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**CONFERENCE ON FUNDAMENTAL SYMMETRIES  
AND FUNDAMENTAL CONSTANTS**

**15 - 18 September 2004**

**ATOMIC CLOCK TESTS OF LORENTZ AND CPT SYMMETRY**

**R. Walsworth  
Harvard, USA**

# Atomic clock tests of Lorentz and CPT symmetry

Ronald Walsworth

*Harvard-Smithsonian Center for Astrophysics*



## In this talk...

- An atomic physics experimentalist's view of the rationale for Lorentz and CPT symmetry tests
- What are the observable phenomena and experimental challenges?
- An incomplete survey of Lorentz/CPT tests to date:  
*some have (naive) Planck-scale sensitivity*
- A look at my group's maser (atomic clock) experiments  
*best limits so far for neutron and proton*
- Coming attractions, challenges, and provocative comments...

## Motivation and context

- Fundamental extended objects, cosmological dynamics  
→ low-energy violation of Lorentz (and hence CPT) symmetry
- Atomic clock comparisons are particularly sensitive to (small) Lorentz and CPT violations  
*sensitivity for spin couplings  $\sim 10^{-31}$  GeV*  
*2 orders of magnitude improvement in next few years*
- Standard Model Extension of Kostelecky et al. is the comprehensive formalism to interpret experiments

**Fundamental theory  
at Planck scale**

18 orders of magnitude...  
Spontaneous Lorentz symmetry breaking...

**Standard Model Extension**

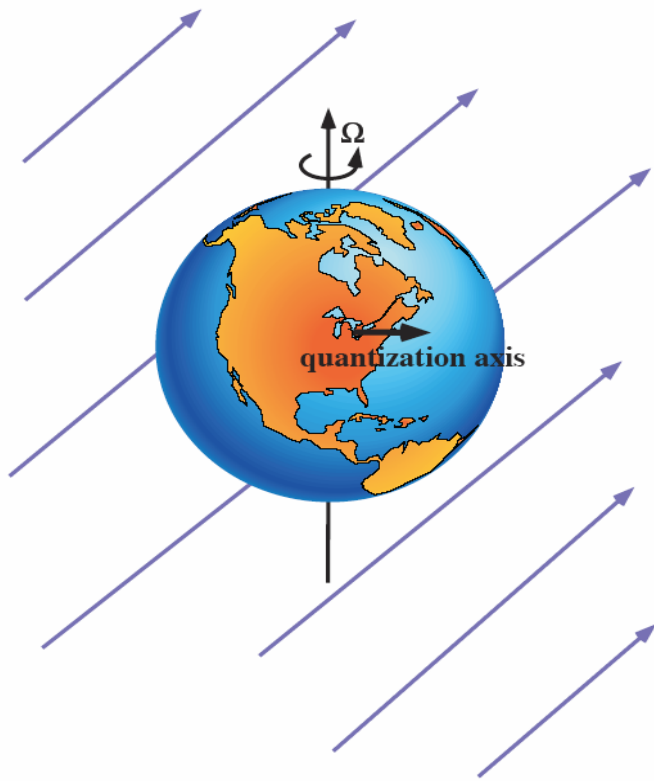
Kostelecky et al.

**QCD extension**  
meson effects

**Atoms, nuclei, etc.**  
clock comparisons

**QED extension**  
optical cavity tests

# Implications of Lorentz-violation for "low energy" physics



*Spins, mesons, photons, etc.  
can couple (perhaps differently)  
to background fields*

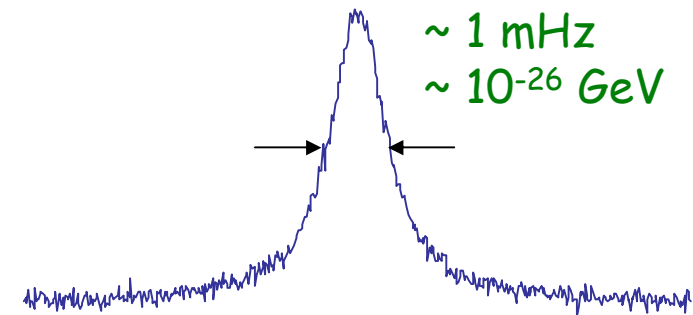
- > orientation and boost dependent
- Zeeman splittings
  - meson decays
  - speed of light
  - birefringence of vacuum  
etc.

## Experimental challenges

- Small effects !!
  - need a narrow bandwidth observable,  
high-sensitivity detection (good S/N)
- Slowly-modulated signal (if using Earth's rotation)
  - excellent long-term stability of apparatus
- Discrimination from confounding systematic effects
  - good co-magnetometer (spins have magnetic moments)*
  - day/night thermal cycle (if using Earth's rotation)*
  - noise associated with a rotating platform*
  - variations in matter/antimatter loadings (meson sector)*
  - unknown astrophysical effects (photon sector)*

## What makes a good spin Lorentz symmetry test?

- *Clean*: simple spin structure (e.g.,  $^3\text{He}$ , H)
- *Sensitive to absolute energy changes*:  
Narrow bandwidth resonance  
Large signal-to-noise ratio  
Stable over sidereal modulation period
- *Suppress magnetic field effects*:  
E.g., co-magnetometer that does not eliminate Lorentz-violation sensitivity
- *Minimize systematics*:  
Differential measurements, environmental control, etc.



Hydrogen and noble gas masers meet criteria



# Current limits

## ***Lorentz symmetry tests (CPT odd and even effects)***

## ***CPT tests***

### System

<u>Isotropy</u>	<u>Boosts</u>		<u>Isotropy</u>	<u>Boosts</u>
$10^{-24}$ GeV (Penning trap)		$e^-$	$10^{-25}$ GeV ( $e^+/e^-$ in Penning trap)	
$10^{-29}$ GeV (torsion pendulum)				
$10^{-23}$ GeV (muonium, $\mu^+e^-$ )		$\mu$	$10^{-22}$ GeV ( $\mu^+/\mu^-$ at CERN)	
$10^{-24}$ GeV?? (BNL storage ring)			$10^{-23}$ GeV?? (BNL storage ring)	
$10^{-27}$ GeV (hydrogen maser)		$p$		
$10^{-31}$ GeV	$10^{-27}$ GeV	$n$		
(noble gas maser)				

***Lorentz symmetry tests  
(CPT odd and even effects)***

***CPT tests***

Isotropy

Boosts

**System**

Isotropy

Boosts

**D meson**

$10^{-13} \text{ GeV}$

$10^{-13} \text{ GeV}$

(FOCUS)

**K meson**

$10^{-21} \text{ GeV}$

(KTeV)

**B meson**

$10^{-16} \text{ GeV}$

(BaBAR)

$10^{-15}$

(cryogenic optical  
cavities)

$10^{-11}$

**speed of light**

$10^{-42} \text{ GeV}$  limit from  
cosmological data;

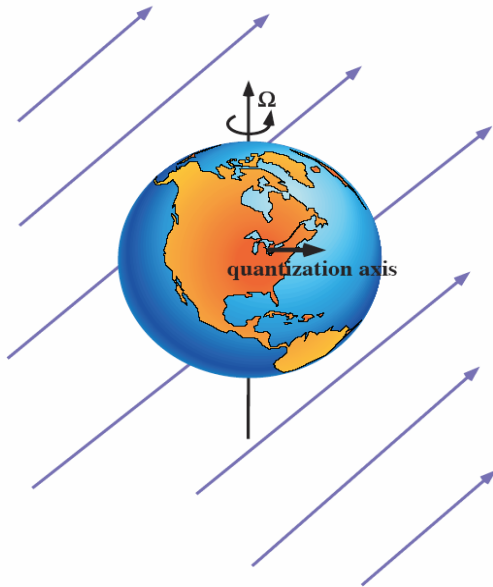
$10^{-32}$

(spectral polarimetry  
of cosmological sources)

**birefringence  
of vacuum**

strong arguments =>  
must be zero

# Search for Lorentz-violating coupling of spins to background fields



*Rotations: sidereal day modulation of atomic Zeeman splittings?*

*Boosts: sidereal year modulation of atomic Zeeman splittings?*

## Assumptions

- Simple, additive effect of coupling to valence nucleon and electron spins
- Couplings do not scale with magnetic moments
- Large domain size for Lorentz-violating fields
- Conventional magnetic shields do not screen Lorentz-violating fields
- Interpret results in terms of Standard Model Extension of Kostelecky et al.

Hydrogen maser

Hydrogen masers are one of the most stable oscillators for periods of seconds to weeks:

$$\Delta f/f \sim 10^{-15}$$



CfA hydrogen masers are used throughout the world for spacecraft tracking, radio astronomy, atomic physics, etc.

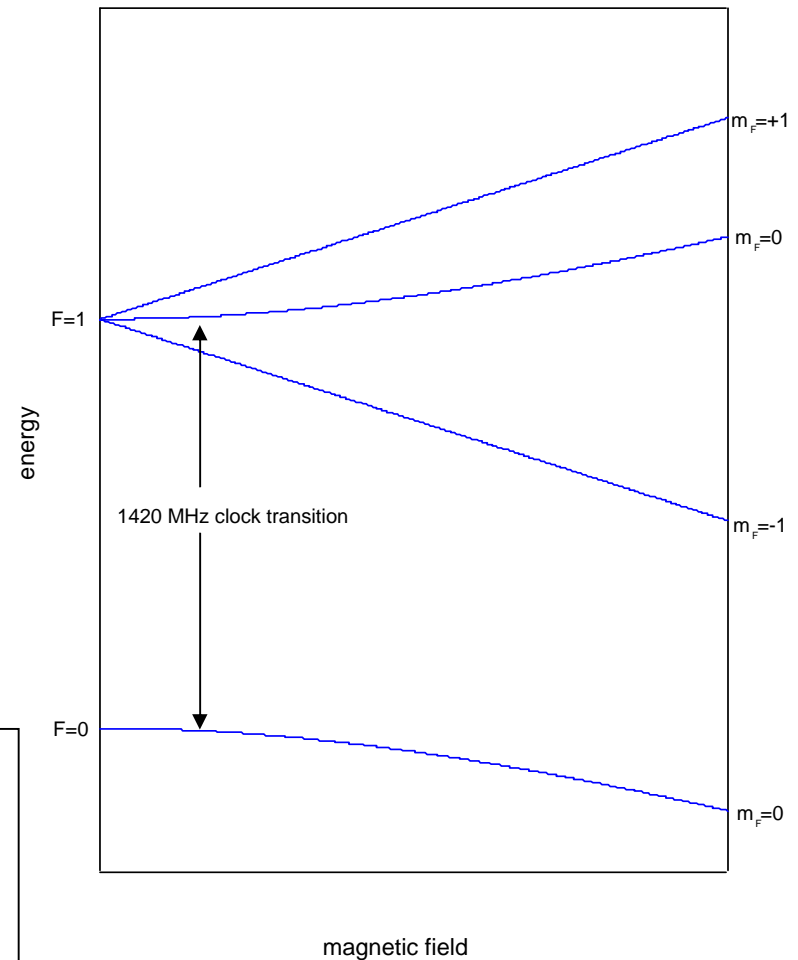
# Test of Lorentz symmetry with H maser

*Search for sidereal variations  
in difference of Zeeman and  
maser frequencies*

- Zeeman transition:  
leading order dependence  
on Lorentz-violating couplings  
to electron and proton spins
- Maser clock transition:  
no leading order Lorentz-  
violating effects

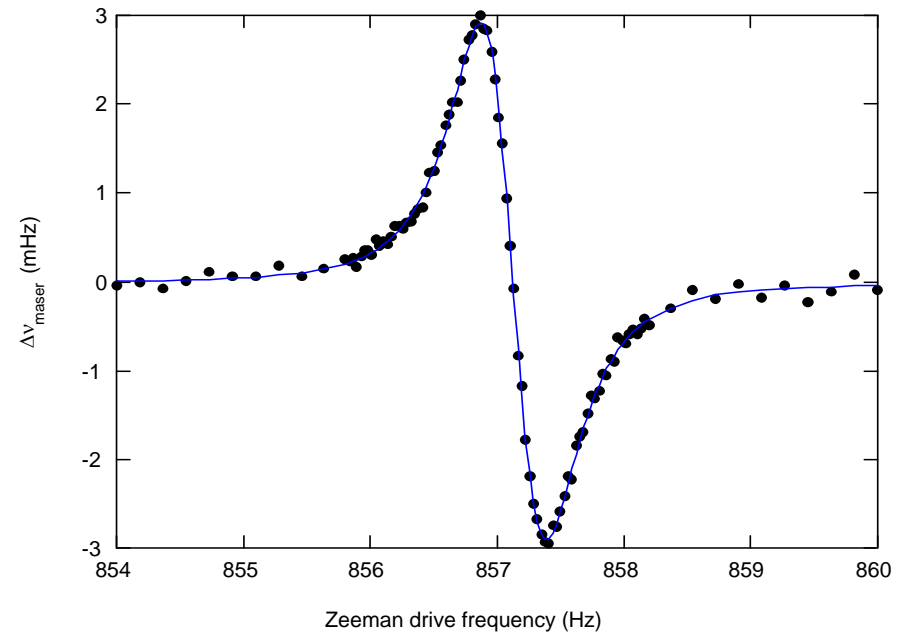
Zeeman frequencies  
 $\sim 700 \text{ Hz} \sim 0.5 \text{ mG}$

Differential splitting  
between two Zeeman  
transitions  $< 1 \text{ mHz}$

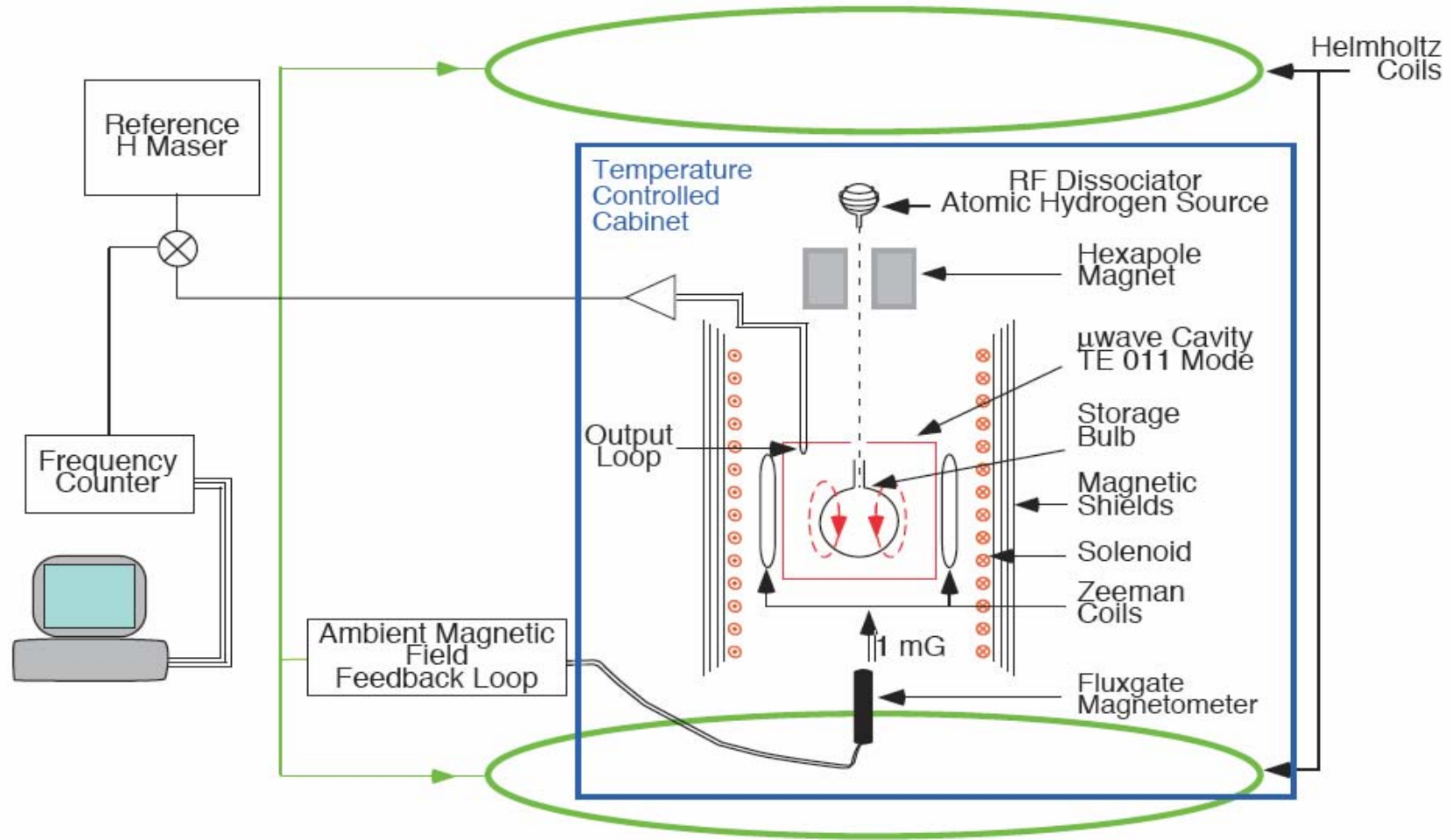


## Zeeman frequency measured with a double-resonance technique (Andresen effect)

- Very weak Zeeman excitation pulls maser frequency observably with negligible change in state populations
- Zeeman frequency resolution  $\sim 1$  mHz in single sweep of resonance
- Maser and Zeeman frequency measurements alternated continuously over many days

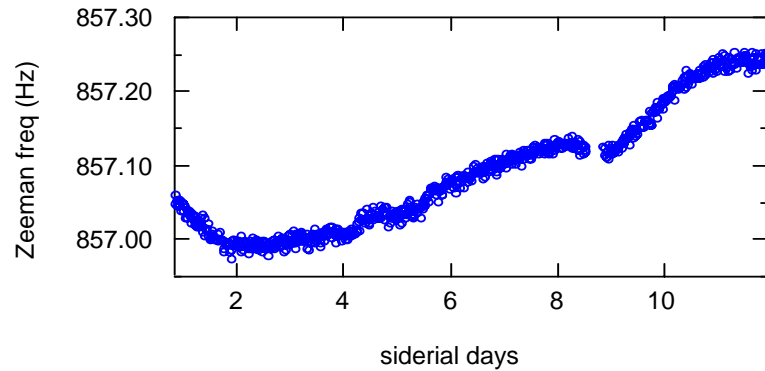


# Experiment schematic



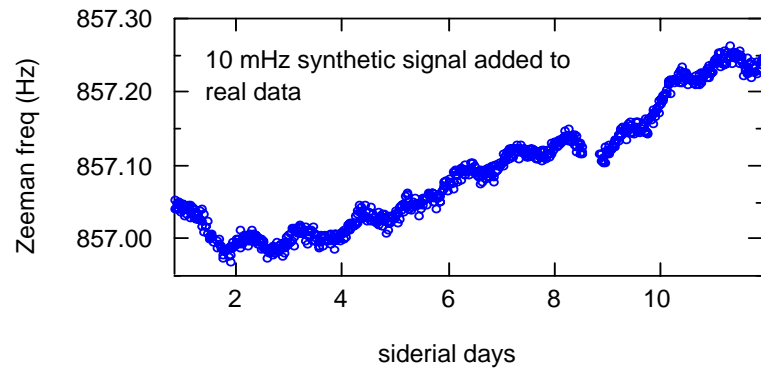


# Example hydrogen Zeeman frequency data



*Fit model includes:*

- *piecewise linear function to account for frequency drift (slope varied for each day)*
- *sinusoid with sidereal period*



*10 mHz faux sidereal modulation  
observable by eye*

*Fitting gave better than 1 mHz sensitivity  
to sidereal modulation with small data  
set from first generation experiment*

*1-2 orders of magnitude improvement possible with  
engineering upgrades & more data taking*

## Data analysis for 2000 H maser experiment

- Three runs: 19 useful days over 5 months

1-sigma limit:  $|\Delta v_{\text{Zeeman}}| = 0.49 \pm 0.34 \text{ mHz}$

- **Clean bound** on Lorentz-violating isotropy effects:

$$\left| \tilde{b}_{,XY}^{e^-} + \tilde{b}_{,XY}^p \right| \leq (3 \pm 2) \times 10^{-27} \text{ GeV}$$

$$\tilde{b}_J^w = b_J^w - m_w d_{J0}^w - \frac{1}{2} \varepsilon_{JKL} H_{KL}^w$$

D. Phillips et al., PRD **63**, 111101 (2001)

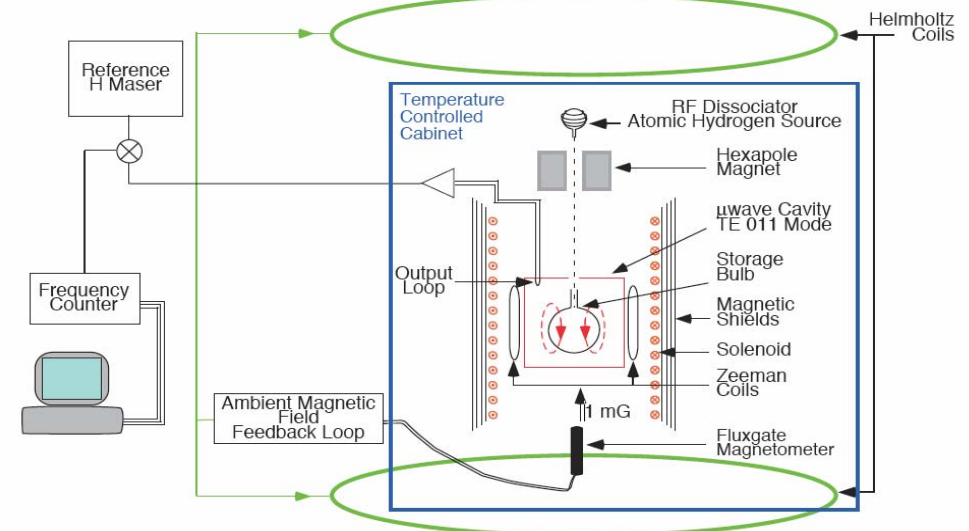
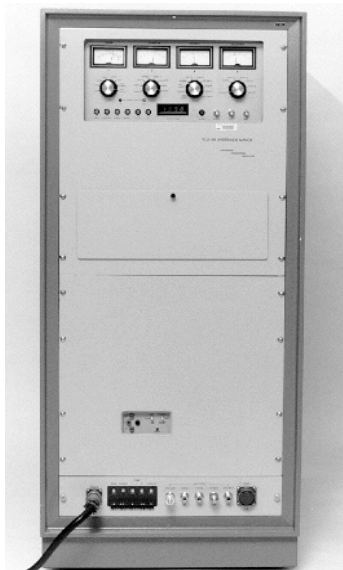
M. Humphrey et al., PRA **62**, 63405 (2000)

**M. Humphrey et al., PRA **68**, 63807 (2003)**

## Next-generation H maser experiment (ongoing)

Optimized/dedicated H maser for Lorentz symmetry test:

- Improved magnetometry
- Rebuilt internal heater and other systems to reduce meander of internally-generated magnetic fields
- Operation in lab with improved environmental control
- Much greater data taking



Dual noble gas maser

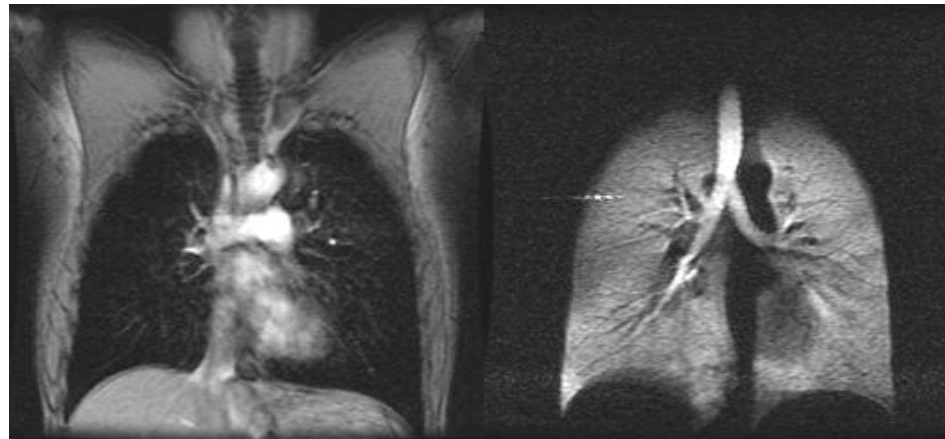
## Spin-polarized noble gas NMR

The nuclear spin 1/2 noble gases,  $^3\text{He}$  &  $^{129}\text{Xe}$ , can be given large spin polarization ( $\sim 50\%$ ) via spin-exchange optical pumping

=> inert, magnetized gases, detectable with NMR

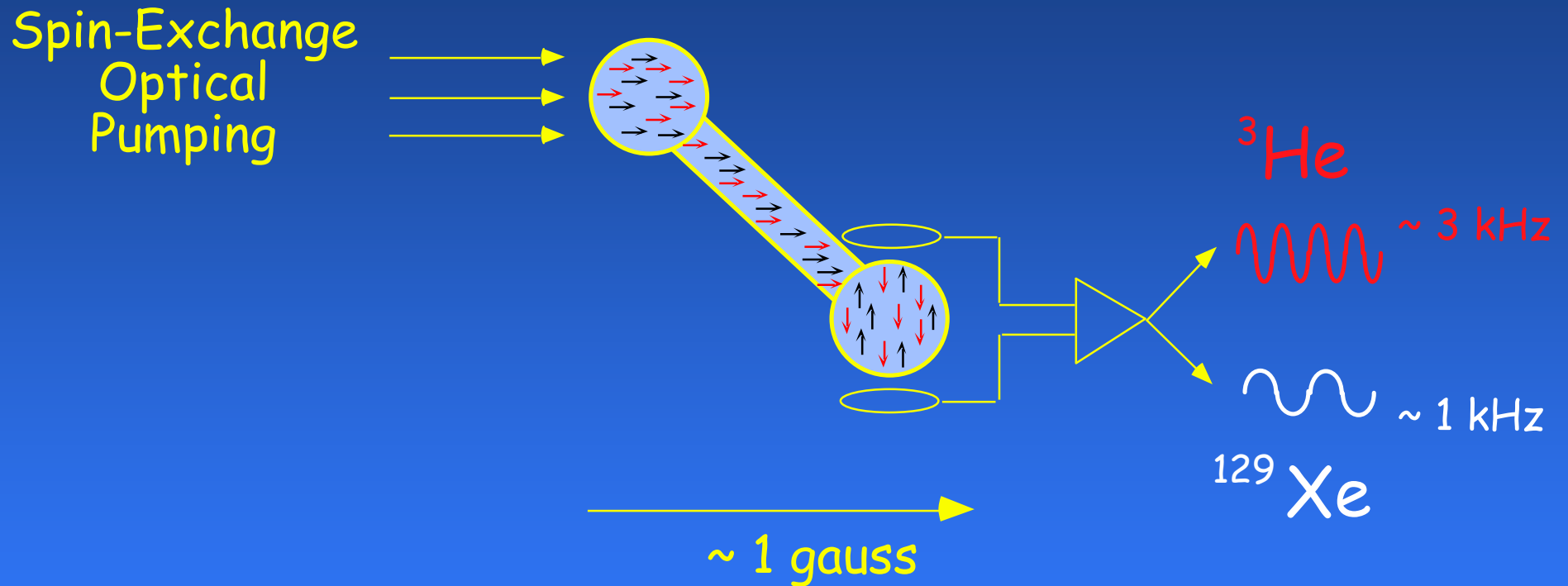
=> biomedical imaging, probing porous media

Conventional  
proton MRI  
of chest



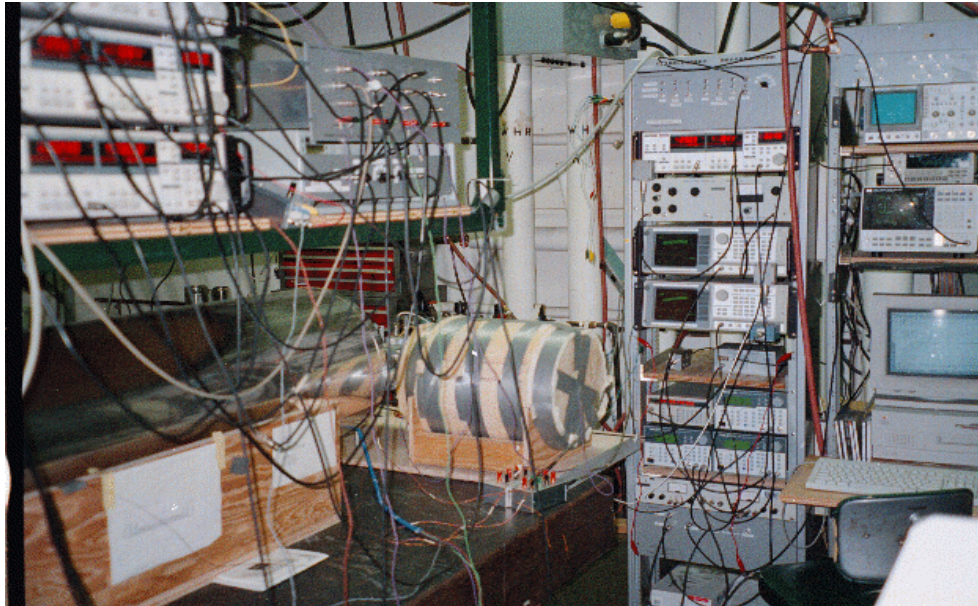
MRI of inhaled  
laser-polarized  
 $^3\text{He}$  gas

# Dual Noble Gas Maser

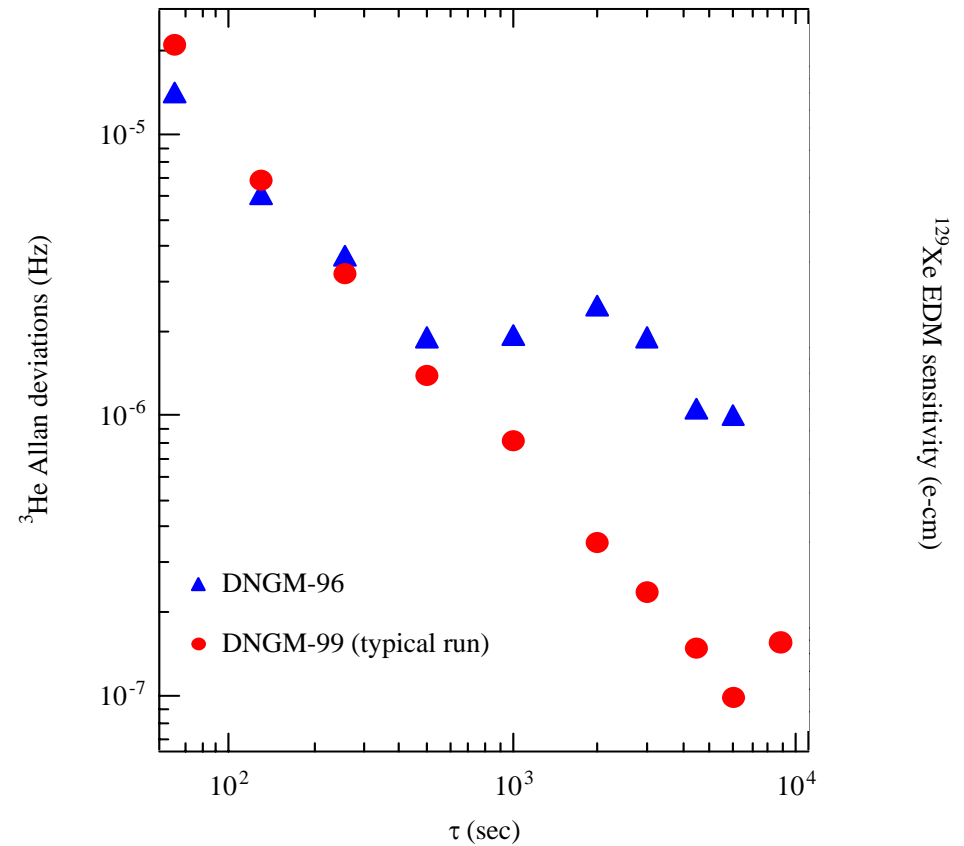


$\sim 100$  nanohertz frequency sensitivity on timescale of hours  
*Best test to date of Lorentz and CPT symmetry of the neutron*

# Testing Lorentz symmetry with noble gas masers



- Lorentz violation couples similarly to  $^3\text{He}$  and  $^{129}\text{Xe}$  (valence neutron)
- $^3\text{He}/^{129}\text{Xe}$  magnetic moment ratio  $\sim 3$

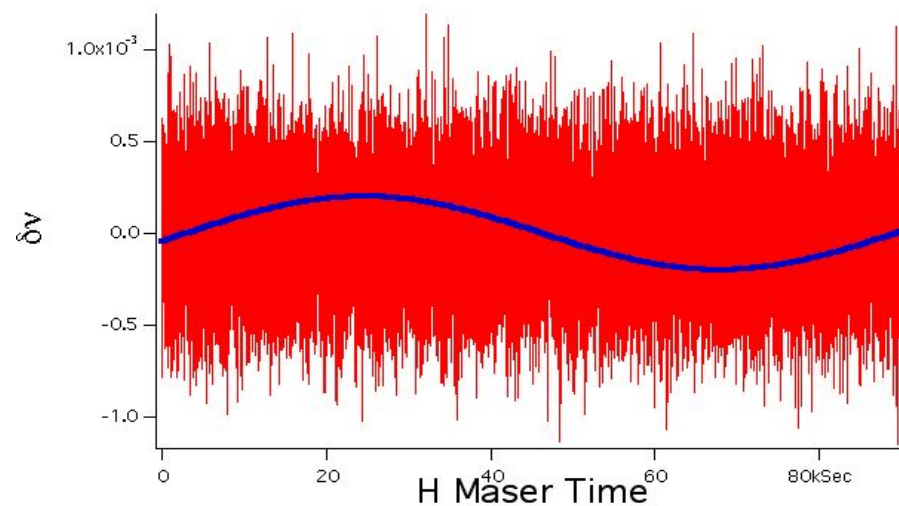


## Data analysis for 2000 isotropy symmetry test

- Fit free-running  $^3\text{He}$  maser phase data for each sidereal day to model including Larmor precession and sinusoid with sidereal periodicity.
- Runs performed for three cells in both east and west orientations.
- Bound isotropy-violation from weighted means of sidereal modulation coefficients.

$$\delta\nu^{\text{exp}} = \delta\nu_X \sin\omega_{\oplus}t + \delta\nu_Y \cos\omega_{\oplus}t$$

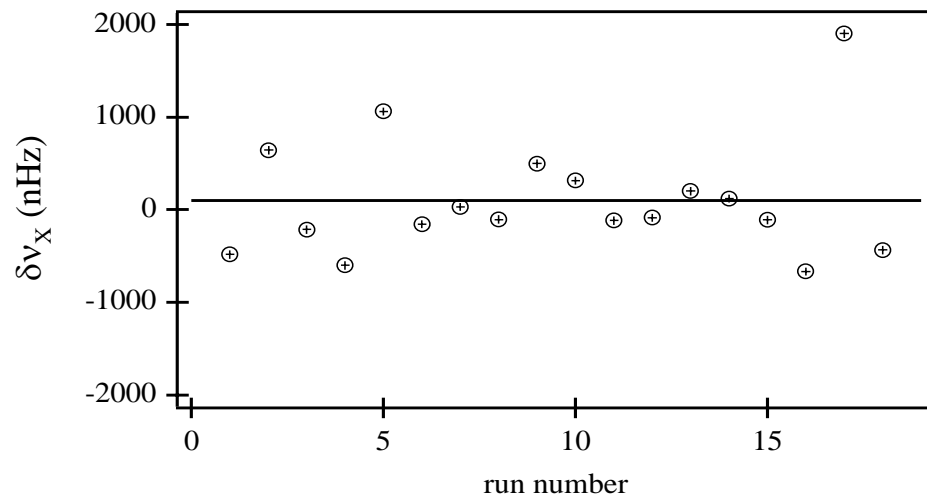
sidereal day  
frequency





## Data analysis for 2000 isotropy symmetry test

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- Runs performed for three cells in both east and west orientations.
- Bound isotropy-violation from weighted means of sidereal modulation coefficients.



Results for sidereal modulation coefficient  $\delta\nu_x$  with cell SE3/east

## Result of 2000 isotropy symmetry test

- Eight runs: 90 useful days over 13 months

1-sigma limit:  $|\Delta v_{3\text{He Zeeman}}| = 53 \pm 45 \text{ nHz}$

- Bound on Lorentz-violating orientation effects assuming only valence neutron is important in  $^3\text{He}$  &  $^{129}\text{Xe}$ :

$$|\tilde{b}_{X,Y}^n| \leq (6 \pm 5) \times 10^{-32} \text{ GeV}$$

$$\tilde{b}_J^w = b_J^w - m_w d_{J0}^w - \frac{1}{2} \varepsilon_{JKL} H_{KL}^w$$

D. Bear et al., PRL **85**, 5038 (2000)

## Best bounds on isotropy-violation (coupling to spins)

Experiment	electron	proton	neutron
<i><sup>199</sup>Hg and <sup>133</sup>Cs precession frequencies (Hunter, Lamoreaux et al.)</i>	$10^{-27} \text{ GeV}$	$10^{-27} \text{ GeV}$	$10^{-30} \text{ GeV}$
<i>spin-polarized torsion pendulum (Adelberger, Heckel et al.)</i>	$10^{-29} \text{ GeV}$	—	—
<i>H maser double resonance (Harvard-Smithsonian)</i>	$10^{-27} \text{ GeV}$	$10^{-27} \text{ GeV}$ <i>(clean test)</i>	—
<i><sup>129</sup>Xe/<sup>β</sup>He maser (Harvard-Smithsonian)</i>	—	—	$10^{-31} \text{ GeV}$

Naive Planck-scale sensitivity  $\sim 10^{-19} \text{ GeV}$  for neutron & proton

# New $^{129}\text{Xe}/^3\text{He}$ maser result: sensitive test of *boost*-symmetry for the neutron

- In the **lab frame**, the net effect of Lorentz-violation includes both **rotations** ( $b_{X,Y}$ ) and **boosts** ( $b_T$ ):

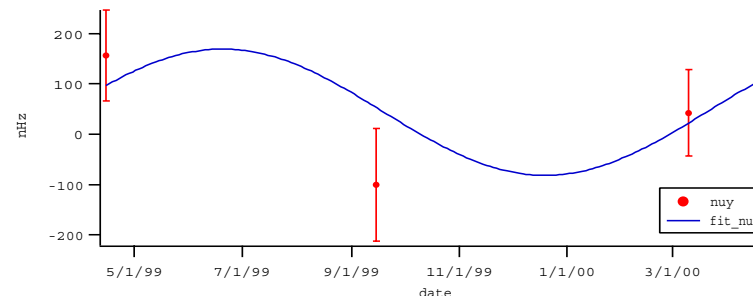
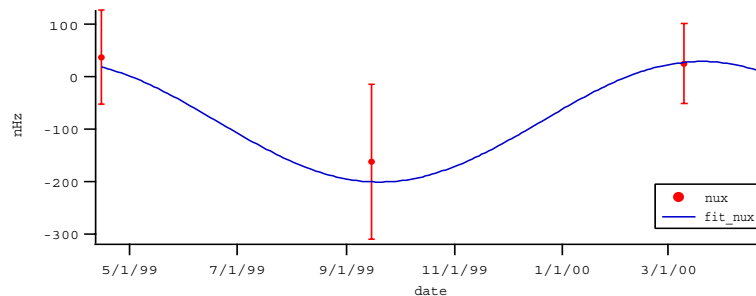
$$b_2 = b_T \beta_L - (b_X + b_T \beta_{\oplus} \sin \Omega_{\oplus} T) \sin \omega_{\oplus} T_{\oplus} + (b_Y - b_T \beta_{\oplus} \cos \Omega_{\oplus} T) \cos \omega_{\oplus} T_{\oplus}$$

↑  
sidereal year  
frequency

↑  
 $v_{\text{orbit}}/c \sim 10^{-4}$

↑  
sidereal day  
frequency

- We analyzed  $^{129}\text{Xe}/^3\text{He}$  maser data with 3 free parameters  $b_X, b_Y, b_T$

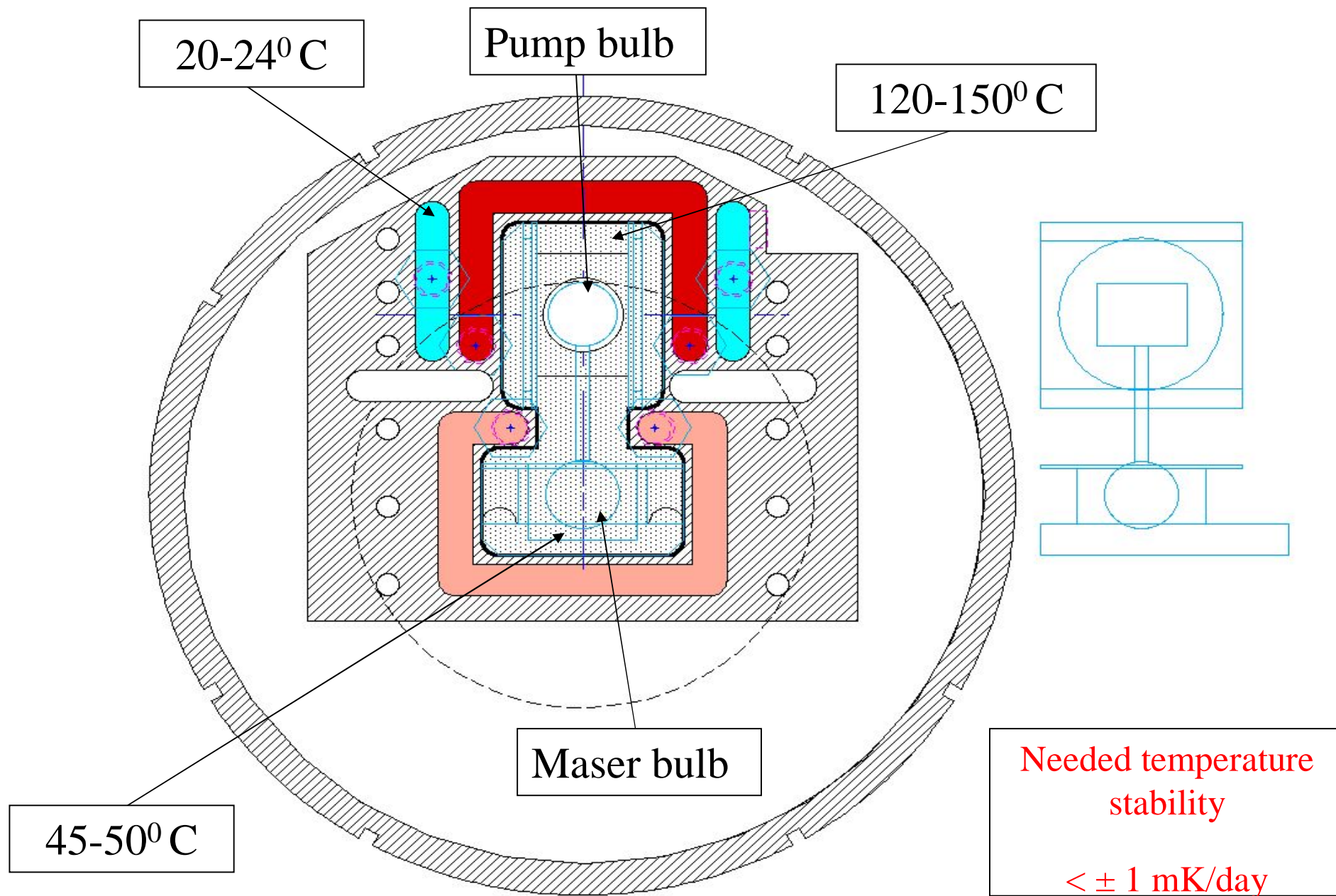


$$b_T^n = (1.5 \pm 0.9) 10^{-27} \text{ GeV}$$

F. Cane et al., PRL (2004)

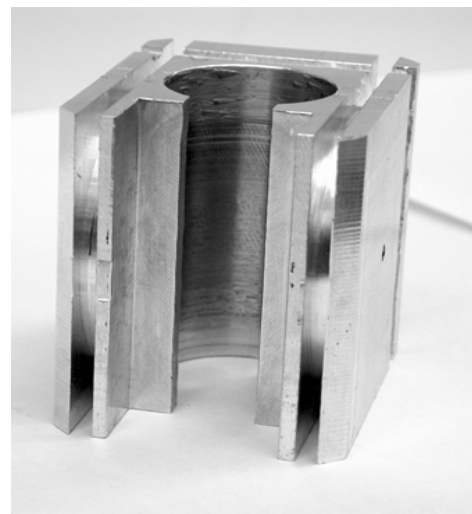
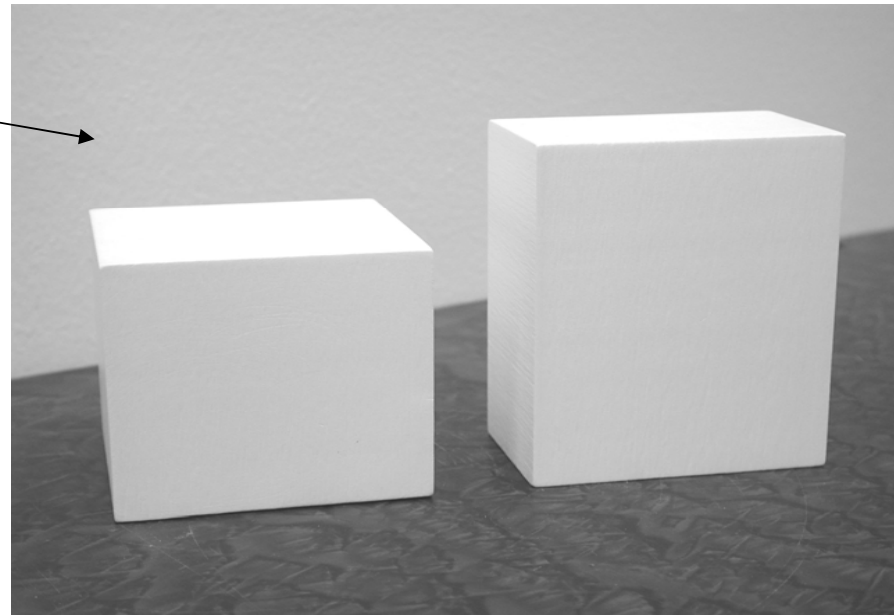
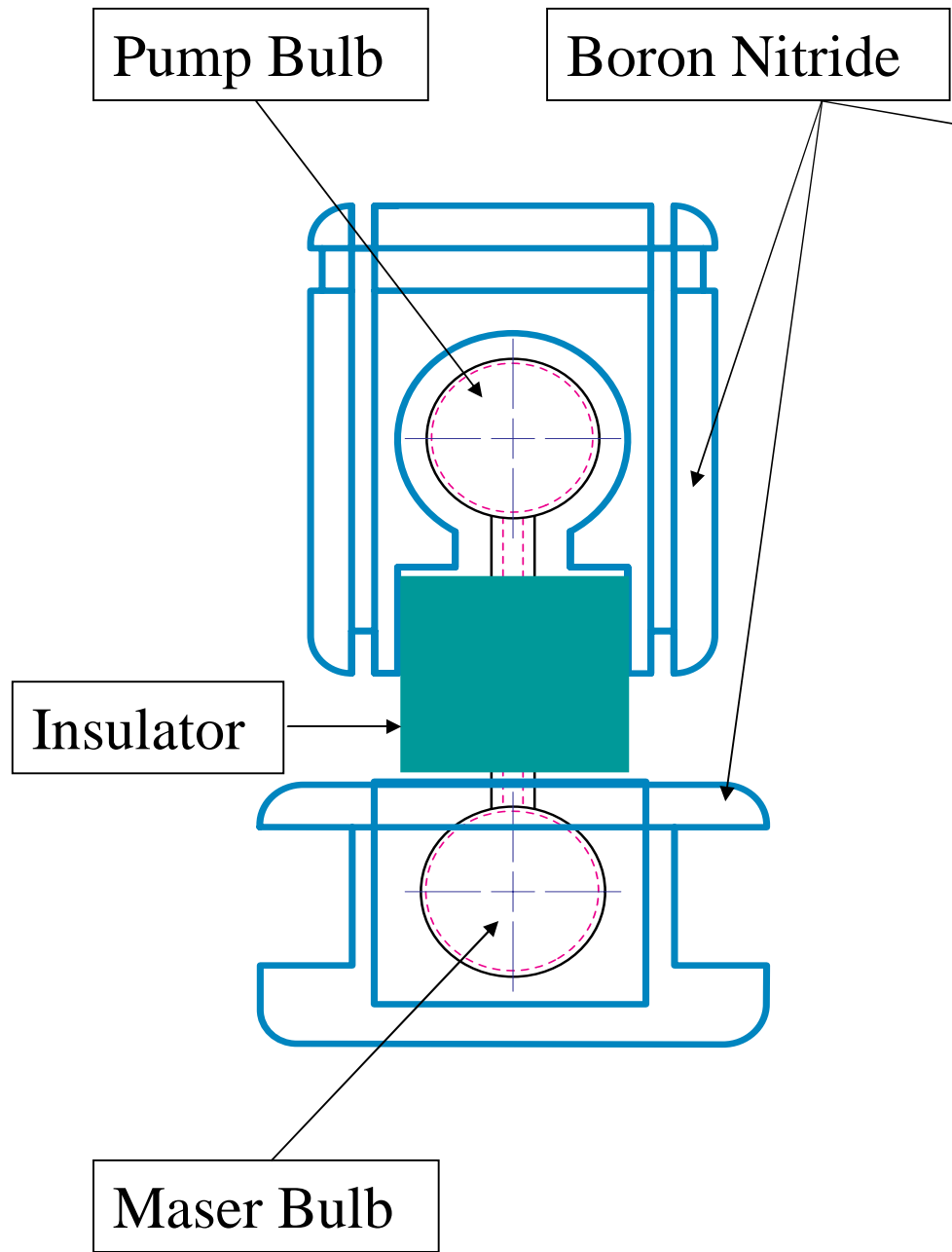
## Next-generation noble gas maser experiment (ongoing)

- Optimize cell geometry & gas pressures
  - Improve temperature control
  - Improve mechanical and thermo-mechanical stability
  - Narrow-spectrum optical-pumping laser
- improved co-magnetometry  
& reduced medium-term frequency noise

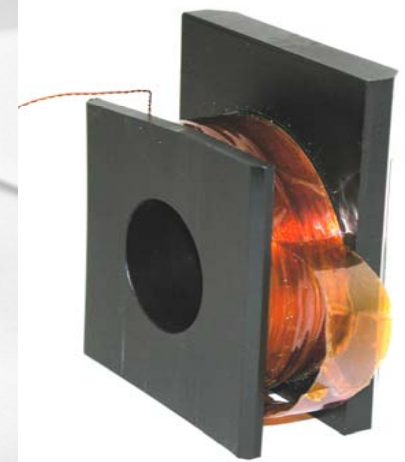


## Thermal properties of materials

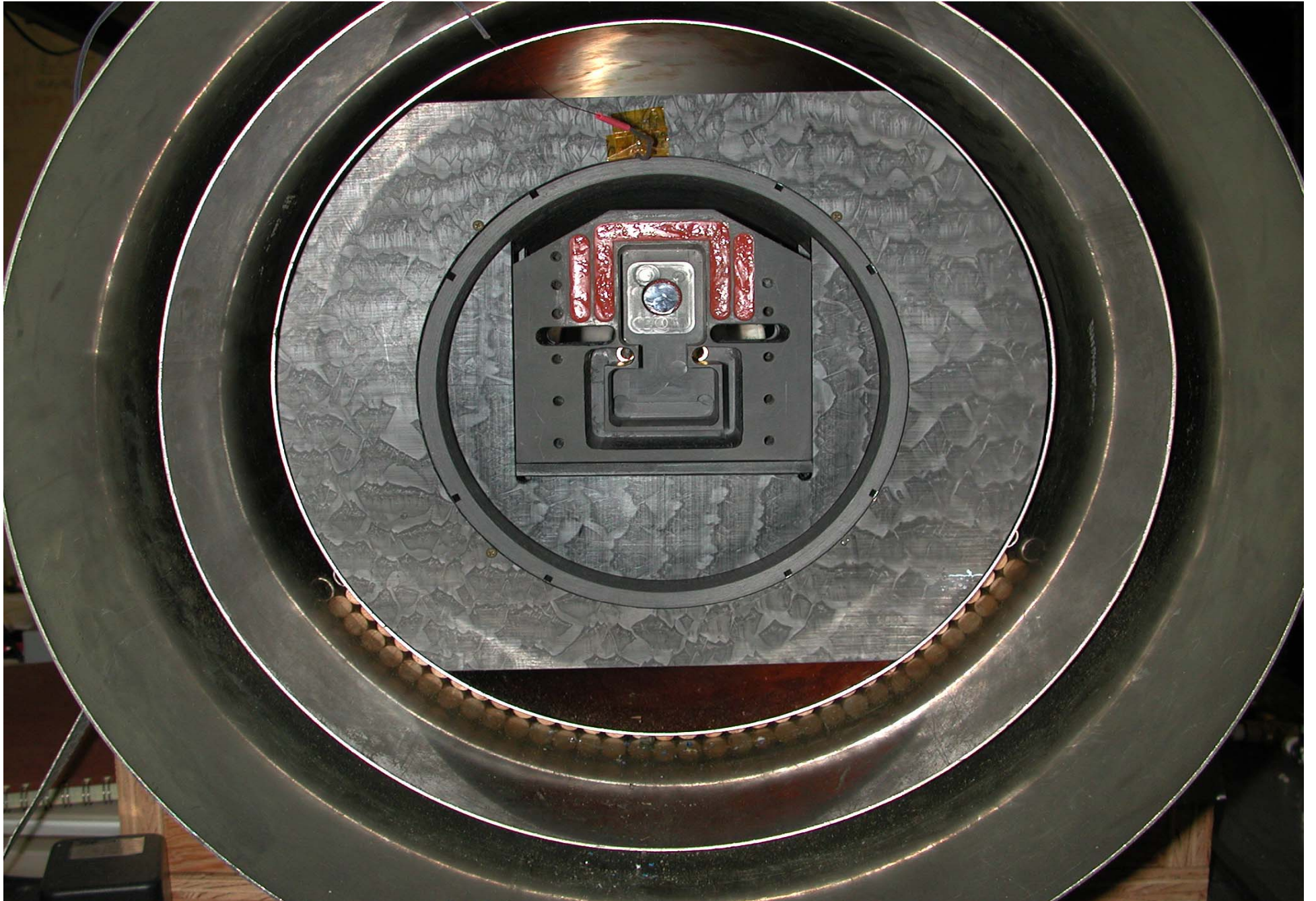
Material	Density (Kg/l)	Specific Heat (J/Kg-K)	Thermal Conductivity (W/m-K)	Coefficient of Thermal Expansion (K <sup>-1</sup> )	Continuous Service in Air (Max °C)
<b>Ultem® 1000</b> PEI, Polyetherimid, unfilled, extruded	1.28	-	<b>0.12</b>	0.56 10 <sup>-4</sup>	<b>171</b>
<b>Nylatron® GS</b> Nylon, MoS2 filled, extruded	1.16	-	<b>0.24</b>	0.72 10 <sup>-4</sup>	<b>104</b>
<b>Boron Nitride</b> (Grade AX05)	1.9	809	<b>78/130</b>	0.3-1 10 <sup>-6</sup>	850
<b>Aluminum</b>	2.68	897	<b>240</b>	-	-



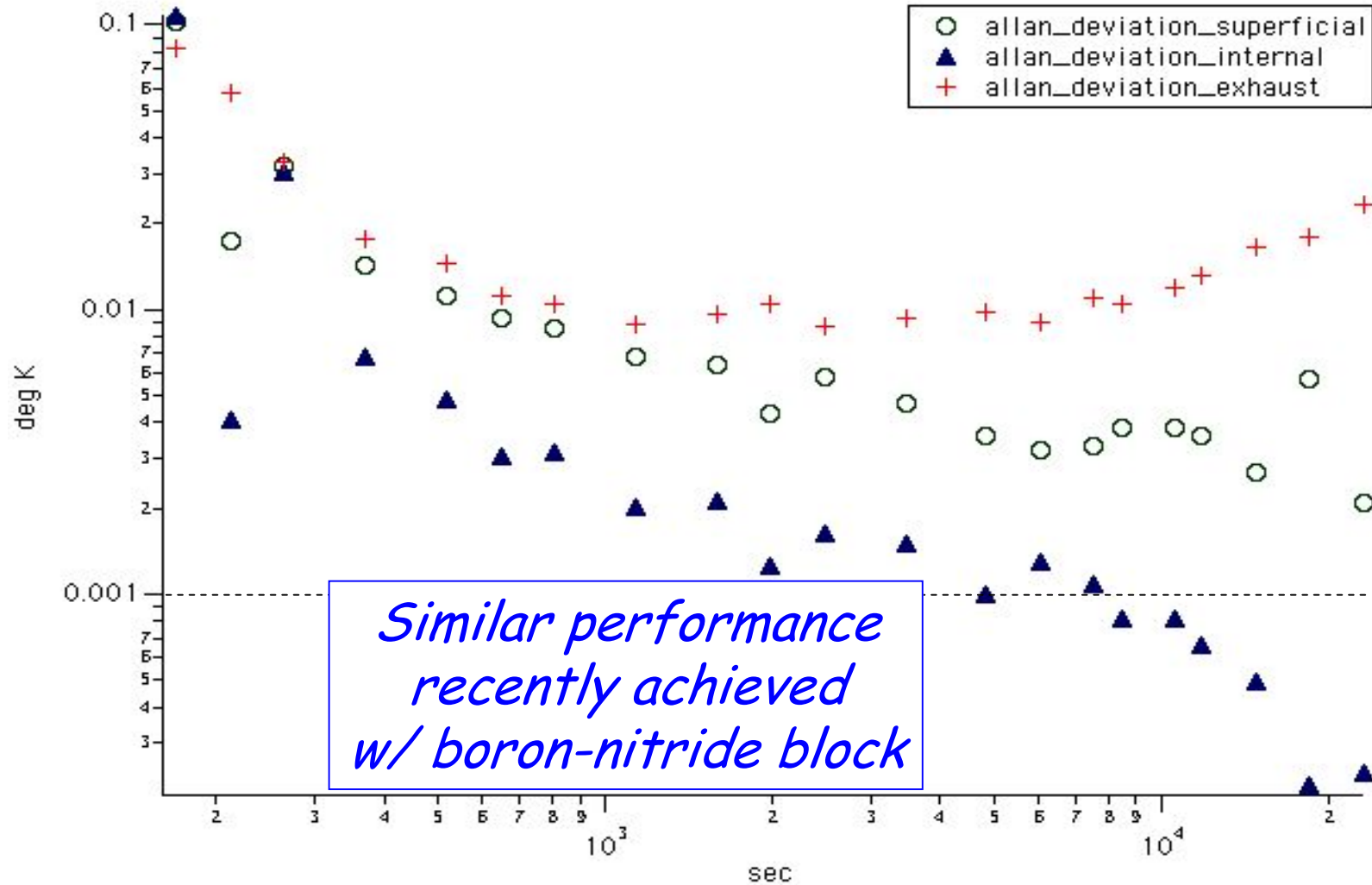
Al test block







# Double temperature lock tested with Al block



## Target isotropy-violation sensitivity of new experiments

Experiment	electron	proton	neutron
<i><sup>199</sup>Hg and <sup>133</sup>Cs spectroscopy on rotating table (Amherst)</i>	<i><math>10^{-29}</math> GeV</i>	<i><math>10^{-29}</math> GeV</i>	<i><math>10^{-32}</math> GeV</i>
<i>Optimized spin-polarized torsion pendulum (U. Washington)</i>	<i><math>10^{-31}</math> GeV</i>	—	—
<i><math>K^{\beta}</math>He spectroscopy (Princeton)</i>	<i><math>10^{-30}</math> GeV</i>	—	<i><math>10^{-33}</math> GeV</i>
<i>Optimized H maser double resonance (Harvard-Smithsonian)</i>	<i><math>10^{-29}</math> GeV</i>	<i><math>10^{-29}</math> GeV (clean test)</i>	—
<i>Upgraded noble gas masers (Harvard-Smithsonian)</i>	—	—	<i><math>10^{-33}</math> GeV</i>

How much better  
can one do?

## Experimental challenges

- Narrow bandwidth, high S/N spin resonance
- Good co-magnetometry
- Excellent long-term stability and immunity from environment

## Current limitations

- Thermal noise  
(2-5 orders of magnitude worse than shot noise)
- Properties of materials  
(thermal expansion and conductivity, magnetic permeability, etc.)
- Slowness of Earth's rotation

## Modest proposals

- Develop facilities to aid Lorentz symmetry experiments:  
e.g., a low-noise rotating platform for (modest-sized) experiments
- Community commitment to support 2+ experiments (of roughly comparable sensitivity) in each sector  
→ a systematic attack on problem

*How ?*

## Immodest questions

- What is the relative magnitude of Lorentz-violating effects between different sectors?
- Relative magnitude *within* a sector?  
"Enhancement factors" to aid experimentalists?