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**SPRING COLLEGE ON SCIENCE AT THE NANOSCALE**  
**(24 May - 11 June 2004)**

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**TDDFT THEORY:**

**APPLICATIONS TO NANO AND BIO-STRUCTURES**

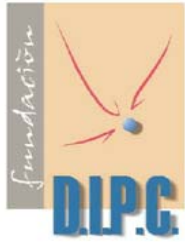
**Optical Properties of Nanostructures:**  
**Extended systems: problems and new developments**

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*These are preliminary lecture notes, intended only for distribution to participants.*



# *Optical properties of nanostructures*

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*I. Motivation. Basic concepts. Foundations TDDFT.*

*II. Illustration of the physics for nano- and bio structures*

*III. Extended systems: problems and new developments*



*ICTP Spring College on Science at the Nanoscale, Trieste May 24<sup>th</sup> -June 11<sup>th</sup> 2004*

# *Optical properties of nanostructures*

## *III. Extended systems: problems and new developments*

Introduction:

*how to handle the electron dynamics in extended systems under the influence of an external electromagnetic field?*

TDDFT:

- Problems with standard exchange-correlation functionals*
- A new fxc derived from Many-body perturbation theory  
proper description of excitonic effects!!!*
- Applications to polyacetylene as one-dimensional system*

*G. Onida, L. Reining and AR, Rev. Mod. Phys. 74, 601 (2002)*

*ICTP Spring College on Science at the Nanoscale, Trieste May 24<sup>th</sup> -June 11<sup>th</sup> 2004*

# Time-dependent approach for extended systems: a gauge formalism

G.F. Bertsch, J.I. Iwata, AR, K. Yabana, PRB62, 7998 (2000)

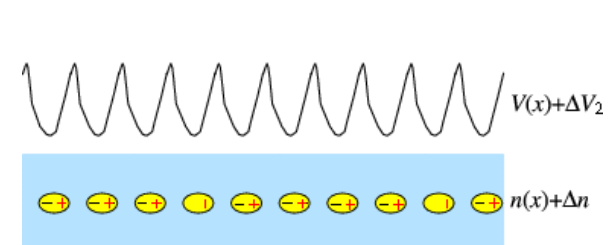
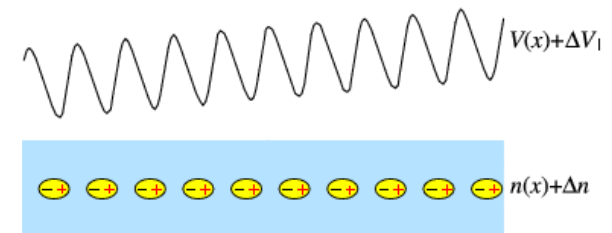
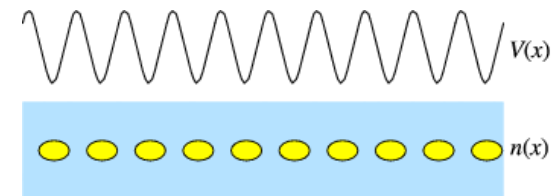
The Lagrangian of a periodic system in a volume V under a uniform field is

$$L = \sum_i \langle \psi_i | i \hbar \frac{\partial}{\partial t} - \frac{1}{2m} \left( \vec{p} + \frac{e}{c} \vec{A} \right)^2 - V_{ion} | \psi_i \rangle - E_{Hartree} - E_{xc} + \frac{V}{8\pi c^2} \left( \frac{d\vec{A}}{dt} \right)^2$$

The equation of motion are:

$$i \hbar \frac{\partial}{\partial t} \psi_i = \left[ \frac{1}{2m} \left( \vec{p} + \frac{e}{c} \vec{A} \right)^2 + V_{ion} + V_H + V_{xc} \right] \psi_i$$

$$\frac{d^2 \vec{A}}{dt^2} = -4\pi e^2 \frac{n}{m} \vec{A} - 4\pi c \frac{e}{V} \sum_i \langle \psi_i | \frac{\vec{p}}{m} | \psi_i \rangle$$

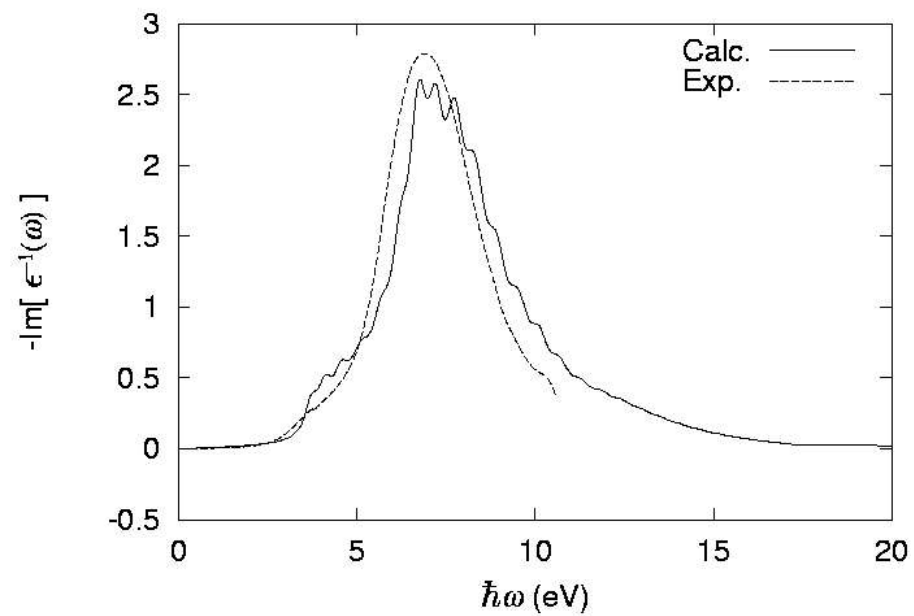
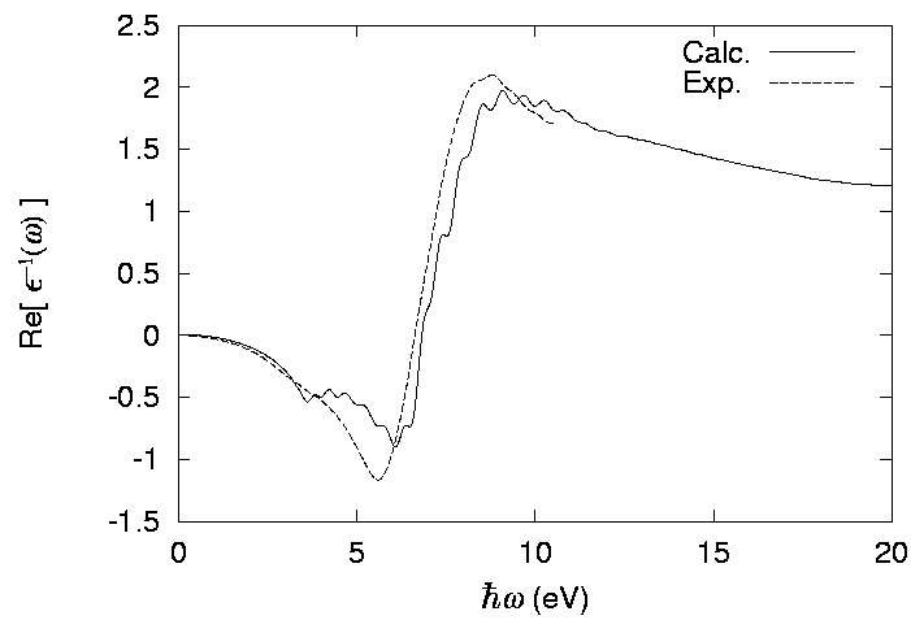


For the electric field is:

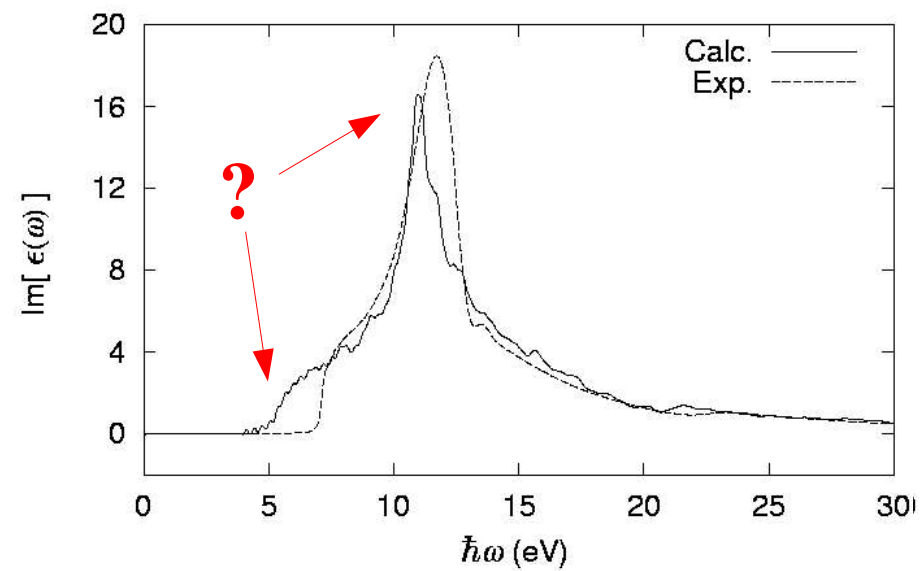
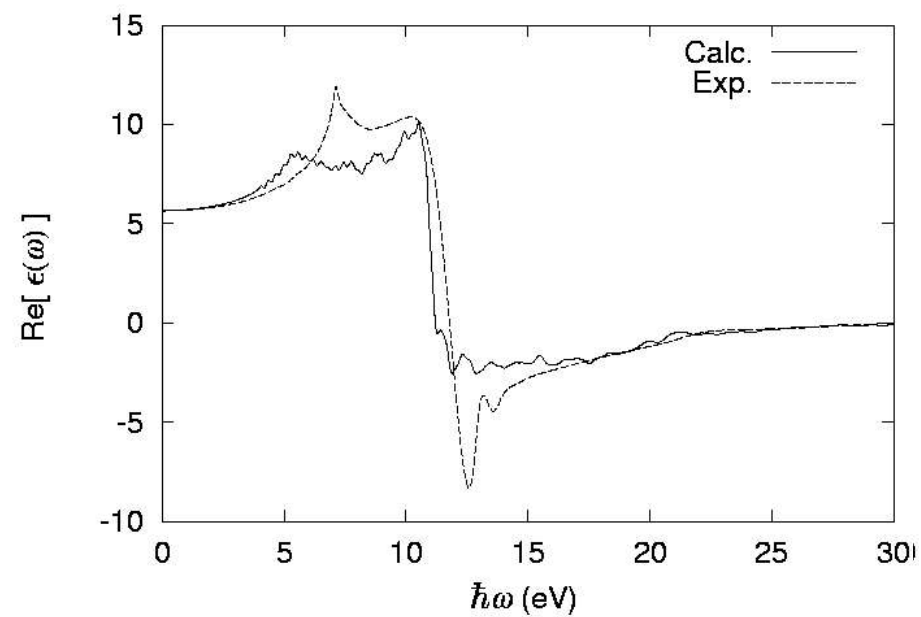
$$\vec{E}(t) = \frac{-1}{c} \frac{d\vec{A}}{dt}$$

$$\frac{d\vec{E}}{dt} = -4\pi \vec{j} \quad \text{and} \quad \vec{j} = \frac{-e}{V} \sum_i \langle \psi_i | \frac{\vec{p}}{m} | \psi_i \rangle - \frac{e^2}{c} n \vec{A}$$

## Lithium

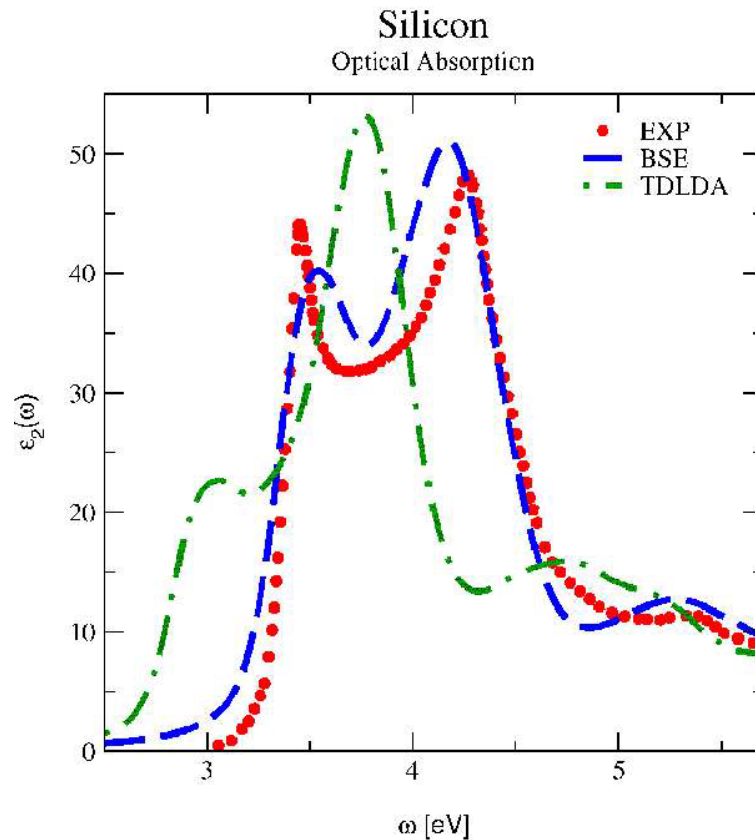


## Diamond



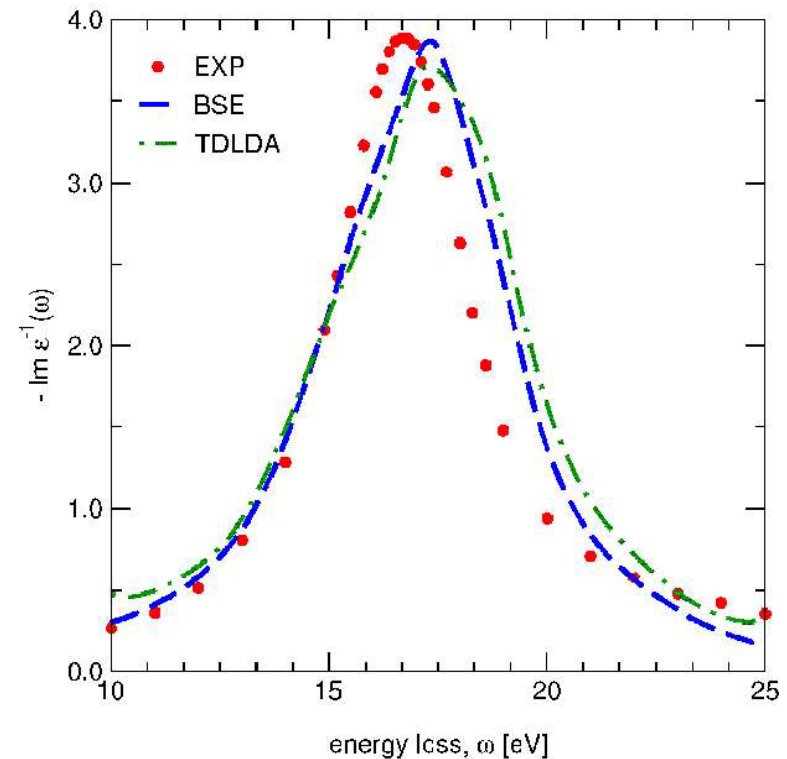
## Non-local fxc for extended systems:

### Motivation



The LDA Kernel is not able to reproduce Optical Properties in Solids

### BSE vs TDLDA comparison on EEL



The LDA Kernel already offers a good representation of the Electron Energy Loss (EEL) spectrum in Solids

See for a review: *G. Onida, L. Reining and AR, Rev. Mod. Phys. 74, 601 (2002)*

## Why a non-local (static?) fxc for extended systems:

- In the EEL spectra  $f_{xc}$  is added to the full coulomb that **already contains** a long range contribution

$$f_{xc} = -\alpha(\omega)/q^2$$

$$EEL \propto \epsilon^{-1}(\omega) = 1 + v\chi$$

$$\chi(\omega) = \chi_0(\omega) + \chi_0(\omega)(v + f_{xc}(\omega))\chi(\omega)$$

- In the absorption spectra  $f_{xc}$  is added to the full coulomb that **does not contains** the long range contribution ( $q=0$ )

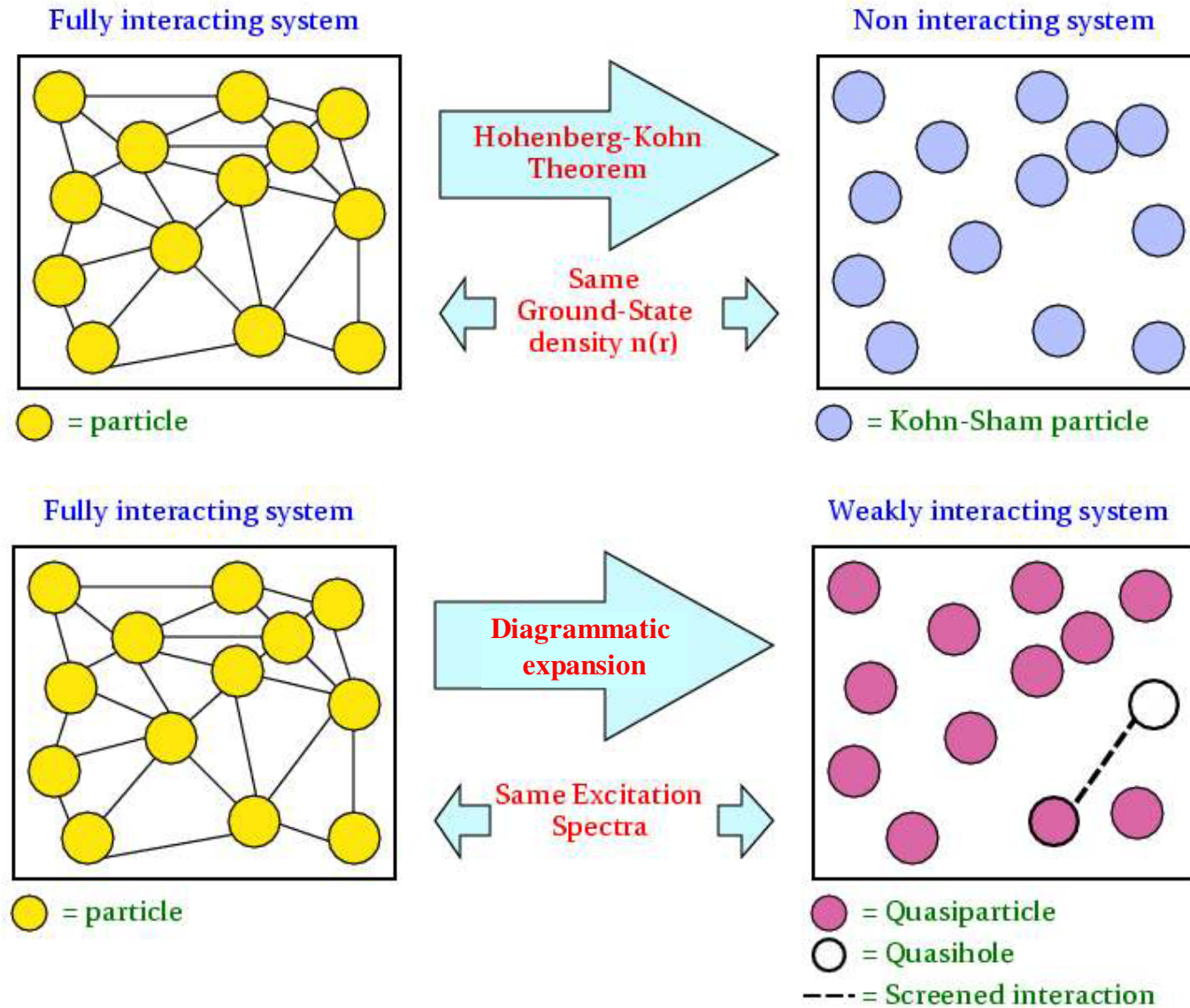
$$\epsilon_M(\omega) = 1 - v\bar{\chi} \quad \epsilon_M^{RPA} \equiv 1/[1 - v\chi_0]_{G=G'=0}$$

$$\bar{\chi}(\omega) = \chi_0^{GW}(\omega) + \chi_0^{GW}(\omega)(\bar{v} + f_{xc}(\omega))\bar{\chi}(\omega)$$

*The lack of a long range term in  $f_{xc}^{LDA}$  is relatively weightless in the EEL but is crucial in the absorption spectra!!!*



# Density Functional versus Many-body perturbation theory



*Band-gap problem!!!!*



# Density Functional Theory and Many-Body Perturbation Theory

$$\left[ -\frac{\nabla^2}{2} + V_{ext}(\mathbf{r}) + V_{Hartree}([n], \mathbf{r}) + V_{xc}([n], \mathbf{r}) \right] \phi_i(\mathbf{r}) = \epsilon_i \phi_i(\mathbf{r})$$

R. O. Jones and O. Gunnarsson, Rev. Mod. Phys. **61**, 689 (1989)

$$V_{xc}([n], \mathbf{r}) = \frac{\delta E_{xc}[n]}{\delta n(\mathbf{r})} \quad E_{xc}^{LDA}[n] = \int d\mathbf{r} n(\mathbf{r}) \epsilon_{xc}^{hom}([n]; \mathbf{r})$$

*Density Functional Theory*

Exchange-correlation Potential: Real, Local in space, Frequency independent

Self-Energy: Complex, Non-local in space, Frequency dependent

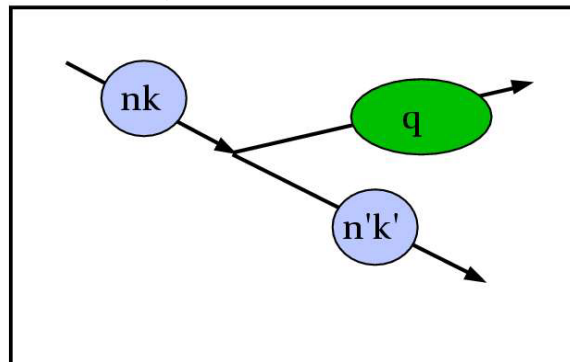
*Many-Body Perturbation Theory*



$$[\mathcal{H}_{KS} - V_{xc}(\mathbf{r})] \phi_i(\mathbf{r}; E_\lambda) + \int d\mathbf{r}' \Sigma(\mathbf{r}, \mathbf{r}'; E_\lambda) \phi_i(\mathbf{r}'; E_\lambda) = E_\lambda(\omega) \phi_\lambda(\mathbf{r}, E_\lambda)$$

G. Onida, L. Reining and AR, Rev. Mod. Phys. **74**, 601 (2002)

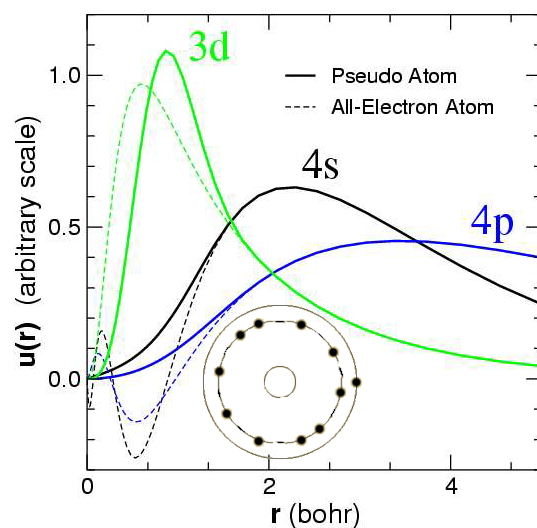
F. Aryasetiawan, Rep. Prog. Phys. **61**, 237-312 (1998)

## The self-energy physics

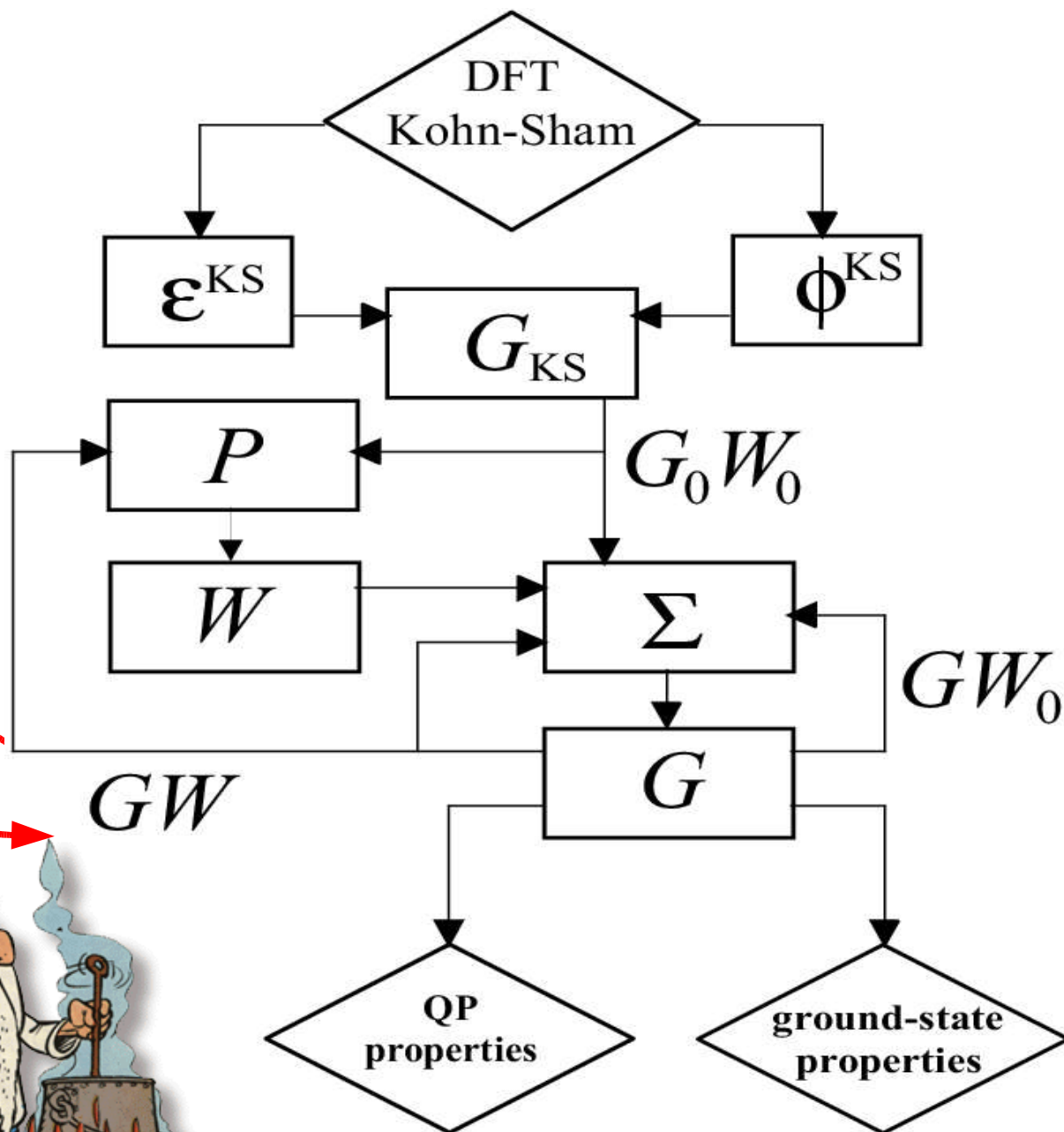


 = Kohn-Sham states  
 = Plasmons/Electron-hole states

## The pseudopotential approach



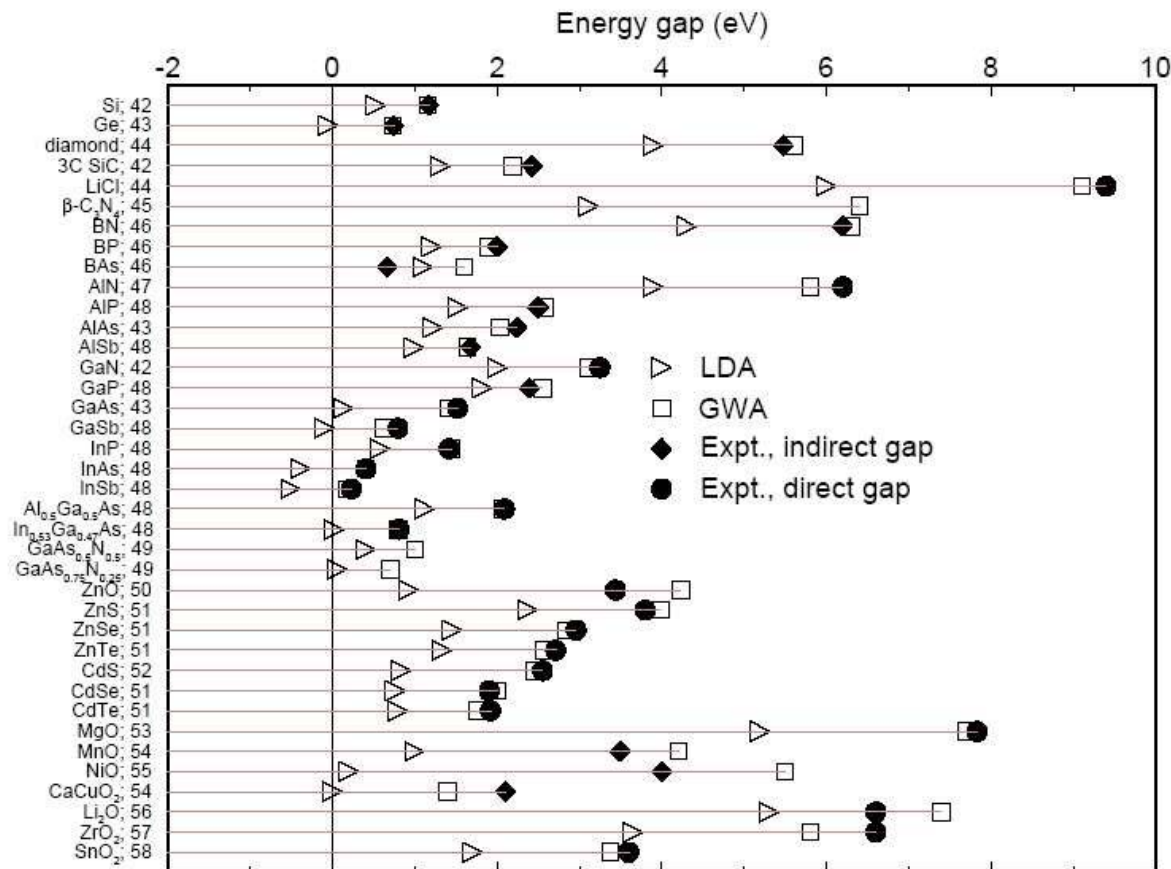
The GW "soup"



$$P(12) = -iG(12)G(21^+)$$

$$\Sigma(12) = iG(12^+)W(12)$$

# $G_0W_0$ Band Structures of Insulators



$$E_n^{QP} \simeq \epsilon_n^{KS} + \langle \psi_n | \sum (\epsilon_n^{KS}) - v_{xc} | \psi_n \rangle$$

From "Quasiparticle calculations in solids", W.G. Aulbur, L. Jönsson and J.W. Wilkins, *Solid State Physics* 54 1 (2000),

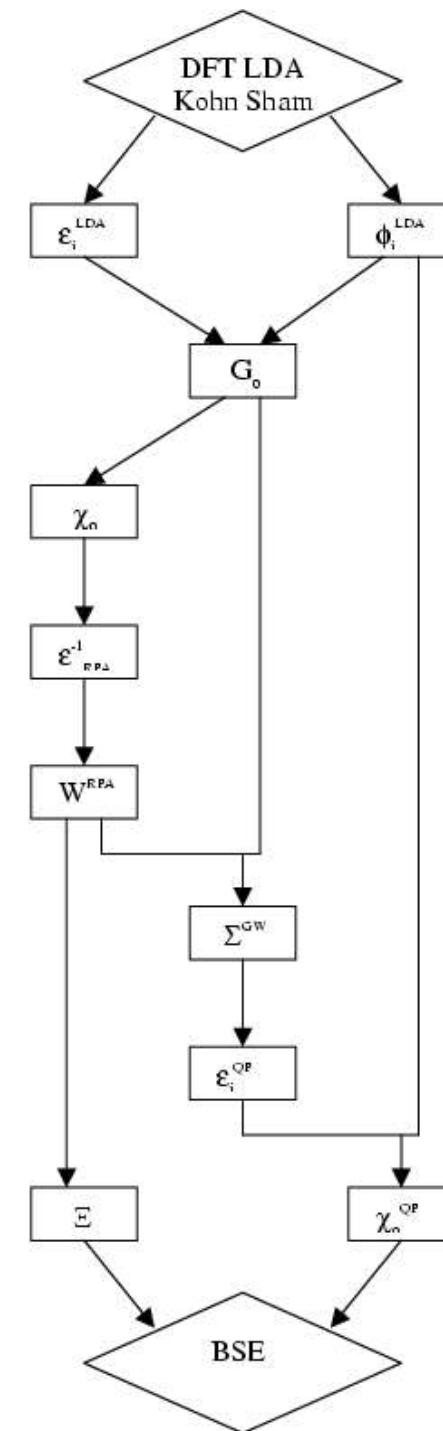
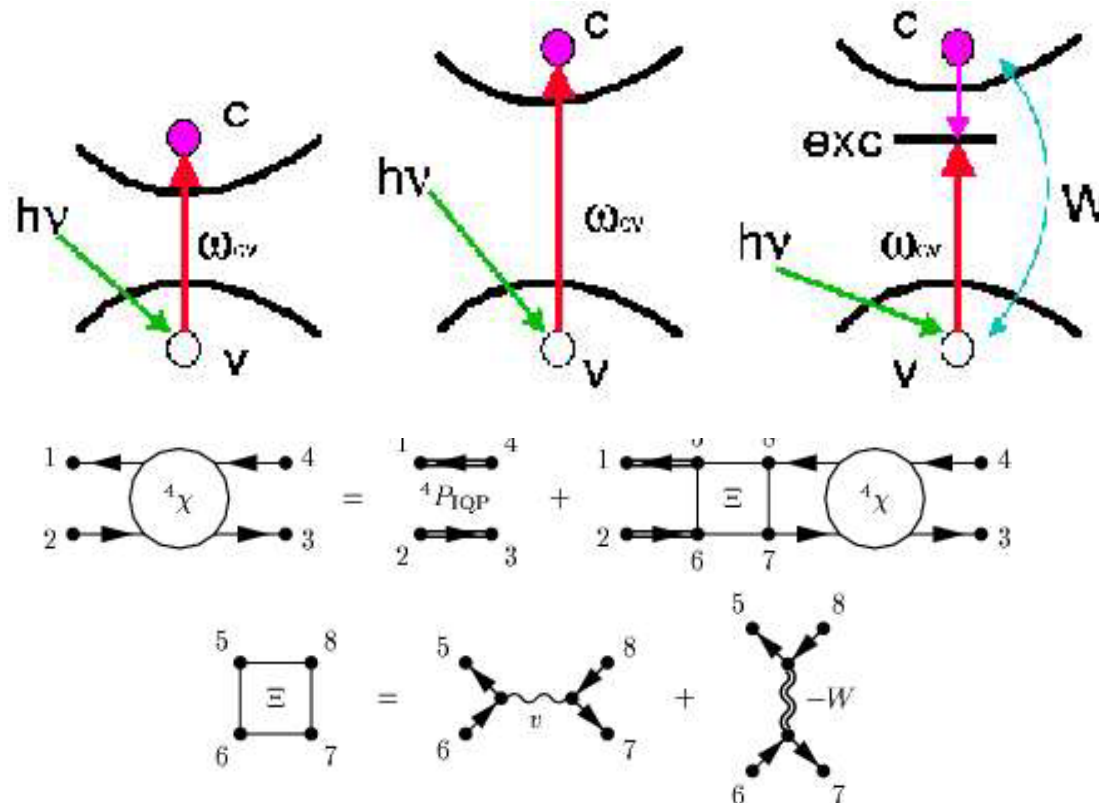
also available in preprint form at <http://www.physics.ohio-state.edu/~wilkins/vita/publications.html#reviews>

# Bethe-Salpeter equation: excitonic effects

$$\Sigma = iG_0 W_0; W_0 = \epsilon_{RPA}^{-1} V$$

$$\epsilon_{RPA} = 1 - v_c \chi^{(0)}$$

$$\chi^{(0)}(r, r', \omega) = 2 \sum_{i \neq j} (f_i - f_j) \frac{\phi_i(r) \phi_j(r) \phi_i^*(r') \phi_j(r')}{\epsilon_i - \epsilon_j - \omega - i\eta}$$



# TDDFT ...

$$t \left( \tilde{P}_{G_1 G_2}(t) \right) = \text{bubble}(\tilde{P}_{G_1, G_2}^0(t)) + \text{bubble}(\tilde{P}_{G_1, G_3}^0(t - t_1)) \text{ circle}(f_{G_3, G_4}^{xc}(t_1 - t_2)) \text{ rectangle}(\tilde{P}_{G_4 G_2}(t_2))$$

$$\iint d\mathbf{r}_2 d\mathbf{r}_3 \chi_s(\mathbf{r}_1, \mathbf{r}_2; \omega) \left[ \frac{1}{|\mathbf{r}_1 - \mathbf{r}_2|} + f^{xc}(\mathbf{r}_2, \mathbf{r}_3; \omega) \right] \xi(\mathbf{r}_3; \omega) = \lambda(\omega) \xi(\mathbf{r}_1; \omega) \quad \lambda(E_\lambda) = 1$$

$$t \left( \tilde{L}_{K_1 K_2}(t) \right) = \text{bubble}(\tilde{L}_{K_1}^0(t) \delta_{K_1 K_2}) + \sum_{K_3} i \int dt_1 \text{ wavy}(i \int dt_1) \text{ rectangle}(\tilde{L}_{K_3 K_2}(t_1)) \quad K_1 \equiv \{c_1, v_1, \mathbf{k}_1\}$$

$$\tilde{P}_{G_1, G_2}(\omega) \propto \sum_{K_1, K_2} \Phi_{K_1}^*(G_1) L_{K_1, K_2}(\omega) \Phi_{K_2}(G_2) \quad \Phi_{K_1}(G_1) = \langle c_1 \mathbf{k}_1 | e^{G_1 \cdot \mathbf{r}} | v_1 \mathbf{k}_1 \rangle$$

$$\tilde{P}_{G_1, G_2}(\omega) \propto \sum_{\lambda} \frac{\Phi_{\lambda}^*(G_1) \Phi_{\lambda}(G_2)}{\omega - E_{\lambda}} \quad H|\lambda\rangle = E_{\lambda}|\lambda\rangle \quad H_{K_1, K_2} = (\epsilon_{c_1 \mathbf{k}_1} - \epsilon_{v_1 \mathbf{k}_1}) \delta_{K_1, K_2} + iW_{K_1, K_2}$$

... and Many-Body Perturbation Theory

# *Many-Body approach to the Exchange-Correlation Kernel of TDDFT*

A diagrammatic approach

## Hypothesis

It exists a "many-body xc-kernel" such that  
the TDDFT and Many-Body polarization  
functions are identical

*Consequently TDDFT equation can be used as an equation for the xc-kernel  
and as a formal solution can be found in terms of an iterative equation for  
the  $n$ th order contribution*



# Many-Body approach to the Exchange-Correlation Kernel of TDDFT

## TDDFT

$$\tilde{\mathbf{P}}(\mathbf{q}, \omega) = \mathbf{P}^{(0)}(\mathbf{q}, \omega) + \mathbf{P}^{(0)}(\mathbf{q}, \omega) \mathbf{f}_{xc}(\mathbf{q}, \omega) \tilde{\mathbf{P}}(\mathbf{q}, \omega)$$

$$\tilde{P}_{\mathbf{G}_1, \mathbf{G}_2}(\mathbf{q}, \omega) = \text{const.} \sum_{\mathbf{K}_1, \mathbf{K}_2} \Phi_{\mathbf{K}_1}^*(\mathbf{q}, \mathbf{G}_1) \tilde{S}_{\mathbf{K}_1, \mathbf{K}_2}(\mathbf{q}, \omega) \Phi_{\mathbf{K}_2}(\mathbf{q}, \mathbf{G}_2)$$

## MBPT

$$\tilde{\mathbf{S}}(\mathbf{q}, \omega) = \mathbf{S}^{(0)}(\mathbf{q}, \omega) + \mathbf{S}^{(0)}(\mathbf{q}, \omega) \mathbf{W}(\mathbf{q}) \tilde{\mathbf{S}}(\mathbf{q}, \omega)$$

$$\Phi_{\mathbf{K}}(\mathbf{q}, \mathbf{G}) = \langle c\mathbf{k} | e^{i(\mathbf{q}+\mathbf{G})\cdot\mathbf{r}} | v\mathbf{k} - \mathbf{q} \rangle \quad \mathbf{K} := (c v \mathbf{k})$$

*Bethe-Salpeter Equation*

$$\mathbf{f}_{xc}^{(n)}(\mathbf{q}, \omega) = \frac{1}{\mathbf{P}^{(0)}(\mathbf{q}, \omega)} \left[ \delta \tilde{\mathbf{P}}^{(n)}(\mathbf{q}, \omega) \left( \mathbf{P}^{(0)}(\mathbf{q}, \omega) \right)^{-1} - \sum_{m=1, n-1} (-1)^m \delta \tilde{\mathbf{P}}^{(m)}(\mathbf{q}, \omega) \mathbf{f}_{xc}^{(n-m)}(\mathbf{q}, \omega) \right]$$

$$\mathbf{f}_{xc}(\mathbf{q}, \omega) = \sum_n \mathbf{f}_{xc}^{(n)}(\mathbf{q}, \omega) \quad \mathbf{f}_{xc}^{(0)}(\mathbf{q}, \omega) = 0$$

*Iterative equation for  $f_{xc}$*

*A. Marini, R. Del Sole and AR, PRL (2003)*

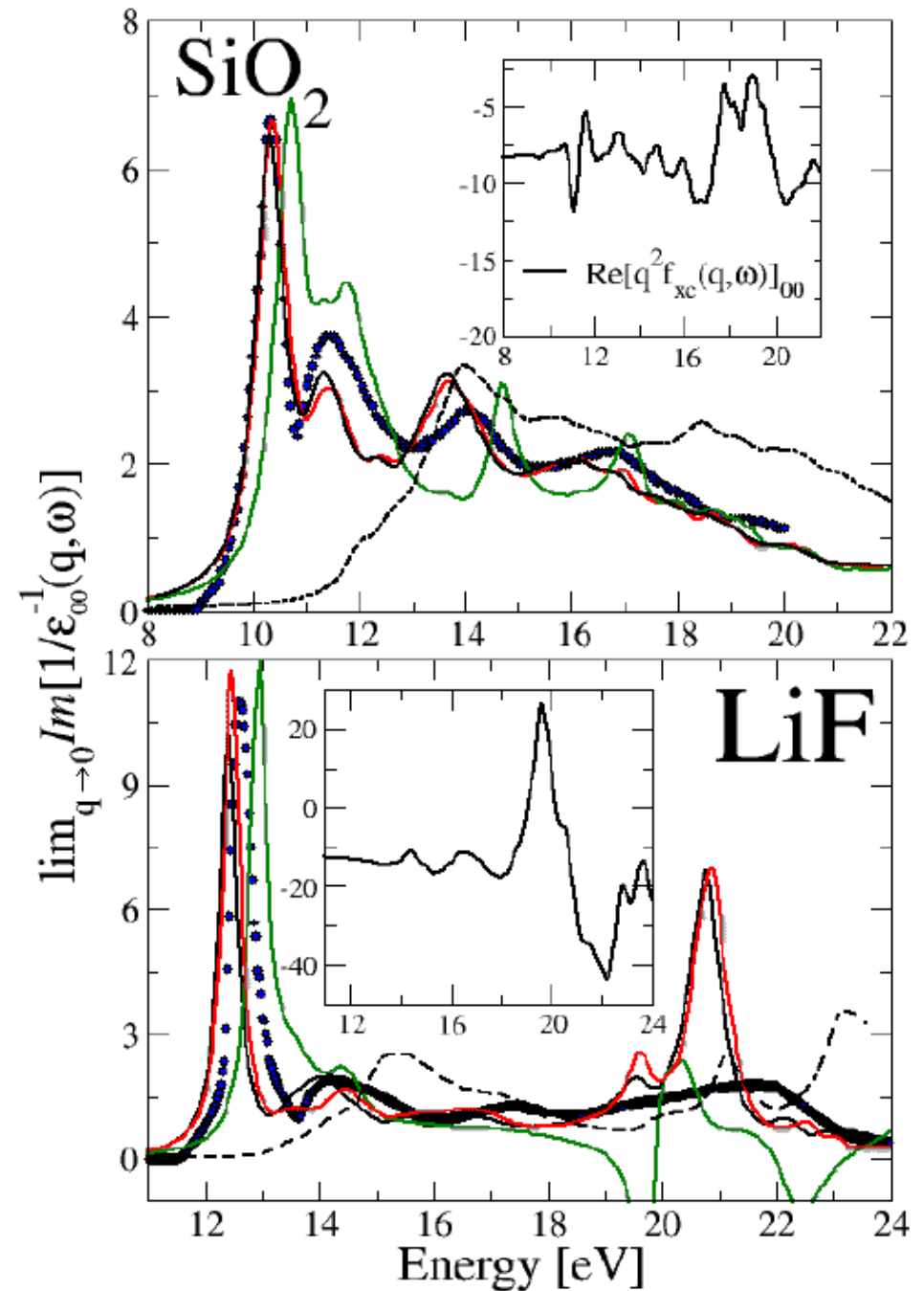
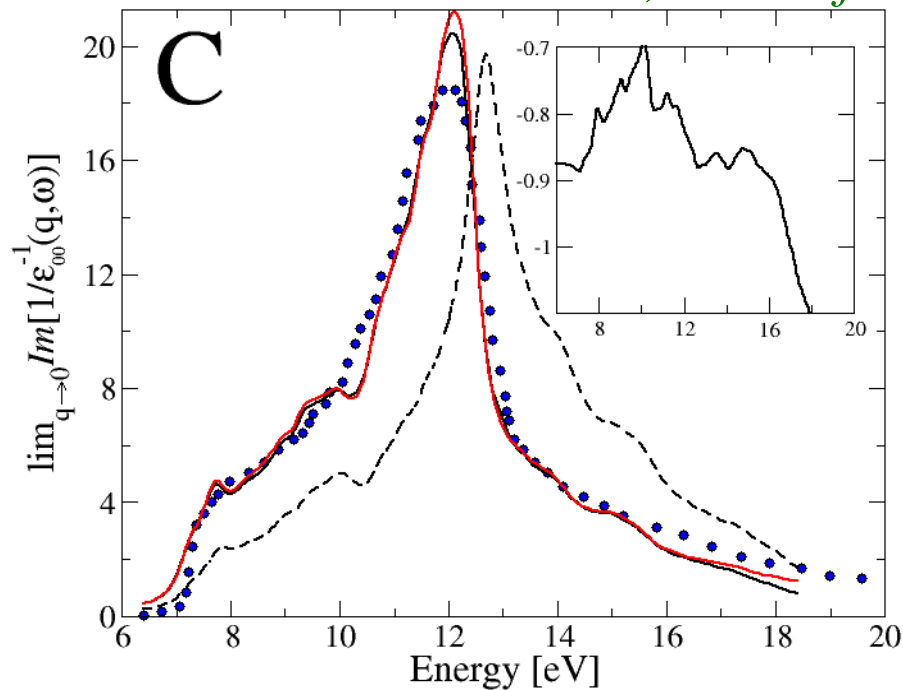


# Bound excitons in TDDFT

$$f_{xc}^{(1)}(\mathbf{q}, \omega) = \text{diagram}$$

$$\text{wavy line} := [\mathbf{P}^{(0)}(\omega)]^{-1}$$

— *TDDFT*    ●●● *Experiment*  
— *BSE*    — *TDDFT, scalar f<sub>xc</sub>*



*A. Marini, R. Del Sole and AR, PRL (2003)*

# How many terms ?

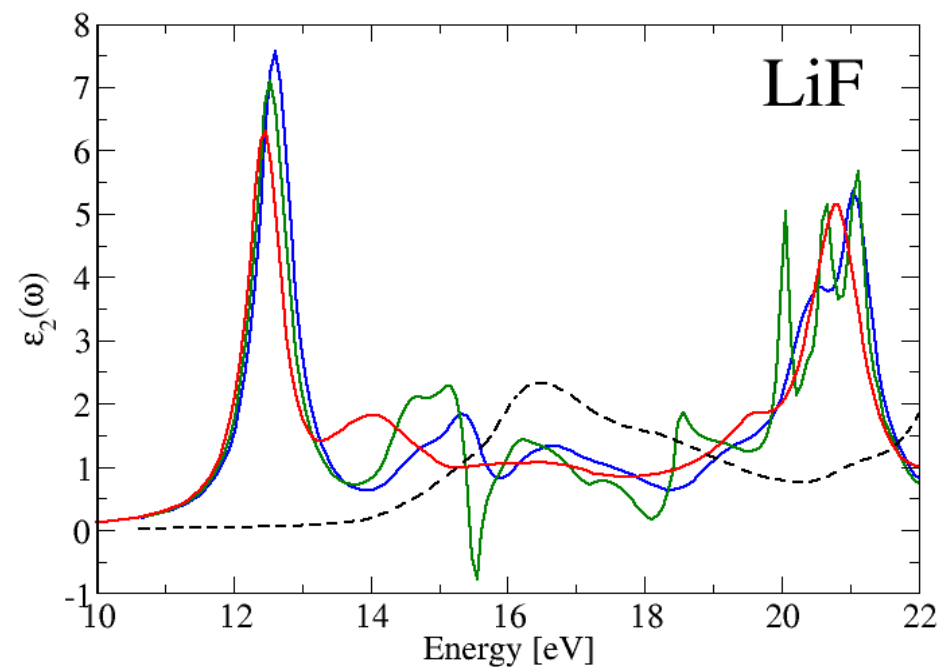
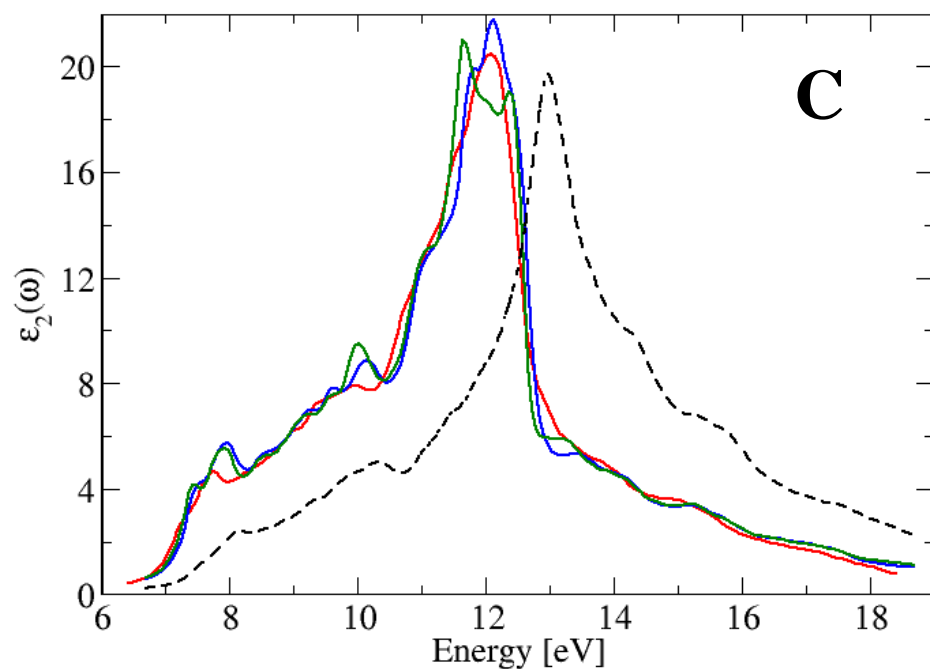
$$\mathbf{f}_{xc}^{(1)}(\mathbf{q}, \omega) = \text{diagram}$$

$$\mathbf{f}_{xc}^{(2)}(\mathbf{q}, \omega) = \text{diagram} - \text{diagram}$$

$$\mathbf{f}_{xc}^{(3)}(\mathbf{q}, \omega) = \text{diagram} + \text{diagram} - 2 \text{diagram}$$

$$\text{wavy line} := [\mathbf{P}^{(0)}(\omega)]^{-1}$$

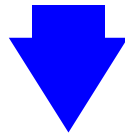
— *BSE*      - - - *QP-RPA*



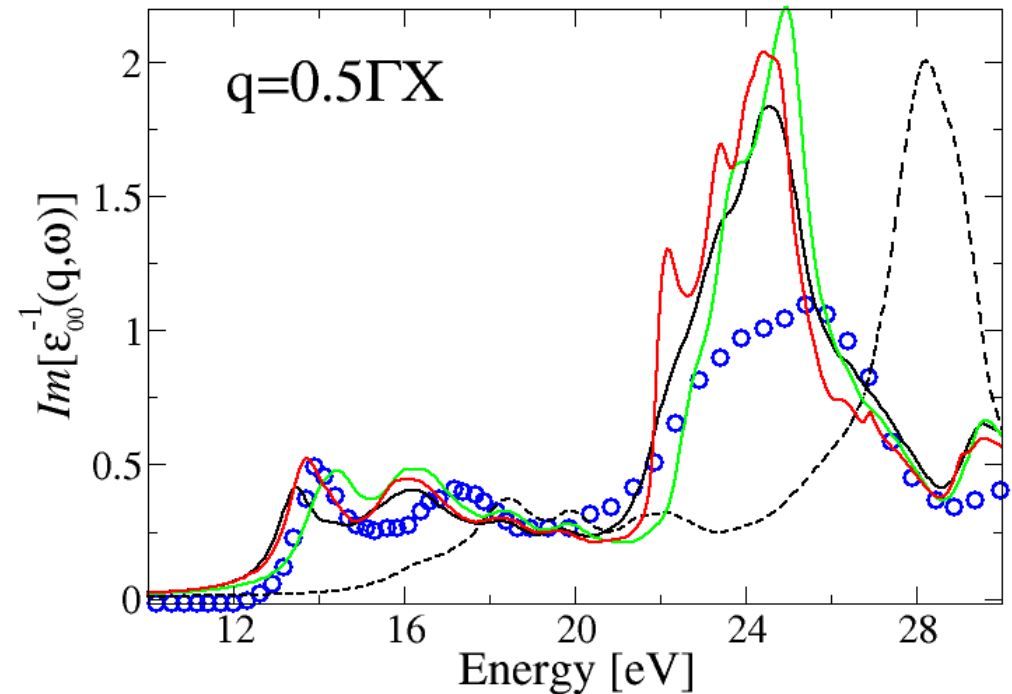
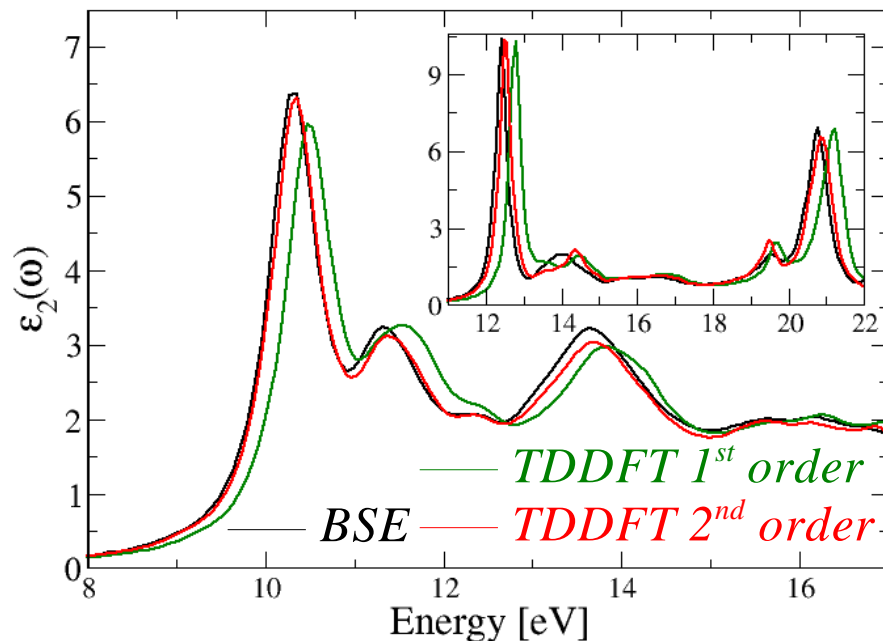
# A many-body causal TDDFT kernel

$$\mathbf{f}_{xc}^{(n)}(\mathbf{q}, \omega) = \frac{1}{\mathbf{P}^{(0)}(\mathbf{q}, \omega)} \left[ \delta \tilde{\mathbf{P}}^{(n)}(\mathbf{q}, \omega) \left( \mathbf{P}^{(0)}(\mathbf{q}, \omega) \right)^{-1} - \sum_{m=1, n-1} (-1)^m \delta \tilde{\mathbf{P}}^{(m)}(\mathbf{q}, \omega) \mathbf{f}_{xc}^{(n-m)}(\mathbf{q}, \omega) \right]$$

*Causal/T-ordered*



*Causal/T-ordered  $f_{xc}$*



● Same agreement between BSE and TDDFT for the finite transferred momentum absorption spectra...

● ...and for the off-diagonal elements of the microscopic dielectric function

# Low dimensional systems (1D): polyacetylene

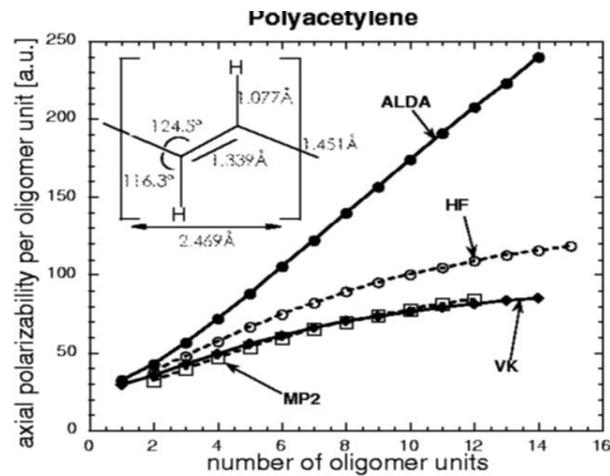


FIG. 1. ALDA and VK static axial polarizability of polyacetylene compared with restricted Hartree-Fock [18] and MP2 [22] results.

M. van Faassen et al. PRL **88** 186401 (2002)

## Electric field dependence of the XC Potential in Molecular Chains

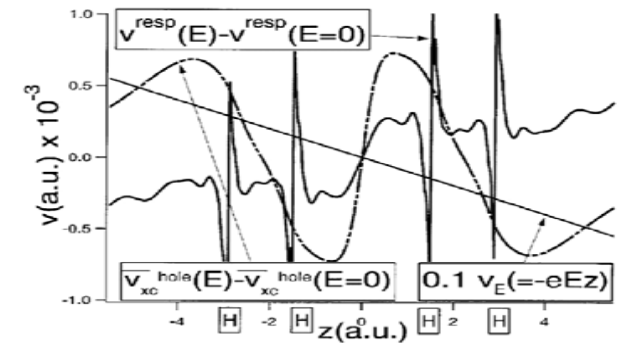


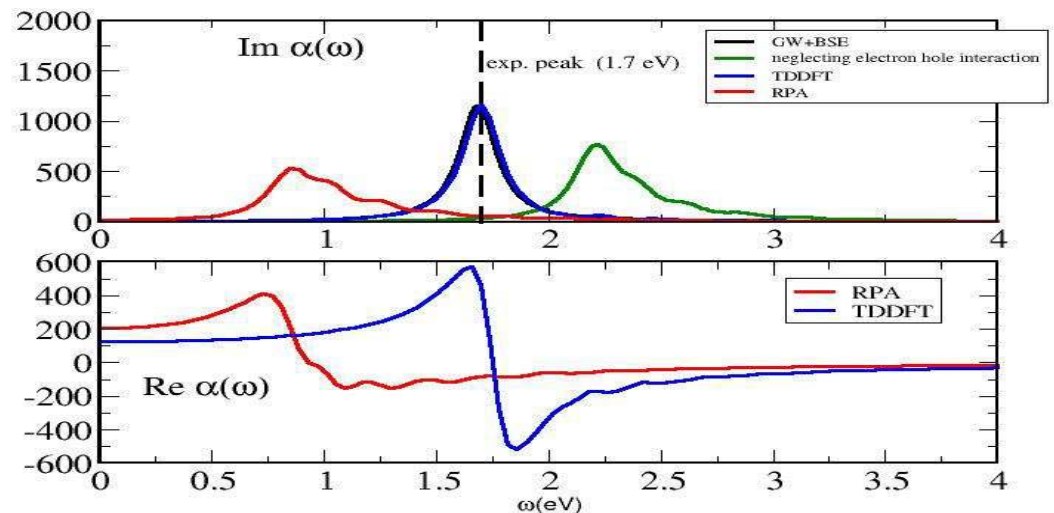
FIG. 2. Changes, due to an electric field of 0.001 a.u. in response and hole potentials for H<sub>2</sub>-H<sub>2</sub>, constructed from multireference CI singles doubles density with a large (cc-pV6Z without *d* and *f* functions) basis set, compared to the applied field (potential  $v_E$ ).

S.J.A. Van Gisbergen PRL **83** 694 (1999)

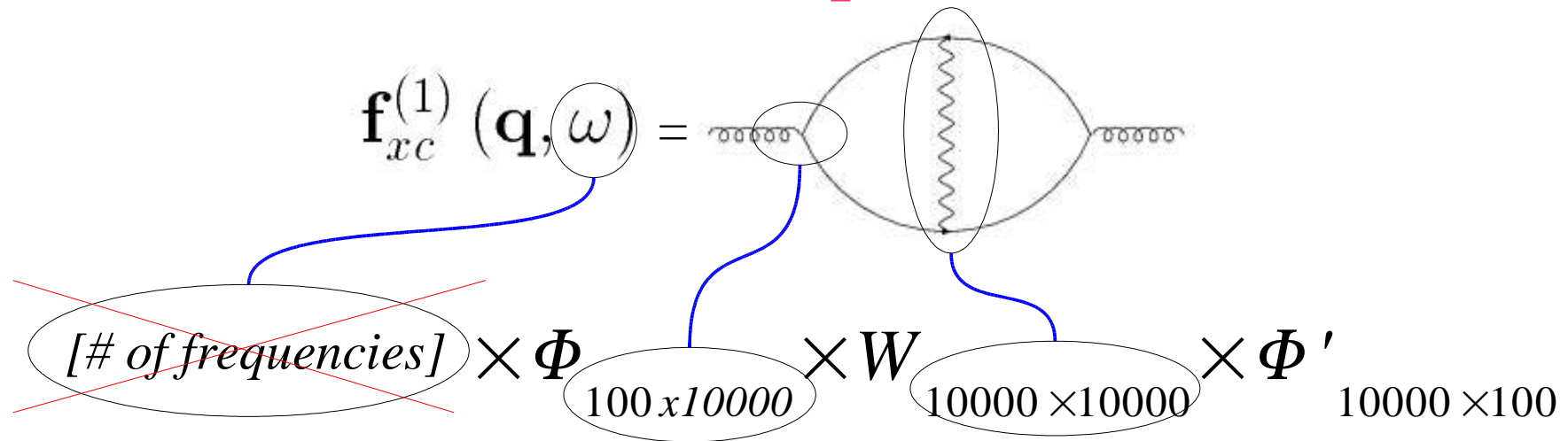
*In LDA and GGA xc potential lack of a term counteracting the applied electric field*

$$f_{xc}^{BSE}(r, r', \omega)$$

*Isolated infinite Polyacetylene chain*



# Is TDDFT "fast" compared to the BSE ?



$$\mathbf{f}_{xc}^{(1)}(\mathbf{q}, \omega) = \frac{2}{\Omega N_k} \left[ \mathbf{P}^{(0)}(\mathbf{q}, \omega - \Delta_{\mathbf{q}}) \right]^{-1} \sum_{\mathbf{K}} \left[ \frac{\mathbf{R}_{\mathbf{K}}^{(\mathbf{q})} + \mathbf{R}_{\mathbf{K}}^{(\mathbf{q})\dagger}}{\omega - E_{\mathbf{K}}^{(\mathbf{q})} - \Delta_{\mathbf{q}} + i0^+} + \frac{\mathbf{Q}_{\mathbf{K}}^{(\mathbf{q})}}{(\omega - E_{\mathbf{K}}^{(\mathbf{q})} - \Delta_{\mathbf{q}} + i0^+)^2} \right] \left[ \mathbf{P}^{(0)}(\mathbf{q}, \omega - \Delta_{\mathbf{q}}) \right]^{-1}$$

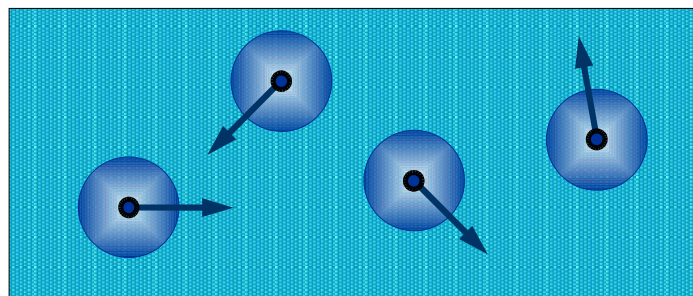
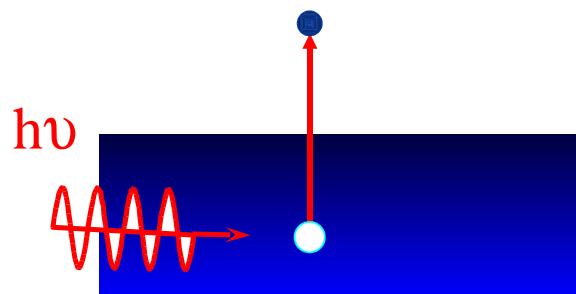
$$\left[ R_{\mathbf{K}}^{(\mathbf{q})} \right]_{\mathbf{G}_1, \mathbf{G}_2} = \sum_{\mathbf{K}', E_{\mathbf{K}'}^{(\mathbf{q})} \neq E_{\mathbf{K}}^{(\mathbf{q})}} \frac{\Phi_{\mathbf{K}}^*(\mathbf{q}, \mathbf{G}_1) W_{\mathbf{K}, \mathbf{K}'}(\mathbf{q}) \Phi_{\mathbf{K}'}(\mathbf{q}, \mathbf{G}_2)}{E_{\mathbf{K}}^{(\mathbf{q})} - E_{\mathbf{K}'}^{(\mathbf{q})}} \quad \left[ Q_{\mathbf{K}}^{(\mathbf{q})} \right]_{\mathbf{G}_1, \mathbf{G}_2} = \sum_{\mathbf{K}', E_{\mathbf{K}'}^{(\mathbf{q})} = E_{\mathbf{K}}^{(\mathbf{q})}} \Phi_{\mathbf{K}}^*(\mathbf{q}, \mathbf{G}_1) W_{\mathbf{K}, \mathbf{K}'}(\mathbf{q}) \Phi_{\mathbf{K}'}(\mathbf{q}, \mathbf{G}_2)$$

- When the only optical spectra is calculated TDDFT is as time consuming as BSE...
- ...but when the full dielectric matrix is needed TDDFT is more favorable than BSE

# What about the description of decaying quasiparticle processes within TDDFT?

*G. Onida, L. Reining and AR, Rev. Mod. Phys. 74, 601 (2002)*

## *Lifetime of quasiparticles*



interactions between quasiparticles limit how long the corresponding quantum states retain their identity, i.e., the **lifetime** of the excitation.

In combination with the velocity, this lifetime determines the **mean free path**, a measure of influence of the excitation

### **Importance of lifetime**

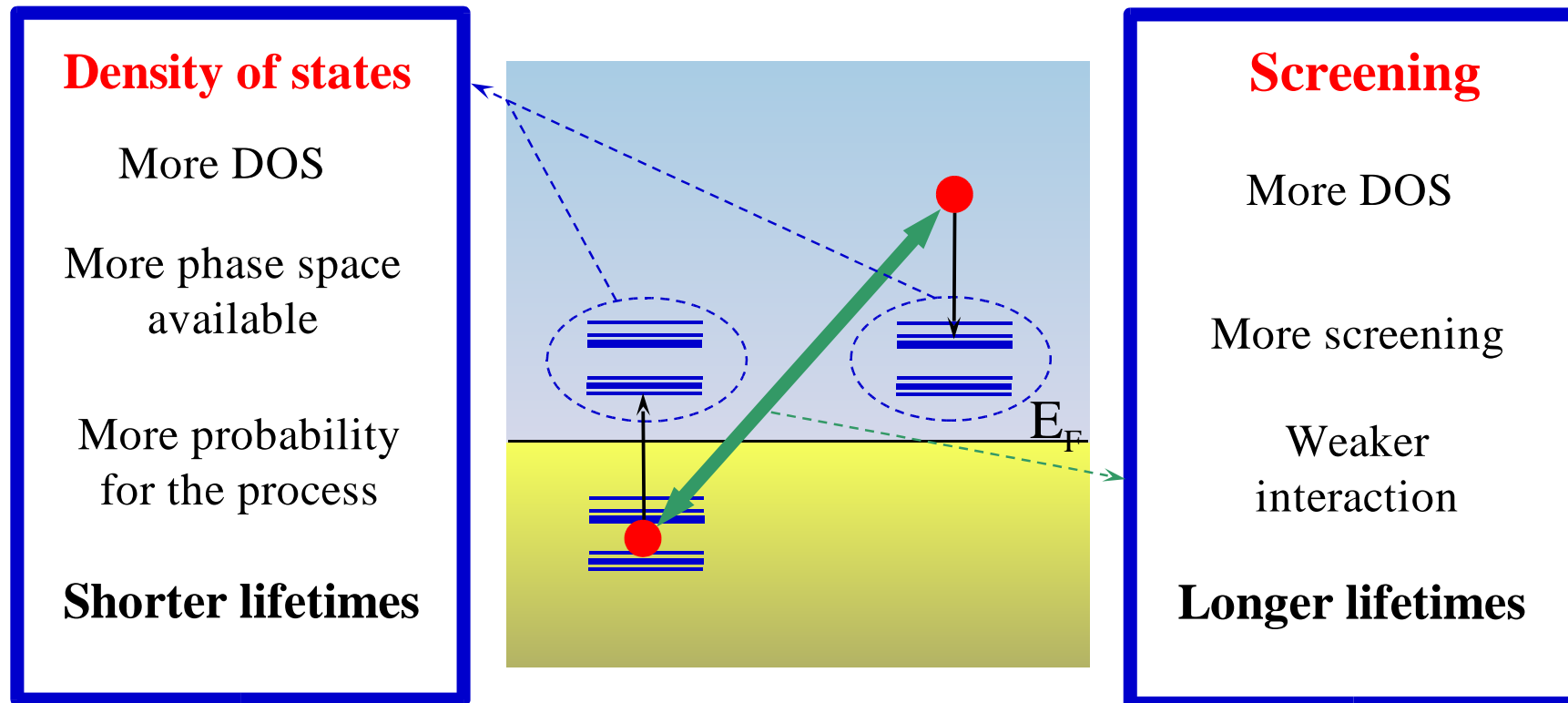
- screening in an electron gas
- surface photochemistry
- electron-phonon coupling
- electron transfer across interfaces
- localization
- electron dynamics and energy transfer



# PHYSICS OF LIFETIME

$$\tau^{-1} = 2 \sum \int d\mathbf{r} \int d\mathbf{r}' \phi_i^*(\mathbf{r}) \phi_f^*(\mathbf{r}') \text{Im} W(\mathbf{r}, \mathbf{r}'; \omega) \phi_i(\mathbf{r}') \phi_f(\mathbf{r})$$

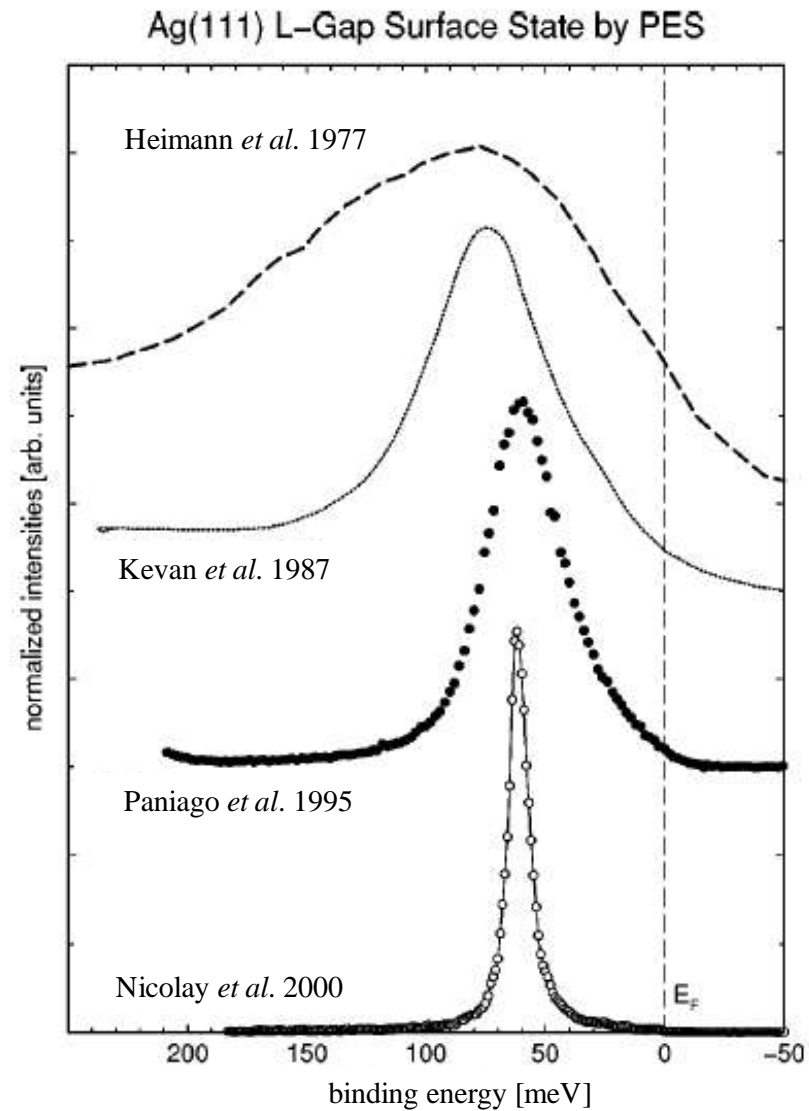
## Density of States (DOS) versus Screening



Free electrons  
**Quinn (1962)**

$$\tau \approx \frac{263 r_s^{-5/2}}{(E-E_F)^2} \propto \frac{n^{5/6}}{(E-E_F)^2}$$

Experimental lifetimes change quickly with time!



from F.Reinert *et al.*, PRB **63** (2001) 115415.

# The 2-point vertex function

Suppose to have a good approximation for the (TD)DFT *potential*...

$$\hat{H} = \int d\mathbf{x} \hat{\psi}^\dagger(\mathbf{x}) [h_0(\mathbf{x}) + v_{xc}(\mathbf{x})] \hat{\psi}(\mathbf{x}) + H_{interaction} - \int d\mathbf{x} \hat{\psi}^\dagger(\mathbf{x}) v_{xc}(\mathbf{x}) \hat{\psi}(\mathbf{x})$$

$$\chi(1, 2) = \tilde{\chi}(1, 2) + \int d34 \tilde{\chi}(1, 2) [v(3, 4) + f_{xc}(3, 4)] \chi(4, 2)$$

$$f_{xc}(1, 2) \equiv \delta v_{xc}(1) / \delta \rho(2)$$

$$\tilde{\Gamma}(1, 2; 3) = \delta(1, 2) \delta(2, 3) + \int d4567 \Xi(1, 5; 2, 4) G(4, 6) G(7, 5) \tilde{\Gamma}(6, 7; 3)$$

$$\Xi(1, 4; 2, 3) \approx W(1, 2) \delta(1, 3) \delta(2, 4) - f_{xc}(1, 3) \delta(1, 2) \delta(3, 4)$$

$$\Sigma_{G_0 W_0} \rightarrow i \int d3 W^{TDDFT}(1^+, 3) \tilde{\Gamma}_{loc}(3, 2) G(1, 2) \quad \tilde{\Gamma}_{loc}(1, 2) = \int d3 \chi_0^{-1}(1, 3) \tilde{\chi}(3, 2)$$

No difference with GoWo using ALDA or similar approaches

PRL 62, 2718 (1989); PRB 49, 8024 (1994); PRB 56, 12832 (1997).

**BUT IS**  $\tilde{\Gamma}(1, 2; 3) = \delta(1, 2) \delta(2, 3) + \tilde{\Gamma}_3(1, 2; 3) - \tilde{\Gamma}_{loc}(1, 3) \delta(1, 2) \sim \delta(1, 2) \delta(2, 3) ?$

● PRL 91, 056402 (2003); PRL 91, 256402 (2003). PRL 88, 066404 (2002) etc etc

# The 3-point vertex function

$$\mathbf{f}_{xc}^{(1)}(\mathbf{q}, \omega) = \text{diagram} \quad \text{diagram} := [\chi_0(\omega)]^{-1}$$

$$\tilde{\chi}(1, 2) = \chi_0(1, 2) + \int d34 \chi_0(1, 3) \text{diagram} \tilde{\chi}(4, 2) = -i \int d34 G(1, 3) G(4, 1) \tilde{\Gamma}_{TDDFT}^{(1)}(3, 4; 2)$$

If

$$\tilde{\Gamma}_{TDDFT}^{(1)}(1, 2; 3) \equiv \delta(1, 2) \delta(2, 3) + i W_0(1, 2) \int d4 G_0(1, 4) G_0(4, 2) \tilde{\Gamma}_{loc}(4, 3)$$

$$\tilde{\Gamma}_{TDDFT}^{(1)}(1, 2; 3) \equiv \delta(1, 2) \delta(2, 3) + i \text{diagram} \tilde{\chi}(4, 3)$$

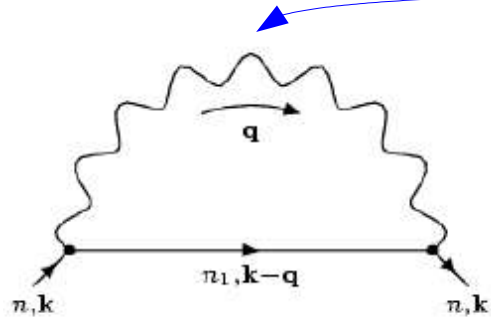
Closed expression for the "on mass-shell" electronic lifetime

$$\tau_{ck}^{-1} = \tau_{ck,0}^{-1} + \Delta\tau_{ck}^{-1}$$

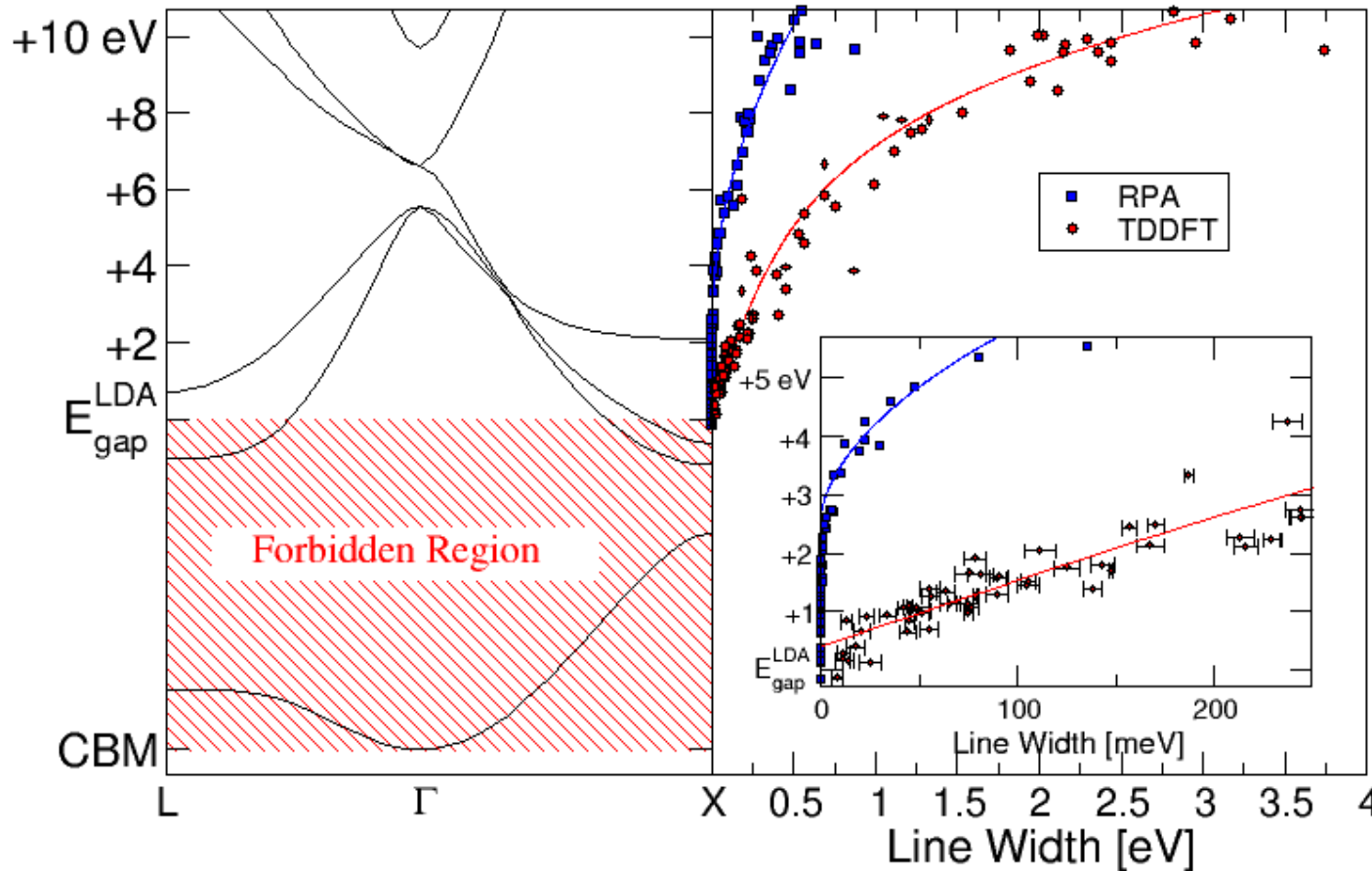
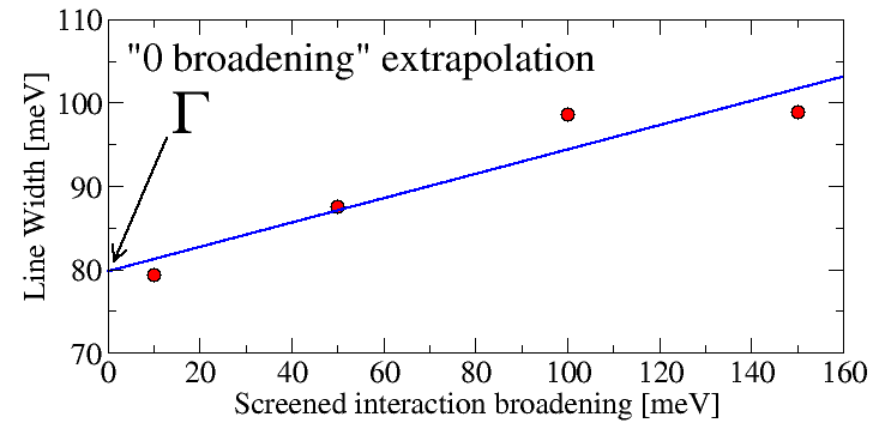
$$\tau_{ck,0}^{-1} = -2\Omega^{-1} \sum_{\mathbf{G}_1, \mathbf{G}_2} \sum_{\mathbf{q}, c'} \rho_{cc'}(\mathbf{kqG}_1) \rho_{cc'}^*(\mathbf{kqG}_2) \text{Im} [W_{\mathbf{G}_1 \mathbf{G}_2}^{TDDFT}(\mathbf{q}, \epsilon_{c\mathbf{k}} - \epsilon_{c'\mathbf{k}-\mathbf{q}})] ,$$

$$\Delta\tau_{ck,0}^{-1} = -2\Omega^{-1} \sum_{\mathbf{G}_1, \mathbf{G}_2} \sum_{\mathbf{q}, c'} \text{Re} [(\Gamma_{cc'}^{cv}(\mathbf{kqG}_1) + \Gamma_{cc'}^{vc}(\mathbf{kqG}_1)) \rho_{cc'}^*(\mathbf{kqG}_2)] \text{Im} [W_{\mathbf{G}_1 \mathbf{G}_2}^{TDDFT}(\mathbf{q}, \epsilon_{c\mathbf{k}} - \epsilon_{c'\mathbf{k}-\mathbf{q}})]$$

# Excitonic effects (via TDDFT) on the lifetimes of LiF



- 10'000x10'000 BS kernel
- Up to 200 G-vectors dielectric function, 256 Q-points in the whole BZ
- Small broadening stability



- Linear behaviour
- Small penetration of the RPA "forbidden region"
- The  $f_{xc}$  kernel remains stable and robust even with a 10 meV broadening and energies up to 20 eV
- A BS-based calculation is, in this case, **enormously less convenient** than using TDDFT

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***It is one of the first duties of a professor, in any subject,  
to exaggerate a little both the importance of his subject and his  
own importance in it.***

**G.H. Hardy (A Mathematician's Apology)**

**Thank you**

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