



## 1<sup>st</sup> Teaching Workshop on Environmental Economics

for the Middle East and North Africa

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### Valuation Approches

*Mordechai Shechter*

*University of Haifa*

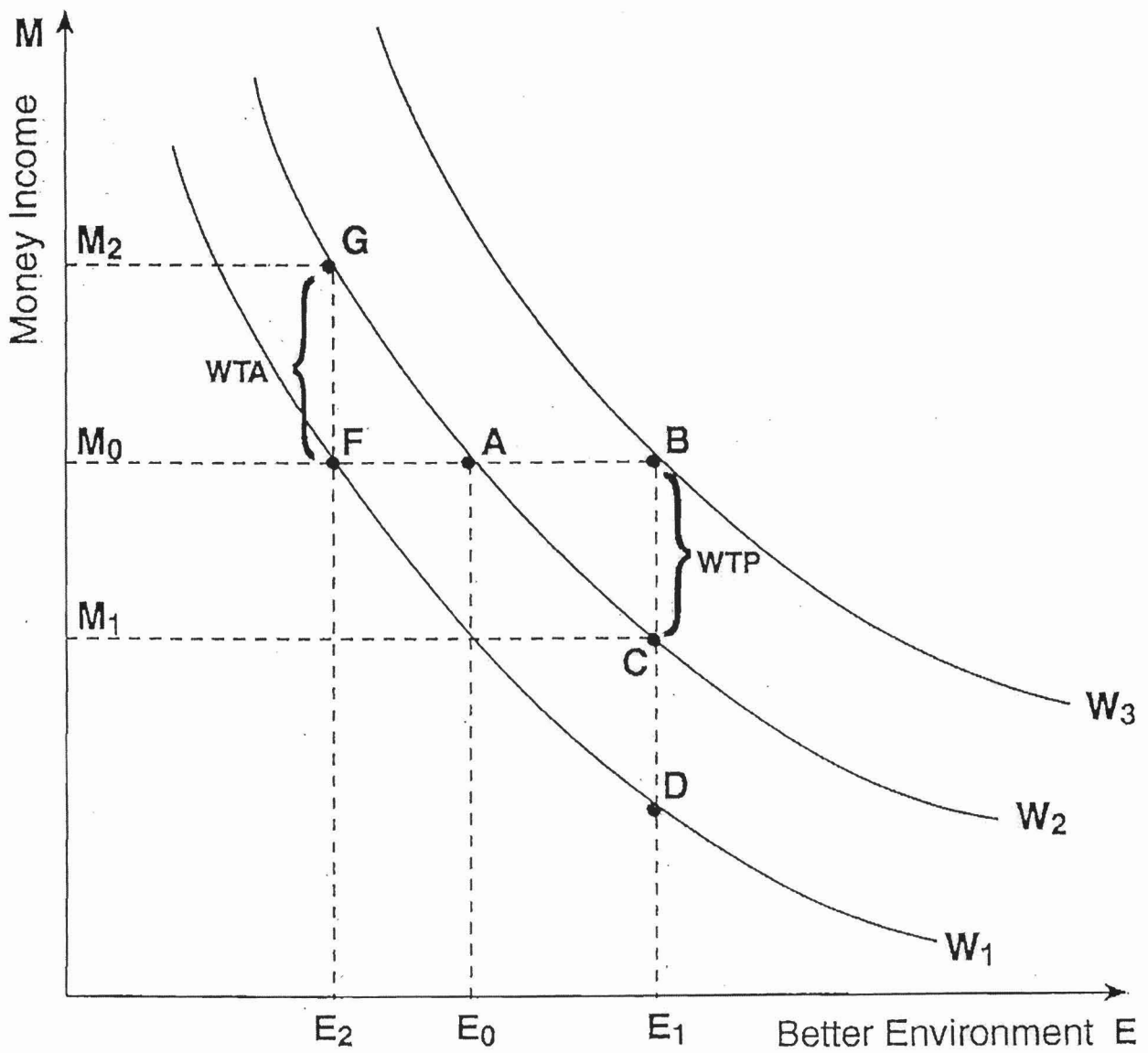
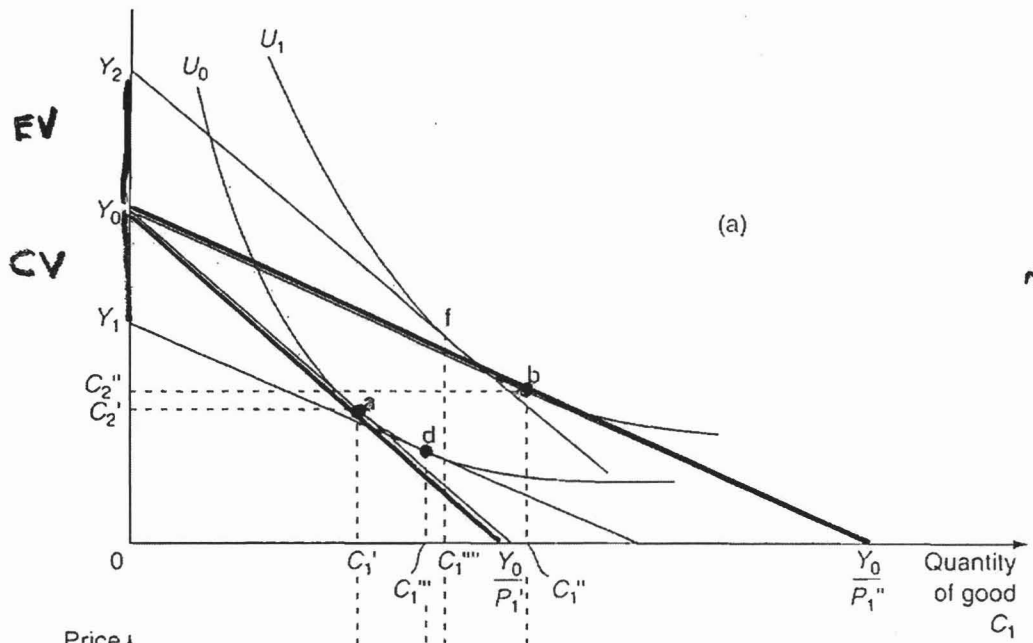
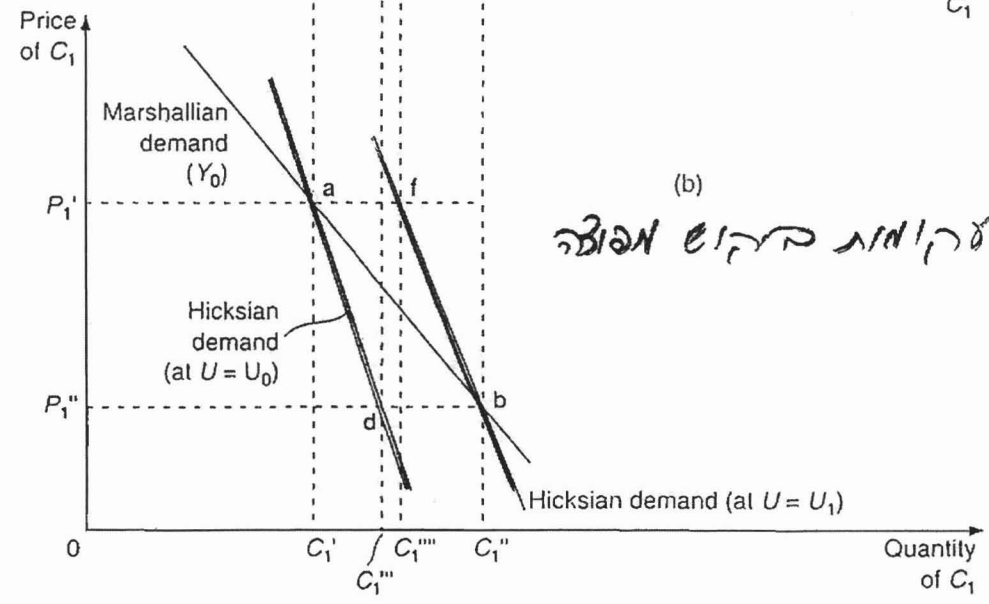


Figure 1: Translating preferences into monetary values

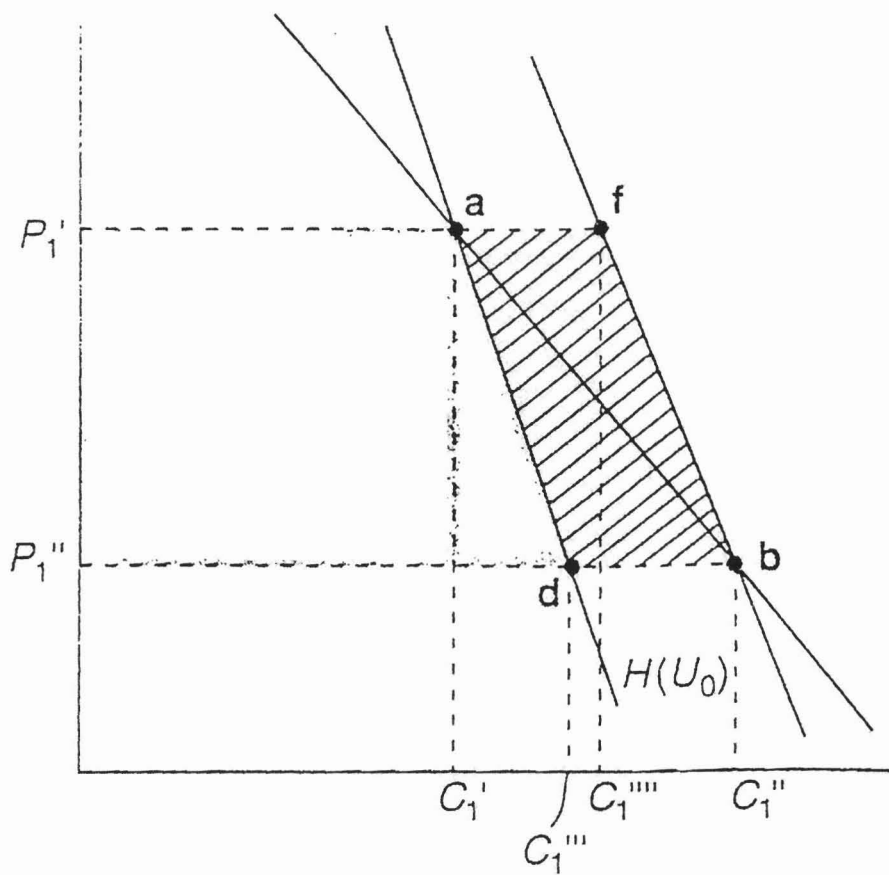


יכולים להיות  
 קצת יותר סוף  
 $P_1' \rightarrow P_1''$   
 $C_1' - C_1'''$  ונתחילה  
 $C_1''' - C_1''$  עלתה הריבוי



עקומות קצוות אלו

Figure 14.3 (a) The compensating variation of a price fall. (b) Hicksian and Marshallian demands.



For a fall in the price of  $C_2$ :

$$CV = \int_{P_1''}^{P_1'} H(U_0) dP = \text{shaded area}$$

$$EV = \int_{P_1''}^{P_1'} H(U_1) dP = \text{shaded area} + \text{hatched area}$$

Figure 14.4 Compensating variation and equivalent variation.

Table 14.2 Monetary measures for price change effects.

	CV	EV
Price fall	WTP for the change occurring	WTA compensation for the change not occurring
Price rise	WTA compensation for the change occurring	WTP for the change not to occur

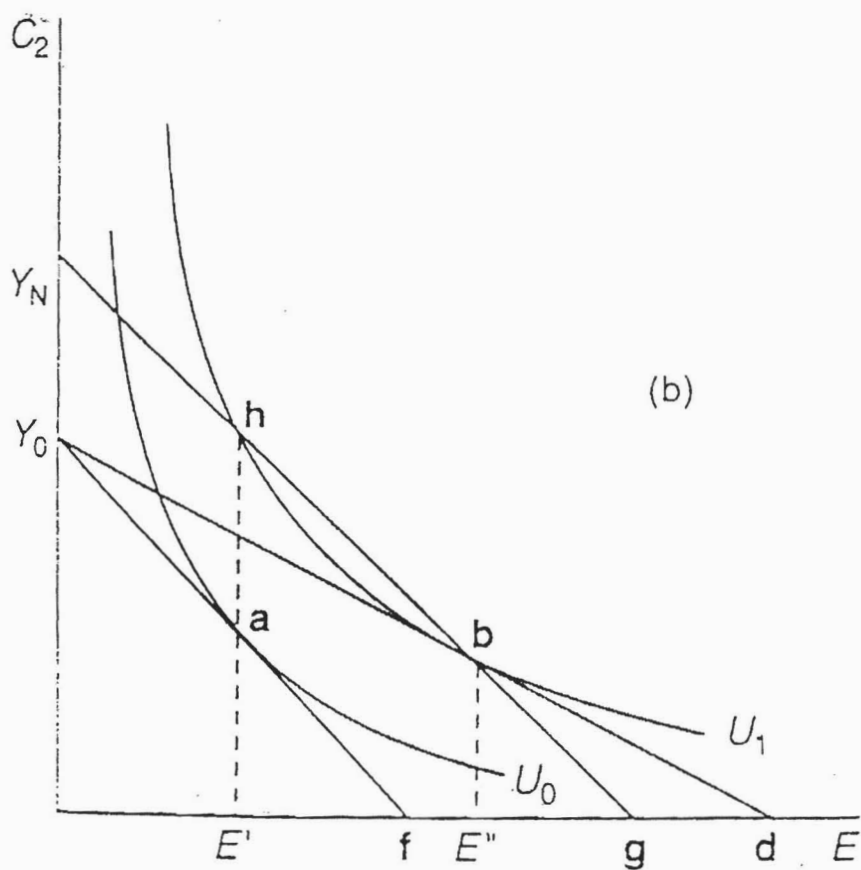
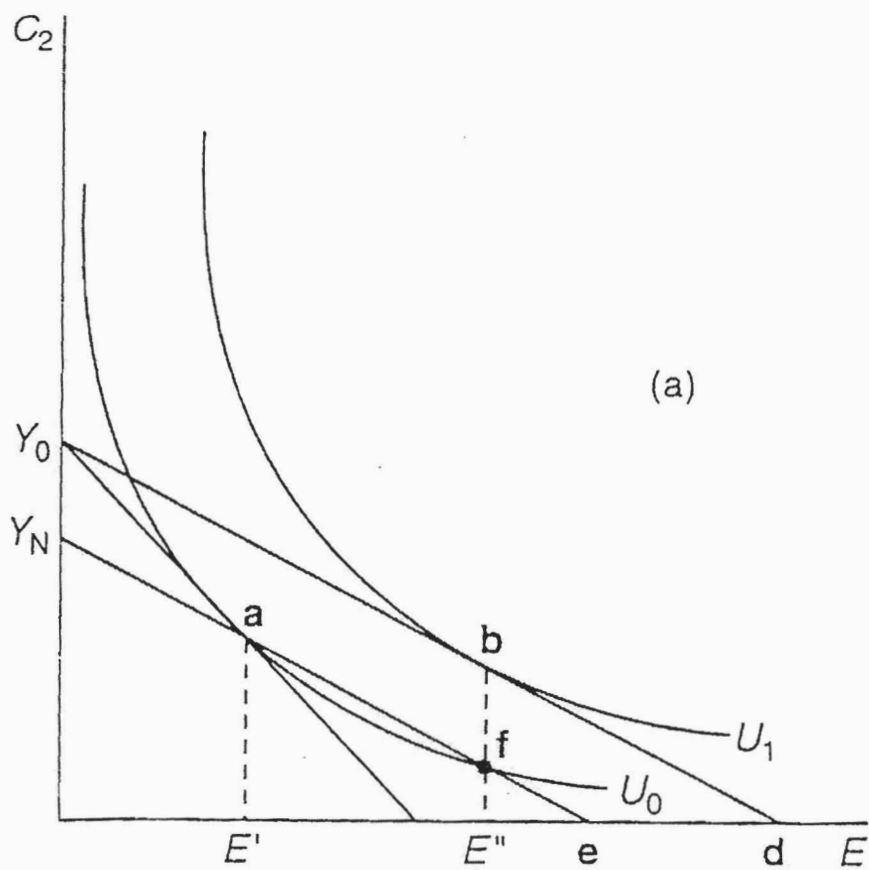


Figure 14.5 Equivalent and compensating surplus.

Table 14.3 Monetary measures for environmental quality changes.

	CS	ES
Improvement	WTP for the change occurring	WTA compensation for the change not occurring
Deterioration	WTA compensation for the change occurring	WTP for the change not to occur

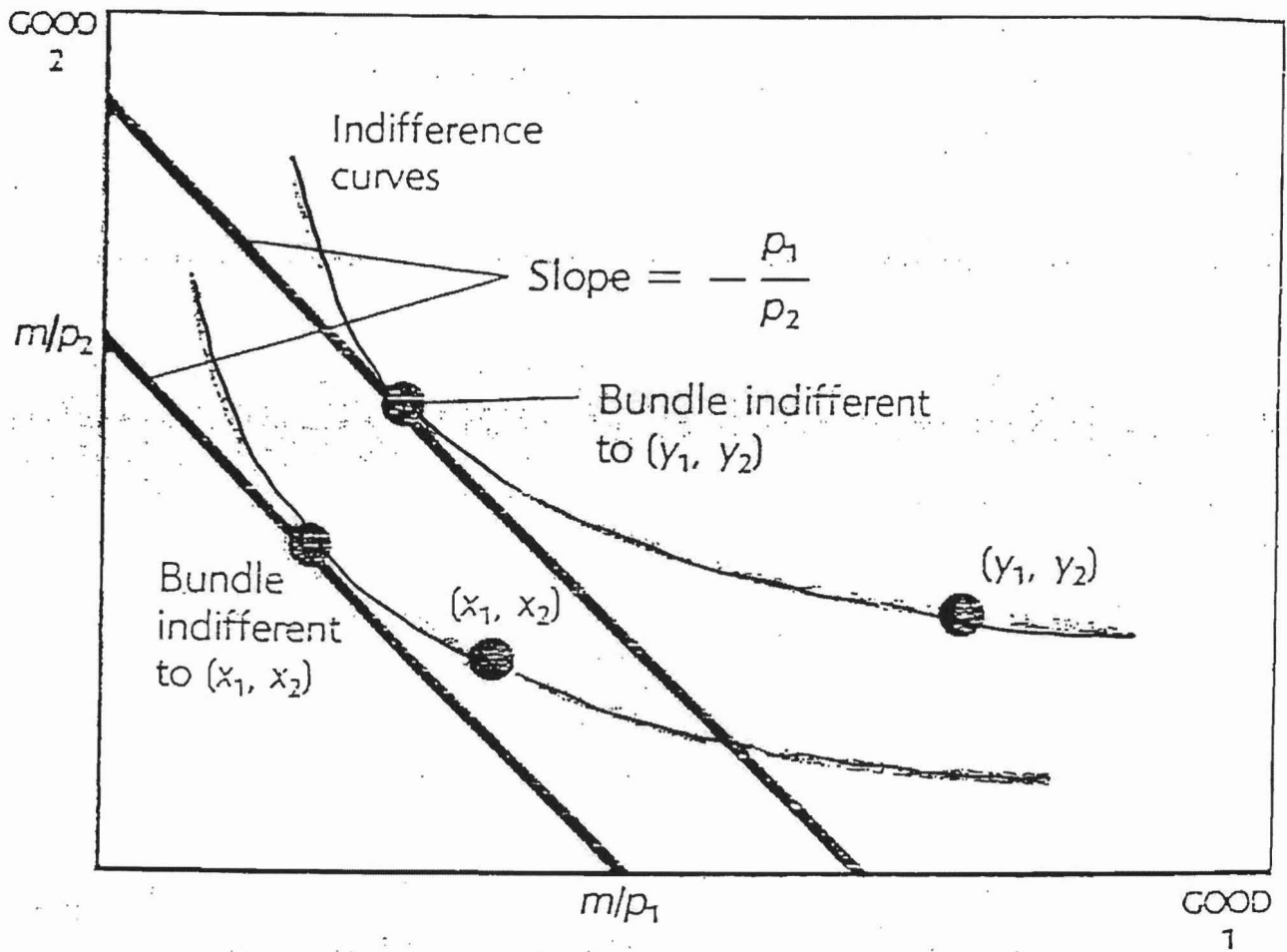
### Money Metric Utility Function

$$m(p_1, p_2, x_1, x_2)$$

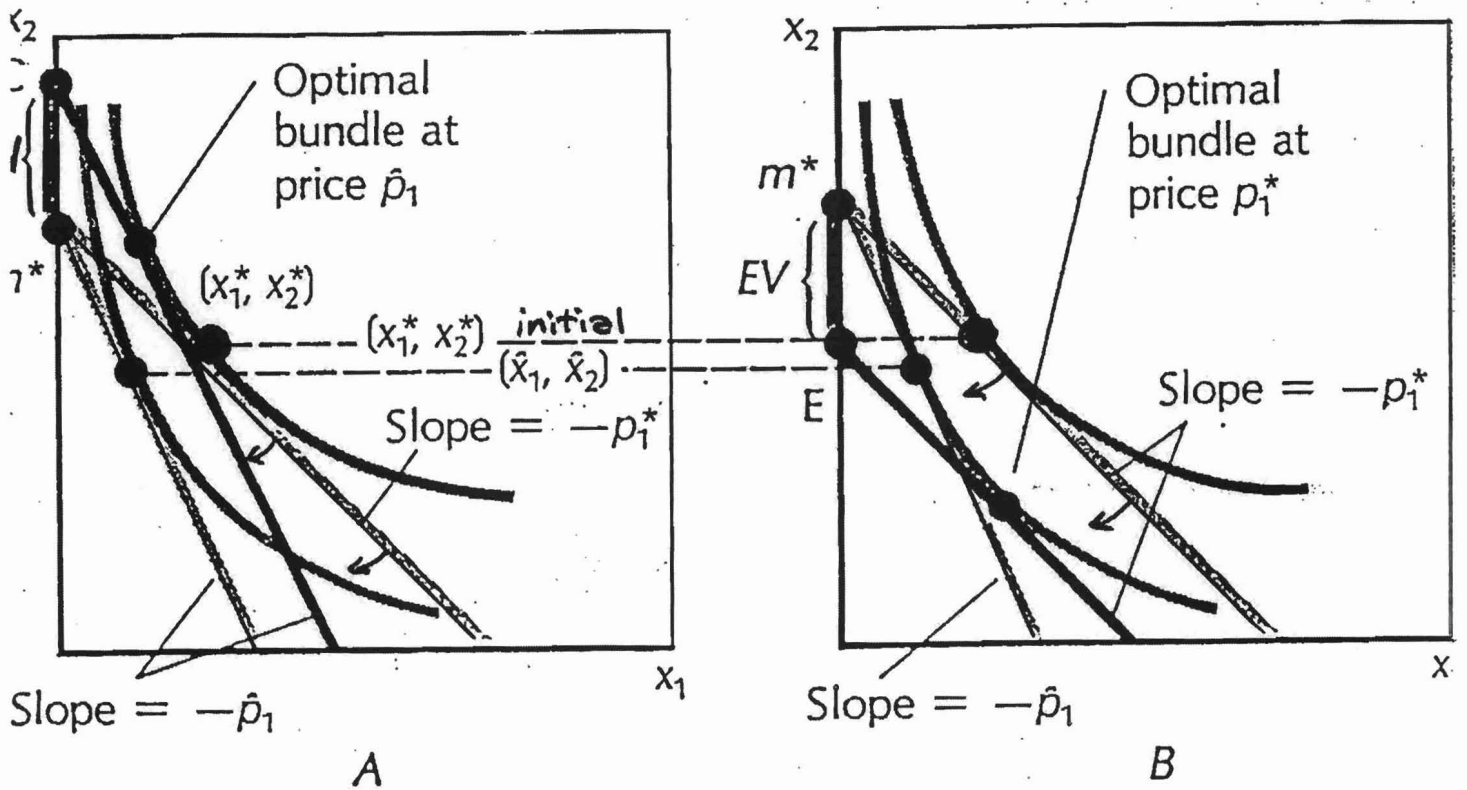
The amount of money that a consumer would need at prices  $(p_1, p_2)$  to be as well-off as he would be consuming the bundle  $(x_1, x_2)$ .

In *some* sense, it represents the monetary value of the consumption bundle  $(x_1, x_2)$  to the consumer.





The money metric utility function. The vertical intercept times  $p_2$  measures the amount of money necessary at prices  $(p_1, p_2)$  to purchase a bundle that is just as good as  $(x_1, x_2)$  according to this consumer's preferences.



The compensating and the equivalent variations. Panel A shows the compensating variation (CV) and panel B shows the equivalent variation (EV).

**Compensating Variation:** measures the change in income that will just *compensate* the consumer for the posited change (in price or quantity) - and will restore him to his *original* indifference curve *after* the change had taken place.

**Equivalent Variation:** measures the change in income that is *equivalent* (in utility terms) to the posited change - and will move him to the final indifference curve *in lieu* of that change.

$$u = u(x_1, x_2) = x_1^{1/2} x_2^{1/2} \quad a = 1/2$$

$$p^0 = (p_1^0, p_2^0) = (1, 1)$$

$$m = 100$$

$$p_1 \uparrow \rightarrow p_1 = 2$$

$$\text{Demand: } x_1 = x_1(p_1, p_2, m) = m/2p_1 \quad \left(\frac{1/2 \cdot m}{p_1}\right)$$

$$x_2 = x_2(p_1, p_2, m) = m/2p_2 \quad \left(\frac{1/2 \cdot m}{p_2}\right)$$

$$\Rightarrow x_1^0 = 50 \quad x_2^0 = 50$$

$$x_1^1 = 25 \quad x_2^1 = 50$$

$$\text{CV: At } p^1 = (2, 1) \quad x^1 = (m/4, m/2)$$

$$\text{At } p^0 = (1, 1) \quad x^0 = (50, 50)$$

$$\left(\frac{m}{4}\right)^{1/2} \left(\frac{m}{2}\right)^{1/2} = 50^{1/2} 50^{1/2}$$

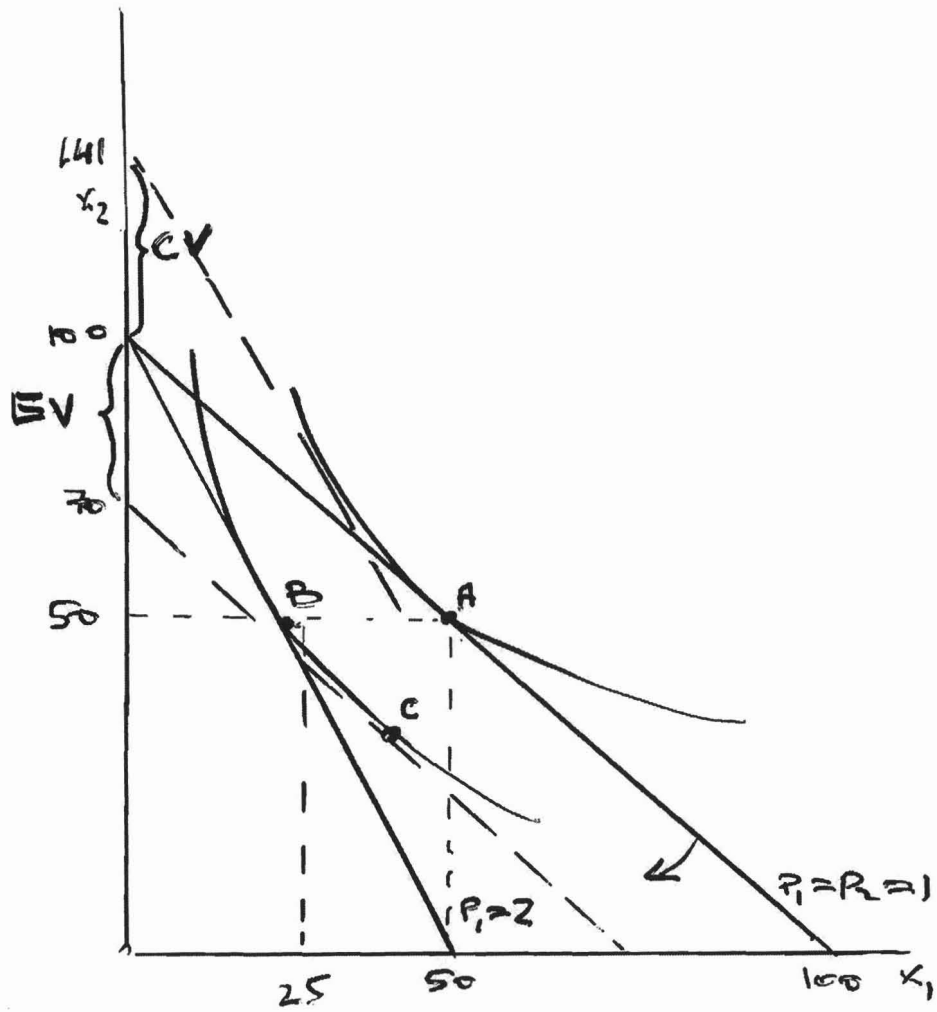
$$m = 100\sqrt{2} \approx 141 \Rightarrow \boxed{\text{CV} = 41}$$

$$\text{EV: } \left(\frac{m}{2}\right)^{1/2} \left(\frac{m}{2}\right)^{1/2} = 25^{1/2} 50^{1/2}$$

$$m = 50\sqrt{2} = 70 \quad \boxed{\text{EV} = 30}$$

money metric utility:

$$m(\cdot) = \left(\frac{p_1}{a}\right)^a \left(\frac{p_2}{1-a}\right)^{1-a} x_1^a x_2^{1-a} = \left(\frac{2}{1/2}\right)^{1/2} \left(\frac{1}{1/2}\right)^{1/2} \left[50^{1/2} \cdot 50^{1/2}\right] = 100\sqrt{2}$$



## From Theory to Measurement

The exploitation of possible relationships between environmental goods and private goods leads to several empirical techniques for estimating environmental and resource values.

These techniques have the following characteristics:

1. They are consistent with the basic theory of demand and consumer preferences;
2. They provide a means for estimating the indirect utility function, the expenditure function, or the compensated demand function for the environmental service;
3. They are practical in the sense of imposing realistic data and computational requirements.

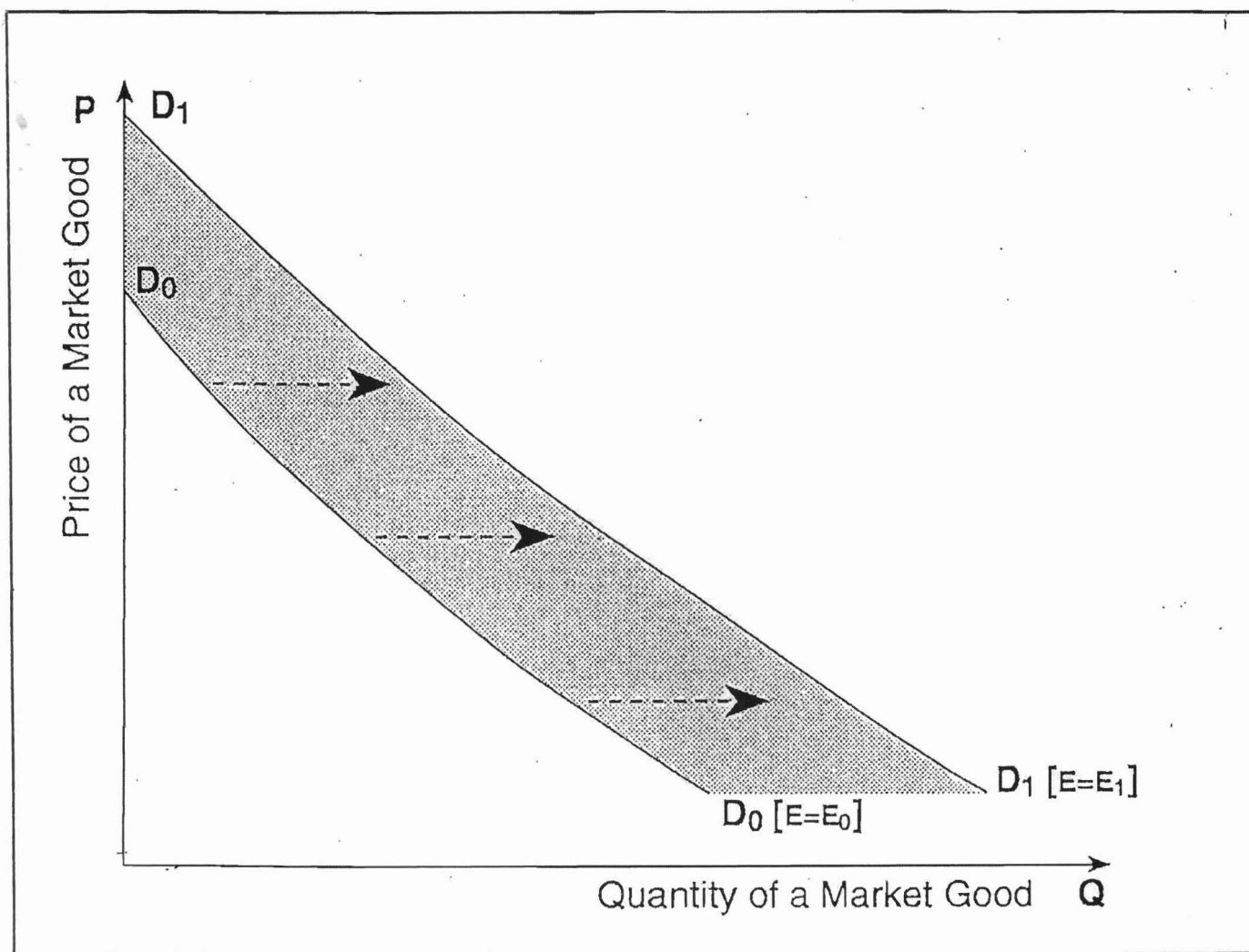


Figure 2: Measuring environmental benefits from shifts in the demand for a market good

### Environmental Quality as a Factor Input

When  $E$  is a factor of production, changes in  $E$  lead to changes in production costs which in turn affect the price and quantity of output or the returns to other factors of production, or both.

The benefits of changes in  $E$  can be inferred from these changes in *observable* market data.

Assume that  $x$  is produced with a production function

$$x = x(k, l, \dots, E)$$

where  $k$  and  $l$  are capital and labor, and where  $\delta x / \delta E > 0$ .

From these production function we can derive the cost function:

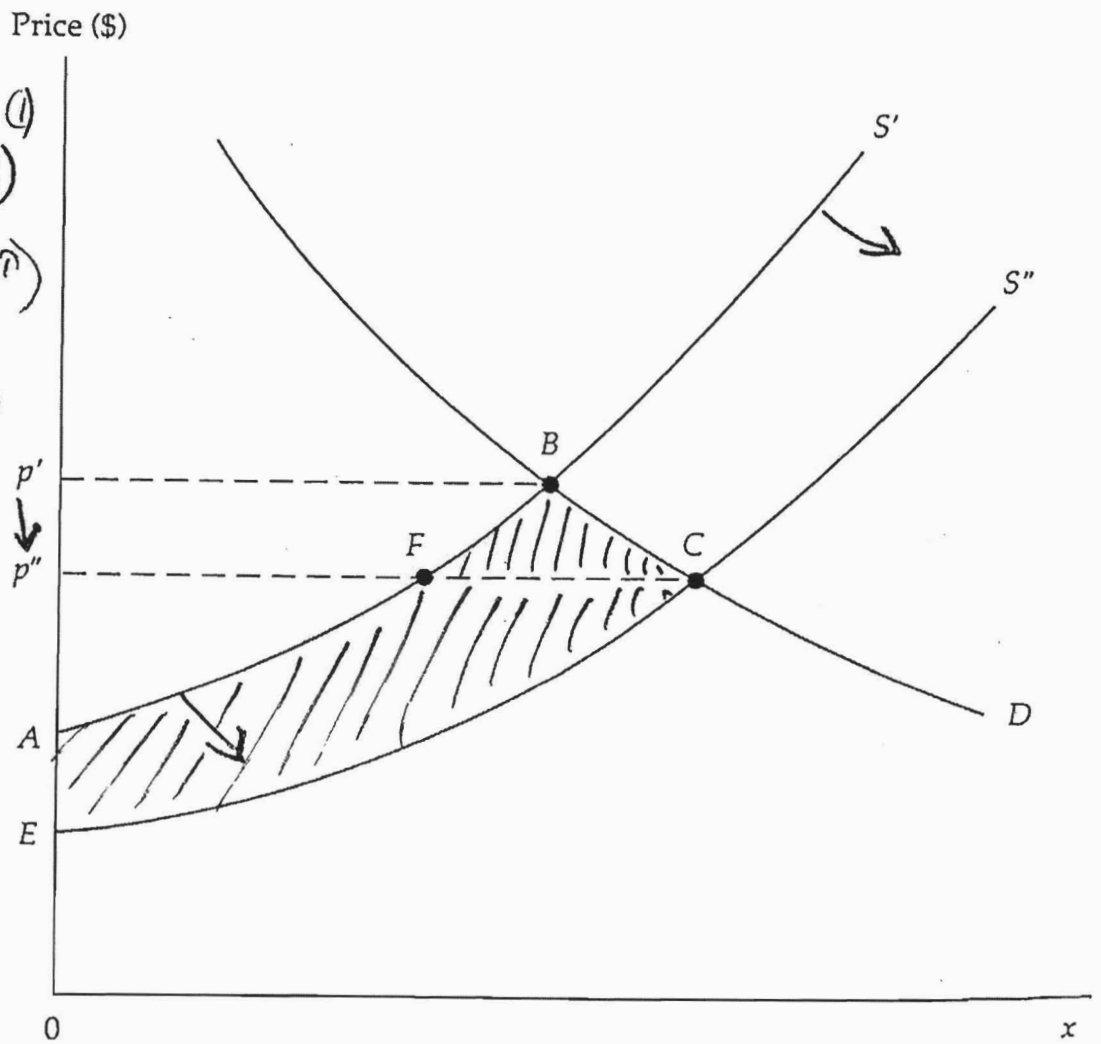
$$C = C(p_k, p_l, x, E)$$

the  $MC$  function, and the market *supply function* for  $x$ .

$\Rightarrow$  A change in  $E$  will cause a shift in the supply and factor demand curves, leading to (1) changes in the price of  $x$  to consumers, and (2) changes in the incomes received by owners of factor inputs used in the production of  $x$ .

# E as a factor input in production

אזור צריכה נטו (1)  
 $BCp''$  ( $\Delta S$ )  
 $p'BFP'$  (אזור ייצור)  
 $p''BCE$  (1)  
 אזור פיצול (2)  
 $p''CE$  : (1)  
 $p'FA$  (אזור ייצור)  
 $AFCE$   
 אזור פיצול  
 : אזור ייצור  
 (1) : (1)  
 : (1) +  
 $ABCE$



The welfare measure when  $q$  affects the production of  $x$



## HOUSEHOLD HEALTH PRODUCTION MODEL

Household produce "health",  $H$ , using market goods ( $z$ ) and a nonmarket (environmental) good,  $Y$ , as inputs in the production process.

$$\text{Max } U = U(x, H) \quad \text{s.t.} \quad p_x x + p_z z = M$$

$$H = H(z, Y) - \text{The health production function}$$

Note: \* The state of health,  $H$ , and *not* the nonmarket good,  $Y$ , enters the utility function.

\*  $Y$  and  $z$  are substitutes.

$\Rightarrow$  *If* the production function  $H(\cdot)$  is known, the WTP for  $Y$  (associated with a *non-compensated* demand function for the nonmarket good) can be calculated from the *observed* market demand functions for  $z$ .

Environmental Quality as a Direct or indirect Argument in the  
Individual Utility Function

Consider an individual maximizes the utility function

$$u = u(X, E)$$

subject to the budget constraint

$$\sum p_i x_i = M$$

where  $X$  is a vector of private goods, and  $M$  is money income.

The individual takes  $E$  as given and does not have to pay a price for this “imposed” quantity.

Note: We assume here that the individual *perceives at least the effects of changes in  $E$  on his/her well-being.*

The solution to this problem yields a set of *ordinary demand functions*

$$x_i = x_i(p_1, \dots, p_n, M, E)$$

The *dual* to the utility maximization problem can be stated as:

*Minimize* expenditure  $\sum p_i x_i$ , subject to a given utility level,  $u^0$ .

The solution to this problem gives the *expenditure function*

$$e(p_1, \dots, p_n, E; u^0) = M$$

where

ERROR:  $\delta e / \delta p_i = h_i(p_1, \dots, p_n, E; u^0)$   
OFFENDING COMMAND: timeout

that is, the *Hick-compensated demand function* for  $x_i$ .

Similarly,

$$-\delta e(p_1, \dots, p_n, E; u^0) / \delta E = w_E(p_1, \dots, p_n, E; u^0) \quad (1)$$

is the *Hick-compensated demand function* for  $E$ , or the marginal willingness to pay for a change in  $E$ ,  $w_E$ .

If the value of the derivative  $\delta e / \delta E$  can be inferred from observed data, then we have a point estimate of the *MWTP* for  $E$ . If this derivative can be estimated as a function of  $E$ , then we have the *MWTP function* (or demand schedule) for  $E$ . Then we also can obtain the benefit to the individual of a non-marginal increase in the supply of  $E$ :

$$W = - \int_{E_1}^{E_2} \delta e(p_1, \dots, p_n, E; u) / \delta E$$
$$= e(p_1, \dots, p_n, E_1; u) - e(p_1, \dots, p_n, E_2; u) \quad (2)$$

which is either a *Compensating Surplus (CS)* or an *Equivalent Surplus (ES)* depending on the level of utility at which this expression is evaluated.

## THE COST OF ILLNESS METHOD (COI)

Measures the *total economic costs* which morbidity imposes on society = *Direct Cost + Indirect Cost*

*Direct Costs* = The value of resources devoted to the treatment of illness:

- (a) hospital care
- (b) nursing home care
- (c) home health care
- (d) services of physicians, dentists, and other care specialists
- (e) medication
- (f) eye glasses, etc.

*Indirect costs* = measure the value of lost productivity due to illness

### Not included:

- Disutility of illness and psychological costs (pain, suffering, anxiety)
- Defensive expenditures

⇒ COI ≠ WTP

*Prevalence Basis:* All costs associated with all cases of the disease in a given time period.

*Incidence Basis:* All discounted costs associated with *new* cases of a disease, from the onset of illness until recovery or death occurs.

## THE CONTINGENT VALUATION METHOD (CVM)

Respondents are asked for their *maximum WTP* or *minimum WTA*, by being presented with *hypothetical* situations describing

- (a) how a change in morbidity will be accomplished
- (b) how payment would be made.

### *Payment Mechanisms:*

- (a) Open Maximum-WTP/minimum-WTA questions
- (b) Iterative bidding
- (c) Payment cards
- (d) Referendum-type questions

*Data Sources:* Primary - Sample surveys

### *Biases:*

- Strategic misrepresentation of preferences
- Unfamiliarity with the commodity
- Vehicle bias
- Starting point bias

*Two approaches* to empirical estimation:

- (1) Assessing WTP for improvements in health
- (2) Valuing reductions in air pollution (implicit estimation of dose-response function)