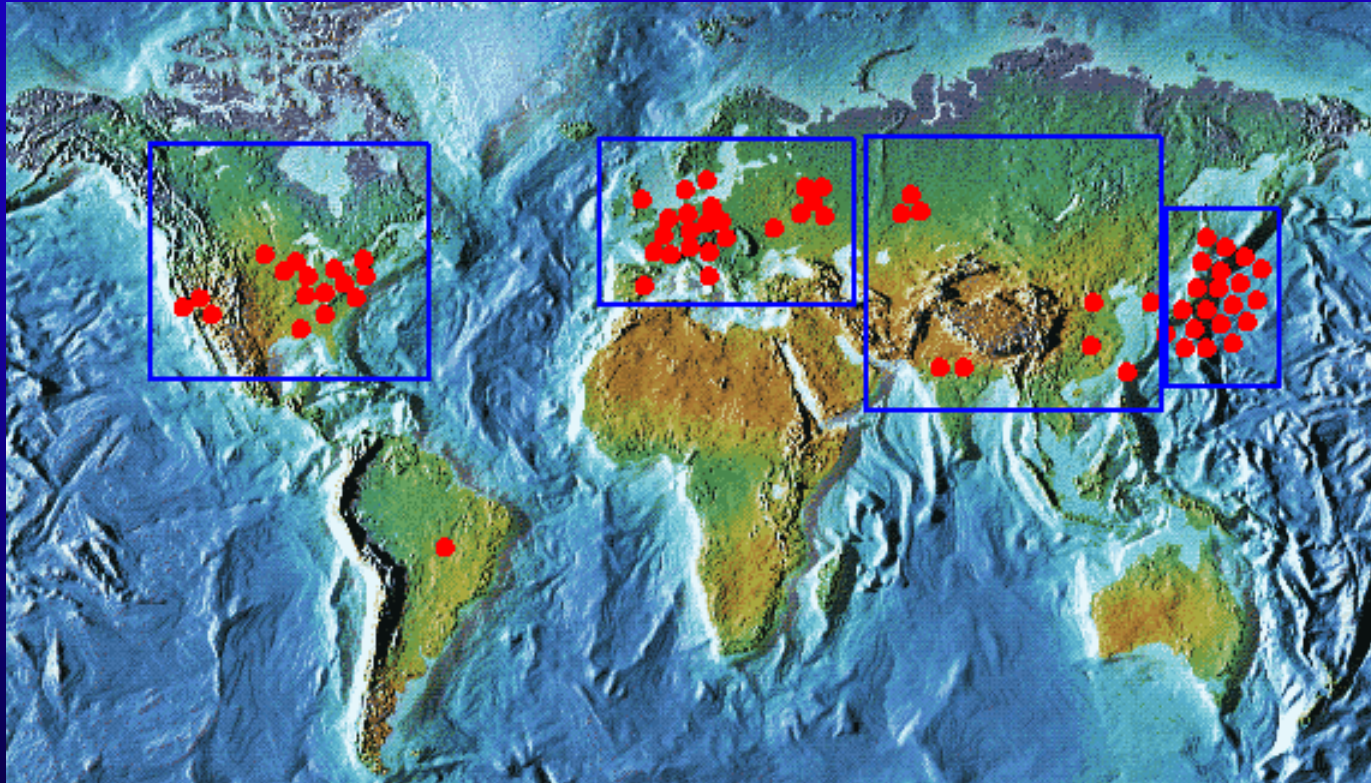


SYNCHROTRON RADIATION SOURCES AND PROPERTIES

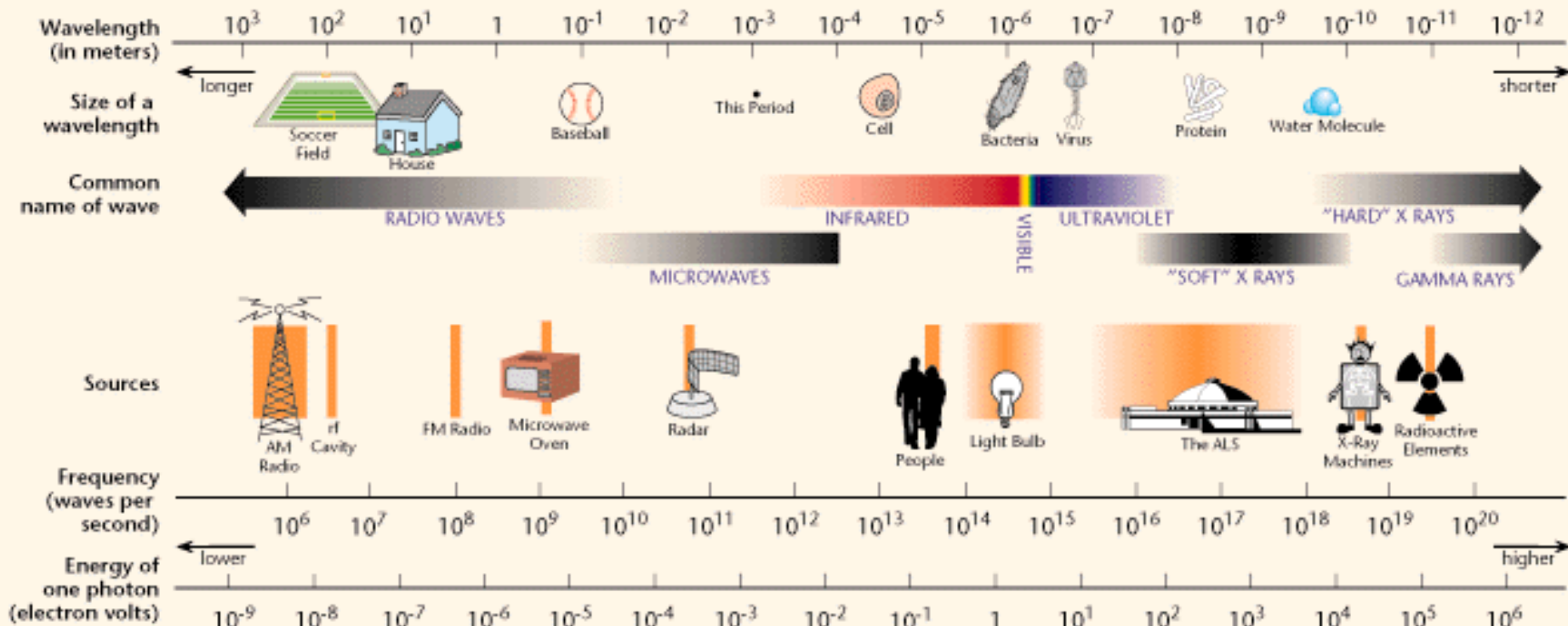
Lenny Rivkin
Paul Scherrer Institute, Switzerland

ICTP SCHOOL ON SYNCHROTRON RADIATION AND APPLICATIONS
Trieste, Italy, May 2006

60 000 users world-wide

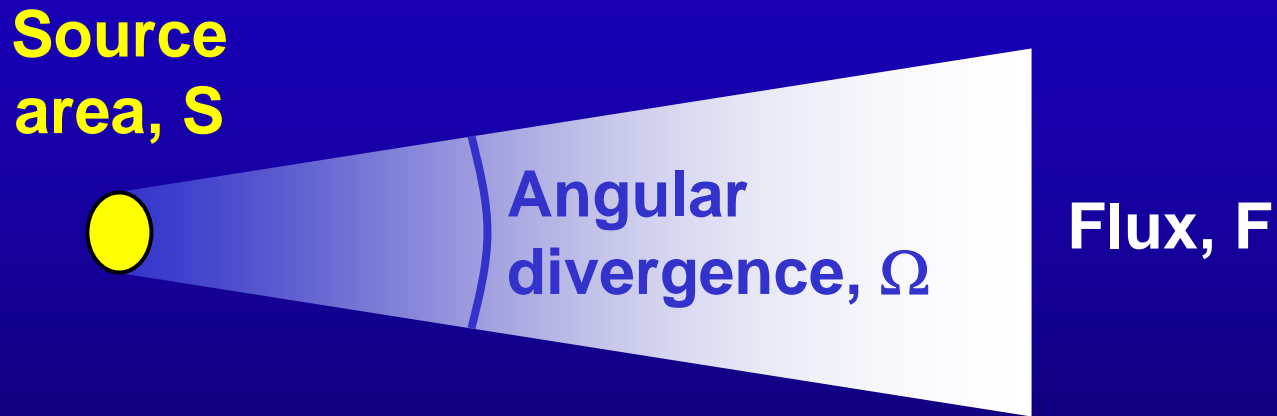


THE ELECTROMAGNETIC SPECTRUM



Wavelength continuously tunable !

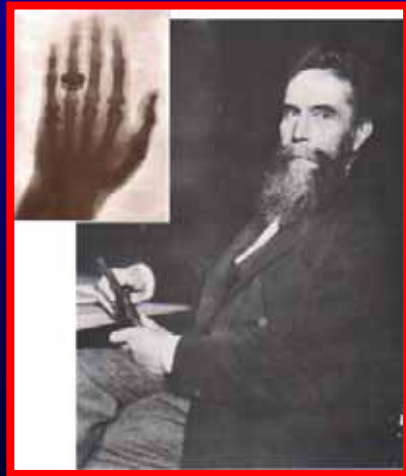
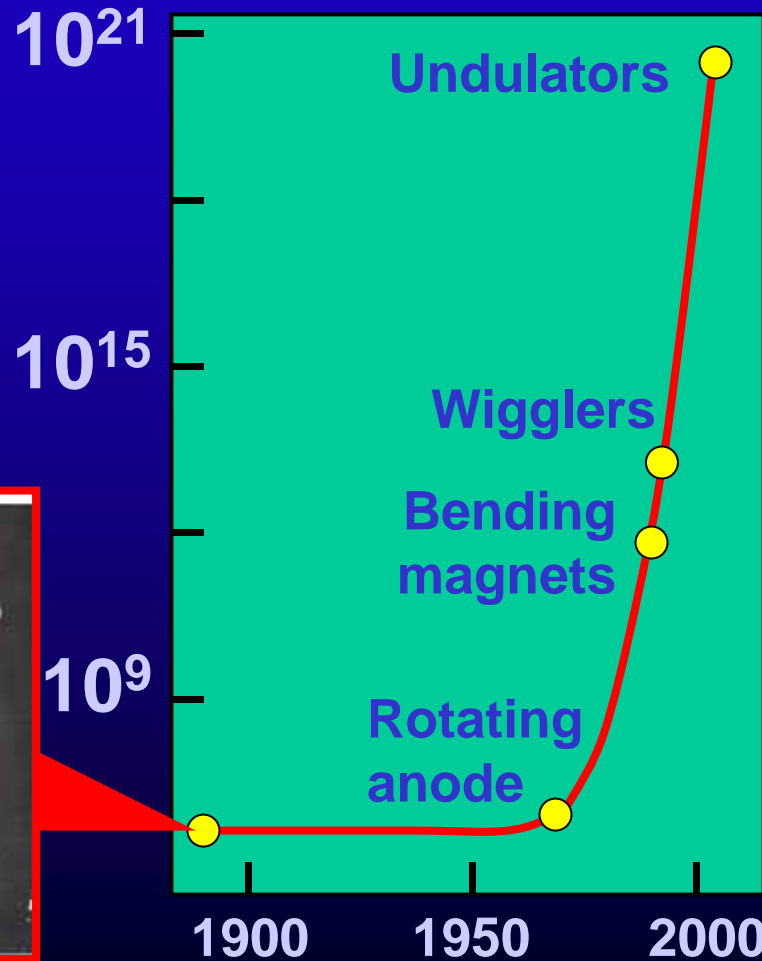
The “brightness” of a light source:



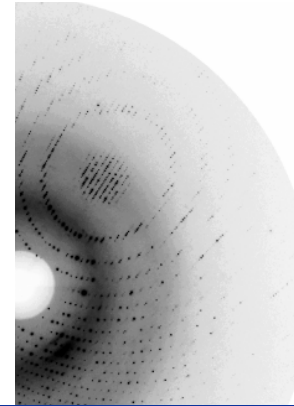
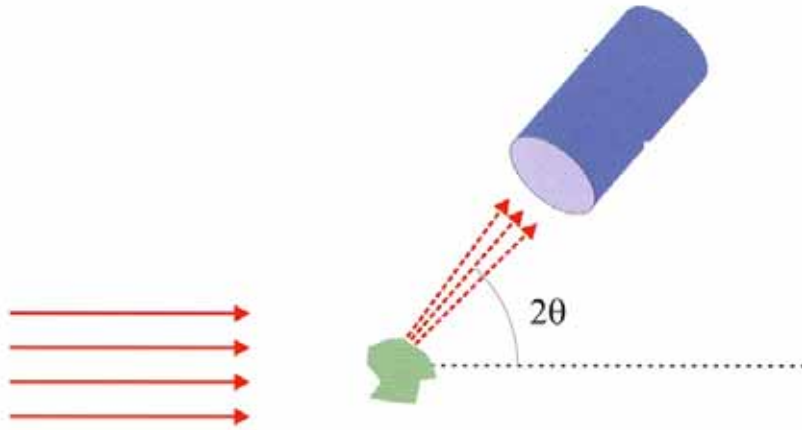
$$\text{Brightness} = \text{constant} \times \frac{F}{S \times \Omega}$$

Steep rise in brightness/brilliance

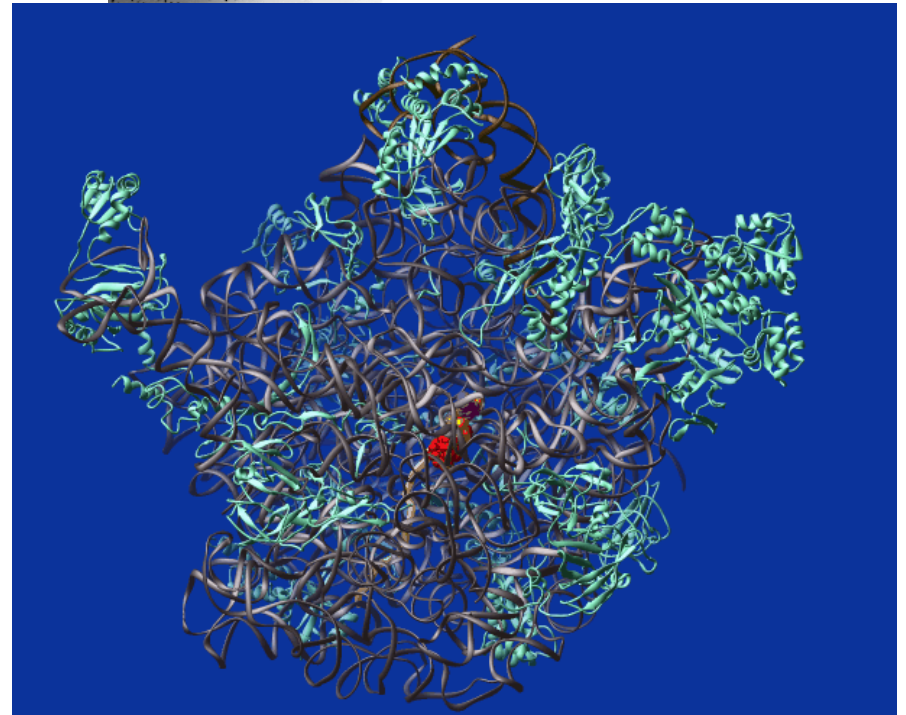
(units: photons/mm²/s/mrad², 0.1% bandwidth)



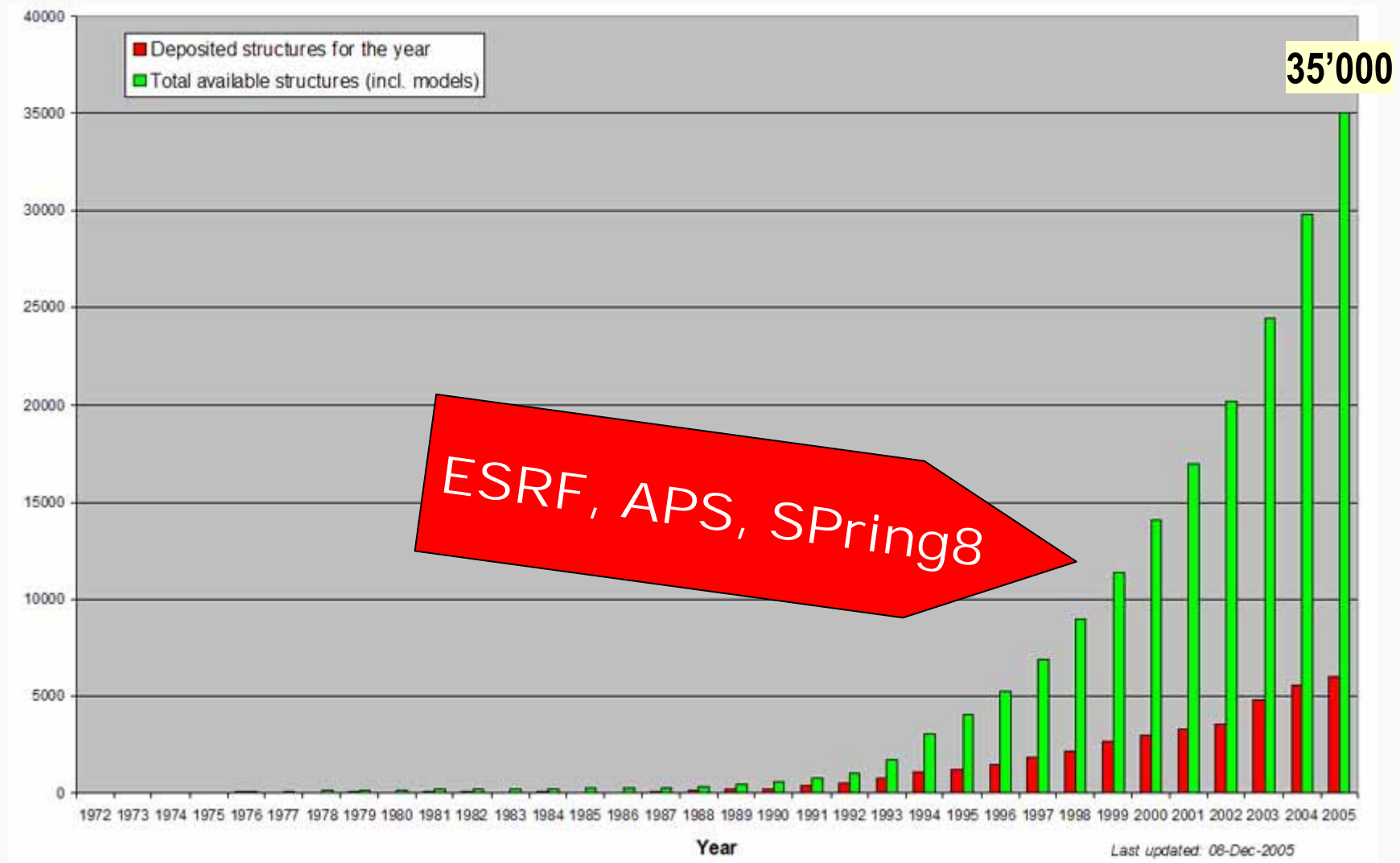
Protein structure



Diffraction pattern



Spectacular growth of structural biology



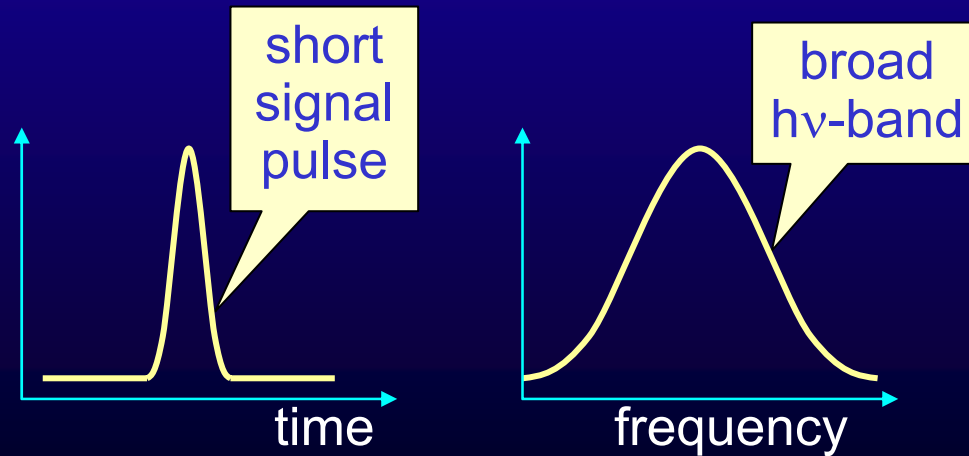
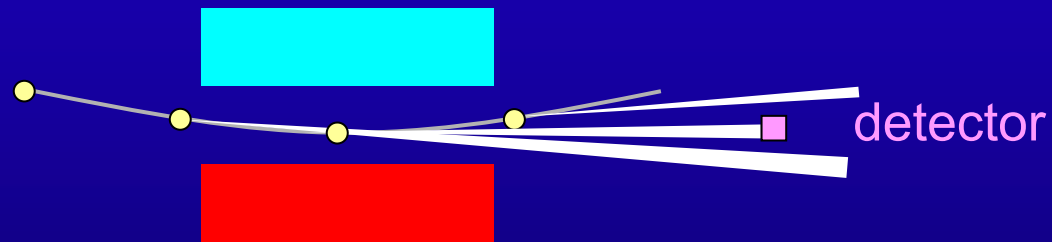
Higher brightness:

more photons on small sample

- measurements on very small probes
(few μm crystals)
- small divergence:
 - compact mirrors, optics elements
 - minimized aberrations
- short measurement times
- high transverse coherence
 - phase contrast imaging

3 types of storage ring sources:

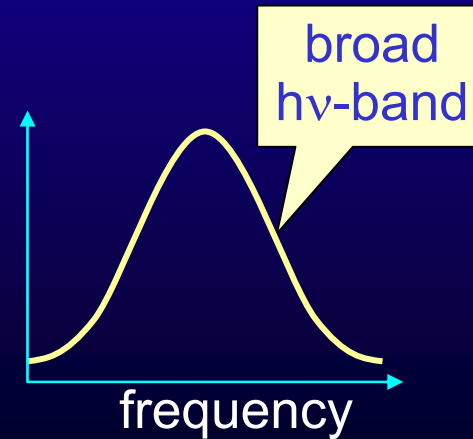
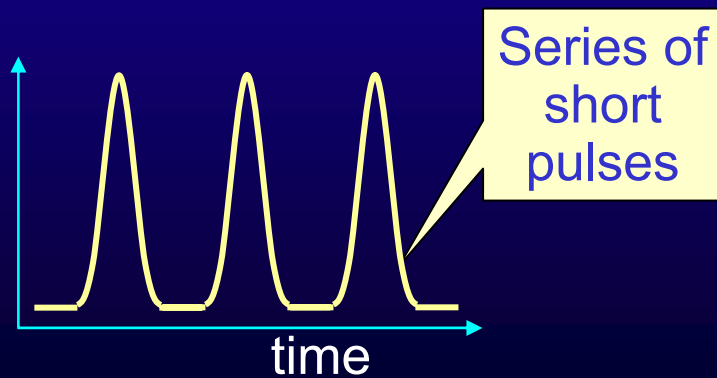
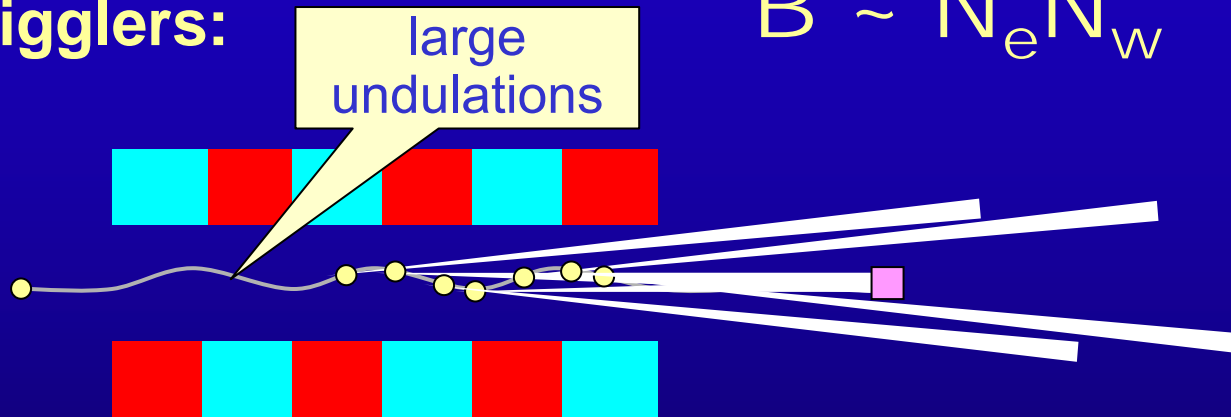
1. Bending magnets: $B \sim N_e$



3 types of storage ring sources:

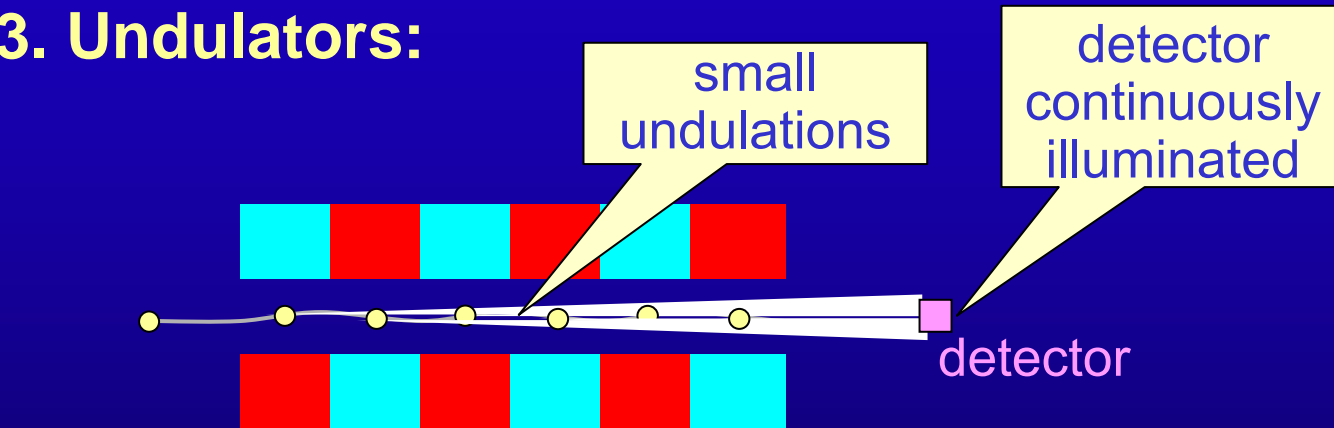
2. Wigglers:

$$B \sim N_e N_w \times 10$$

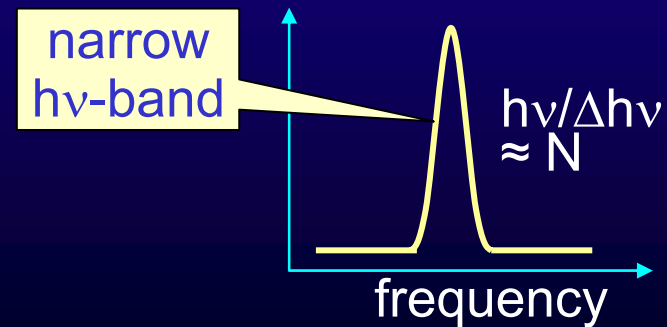
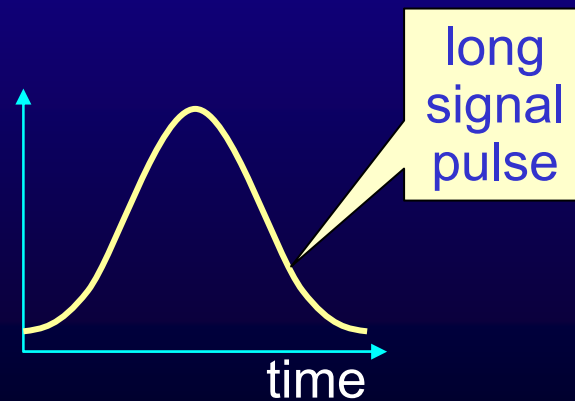


3 types of storage ring sources:

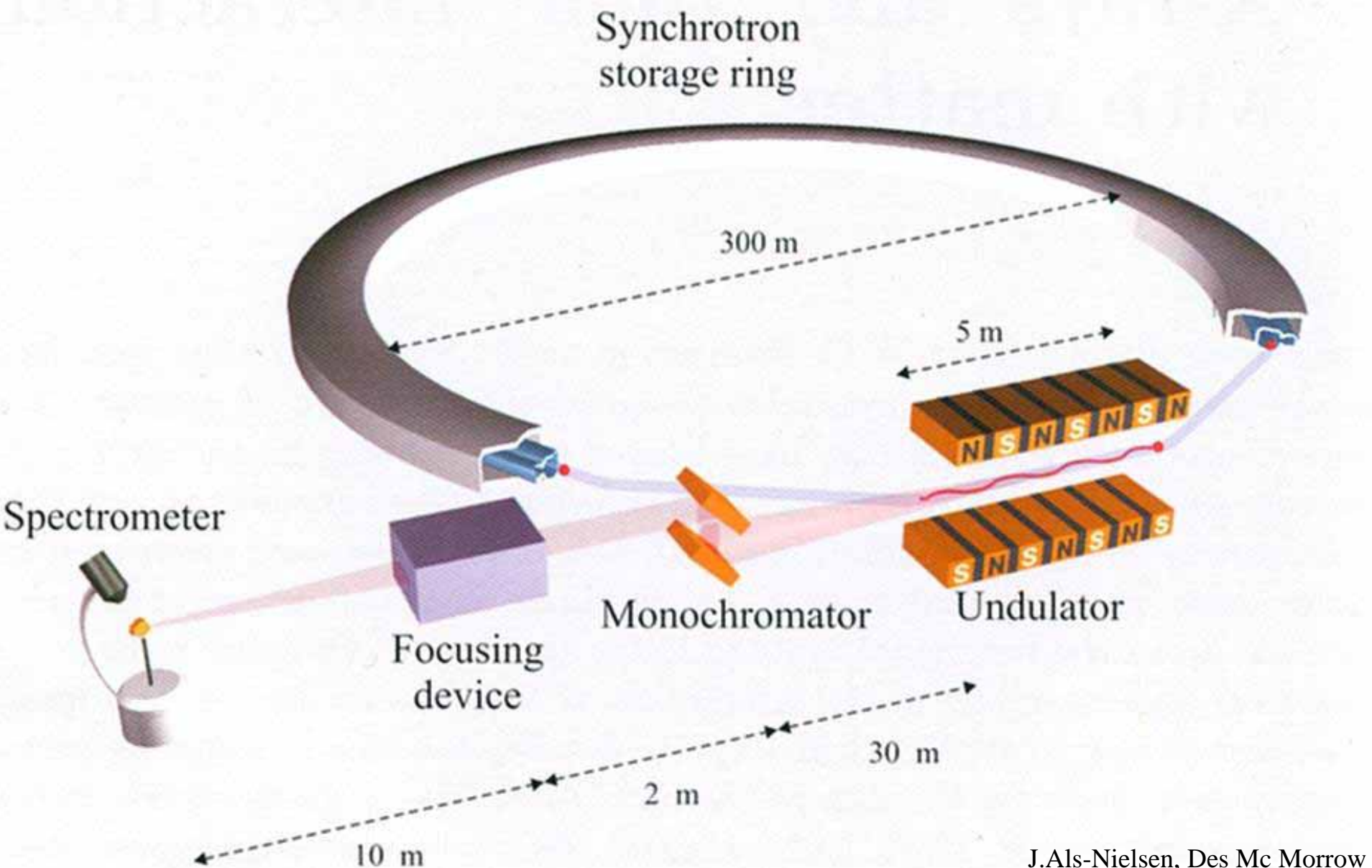
3. Undulators:

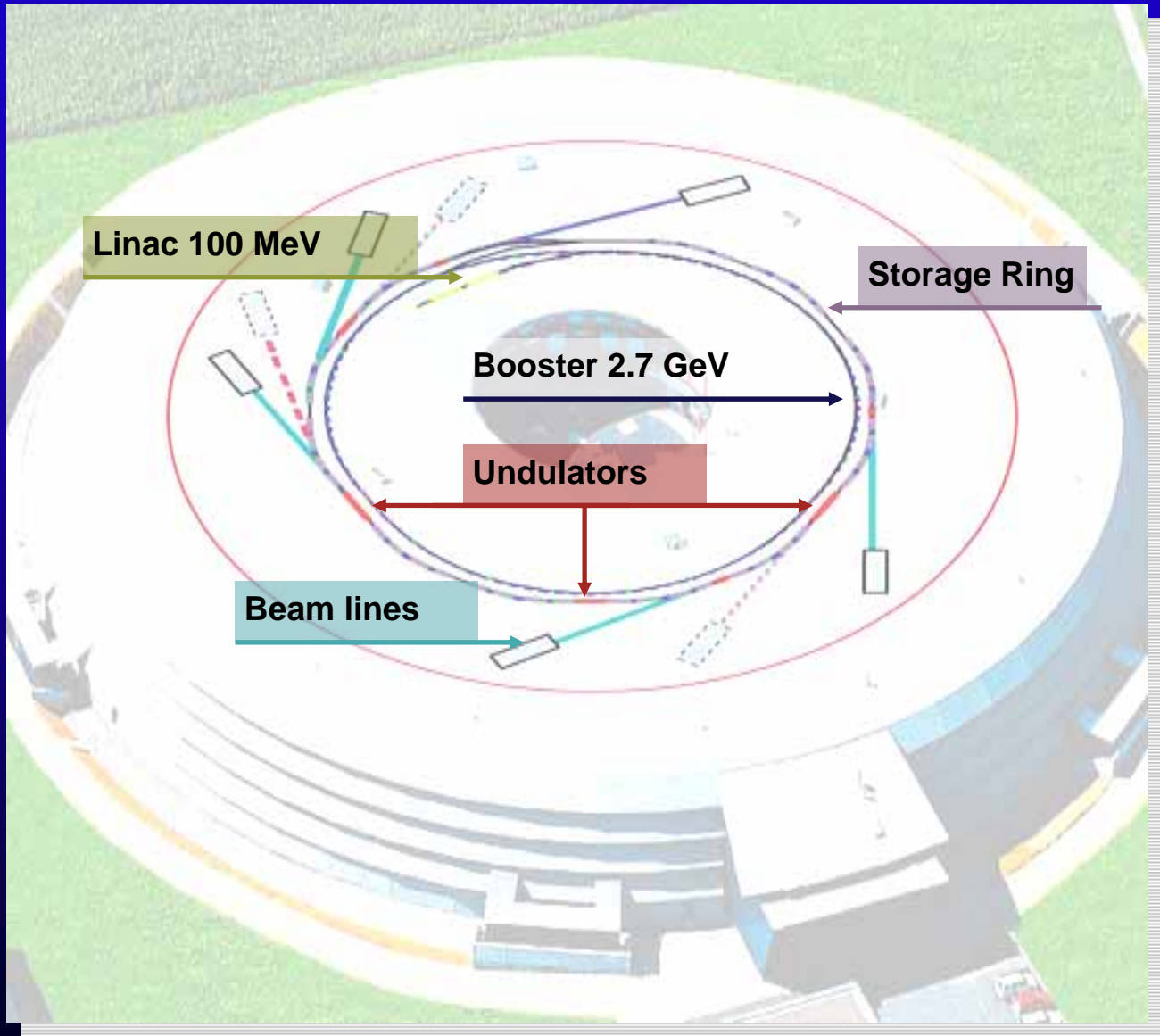


$$B \sim N_e N_u^2 \times 10^3$$



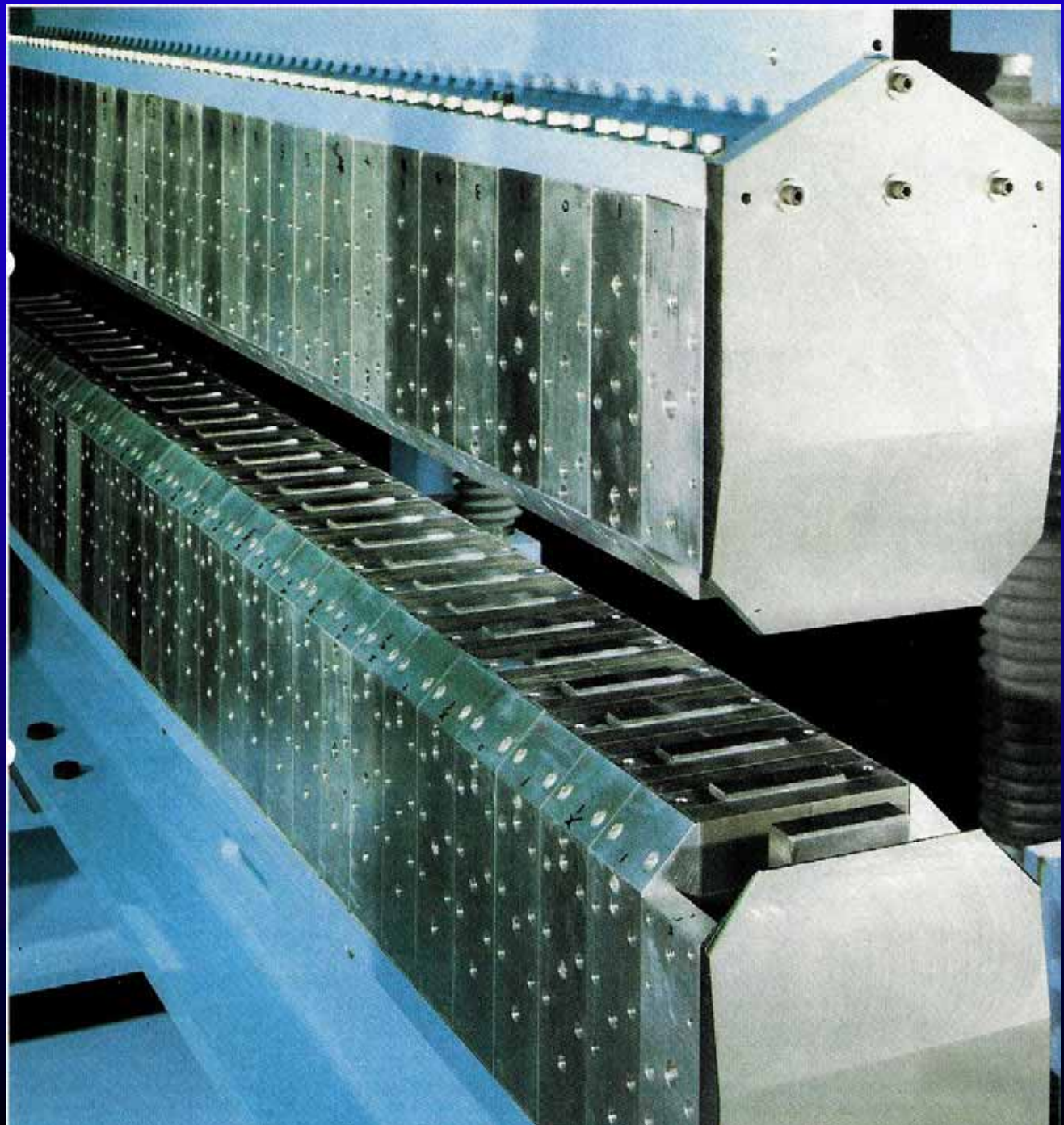
About 60 ring sources world-wide



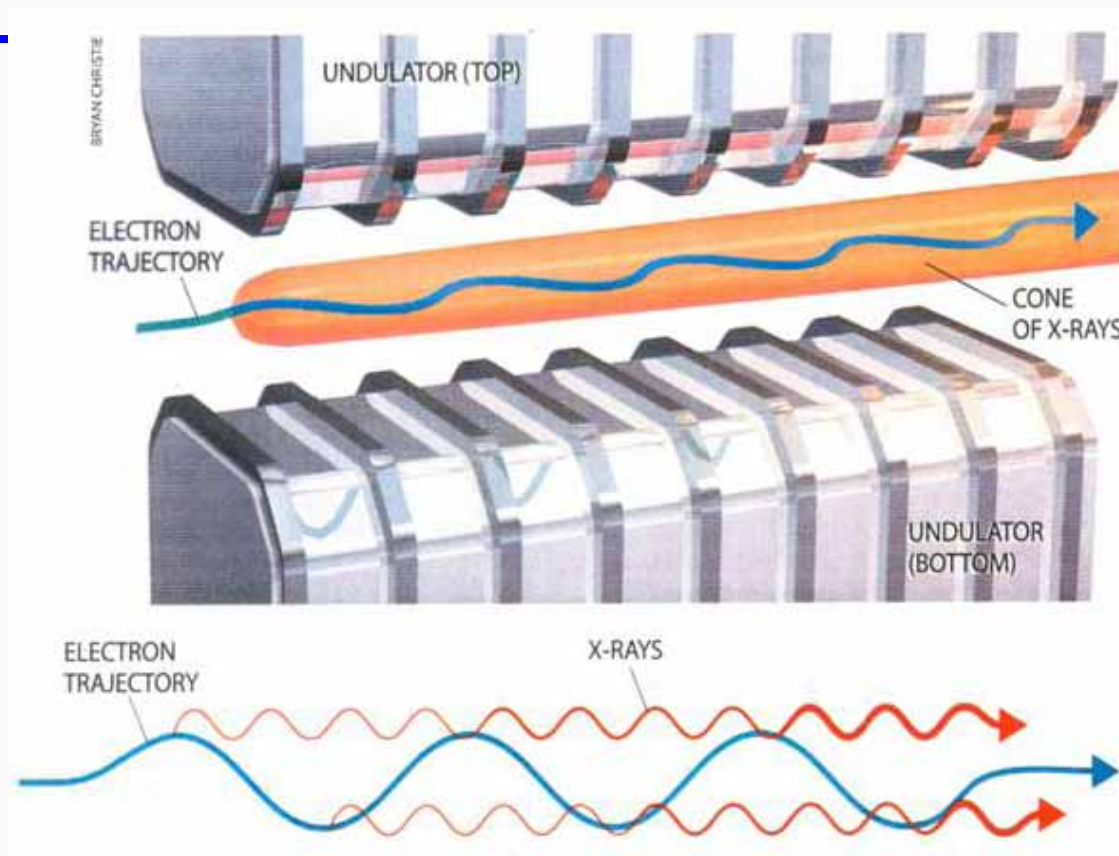


Electromagnetic undulator, long periods (212 mm)





Undulators

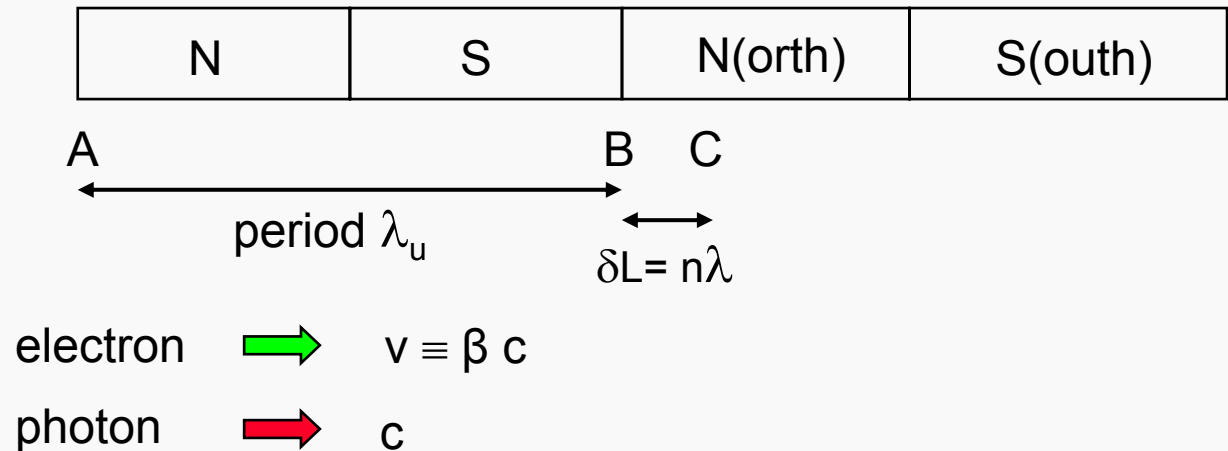


$$T_{obs} = T_{emit} (1 - \beta)$$

$$\lambda_{light} \approx \frac{\lambda_u}{2\gamma^2}$$

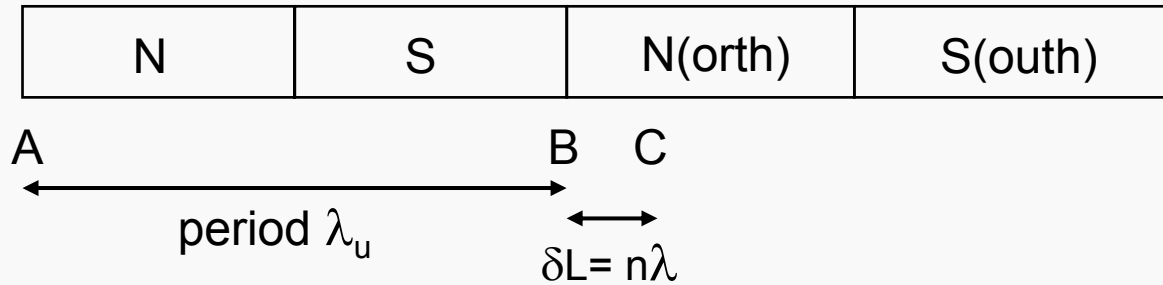
Selection of wavelength in an undulator



In an undulator
an electron
(on a slalom)
races an emitted
photon



at A an electron emits a photon with wavelength λ and flies one period λ_u ahead to B with velocity $v = \beta c$. There it emits another photon with the same wavelength λ . At this moment the first photon is already at C. If the path difference δL corresponds to n wavelengths, then we have a positive interference between the two photons. This enhances the intensity at this wavelength.

Selection of wavelength in an undulator II



electron  $v \equiv \beta c$
 photon  c

The path difference $\delta L \equiv n\lambda \approx (1 - \beta) \lambda_u$, $1 - \beta \approx \frac{1}{2\gamma^2}$

$$\lambda = \frac{\lambda_u}{2n\gamma^2} \left(1 + \frac{K^2}{2} \right)$$

detour through
slalom

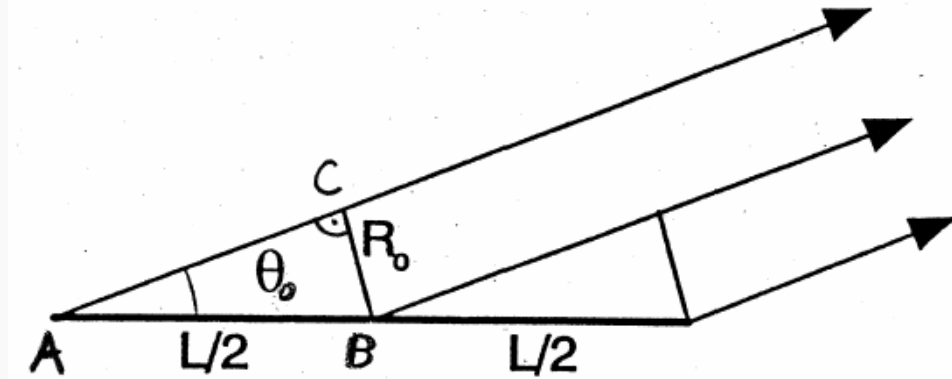
$$K = 0.0934 \cdot \lambda_u [mm] \cdot B [T]$$

Radiation cone of an undulator

Undulator radiates from its whole length L into a narrow cone.

Propagation of the wave front BC is suppressed under an angle θ_0 ,

if the path length AC is just shorter by a half wavelength compared to AB (negative interference). This defines the central cone.



$$\Delta L = AB - AC = \frac{1}{2}L(1 - \cos \theta_0) \approx \frac{1}{4}L\theta_0^2$$

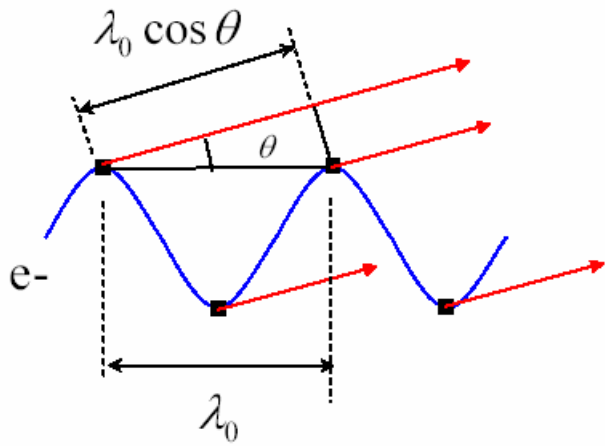
Negative interference for $\Delta L = \frac{\lambda}{2}$

$$\theta_0 = \sqrt{\frac{2\lambda}{L}}$$

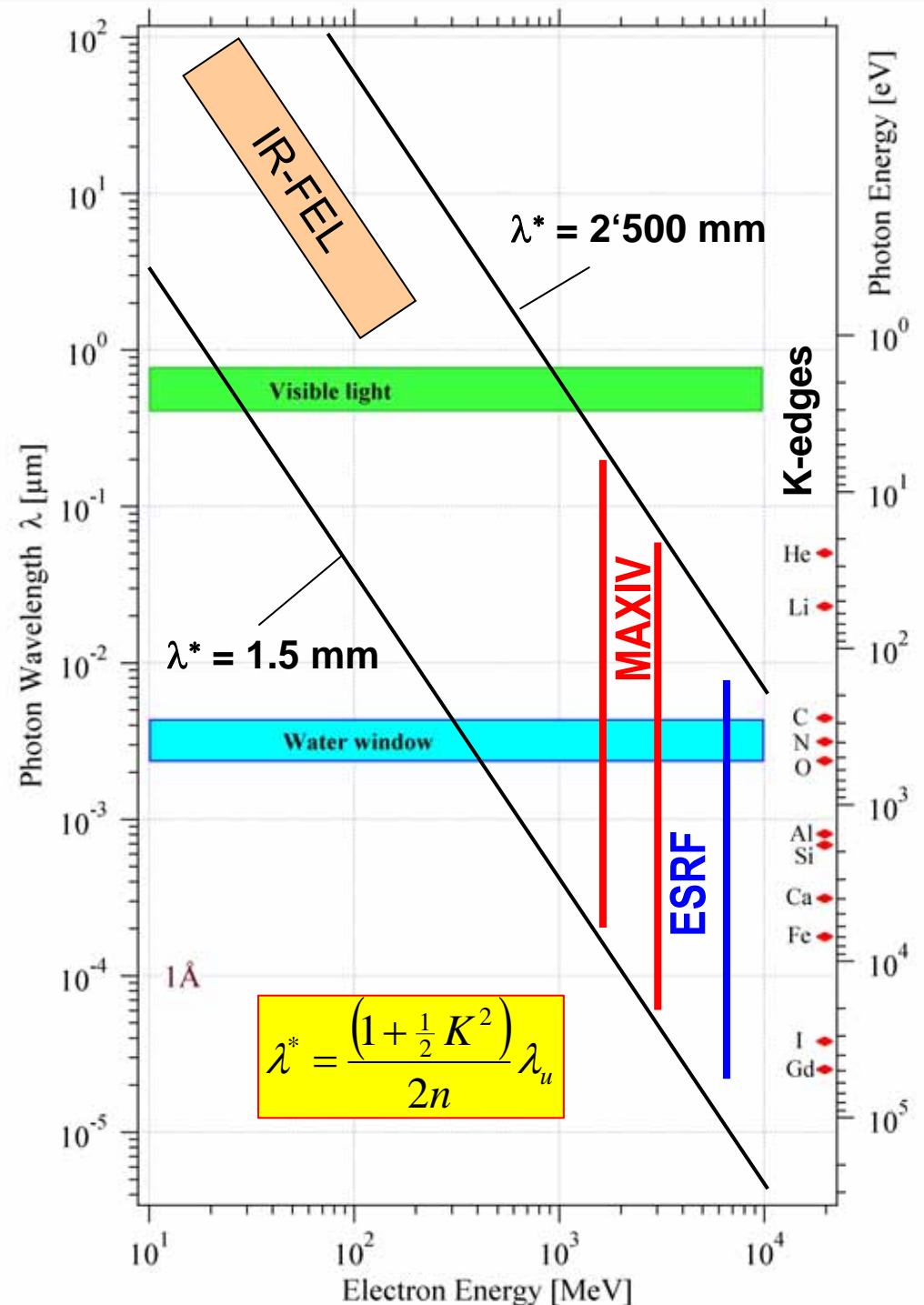
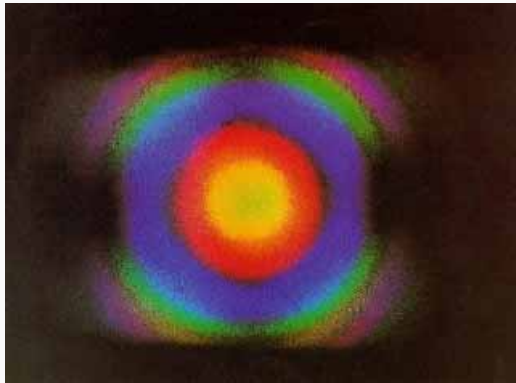
$$R_0 = \sqrt{\frac{\lambda \cdot L}{2}}$$

$$\varepsilon_0 = \theta_0 R_0 = \lambda$$

Undulator radiation



$$\lambda = \frac{\lambda_u}{2n\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$



The Scale of Things – Nanometers and More

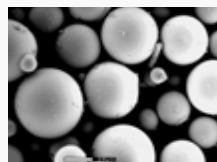
Things Natural



Dust mite
200 μm



Ant
~ 5 mm



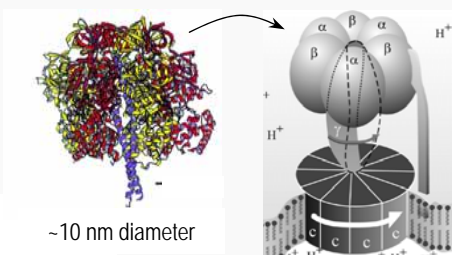
Fly ash
~ 10-20 μm



Human hair
~ 60-120 μm wide

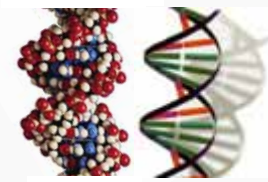


Red blood cells
(~7-8 μm)

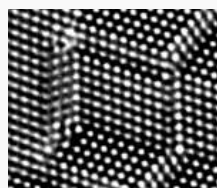


~10 nm diameter

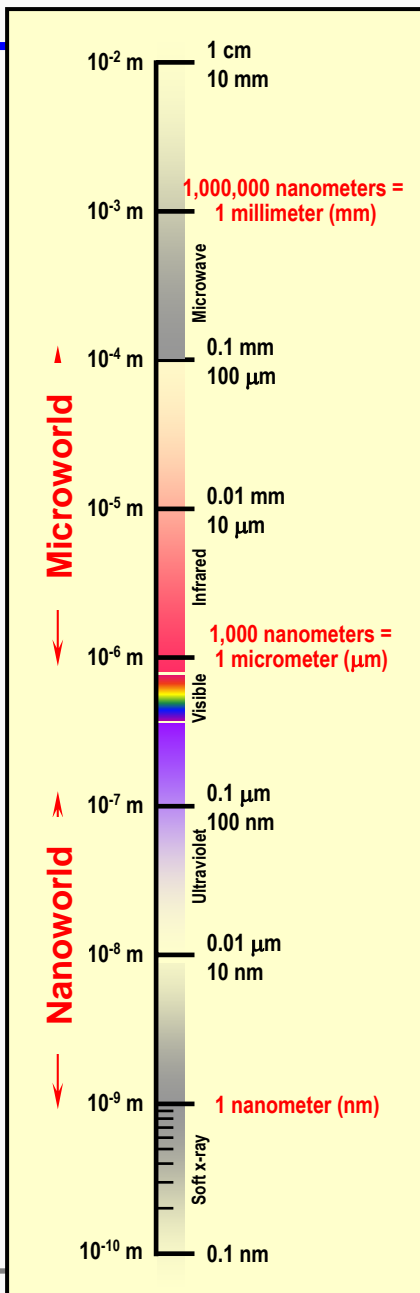
ATP synthase



DNA
~2-1/2 nm diameter



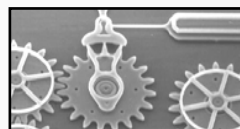
Atoms of silicon
spacing ~tenths of nm



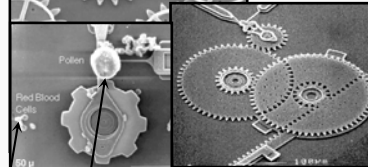
Things Manmade



Head of a pin
1-2 mm

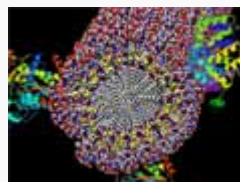


MicroElectroMechanical (MEMS) devices
10-100 μm wide

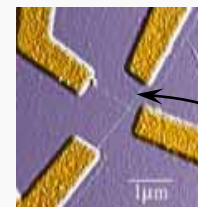


Pollen grain
Red blood cells

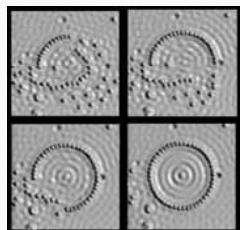
Zone plate x-ray "lens"
Outer ring spacing ~35 nm



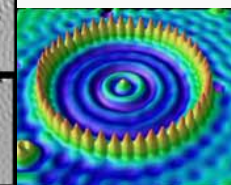
Self-assembled, Nature-inspired structure
Many 10s of nm



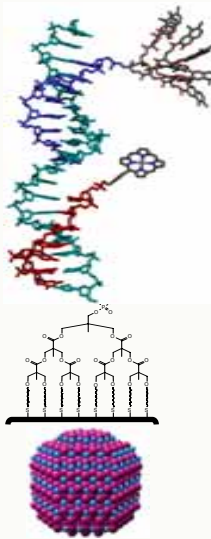
Nanotube electrode



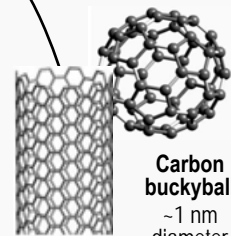
Quantum corral of 48 iron atoms on copper surface
positioned one at a time with an STM tip
Corral diameter 14 nm



The Challenge



Fabricate and combine nanoscale building blocks to make useful devices, e.g., a photosynthetic reaction center with integral semiconductor storage.



Carbon buckyball
~1 nm diameter

Carbon nanotube
~1.3 nm diameter

The electron beam “emittance”:

Source
area, S



Angular
divergence, Ω

The brightness
depends on the
geometry of the
source, i.e., on the
electron beam
emittance

$$\text{Emittance} = S \times \Omega$$

WHAT DO USERS EXPECT FROM A HIGH PERFORMANCE LIGHT SOURCE ?

- PROPER PHOTON ENERGY FOR THEIR EXPERIMENTS
- BRILLIANCE 
- STABILITY

$$B = \frac{\Phi}{(2\pi)^2 \Sigma_x \Sigma_{x'} \Sigma_y \Sigma_{y'}}$$

FIGURE OF MERIT

$$\Sigma^2 = \sigma_e^2 + \sigma_\gamma^2$$

$$\Sigma_x \Sigma_{x'} \approx \sigma_x \sigma_{x'} \sim \varepsilon_x$$

Photon beam size (U):

$$\sigma_{x'} = \sqrt{\frac{\lambda}{L}}$$

$$\sigma_\gamma = \frac{\sqrt{\lambda L}}{4\pi}$$

Undulator based sources

Brightness

$$B = \frac{N_{ph}}{\Delta t} \cdot \frac{1}{\Delta S \cdot \Delta \Omega} \cdot \frac{1}{\Delta \lambda / \lambda}$$

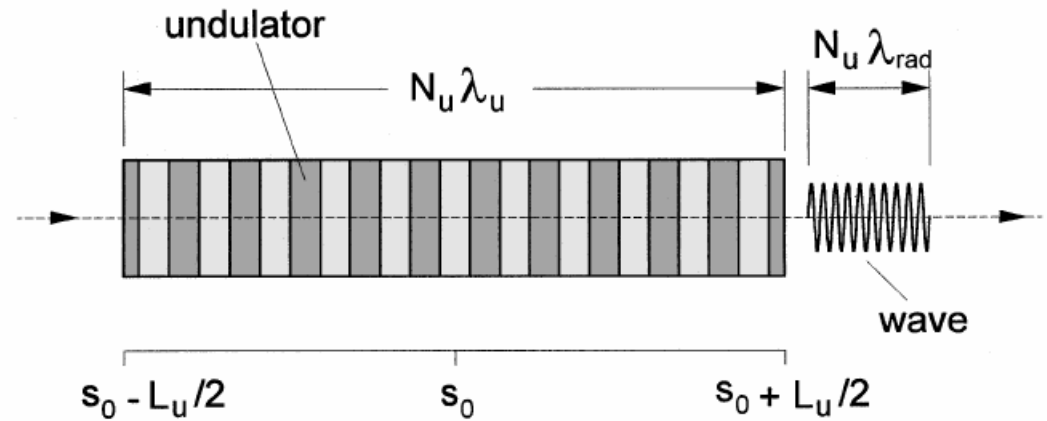
Flux $N_{ph} \propto N_u$ (periods)

The line width $\frac{\Delta \lambda}{\lambda} \sim \frac{1}{N_u}$ **if** $\frac{1}{N_u} > 2\pi \cdot \frac{\sigma_E}{E}$

If energy spread is small enough

$$B \sim N_u^2$$

Undulator line width



Undulator of infinite length

$$N_u = \infty \Rightarrow \frac{\Delta\lambda}{\lambda} = 0$$

Finite length undulator

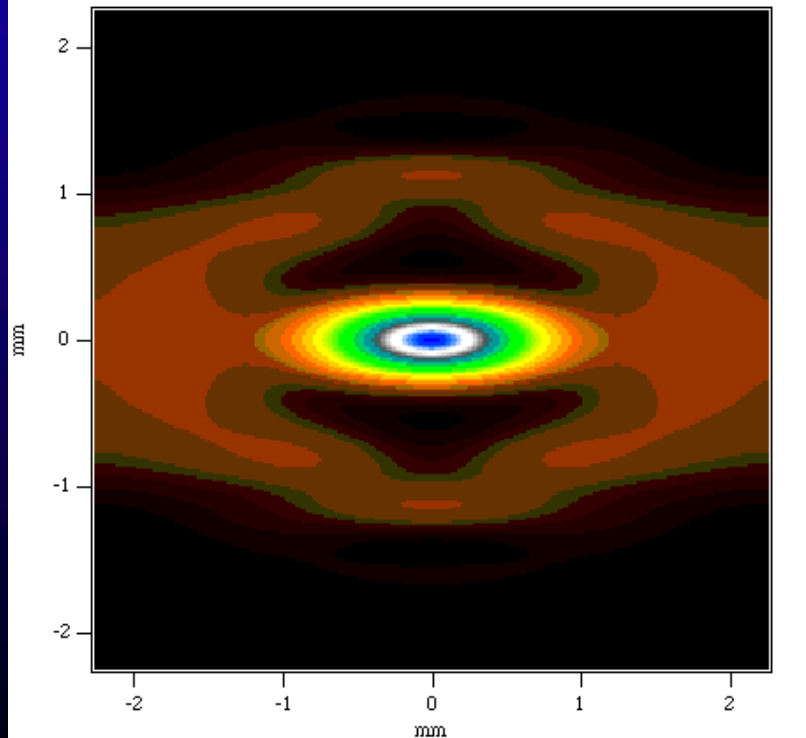
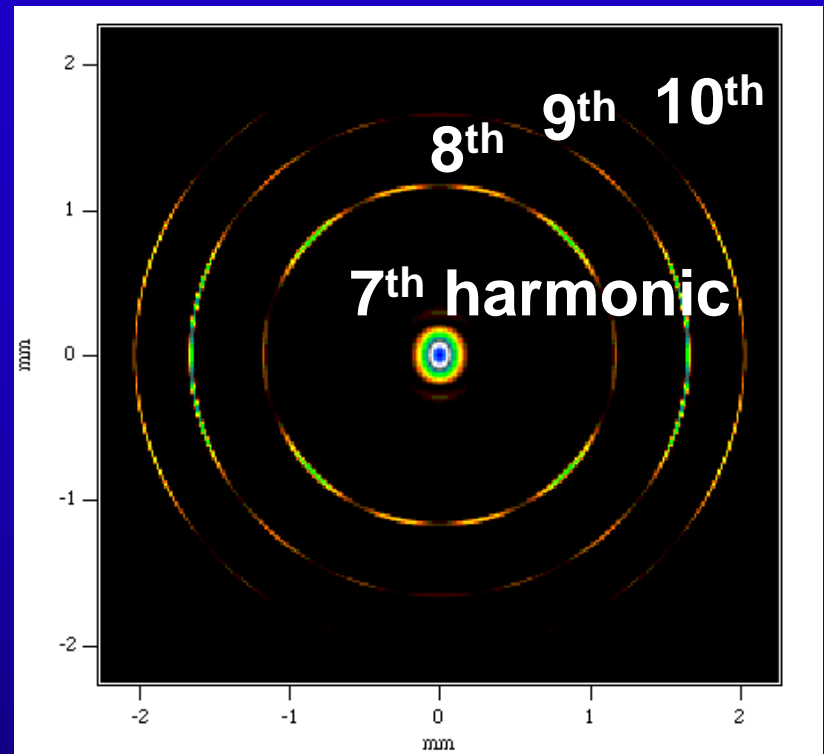
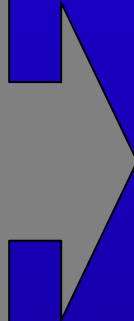
- radiation pulse has as many periods as the undulator
- the line width is

$$\frac{\Delta\lambda}{\lambda} \sim \frac{1}{N_u}$$

Due to the electron energy spread

$$\frac{\Delta\lambda}{\lambda} = 2 \frac{\sigma_E}{E}$$

Undulator radiation
from 6 GeV beam
with zero emittance,
energy spread
(example ESRF)



Emittance 4 nm·rad,
1% coupling,
finite energy spread

Storage ring based sources

The flagships: ESRF, APS, SPring8

- Proof-of-principle, development of new techniques

Medium energy machines: to serve large user community

- Short period, small gap undulators
- Use of higher harmonics
- Stability with top-up

Permanent magnet undulators

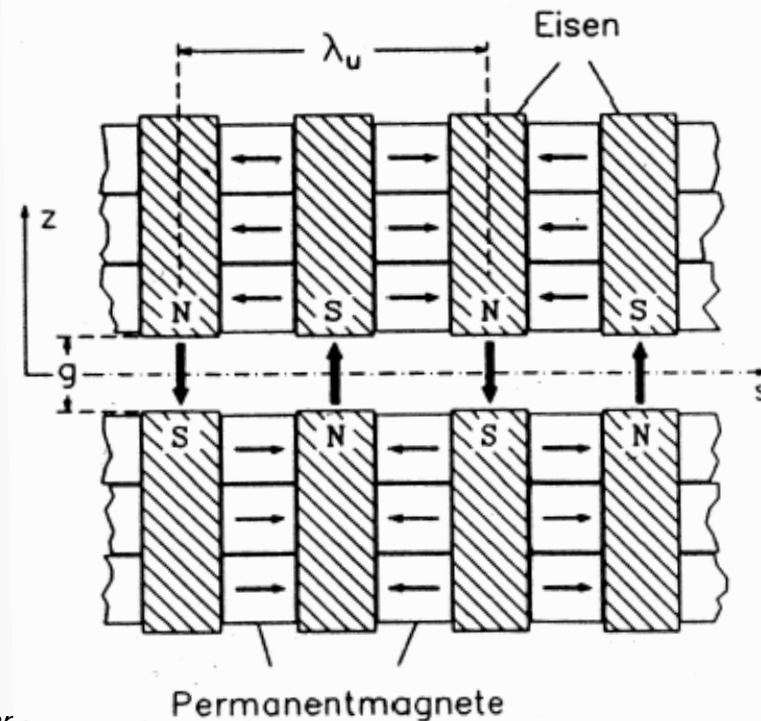
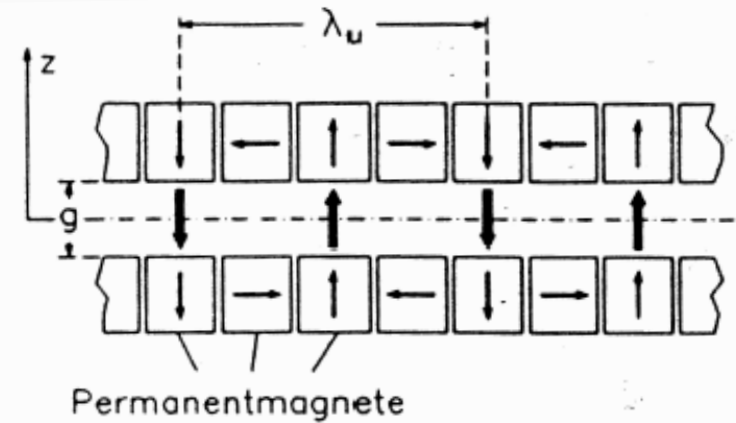
Permanent magnet materials: SmCo_5 , NdFeB

e.g. a pencil made of such material

corresponds to 15'000 A-turns!

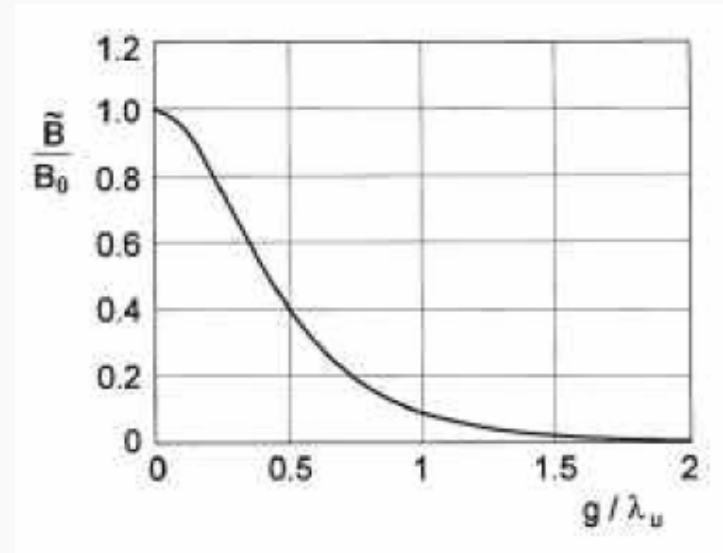
Hybrid undulator:

permanent magnets and iron



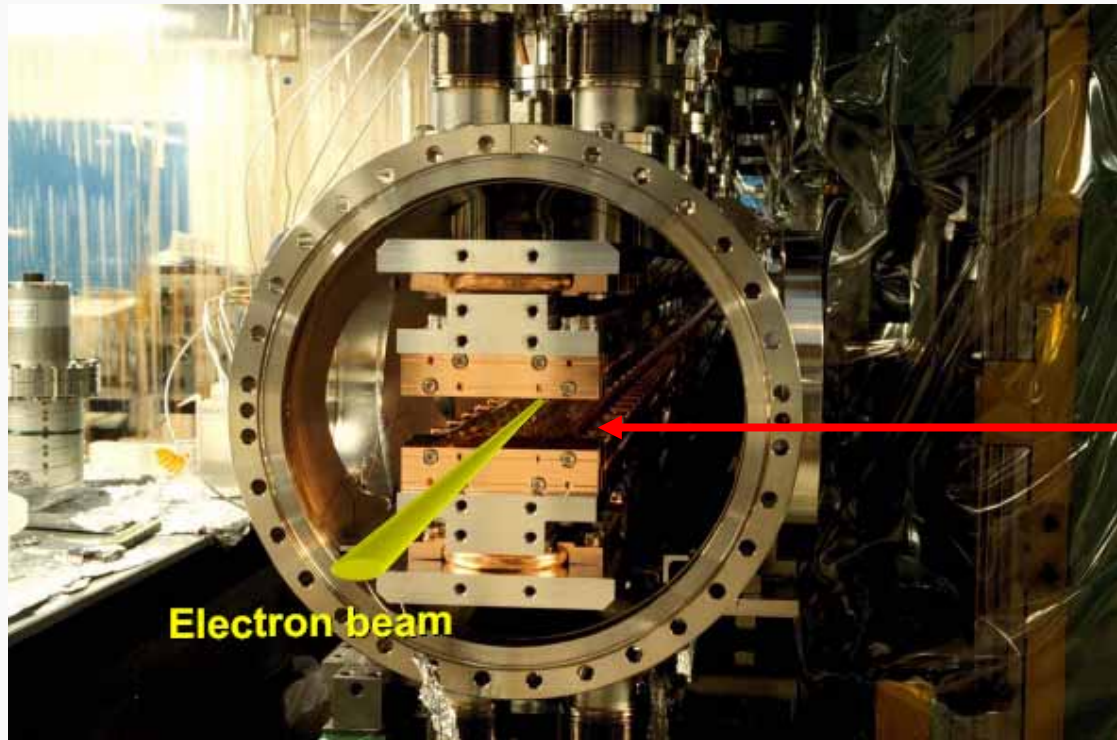
Field tuning with gap

$$B \approx 1.8 \cdot B_r \cdot e^{-\pi \cdot \frac{gap}{\lambda_u}}$$



Permanent magnet material	Remanent field [T]
SmCo ₅	0.9 – 1.0
Sm ₂ Co ₁₇	1.0 – 1.1
NdFeB	1.0 – 1.4

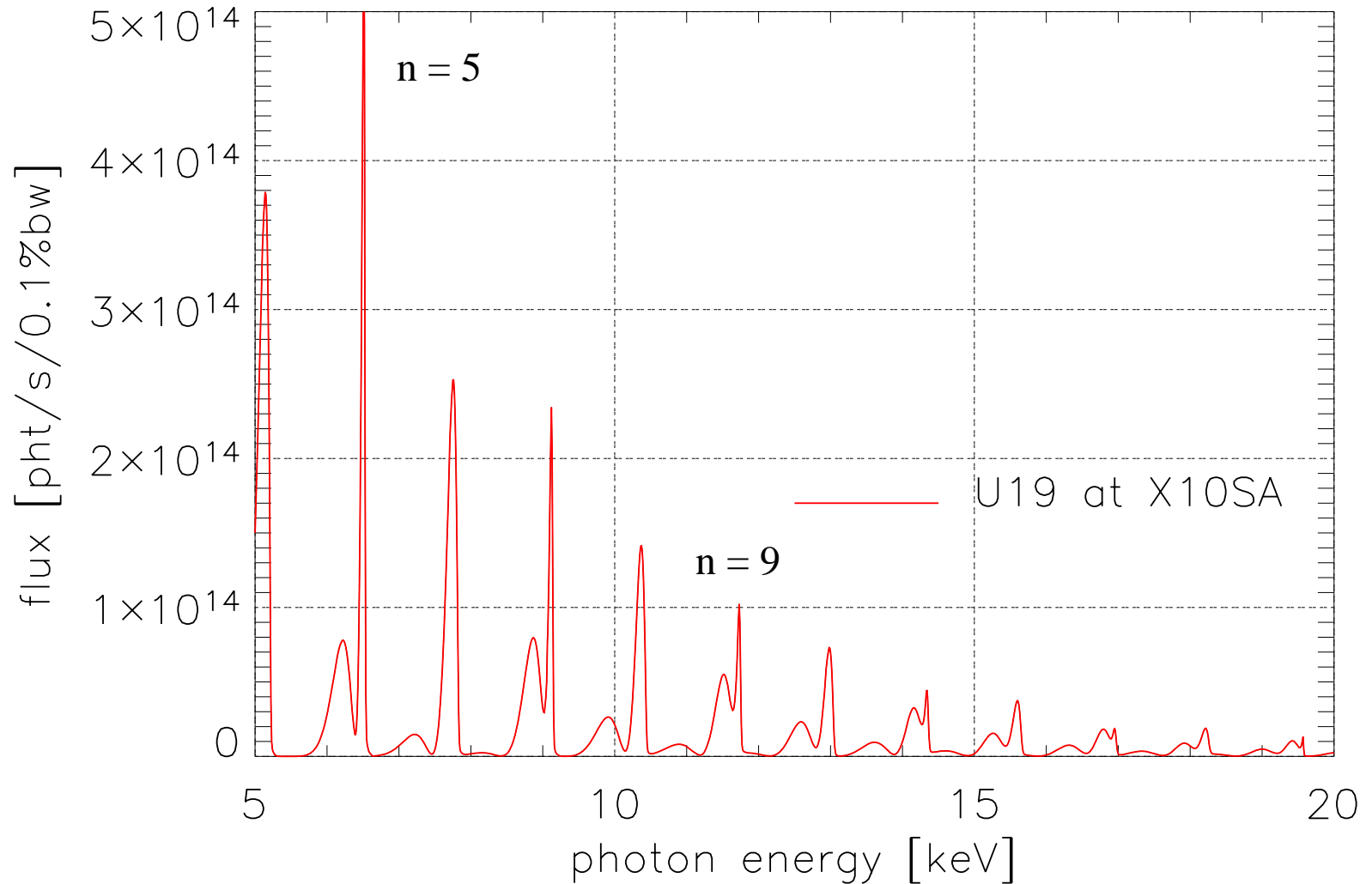
In-vacuum undulators / s.c. undulators



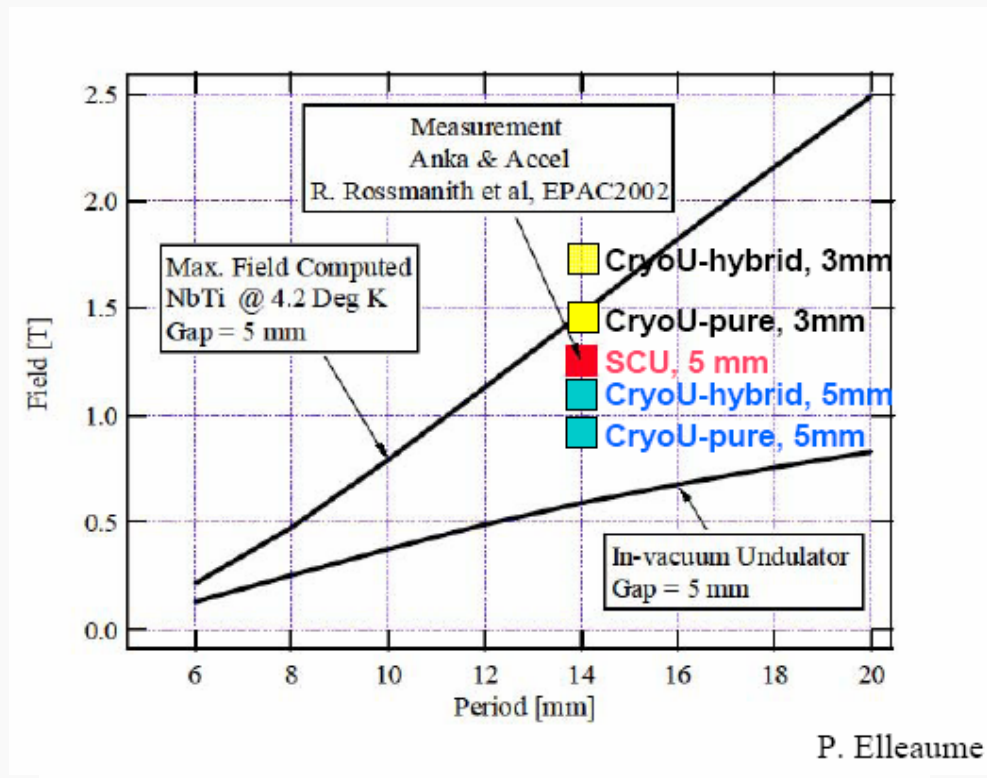
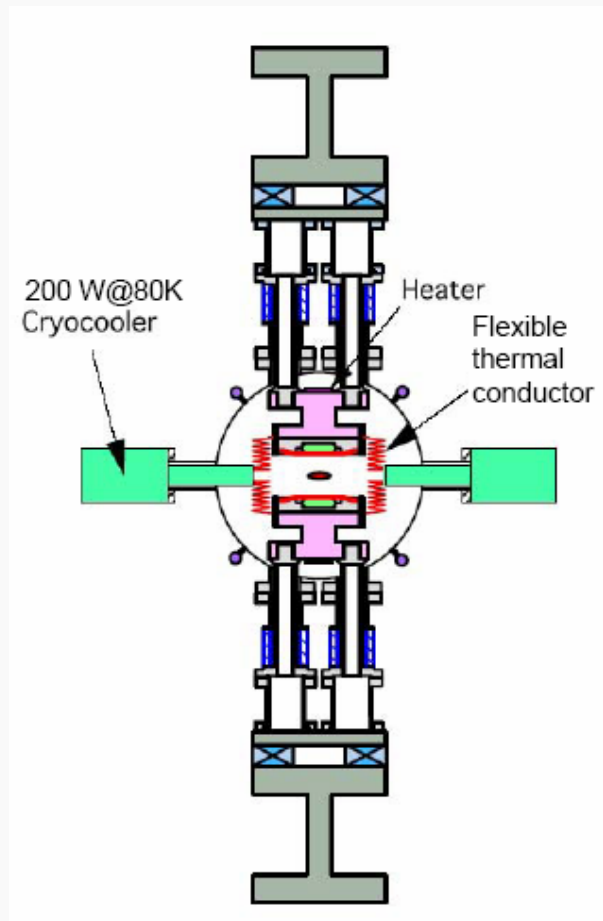
Gaps
down
to
3 mm

High harmonics with small gap (5 mm)

N = 100, K = 1.6

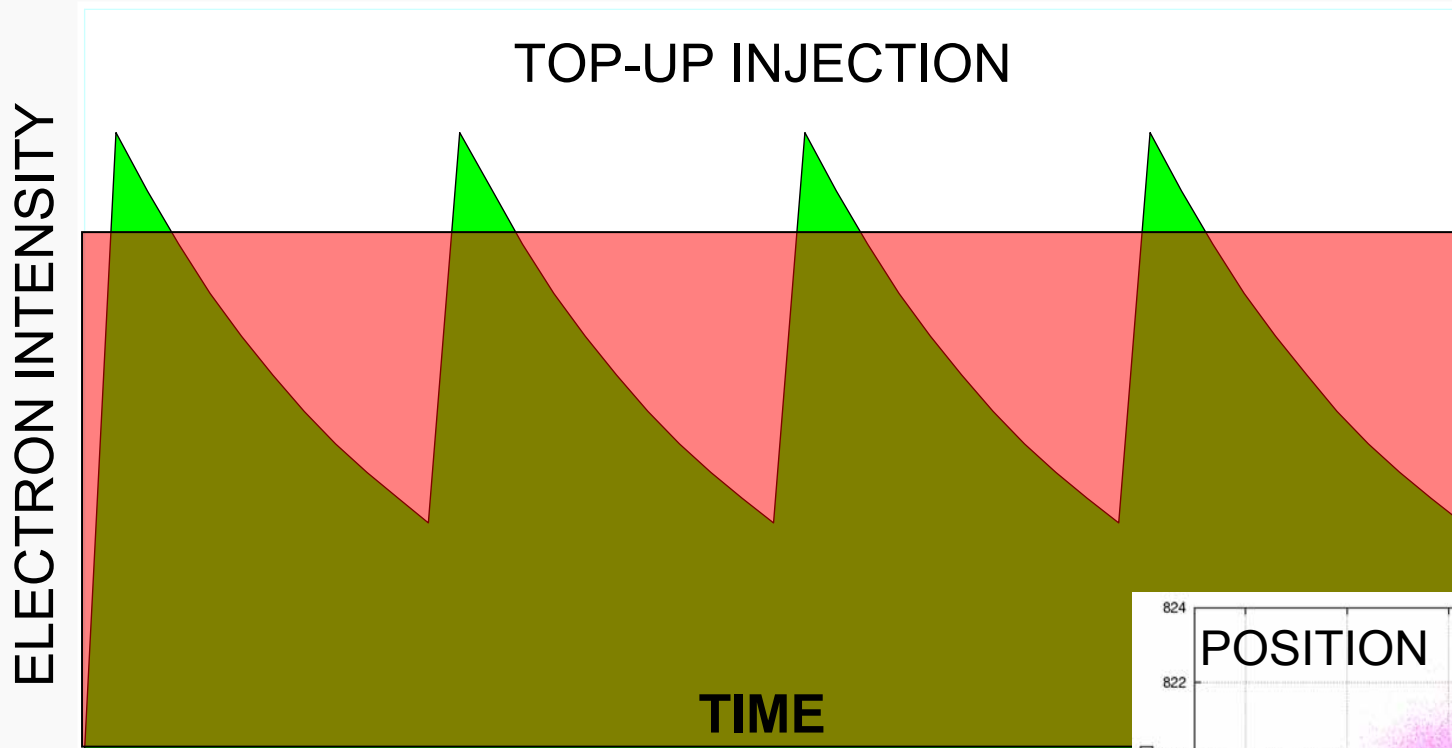


Cryo-cooled undulators

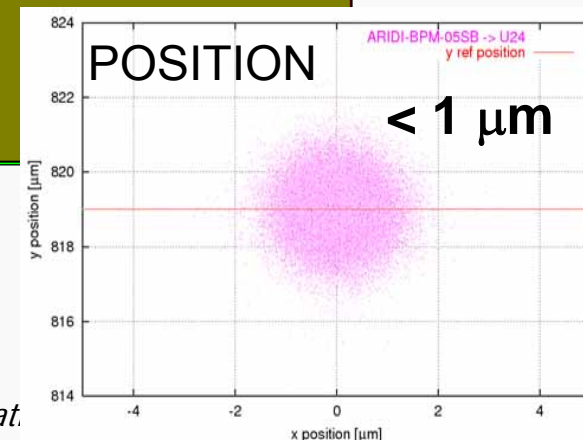


H. Kitamura, SPring-8

INTENSITY STABILITY



Steady state glow at the SLS

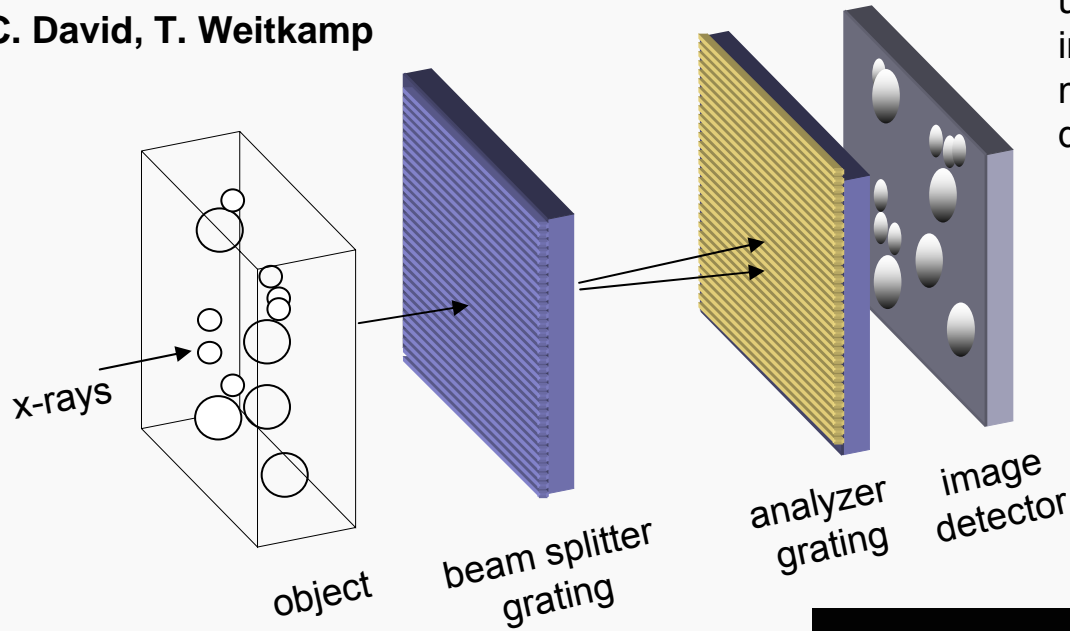


Transverse coherence

- High brightness gives coherence
- Wave optics methods for X-rays
(all chapters in Born & Wolf)
- Holography

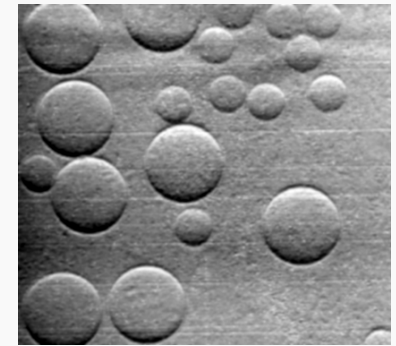
X-ray phase contrast imaging

C. David, T. Weitkamp



using a shearing interferometer based on microfabricated silicon diffraction gratings

F. Pfeiffer et al., PRL 94, April 2005



Phase-object example:
100 μm and 200 μm
styrene beads



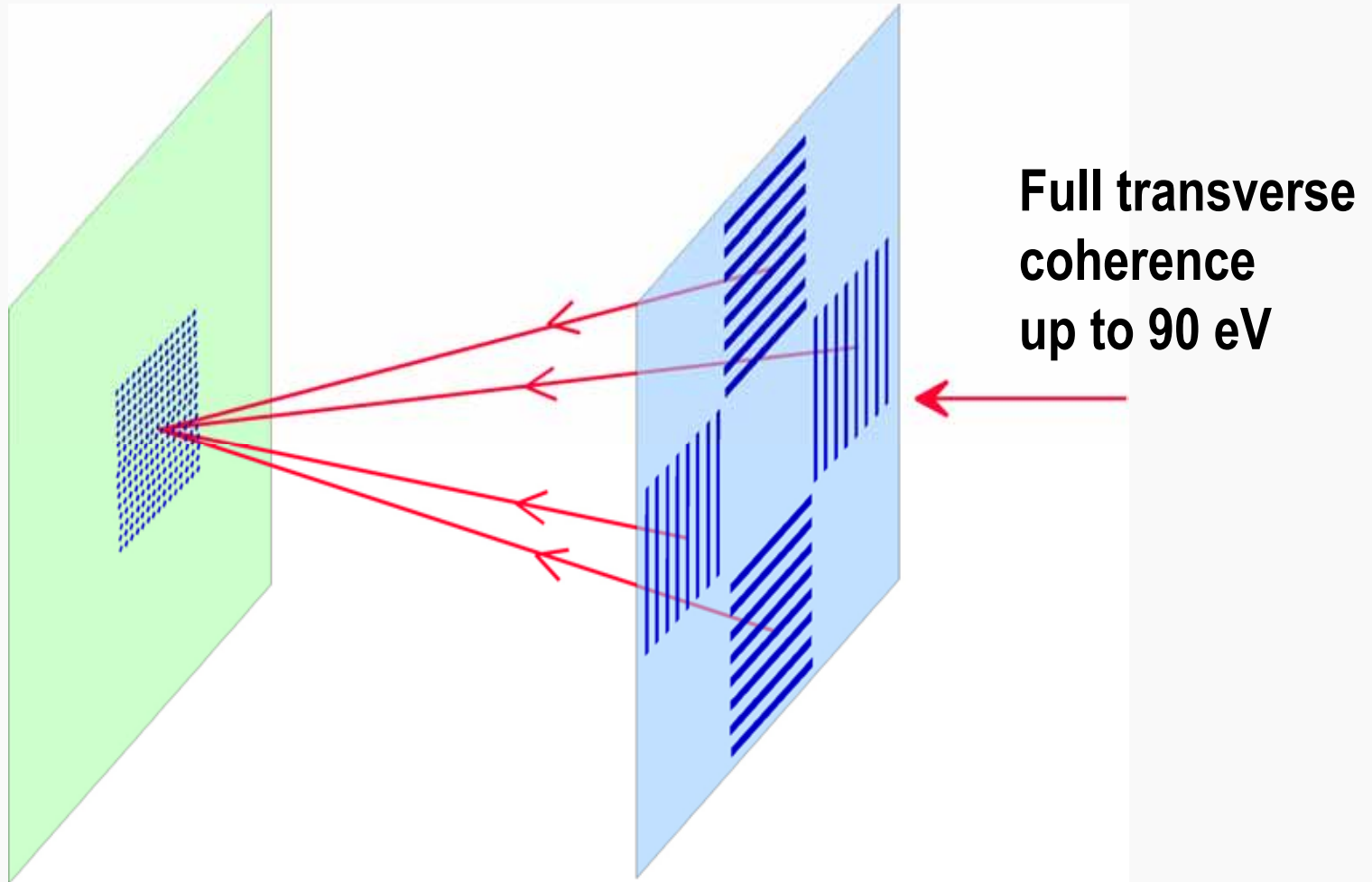
Tomographic phase reconstruction of a spider

Advantages:

- significantly enhanced contrast compared to conventional "absorption-mode" for light materials
- High potential in medical diagnosis and research

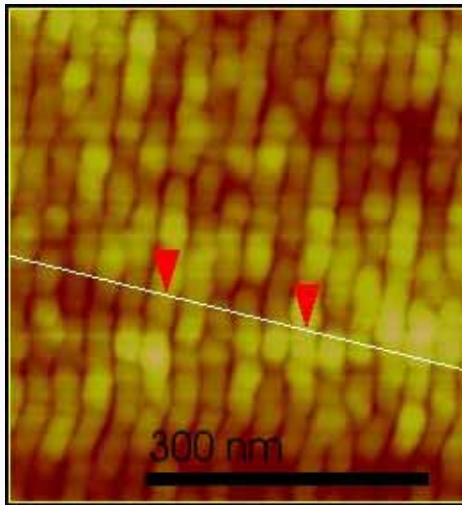
Writing ultra-small structures...

H. Solak, PSI

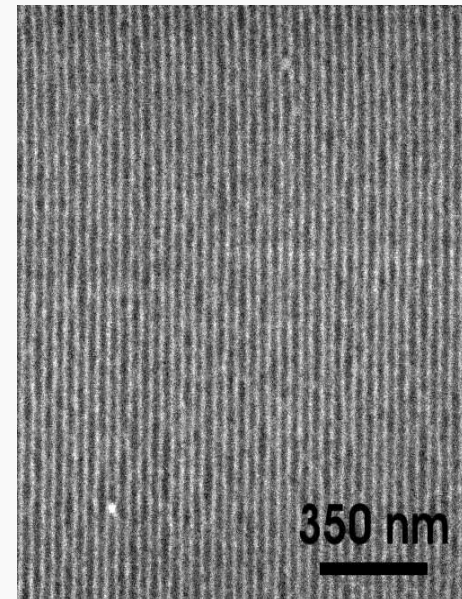


Record resolution in lithography with photon beams

- Large area **15 nm** resolution (30 nm period)*
- 10nm seems feasible
- Directed self-assembly



AFM of 30 nm period grating (PMMA)



SEM of 35 nm period grating (PMMA)

* Previous record stood at 17.5 nm (D. C. Flanders Appl. Phys. Lett. 36, 93 (1980))

1878: E. Muybridge at Stanford

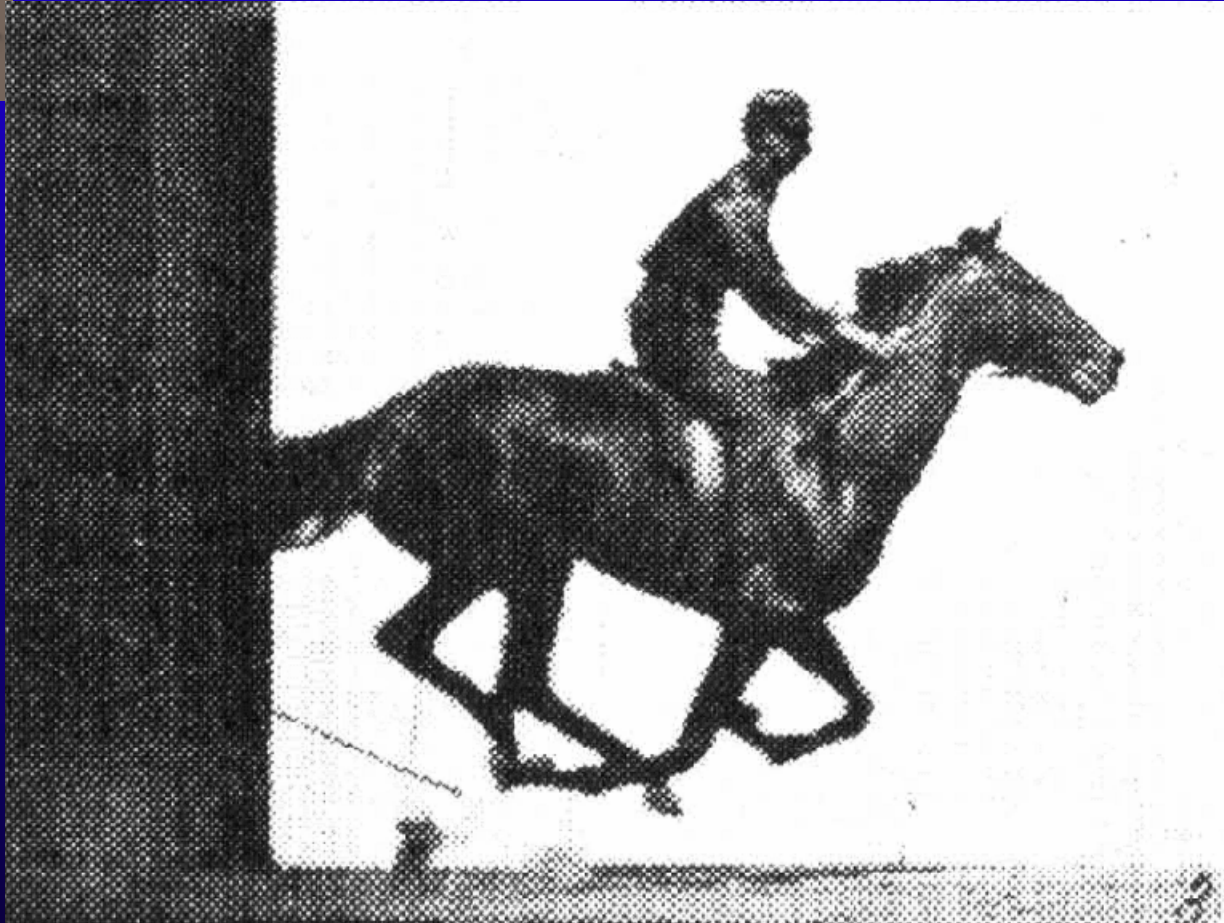
Tracing motion of animals by spark photography



E. Muybridge



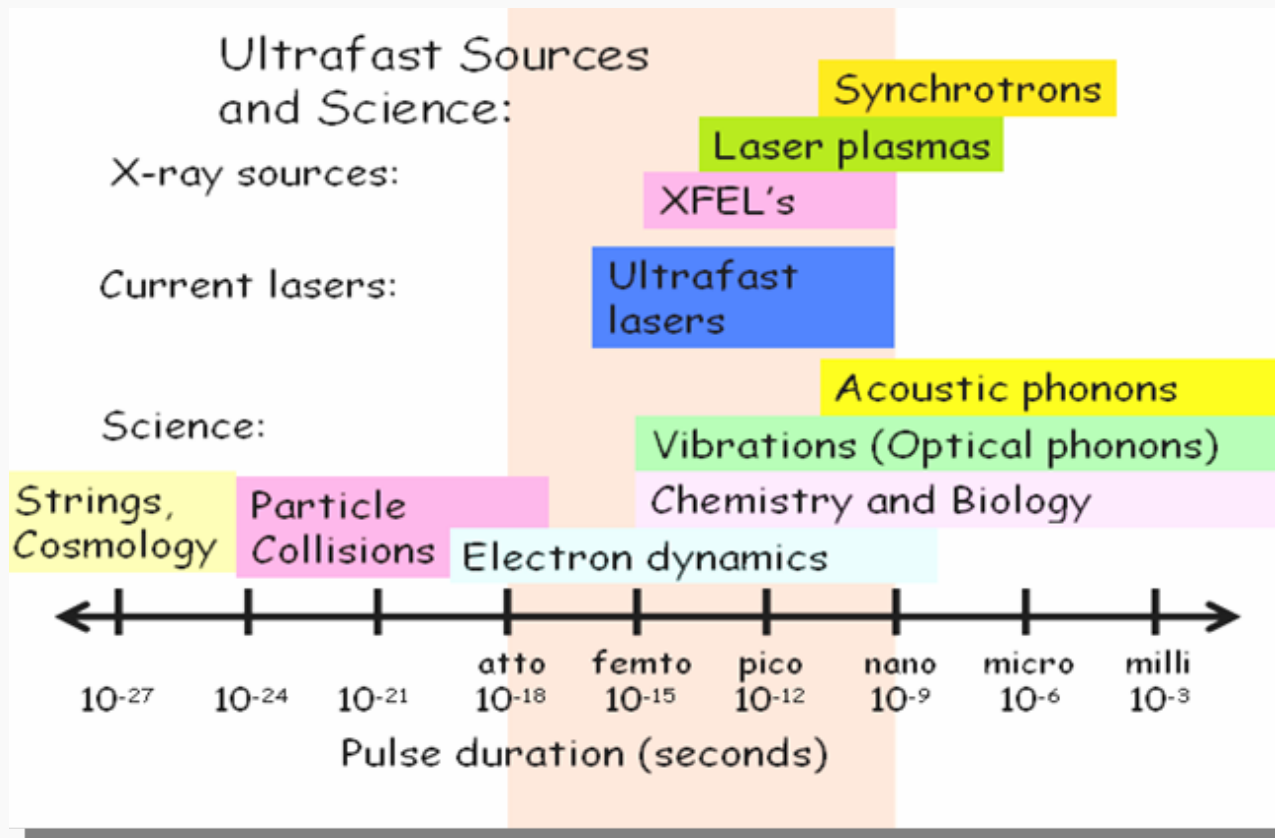
L. Stanford



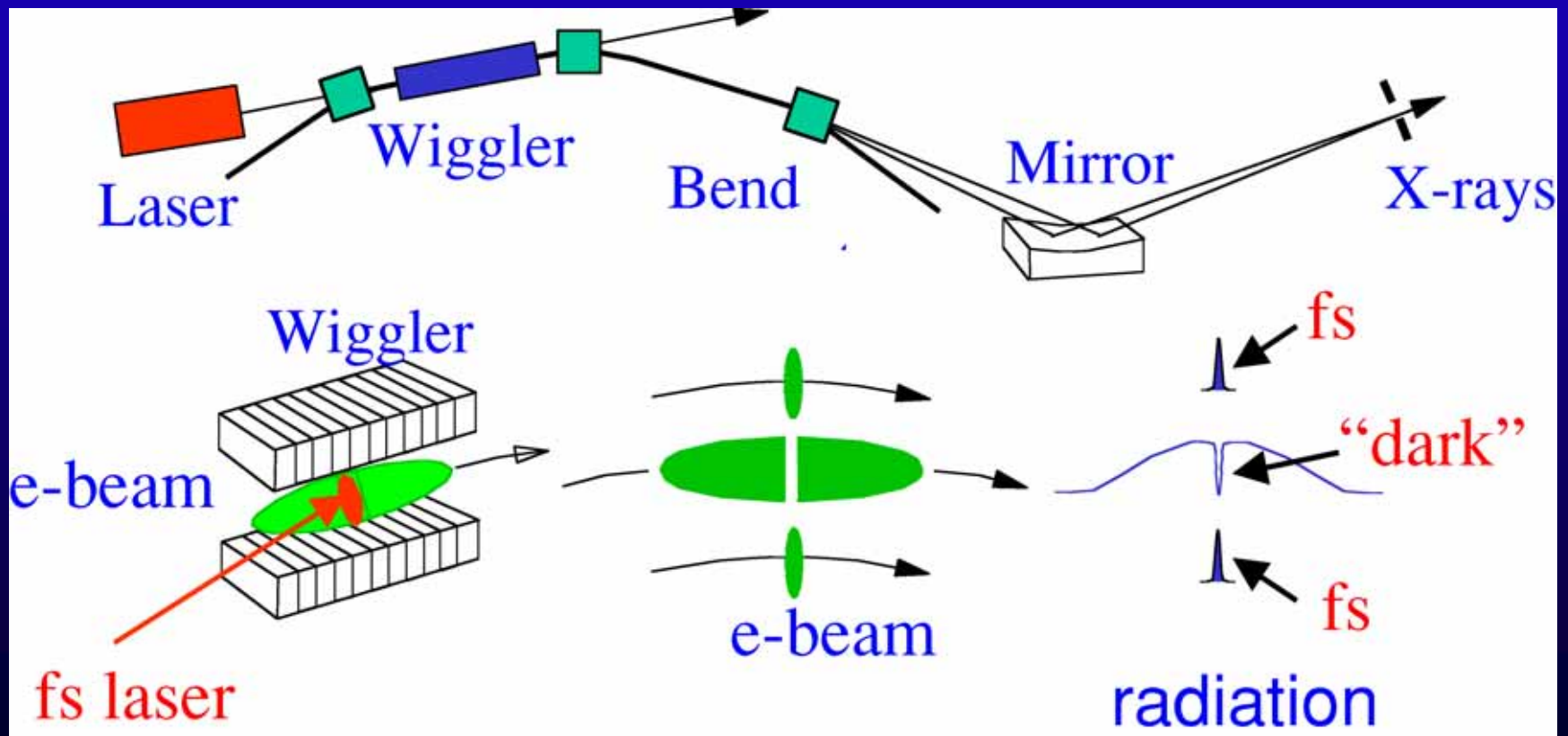
Muybridge and Stanford disagree whether all feet leave the ground at one time during the gallop...

E. Muybridge, *Animals in Motion*, ed. by L. S. Brown (Dover Pub. Co., New York 1957).

Time resolved studies: the relevant time scales



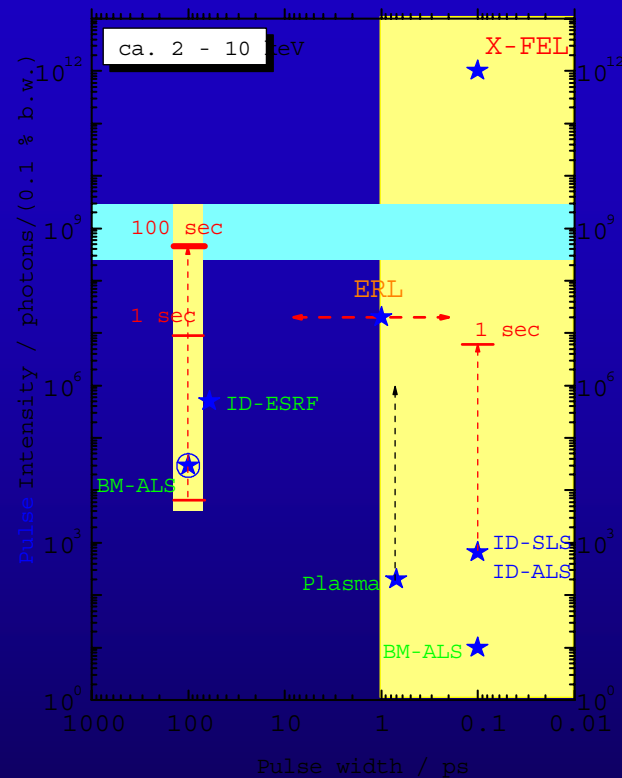
Laser slicing: fs pulses



Low intensity...



Current And Future X-Ray Sources



With pump-probe techniques one can accumulate signal. That helps.