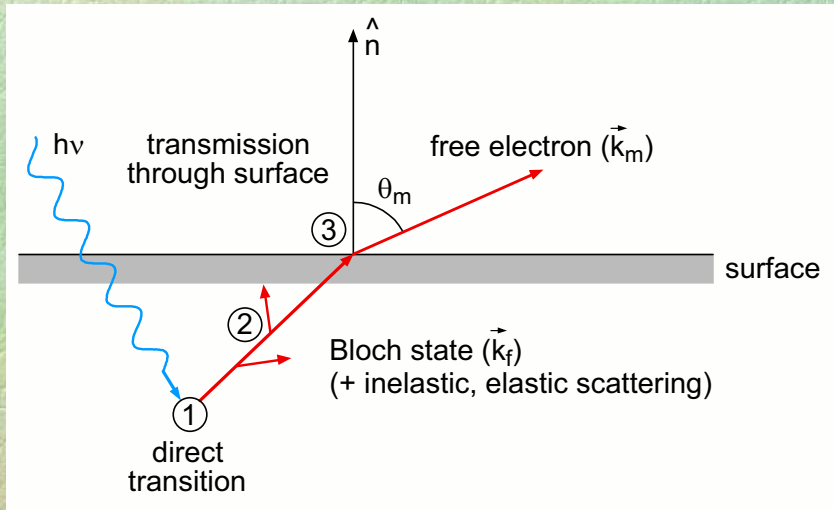
magnitude: from $\varepsilon_f(\vec{k})$ (ε_f is measured)

Problem: $\varepsilon_f(\vec{k})$ usually not known

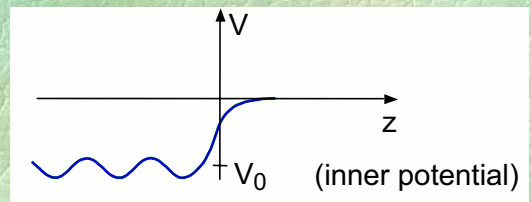
Solution: free electron final state

$$\varepsilon_f(\vec{k}) = \frac{\hbar^2 k^2}{2m}$$

The 3-Step Model



- ① Photoexcitation
- ② Propagation to surface
- ③ surface potential step \rightarrow Refraction

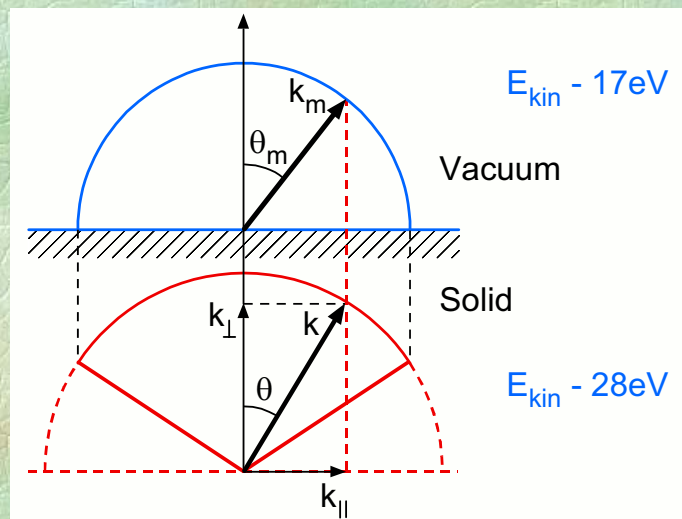


periodicity within surface $\rightarrow \vec{k}_{f\parallel} = \vec{k}_{m\parallel}$

surface potential step $\rightarrow \vec{k}_{f\perp} > \vec{k}_{m\perp}$

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Refraction at the Surface Potential Step

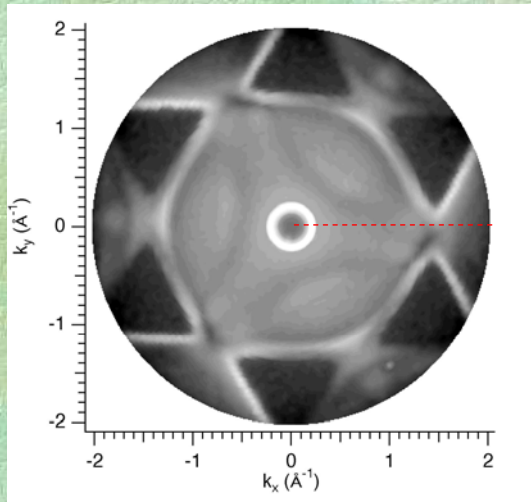
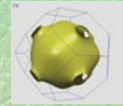


$$\sin \theta = \sin \theta_m \sqrt{\frac{h\nu - \Phi}{h\nu - \Phi + V_0}}$$

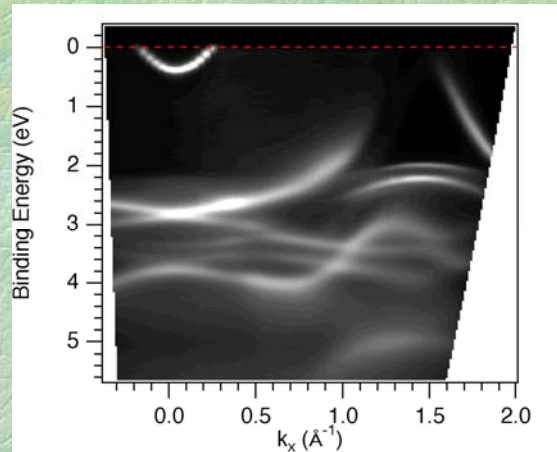
Φ : work function
 V_0 : inner potential

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Angle-Resolved Photoemission from Cu(111)

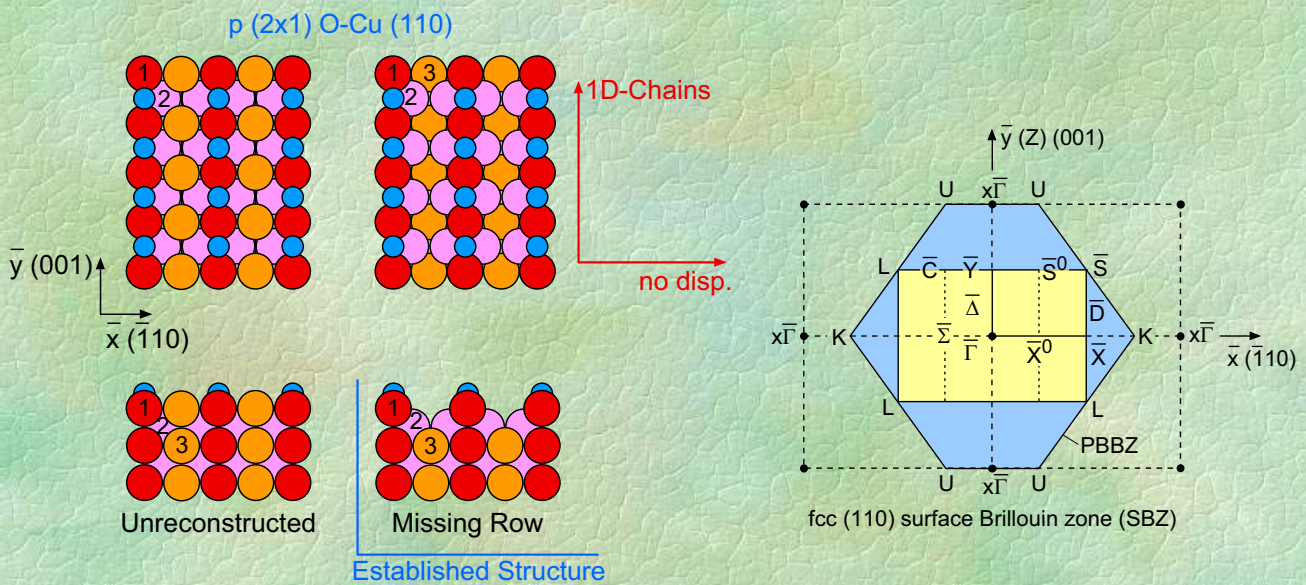


$E_i = E_{fermi}$ scanning of (θ, ϕ) :
Cut through the bulk Fermi surface

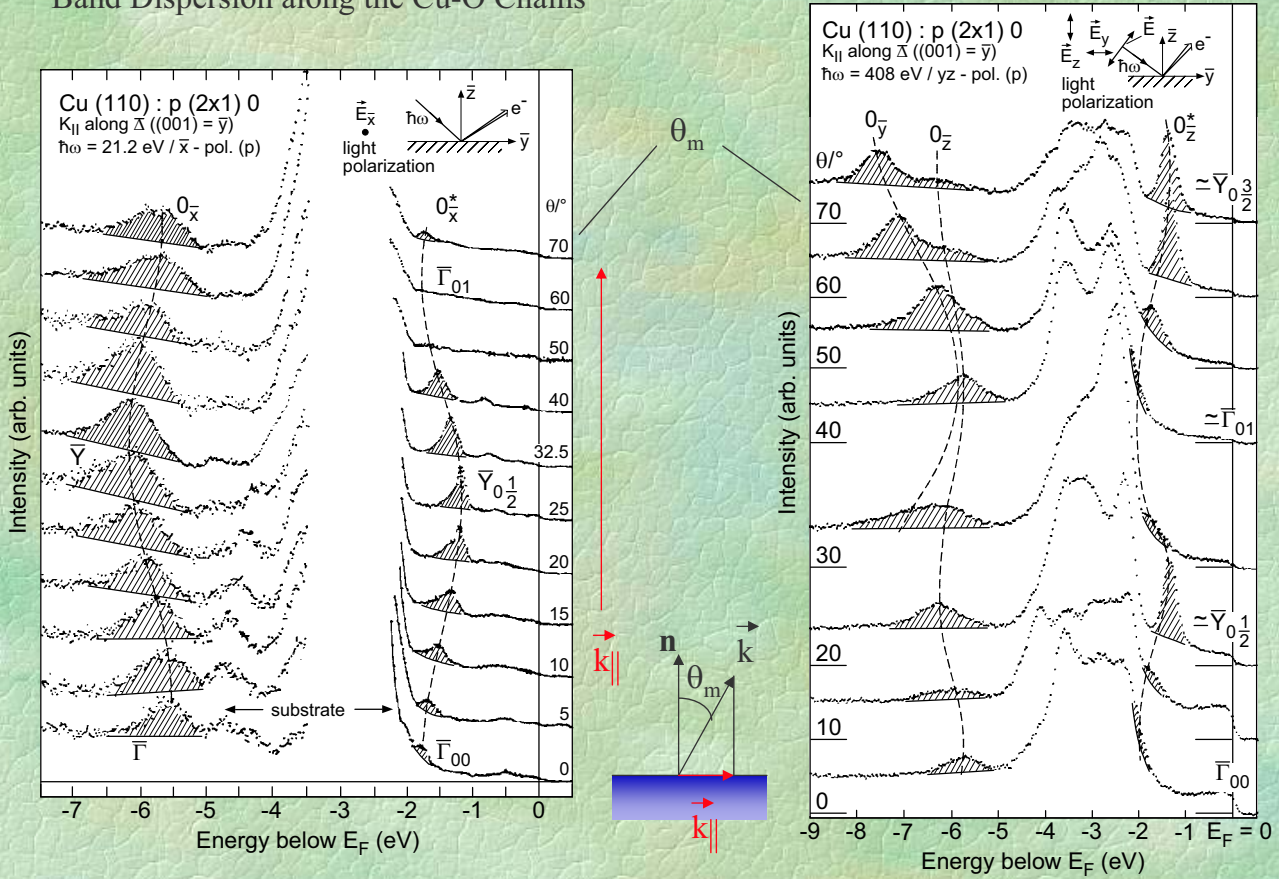


scanning of E_i and θ :
Band structure along curved line in
3D k - space

A One-Dimensional Example:

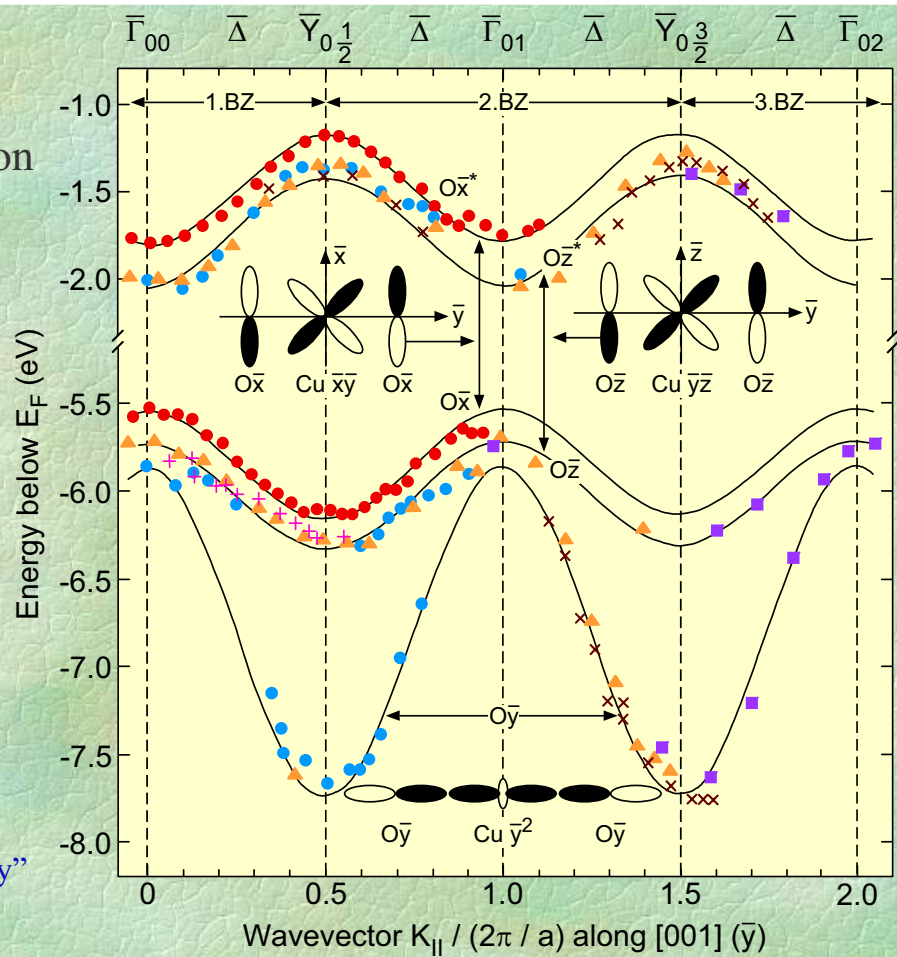


Band Dispersion along the Cu-O Chains

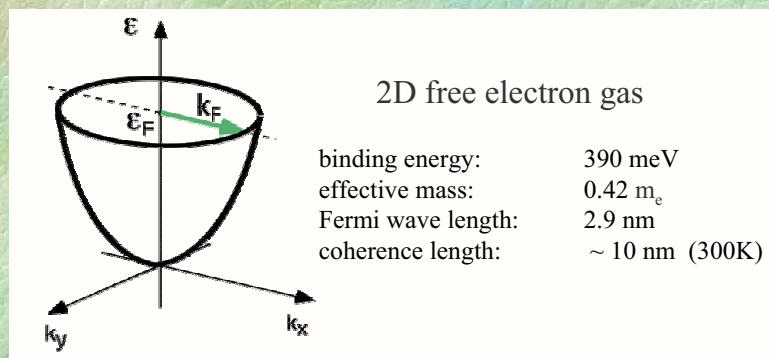
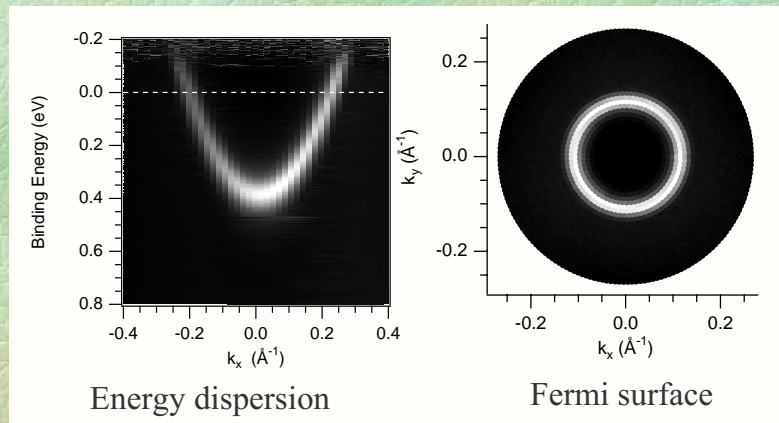


Finding all the States - Interpretation

Often a simple tight binding model works quite well !

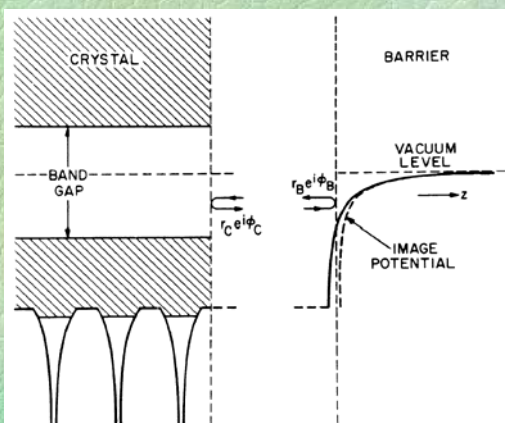


A 2D Example: The Shockley Surface State on Cu(111)

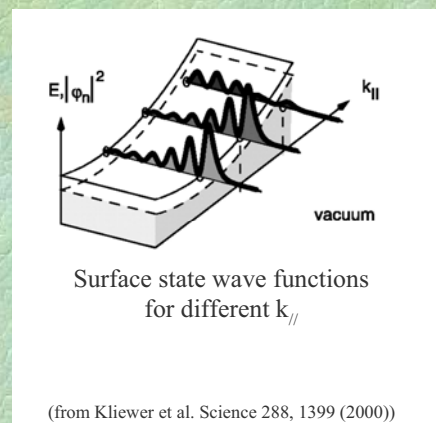


Multiple reflection model for surface states:

(N.V. Smith, PRB 32, 3549 (1985))



N.V. Smith, PRB 32, 3549 (1985)



$$\phi_c + \phi_b = 2\pi n$$

$$\text{Cu(111), } n = 0: E_B = 0.3\text{eV}, m^* = 0.5m_e$$

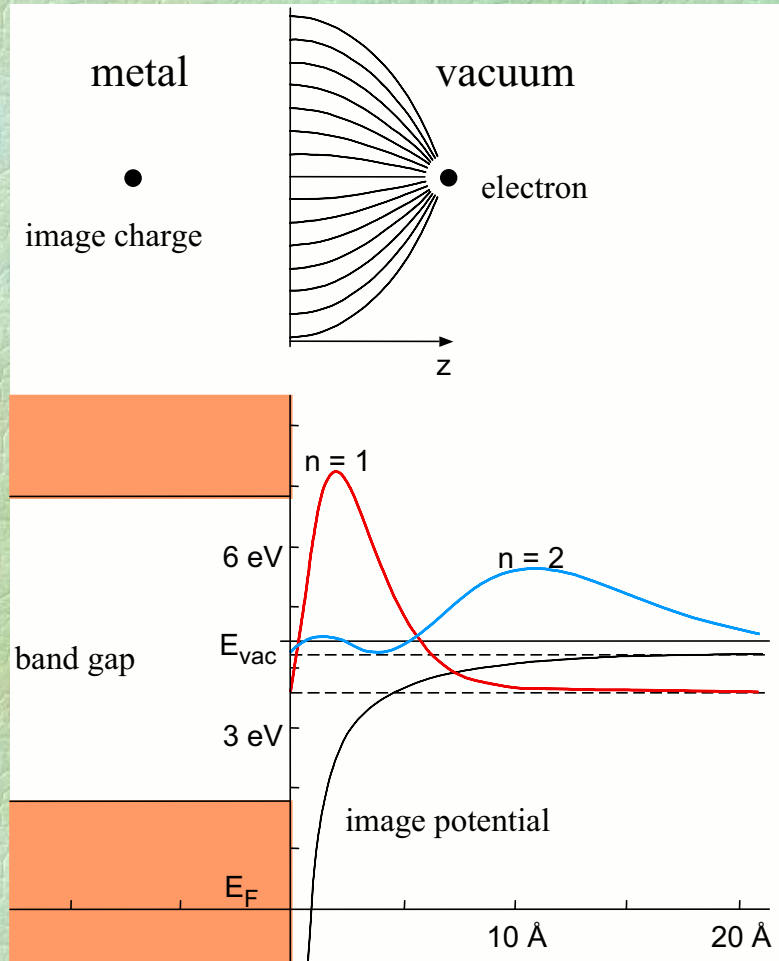
The Long-Range Image Potential Near a Metal Surface

Image Potential States:

$$E_B = 0.85 \text{ eV} / (n+a)^2$$

(hydrogen-like Rydberg Series, with 'quantum defect' accounting for electron reflectivity at the metal surface)

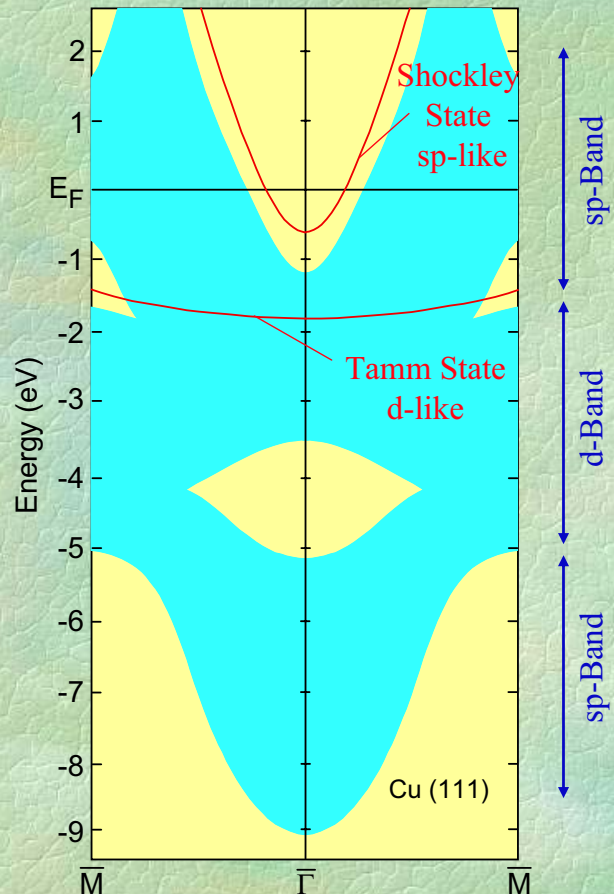
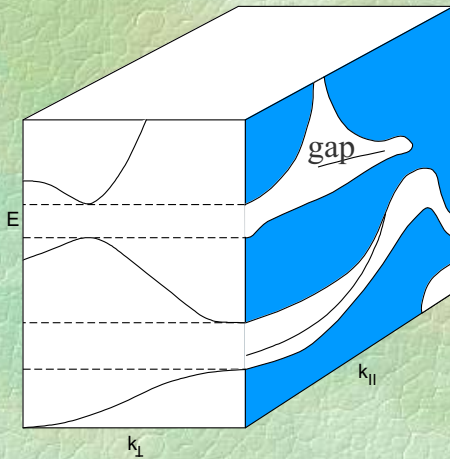
T. Fauster, *Appl. Phys. A* 59, 63 (1994)



Where do surface states live in k space?

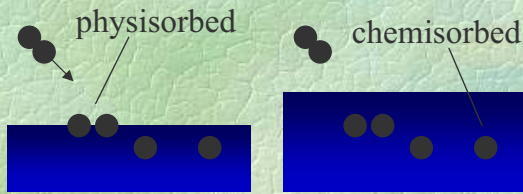
Experimental identification:

- "crud test" (sensitivity to adsorbates)
- no dispersion in k_{perp} (use synchrotron rad.)
- lives in projected band gap



Are Surface States Important at All ?

Dissociative chemisorption:

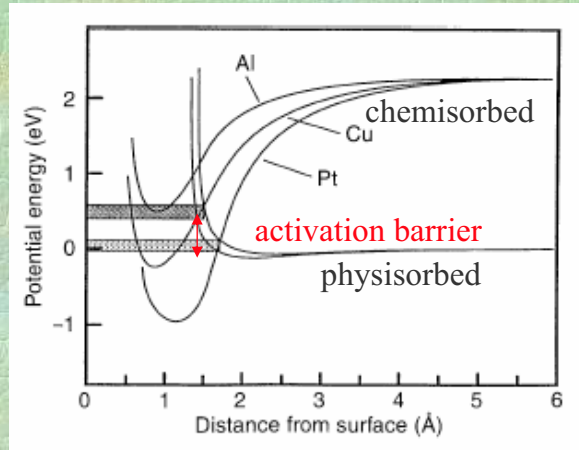


Without S.S.

With S.S.

E. Bertel et al.,

Appl. Phys. A 63, 523 (1996)



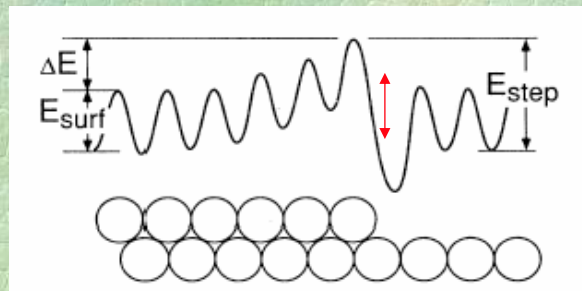
Surface Diffusion:

Schwöbl barrier is reduced by surface state !

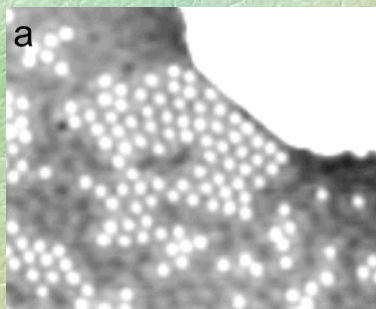
⇒ Adatoms can move across steps.

⇒ Layer-by-layer growth of films

Memmel, Bertel, PRL 75, 485 (1995)



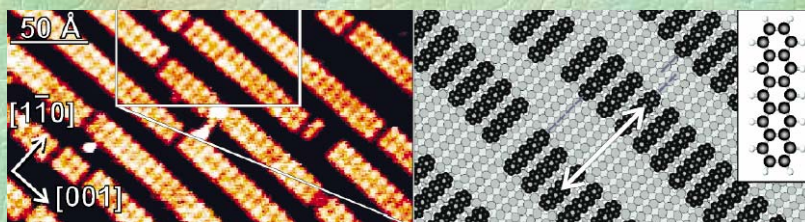
Surface state mediated long range interactions of adatoms and adsorbates



Cu/Cu(111), T=15K:

Oscillatory interaction with $\lambda_r/2=14\text{\AA}$

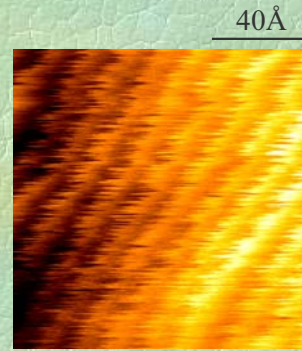
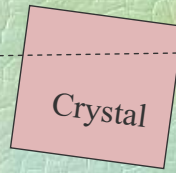
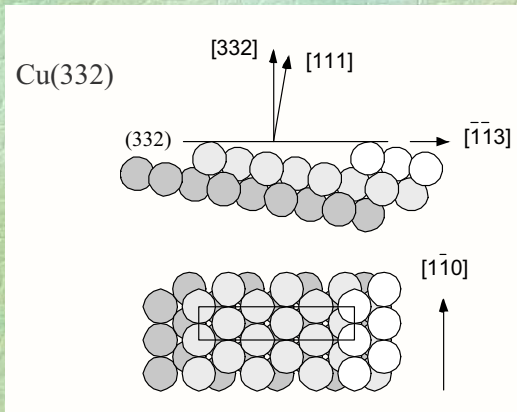
J. Repp et al., PRL 85, 2981 (2000)



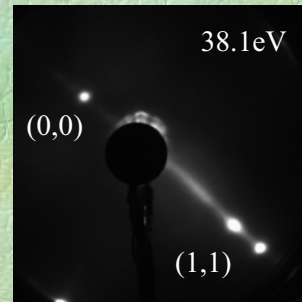
Pentacene, on Cu(110)

S. Lukas et al., PRL 88, 028301 (2002)

Vicinal Cu(111) Surfaces



Scanning tunneling microscopy (STM), Cu(332)

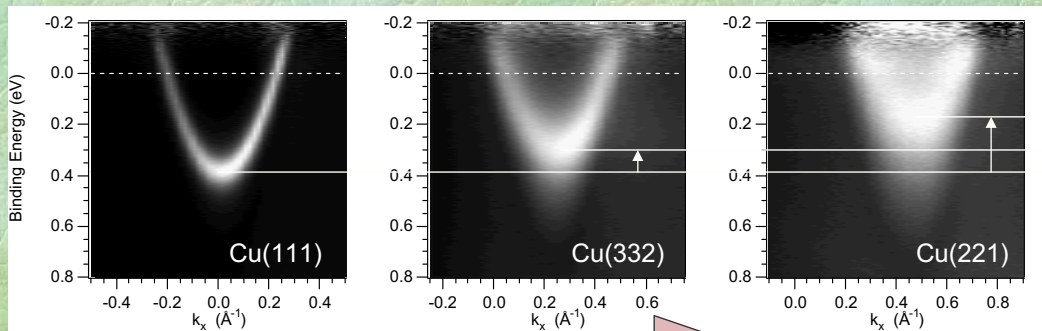


Low energy electron diffraction (LEED), Cu(332)

	Cu(112)	Cu(221)	Cu(332)	Cu(443)
α	19.5°	15.8°	10.0°	7.3°
l	6.24Å	7.66Å	12Å	16.3Å
n	3	4	6	8

Neat way for nanostructuring surfaces !

How does the electron gas react to the steps ?

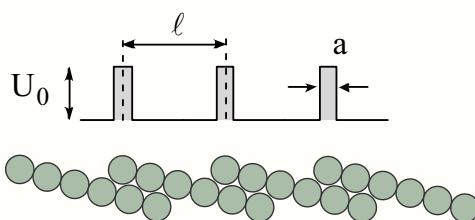


Decreasing terrace width (l)

1D periodic potential:

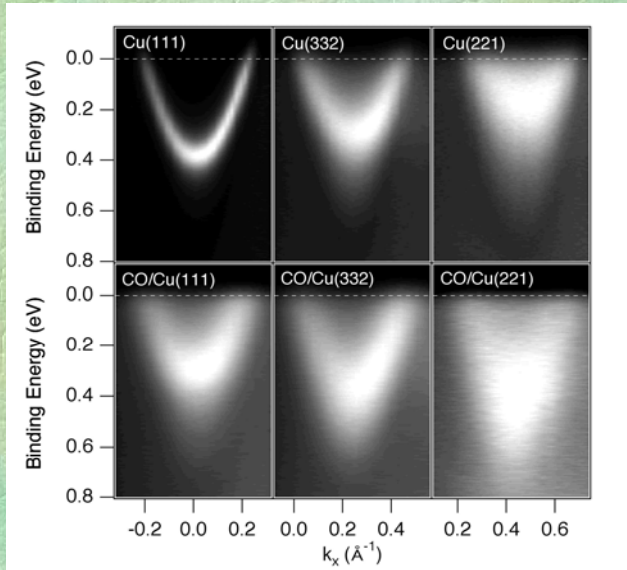
$$\Delta E_B = \frac{U_0 a}{l}$$

$$U_0 a = 1.3 \text{ eVÅ}$$



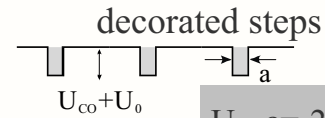
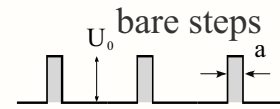
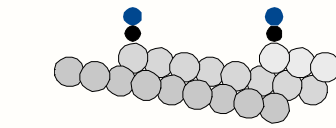
Steps act as potential barriers

Tailoring confining barriers: CO/vicinal Cu(111)



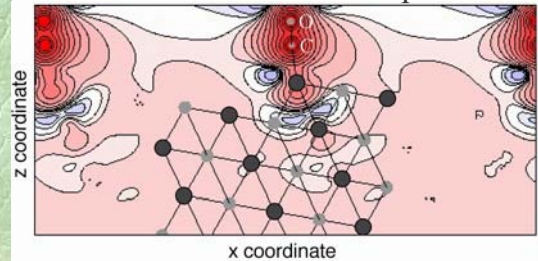
F. Baumberger et al.,
PRL 88, 237601 (2002)

CO molecules decorate steps



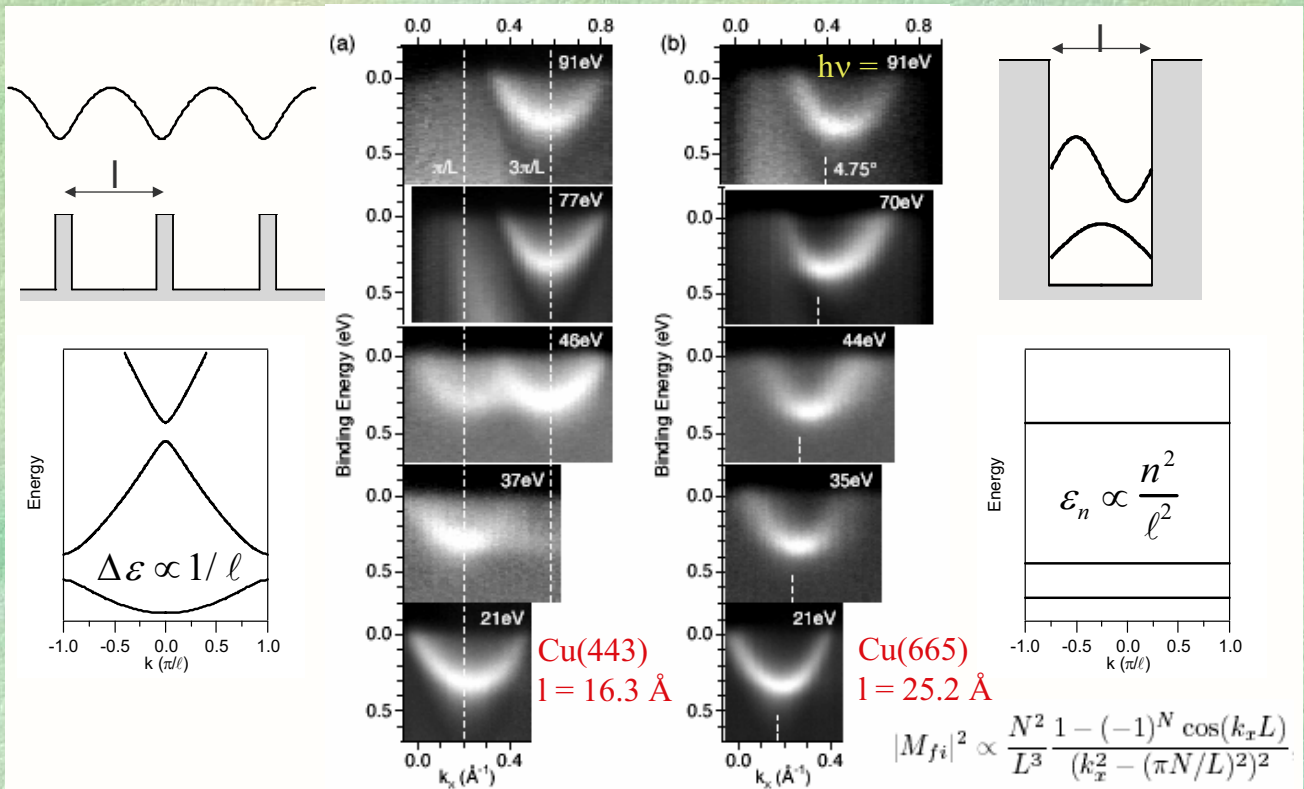
$$U_{CO}a = -2.9\text{eV}\text{\AA}$$

Difference in electrostatic potential



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Periodic potential or decoupled quantum wells?



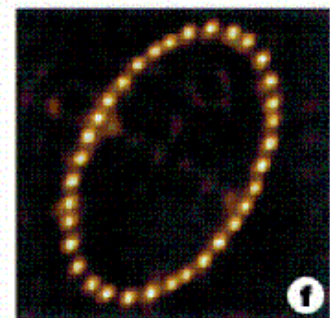
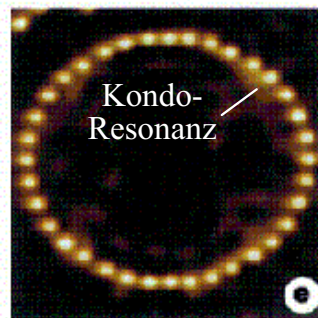
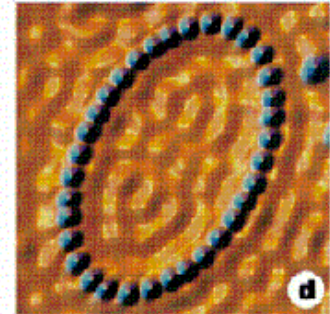
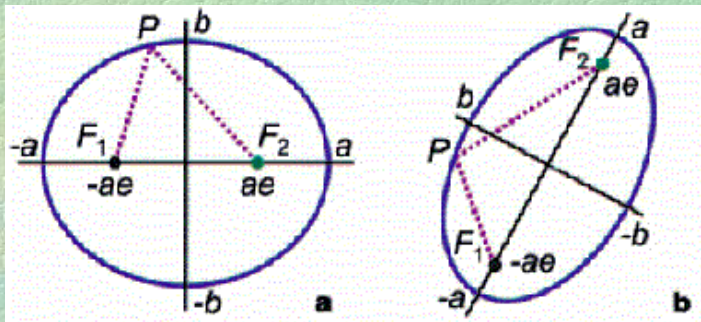
Photon energy (k_{perp}) dependence can unravel the character of the wave functions

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Elliptical
"Quantum Corrals"
Prepared and Imaged
by a 4K STM

H. C. Manoharan, C. P. Lutz,
D. M. Eigler,
Nature 403 (2000) 512

Valence Bands - Lecture 1



Photoemission from Valence Bands, Dispersion and Fermi Surface Mapping

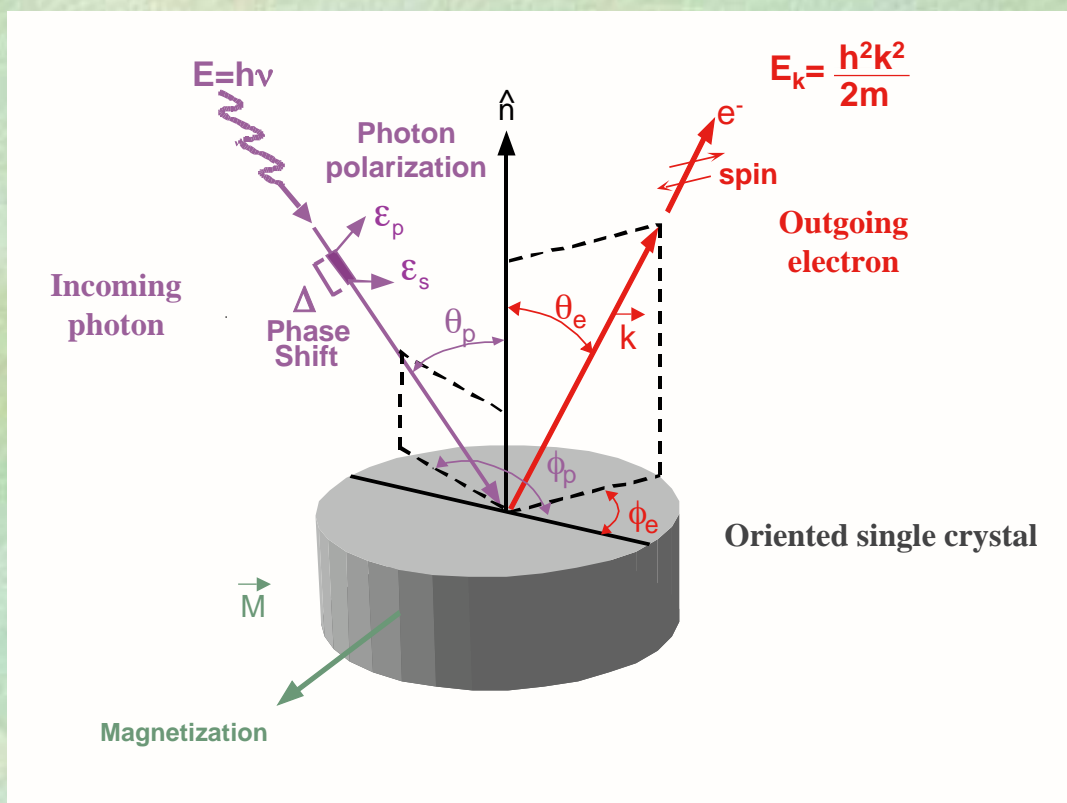
Jürg Osterwalder

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CH-8057 Zürich, Switzerland - osterwal@physik.unizh.ch
<http://www.physik.unizh.ch/groups/grouposterwalder/>

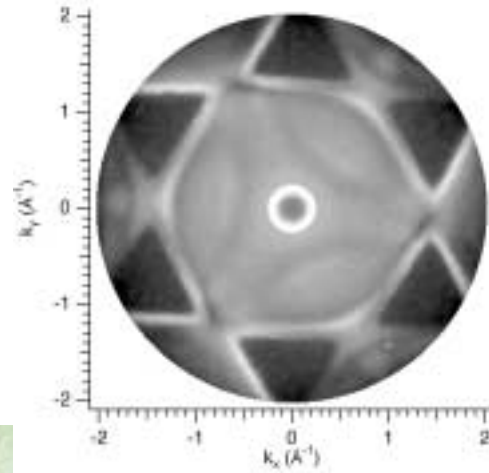
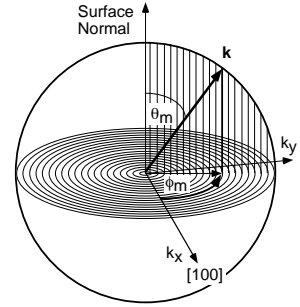
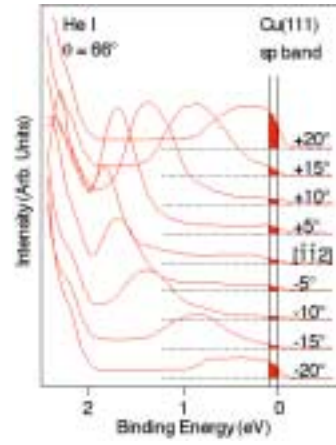
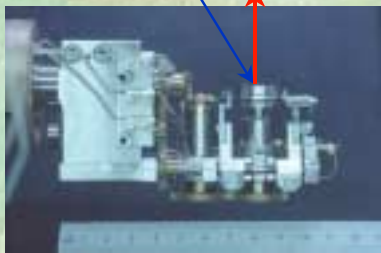
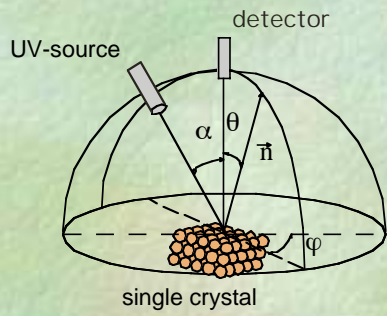
Lecture 2

- Constant Energy Mapping in 3D Systems
- A Few Words about the Fermi Surface in General
- 3D Examples for Fermi Surface Mapping: Cu, Al
- The Fermi Surface of Ni: Case of an Itinerant Ferromagnet
- The Magnetic Phase Transition in Ni: More Details

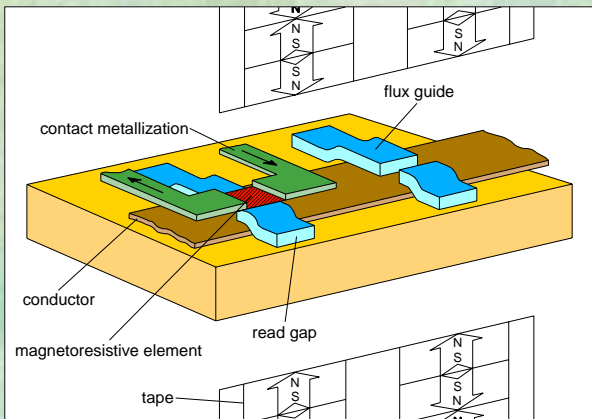
The photoemission experiment



Fermi Surface Mapping by Photoemission



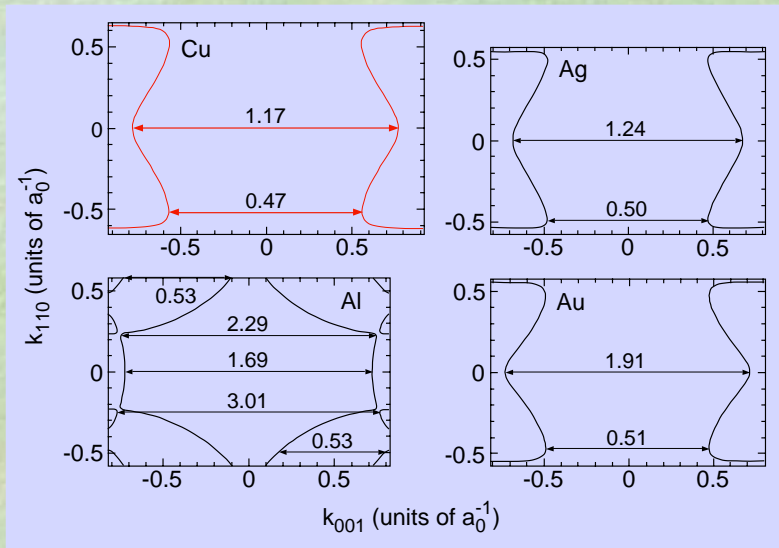
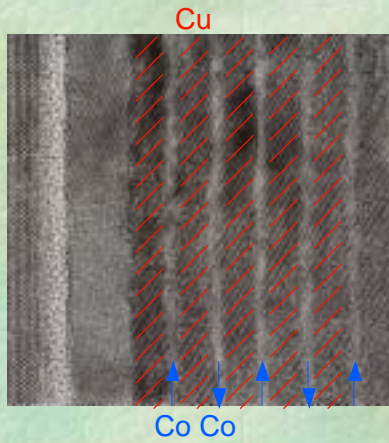
Magnetic Read Heads Based on Giant Magneto-Resistance in Magnetic Multilayers



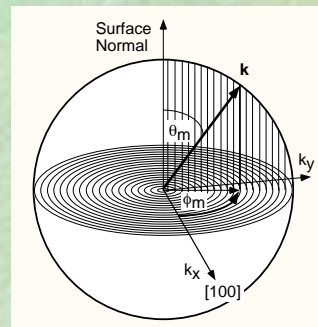
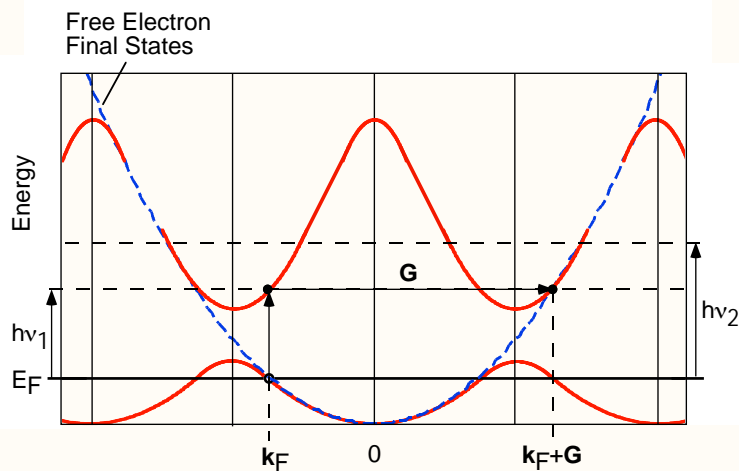
Exchange coupling in magnetic heterostructures

M. D. Stiles

National Institute of Standards and Technology, Gaithersburg, Maryland 20899
(Received 3 May 1993)



Direct Transitions from the Fermi Surface



$$E_{kin}^m = h\nu - \Phi - E_B$$

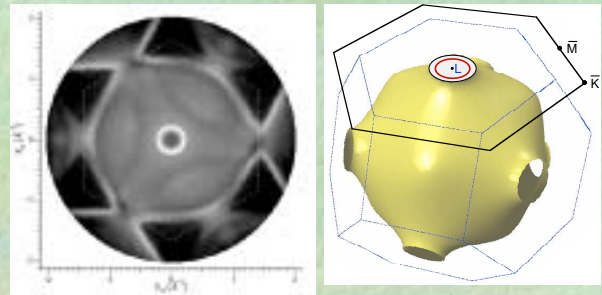
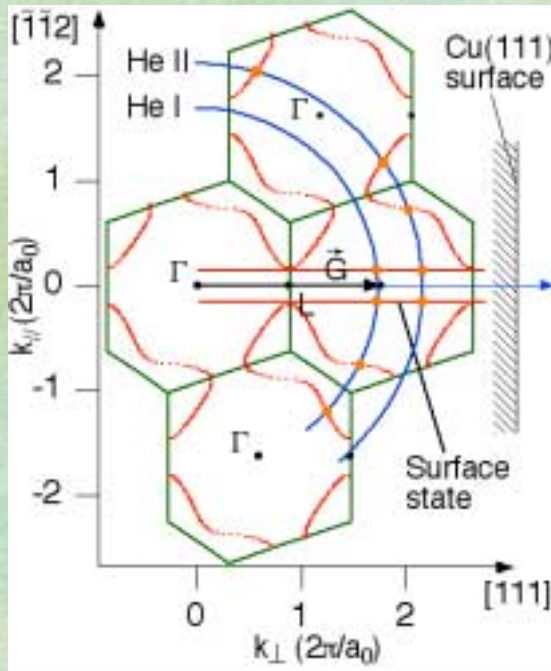
$$|\vec{k}_{||}| = \frac{1}{\hbar} \sqrt{2mE_{kin}^m} \sin \theta_m$$

$$k_{\perp} = \frac{1}{\hbar} \sqrt{2m(E_{kin}^m + V_0)} \cos \theta_m$$

Refraction: $\sin \theta = \sin \theta_m \sqrt{\frac{E_{kin}^m}{(E_{kin}^m + V_0)}}$

Fermi surface mapping

Section along (110) plane in reciprocal space



In the photoemission process:

Energy conservation:

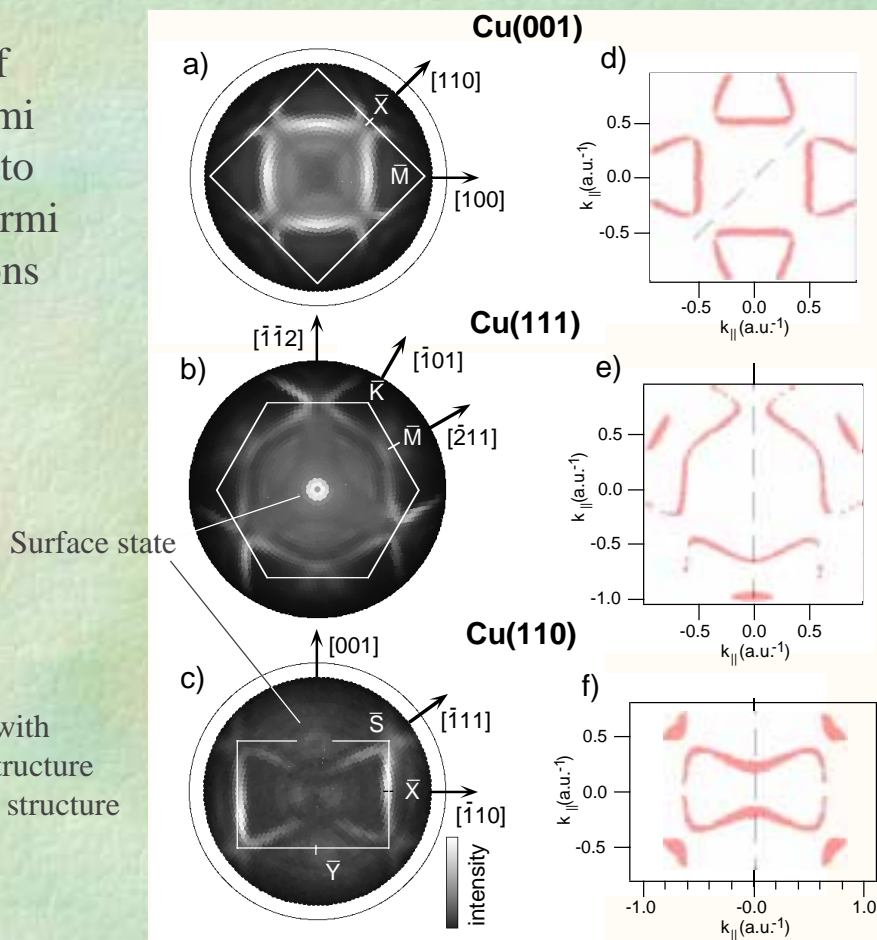
$$E_f = E_i + h\nu$$

Momentum conservation:

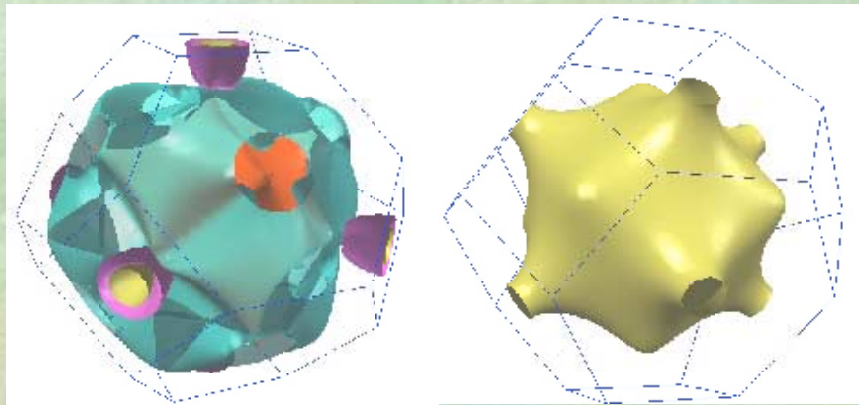
$$\vec{k}_f = \vec{k}_i + \vec{G}$$

Comparison of Measured Fermi Surface Maps to Calculated Fermi Surface Sections

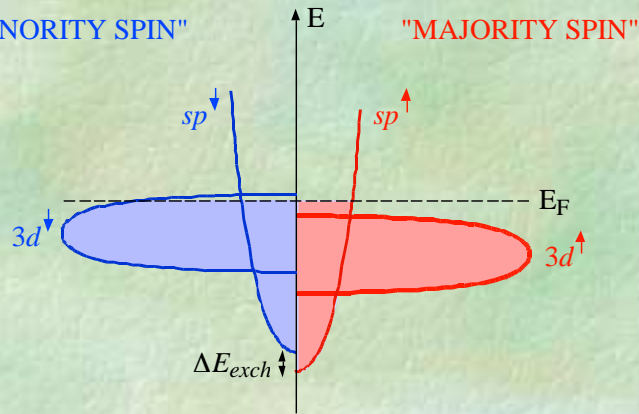
Calculations done with the Wien2k band structure code, assuming the structure of bulk Cu.



The Two Fermi Surfaces of Nickel Metal



Schematic
Density of States

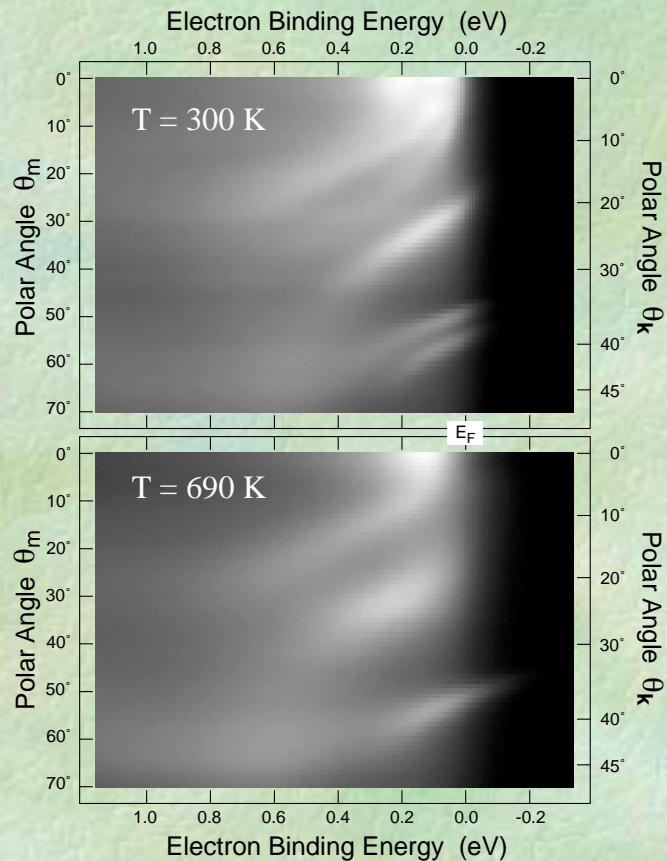


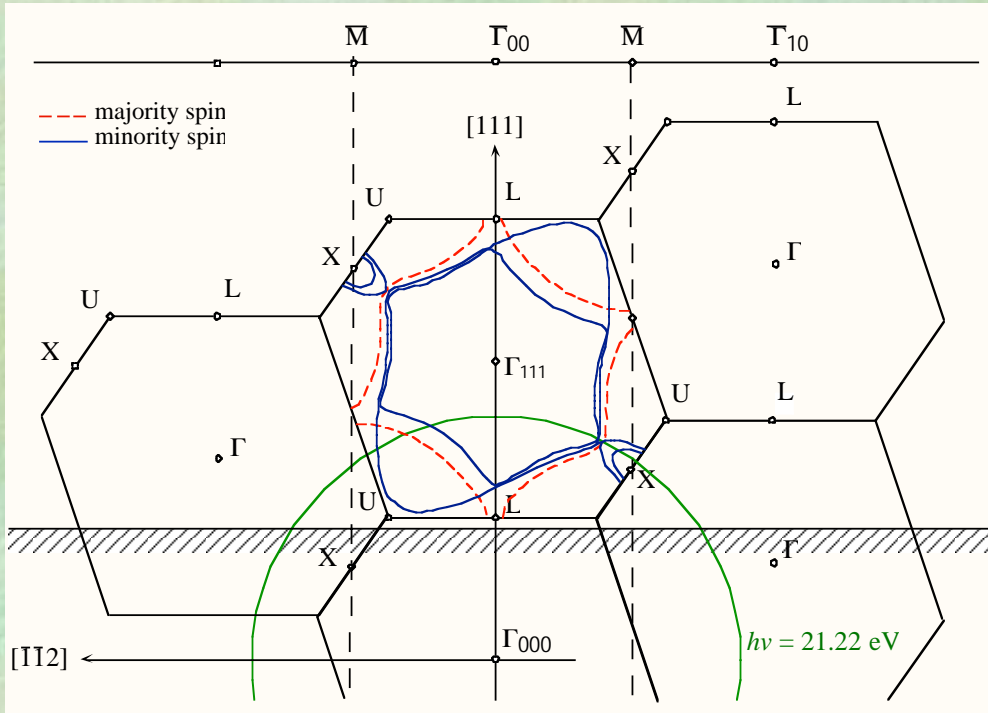
Monitoring the Magnetic Phase Transition

$$T_c = 631 \text{ K}$$

Question:
How does the band structure
change when nickel goes
from the ferromagnetic to
the paramagnetic state ?

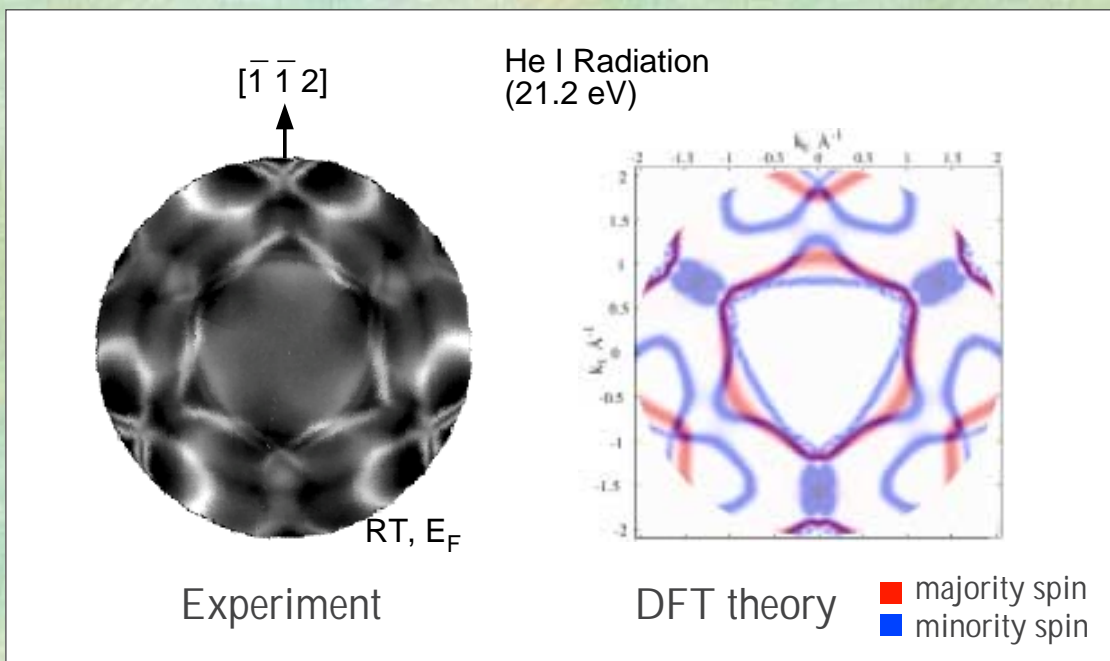
Answer:
Magnetic exchange
splittings disappear



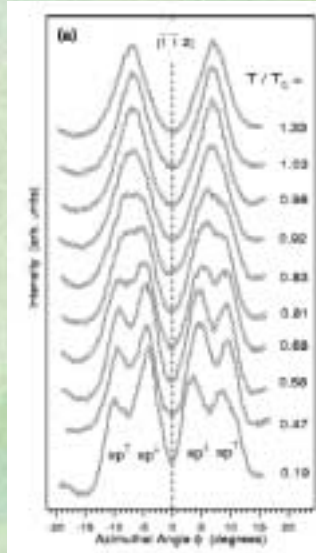
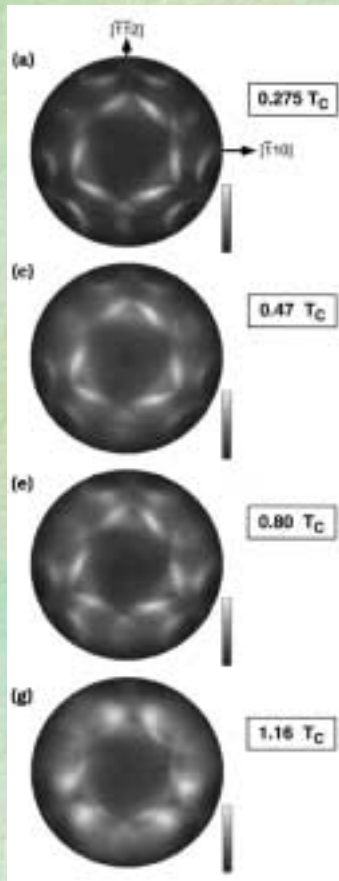


Fermi surface calculation (density functional theory, Wien 97)

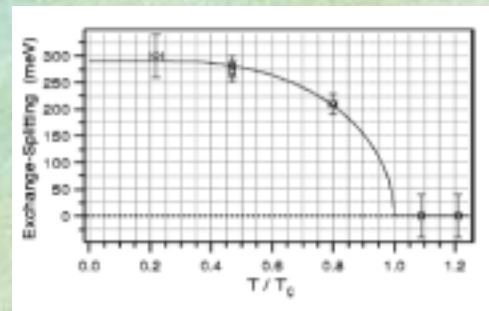
FermiSurface of Ni as Seen Through the Ni(111) Surface



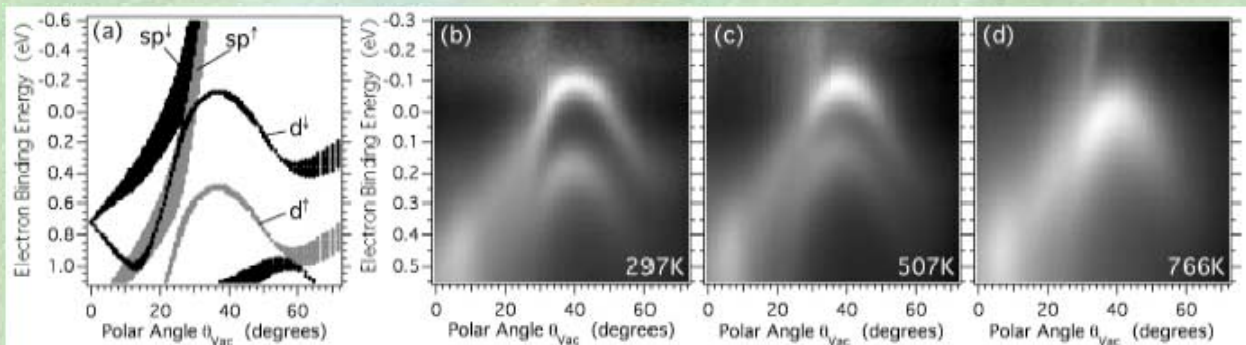
Evolution of the Fermi Surface During the Phase Transition



... and quantifying the exchange splitting:

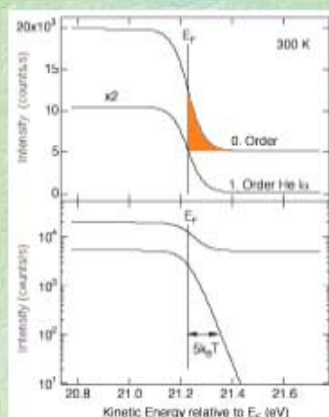


Observing the Magnetic Exchange Splitting in the d Band

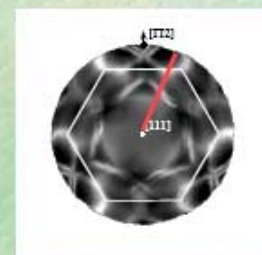


Photoemission above the Fermi Level ?

T. Greber et al., PRL 79, 4465 (1997)

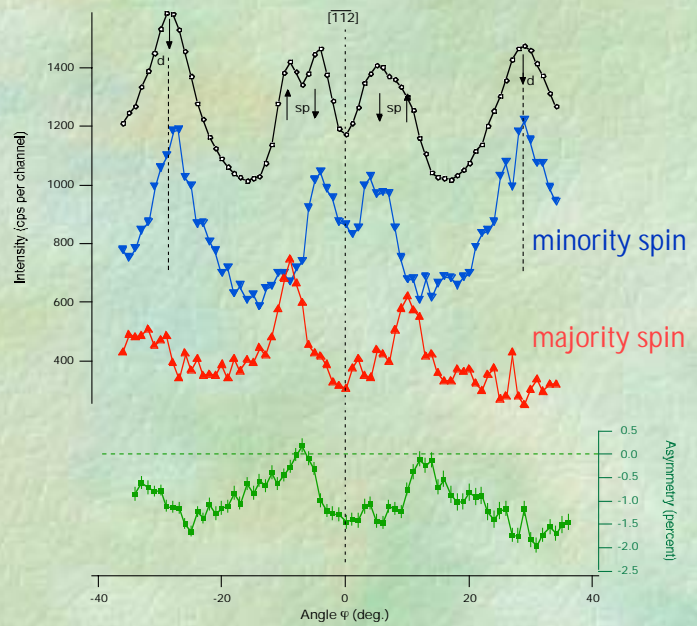
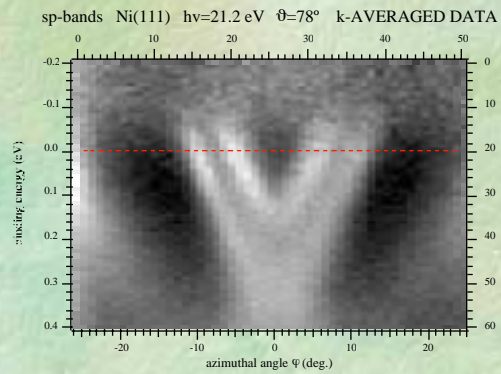
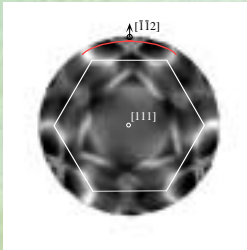


Polar Scan



Spin-Resolved Fermi Surface Mapping

Azimuthal Scan



... a new, spin-resolved spectrometer

Photoemission from Valence Bands, Dispersion and Fermi Surface Mapping

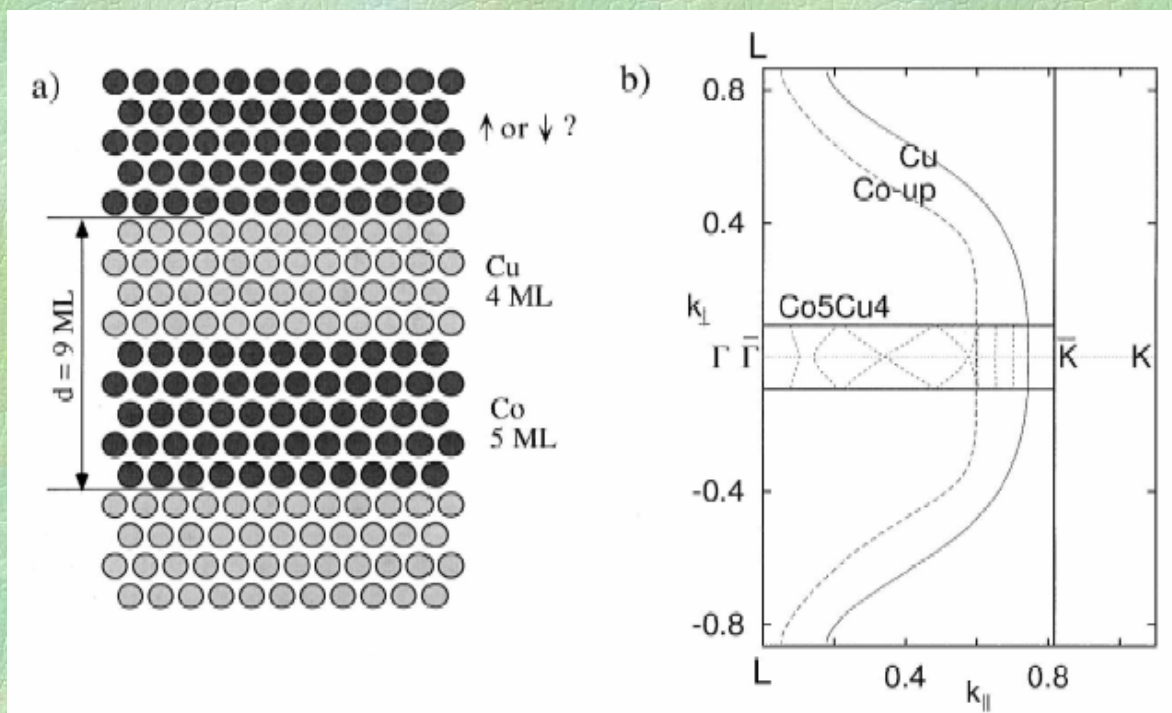
Jürg Osterwalder

Physik-Institut, Universität Zürich, Winterthurerstr. 190,
CH-8057 Zürich, Switzerland - osterwal@physik.unizh.ch
<http://www.physik.unizh.ch/groups/grouposterwalder/>

Lecture 3

- Fermi Surface Mapping with Spin Resolution: Design of a New Spectrometer
- Spin-Resolved Fermi Surface Contours in Nickel
- Spin-Orbit-Split Surface State on Au(111)
- Ultrathin Films of Ni on Cu(001)
- Intensities in Valence Photoemission: Polarization Effects
- Intensities in Valence Photoemission: Atomic Effects
- Intensities in Valence Photoemission: Diffraction Effects

Magnetic Bandstructure in Multilayered Films



Band folding along k_{perp} leads to a multitude of bands!

Spin-Resolved Fermi Surface Mapping

Problem:

Sample rotation over $2\pi \Rightarrow$ rotation of the magnetization over 2π

\Rightarrow need a 3D spin polarimeter !

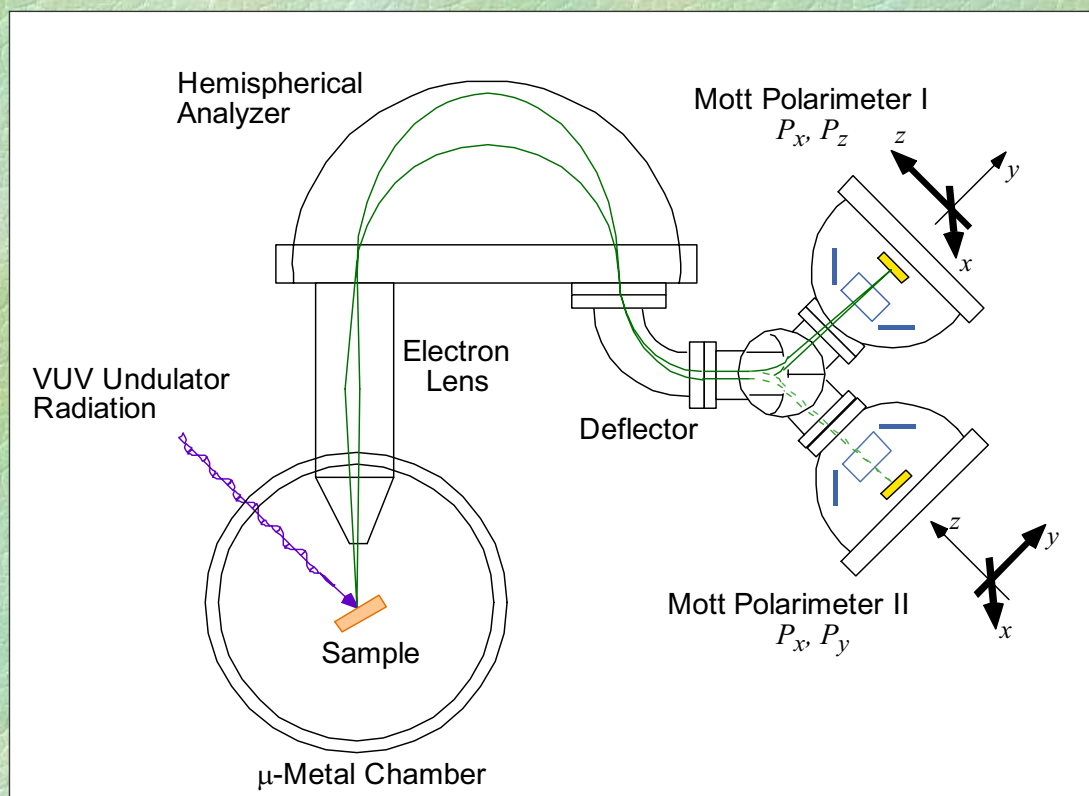
COPHEE: the complete photoemission experiment

...measures all properties of the photoelectron:

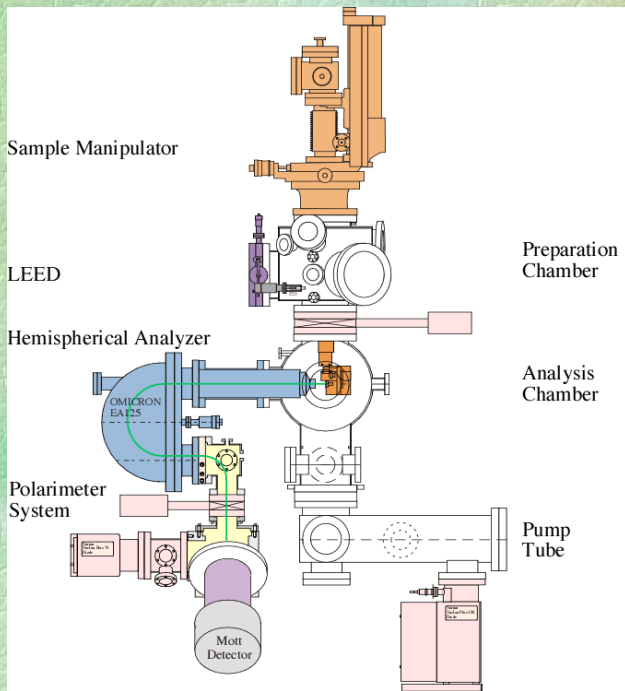
- energy
- momentum (\sim 3D, at the SLS !)
- spin (3D)

... controlled by **CROISSANT** software !

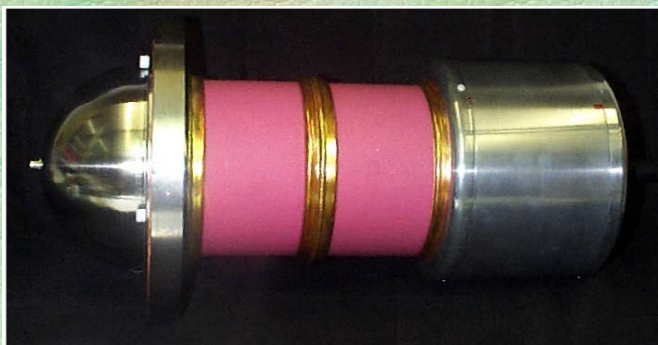
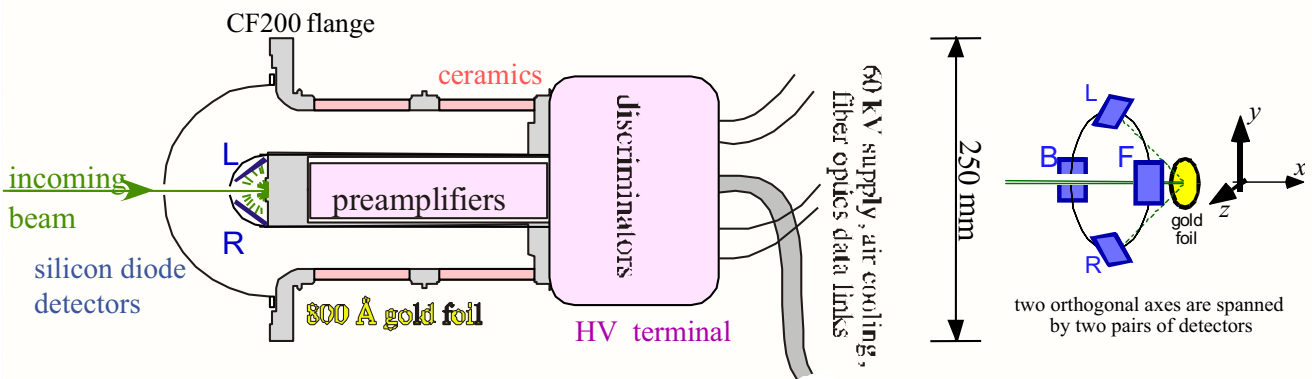
COPHEE - The Complete Photoemission Experiment



Setup of COPHEE:



The 60 keV Mott Detector



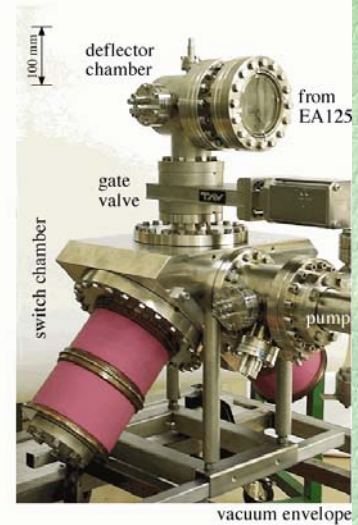
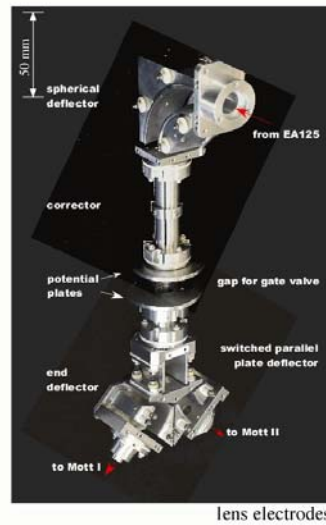
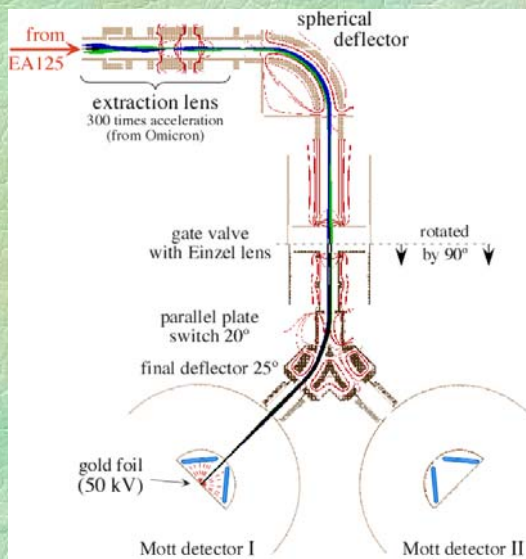
$$\text{asymmetry } A = \frac{(N_L - N_R)}{(N_L + N_R)}$$

$$\text{electron polarization } P = \frac{A}{S}$$

S = "Sherman function"
(analyzing power)

Backscattering at high energies:
Very inefficient process ($\sim 10^{-3}$)

The Transfer / Distributor Lens

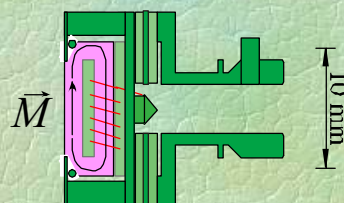
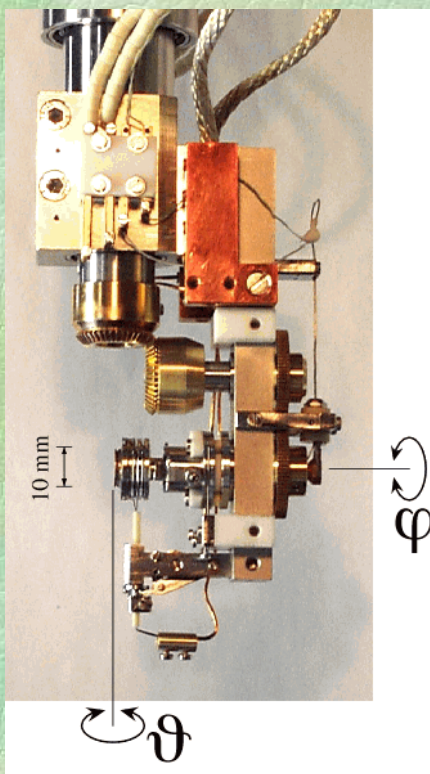


M. Hoesch et al., JES 124, 263 (2002)

7

Goniometer Head of the Sample Manipulator

- 2 axis rotation
- liquid He cooling (60 K)
- contacts for heating and magnetizing
- sample transfer to preparation facilities



Swiss Stub sample holder with picture frame sample



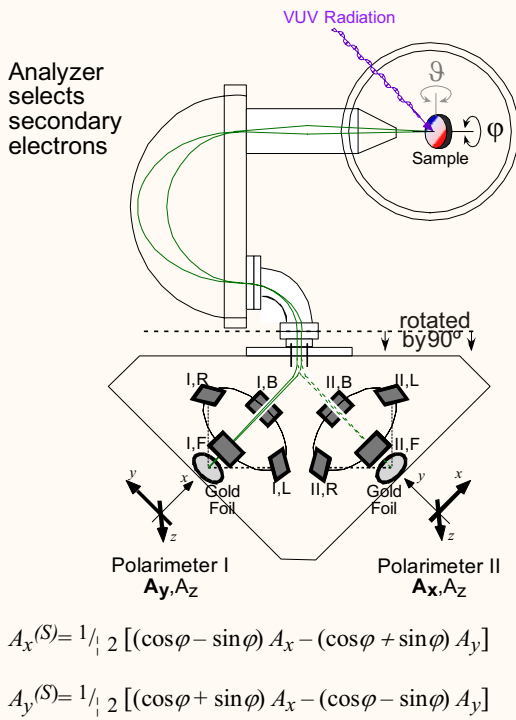
Nickel sample with the filament for DC resistive heating and pulsed current magnetizing remanence ~30%

8

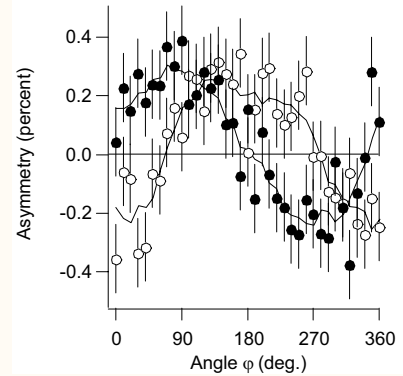
Secondary electron polarimetry

Courtesy M. Hoesch

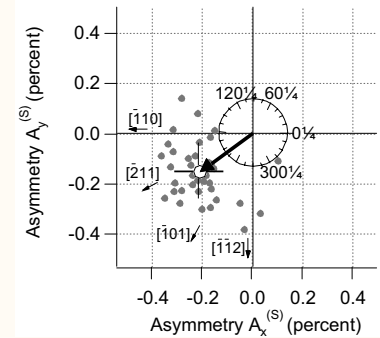
secondary electrons from a magnetized sample are polarized along the magnetization direction (M. Landolt *et al.* 1985)



Measured asymmetries A_x, A_y (detector coordinates)



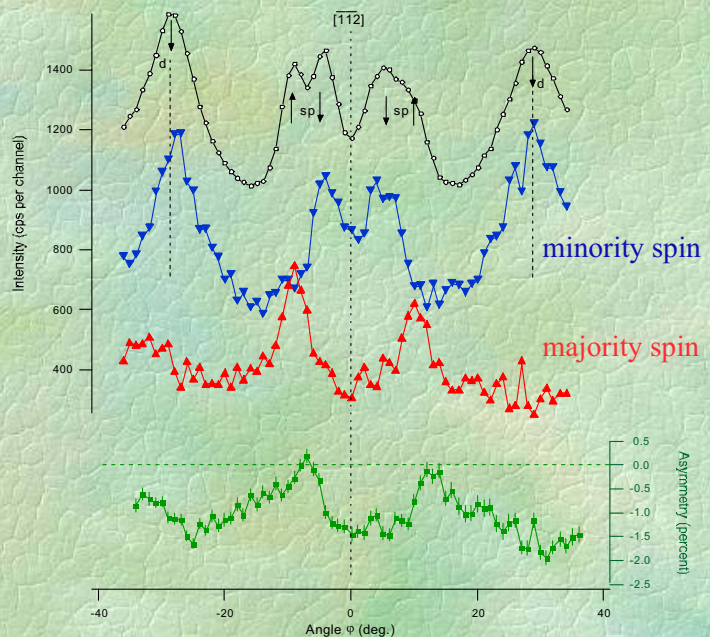
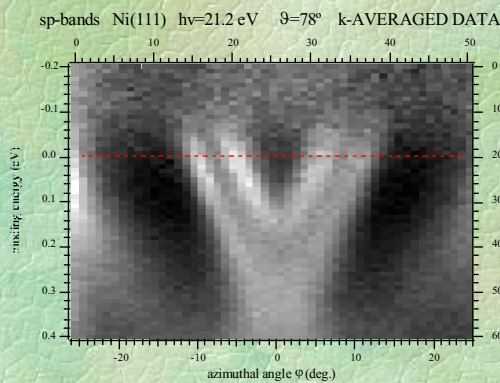
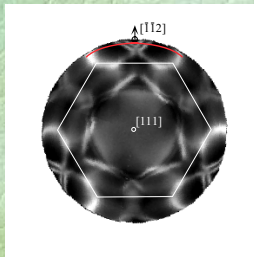
Reconstructed asymmetries $A_x^{(S)}, A_y^{(S)}$ (sample coordinates)



=> vectorial sensitivity ! 9

Spin-Resolved Fermi Surface Mapping

Azimuthal Scan



... a new, spin-resolved spectrometer

Surfaces/Interfaces: Spectroscopy beamline (SIS) at the Swiss Light Source (SLS)

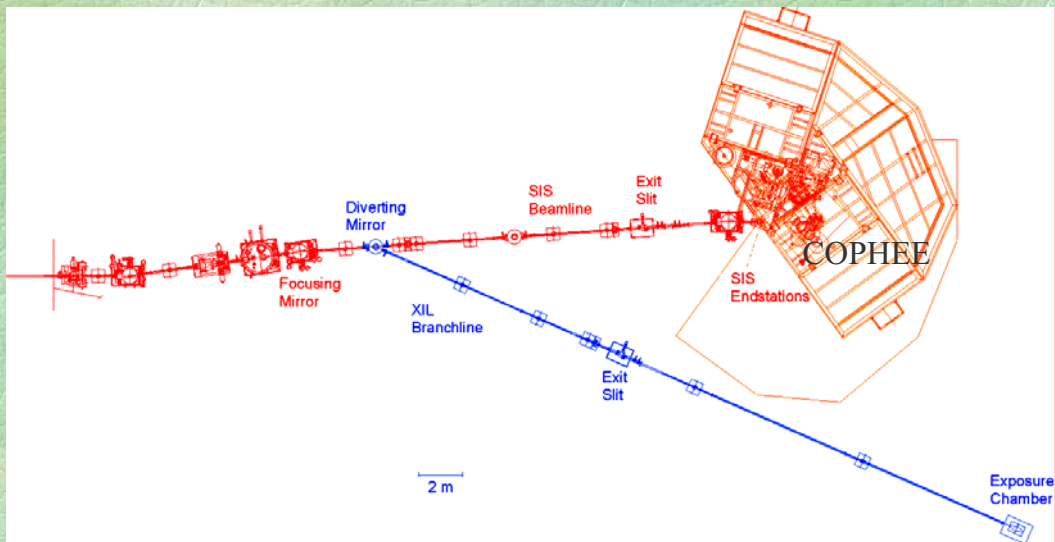
Side view:



Twin UE212

Optics

Spectrometers



Valence Bands - Lecture 3

Courtesy L. Patthey / SLS

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COPHEE at the SIS beamline

⇒ Access to very interesting photon beam properties

- small light spot on sample ⇒ high energy resolution with Omicron EA125 !
- photon energy range: k-space mapping (ARPES) and also core level spectroscopy (incl. XPD)
- fast polarization switching (future) ⇒ dichroism with spin detection
- clean photons (low background in quasiperiodic mode) ⇒ photoemission of thermally excited electrons

First taste: the surface state on Au(111)

Valence Bands - Lecture 3

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The Spin-Orbit Split Surface State on Au(111)

VOLUME 77, NUMBER 16

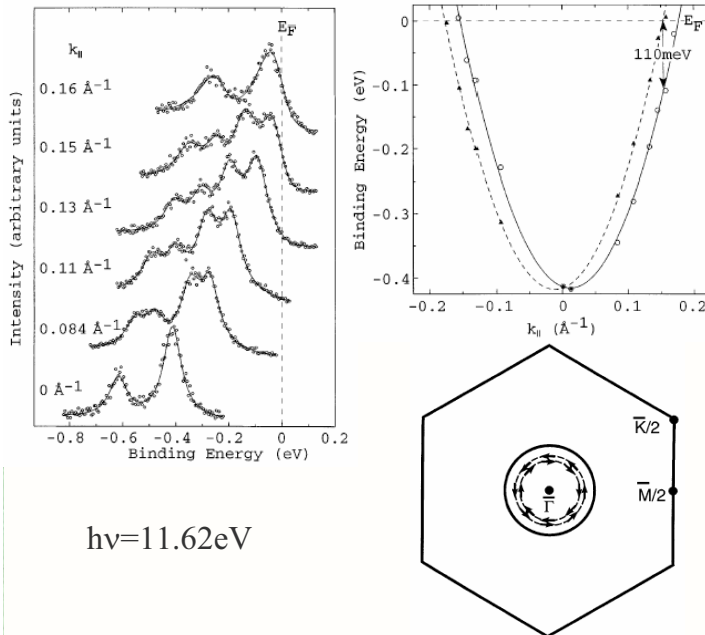
PHYSICAL REVIEW LETTERS

14 OCTOBER 1996

Spin Splitting of an Au(111) Surface State Band Observed with Angle Resolved Photoelectron Spectroscopy

S. LaShell, B. A. McDougall, and E. Jensen

Physics Department, Brandeis University, Waltham, Massachusetts 02254
(Received 19 July 1996)

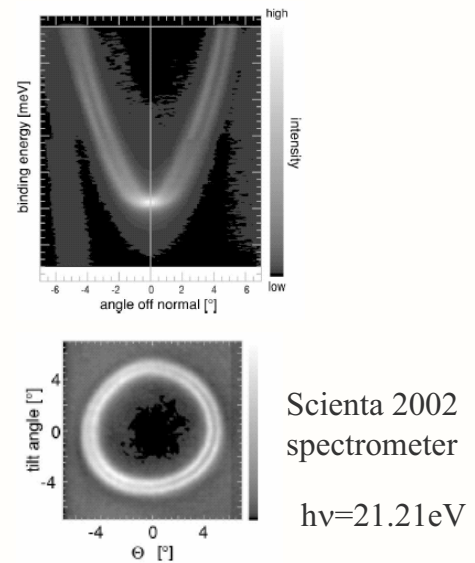


$h\nu = 11.62 \text{ eV}$

PHYSICAL REVIEW B, VOLUME 63, 115415

Direct measurements of the L-gap surface states on the (111) face of noble metals by photoelectron spectroscopy

F. Reinert,* G. Nicolay, S. Schmidt, D. Ehm, and S. Hüfner
Fachrichtung Experimentalphysik, Universität des Saarlandes, 66041 Saarbrücken, Germany
(Received 6 October 2000; published 1 March 2001)



\Rightarrow spin-resolution is a challenging task

13

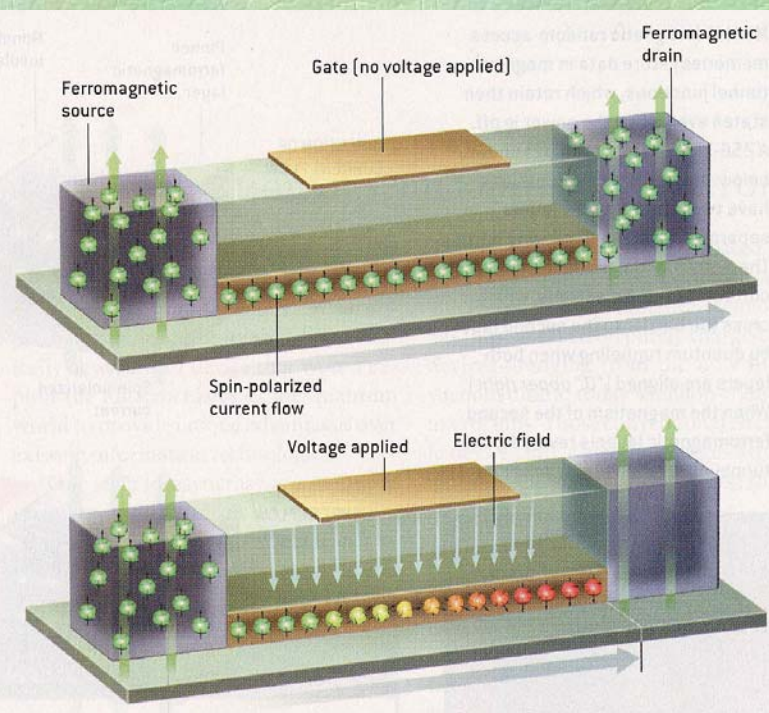
Valence Bands - Lecture 3

The Spin Field Effect Transistor (spin FET)

Principle – electric field from gate causes spins to precess. Channel impedance depends of extent of spin rotation

Advantage – much less energy and time required to flip spins than to depopulate channel

Problem – has yet to be built due to lack of suitable spin injectors for III-Vs and Si. Ferromagnetic semiconductors are best due to conductivity match. Need high T_c DMS materials!

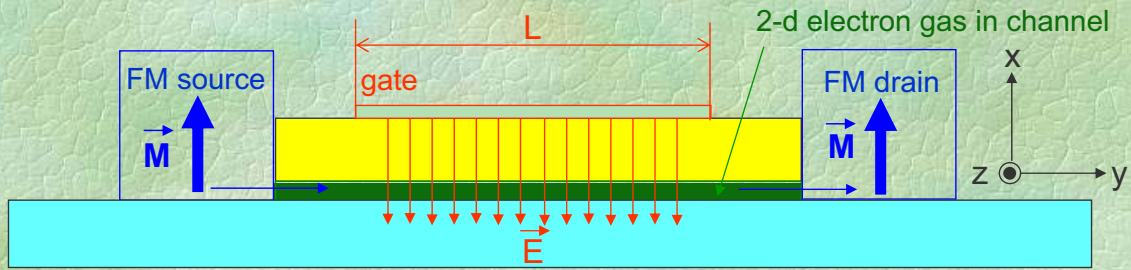


S. Datta & B. Das,
Appl. Phys. Lett. 56, 665 (1990)

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Valence Bands - Lecture 3

Spin precession in an electric field (?)



Spin-orbit interaction: $H_{SO} \sim (\vec{E} \times \vec{k}) \cdot \vec{\sigma}$ (Rashba term)

In the channel: $H_{SO} \sim k_y \sigma_z$

Source: injects spins with $|s_x\rangle = |-1/2\rangle$

In rotated frame: $|s_z\rangle = 1/\sqrt{2} |-1/2\rangle + 1/\sqrt{2} |+1/2\rangle$

$$E(|+1/2\rangle) = E_{kin} + \alpha k_y \quad E = E_F \rightarrow k_{F(\uparrow)} - k_{F(\downarrow)} = 2m^*\alpha / \hbar^2$$

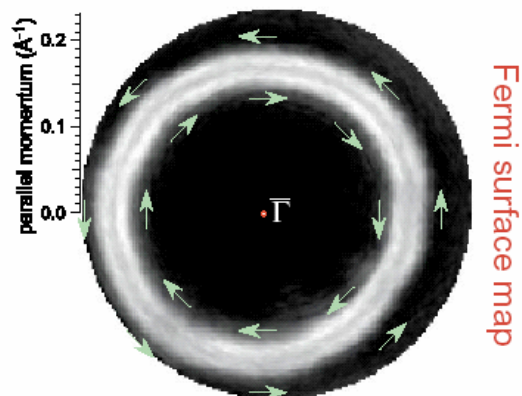
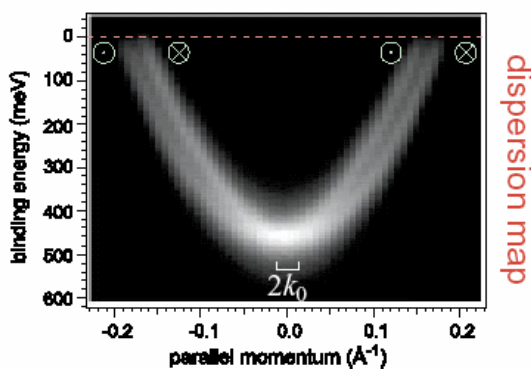
$$E(|-1/2\rangle) = E_{kin} - \alpha k_y$$

$$\rightarrow \text{Phase shift } \Delta\phi = (k_{F(\uparrow)} - k_{F(\downarrow)})L = (2m^*\alpha / \hbar^2)L$$

→ Spin precession around z axis !

The Shockley surface state on Au(111)

spin-integrated photoemission at $h\nu = 21.1$ eV, $T = 160$ K instrumental resolution $\Delta E = 25$ meV, $\Delta\theta = 0.5^\circ$ (FWHM)



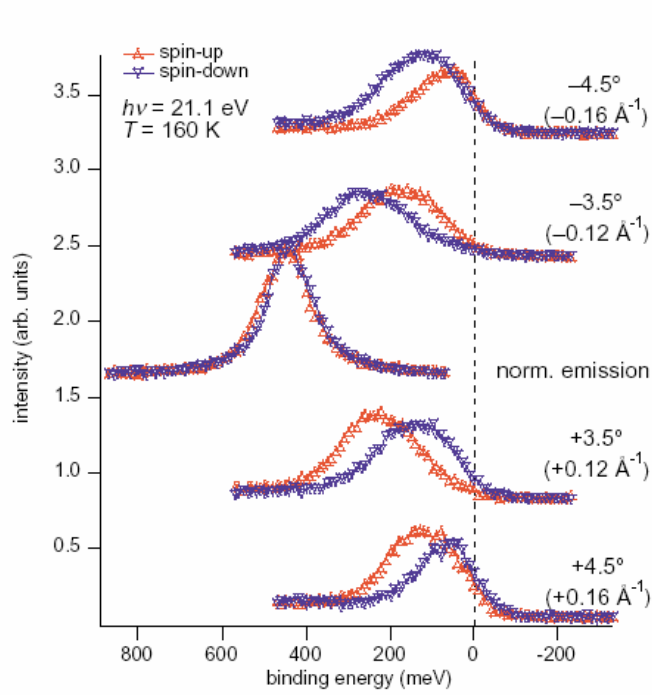
$$2k_0 = 0.026 \text{ \AA}^{-1} \quad E_B = 470 \text{ meV} \quad k_F = 0.173 \text{ \AA}^{-1} \pm k_0 \quad m^* = 0.24 m_e$$

Theory: spin-orbit coupling

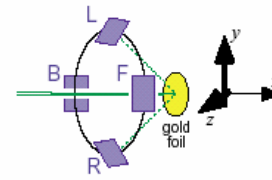
$$H_{SOC} = \frac{\mu_B}{2c^2} (\vec{v} \times \vec{E}) \cdot \vec{\sigma}$$

$$E^{\uparrow\downarrow}(k) = E_0 + \frac{(k \pm k_0)^2}{2m^*}$$

Spin-resolved spectra of the surface state on Au(111)



instrumental resolution
 $\Delta E = 120$ meV, $\Delta\theta = 1.8^\circ$ (FWHM)



Mott scattering spin detector

$$\text{asymmetry } A = \frac{(N_L - \eta N_R)}{(N_L + \eta N_R)}$$

$$\text{electron polarization } P = \frac{A}{S}$$

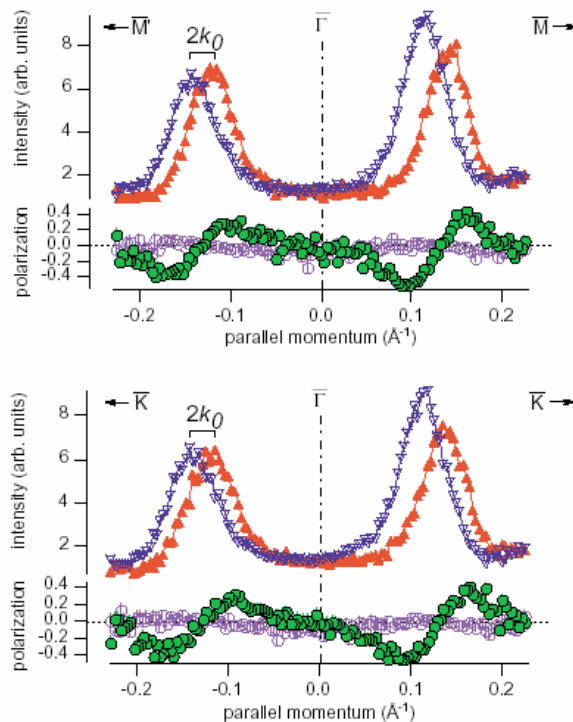
$$\text{Intensities } I^{\pm} = I_0 \cdot (1 \pm P)$$

parameters for analysis:

η = Correction of detection efficiency (instrumental asymmetry)

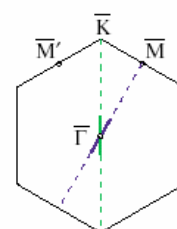
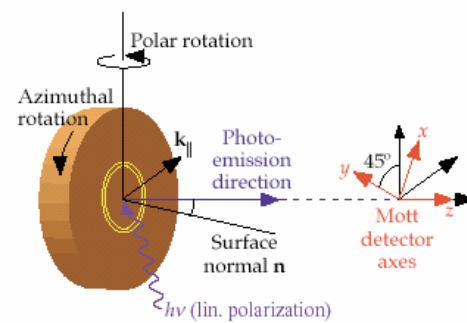
S = "Sherman function" (analyzing power)

Spin-resolved momentum distribution curves of the surface state on Au(111)



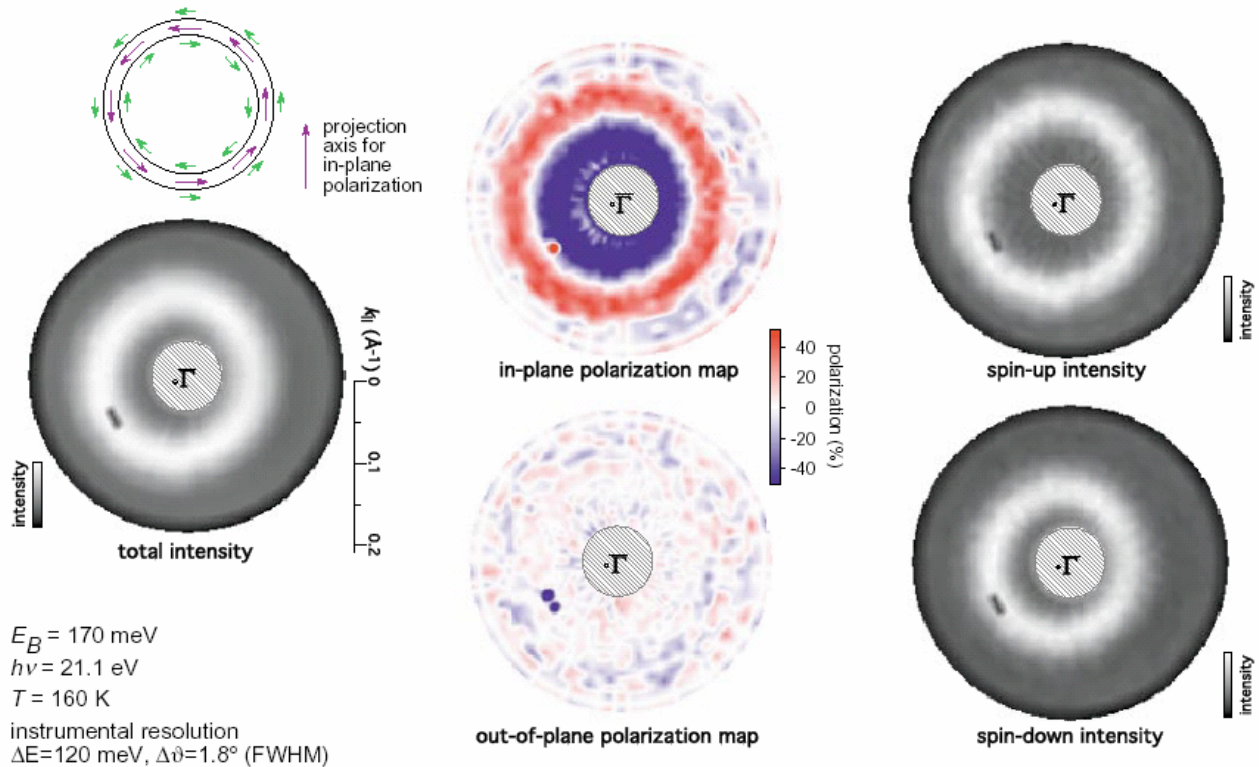
instrumental resolution
 $\Delta E = 120$ meV, $\Delta\theta = 1.8^\circ$ (FWHM)

- ▲ spin-up intensity
 - ▼ spin-down intensity
 - in-plane polarization
 - out-of-plane polarization
- $E_B = 170$ meV
 $h\nu = 21.1$ eV
 $T = 160$ K



Surface Brillouin zone

Spin-resolved momentum distribution map of the surface state on Au(111)



=> First spin-resolved "Fermi surface" map

Valence Bands - Lecture 3

Ultrathin Films of Ni on Cu(001)



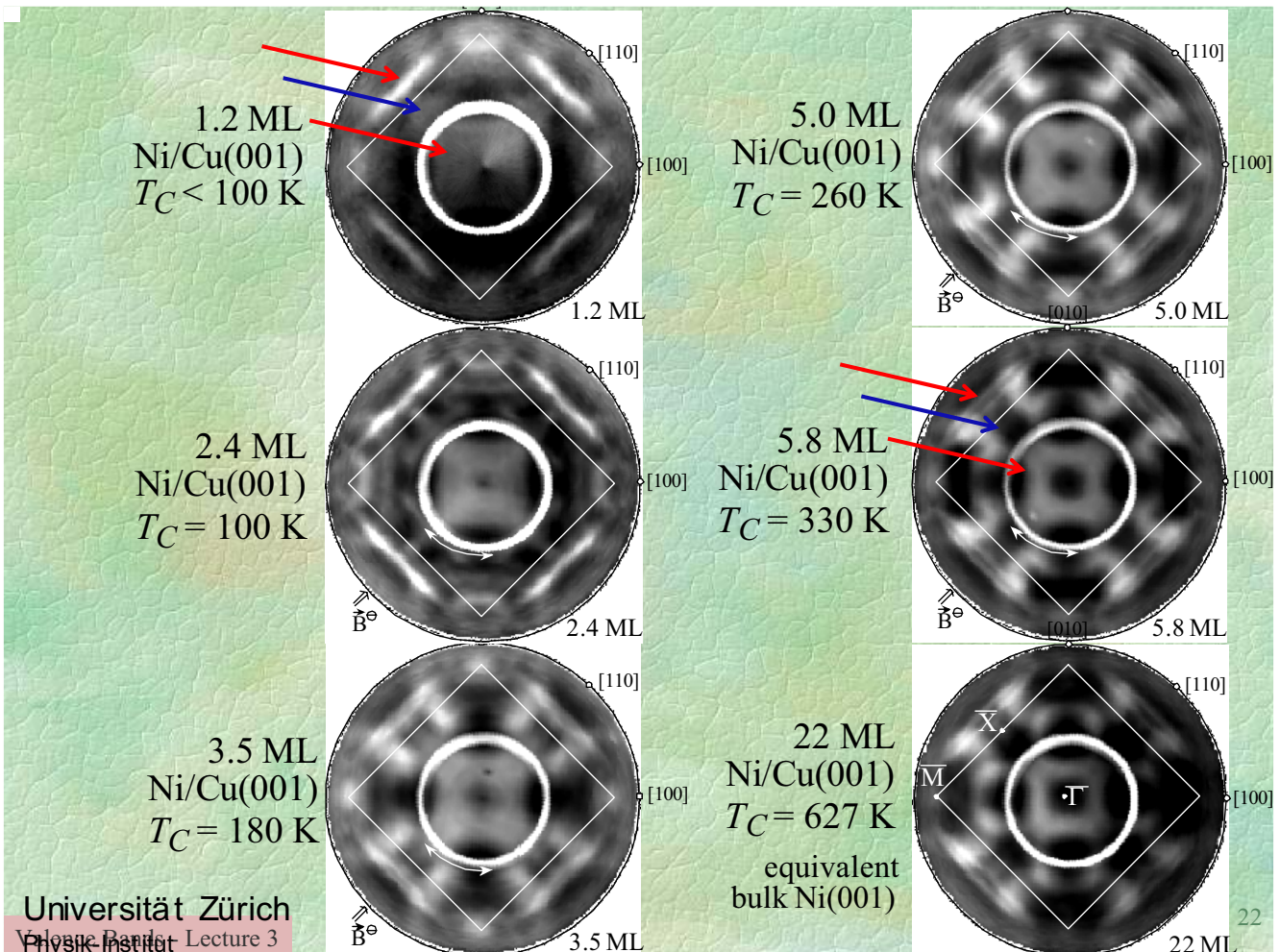
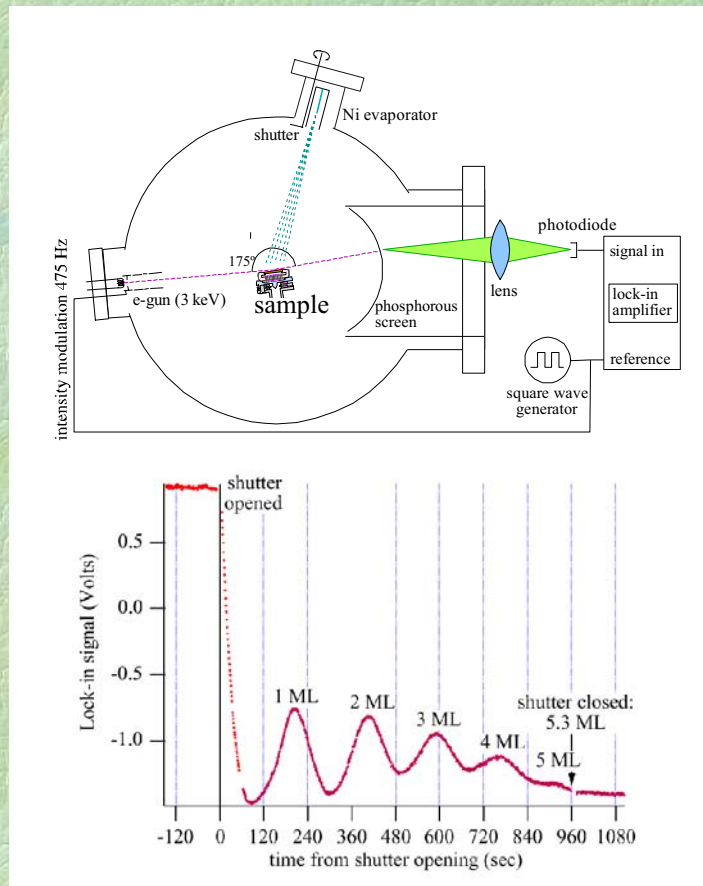
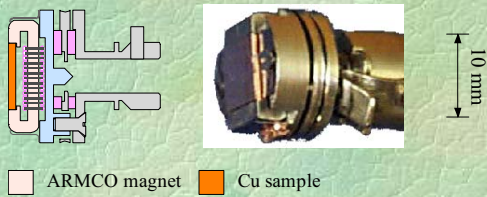
- grows epitaxially
- well ordered films
- T_c depends on film thickness
- bulk-like Fermi surface already at 1 ML (G. J. Mankey et al., PRL 78, 1146 (1997))
- Full 3d magnetic moment reached only at 6 ML (P. Srivastava et al., PRB 56, R4398 (1997))

Preparation of Monolayer Films of Ni on Cu(001)

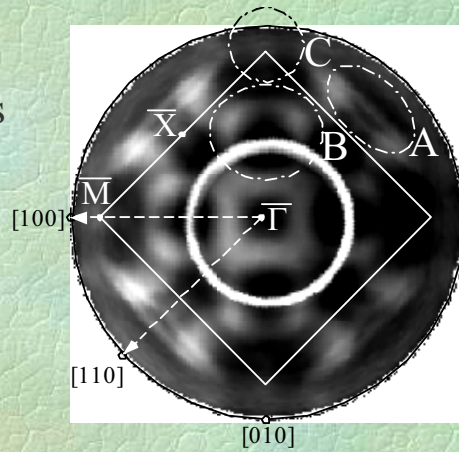
Ni deposited from e-beam heated rod at 0.33 ML/min. onto clean Cu(001)

Annealing to 420 K.

Cooling to 150 K (liquid N₂).



Band Character of
Fermi Surface Contours
(thick film ~ bulk-like)

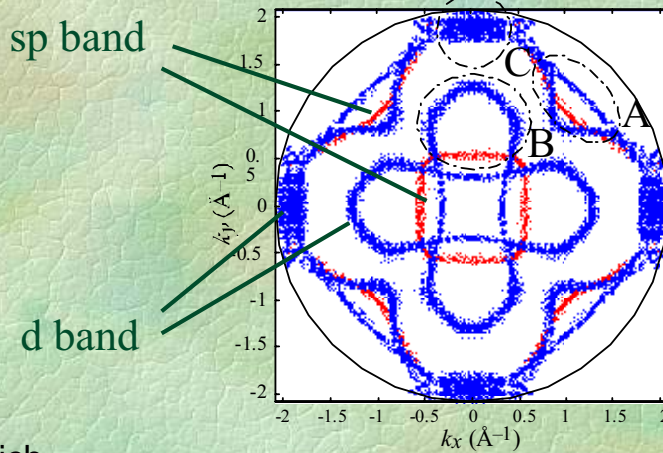


data from
22 ML
Ni/Cu(001)
 $h\nu = 21.22$ eV
equivalent
bulk Ni(001)

Fermi surface
calculation

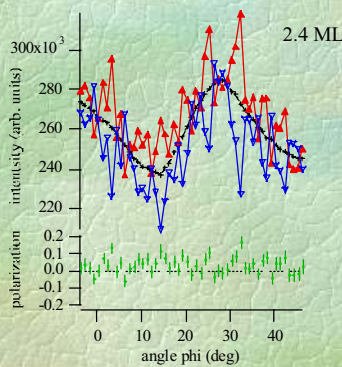
free electron
final state
approximation

$h\nu = 21.22$ eV
 $\Phi = 5.2$ eV
 $V_0 = 10.2$ eV

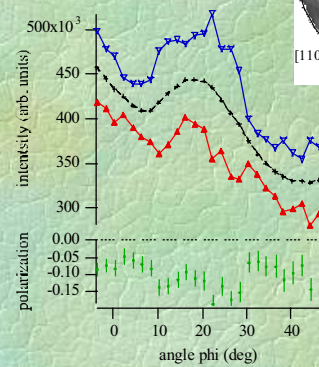


Ni/Cu(001) azimuthal scans at E_F , $\vartheta = 28^\circ$,
 $h\nu = 21.22$ eV, $T = 150$ K

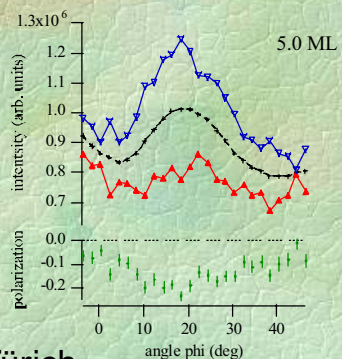
2.4 ML
Ni/Cu(001)
 $T_C = 100$ K



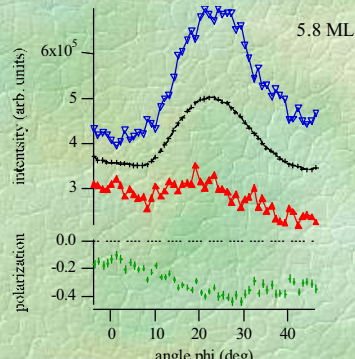
3.5 ML
Ni/Cu(001)
 $T_C = 180$ K



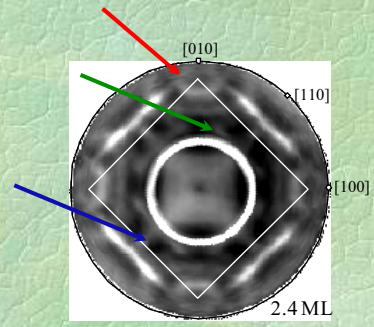
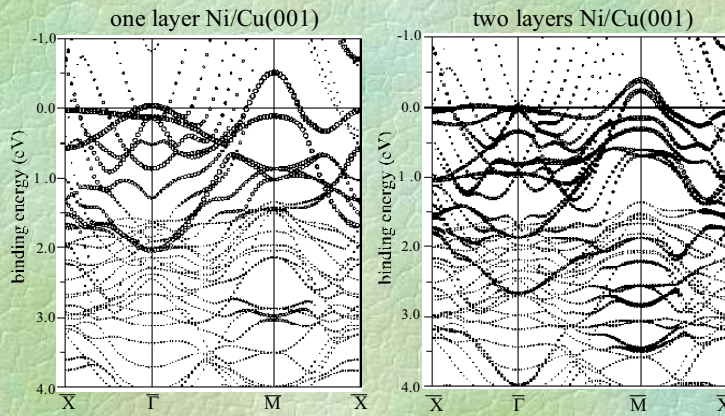
5.0 ML
Ni/Cu(001)
 $T_C = 260$ K



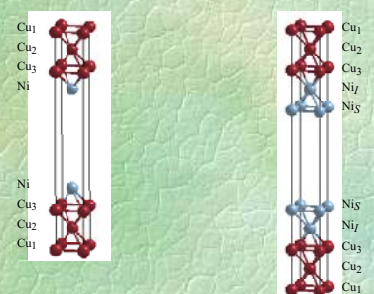
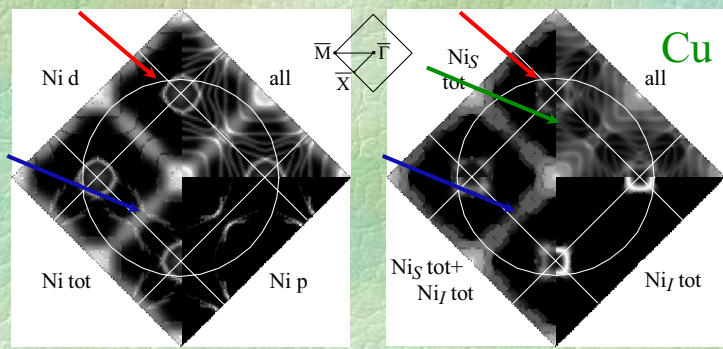
5.8 ML
Ni/Cu(001)
 $T_C = 330$ K



Ni/Cu(001) Slab Calculations



data from
2.4 ML Ni/Cu(001)
 $h\nu = 21.22 \text{ eV}$

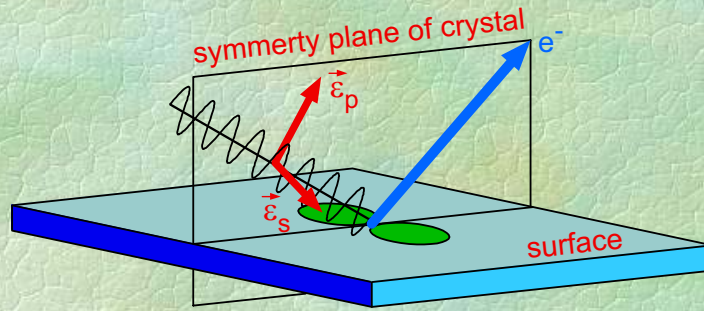


1 ML Ni/5 ML Cu/1 ML Ni 2 ML Ni/5 ML Cu/2 ML Ni

Ultrathin films of Ni on Cu(001)

- ∞ < 3 ML: paramagnetic interface band structure
- ∞ Around 3 ML two things happen:
 - $T_c > T_{meas} \Rightarrow$ Exchange splitting appears
 - Band structure becomes bulk-like (3D)
- ∞ The sp bands are bulk-like already at ~1 ML
- ∞ The d bands form interface states for < 3 ML

Intensities in Valence Photoemission - Symmetry Effects



$\vec{\epsilon}_p$ photon polarization in...
 $\vec{\epsilon}_s$...perpendicular ("senkrecht") to...scattering plane

photoemission matrix element:

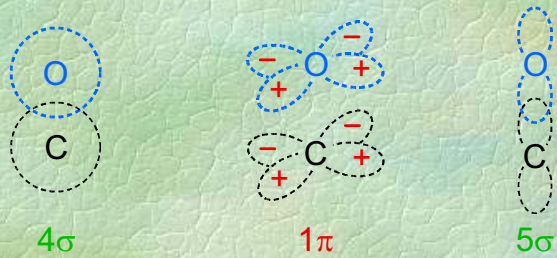
$$| \langle \phi_{f,kin} | \vec{r}_k \cdot \vec{\epsilon} | \phi_{i,k}(\vec{r}_k) \rangle |^2 \rightarrow \text{Intensity}$$

mirror reflection symmetries:

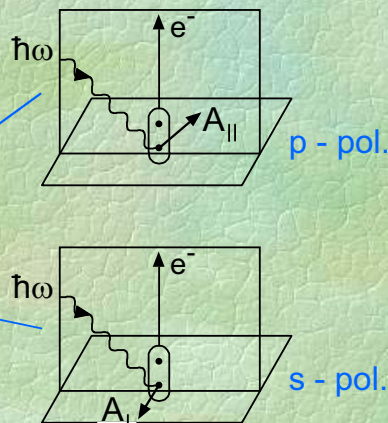
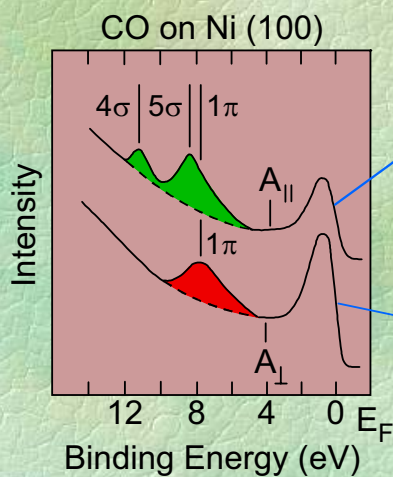
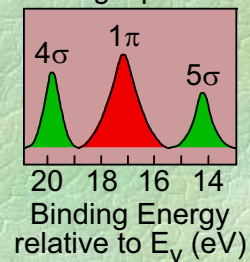
p - pol.	+1	+1	-1	0
	+1	+1	+1	max.
s - pol.	+1	-1	-1	max.
	+1	-1	+1	0

27

CO Molecular Orbitals



CO gasphase



from Hüfner

28

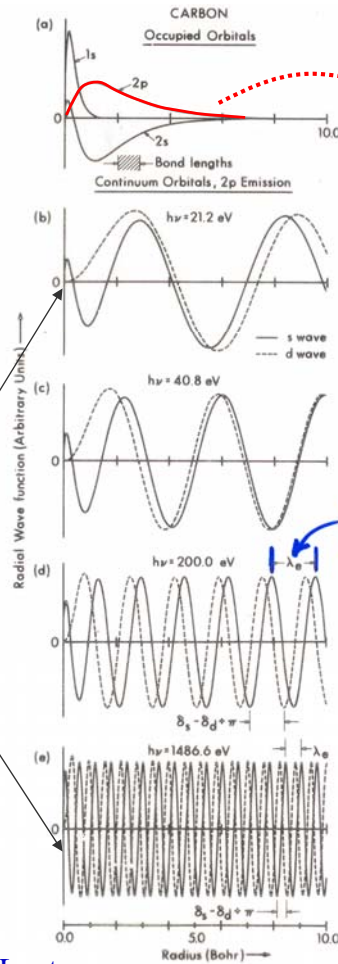
Intensities in
Valence Photoemission
- Atomic Effects

$$m_{i,f} \sim \langle \phi_{f,kin} | \vec{r} \cdot \vec{\epsilon} | \phi_{i,k} \rangle$$

as for core levels

**RADIAL MATRIX ELEMENTS
TO $\pm 1 = s$ and d CHANNELS:**

... for various
energies

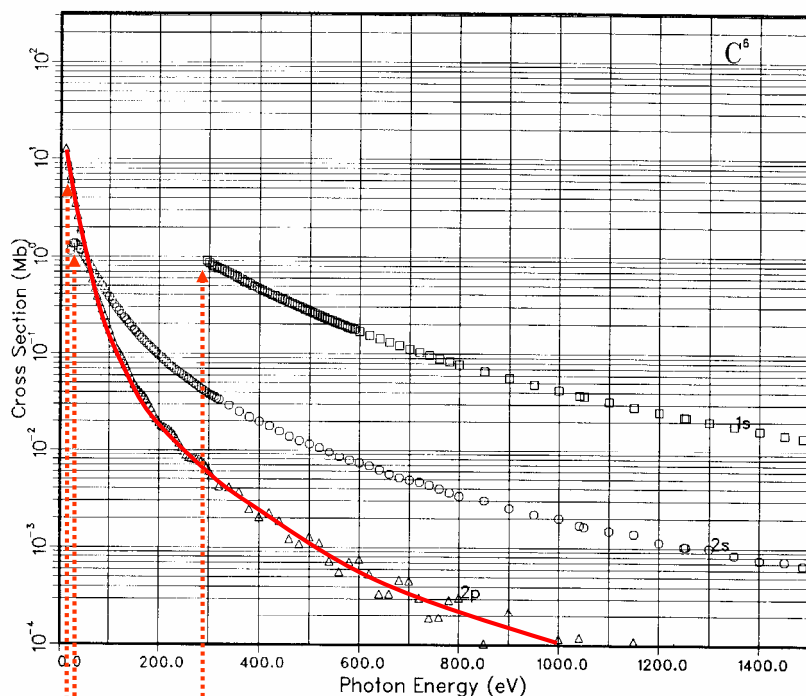


DE BRAGLIE WAVELENGTH = $\frac{h}{p} = \frac{2\pi}{k}$

PHASE SHIFT DIFFERENCE

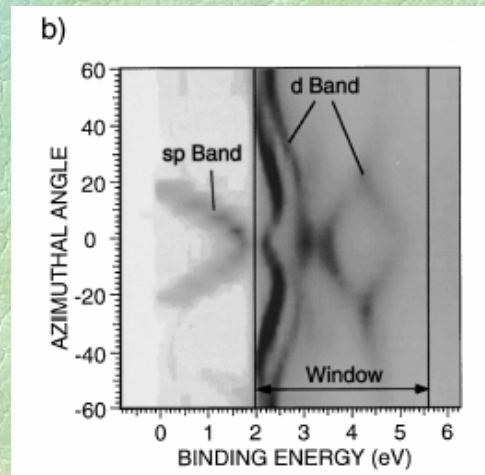
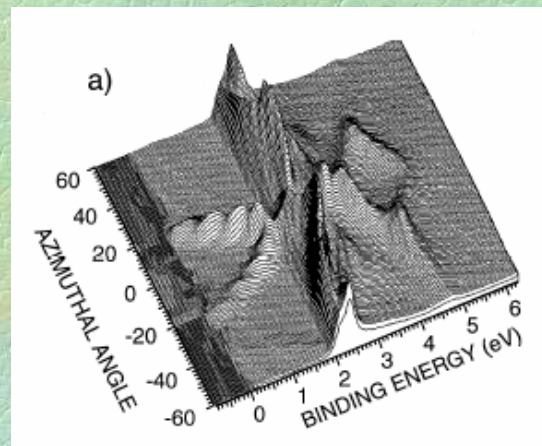
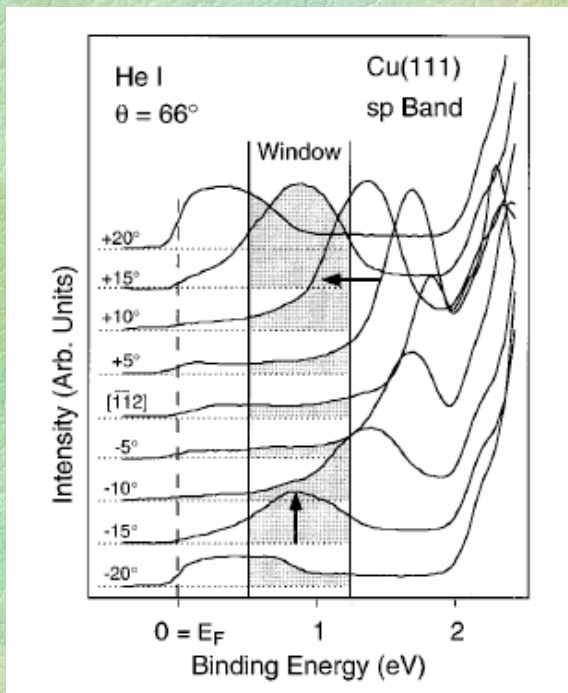
Plus other
Examples
from Yeh and
Lindau
in Sec. 1.5 of
X-Ray Data
Booklet, and
plots for all
elements at:
[http://
ulisse.elettra.
trieste.it/
elements/
WebElements.
html](http://ulisse.elettra.trieste.it/elements/WebElements.html)

GRAPH 1. Atomic Subshell Photoionization Cross Sections for 0-1500 eV, $1 \leq Z \leq 103$
See page 6 for Explanation of Graphs



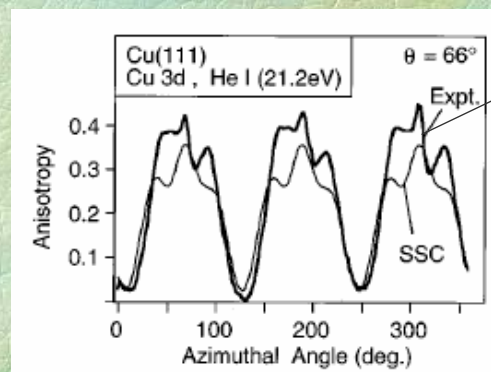
C binding energies(eV) are:
1s(2) 290.860 2s(2) 17.5409 2p(2) 8.98202

Intensities in Valence Photoemission - Diffraction Effects



Integration of Intensities over the Entire d-Band Region

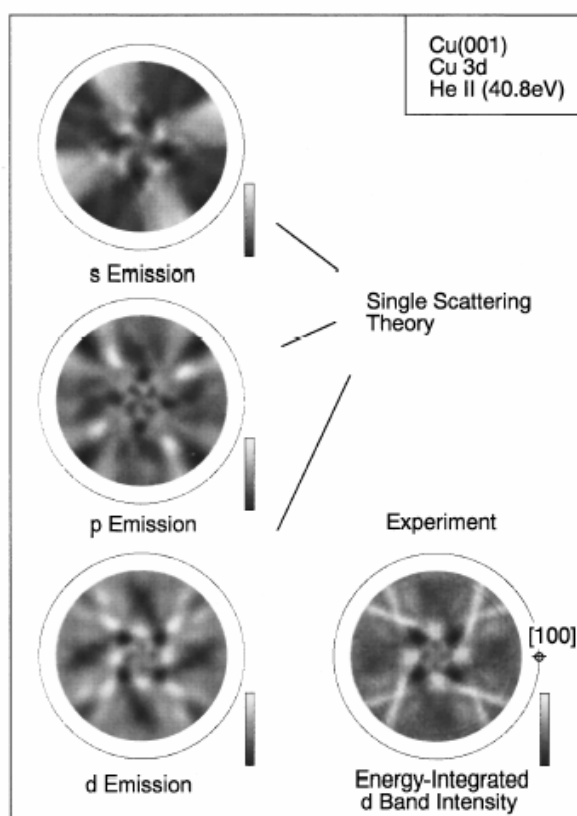
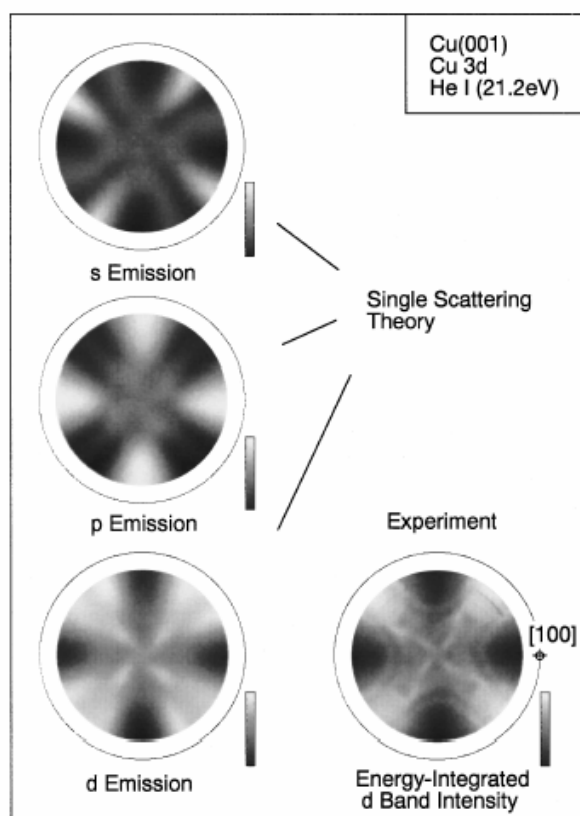
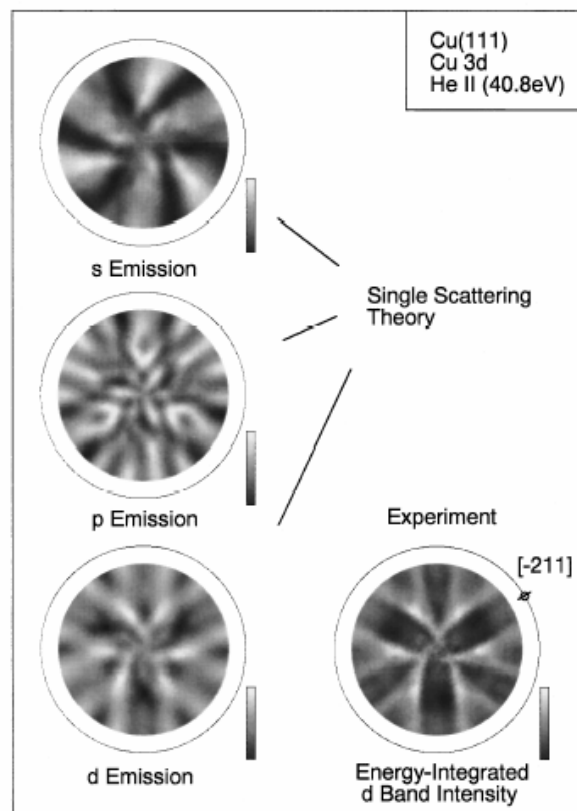
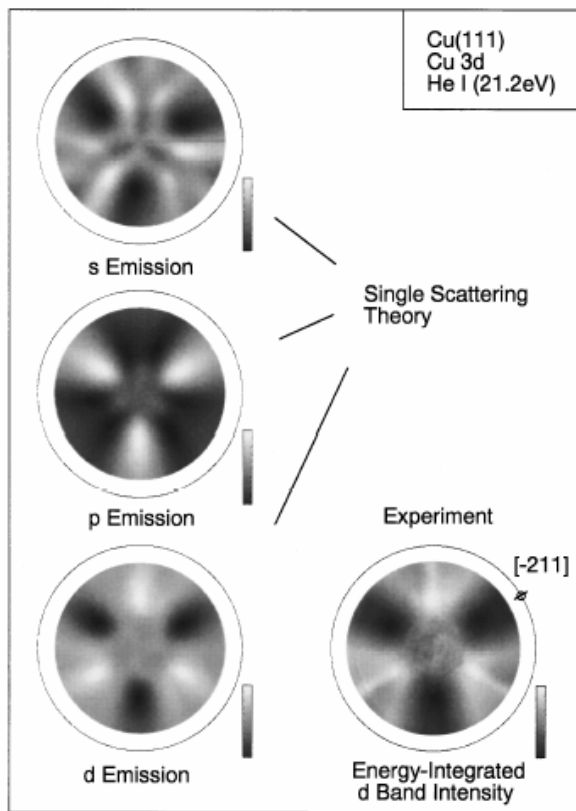
Choose energy window large enough so the d-band peak never leaves the window => the intensity variation of the peaks can be monitored



Theoretical curve: Single Scattering Cluster (SSC) calculation for a cluster representing a Cu(111) surface from a localized full d shell (like in x-ray photoelectron diffraction (XPD), hence

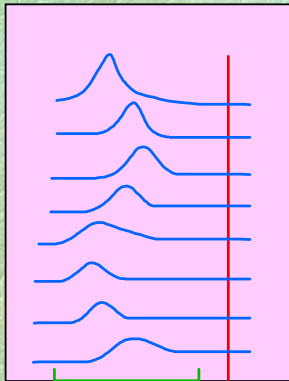
ultraviolet photoelectron diffraction (UPD)

J. Osterwalder et al., PRB 53, 10209 (1996)



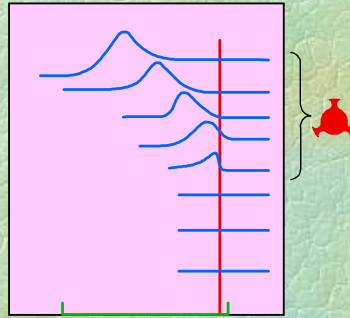
UPD and Photoemission Intensities

filled shells:



Window ϵ_F

unfilled shells: ?



Window ϵ_F

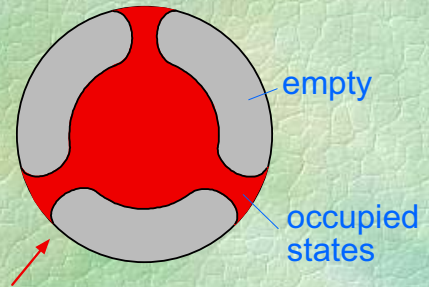
direct transition is lost at Fermi surface.

direct transition never disperses out of measurement window (e.g. Cu 3d).



UPD describes overall band intensities !

(sum rule over several subbands)



But: Must know angular momentum compos. of occupied (crystal field) states !

UPD may describe intens. in occupied k-Region