united nations educational, scientific and cultural organization (international atomic energy agency the **abdus salam** international centre for theoretical physics **4** O anniversary 2004

H4.SMR/1586-2

"7th Workshop on Three-Dimensional Modelling of Seismic Waves Generation and their Propagation"

25 October - 5 November 2004

Modelling of Seismic Input

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Seventh workshop on *Three-Dimensional Modeling of Seismic waves Generation, Propagation and their inversion - ICTP 2004* 

# MODELLING OF SEISMIC INPUT

### Giuliano F. Panza





More effective prevention strategies would save not only tens of billions of dollars, but save tens of thousands of lives. Funds currently spent on intervention and relief could be devoted to enhancing equitable and sustainable development instead, which would further reduce the risk for war and disaster - Kofi Annan, 1999



The realistic modelling of ground motion can now be done by making use of global observations from digital networks, application of modern theories for the forward and the inverse problems, and by use of widely available computers.

We do not have to wait for earthquakes to occur in likely focal regions and then to measure ground motion with an extremely dense set of recording instruments.

With the available geological, geophysical, seismological and seismotectonic data, we can compute these seismograms from theoretical considerations (Panza, Radulian and Trifu, Editors, 2000)

A complete database for all sites and predicted focal mechanisms can be constructed immediately no delay is necessary while we wait for experimental evidence and recordings.

This database is then, naturally, updated continuously by comparison with incoming new experimental data (Costa et al., 1993, Panza et al., 1999, 2001)

## seismic nput he modelling we developed 2005 **ress** pects such as:

the direct evaluation of resulting maps in terms of design parameters, without requiring the adaptation of probabilistic maps to design ground motions; the effect of crustal properties on attenuation;

the derivation of ground motion parameters from synthetic time histories, instead of using overly simplified attenuation functions; thegeneralization of design parameters to locations where there is little seismic history.

## The example of Italy









### Flow-chart of the method











Our modelling gives the envelope the ground motion (like acceleration, velocity  $\left( \right)$ displacement) determined considering scenario earthquakes consistent with the seismic history and the seismotectonic of the study area.



**Deterministic method** 

#### Conversion between Intensity (MCS) and Peak ground motion parameters in ITALY

ING Intensity data – NT4.1.1 Magnitudes

Intensity	<b>Displacement (cm)</b>	Velocity (cm/s)	DGA (g)
V	0.1 – 0.5	0.5 - 1.0	0.005 - 0.01
VI	0.5 - 1.0	1.0 - 2.0	0.01 - 0.02
VII	1.0 - 2.0	2.0 - 4.0	0.02 - 0.04
VIII	2.0 - 3.5.	4.0 - 8.0	0.04 - 0.08
IX	3.5 - 7.0	8.0 - 15.0	0.08 - 0.15
X	7.0 - 15.0	15.0 - 30.0	0.15 – 0.30
XI	15.0 - 30.0	30.0 - 60.0	0.30 - 0.60
			/mm/
			Dotorministic m

**Deterministic method** 

#### Conversion between Intensity (MCS) and Peak ground motion parameters in ITALY

ISG Intensity data – NT4.1.1 Magnitudes

	Intensity	<b>Displacement (cm)</b>	Velocity (cm/s)	DGA (g)	
HH	VI	1.0 - 1.5	1.0 - 2.0	0.01 - 0.025	h
	VII	1.5 – 3.0	2.0 - 5.0	0.025 - 0.05	10
++++	VIII	3.0 - 6.0	5.0 - 11.0	0.05 - 0.1	
	IX	6.0 – 13.0	11.0 - 25.0	0.1 - 0.2	L.
$\Pi \Pi \Pi$	Х	13.0 - 26.0	25.0 - 56.0	0.2 - 0.4	
	7 Ç			<u> </u>	
				Determin	istic

method



The slope of the regression maximum observed macroseismic intensity, (MCS), and computed peak values of ground motion is always close to 0.3, a value common to many empirical relations (Shteinberg et al., 1993) found considering Peak Ground Accelerations. Cancani in 1904 modified the original Mercalli scale, defining the MCS scale, indeed with the declared purpose to obtain the slope (



## GENERAL PROBLEMS IN SEISMIC HAZARD ASSESSMENT

Case studies indicate the limits currently the used ethodologies, deeply rooted in engineering practice, based a probabilistic approach

probabilistic supplies analysis Ihe indications that can be useful but are no ifficiently reliable to characterize seismic examples Recent Kobe hazard. (26.1.2001)<u>7.1.1995),</u> Bhuj (21.5.2003)Boumerdes and Bam (26.12.2003) events

### ? GSHAP ?

Kobe (17.1.1995), Gujarat (26.1.2001), Boumerdes (21.5.2003) and Bam (26.12.2003) earthquakes PGA(g)

#### Expected

with a probability of exceedence of 10% in 50 years (return period 475 years)

Observed

 Kobe
 0.40-0.48
 0.7-0.8

 Gujarat
 0.16-0.24
 0.5-0.6

 Boumerdes
 0.08-0.16
 0.3-0.4\*

 Bam
 0.16-0.24
 0.7-0.8

from I, if liquefaction is considered the value may be smaller

The mathematical modelling, based on probabilistic concepts cannot 01 de 20 behind an earthquake, at the cess most it can supply some guidelines.

mathematical modelling may lhe validity///in dealing with oose Incertainties that are so large that be quantifiable ma not a meaningful sense (Chandler et al it/ happens as In seismicity regions. moderate lacking historical regions anc instrumental earthquake data.

definition proper / seismic input at a en site can be llowind

The first approach is based on the analysis of the available strong motion databases, collected existing seismic networks, and on the grouping of those accelerograms that contain similar source, path and site effects (e.g. Decanini and Mollaioli, 1998).
The second approach is based on modelling techniques, developed from the knowledge of the seismic source process and of the propagation of seismic waves, that can realistically simulate the ground motion (Panza et al., 1996; Field et al., 2000)

The ideal procedure 0 OW the omplementary Ways validate umerical modelling with the available recordings e.g. Decanini et al., 1999; Panza et al., 2000a,b,c

For example, in constructing design input motions, estimates of the peak ground motions at the site can be made in a probability hazard analysis (including interoccurrence probabilities). Then final selection of appropriate accelerograms with their associated ground velocities and displacements would follow a deterministic approach. The choices would be guided by wave propagation modelling that includes appropriate phasing and duration of the dominant waves in the time histories (Bolt, 2003).



# BASE SEISMIC ISOLATION

eterministic Where the numerical modelling successfu compared svnthet records, he seismograms microzoning, , based upon a oossible sce 12 23 

General Problems in Seismic Hazard Assessment

### ere no recordings are available the synthetic signals used to estimate d motion without **N**RI Str 8 788 F General Problems in Seismic Hazard Assessment

#### modelling İS ISE ecessary because, contrary to practice, 10 effects c Ø SI **R** General Problems in Seismic Hazard Assessment

of realistic wide **Ine** USe synthetic time histories, MA **che** allo scenarios based ruct significant round motion Darameters (velocity and displacement

General Problems in Seismic Hazard Assessment

Among the cost effective advance action aimed at creating knowledge based hazard resilient public assets a particular role is played by se tion, an innovative technology that is getting a steadily increasing diffusion on global scale.

Base Seismic Isolation







Generally, for isolated structures, seismic isolation systems rubber bearings, frictional type etc.) need svstems, icient displacement and e pation capacities **Base Seismic Isolation** 

with order to cope these requirements, the evaluation of the critical input for this kind of seismic protection systems should consider, beyond strength demands influence significant isplacement and energy demands **Base Seismic Isolation** 

It is then evident that the importance of outlined aspects, and the the corresponding structural design choices, evaluati ne 6 e stro  $\mathbf{O}(\mathbf{O})$ **1** 0 n he 210 **ISO** 52 2 which from energetic parameters can be extracted.

Base Seismic Isolation





### Hybrid Method:

### Modes Summation+Finite Differences.



Artificial boundaries, limiting the FD grid.



Zone of high attenuation, where Q is decreasing linearly toward the artificial boundary.

Adjacent grid lines, where the wave field is introduced into the FD grid. The incoming wave field is computed with the mode summation technique. The two grid lines are transparent for backscattered waves (Alterman and Karal, 1968).



Local heterogeneous model

Site

Wave propagation is treated by means of the modal summation technique from the source to the vicinity of the local structure (anelastic bedrock structure).

The finite differences technique is applied in the laterally inhomogeneous part of the model (sedimentary basin).

Synthetic seismic signal obtained consider simultaneously the seismic moment tensor, average mechanical characteristics of the traveled path and detailed local site conditions.

Complete synthetic seismograms in terms of displacement, velocity and acceleration are and P-SV waves in the frequency range of interest.

A comprehensive description of the theory used to compute the synthetic signals is given in Advances in Geophysics, Vol. 43, 2001, Academic Press. For urban areas where the numerical modelling of ground motion has been successfully compared with strong motion records, the computations of synthetic seismograms permit a detailed microzoning based upon the set of possible scenario earthquakes.

For areas where very limited or no recordings are available the synthetic time series can be used to estimate the expected ground motion, thus leading to a pre-disaster microzonation without having to wait for an earthquake to occur. In both cases the use of synthetic computations is necessary to overcome the fact that the so-called local site effects can be strongly dependent upon the properties of the seismic source generating the seismic input (Panza et al, 2000).

# •H/V is the spectral ratio between the horizontal and vertical components of motion.

#### Modeling of seismic input (azimuth effect)



•**RSR** is the ratio between the amplitudes of the response spectra, for 5% damping, obtained considering the bedrock structure, and the corresponding values, computed taking into account the local heterogeneous medium.

#### Modeling of seismic input (azimuth effect) T 5 2 4 з 1 $(80^{\circ})$ 3 hequency (Hz) 0. Τ 10 8 7 6 5 4 з 2 9 1 $(180^{\circ})$ зinquency (HZ) N 1 -

23

Alluvial deposits  $\rho=1.99 \text{ g/cm}^3$  $\alpha=450 \text{ m/s} \beta =210 \text{ m/s}$ 

 $\begin{array}{c} \text{Quartzous sands} \\ \text{Sg } \rho = 2.12 \text{ g/cm}^3 \\ \alpha = 1600 \text{ m/s} \beta = 500 \text{ m/s} \end{array}$ 

25

24

22

20

Μ

21

19

 $ASg \begin{array}{c} \text{Yellow clays} \\ \rho=2.04 \text{ g/cm}^3 \\ \alpha=1400 \text{ m/s} \beta=280 \text{ m/s} \end{array}$ 

Sands  $\rho = 1.91 \text{ g/cm}^3$  $\alpha = 550 \text{ m/s} \beta = 280 \text{ m/s}$ 

18

17

16

Aa

15

14

Grey-blue clays  $\rho=2.06 \text{ g/cm}^3$  $\alpha=1700 \text{ m/s} \beta=650 \text{ m/s}$ 

 $\begin{bmatrix} Lavas \\ \rho = 2.45 \text{ g/cm}^3 \\ \alpha = 1700 \text{ m/s} \beta = 500 \text{ m/s} \end{bmatrix}$ 

RSR for the SH component of motion

-90

13

• Therefore we can conclude, in agreement with the recent paper by Field and the SCEC phase III Working Gourp (2000), that our best hope is via waveform modeling based on first principles of physics.



These images of the Los Angeles Basin show "hotspots" predicted from computer simulations of an earthquake on the Elysian Park Fault and an earthquake on the Newport-Inglewood Fault (represented by the white dashed lines). What is shown is **not** how much shaking was experienced at a particular site but rather how much more or less shaking (highest levels are shown in red) a site receives **relative to what is expected** from only the magnitude of the earthquake and the site's distance from the fault. These images consider only part of the total shaking (long-period motions) and were calculated by using a simplified geologic structure. (Data for images courtesy of Kim Olsen, University of California, Santa Barbara, SCEC Phase III report)



"hotspots" predicted from computer simulations of an earthquake on the Santa Monica Fault and an earthquake on the Palos Verdes Fault (represented by the white dashed lines). SCEC Phase III report, Field, 2000, BSSA, see also http://www.scec.org/phase3/

## Near-Fault Ground Motions

Near-fault ground motions often contain large longperiod (2-5 sec) wave pulses. There are two causes of these long-period pulses: first, constructive interference of the radiated waves due to directivity of the fault rupture; second, movement of the ground associated with the permanent geodetic offset. To keep these two effects separate, the terms "directivity pulse" and "fling-step" are used for the rupture directivity and elastic rebound effects, respectively (Bolt & Abrahamson, 2003).


Figure 1: Strong motion recordings at the Pacoima station, California in the 1971 San Fernando (bottom) and 1994 Northridge (top) earthquakes. All are S16E horizontal components of (1a) acceleration, (1b) velocity, and (1c) displacement, respectively.



Figure Ib: Ground velocity, S16E Pacoima 1971, 1994.

### Nice examples of velocity pulses

Rupture directivity effects occur when the fault ruptures toward the site and the slip direction (on the fault plane) is aligned with the rupture direction (Somerville et al., 1998). The consequent pulse is strongest on the component of motion perpendicular to the strike of the fault (fault-normal component). Fling-step ground motion occurs close to a ruptured fault with significant surface offset. It is limited to the ground displacement component parallel to the slip direction. Thus, for strikeslip earthquakes, the rupture directivity pulse and the fling-step pulse will naturally separate themselves into two horizontal components. For dip-slip earthquakes the effect is more complicated. The rupture directivity effect will be strongest on the fault normal component at a location updip from the hypocenter. The fling step will be observed on the horizontal component perpendicular to the strike of the fault. Consequently, for dip-slip faults, directivity-pulse effects and fling-step effects can be combined on the same component.



Landers Earthquake (1992). Map showing the velocity time histories at Lucerne (forward) diretivity) and Joshua Tree (backward directivity).









Top: schematic orientation of the rupture directivity pulse and fault displacement (fling step) for strike-slip fault (left) and dip-slip (right) faulting.

Bottom: schematic partition of the rupture directivity pulse and fault displacement between the strike normal and strike parallel components of ground displacement.

Waveforms containing static ground displacement are shown as dashed lines; versions of these waveforms with the static displacement removed are shown as dotted lines (Sommerville, 2002).



Fault normal velocity pulses recorded near 3 moderate magnitude earthquakes (left column) and 3 large magnitude earthquakes (right column), shown on the same scale (Sommerville, 2002).









Chi Chi 1999 event (thrust fault) Accelerations at different sites showing fling effect

3 epicenter



## UNESCO-IUGS-IGCP

## Project

• In the framework of the UNESCO-IUGS-IGCP project "Realistic Modelling of Seismic Input for Megacities and Large Urban Areas", centred at the Abdus Salam International Center for Theoretical Physics, a deterministic approach has been developed and applied to several urban areas for the purpose of seismic microzoning.

The full text of the summary of the main results obtained can be downloaded at:

http://www.ictp.trieste.it/

www\_users/sand/unesco-414.html • Pilot studies show that, distances from the causative fault being equal, for events with magnitude in the range 6.5-7.1 and epicentral distances in the range 10-30 km, the elastic spectra computed from synthetic signals are comparable with those computed from real records.

Elastic  $E_I$  (cm<sup>2</sup>/s<sup>2</sup>) spectra. Comparison between Augusta synthetic signals and strong motion records of Irpinia 1980 (Calitri station) and Loma Prieta 1989 (Gav. Tower, Ucsc and Ysidro stations) earthquakes.



• The envelope of the synthetic elastic energy spectra can reproduce a wide distribution of energy in the most relevant frequency range from the engineering point of view.

• The data set of synthetic seismograms can be fruitfully used and analysed by civil engineers for design and reinforcement actions. • The data set of synthetic seismograms supply 8 particularly powerful and economical tool for the prevention and preparedness aspects of Civil Defence.



## Seismic microzoning of ອີອງໄດ້ເອີຍ

#### The Profiles for Tangshan Earthquake





The local structural model and the synthetic seismograms along the profile TS02.

The lines in the bottom figure outline the three sediment layers.

Radial, transverse and vertical components of the synthetic ground acceleration



The local structural model and the synthetic seismograms along the profile TS03.

The lines in the bottom figure outline the three sediment layers.

Radial, transverse and vertical components of the synthetic ground acceleration.



The local structural model and the synthetic seismograms along the profile TS04.

The lines in the bottom figure outline the three sediment layers. Radial, transverse and vertical components of the synthetic ground acceleration.

#### The Local Structural Model and the Synthetic Seismograms along Profile TS04



RSR versus frequency and distance along Profile **TS04** 

#### RSR of SH-waves at Selected Sites along Profile TS04



#### The Profiles for Zhangbei Earthquake



Profiles for Zhangbei Earthquake. The background contours represent the Quaternary sediment depth in meters. The polygon represents the town of Beijing. Two profiles, ZB05 and ZB06 are shown in the figure. The profiles point towards to the epicenter of the 1998 Zhangbei earthquake, which is located in the northwest. The numbers along the profiles are the distances from the epicenter, in km.



# The local structural model and the synthetic seismograms along the profile ZB05.

The lines in the bottom figure outline the three sediment layers.

Radial, transverse and vertical components of the synthetic ground acceleration.

#### The Local Structural Model and the Synthetic Seismograms along Profile ZB05



#### RSR of SH-waves at Selected Sites along Profile ZB05









Maxmum and average RSR for 4 zones for zero damping and 5% damping.

Absolute spectral accelerations consistent with 1976 Tangshan earthquake





Spectral acceleration (5% damping) for the 4 zones



## Seismic microzoning of Rome

Traianus (98-117) wars to conquer Dacia (101-106) are celebrated by the *Colonna Traiana*, about 30 m (excluding basement) toll, in Roma. The column is made of 17 juxtaposed blocks called *rocchi*.

Essentially equal funeral monument (*Colonna di Marco Aurelio*) was built to celebrate Marcus Aurelius (161-180) wars against Marcomanni.
Colonna Traiana sits on solid soil and is well preserved, while Colonna di Marco Aurelio sits on Tiber sediments and shows a dislocation of about 8 cm between two central *rocchi*.



Colonna Traiana (sinistra) e Colonna di Marco Aurelio (destra



*Rocco* basic element of the two columns



Dislocation of about 8 cm between two rocchi of Colonna di Marco Aurelio



Dislocation of about 8 cm between rocchi IX and X of *Colonna di Marco Aurelio* (from ITALIA 2004, 32<sup>nd</sup> International Geological Congress; 1<sup>st</sup> Circular)



First two free modes of S. Giorgio church in Trignano (a) 2.57Hz, (b) 2.72 Hz





Third and fourth free modes of S. Giorgio church in Trignano (c) 6.26Hz, (d) 9.22 Hz Microzonazione della citta' di Roma consistente con la storia sismica e la sismotettonica della regione

ZONE 1

2

з

4

5



Accelerazioni spettrali attese (n=3)

### La normativa sismica per la citta' di Roma Roma: 3ª categoria Accelerazione orizzontale di ancoraggio dello spettro di risposta elastico:

#### 0.15 [a<sub>g</sub>/g] ~ I=IX

Stima che considera storia sismica e sismotettonica:

max med med + $\sigma$ 

Zona 1: 0.24 - 0.15 - 0.30  $[a_g/g] \sim I = X$ Zona 4: 0.16 - 0.13 - 0.26  $[a_g/g] \sim I = X$ Stima che considera solo la storia sismica: max med med+ $\sigma$ Zona 1: 0.14 - 0.08 - 0.16  $[a_g/g] \sim I = IX$ 

Zona 4: 0.08 - 0.07 - 0.14 [a<sub>g</sub>/g] ~ I=VIII



Zone sismiche del territorio italiano (2003)

zona	accelerazione orizzontale con probabilità di superamento pari al 10 % in 50 anni [ag/g]	accelerazione orizzontale di ancoraggio dello spettro di risposta elastico (Norme Tecniche) [ag/g]
1	> 0,25	0,35
2	0,15-0,25	0,25
3	0,05-015	0,15
4	<0,05	0,05



Modellazione delle Intensita' osservate dedotte dalle accelerazioni spettrali teoriche (n=1)

From historical monuments, we can infer that strong lateral (within < 1km) variations in seismic ground motion can occur in Rome, as confirmed by realistic modeling of seismic ground motion. Il periodo di circa 1 s in corrispondenza del quale ci sono raddoppi delle coordinate spettrali sono particolarmente rilevanti per edifici in cemento armato (CA) di alcuni piani. Un esperimento effettuato a JRC-Ispra ha mostrato che un edificio tipo in CA, di circa 10mx10mx10m (tre piani), ha un periodo proprio di 1.3 s e non 0.3 s, come comunemente stimato in base a relazioni empiriche (Fardis, comm. Pers., 2004).

## CONCLUSIONI

La normativa rispecchia la sollecitazione sismica media della citta', ma non e' in grado di coprire ne' la sollecitazione derivante dal potenziale sismogenetico incombente (storia sismica e sismotettonica), ne' gli effetti locali che risultano alquanto rilevanti (almeno un grado  $I_{MCS}$  in piu') e riguardano zone abbastanza ampie (e.g. valli alluvionali).

In considerazione del deterioramento delle proprieta' meccaniche del sottosuolo (e.g. effetto acque sotterranee), negli ultimi cento anni, un terremoto simile a quello del Fucino puo' indurre in citta' valori di intensita' superiori a quelli osservati nel 1915.





**Journal of International Geoscience** 

### **Studied Cities:**

Algier **Bucharest** Cairo Debrecen Delhi Naples Bejing Russe Santiago de Cuba Thessaloniki Sofia Zagreb



Episodes

## International Working Group composed by about forty scientists:

Giuliano F. Panza (Chairman), Leonardo Alvarez, Abdelkrim Aoudia, Abdelhakim Ayadi, Hadj Benhallou, Djillali Benouar, Zoltan Bus, Yun-Tai Chen, Carmen Cioflan, Zhifeng Ding, Attia El-Sayed, Julio Garcia, Bartolomeo

Garofalo, Alexander Gorshkov, Katalin Gribovszki, Assia Harbi, Panagiotis Hatzidimitriou, Marijan Herak, Mihaela Kouteva, Igor Kuznetzov, Ivan Lokmer, Said Maouche, Gheorghe Marmureanu, Margarita Matova, Maddalena Natale, Concettina Nunziata, Imtyaz Parvez, Ivanka Paskaleva, Ramon Pico, Mircea Radulian, Fabio Romanelli, Alexander Soloviev, Peter Suhadolc, Győző Szeidovitz, Petros Triantafyllidis, Franco Vaccari.

### **UNESCO-IUGS-IGCP** Project

### Seismic microzoning of Naples



Modelling of seismic input (Torre del Greco)



Modelling of seismic input (Torre del Greco)















## Modelling of seismic input Several activities are presently in progress in many urban areas around the World.

• The realistic definition of hazard in scenario like format should be accompanied by the determination of advanced hazard indicators as, for instance, damaging potential. This can be achieved from a joint use of synthetic signals and available observations.

•A selection of main results is given in "Seismic ground motion in Large Urban Areas", Pageoph Topical Volume, 161, 2004, pp342, edited by Panza, Paskaleva and Nunziata





- Complementary to the definition of earthquake scenarios is a good knowledge of the geotechnical properties of the main constituents of the subsoil.
- The velocity models obtained from the inversion of refraction data, when used as input in waveform modelling, may cause a significant underestimate of the ground motion.

 Refraction of waves is a critical phenomenon. As such refracted waves carry very little energy, therefore they cannot be responsible of real damage.

• Damage is caused by reflected or surface waves, especially in soft soils.

 For microzonation purposes, the information obtainable from the inversion of surface waves dispersion is therefore preferable.

 S-wave velocities can be inferred from the inversion of Rayleigh and Love phase and group velocities determined with different techniques, like f(frequency)k(wavenumber), SASW and FTAN methods.



### **Inverted Models**



•Depth (m)






## Characterization of local soil mechanical properties

 For engineering geophysics FTAN method is particularly suitable and provides accurate group velocity measurements.

## Characterization of local soil mechanical properties

 When the elastic properties along the path are known, as well as the location and depth of the source, and fundamental and higher modes are excited, it is possible to determine the gross Q values along the path, by using the synthetic seismograms approach.



a), c) and e) fundamental, first higher mode and their sum extracted with FTAN; b), d) and f) synthetic signals





PHASE VELOCITY MEASUREMENTS?

#### group and phase velocity

#### Group and phase velocity can be defined as follows

 $U(\omega) = x/[t_o + d\phi_H(\omega)/d\omega - d\phi(\omega)/d\omega]$ (1)  $c = x/\{t_o + [f_H(\omega) - f(\omega) \pm 2\pi N]/\omega\}$ (2)

where x is the distance source receiver,  $t_0$  the difference between the origin time and the starting time of the analysed signal,  $\phi_H$  and  $\phi$  are respectively the phase of the recorded signal and the source apparent initial phase, at the frequency  $\omega$ , and N is an integer that can only be determined empirically.

As a rule  $\phi(\omega)$  is a weak function of  $\omega$ , thus  $d\phi(\omega)/d\omega$  can be considered negligible for practical purposes. On the other side, especially at short periods, the determination of N can be very problematic.

group and phase velocity

To eliminate the dependence of the phase velocity from the apparent initial phase of the source,  $\phi(\omega)$ , the so called two-station method can be applied:

 $c = \delta x / [\delta t_o + (\delta \phi_H(\omega) \pm 2\pi \delta N) / \omega]$  (3) where  $\delta x$ ,  $\delta t_o$ ,  $\delta \phi_H(\omega)$  and  $\delta N$  indicate the difference between the quantities appearing in (2) as measured at the two stations. For more details see e.g. Panza (1976).

# THE END

### THANK YOU FOR YOUR ATTENTION