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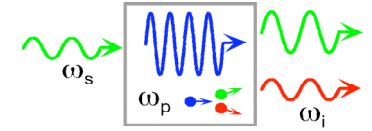
WINTER COLLEGE  
on  
QUANTUM AND CLASSICAL ASPECTS  
of  
INFORMATION OPTICS

*30 January - 10 February 2006*

Optical Communication Channels

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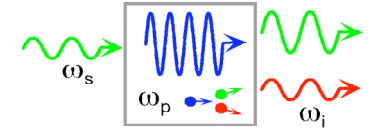
# Optical Communication Channels

Prem Kumar  
Northwestern University

Winter College on  
Quantum and Classical Aspects of Information Optics  
ICTP, Trieste, Italy  
February 8, 2006



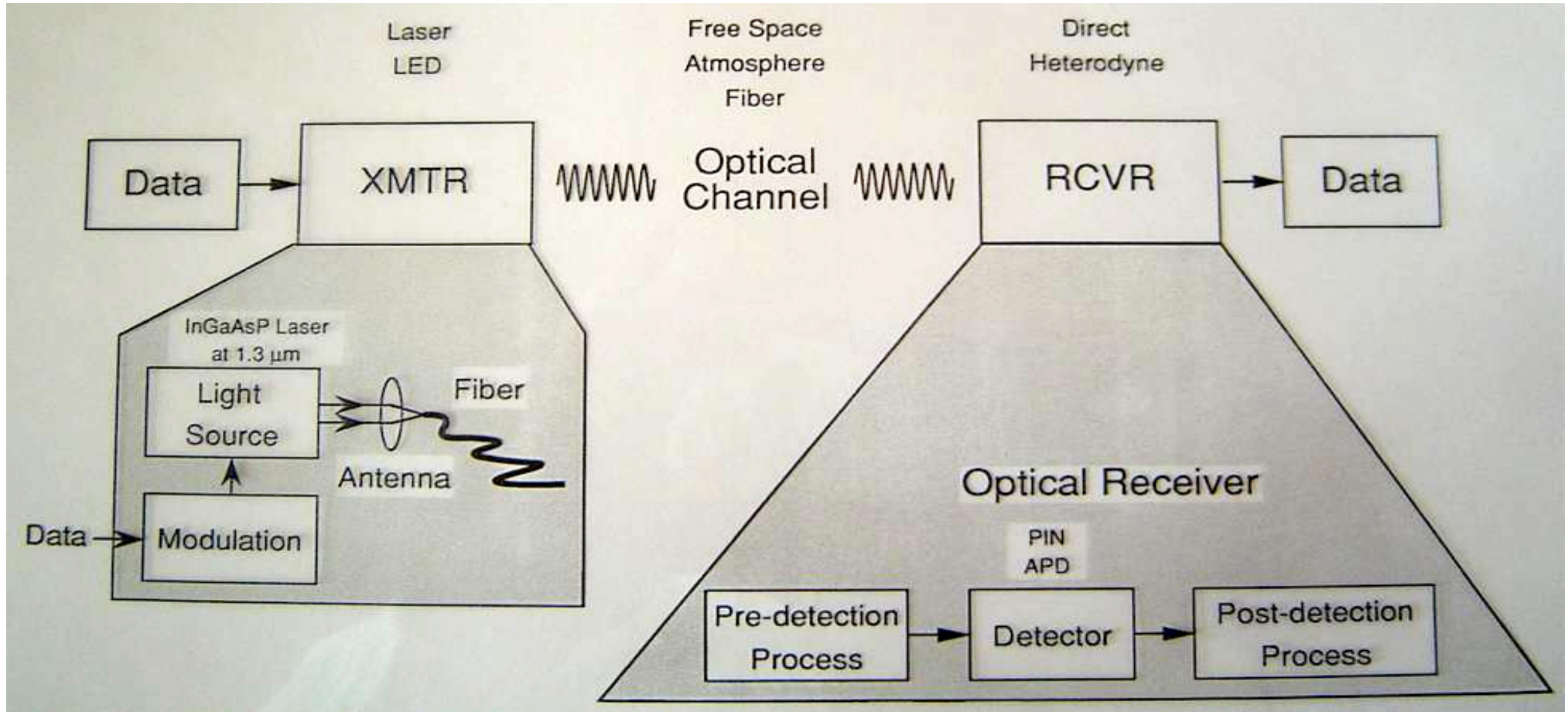
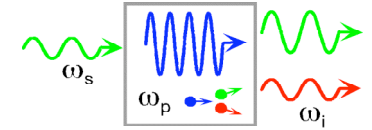
## Topics for Lecture 2



- Free-space channel for optical communications
- Optical fiber channel for optical communications
- Wavelength/frequency division multiplexing
- Optical amplifiers, EDFA, Raman, Parametric etc.
- Channel impairments due to ASE and Nonlinearity
- Role of quantum noise in optical Communications
- Signal regeneration and some advanced concepts



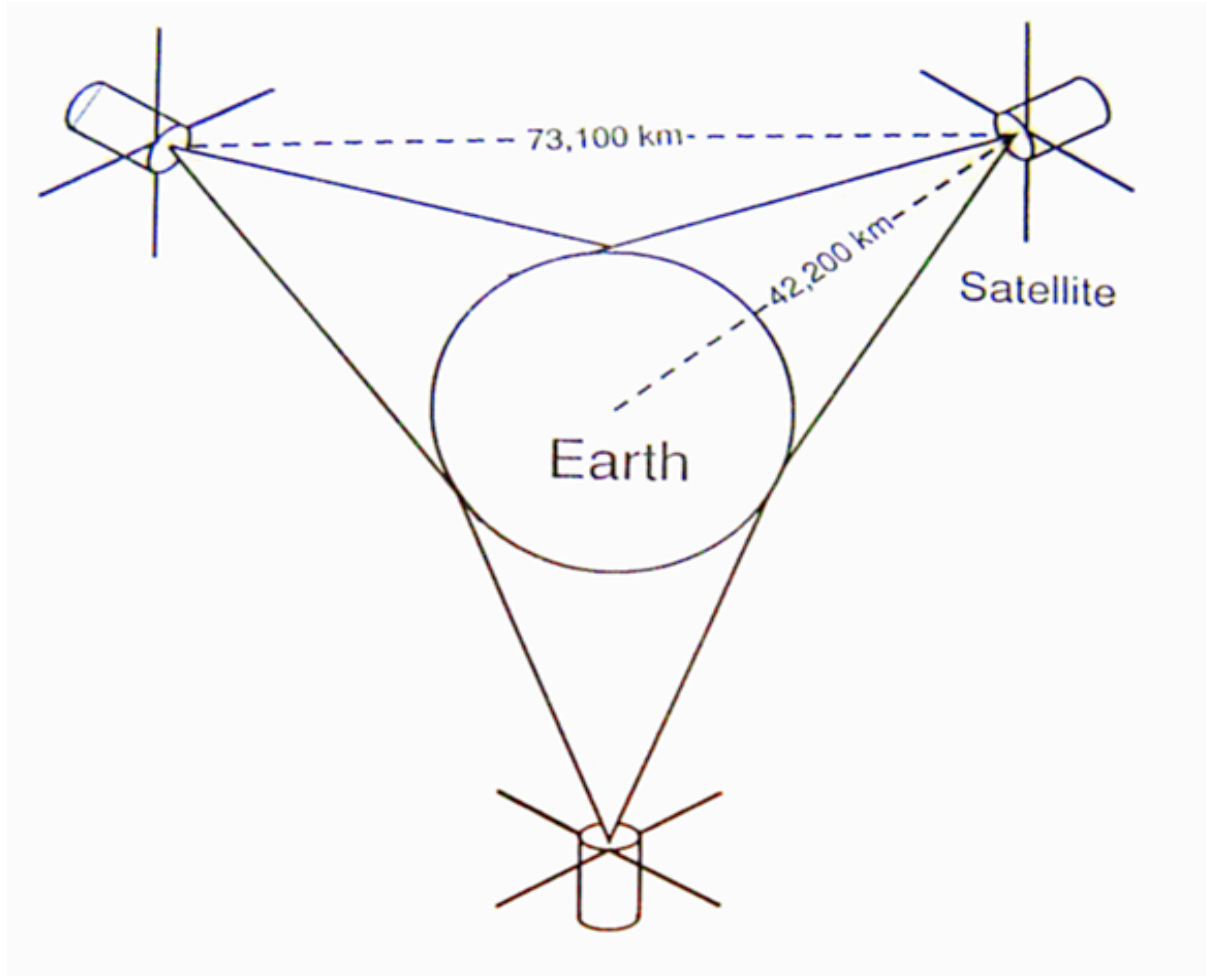
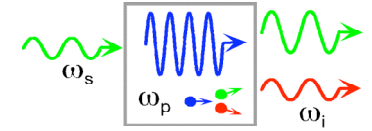
# A Generic Optical Communication System



This is an old schematic, but now a days in most high-end fiber-optic systems the lasers are at 1.5 nm wavelength.

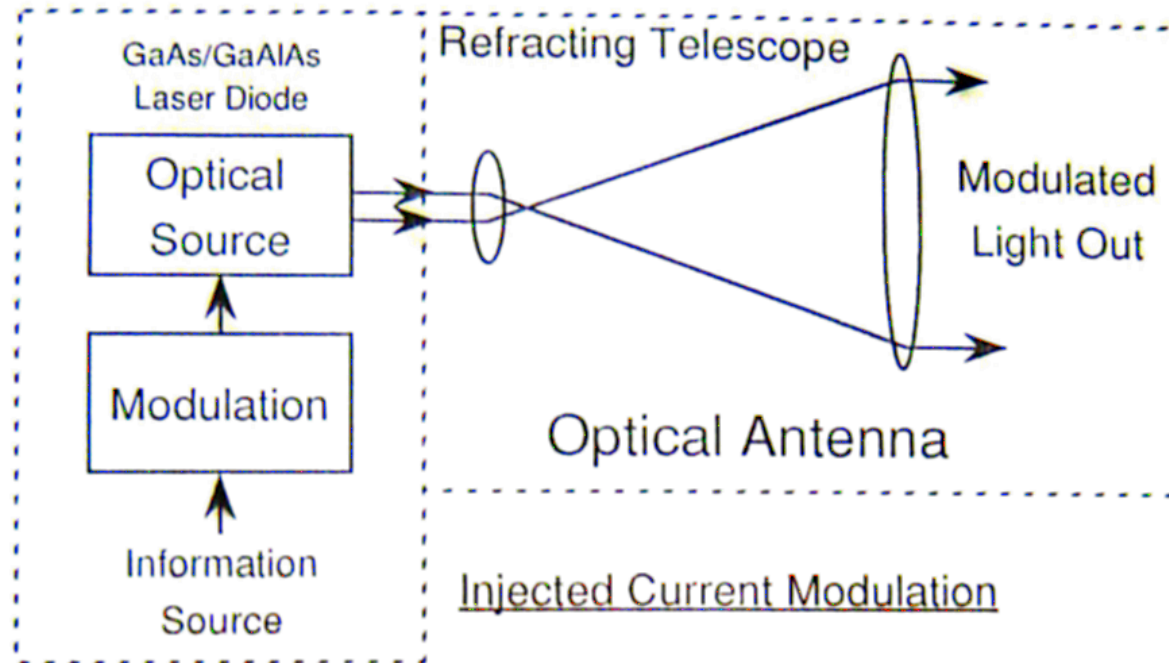
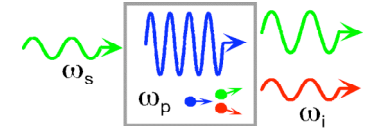


# Free-Space Optical Channel



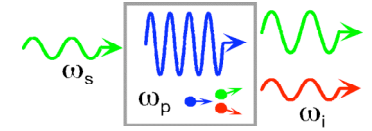


# Transmitter for Free Space Channel

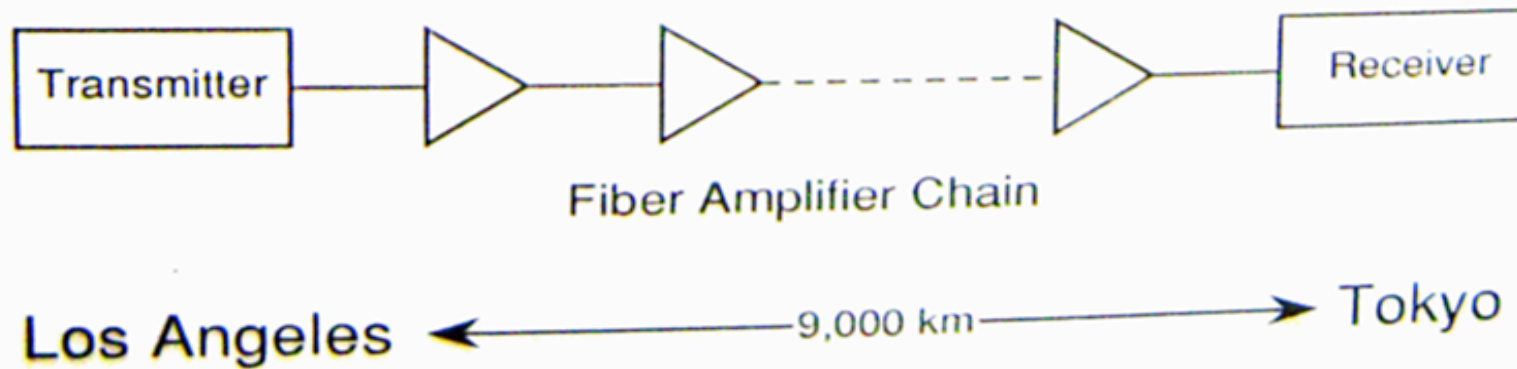




# Optical Fiber Channel

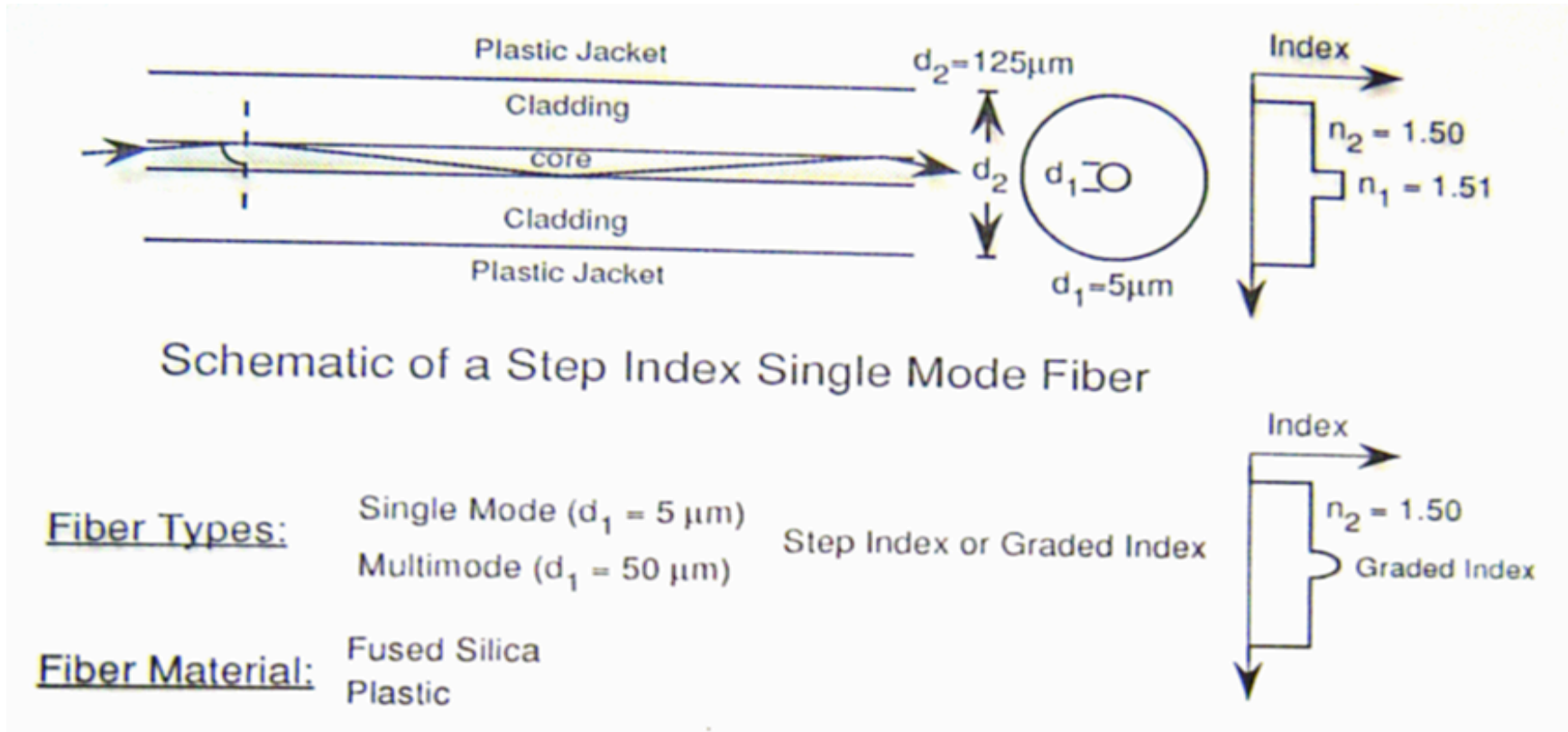
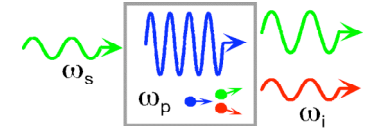


## Terrestrial Link:





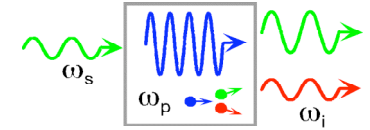
# Structure of Optical Fiber



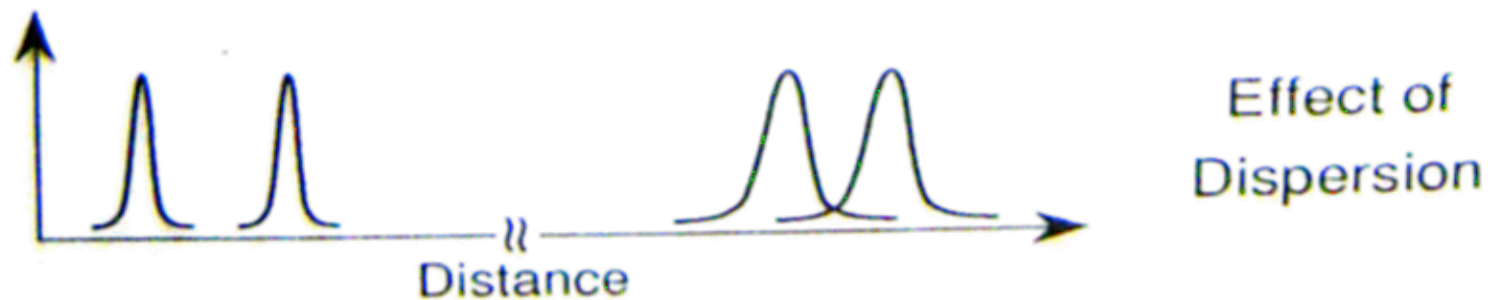




# Key Properties of Optical Fiber

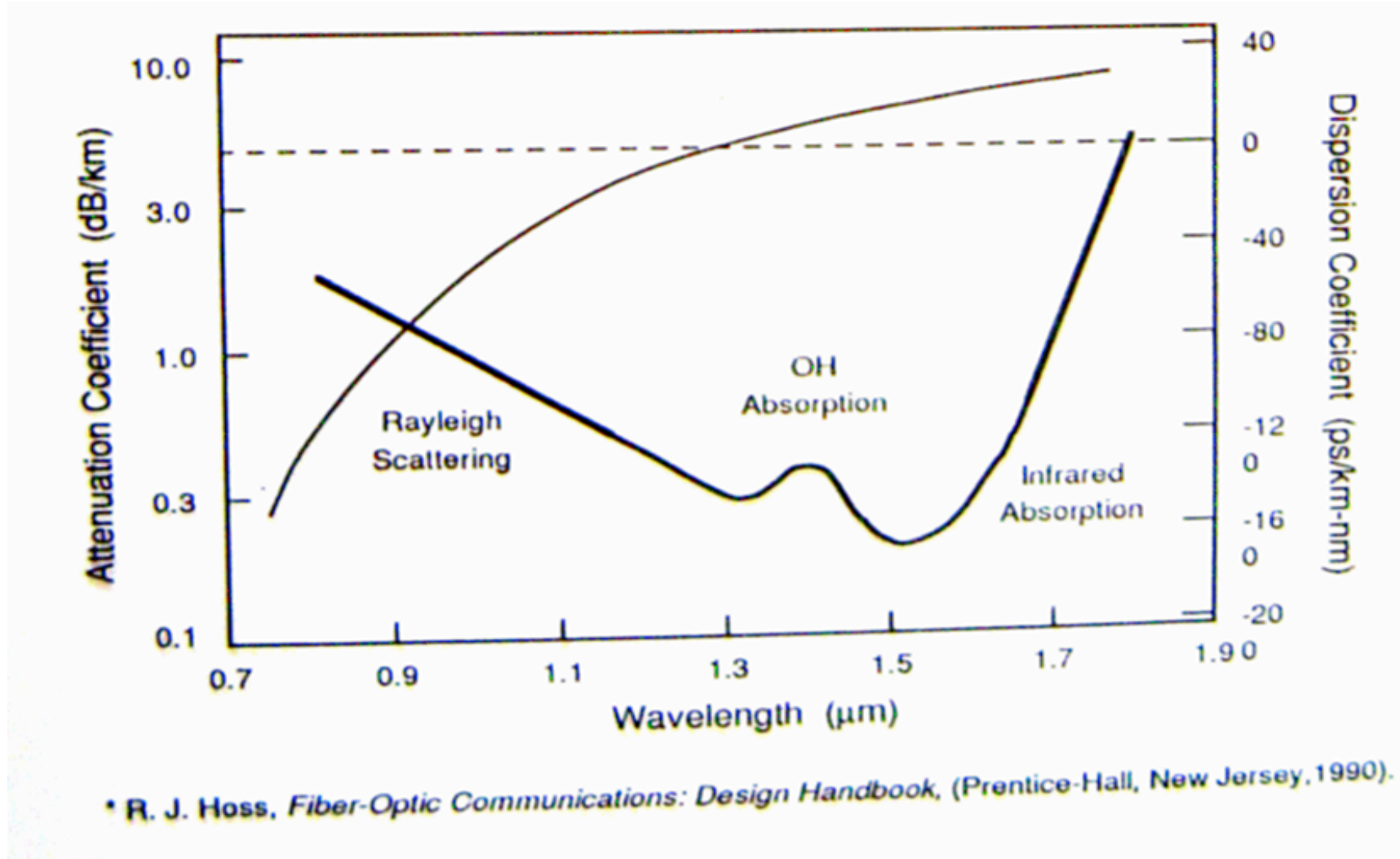
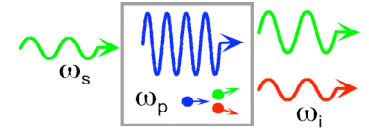


- Loss (less than 0.2 dB/km at 1.55  $\mu\text{m}$ )  
The emergence of the erbium-doped fiber amplifier has revolutionized fiber-optic communications
- Dispersion (group velocity is a function of  $\lambda$ )
- Nonlinearity (intensity dependent refractive index)  
Dispersion and nonlinearity can compensate each other to form *optical solitons*  
-- pulses of light that travel without spreading



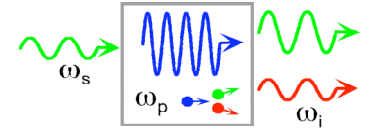


# Attenuation Spectra of Fused Silica Fibers





# Optical Power Transfer



- Free-Space Channel:

The received optical power is given by

$$P_r = P_t \left( \frac{A_t A_r}{\lambda L} \right)^2, \quad (1)$$

whenever  $\sqrt{A_t A_r} \ll \lambda L$ , i.e., the receiver is in the far-field region. Here

$P_r$  = optical power at the receiver,

$P_t$  = optical power transmitted,

$A_r$  = area of the receiving aperture,

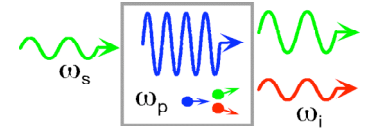
$A_t$  = area of the transmitting aperture,

$\lambda$  = wavelength of light, and

$L$  = transmitter-receiver distance.



# Optical Power Transfer



- Fiber-Optic Channel:

$$P_r = P_c e^{-\log(10)\alpha L/10}, \quad (2)$$

where

$P_r$  = optical power received,

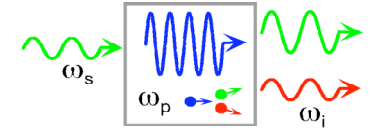
$P_c$  = optical power coupled into the fiber,

$\alpha$  = fiber loss coefficient in dB/km.

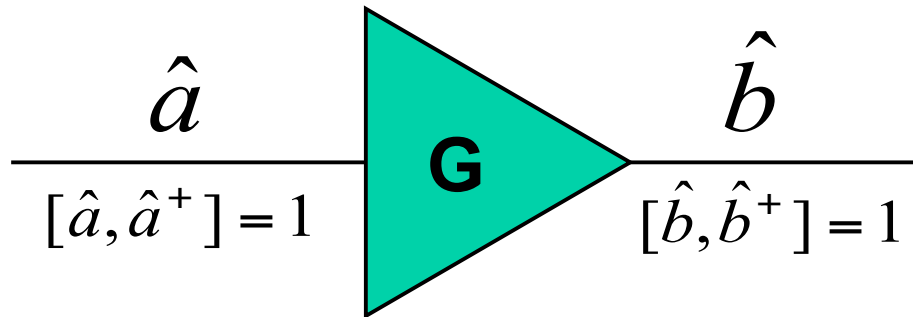
Note: One should take into account the various coupling losses.



# Fundamental Noise Limits of Linear Optical Amplifiers



Lumped Amplifier Model: Haus & Mullen, 1962; Caves, 1982; Yuen, 1992



- Phase Insensitive Amplifiers (PIA)

- Erbium-doped fiber amplifier
- Semiconductor optical amplifier
- Fiber Raman Amplifier
- Optical parametric amplifier

- Phase Sensitive Amplifiers (PSA)

- Optical parametric amplifier

- For PSA:

$$\hat{b} = \sqrt{G} \hat{a} + \sqrt{G-1} \hat{a}^\dagger$$

- Or in terms of quadratures

$$\hat{b} = \sqrt{g} \hat{a}_1 + i \frac{1}{\sqrt{g}} \hat{a}_2$$

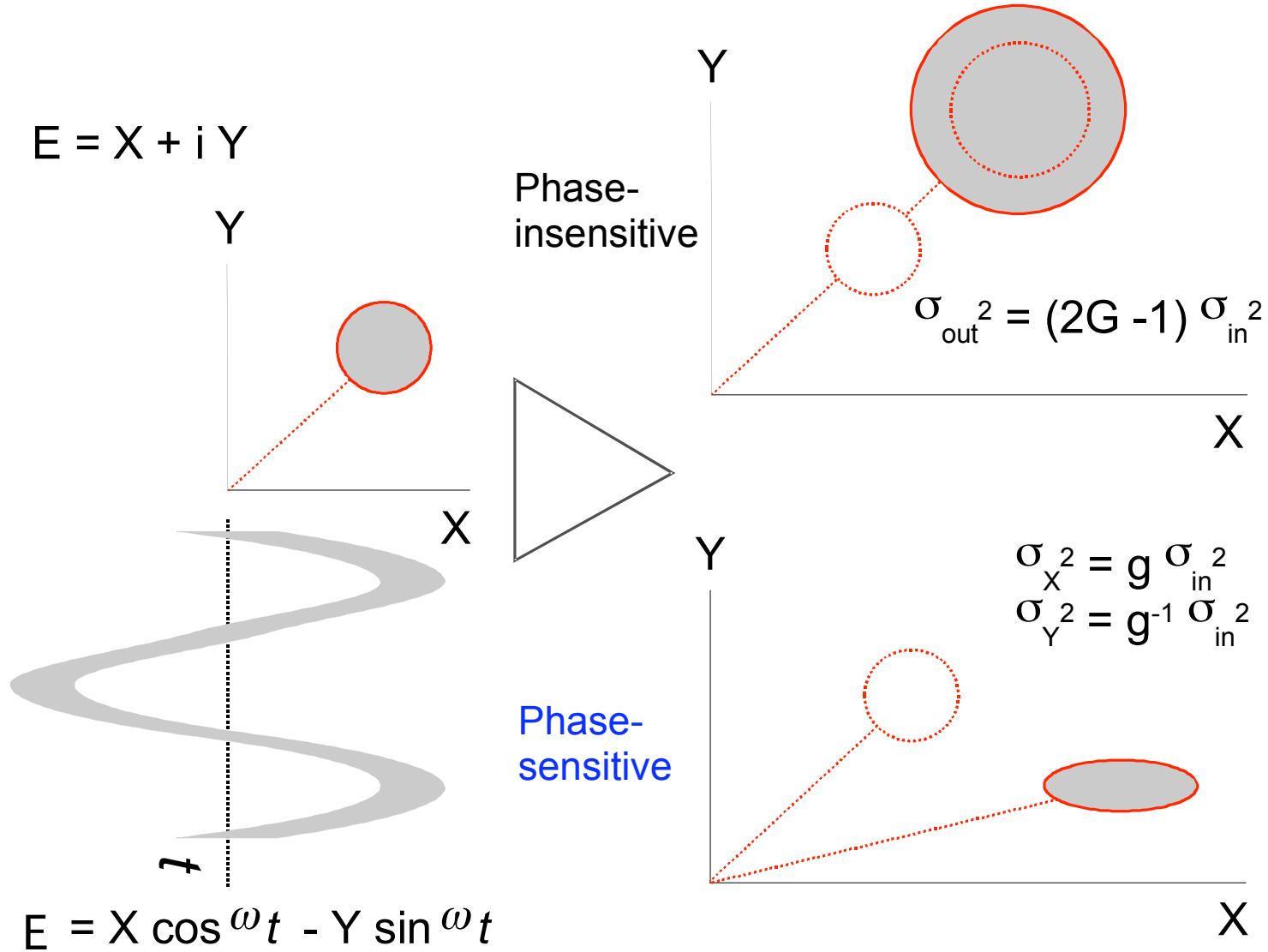
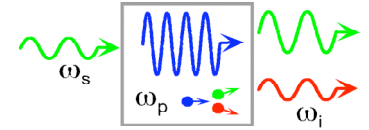
- No need for an extra noise source

- For homodyne detection (and for direct detection with

$$NF_{PSA} = 1 \text{ (0 dB)}$$

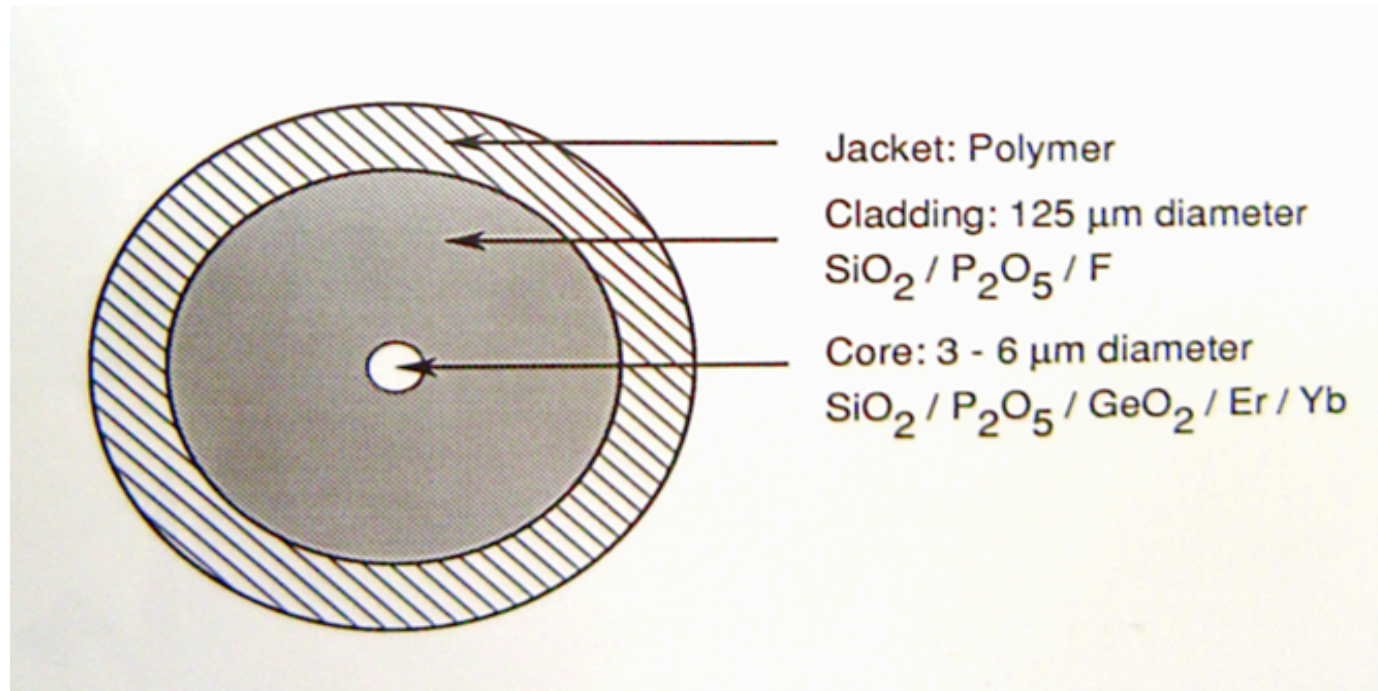
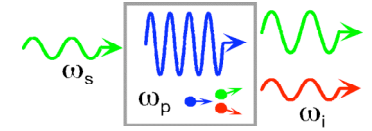


# Pictorial View of Amplification of Coherent Input Light



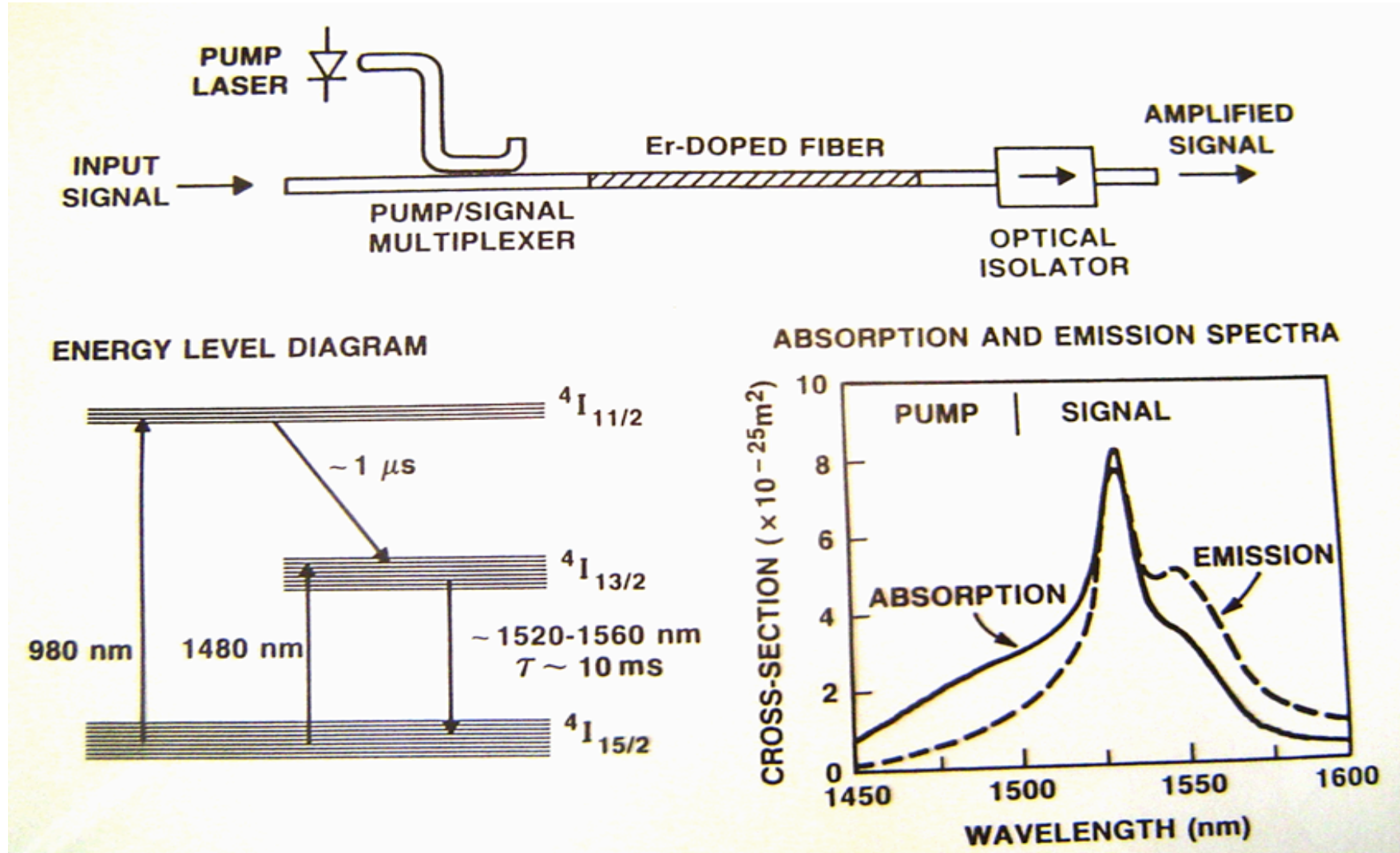
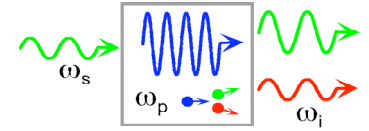


# Erbium-Doped Fiber





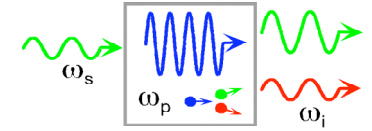
# Erbium-Doped Fiber Amplifier



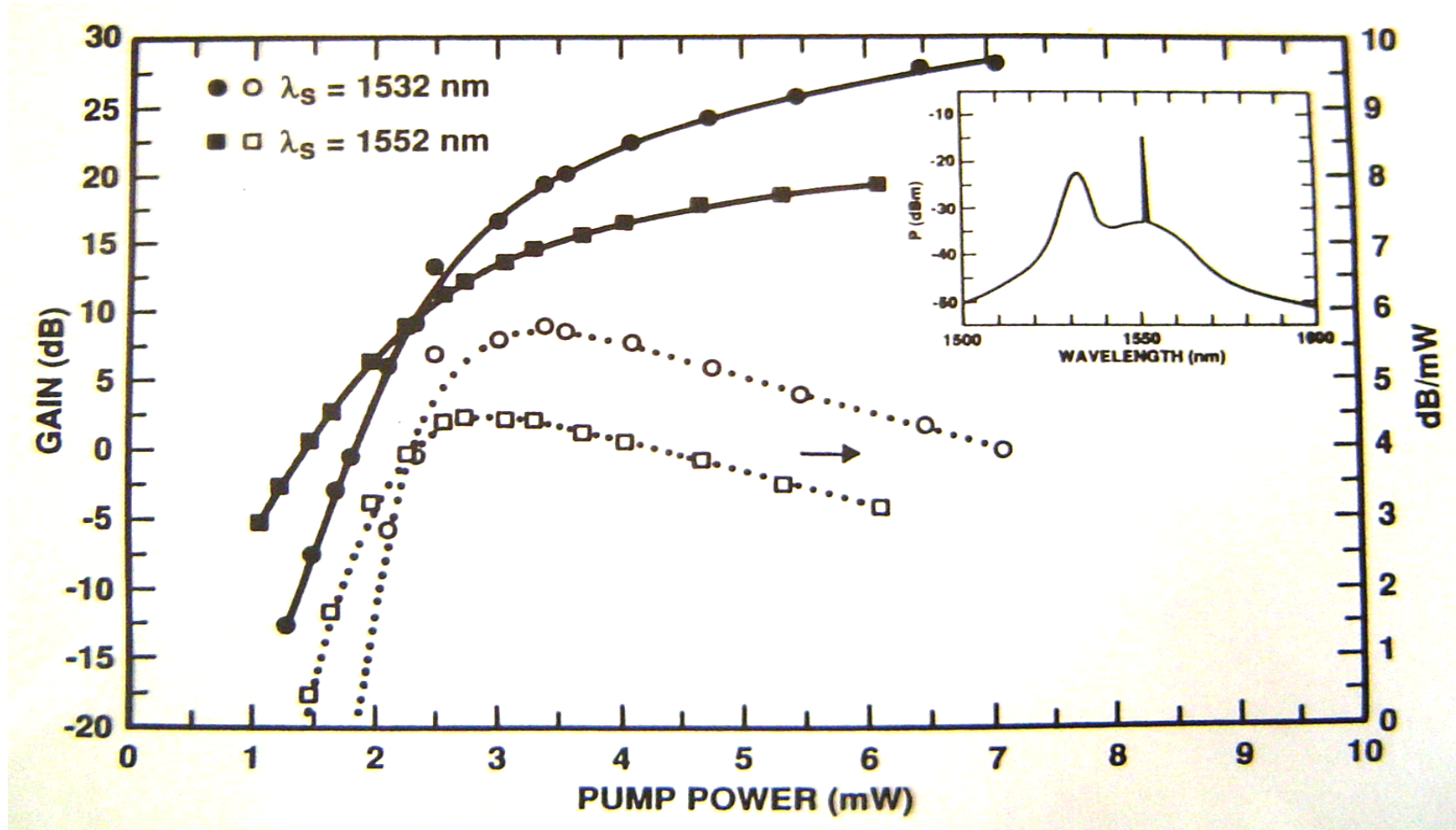




# Gain Properties of an EDFA

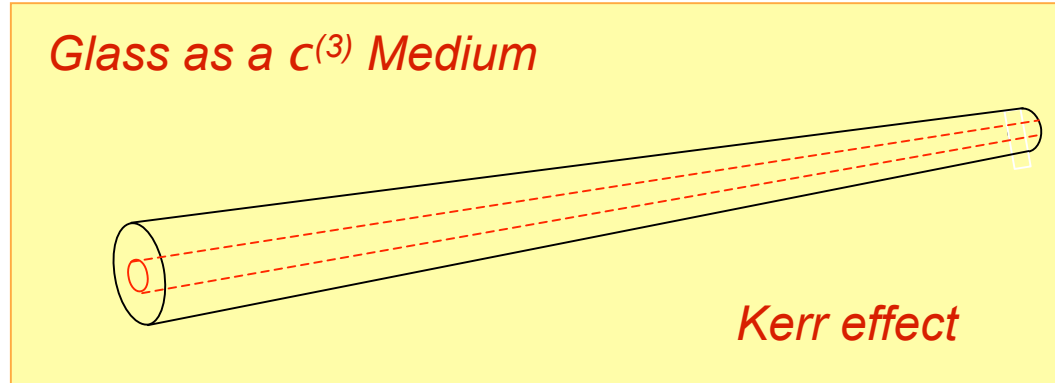
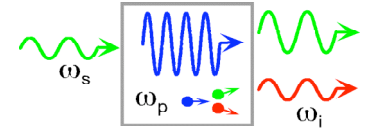


Pump Wavelength = 980 nm





# Nonlinear Optics in Fiber



- Small core  $\rightarrow$  high intensity
- Large interaction length
- Excellent mode matching
- Low loss for some  $\lambda$ 's
- Doping is possible
- Dispersion
- Relatively small  $\chi^{(3)}$

Pump SPM

$$\frac{\partial A_p}{\partial z} + \frac{\alpha}{2} A_p + i \frac{\beta_2}{2} \frac{\partial^2 A_p}{\partial T^2} = i\gamma(|A_p|^2 A_p)$$

XPM

Four-Wave Mixing

$$\frac{\partial A_{s(i)}}{\partial z} + \frac{\alpha}{2} A_{s(i)} + d \frac{\partial A_{s(i)}}{\partial T} + i \frac{\beta_2}{2} \frac{\partial^2 A_{s(i)}}{\partial T^2} = i\gamma \left[ |A_p|^2 A_{s(i)} + A_p^2 A_{i(s)} * \exp(i\Delta k z) \right]$$

Phase Matching

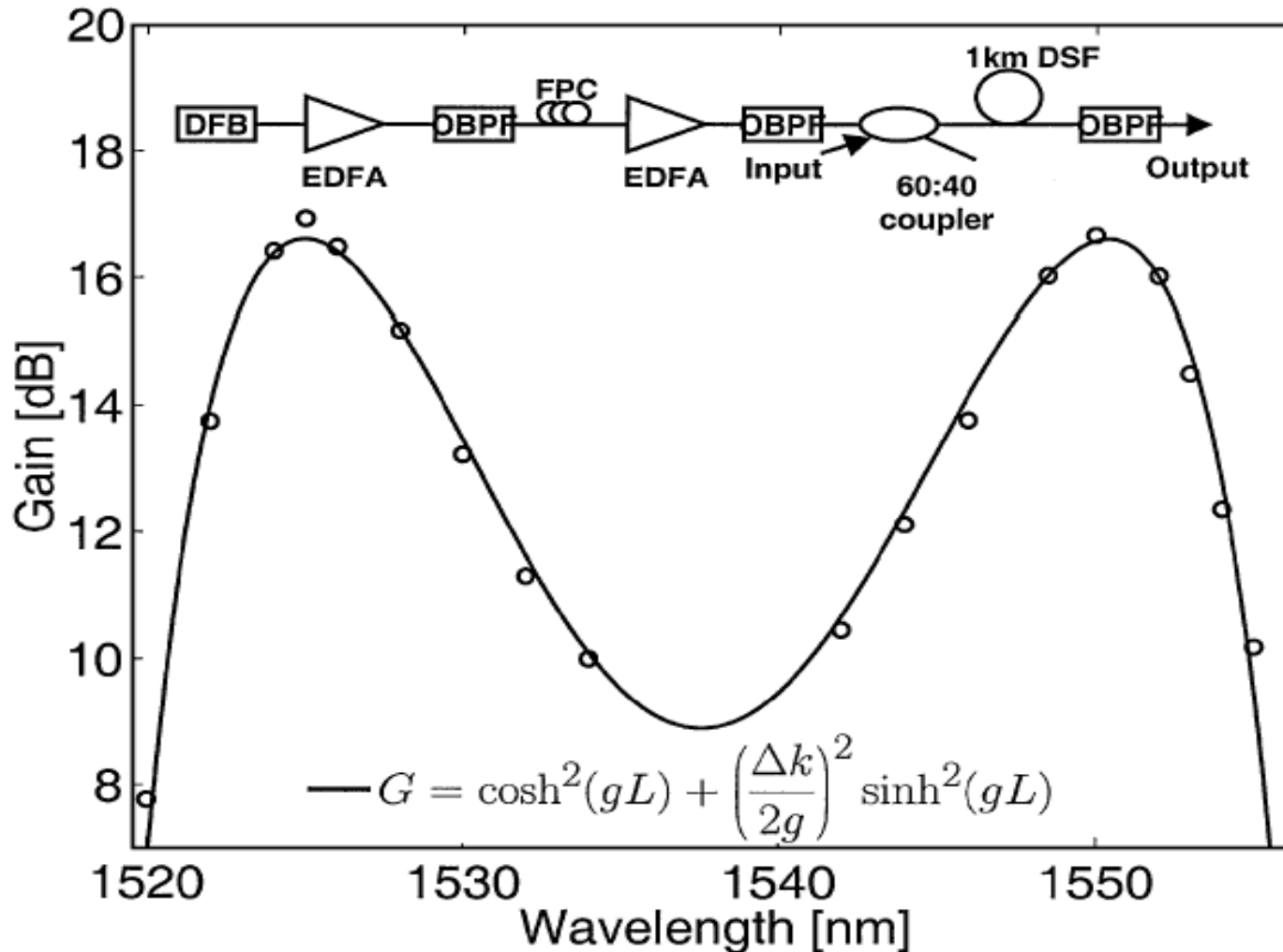
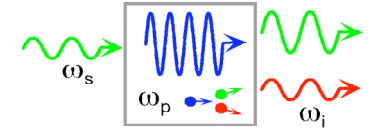
$$2\omega_p = \omega_s + \omega_i \quad \Delta k = 2k_p - k_s - k_i$$

Nonlinear Coefficient

$$\gamma = \frac{n_2 \omega_p}{A_{\text{eff}} c}$$



# Fiber Optical Parametric Amplifier (FOPA): An Example of a PIA

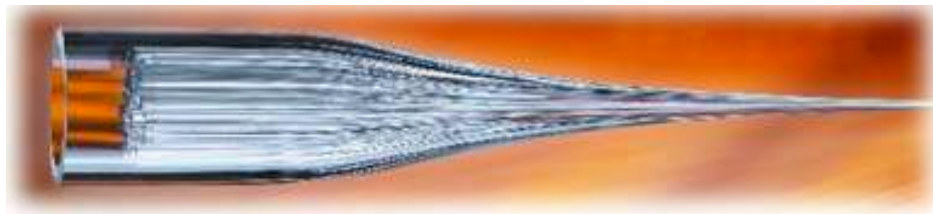
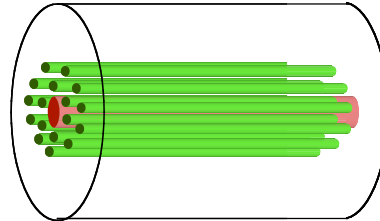
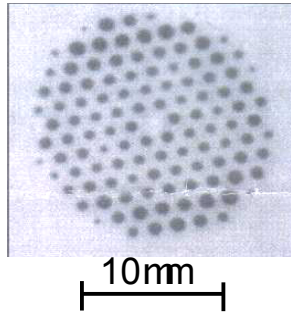
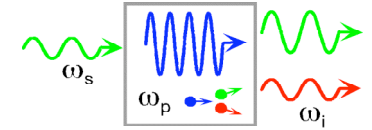


- 1 km linear FOPA configuration
- Gain as high as 20 dB
- 1537.5 nm pump
- 1.3 W pump peak power
- 700 ns pump pulses
- 8 kHz pump pulse rate
- CW signal

$$g = \sqrt{(\gamma P_p)^2 - \left(\frac{\delta k}{2}\right)^2} \quad \delta k = 2\gamma P_p + (k_s + k_i - 2k_p) \approx 2\gamma P_p + \beta_2(\omega_s - \omega_p)^2$$



# Crystal Fibre™ Microstructure Fiber



## Pros/Cons

- + Smaller core & higher nonlinear coefficient
- + Shorter interaction length
- + Less optical power required
- + Doping is possible
- Larger dispersion slope
- Higher loss for some  $\lambda$ 's

## Fiber Parameters

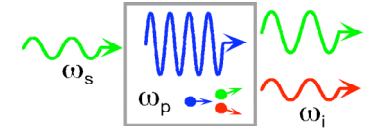
- $n_2 = 2.8 \times 10^{-20} \text{ m}^2/\text{W}$
- Core diameter =  $2.4 \pm 0.2 \text{ mm}$ , surrounded by a hexagonal array of  $\sim 0.8 \text{ mm}$  diameter air voids.
- Effective mode area of  $7 \text{ mm}^2$  at  $1550 \text{ nm}$
- $\alpha = 0.1 \text{ dB/m @ } 1550 \text{ nm}$
- $g \gg 24 \text{ W}^{-1} \text{ Km}^{-1}$  at  $1550 \text{ nm}$
- Asymmetry in the core results in polarization-maintaining fiber

	MF1	MF2
$\lambda_0$	1544 $\pm$ 5nm	1558 $\pm$ 5nm
Length	12.5m	11m

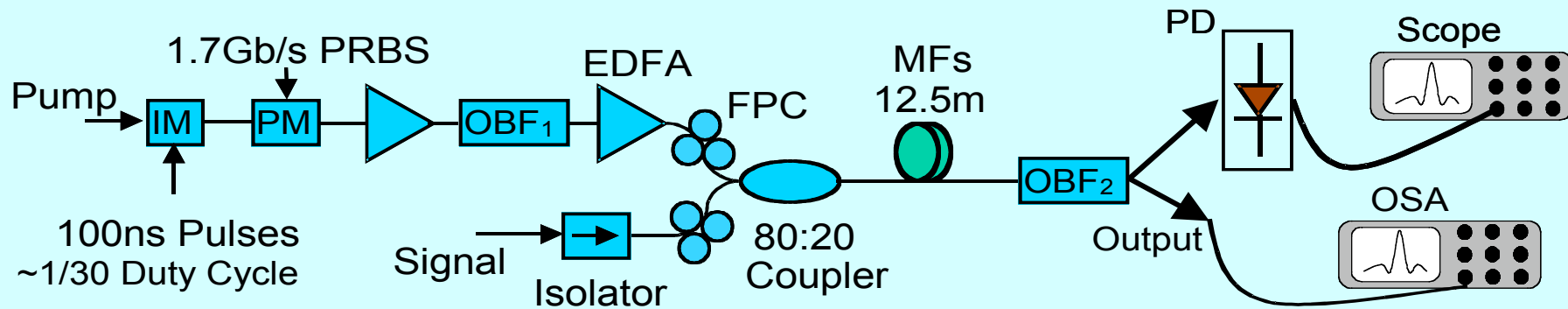


# Telecom-Band High-Gain MFOPA

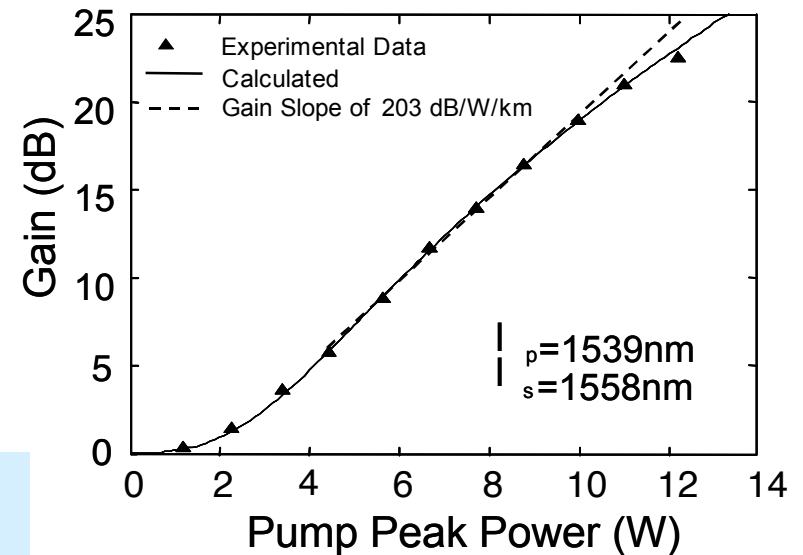
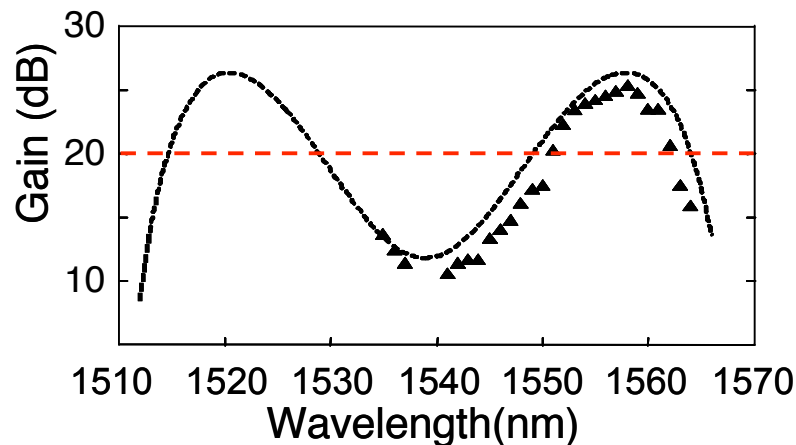
(Gain Slope  $\sim 200$  dB/W/km)



## Experimental Setup Tang et al., Electron. Lett. 39 (2) 195 (2003).



$\lambda_p = 1539$ nm, peak pump power  $\sim 12$ W,  $\lambda_s$  from 1535nm to 1565nm,  $\lambda_o \sim 1544$  (+/- 3) nm



- Gains  $> 20$ dB over  $\sim 30$ nm using only 12.5m-long MF
- A record gain slope of  $\sim 203$ dB/W/Km ( $\sim 8.7g$ )