



The Abdus Salam  
International Centre for Theoretical Physics



Spring Colloquium on  
**'Regional Weather Predictability and Modeling'**  
**April 11 - 22, 2005**

- 1) *Workshop on Design and Use of Regional Weather Prediction Models, April 11 - 19*
- 2) *Conference on Current Efforts Toward Advancing the Skill of Regional Weather Prediction. Challenges and Outlook, April 20 - 22*

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Information content in ensemble data assimilation

**D. Zupanski**  
Cooperative Institute for Research in the Atmosphere, CSU, Ft. Collins  
USA



# Information content in ensemble data assimilation

Dusanka Zupanski  
CIRA/Colorado State University, Fort Collins, CO

Conference on  
*Current Efforts Toward Advancing the Skill of Regional Weather  
Prediction Challenges and Outlook*  
April 11-22, 2005  
ICTP, Trieste, Italy

## Collaborators

- M. Zupanski, L. Grasso, Scott Denning Group (Colorado State University)
- A. Y. Hou, S. Zhang (NASA/GMAO)
- M. DeMaria (NOAA/NESDIS)

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Dusanka Zupanski, CIRA/CSU  
Zupanski@CIRA.colostate.edu

# OUTLINE

- Challenges of advancing skill of regional weather prediction
- Link between information theory and ensemble data assimilation
- Experimental results
- Conclusions and future work

# Challenges of advancing skill of regional weather prediction

➤ Employ state-of-the-art non-linear atmospheric models (without neglecting model errors)

➤ Assimilate observations with high spatial and temporal resolution

➤ Calculate analysis and forecast uncertainty

Ensemble  
data  
assimilation

➤ Determine amount of new information given by the observations

➤ Quantify predictability (calculate entropy reduction)

Information  
theory

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Can we define a link between ensemble data assimilation and information theory?

# METHODOLOGY

## Maximum Likelihood Ensemble Filter (MLEF)

*(Zupanski 2005; Zupanski and Zupanski 2005)*

### Developed using ideas from

- Variational data assimilation (3DVAR, 4DVAR)
- Iterated Kalman Filters
- Ensemble Transform Kalman Filter (ETKF, Bishop et al. 2001)

### MLEF is designed to provide optimal estimates of

- model state variables
- empirical parameters
- model error (bias)

**MLEF also calculates uncertainties of all estimates (in terms of  $P_a$  and  $P_f$ )**

# MLEF APPROACH

Minimize cost function  $J$

$$J = \frac{1}{2}[\mathbf{x} - \mathbf{x}_b]^T \mathbf{P}_f^{-1}[\mathbf{x} - \mathbf{x}_b] + \frac{1}{2}[H(\mathbf{x}) - \mathbf{y}_{obs}]^T \mathbf{R}^{-1}[H(\mathbf{x}) - \mathbf{y}_{obs}] = \min$$

Analysis error covariance

$$\mathbf{P}_a^{1/2} = \mathbf{P}_f^{1/2} (\mathbf{I} + \mathbf{C})^{-1/2}$$

Link between information theory and ensemble data assimilation

$$\mathbf{C} = \mathbf{P}_f^{T/2} \mathbf{H}^T \mathbf{R}^{-1} \mathbf{H} \mathbf{P}_f^{1/2} = (\mathbf{R}^{-1/2} \mathbf{H} \mathbf{P}_f^{1/2})^T (\mathbf{R}^{-1/2} \mathbf{H} \mathbf{P}_f^{1/2})$$

Forecast error covariance

$$\mathbf{P}_f^{1/2} = [p_1^f \quad p_2^f \quad \dots \quad p_{Nens}^f]$$

$$p_i^f = M(x + p_i^a) - M(x)$$

$\mathbf{x}$  - model state vector of dim  $Nstate \gg Nens$

$M$  - non-linear forecast model

$\mathbf{C}$  - information matrix of dim  $Nens \times Nens$

# EXPERIMENTAL DESIGN

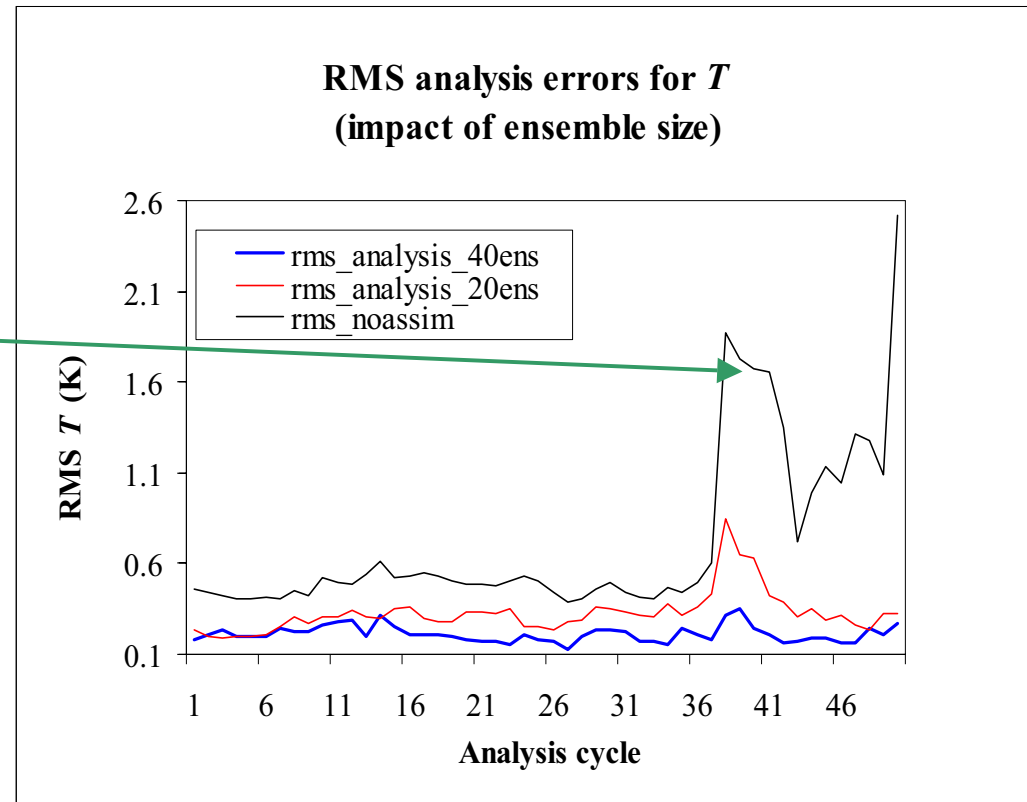
- **NASA GEOS-5 column precipitation model**
- **Tropical Western Pacific site (130E,15N)**
- **50 6-h DA cycles: 00UTC 7 May 1998- 00 UTC 17 May 1998**
- **40 vertical layers**
- **Control variable: T, q (dim=80)**
- **Model simulated observations with random noise (80 obs per DA cycle)**
- **Nens=40**
- **Iterative minimization of J (1 iteration only)**

## RESULTS using GEOS-5 column model

RMS errors of temperature with respect to the “truth”

Largest errors in the experiment without assimilation in last 13 cycles.

Data assimilation reduces RMS errors, by using information from observations.





# RESULTS using GEOS-5 column model

## Information matrix

$$C = P_f^{T/2} H^T R^{-1} H P_f^{1/2} = (R^{-1/2} H P_f^{1/2})^T (R^{-1/2} H P_f^{1/2})$$

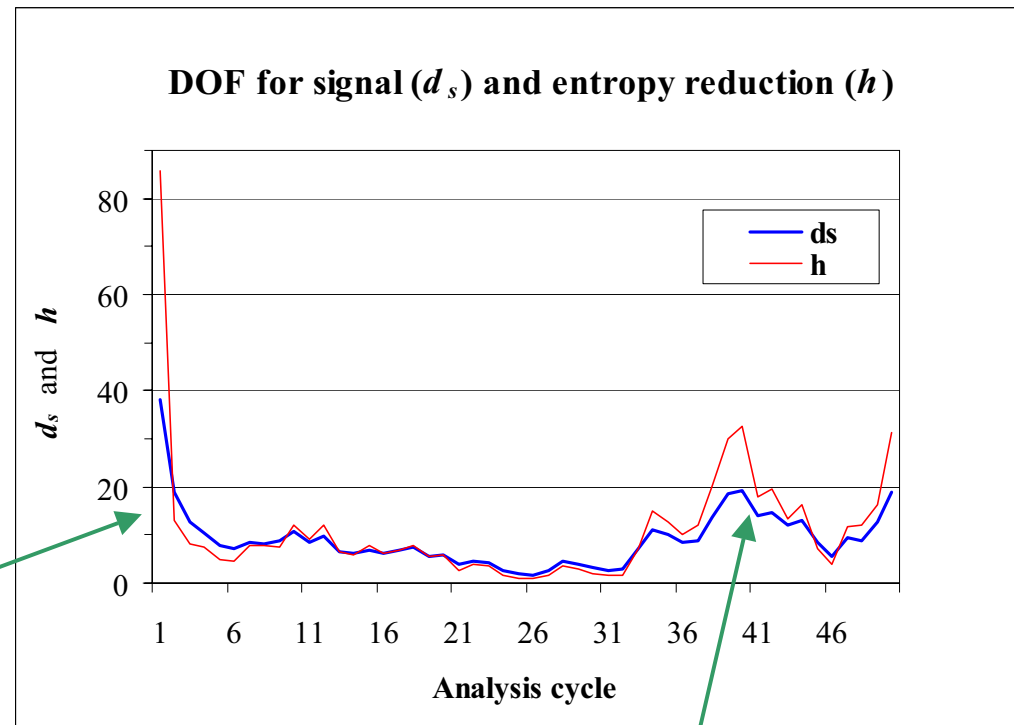
## Degrees of freedom (DOF) for signal

$$d_s = \text{tr}[(I + C)^{-1} C] = \sum_i \frac{\lambda_i^2}{1 + \lambda_i^2}$$

Shannon information content,  
or entropy reduction  
(used for quantifying predictability)

$$h = \frac{1}{2} \sum_i \ln(1 + \lambda_i^2)$$

Inadequate  $P_f$  at  
the beginning of  
data assimilation

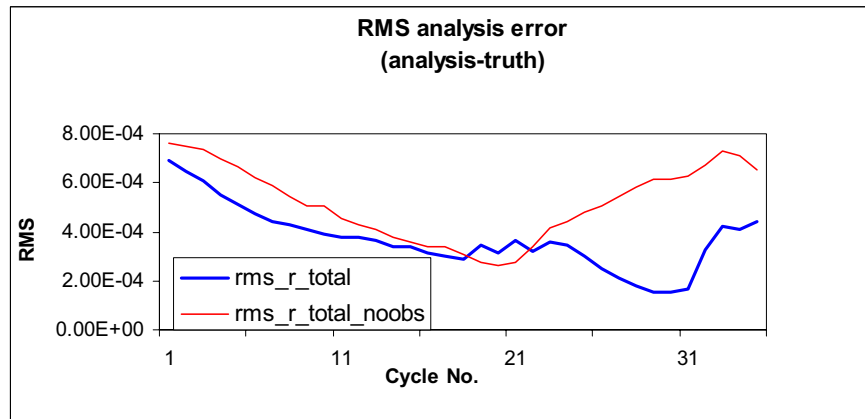
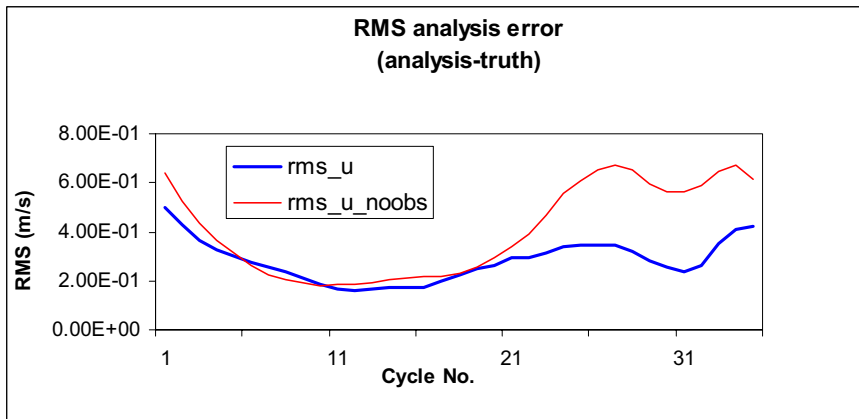
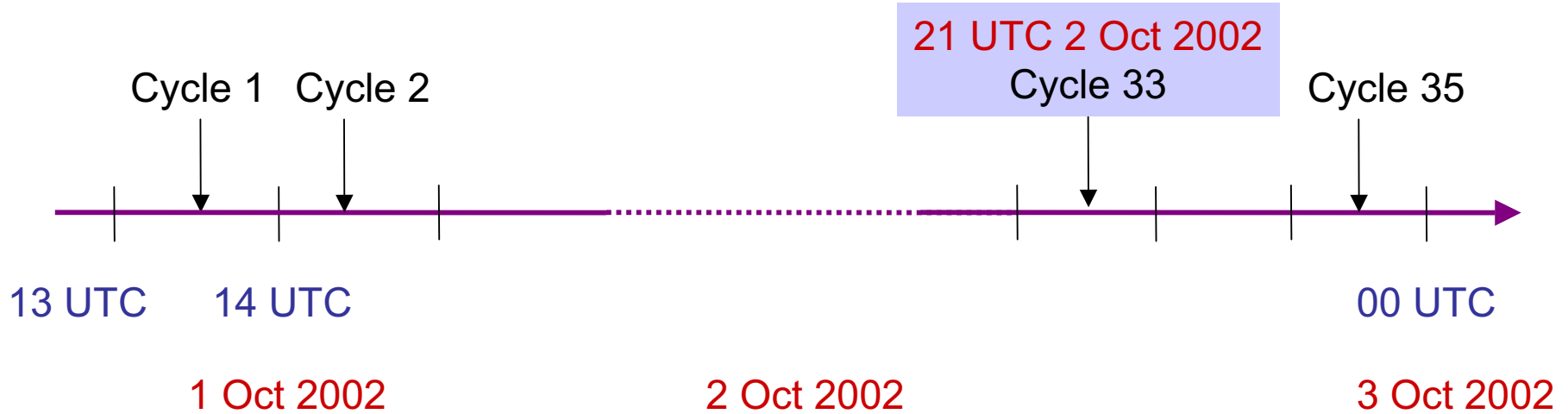


New observed information

# EXPERIMENTAL DESIGN

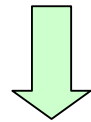
- **CSU-RAMS non-hydrostatic model**
- **Hurricane Lili case**
- **35 1-h DA cycles: 13UTC 1 Oct 2002 – 00 UTC 3 Oct**
- **30x20x21 grid points, 15 km grid distance (in the Gulf of Mexico)**
- **Control variable: u,v,w,theta,Exner, r\_total (dim=54000)**
- **Model simulated observations with random noise (7200 obs per DA cycle)**
- **Nens=50**
- **Iterative minimization of J (1 iteration only)**

# Experimental design (continued)

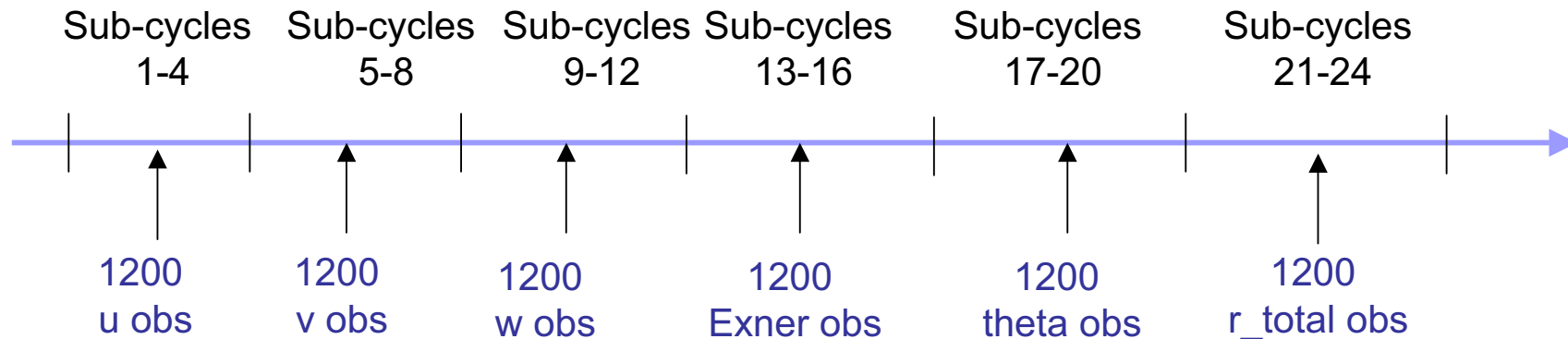


## Experimental design (continued)

- Split cycle 33 into 24 sub-cycles
- Calculate eigenvalues of  $(I+C)^{-1/2}$  in each sub-cycle (information content)

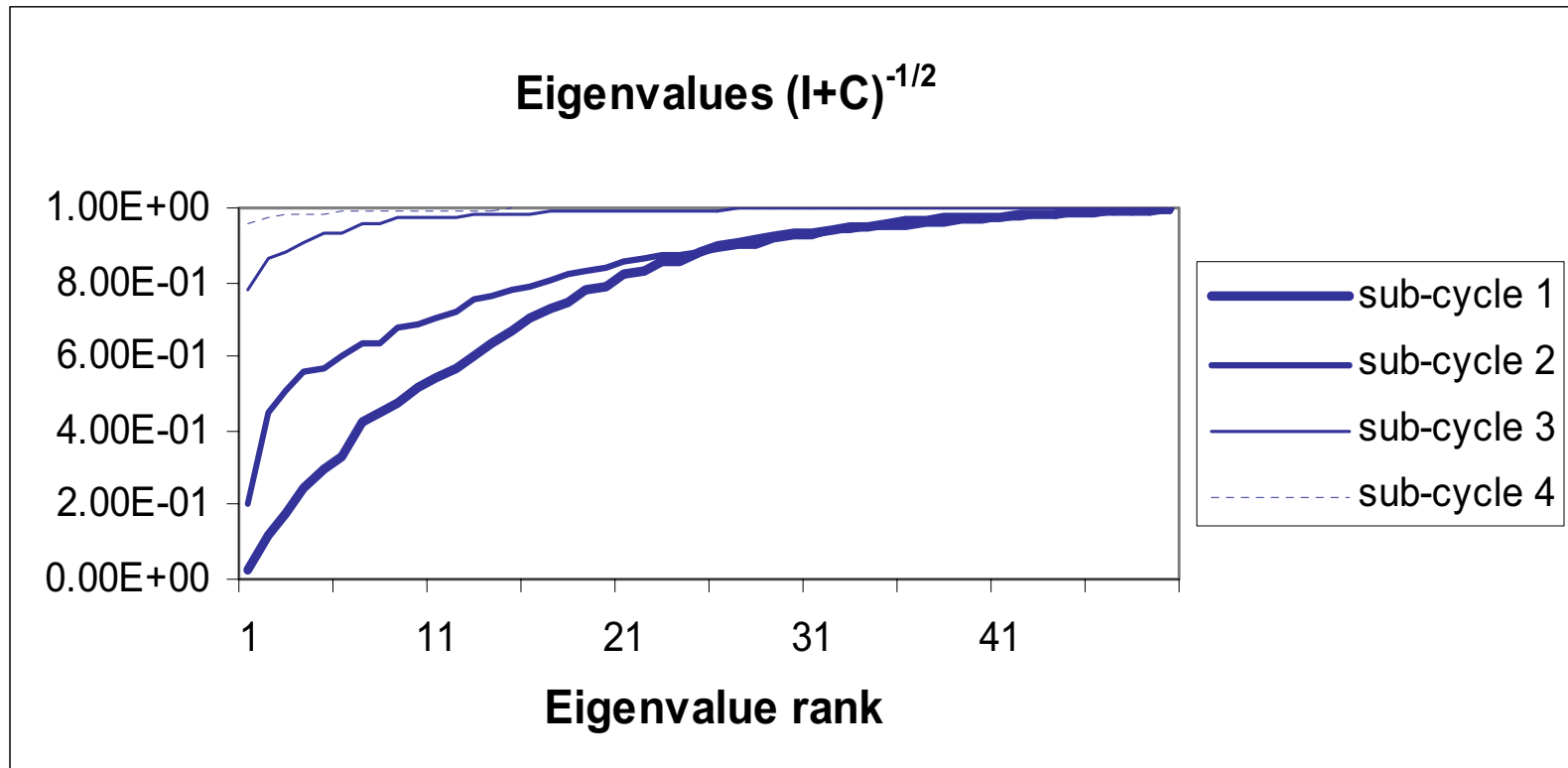


### Information content of each group of observations



# RESULTS using RAMS model

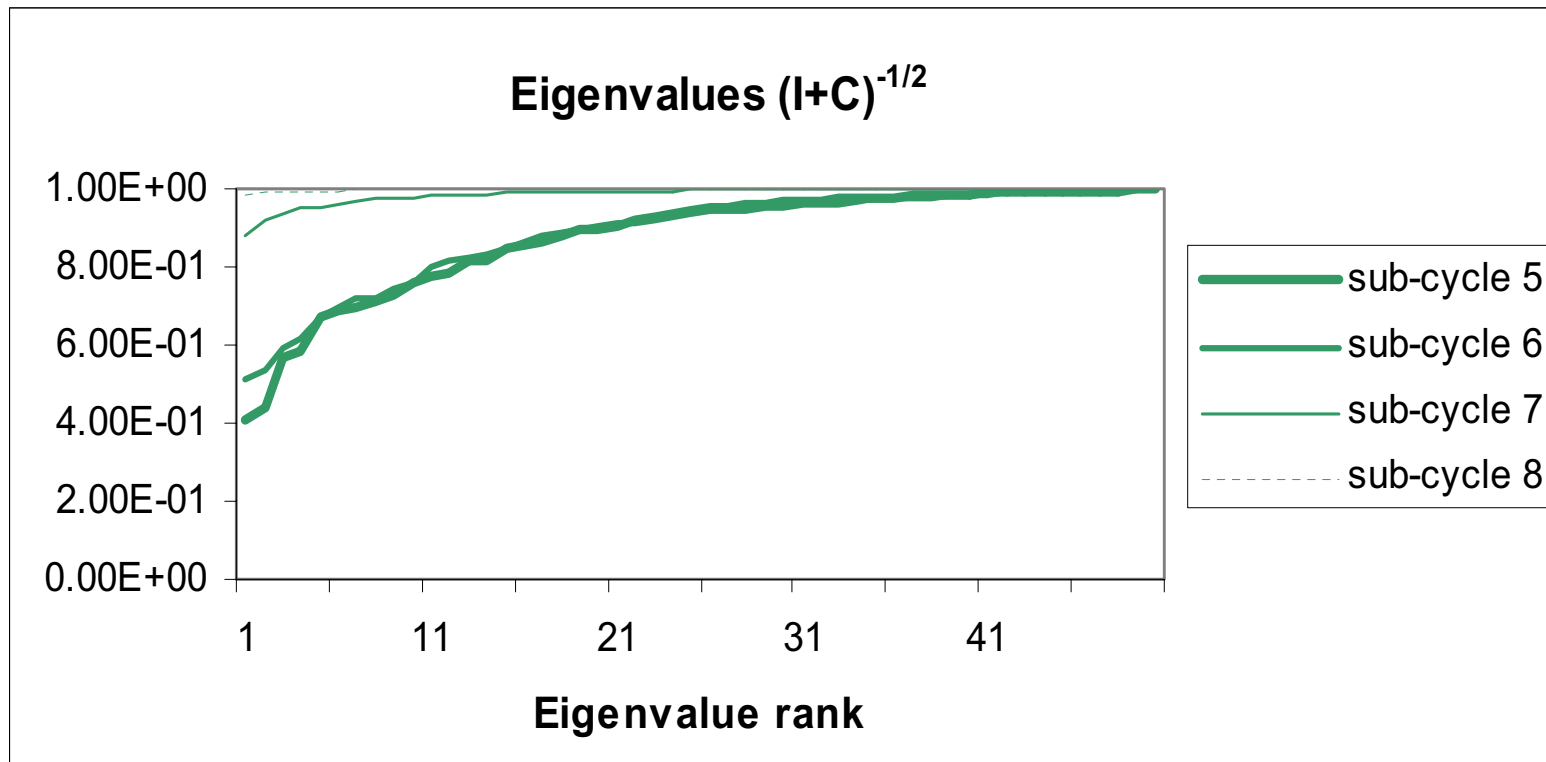
## Sub-cycles 1-4 u- obs groups



System is “learning” about the truth via updating analysis error covariance.

# RESULTS using RAMS model

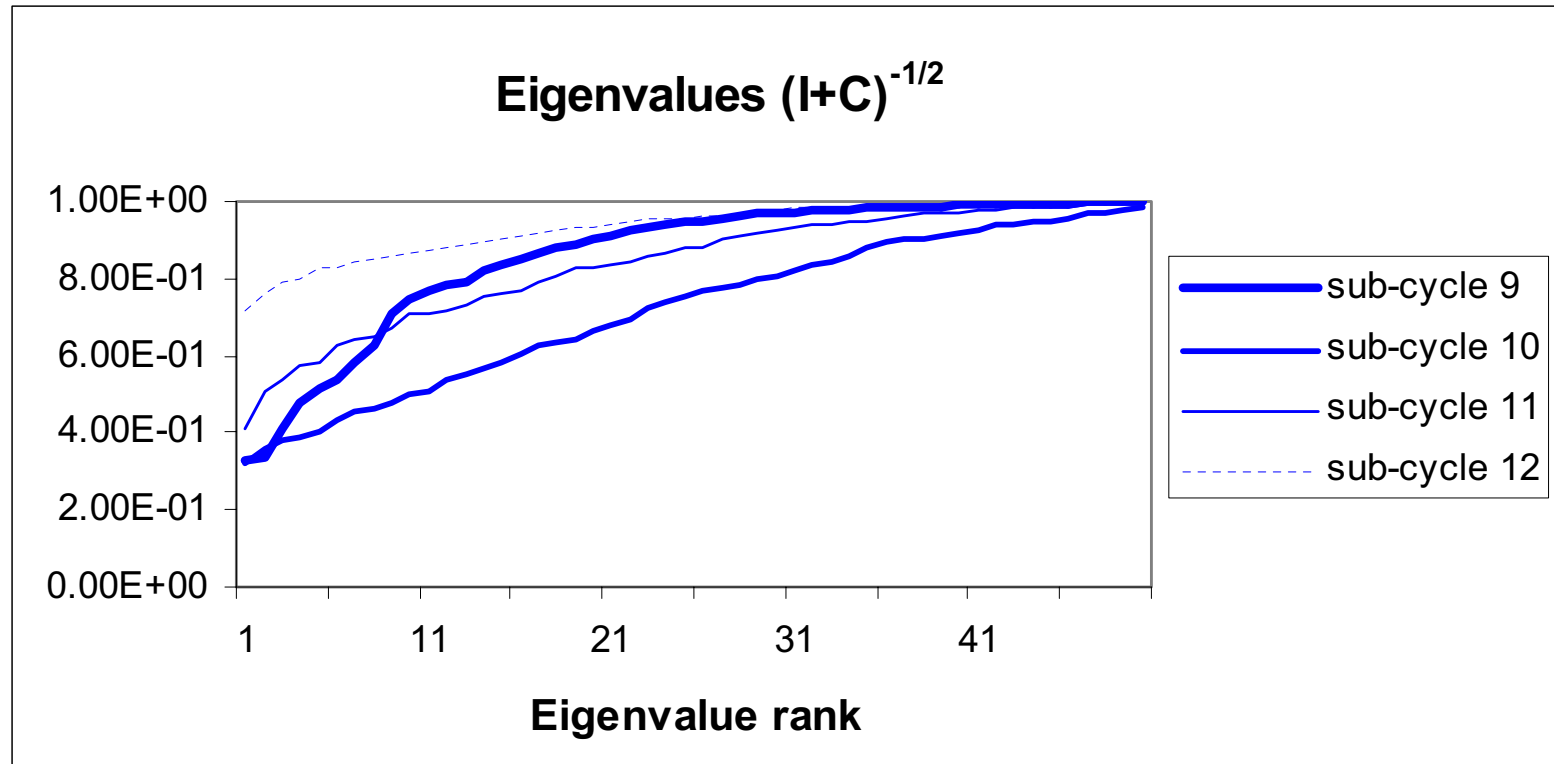
## Sub-cycles 5-8 v- obs groups



**Most information in sub-cycles 5 and 6.**

# RESULTS using RAMS model

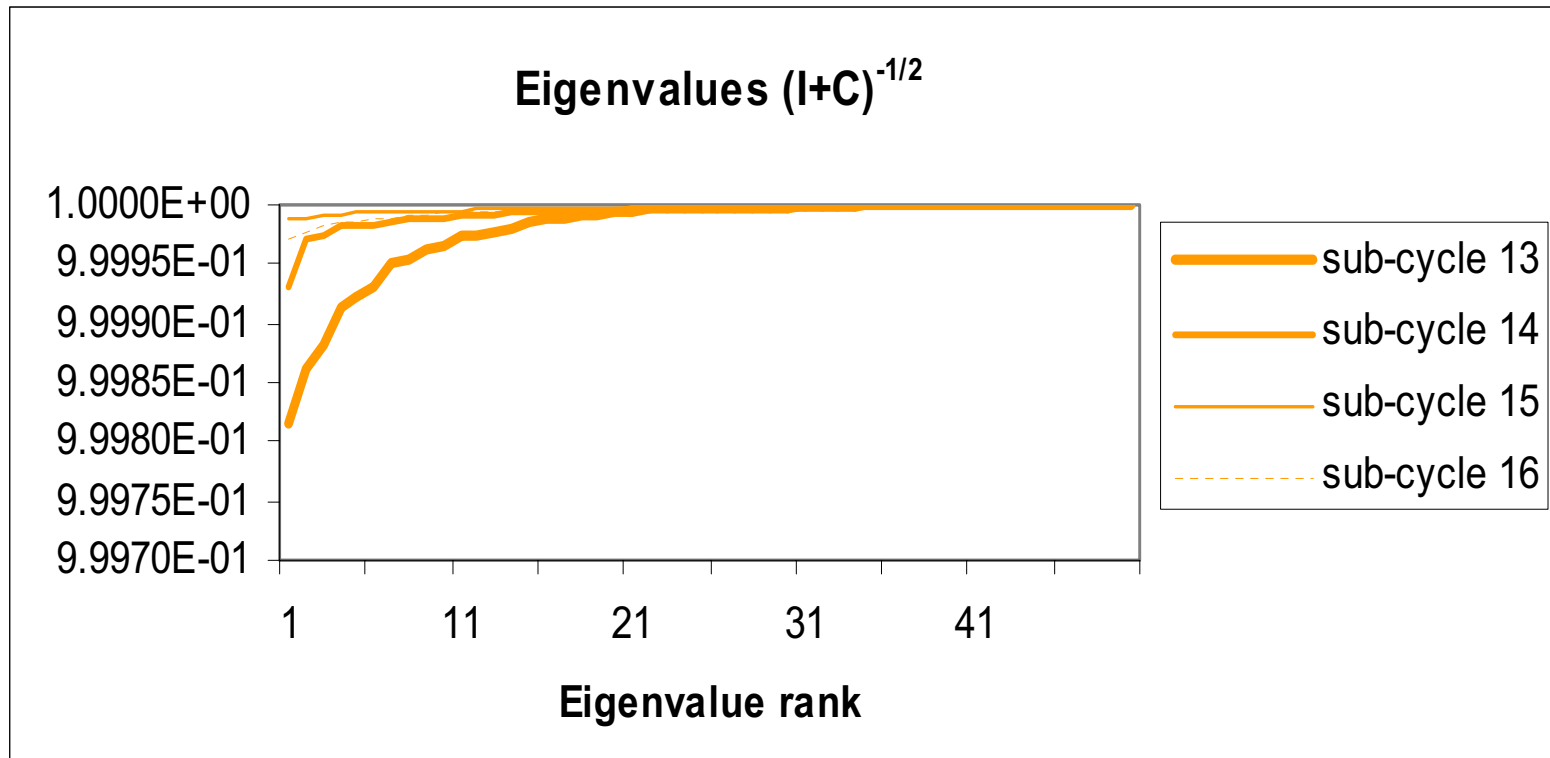
Sub-cycles 9-12  
w- obs groups



**Most information in sub-cycle 10.**

# RESULTS using RAMS model

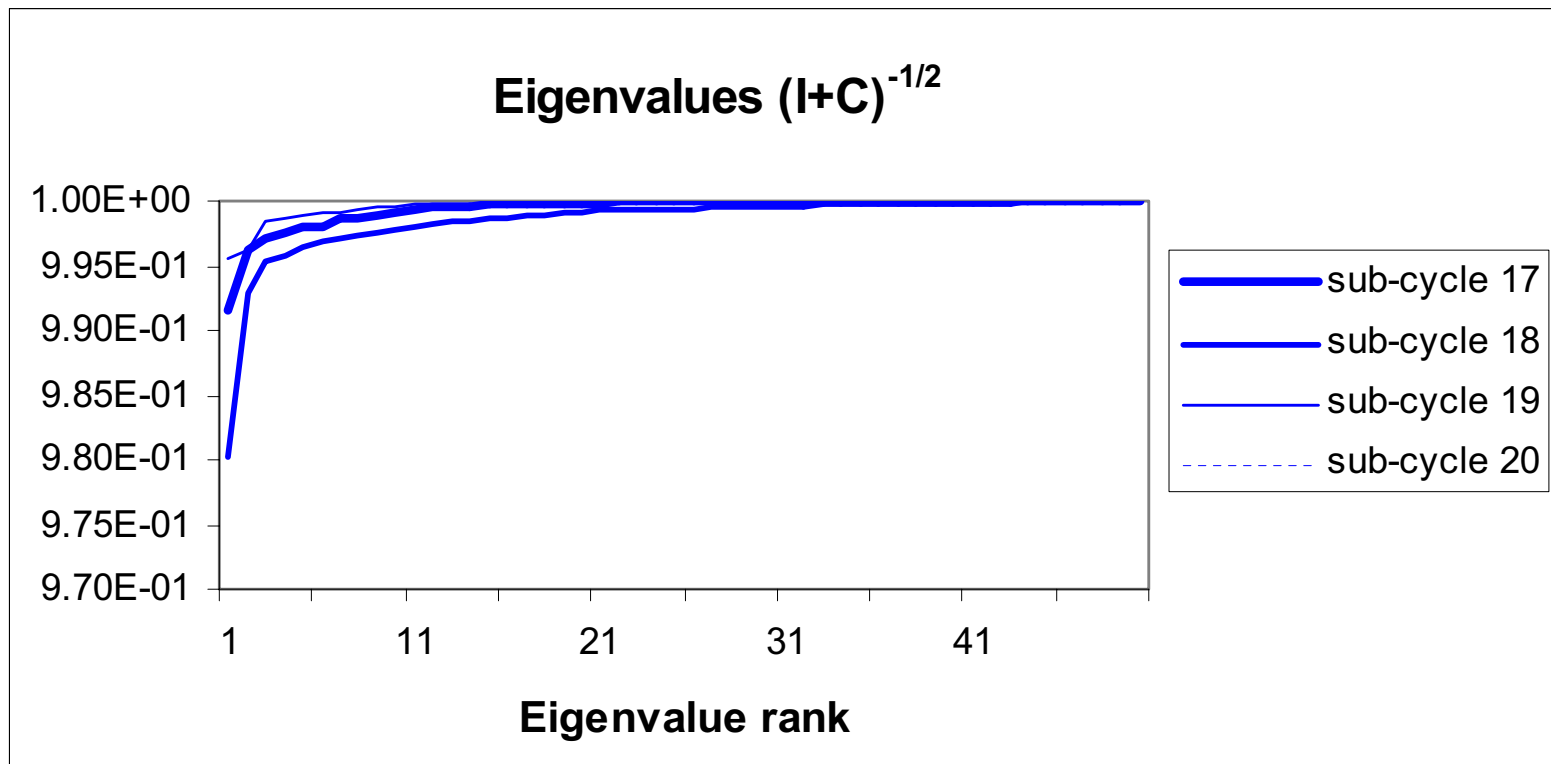
## Sub-cycles 13-16 Exner- obs groups





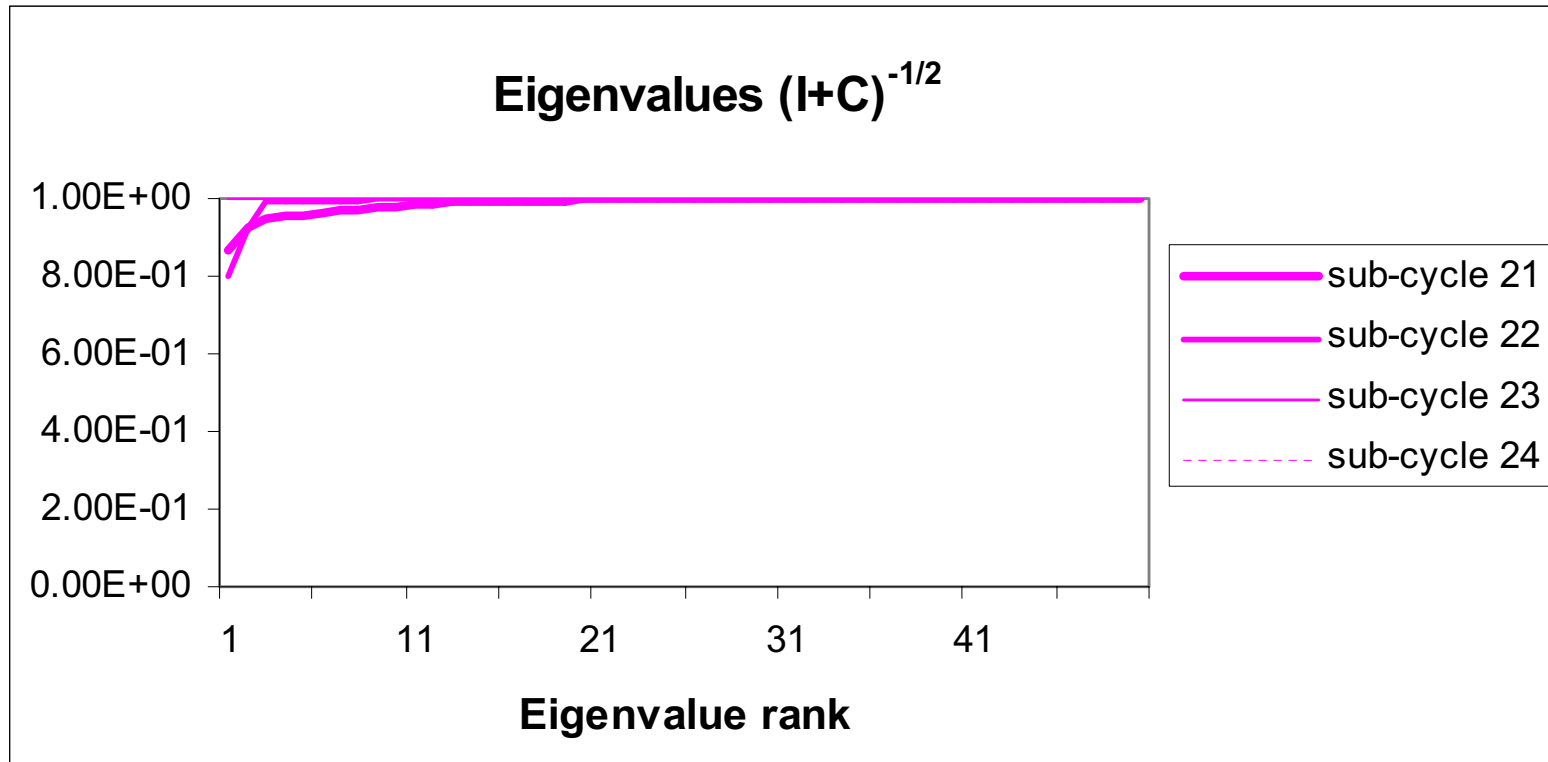
# RESULTS using RAMS model

Sub-cycles 17-20  
theta- obs groups



# RESULTS using RAMS model

Sub-cycles 21-24  
theta- obs groups



Sub-cycles with little information can be excluded  $\Rightarrow$  data selection.

## CONCLUSIONS

- The proposed general framework can be effectively used to quantify information content of various observations.
- Measures of predictability, such as entropy reduction, can also be calculated.
- The framework is applicable to a forecast model of any complexity. Only eigenvalues of a small size matrix ( $N_{ens} \times N_{ens}$ ) need to be evaluated.
- Data assimilation system has a capability to learn from observations.

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Ensemble data assimilation linked with information theory is a powerful approach for addressing challenging issues of regional weather prediction.