

Outline

Surface, interface, and nanoscience—short introduction

Some surface concepts and techniques→photoemission

Synchrotron radiation: experimental aspects

Electronic structure—a brief review

**The basic synchrotron radiation techniques:
more experimental and theoretical details**

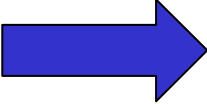
Core-level photoemission



Valence-level photoemission

Microscopy with photoemission

Outline

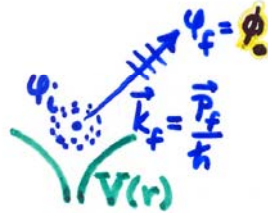
- 
- **Valence-band spectra: low-energy UPS limit and high-energy XPS limit**
 - **Core-level chemical shifts: the potential model**
 - **Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies**
 - **Multiplet splittings**
 - **Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons**
 - **Magnetic circular dichroism (MCD) in core-level emission**
 - **Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)**
 - **Various other final state effects providing information in core-level spectra**

PHOTOELECTRON EMISSION-

BASIC MATRIX ELEMENTS + SELECTION RULES:

• ATOMIC-LIKE (LOCALIZED) STATES \Rightarrow CORE:

$$\psi_i(\vec{r}) = \psi_{n_i, l_i, m_i}(\vec{r}, \theta, \phi) = R_{n_i, l_i}(r) Y_{l_i, m_i}(\theta, \phi)$$



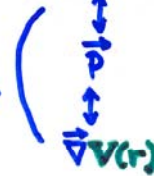
$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f)$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f, m_f}^*(\theta, \phi) Y_{l_f, m_f}(\theta, \phi) R_{E_f, l_f}(r)$$

PHASE SHIFT OF l_f WAVE IN $V(r)$

DIPOLE: INT. $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2 \Rightarrow$

EQUIVALENT WITHIN CONSTANT FACTOR



- $\Delta l = l_f - l_i = \pm 1$
TWO CHANNELS
- $\Delta m = m_f - m_i = 0, \pm 1$
LINEAR POLARIZ.
- $\Delta m = \pm 1$, CIRCULAR POLARIZATION

VALENCE BANDS IN SOLIDS:

• BLOCH-FUNCTION (DELOCALIZED) STATES \Rightarrow VALENCE:

$$\psi_i(\vec{r}) = u_{\vec{k}_i}(\vec{r}) e^{i\vec{k}_i \cdot \vec{r}}$$

$$\psi_f(\vec{r}) = u_{\vec{k}_f}(\vec{r}) e^{i\vec{k}_f \cdot \vec{r}}; E_f = \frac{p_f^2}{2m} = \frac{\hbar^2 k_f^2}{2m}$$

USUALLY NEGLIG.



$$|\langle \psi_f | \hat{E} \cdot \vec{p} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{p} | \psi_i \rangle|^2 \Rightarrow \Delta \vec{k} = \vec{k}_f - \vec{k}_i = \vec{k}_{ph} + \vec{k}_{phonon}$$

$$= \vec{g}_{BULK} \text{ (OR } \vec{g}_{SURF})$$

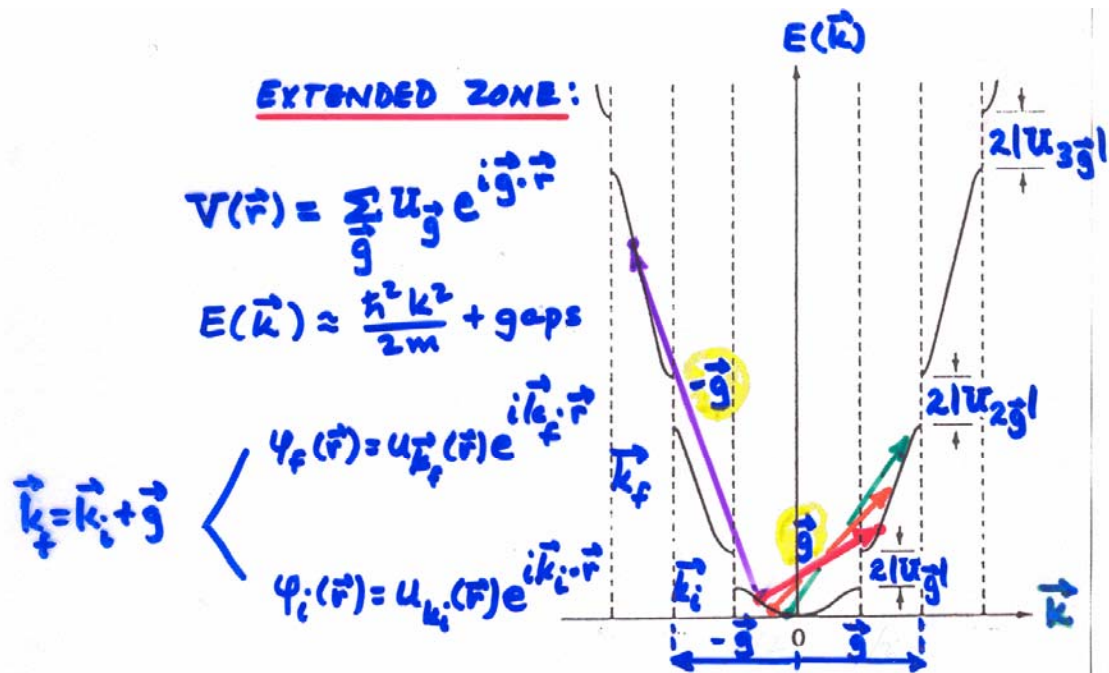
"DIRECT" TRANSITIONS

BUT LATTICE VIBRATIONS \Rightarrow SUM OVER \vec{k}_{PHONON}

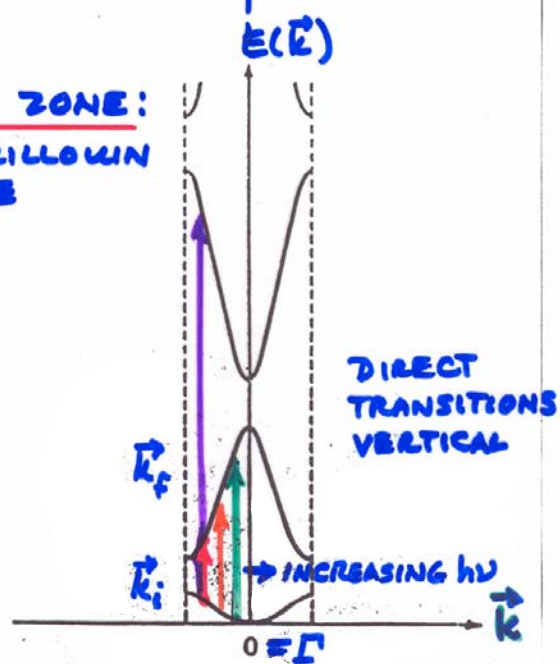
\Rightarrow FRACTION DIRECT \approx DEBYE-WALLER FACTOR

$$= \exp[-g^2 \bar{u}^2]$$

NEARLY-FREE ELECTRONS IN A WEAK PERIODIC POTENTIAL—1 DIM.



REDUCED ZONE:
= FIRST BRILLOUIN ZONE



ALUMINUM - ELECTRONIC BANDS & D.O.S.

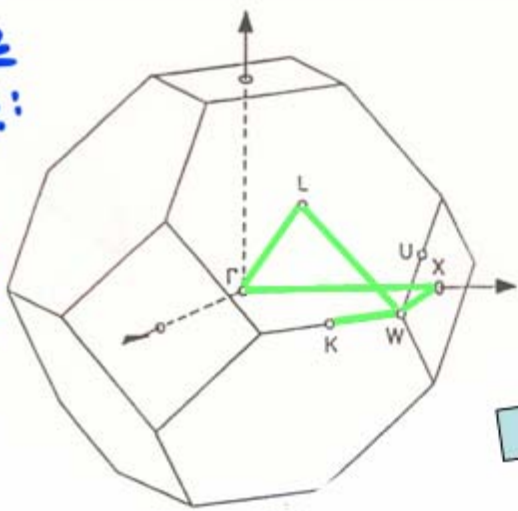
The electronic structure of a nearly free-electron metal—fcc Al

$$\psi(\vec{r}) = u_{\vec{k}}(\vec{r}) e^{i\vec{k}\cdot\vec{r}}; E(\vec{k}) \approx \frac{\hbar^2 k^2}{2m}$$

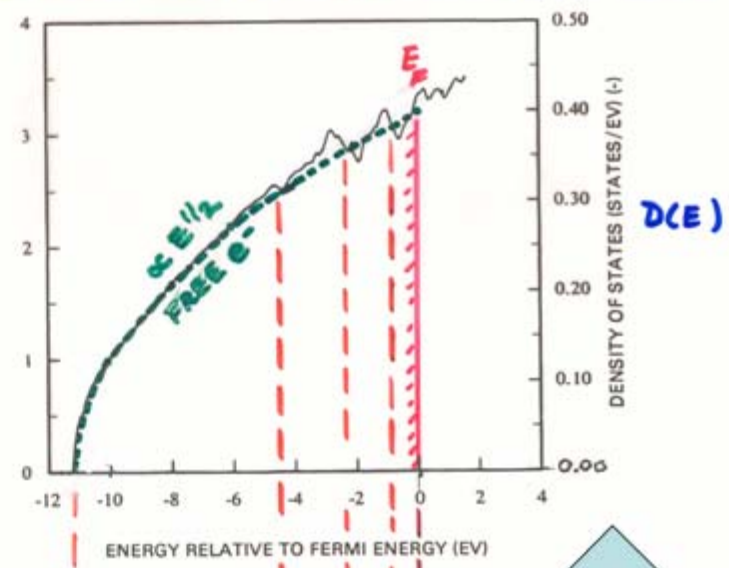
(Bloch)

3D Brillouin zone

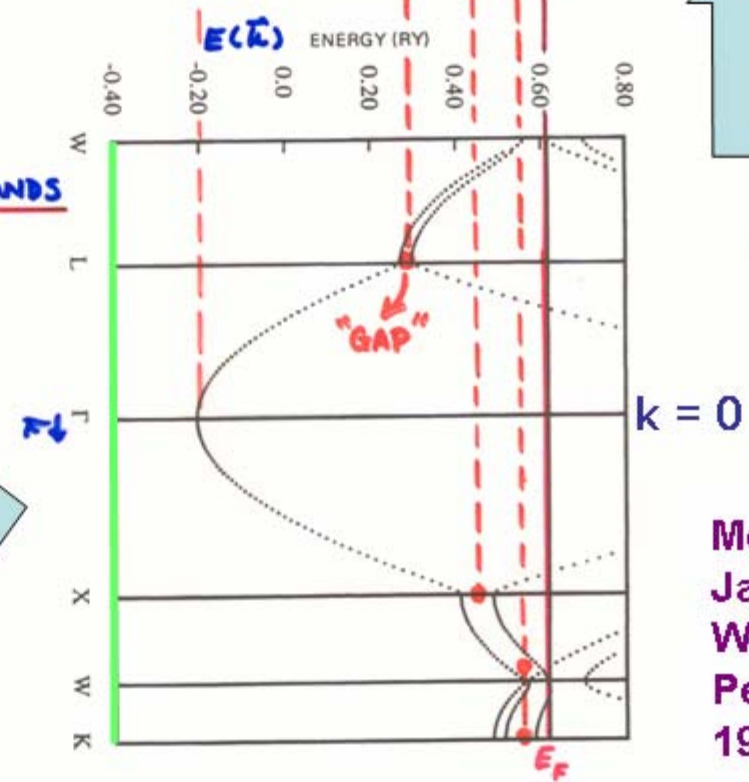
REAL
fcc:
↓
RECIP.
bcc



D.O.S.

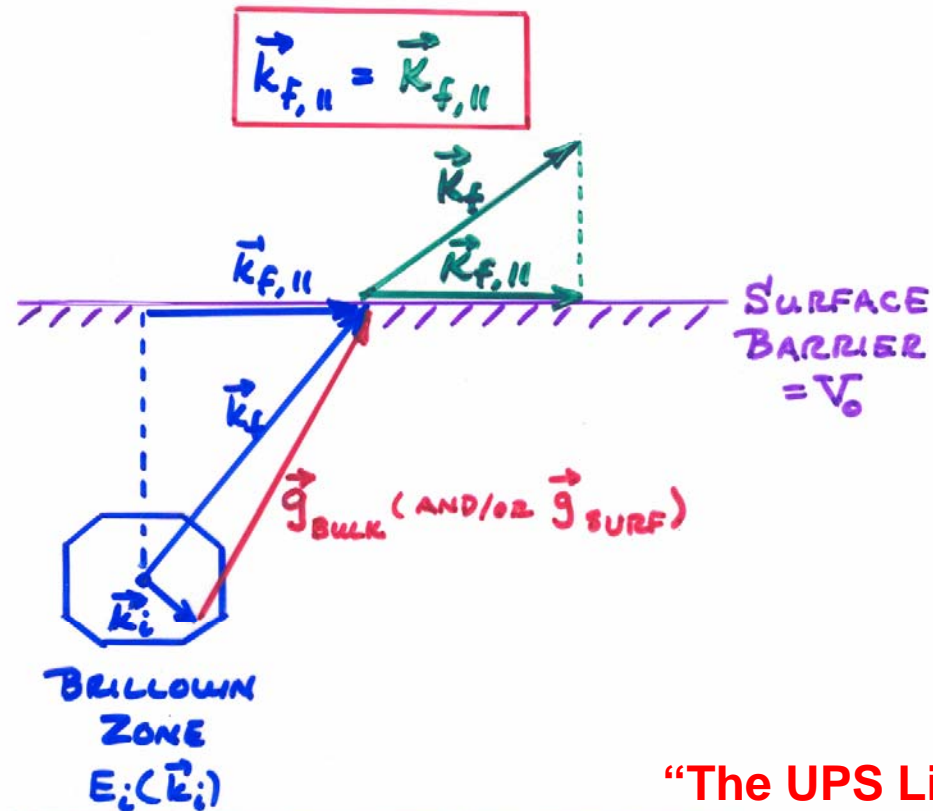


BANDS



Moruzzi,
Janak,
Williams,
Pergamon,
1978

CONSERVATION LAWS IN VALENCE-BAND PHOTOELECTRON SPECTROSCOPY:

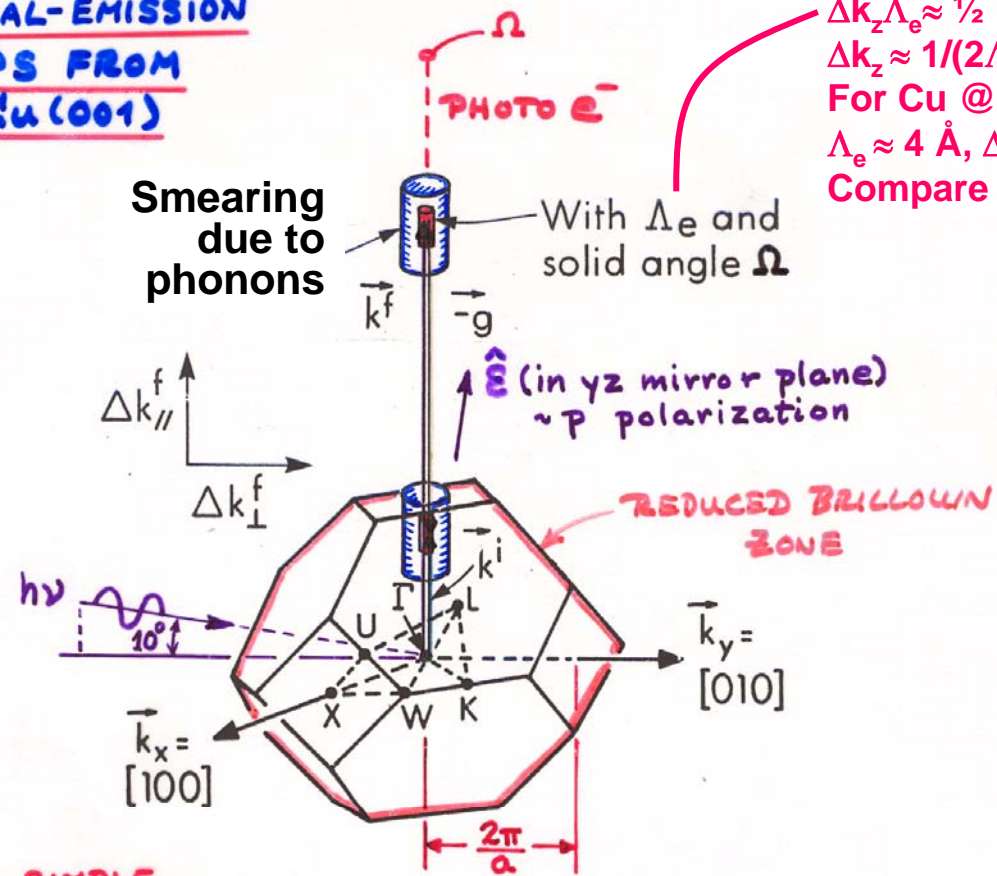


$$\vec{k}_f = \vec{k}_i + \vec{q}_{\text{BULK}} (\vec{q}_{\text{SURFACE}}) + \cancel{\vec{k}_{\text{ph}} + \vec{k}_{\text{PHONON}}}$$

NEGLIGIBLE: $h\nu \lesssim 500$ eV IF $h\nu$ AND/OR T LOW ENOUGH

EXAMPLE:
NORMAL-EMISSION
UPS FROM
Cu(001)

$\Delta p_z \Delta z \approx \hbar/2$
 $\Delta k_z \Delta_e \approx 1/2$
 $\Delta k_z \approx 1/(2\Delta_e)$
 For Cu @ $E_{kin} \approx 80$ eV,
 $\Delta_e \approx 4$ Å, $\Delta k_z \approx 0.12$ Å⁻¹
 Compare $2\pi/a = 0.98$ Å⁻¹



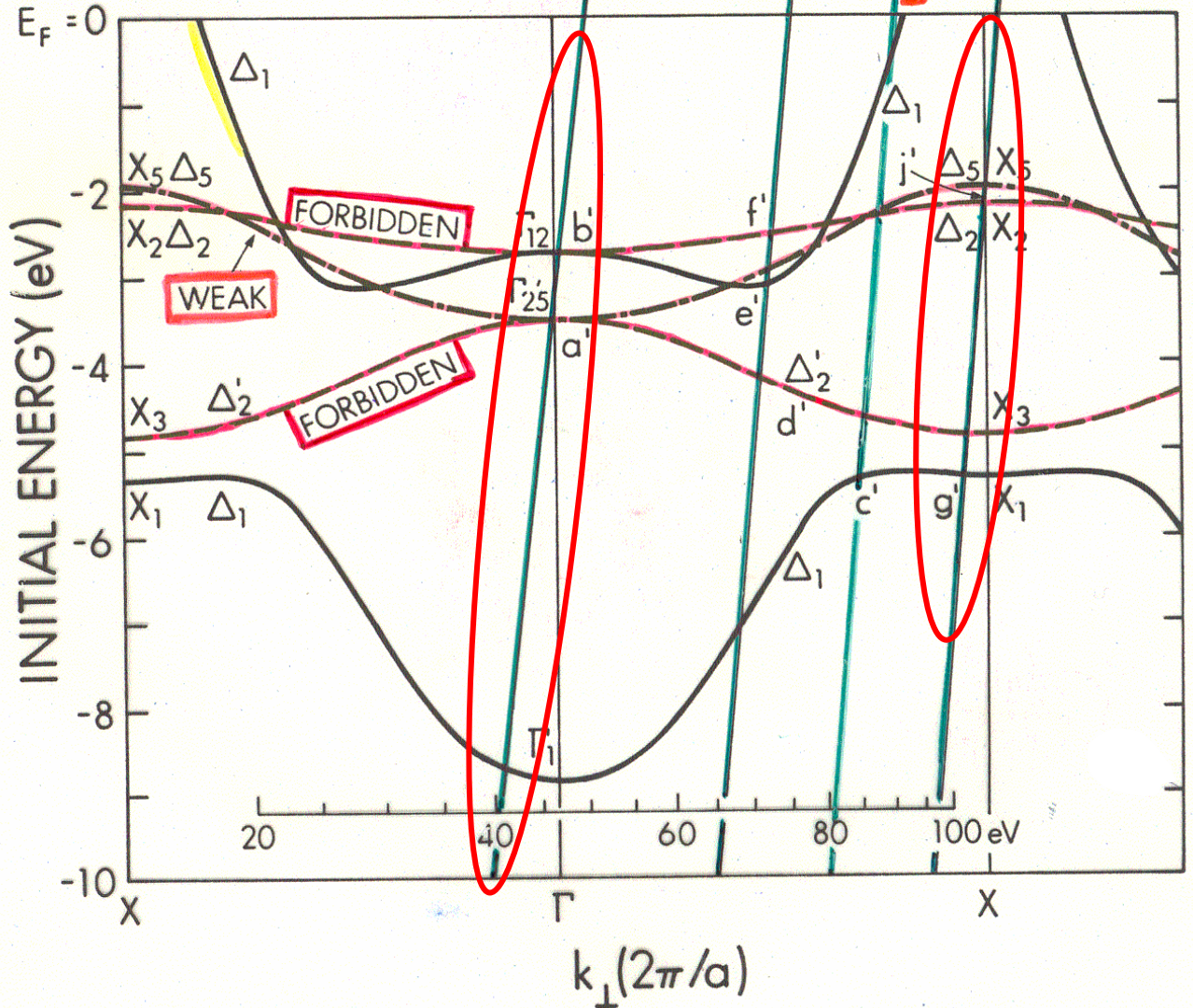
SIMPLE DT MODEL: Direct: $\vec{k}^f = \vec{k}^i + \vec{g} + \vec{k}_{hv}$
 $E^i(\vec{k}^i) =$ initial band structure
 $E^f(\vec{k}^f) \approx \hbar^2 (k^f)^2 / 2m$
 Constant matrix elements

COPPER:

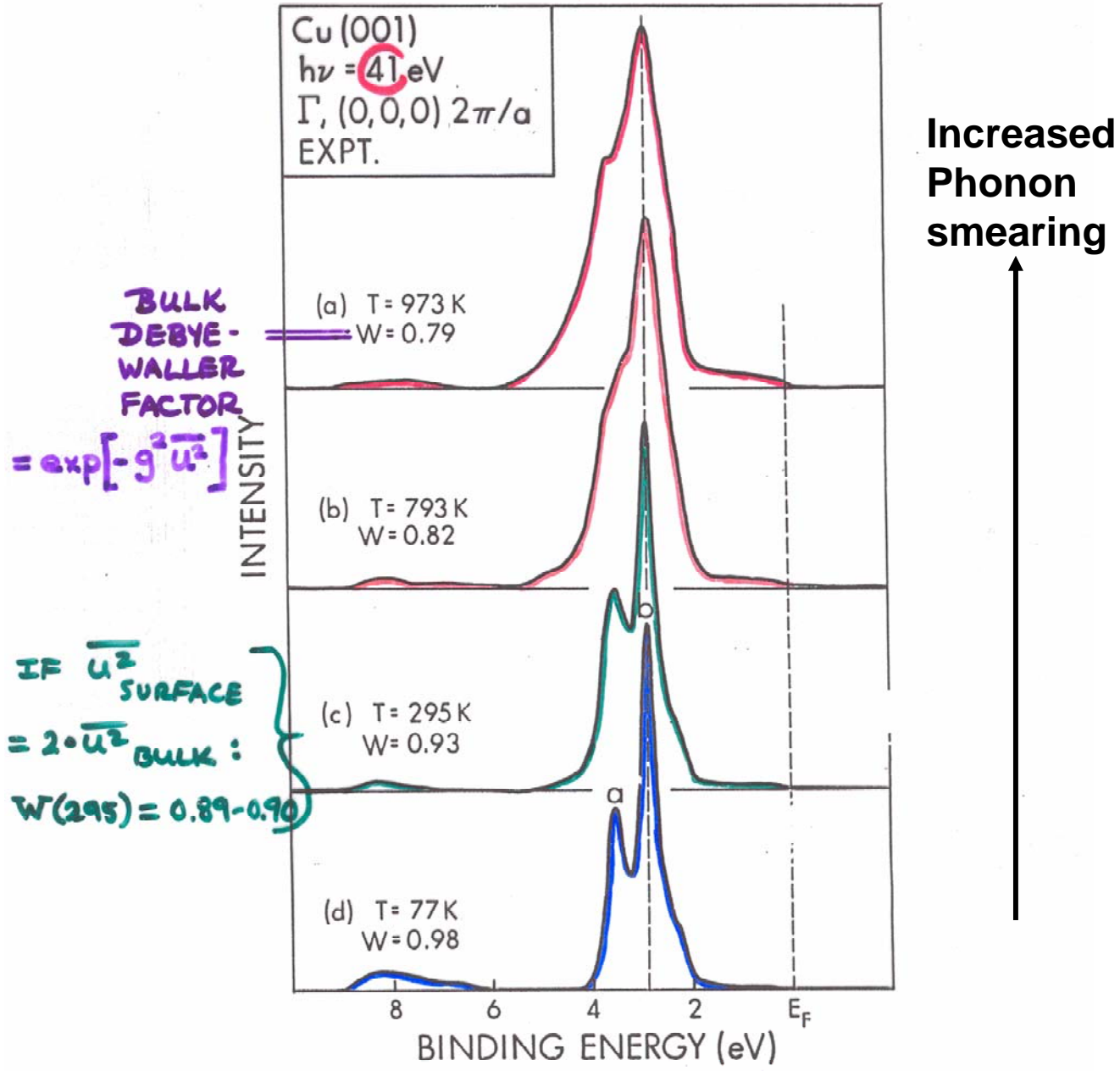
EMISSION ALONG (001)

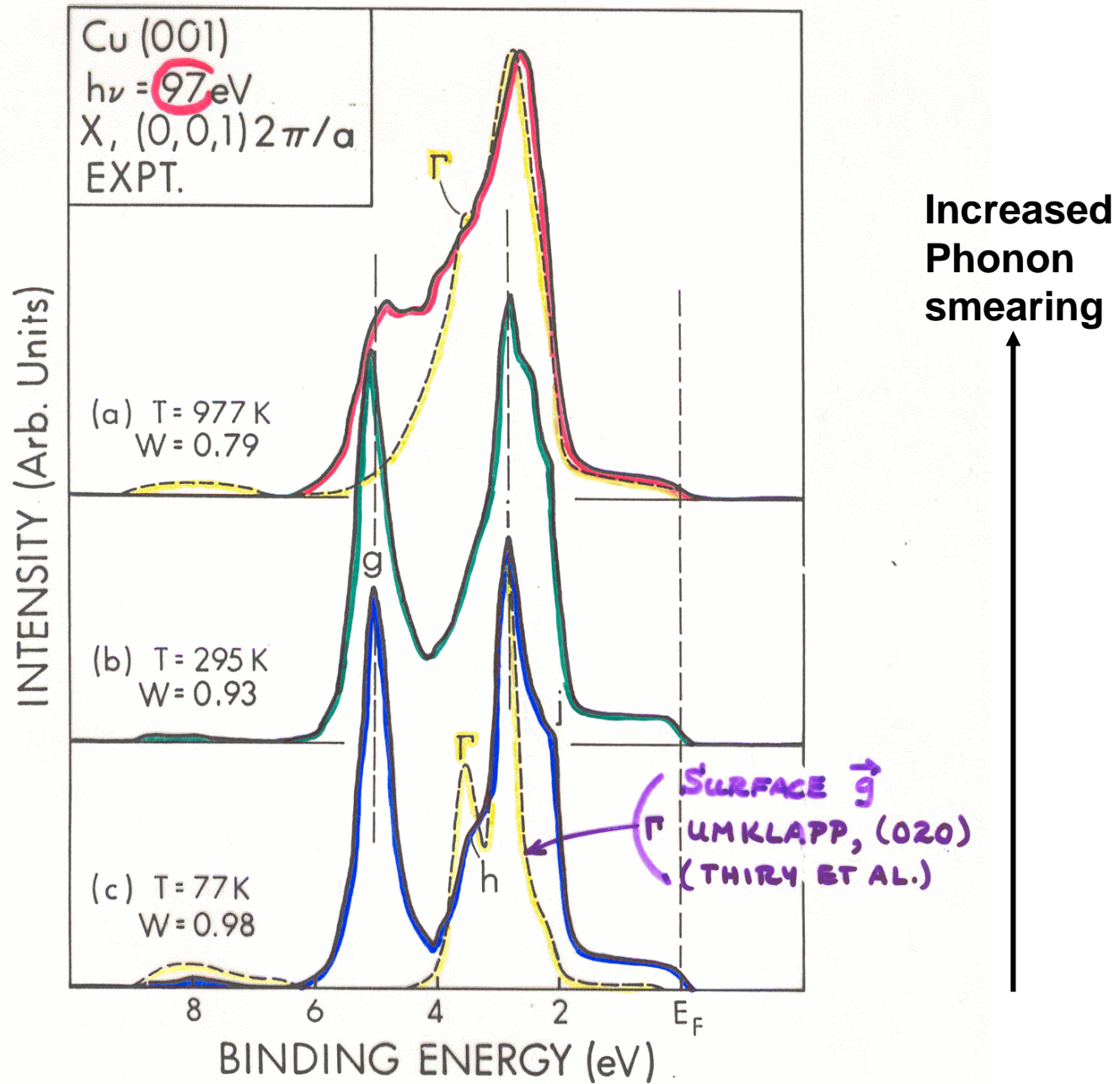
$h\nu = 41\text{eV}$ 66eV 81eV 97eV

20 40 60 80 100eV

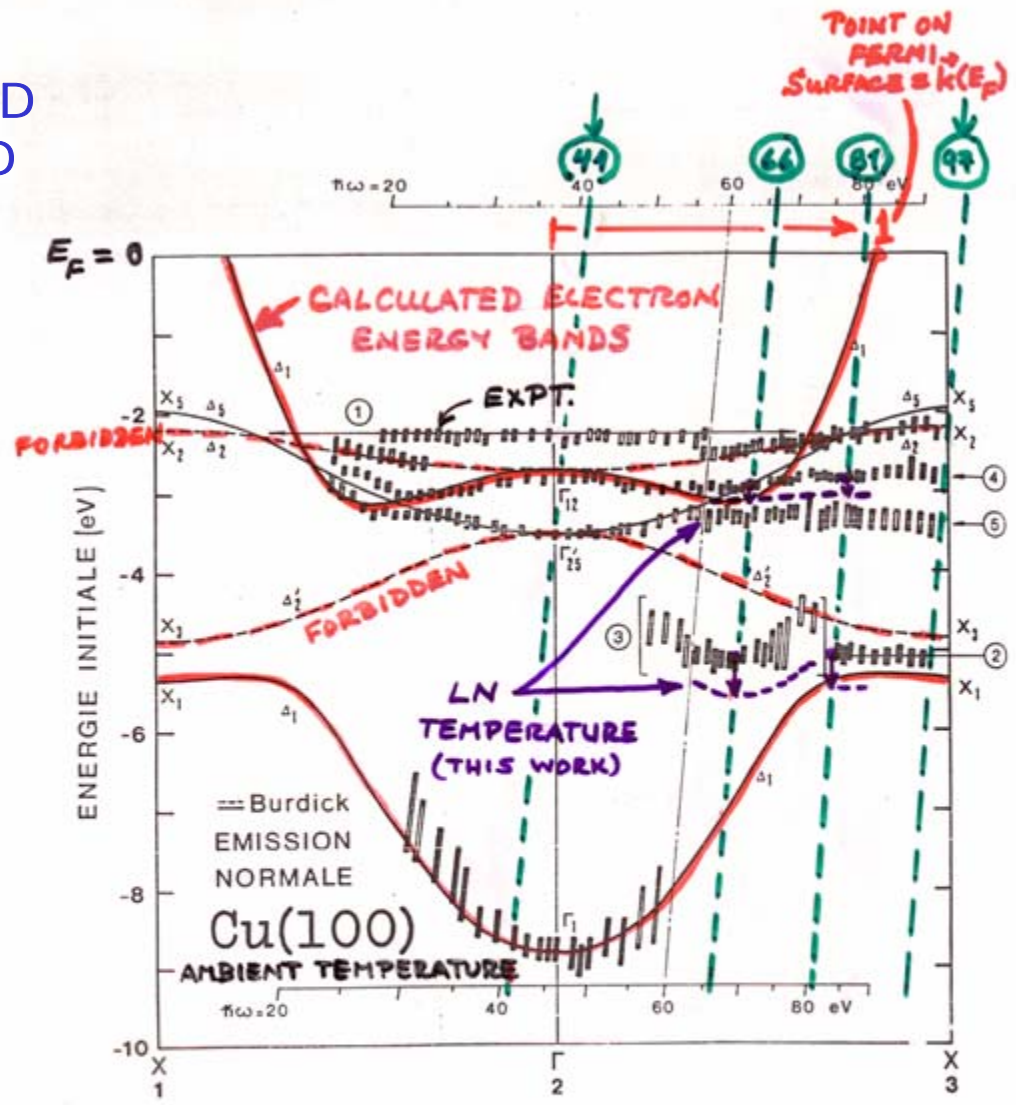


Expectations
from simple
direct-
transition
theory
+ symmetry
considerations
in matrix
elements





Cu: ANGLE-RESOLVED PHOTOEMISSION AND BAND-MAPPING ALONG (001)



$$k_{\perp}(2\pi/a)$$

P. THIRY, THESIS, UNIV. OF PARIS (1980)

+ WHITE ET AL.

P. R. 835,1147

(1987)

FIG.56

Cu: ANGLE-RESOLVED PHOTOEMISSION AND BAND-MAPPING ALONG (110)

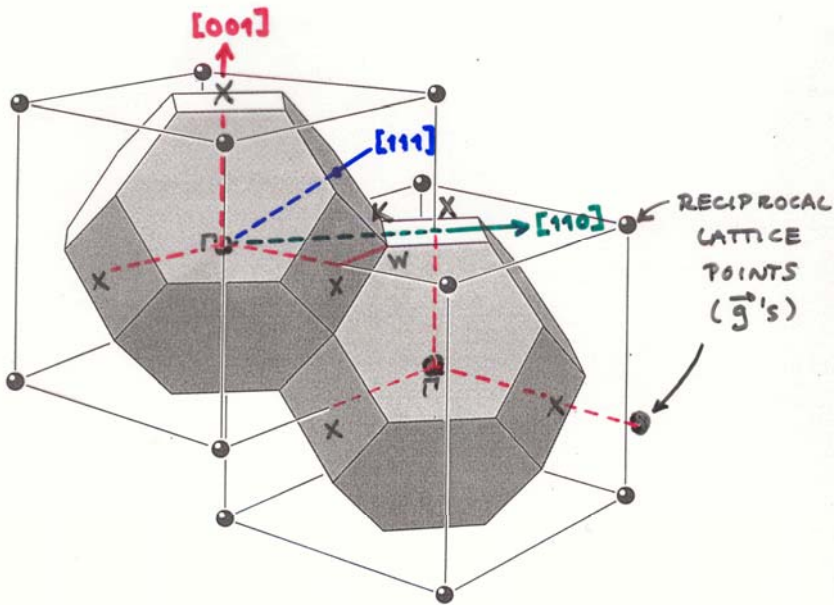
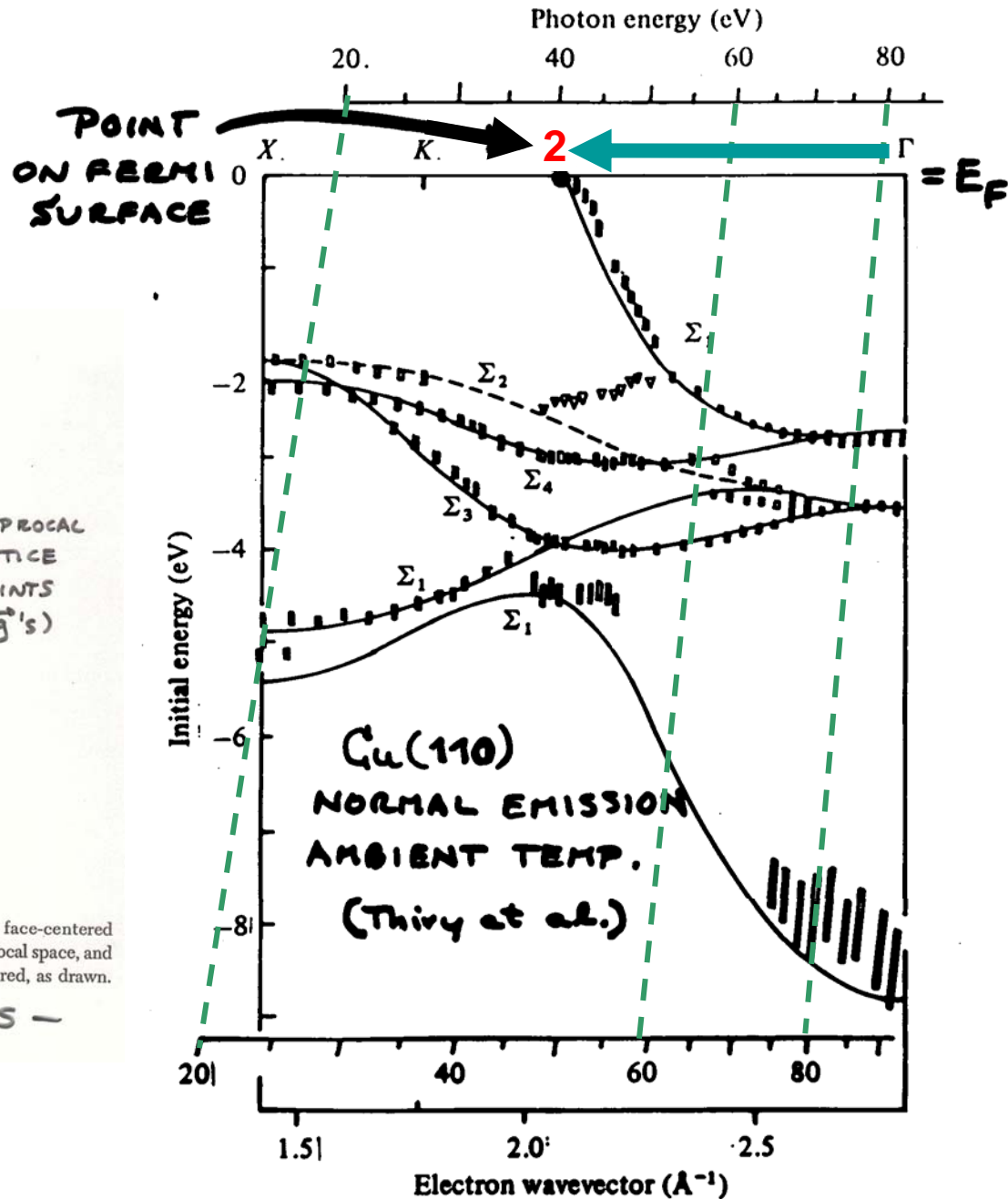


Figure 28 Brillouin zones of the face-centered cubic lattice. The cells are in reciprocal space, and the reciprocal lattice is body-centered, as drawn.

— STACKING OF fcc BRILLOUIN ZONES —

P.Thiry, Ph.D.
thesis, Univ.
of Paris (1980)



Fe (001)

SPIN-RESOLVED BAND STRUCTURE OF A FERROMAGNET

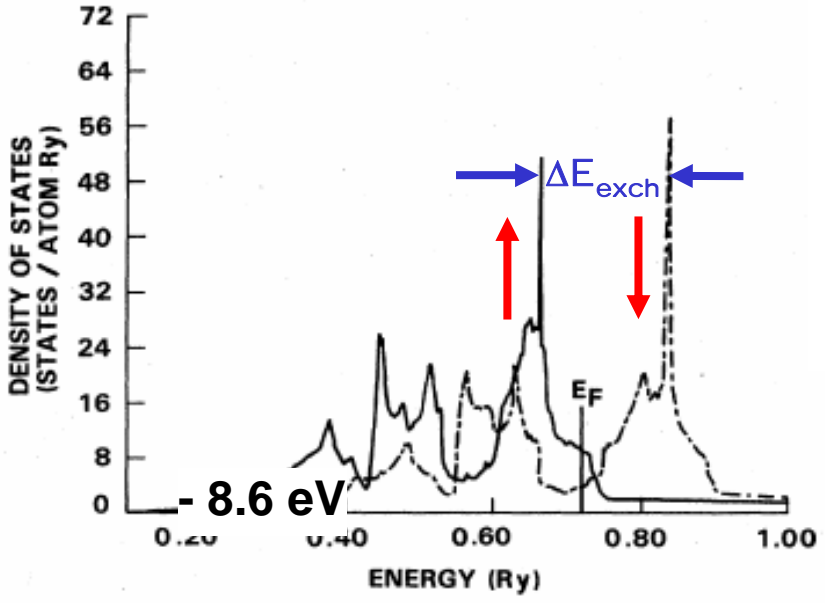
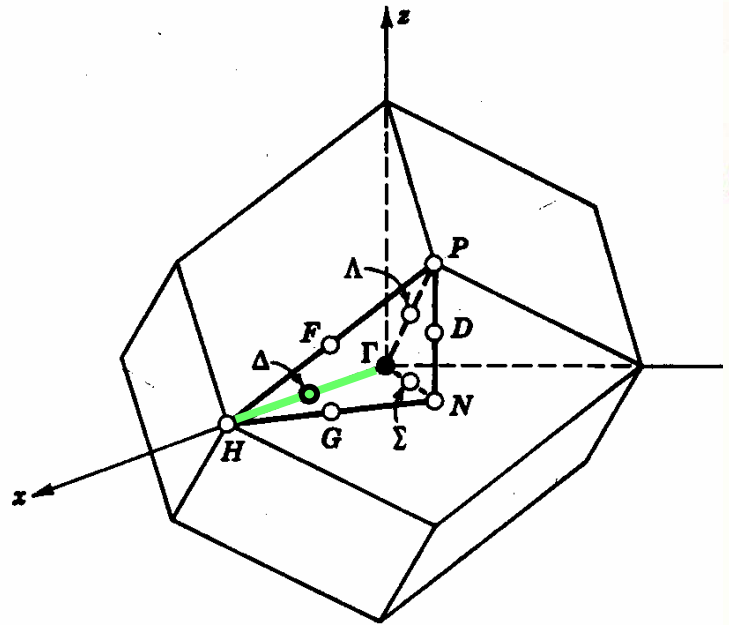
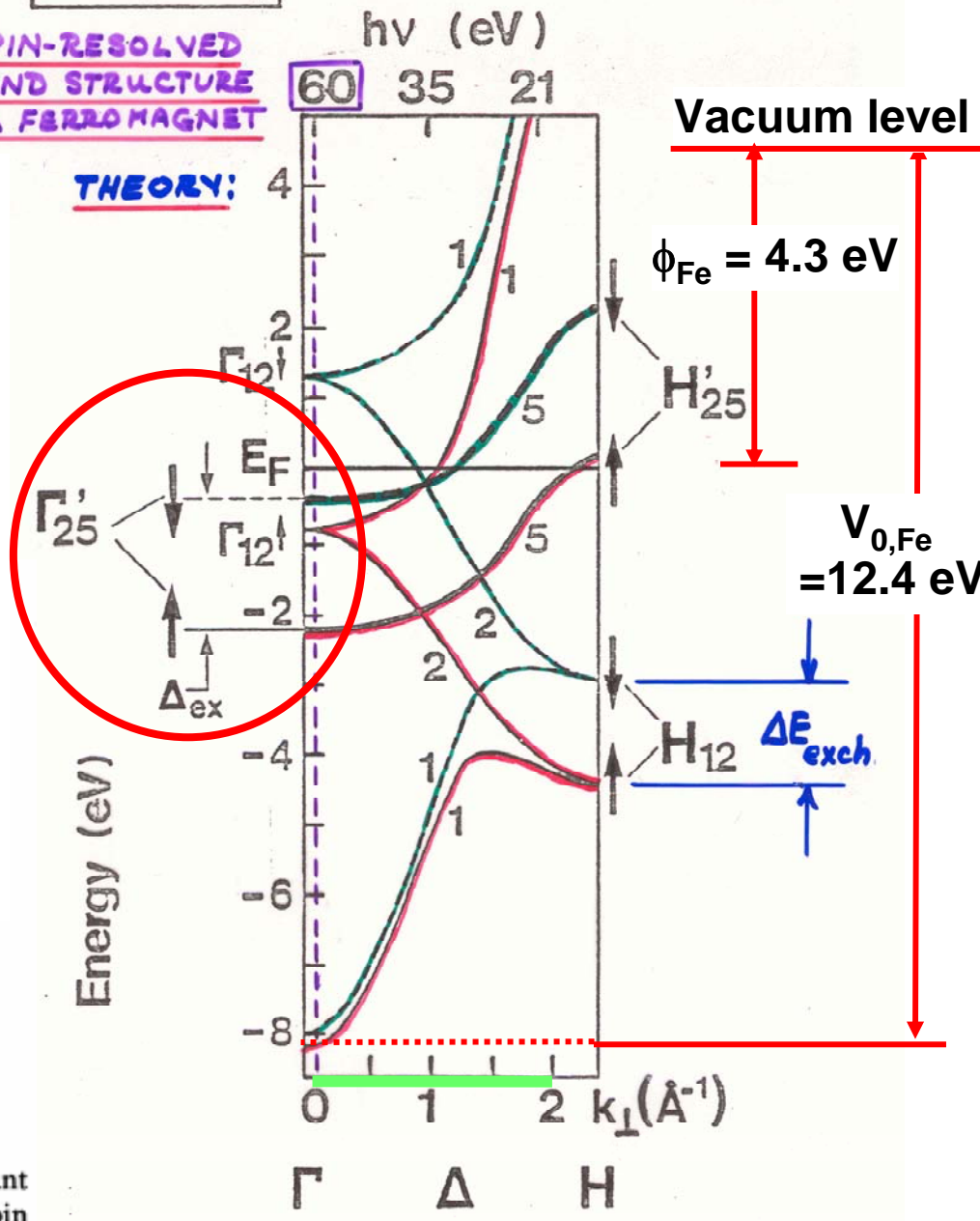


FIG. 4. Density of states at the equilibrium lattice constant of Fe for majority- (solid line) and minority- (broken line) spin states.

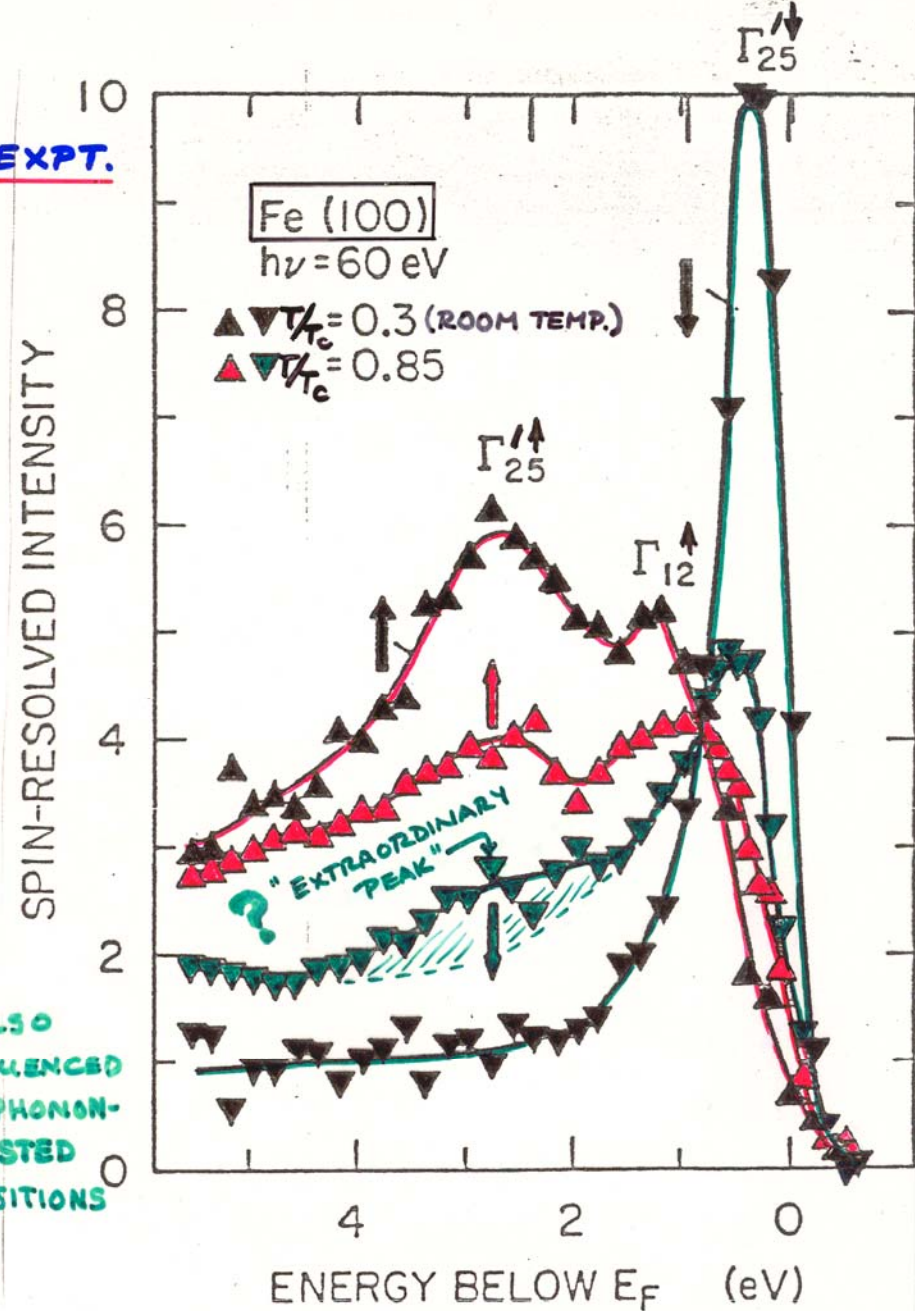
Hathaway et al., Phys. Rev. B 31, 7603 ('85)



E. KISKER ET AL., PHYS. REV. B
31, 329 (1985)

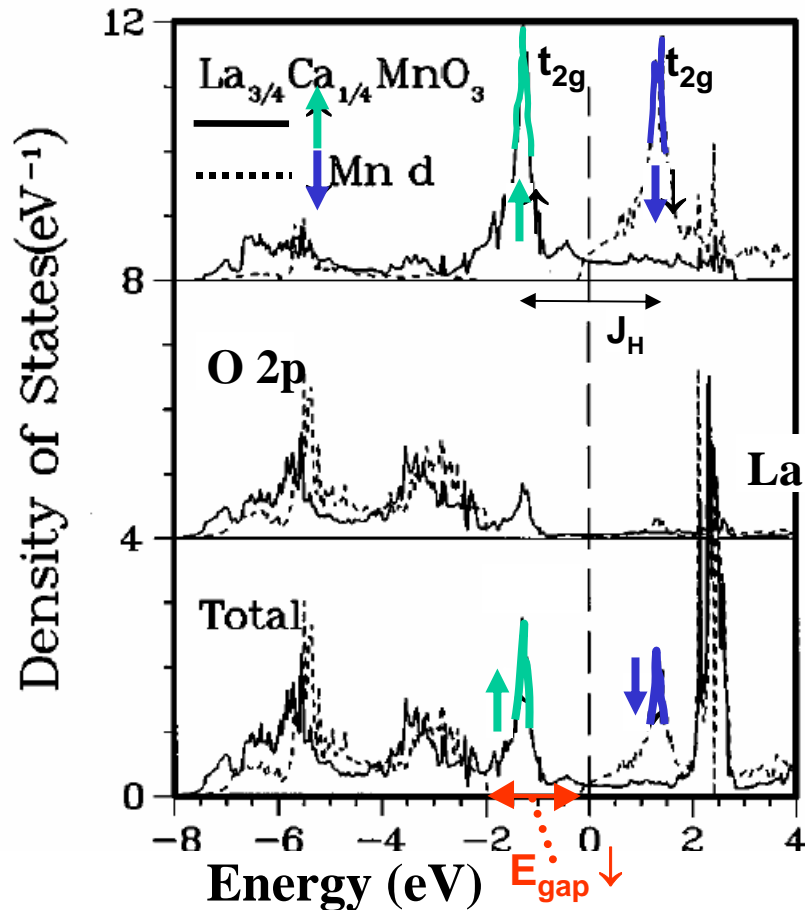
Fe: ANGLE AND SPIN-RESOLVED SPECTRA AT Γ POINT

EXPT.



Half-Metallic Ferromagnetism

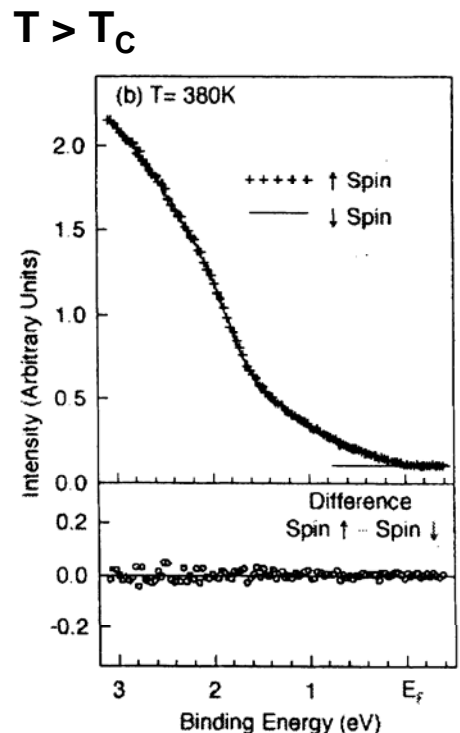
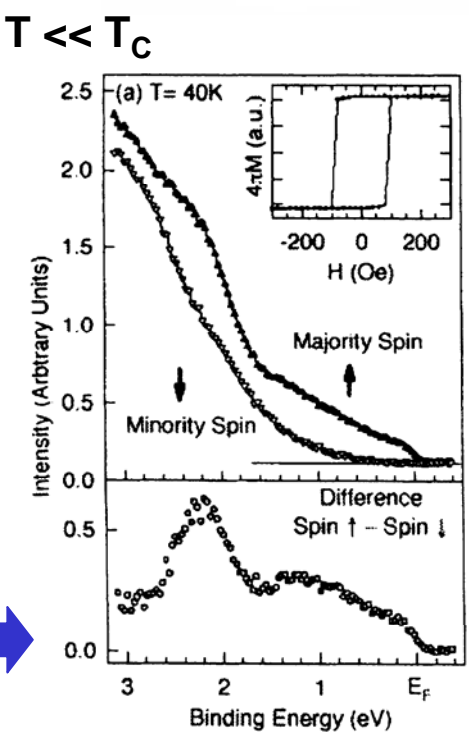
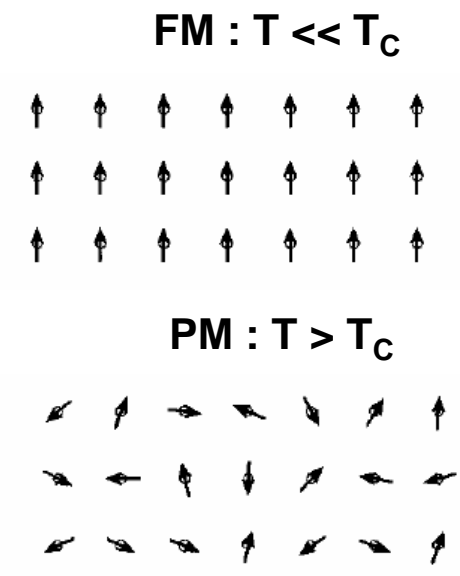
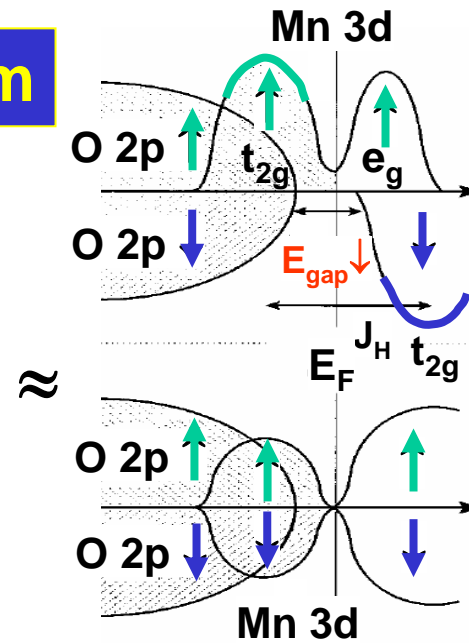
LDA theory- FM $\text{La}_{0.75}\text{Ca}_{0.25}\text{MnO}_3$



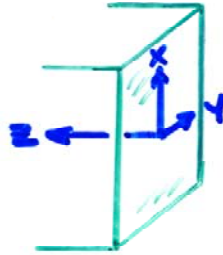
Pickett and Singh, PRB **53**, 1146 (1996)

Experiment- spin-resolved PS
 $\text{La}_{0.70}\text{Sr}_{0.30}\text{MnO}_3$ as thin film

Park et al., Nature, PRB **392**, 794 (1998)



SURFACE ELECTRONIC STATES



$$k_x, k_y \Rightarrow \vec{k}_{||}$$

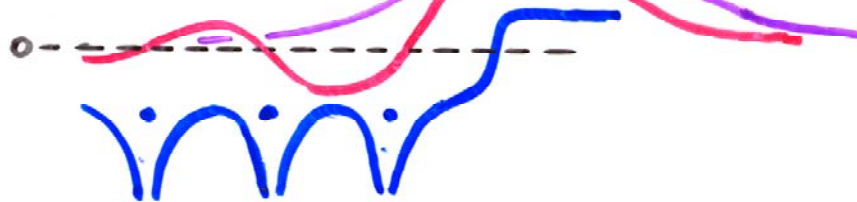
$$k_z \Rightarrow \vec{k}_{\perp}$$

- STRONGLY LOCALIZED NEAR SURFACE
- BLOCH FUNCTION IN $x+y$, BUT DECAYING IN z :

$$\psi_{\vec{k}_{||}}(\vec{r}) \approx u_{\vec{k}_{||}}(\vec{r}) e^{i\vec{k}_{||} \cdot \vec{r}} e^{-\kappa z}$$

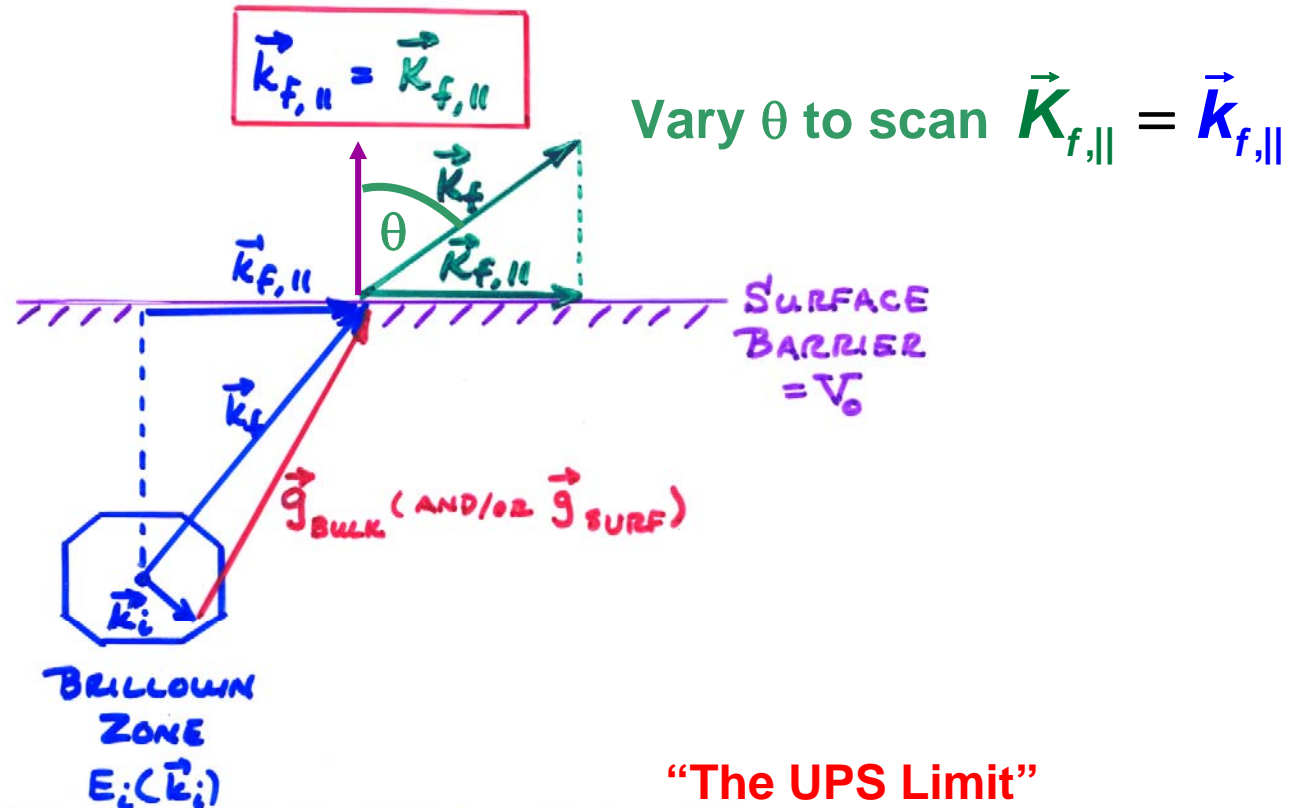
DECAY CONSTANT

- TWO LIMITING TYPES: TAMM STATE
- SHOCKLEY STATE (OSCILLATES INTO BULK A LITTLE)



- ONLY EXIST WHEN NO BULK STATE EXISTS AT SAME $\vec{k}_{||} = k_x \hat{i} + k_y \hat{j}$; OTHERWISE MIXING OCCURS & NOT SURFACE-LOCALIZED

CONSERVATION LAWS IN VALENCE-BAND PHOTOELECTRON SPECTROSCOPY:



$$\vec{k}_f = \vec{k}_i + \vec{g}_{\text{BULK}} (\vec{g}_{\text{SURFACE}}) + \cancel{\vec{k}_{\text{hv}}} + \cancel{\vec{k}_{\text{PHONON}}}$$

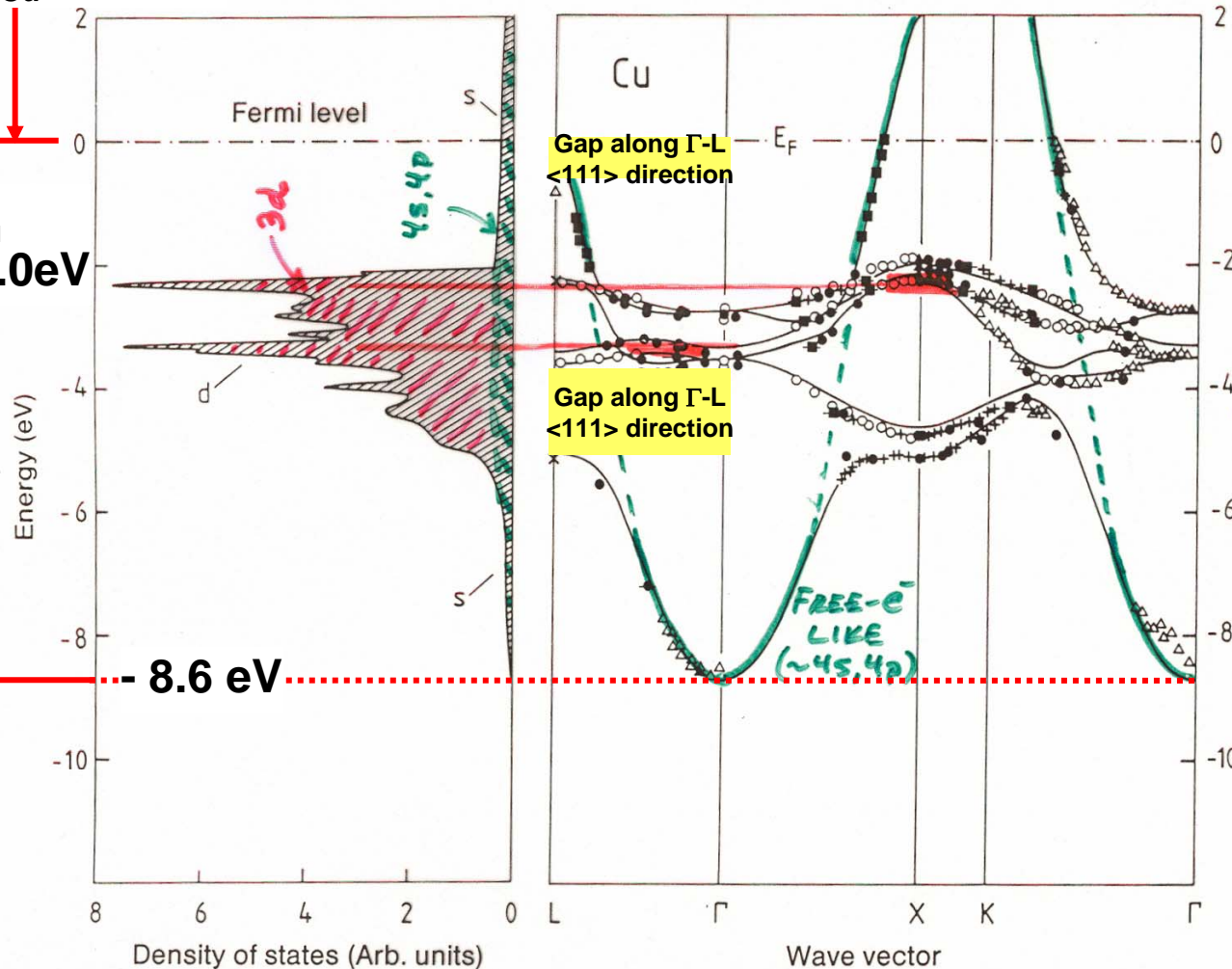
NEGLIGIBLE: $h\nu \lesssim 500$ eV IF $h\nu$ AND/OR T LOW ENOUGH

Vacuum level

The electronic structure of a transition metal—fcc Cu

$$\phi_{\text{Cu}} = 4.4 \text{ eV}$$

$$V_{0,\text{Cu}} = 13.0 \text{ eV}$$



Cu 1s²... 3d¹⁰ 4s¹
ELECTRONIC BANDS
+ DENSITY OF STATE!

MIXING
3d LIKE
MIXING

Experimental points from angle-resolved photoelectron spectroscopy

Fig. 7.12. Bandstructure $E(k)$ for copper along directions of high crystal symmetry (right). The experimental data were measured by various authors and were presented collectively by Courths and Hüfner [7.4]. The full lines showing the calculated energy bands and the density of states (left) are from [7.5]. The experimental data agree very well, not only among themselves, but also with the calculation

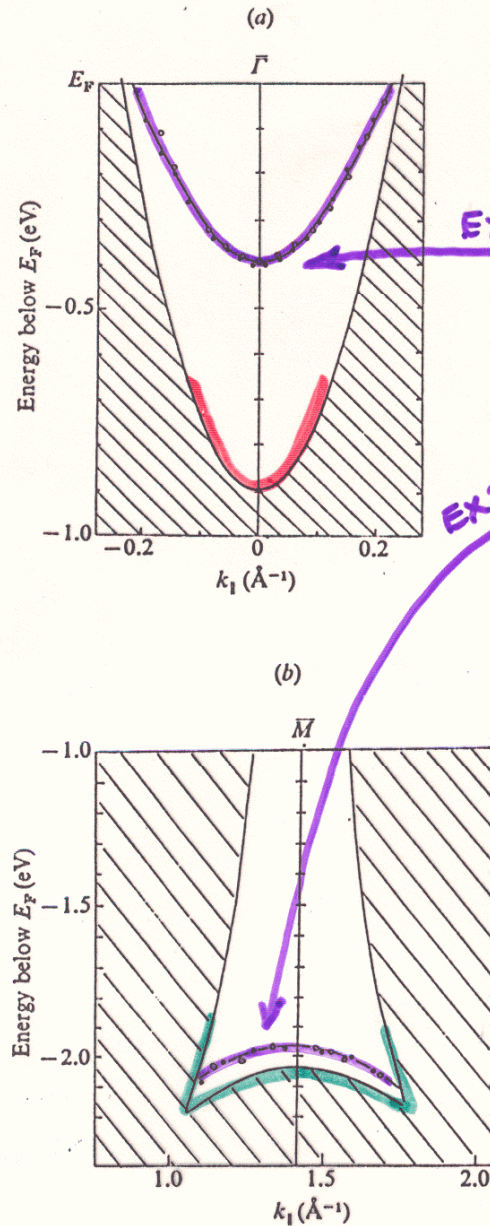
Surface states on Cu(111)

Fig. 4.21. Experimental dispersion of Cu(111) surface states plotted with a projection of the bulk bands: (a) Shockley state near the zone center (Γ Kevan, 1983); (b) Tamm state near the zone boundary (\bar{M} Heimann, Hermanson, Miosga and Neddermeyer, 1979). Compare with Fig. 4.17.

Shockley surface state

Tamm surface state

Zangwill, Surface Physics,



THEORY

Fig. 4.17. Surface states (dashed curves) and bulk projected bands of Cu(111) surface according to a six-layer surface band structure calculation (Euceda, Bylander & Kleinman, 1983).

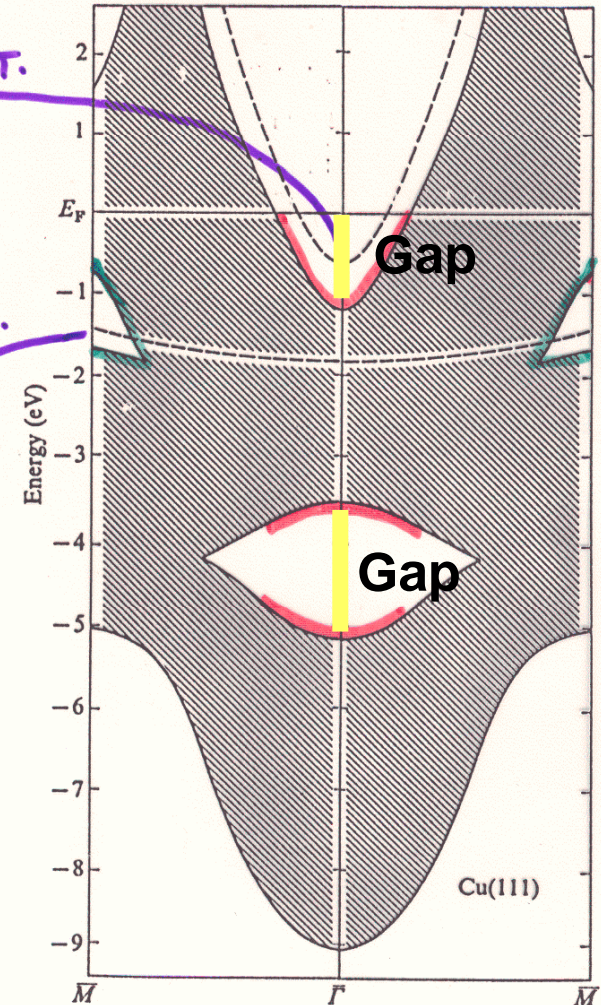
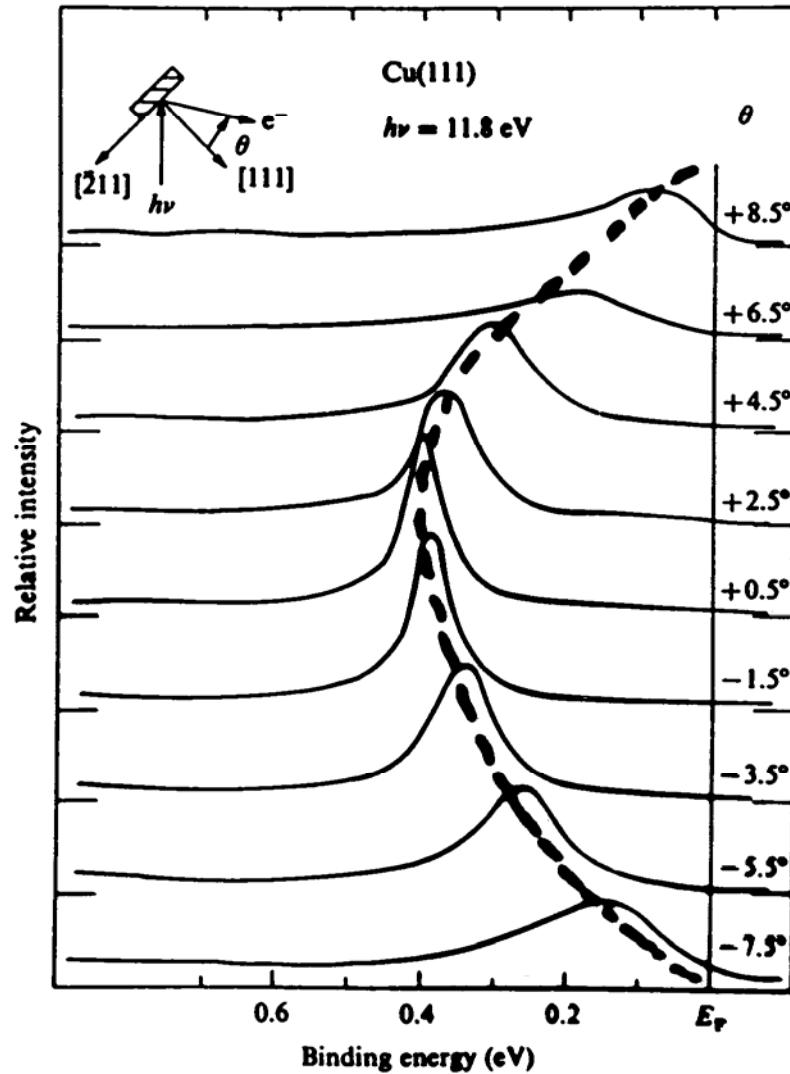
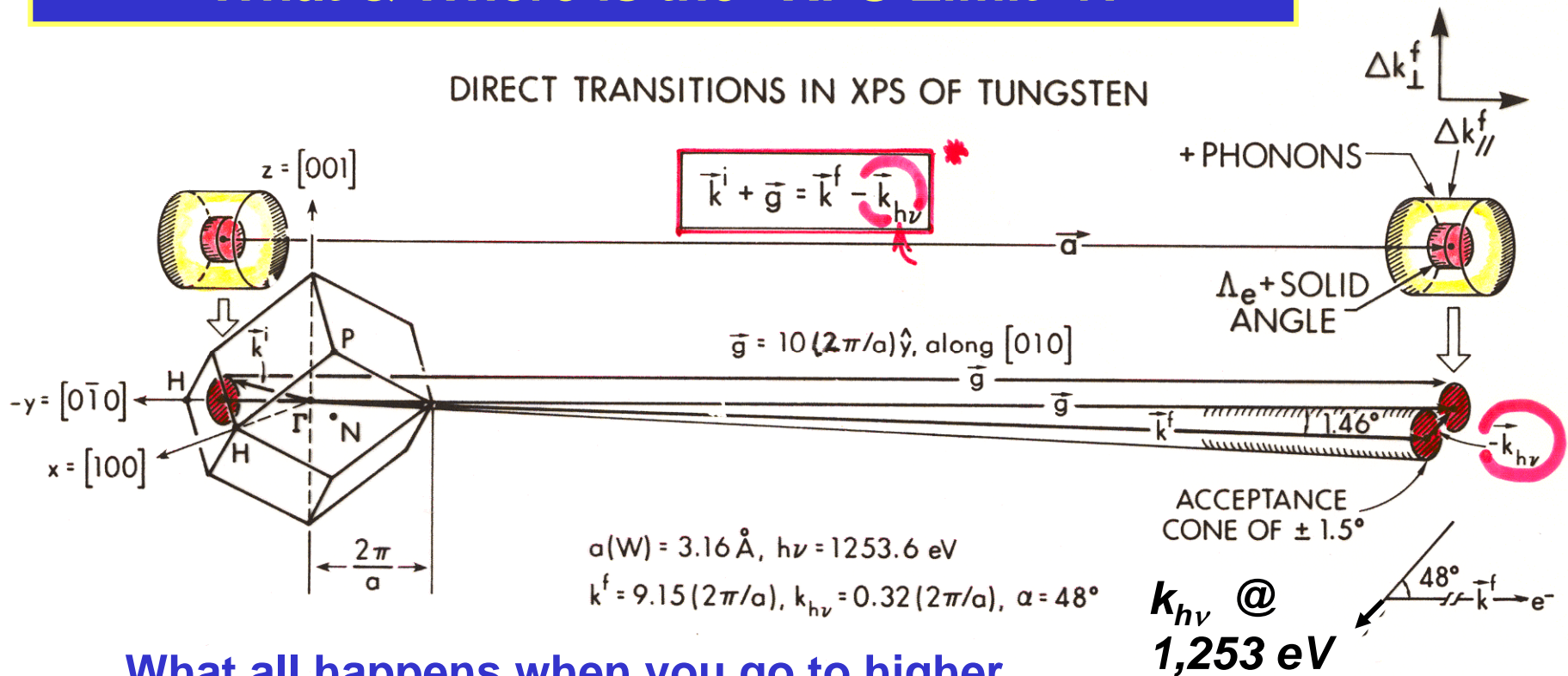


Fig. 4.20. Photoemission energy distribution curves from Cu(111) at different collection angles. Equation (4.32) has been used to express the electron kinetic energy in terms of the binding energy of the electron state (Kevan, 1983).



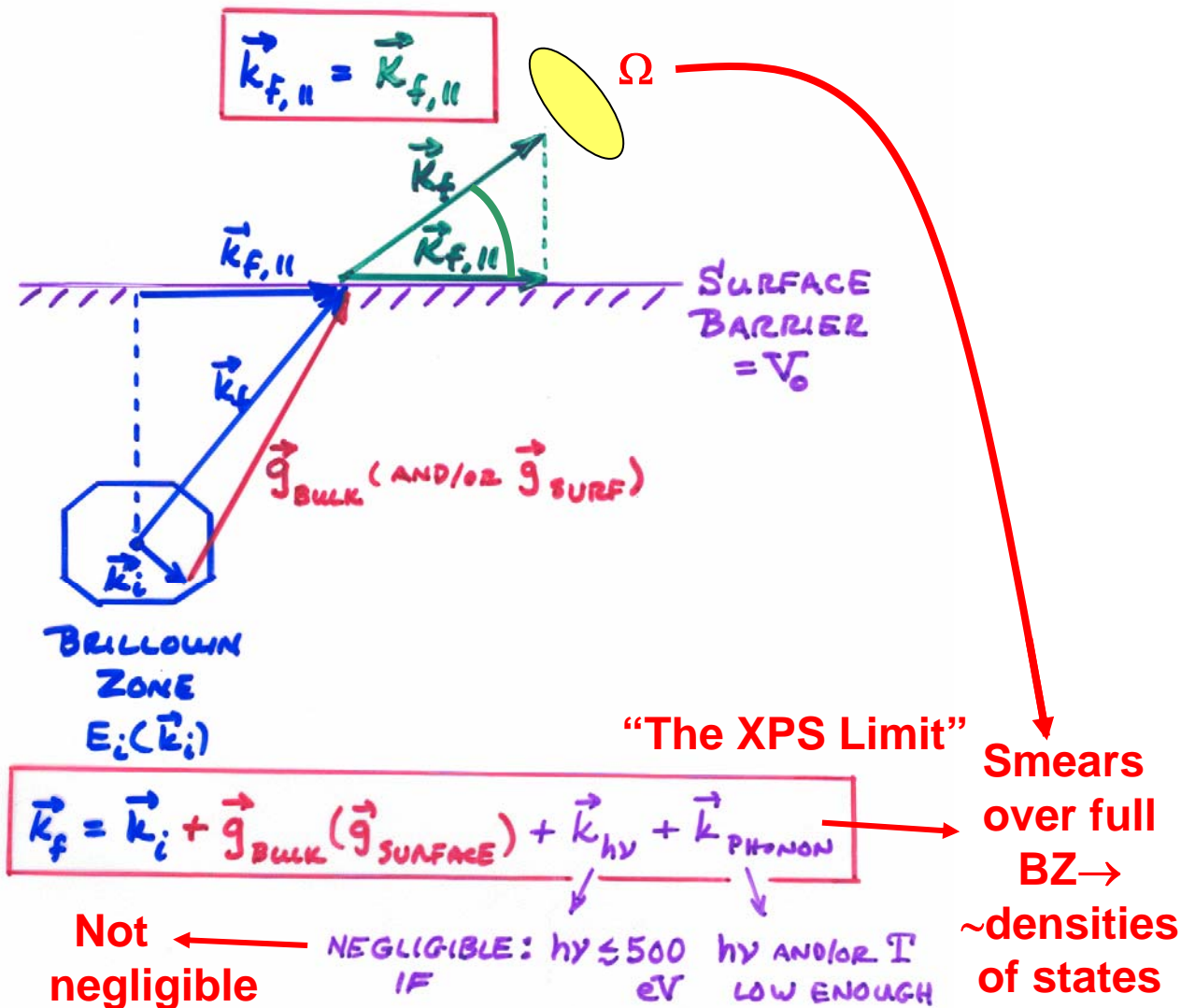
Valence-Band Photoemission at High Energy-- What & Where is the “XPS Limit”?:



What all happens when you go to higher photon energies?

- non-dipole effect → the photon momentum
 - angular acceptance → B.Z. averaging
 - lattice recoil, phonon creation → more Brillouin Zone averaging
- The XPS limit of full B.Z. averaging and D.O.S. sensitivity

CONSERVATION LAWS IN VALENCE-BAND PHOTOELECTRON SPECTROSCOPY:



$h\nu = 1487 \text{ eV}$

Estimating phonon effects: 1st approx.

TABLE I. Tabulation of thermal displacements ($\langle U^2 \rangle$) and Debye-Waller factors [$W(T) = \exp(-\frac{1}{3} \langle U^2 \rangle g^2)$] in the XPS regime ($E_{kin} = 1482 \text{ eV}$) for various elements. The Debye temperatures are taken from Ref. 30. The solid line divides the Debye-Waller factors so as to indicate when $\geq \frac{1}{2}$ of the transitions will be direct. Elements are in order of Z .

Element	Θ_D (K)	A (amu)	T=4 K		T=77 K		T=300 K		T=1000 K	
			$\langle U^2 \rangle$ (10^{-18} cm^2)	W	$\langle U^2 \rangle$ (10^{-18} cm^2)	W	$\langle U^2 \rangle$ (10^{-18} cm^2)	W	$\langle U^2 \rangle$ (10^{-18} cm^2)	W
Be	1440	9.012	0.84	0.34	0.86	0.33	1.07	0.25	2.47	0.04
C	2230	12.001	0.41	0.58	0.41	0.58	0.46	0.55	0.83	0.34
Mg	400	24.312	1.12	0.23	1.40	0.16	3.53	0.01		
Al	428	26.981	0.95	0.29	1.15	0.22	2.79	0.03		
Si	645	28.086	0.60	0.46	0.66	0.42	1.26	0.19	3.07	0.02
Ca	230	40.08	1.19	0.21	1.94	0.08	6.24	0.0		
Ti	420	47.9	0.54	0.49	0.66	0.42	1.63	0.12	5.16	0.0
V	380	50.942	0.56	0.48	0.72	0.39	1.85	0.09	5.93	0.0
Cr	630	51.996	0.33	0.63	0.37	0.63	0.71	0.40	2.15	0.06
Mn	410	54.938	0.48	0.58	0.60	0.46	1.49	0.14	4.72	0.0
Fe	470	55.847	0.42	0.58	0.43	0.58	1.13	0.23	3.58	0.01
Co	445	58.933	0.42	0.58	0.50	0.53	1.19	0.21	3.74	0.0
Ni	450	58.71	0.41	0.58	0.49	0.53	1.17	0.22	3.67	0.01
Cu	343	63.54	0.30	0.58	0.67	0.42	1.82	0.09	5.84	0.0
Zn	327	65.37	0.31	0.51	0.70	0.40	1.92	0.08		
Ge	374	72.59	0.40	0.58	0.51	0.51	1.34	0.17	4.28	0.0
As	282	74.922	0.32	0.51	0.77	0.37	2.25	0.05	7.33	0.0
Zr	291	91.22	0.41	0.58	0.60	0.46	1.74	0.10	5.65	0.0
Nb	275	92.906	0.43	0.57	0.65	0.43	1.90	0.08	6.21	0.0
Mo	450	95.94	0.25	0.72	0.30	0.68	0.71	0.39	2.25	0.05
Ru	600	101.07	0.18	0.78	0.30	0.77	0.40	0.60	1.21	0.21
Rh	480	102.905	0.32	0.75	0.36	0.71	0.59	0.46	1.84	0.09
Pd	274	106.4	0.37	0.61	0.57	0.48	1.68	0.11	5.46	0.0
Ag	225	107.87	0.45	0.58	0.75	0.38	2.44	0.04	8.00	0.0
Cd	209	112.40	0.47	0.55	0.81	0.35	2.70	0.03		
Sn	200	118.69	0.48	0.55	0.83	0.34	2.55	0.04		
Sb	211	121.75	0.43	0.57	0.79	0.35	2.46	0.04		
Hf	252	178.49	0.24	0.72	0.38	0.60	1.18	0.22	3.85	0.01
Ta	240	180.948	0.25	0.72	0.42	0.58	1.28	0.19	4.19	0.0
W	400	183.85	0.15	0.82	0.18	0.79	0.47	0.55	1.48	0.14
Re	430	186.2	0.15	0.82	0.17	0.81	0.40	0.58	1.23	0.19
Os	500	190.2	0.11	0.86	0.13	0.94	0.30	0.68	0.92	0.30
Ir	420	192.2	0.14	0.84	0.17	0.81	0.41	0.58	1.29	0.19
Pt	240	195.09	0.23	0.74	0.30	0.60	1.19	0.21	3.88	0.01
Au	165	196.967	0.24	0.65	0.82	0.35	2.46	0.04	8.14	0.0
Pb	105	207.19	0.51	0.52	1.54	0.13	5.75	0.0		

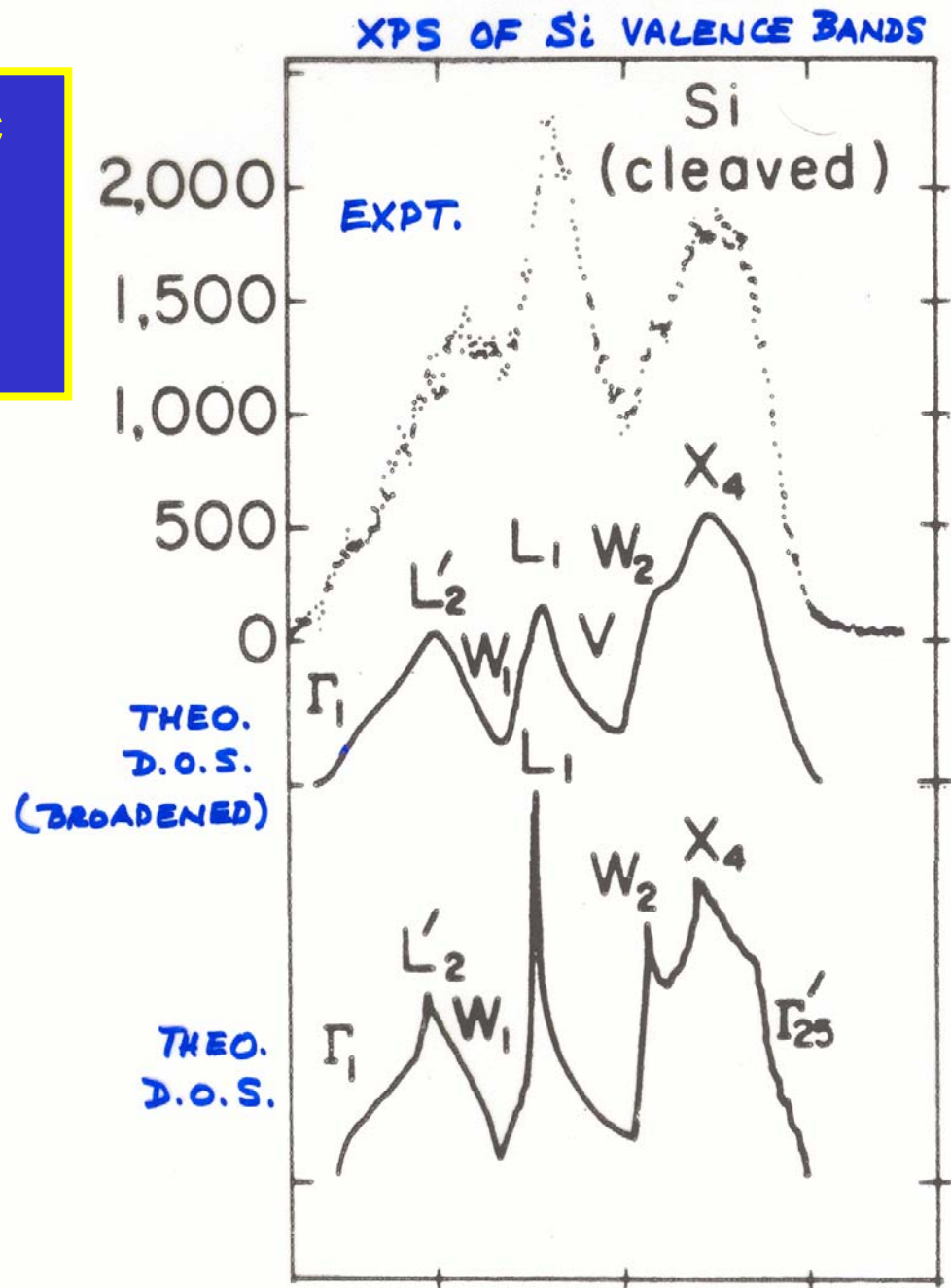
Greater than 50% direct transitions

$$W(T) = \exp\left(-\frac{1}{3} g^2 \langle U^2(T) \rangle\right)$$

$$I(E, T) = W(T)I_{DT} + [1 - W(T)]I_{NDT}$$

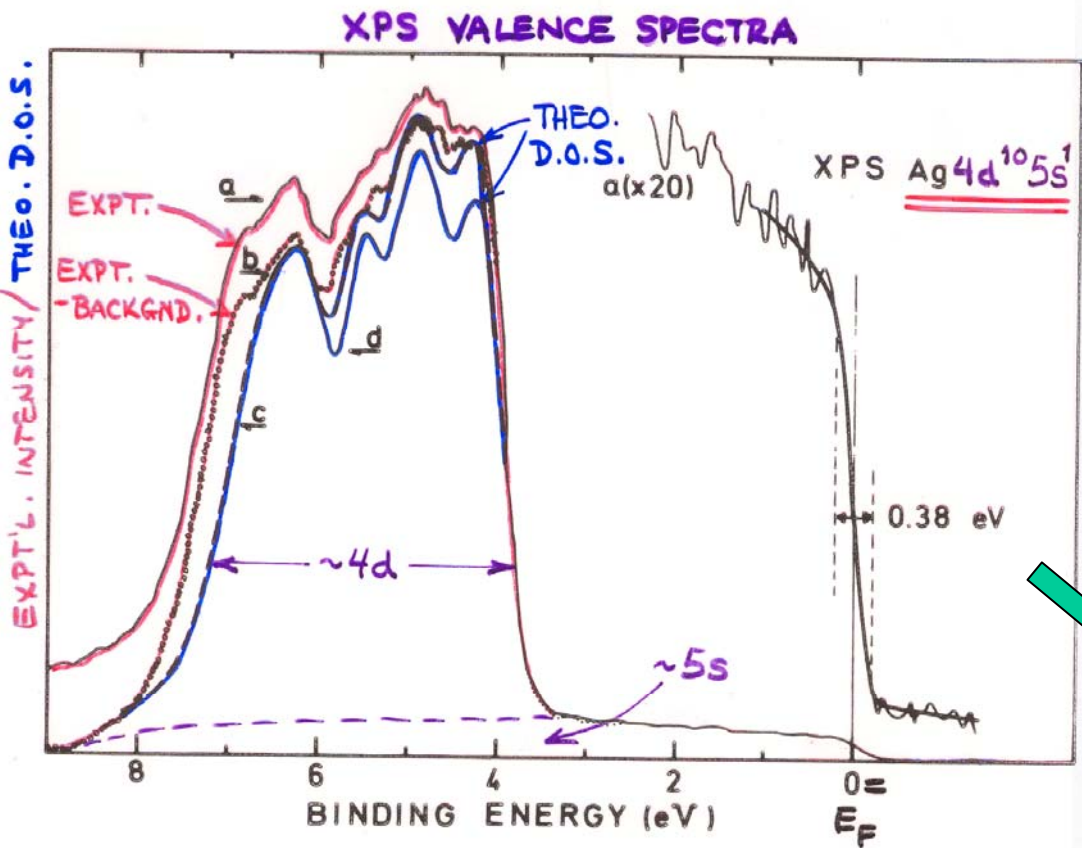
Shevchik, Phys. Rev. B 20, 3020 ('79);
 Hussain et al., Phys. Rev. 22, 3750 ('80)

Some classic cases in the XPS limit:



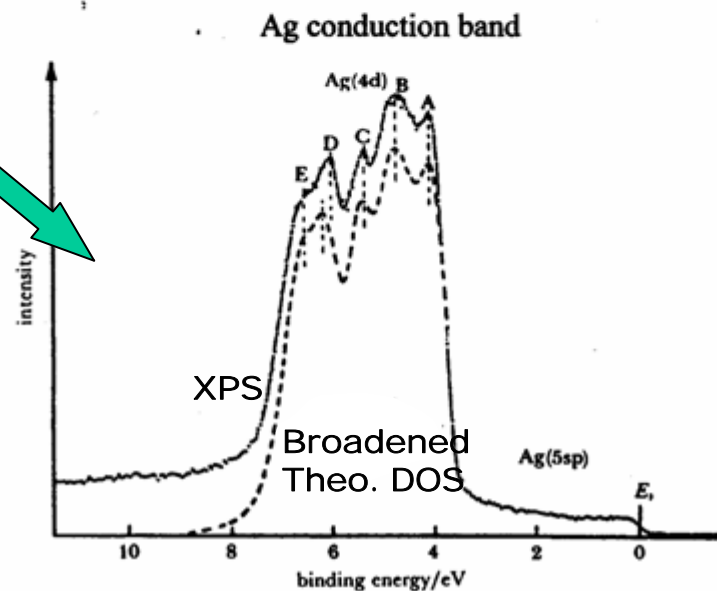
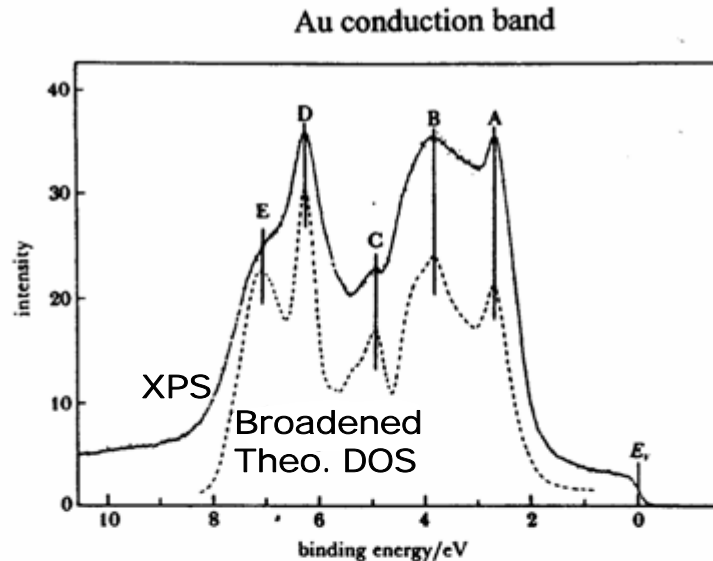
“Basic Concepts of XPS”
Figure 14

Densities of states From XPS spectra

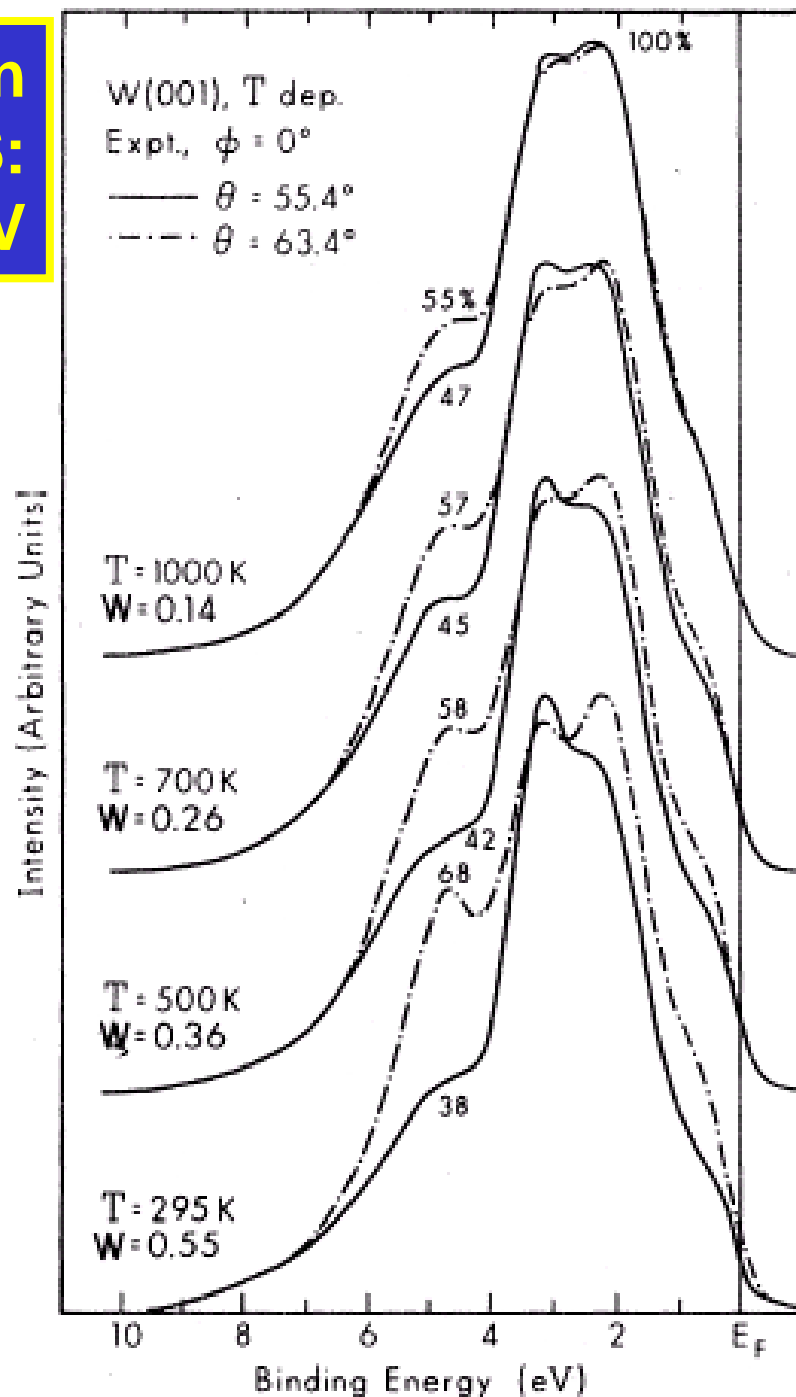


• COMPLETE B.Z. AVERAGE
DUE TO PHONON-ASSISTED
NON-DIRECT TRANSITIONS
⇒ "XPS LIMIT"

"Basic Concepts of XPS"
Figure 13



**Direct-transition
effects in XPS:
W(110) at 1253.6 eV**

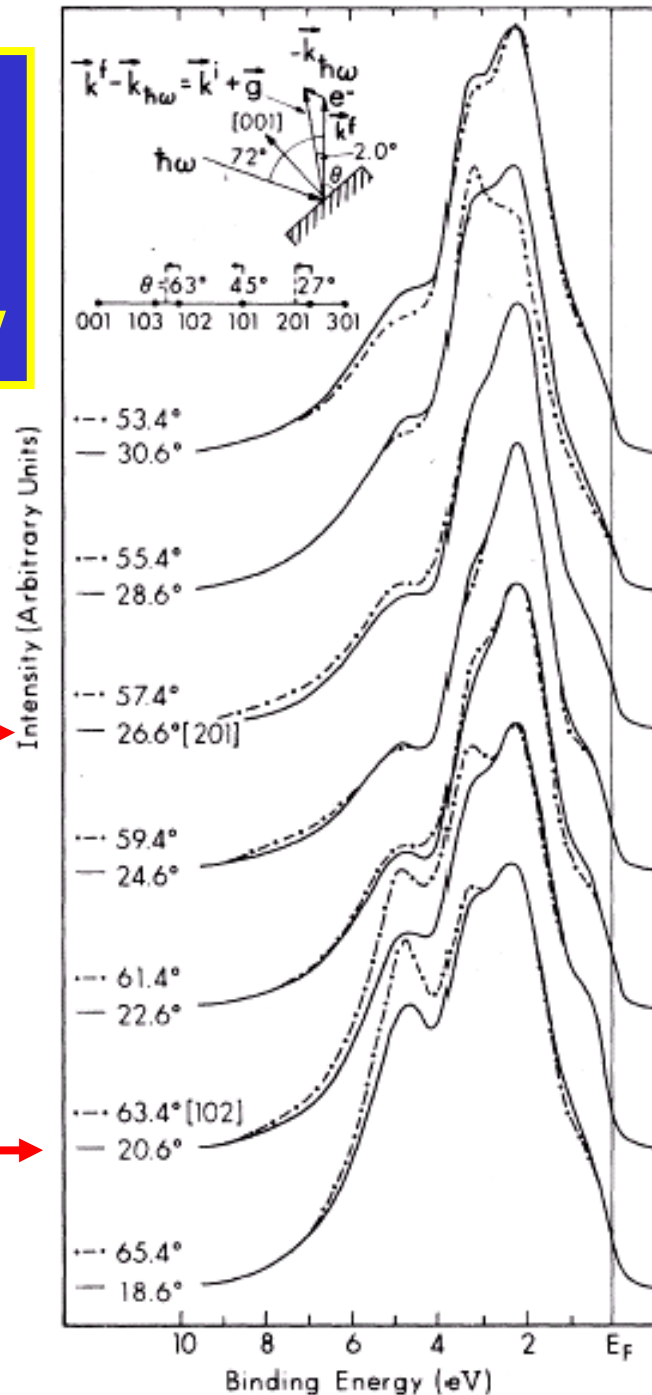


Present if
vibrations stiff
enough (Debye
T high enough),
but suppressed
as temperature is
raised.

Hussain et al.,
Phys. Rev. 22,
3750 (1980)

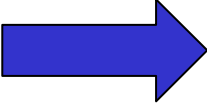
Effect of photon momentum on k conservation: W(110) at 1253.6 eV

Symmetry-related spectra shifted by 6.0° for best match. Theoretical 4.8° due to k_{hv}



Hussain et al.,
Phys. Rev. 22,
3750 (1980)

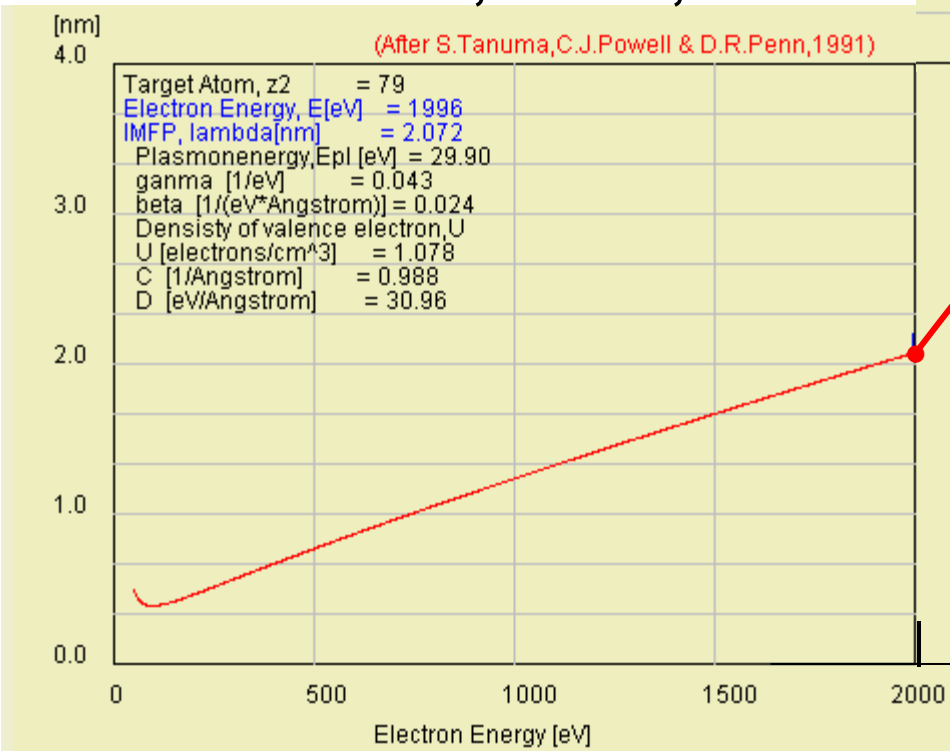
Outline

- 
- Valence-band spectra: low-energy UPS limit and high-energy XPS limit: **Taking the excitation energy up to 5-15 keV**
 - Core-level chemical shifts: the potential model
 - Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
 - Multiplet splittings
 - Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
 - Magnetic circular dichroism (MCD) in core-level emission
 - Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
 - Various other final state effects providing information in core-level spectra

How much deeper do we probe at 10 keV?

Au

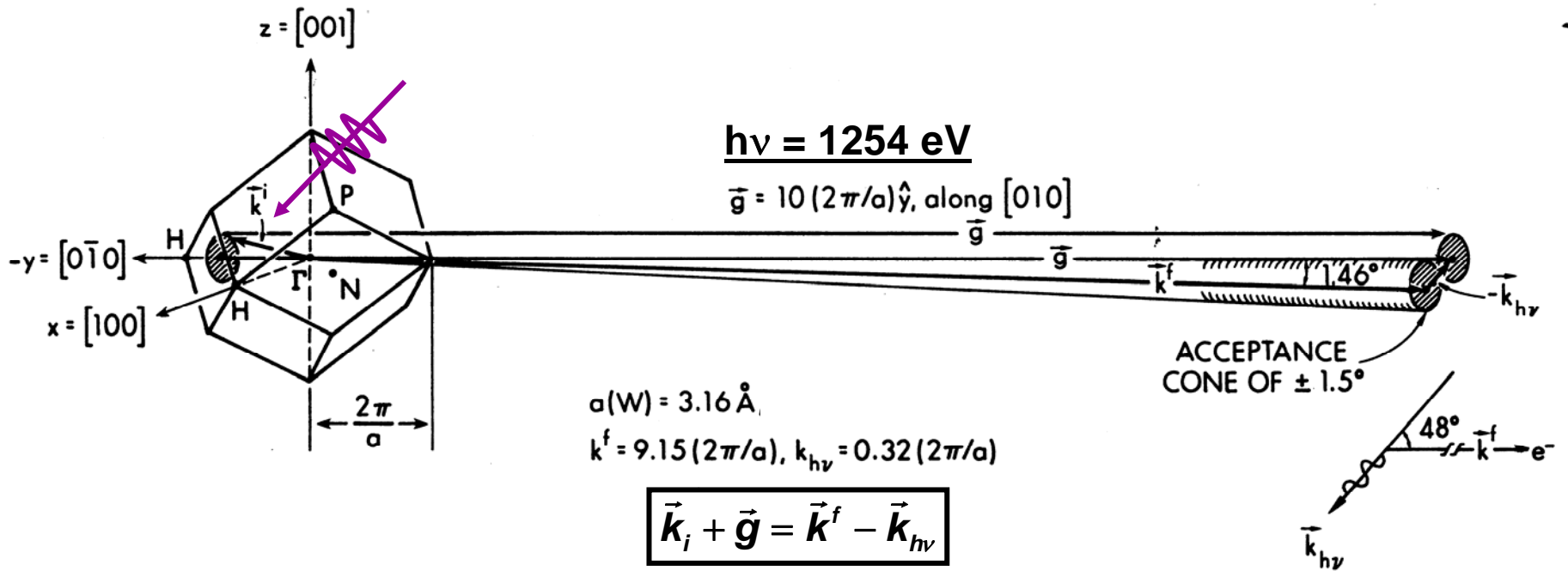
**Inelastic attenuation length
TPP-2M formula
of Tanuma, Powell, Penn**



$\propto (E_{kin})^{0.75}$

**4-5x deeper
than normal
XPS**

**15-20x deeper
than normal
ARPES**



$h\nu = 1254 \text{ eV}$

$\vec{g} = 10(2\pi/a)\hat{y}$, along $[010]$

$a(W) = 3.16 \text{ \AA}$

$k^f = 9.15(2\pi/a)$, $k_{hv} = 0.32(2\pi/a)$

$\vec{k}_i + \vec{g} = \vec{k}^f - \vec{k}_{hv}$

$h\nu = 10,000 \text{ eV}$

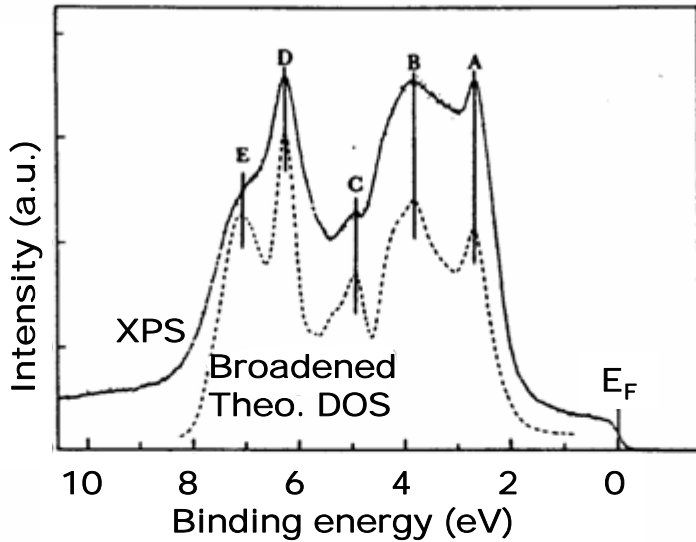
$\vec{g} = 26(2\pi/a)\hat{y}$

$k^f = 25.80(2\pi/a)$, $k_{hv} = 2.54(2\pi/a)$

ACCEPTANCE CONE OF $\pm 0.5^\circ$

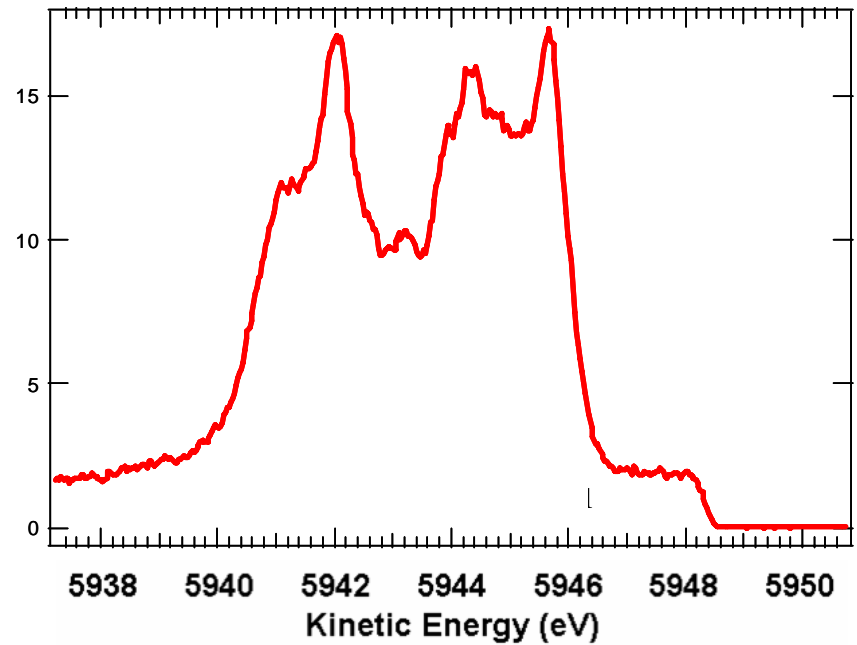
But angular resolutions of 0.01° with an acceptance $\pm 2^\circ$ may be possible!
B. Wannberg

Gold Valence Spectrum



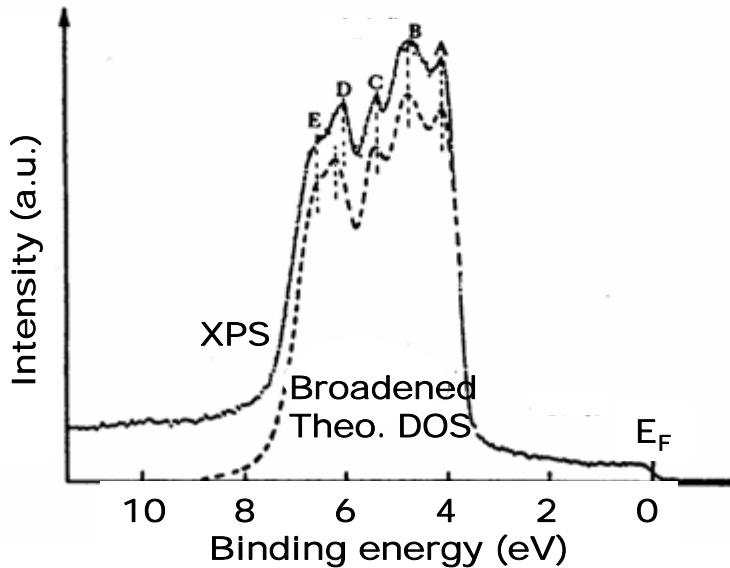
In the XPS Limit

Gold Valence Spectrum



Siegbahn XPS @ 1.487 keV

Silver Valence Spectrum



Measurement time: 3 min 40 s

Total resolution: ca. 80 meV

Takata et al., Spring8 @ 5.495 keV

Varying surface sensitivity for lower electron takeoff angles

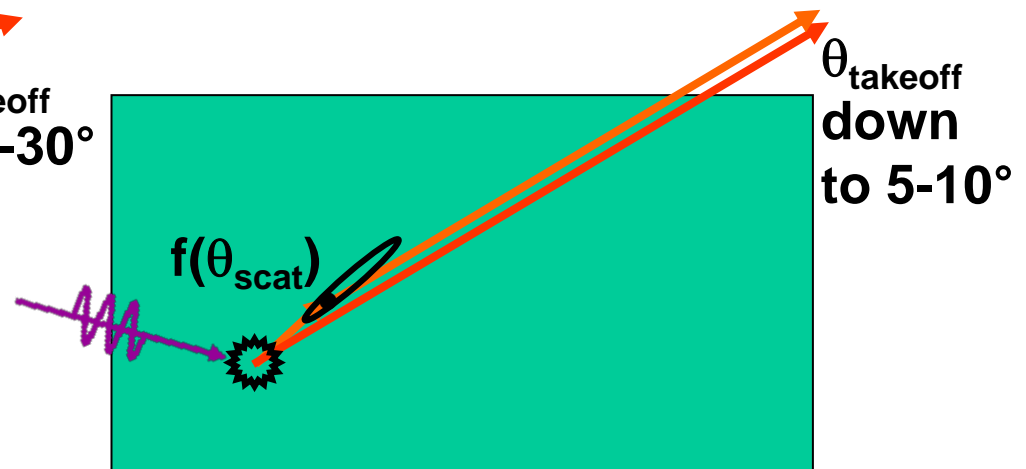
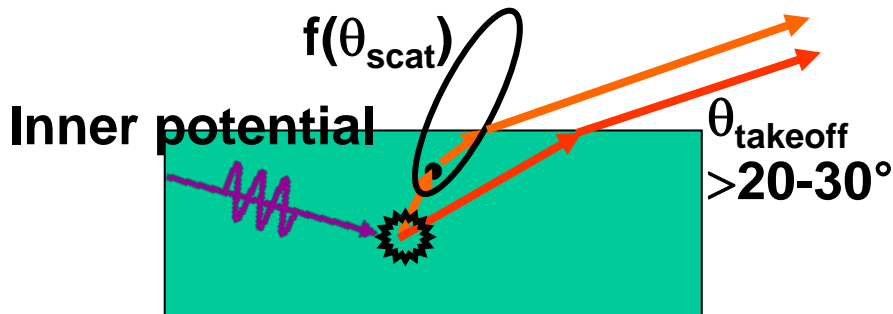
Simplest interpretation:

$$\text{Average emission depth} = \Lambda_{\text{inelastic}} \sin \theta_{\text{takeoff}}$$

How valid?

$E_{\text{kin}} \approx 500-1000 \text{ eV}$

$E_{\text{kin}} \approx 10,000 \text{ eV}$



E.g.: A. Jablonski and C. J. Powell,
J. Vac. Sci. Tech. A 21, 274 (2003):

→ Mean Emission Depth (MED)
more relevant than $\Lambda_{\text{inelastic}}$

Simpler analysis

Cleaner bulk & surface distinction

C. J. Powell, W. Werner et al., priv. comm.;
C.S.F., Nucl. Inst. & Meth. A 547, 24 (2005)

Outline

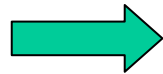
Surface, interface, and nanoscience—short introduction

Some surface concepts and techniques→photoemission

Synchrotron radiation: experimental aspects

Electronic structure—a brief review

**The basic synchrotron radiation techniques:
more experimental and theoretical details**



Core-level photoemission

Valence-level photoemission

Microscopy with photoemission

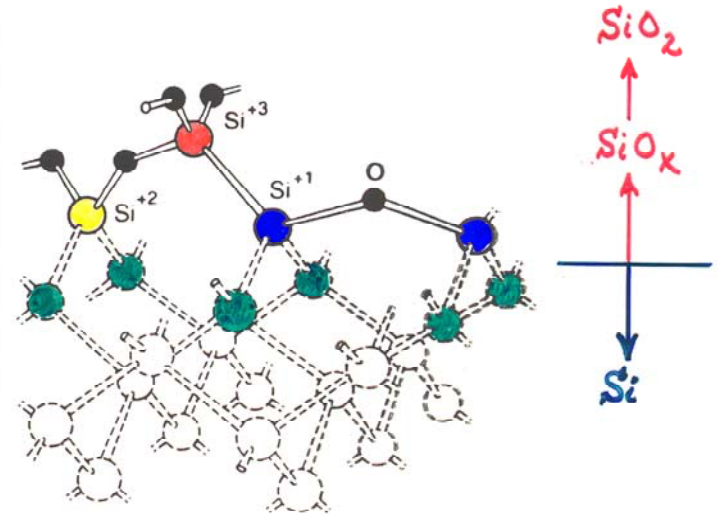
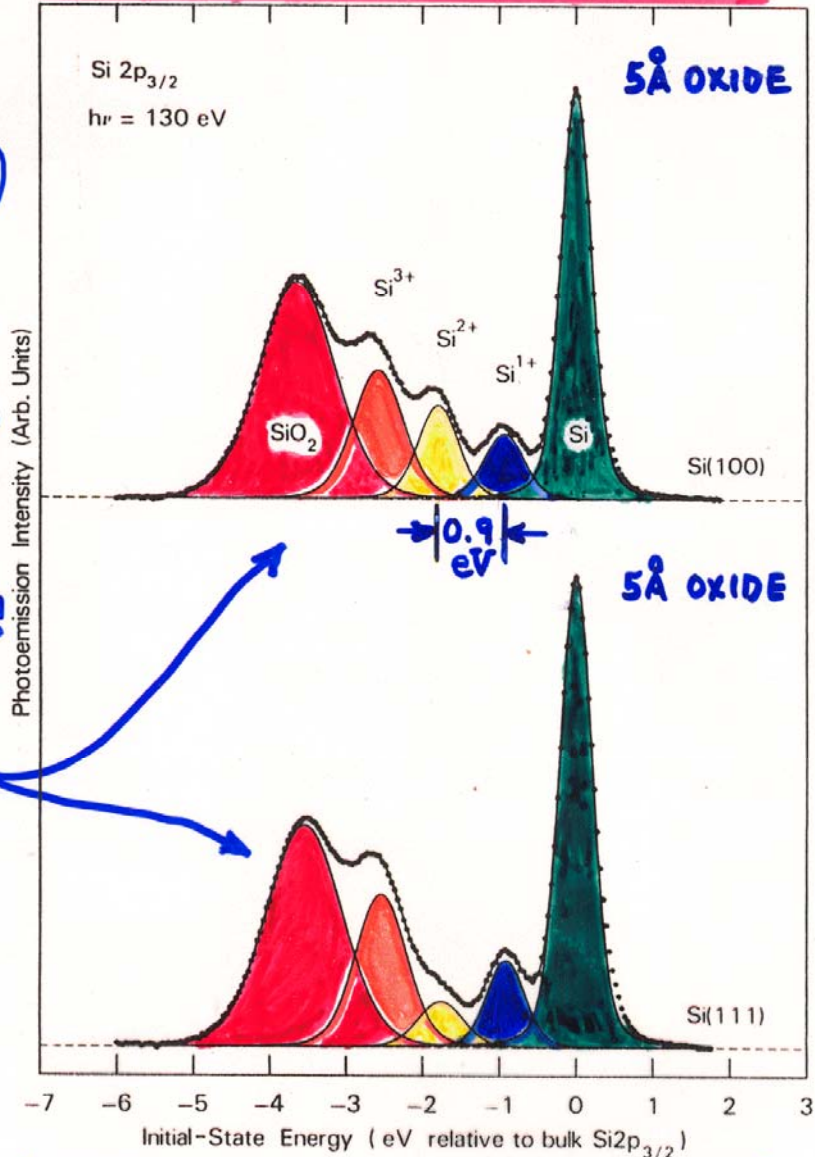
Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
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- Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
- Various other final state effects providing information in core-level spectra

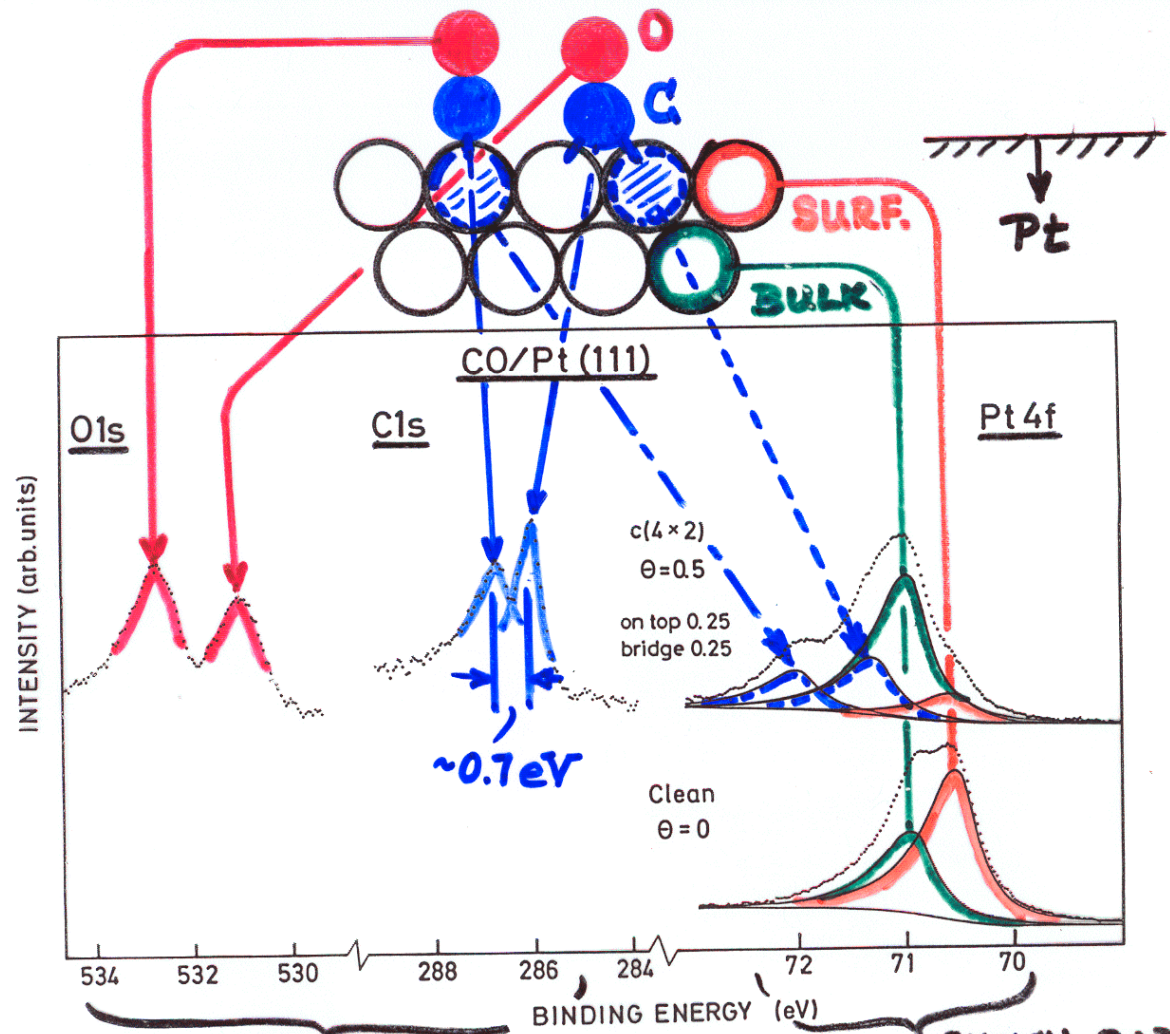
PHOTOELECTRON SPECTRA
OXIDIZED SILICON
CHEMICAL SHIFTS OF CORE LEVELS



EXACTLY
 WHAT IS
 STRUCTURE
 OF INTERFACE?
 NEED STATE-SPECIFIC
 STRUCTURAL
 INFORMATION!



CHEMICAL SHIFTS IN ADSORBATE & SUBSTRATE

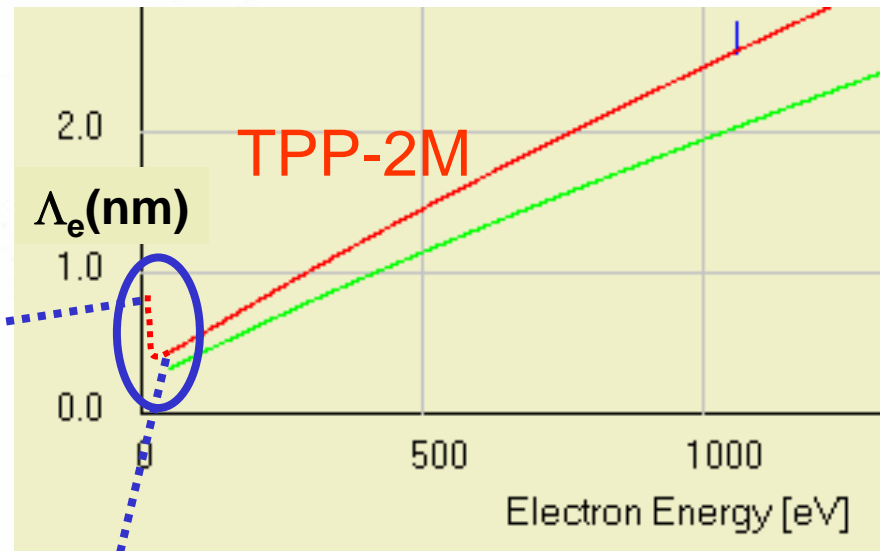
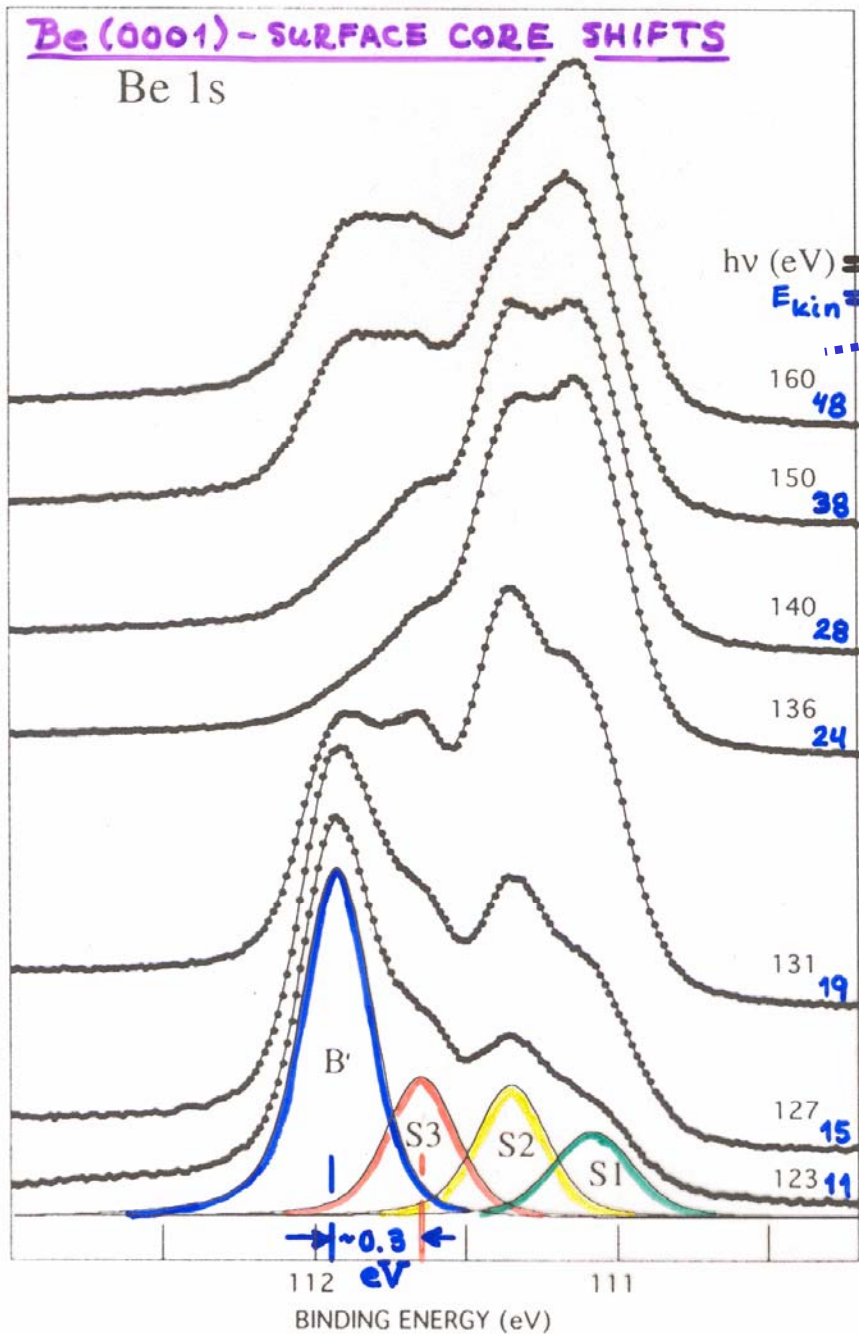


BJÖRNEHOLM
ET AL.
(NILSSON GRP.,
UPPSALA)

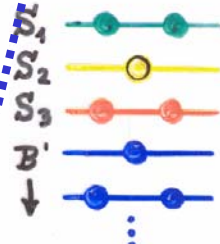
Be (0001) - SURFACE CORE SHIFTS

Be 1s

INTENSITY (arb. units)



MINIMUM IN e^- ESCAPE DEPTH



JOHANSSON ET AL., P.R.L. 71, 2453 (1993)

BINDING ENERGIES + KOOPMANS' THEOREM:

N - e^- SCH. EQN. — $\hat{H}(N)\Psi_j(N) = E_j(N)\Psi_j(N), j=1,2,\dots$

MINIMIZE $E_j(N) \left\{ \Psi_j \approx \Phi_j = \text{SLATER DET.} \right.$

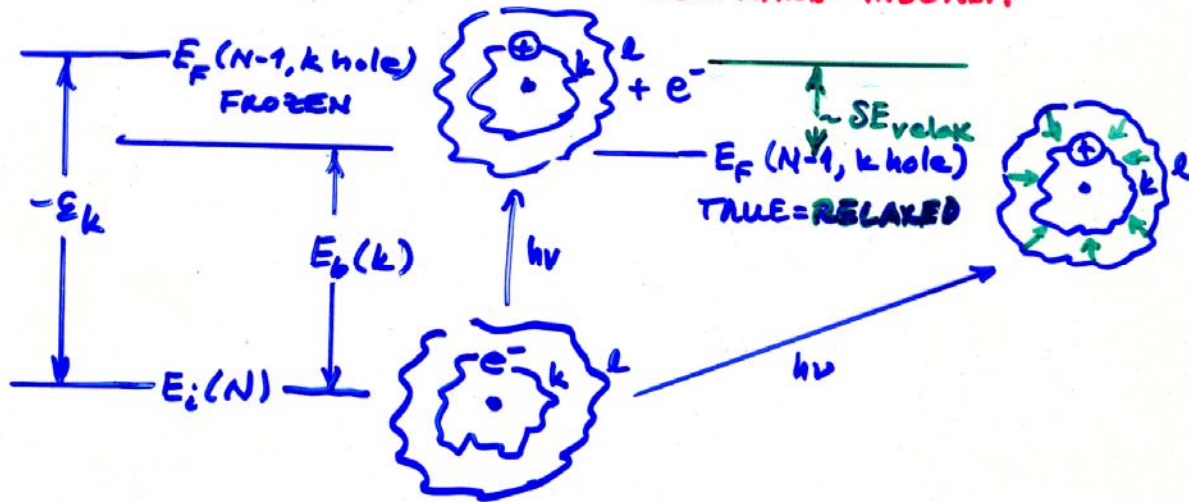
N 1 - e^- HARTREE-FOCK EQNS. — $\hat{H}(1)\psi_k(1) = \epsilon_k(1)\psi_k(1)$

- COUPLED INTEGRO-DIFF.
- COULOMB + EXCHANGE

$E_b(k) = k^{\text{th}}$ BINDING ENERGY = $E_f(N-1, k \text{ hole}) - E_i(N)$

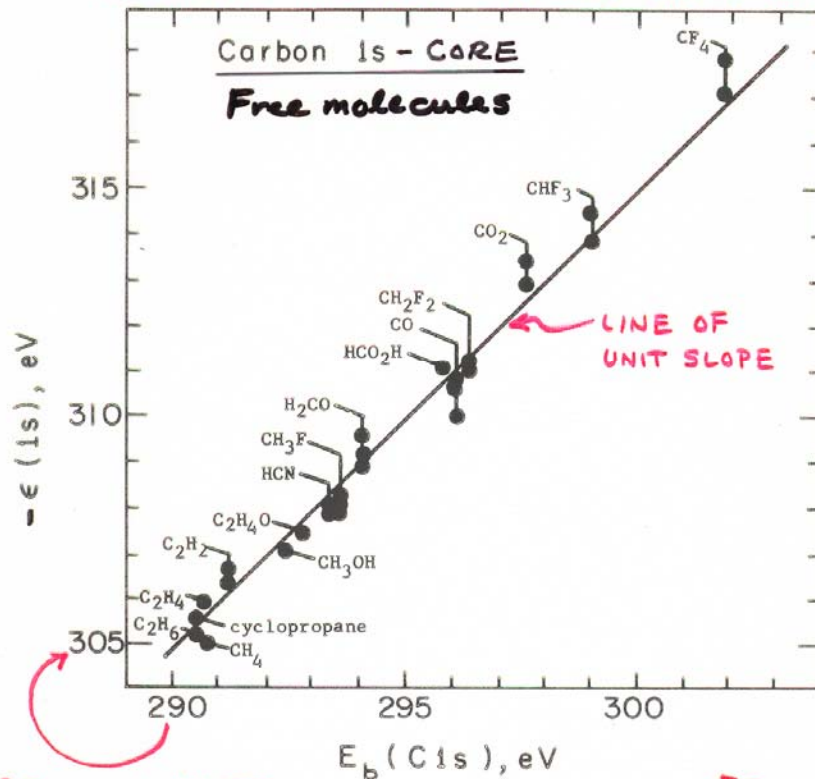
(+) EXACT
OR $E_b(k) = -\epsilon_k$ IF $\psi_{ki} = \psi_{kf}$ (FROZEN ORBITAL)

KOOPMANS' THEOREM



\Rightarrow RELAXATION, SCREENING, CONFIGURATION INTERACTION, SELF-ENERGY EFFECT ALWAYS PRESENT; ANDERSON IMPURITY MODEL ETC.

KOOPMANS' THEOREM CALCULATION OF SHIFTS

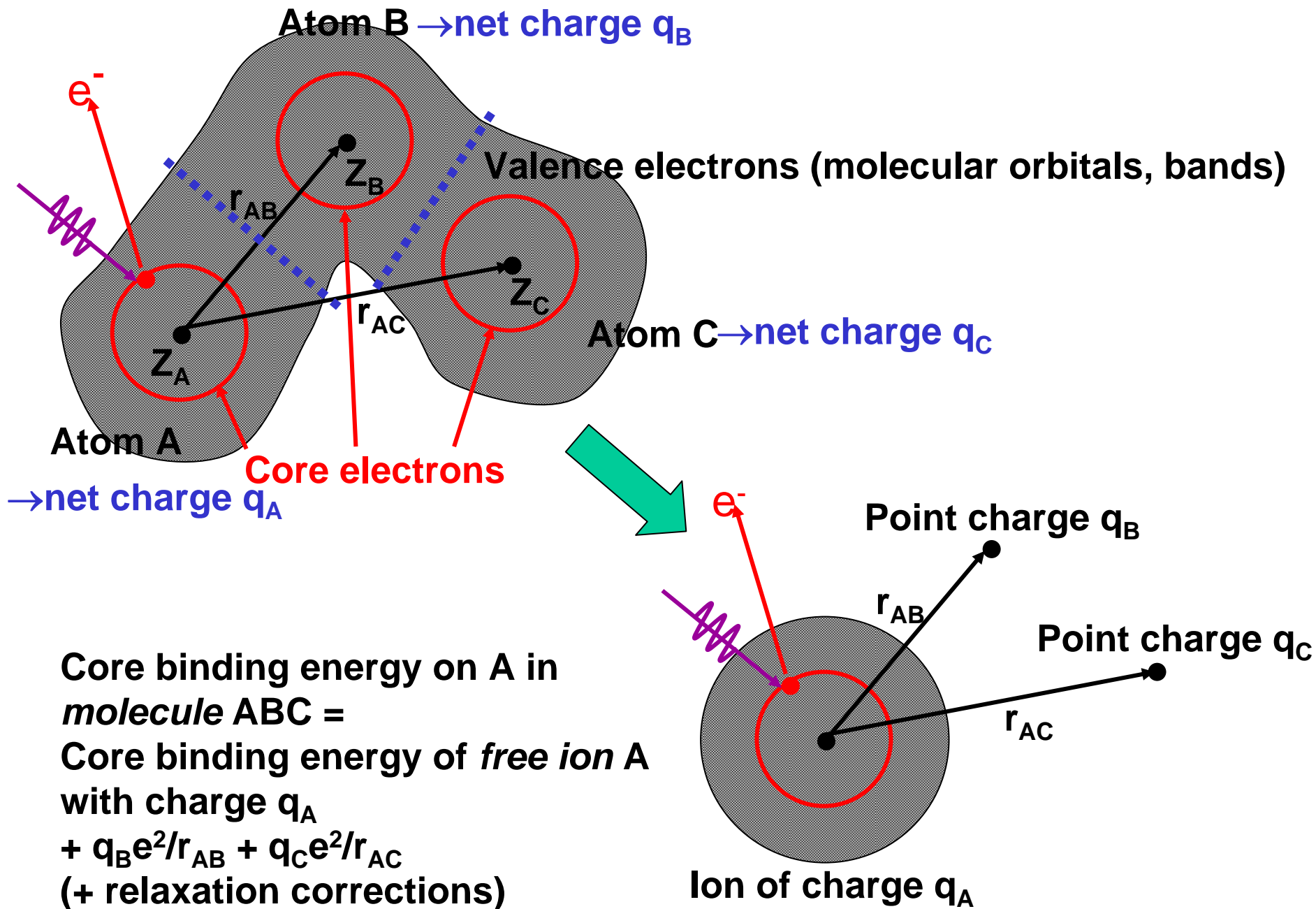


DIFF. = $\Delta E_{\text{relax}} \approx 15 \text{ eV} \approx \text{CONSTANT} \approx 5\% \text{ OF } E_b^V$

$$\Delta E_b(\text{C } 1s, \text{ "I" - CH}_4) = -\Delta E_{\text{C } 1s, \text{ "I" - CH}_4}$$

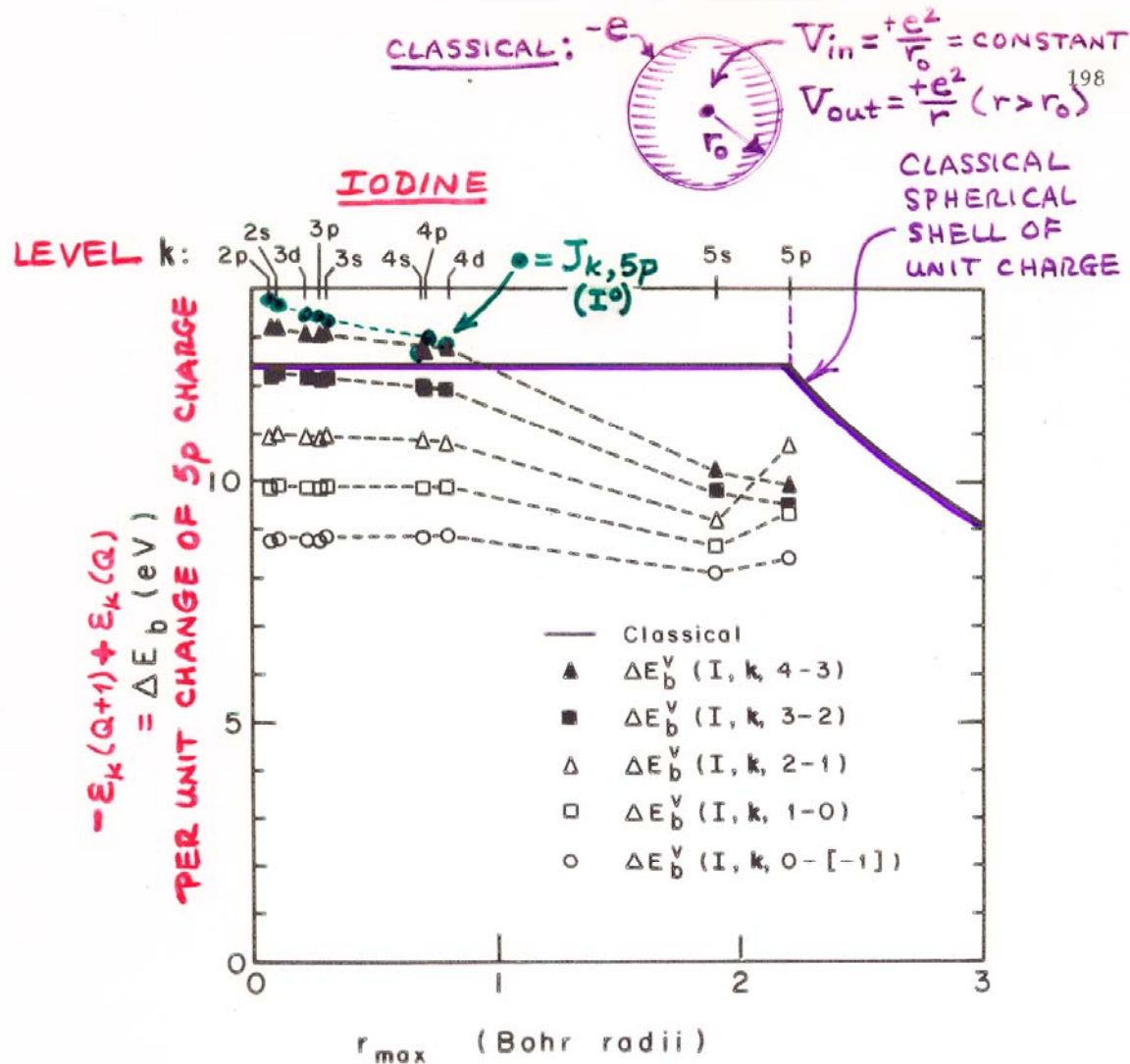
Figure 18 -- Plot of carbon 1s binding energies calculated via Koopmans' Theorem against experimental binding energies for several carbon-containing gaseous molecules. For some molecules, more than one calculated value is presented. The slope of the straight line is unity. The two scales are shifted with respect to one another by 15 eV, largely due to relaxation effects. All of the theoretical calculations were of roughly double-zeta accuracy or better. (From Shirley, reference 7.)

POTENTIAL MODEL FOR CORE-LEVEL CHEMICAL SHIFTS



Core binding energy on A in
molecule ABC =
 Core binding energy of *free ion A*
 with charge q_A
 $+ q_B e^2 / r_{AB} + q_C e^2 / r_{AC}$
 (+ relaxation corrections)

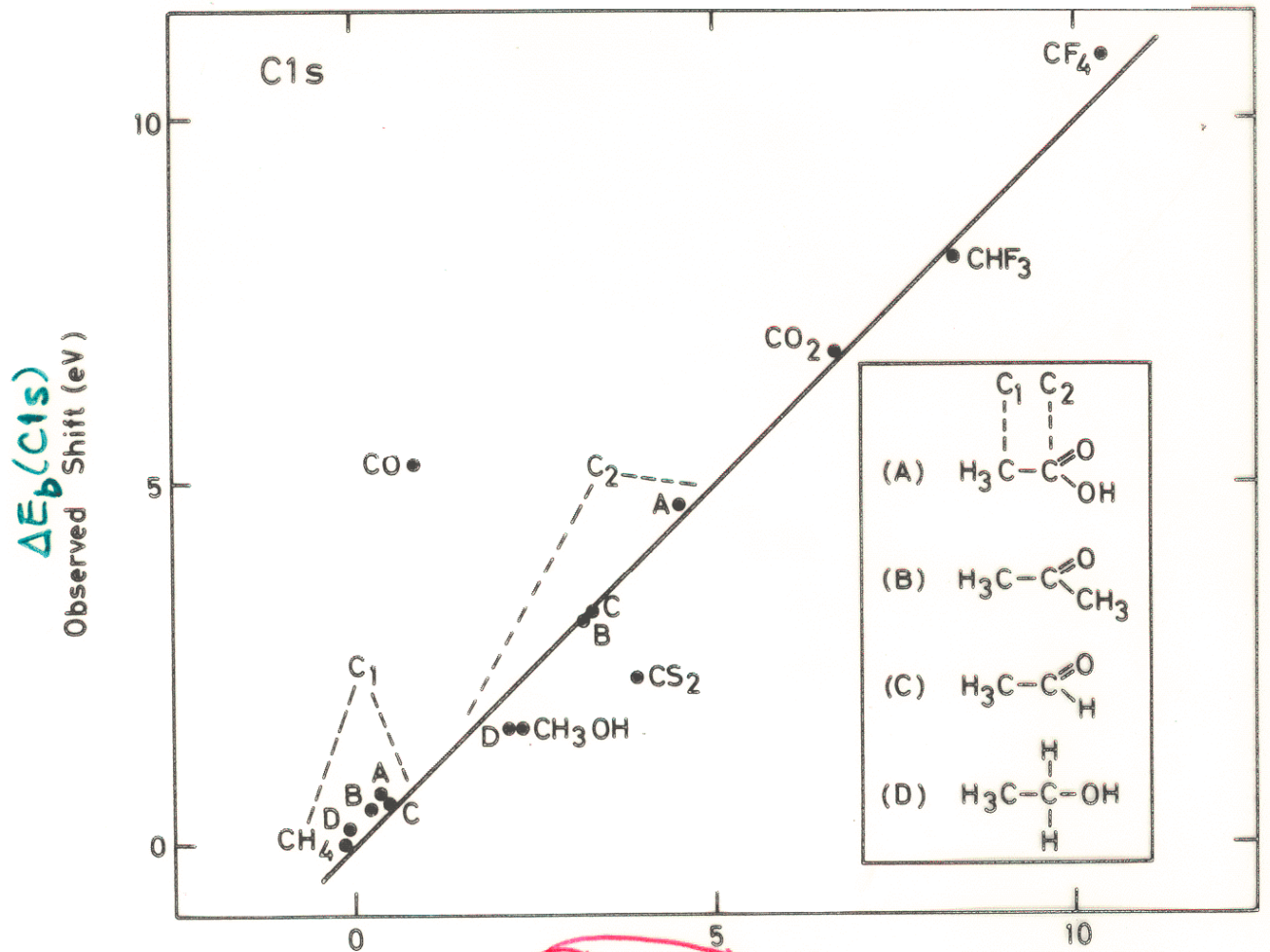
FREE-ION
(INTRAATOMIC)
ASPECTS OF
SHIFTS:
Koopmans'
THEOREM &
CLASSICAL
CHARGED SHELL



⇒ REMOVAL/ADDITION OF VALENCE e^-
 CHARGE IN BONDING SHIFTS ALL
 INNER $e^- E_b$ 'S $\approx E_k$ 'S BY SAME AMOUNT

“Basic Concepts of XPS”
 Figure 19

POTENTIAL MODEL CALCULATION OF CARBON CHEMICAL SHIFTS



$C_A q_A + V + I$ (eV)
 $(\sum q_i / r_{Ai}, q_i$'s FROM CNDO
 THEORY
 CNDO MO
 THEORY
 EMPIRICAL:
 $C_A = 21.9$ eV
 $\approx J_{1s, \text{valence}}$
 $I \approx 0.80$ eV

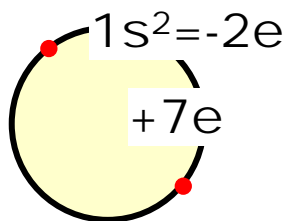
“Basic Concepts of XPS”
Figure 24

Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
- Magnetic circular dichroism (MCD) in core-level emission
- Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
- Various other final state effects providing information in core-level spectra

CORRELATION OF THERMOCHEMICAL DATA WITH CHEMICAL SHIFTS: EQUIVALENT-CORE OR (Z+1) MODEL

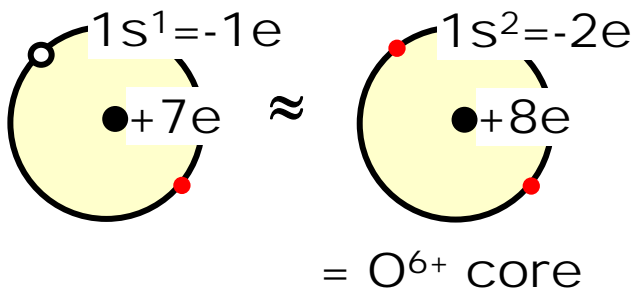
N core = N $1s^2$ = N⁵⁺



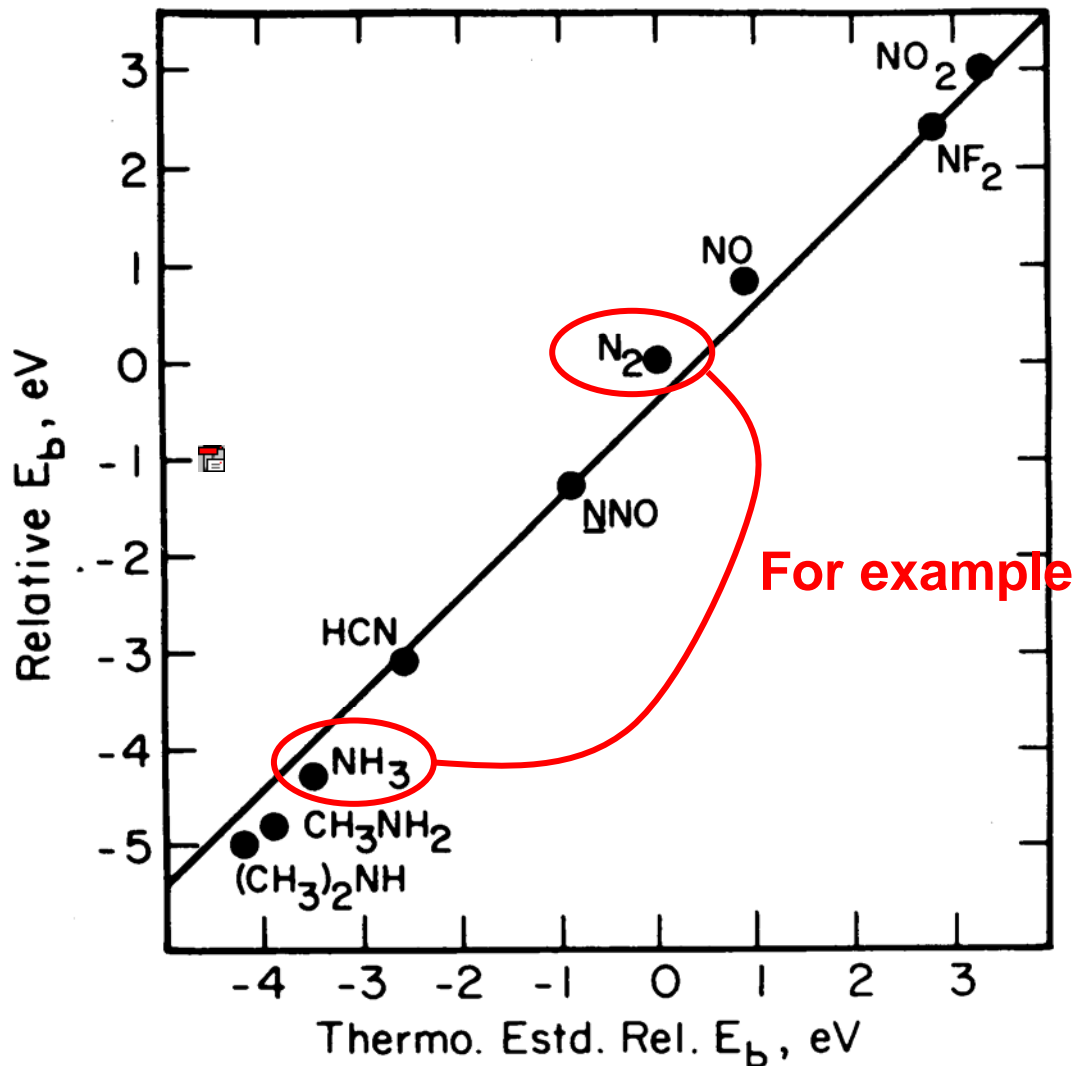
Assume:

N^{6+*} core with

1s hole = N^{6+*} =



Plus see pp. 92-93
in "Basic Concepts
of XPS"

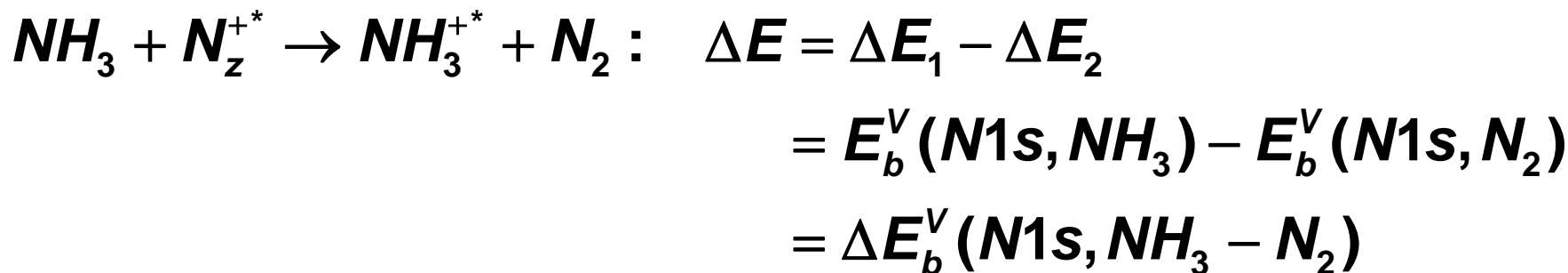


Jolly et al.

Binding energies: * = N 1s core hole present

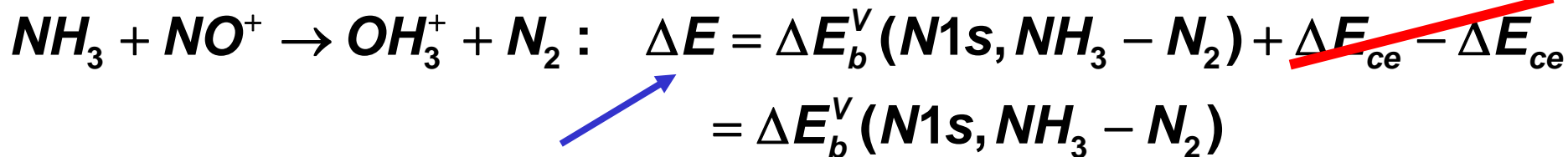


Adding and subtracting:



The chemical shift

Replacing real N 1s core with equivalent O 1s core:

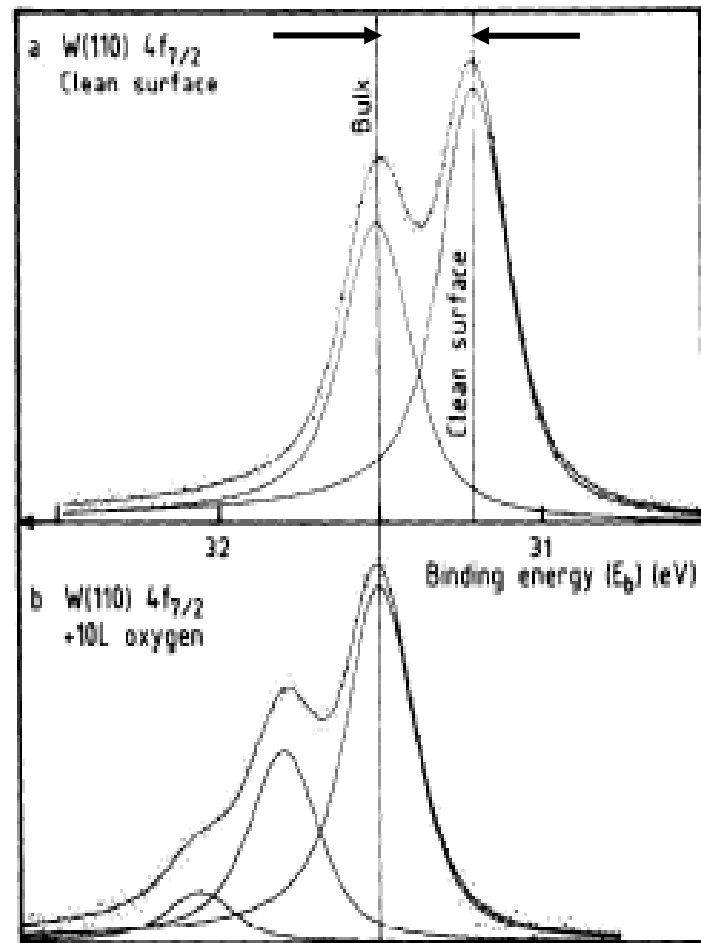
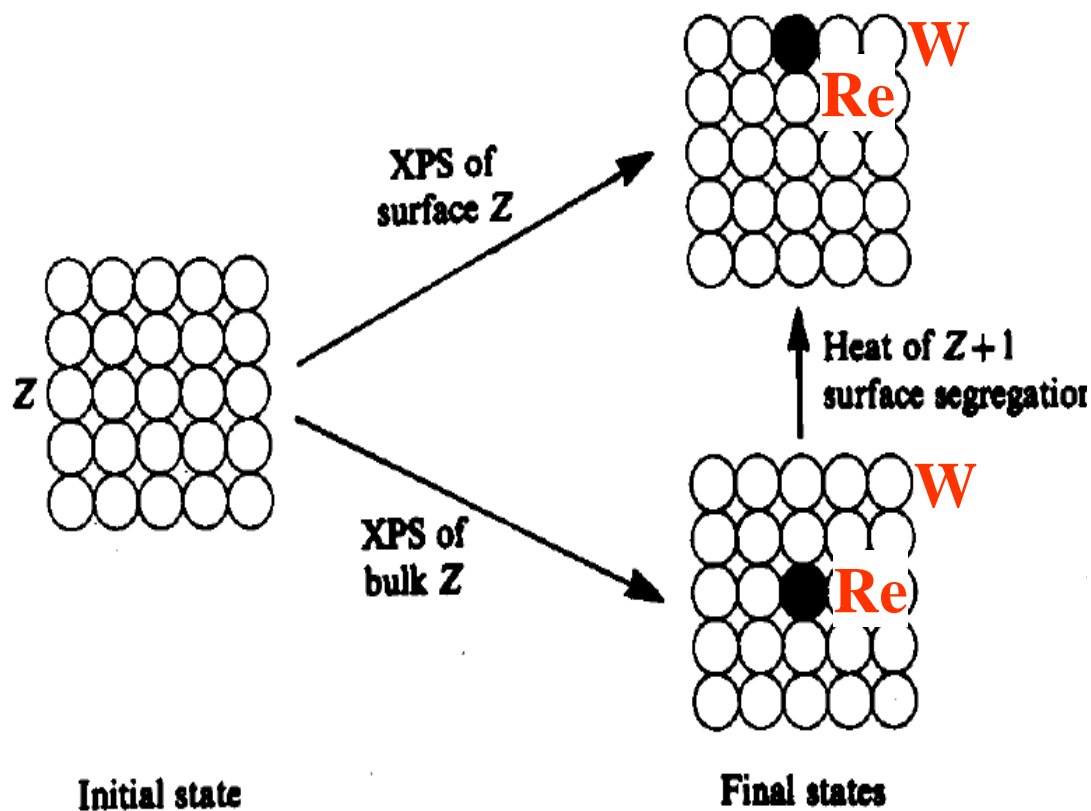


A thermochemical energy

DERIVATION OF HEAT OF SURFACE SEGREGATION FROM SURFACE CORE-LEVEL CHEMICAL SHIFTS

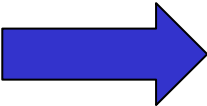
Fig. 4.30. The XPS surface core level shift approach to the heat of segregation of a binary alloy (Egelhoff, 1983). (Zangwill, p. 87)

$$\Delta E_b = \Delta H_{\text{segregation}}$$

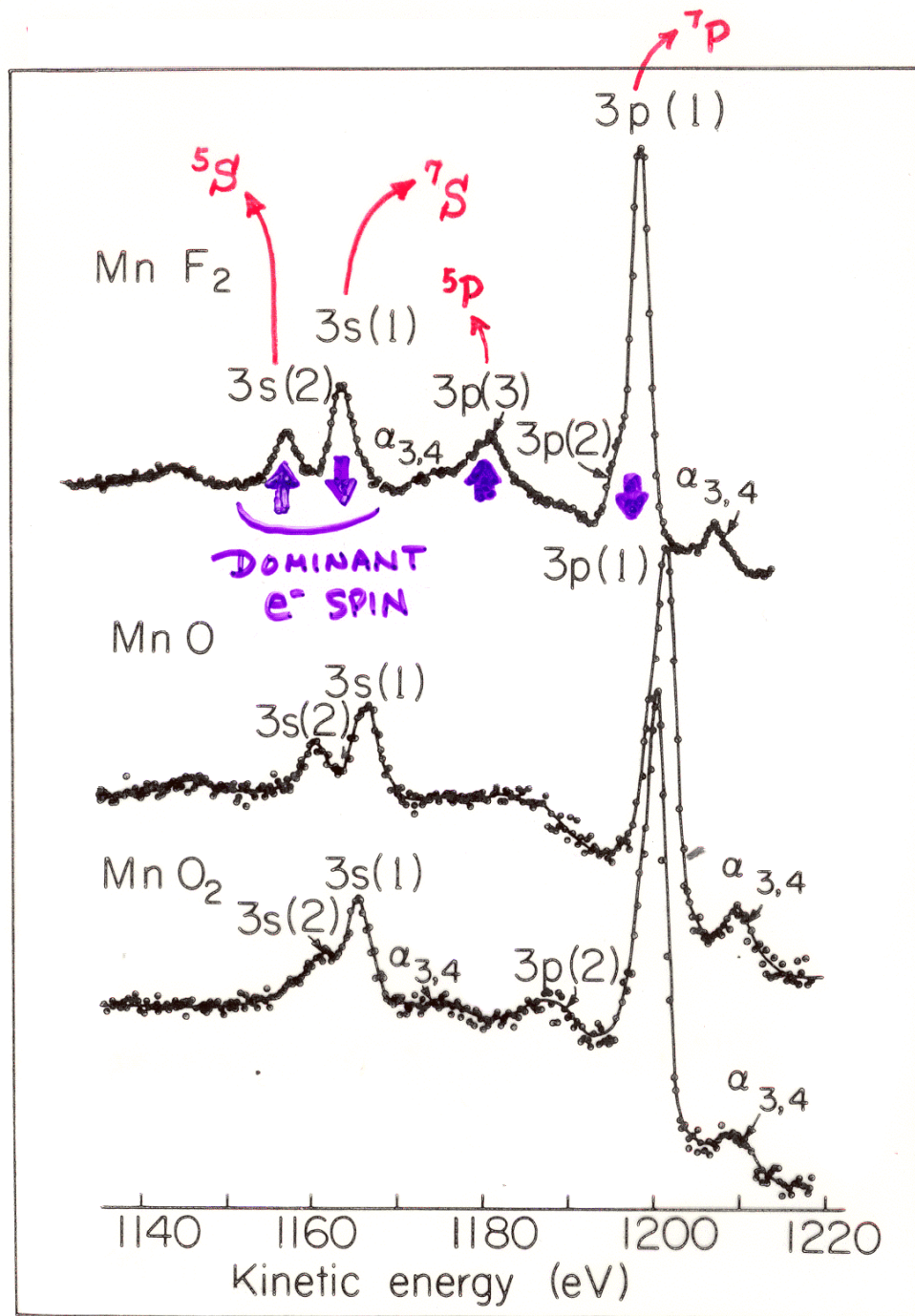


Spanjaard et al., Surf. Sci. Repts. 5, 1 (1985)

Outline

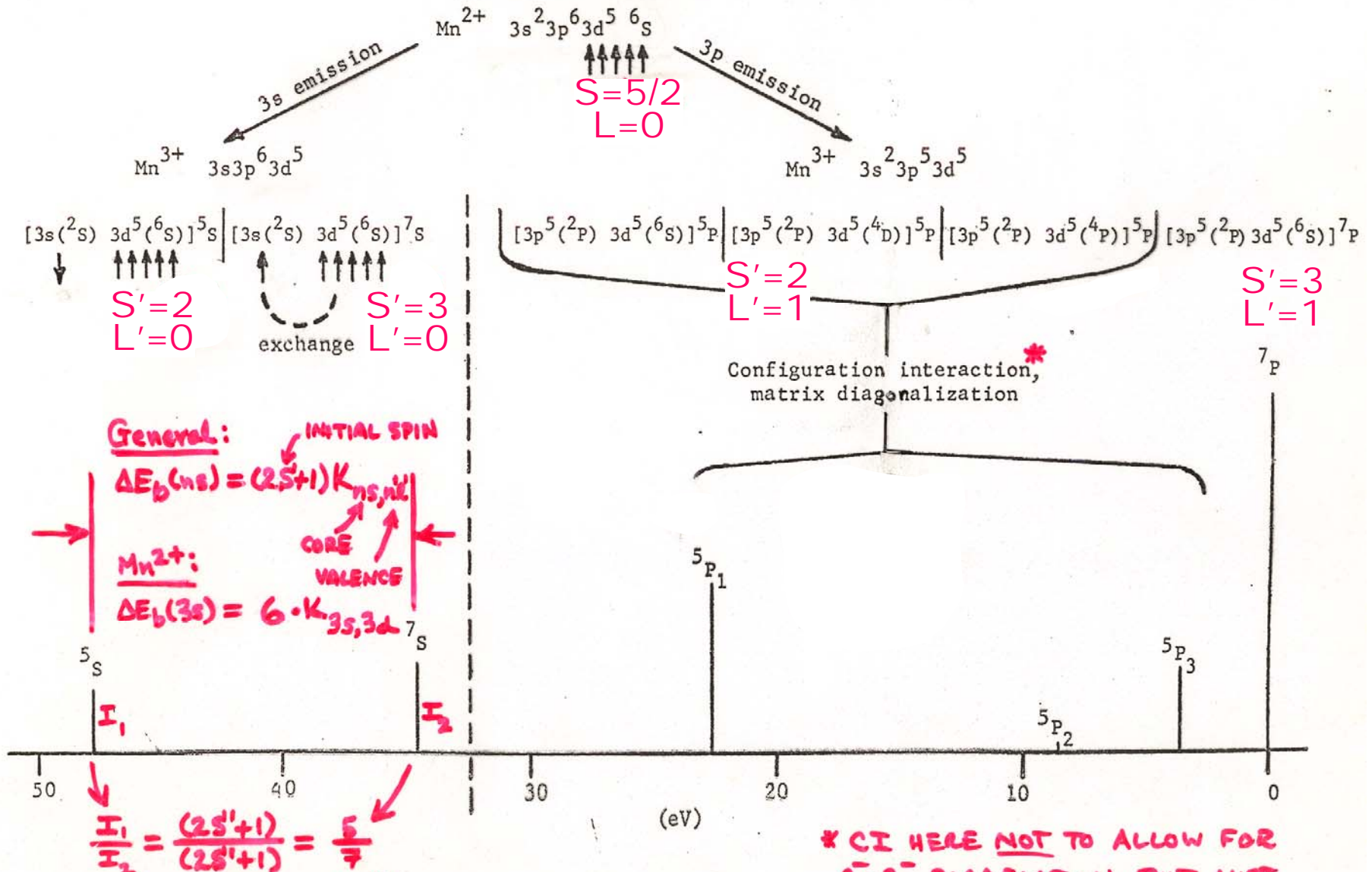
- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
-  Multiplet splittings and magnetism
 - Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
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CORE-LEVEL MULTIPLET SPLITTINGS IN Mn COMPOUNDS



“Basic Concepts of XPS”
Figure 31

ORIGIN OF MULTIPLET SPLITTINGS IN Mn²⁺: "ONE-ELECTRON" THEORY

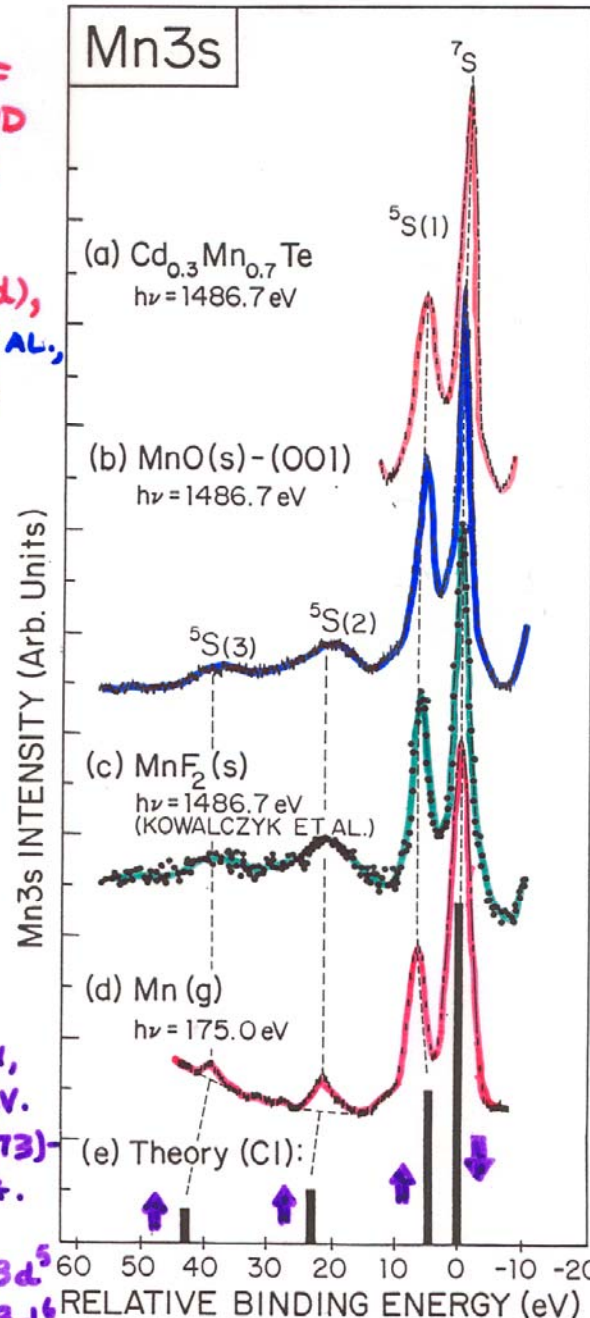


"Basic Concepts of XPS"
Figure 30

* CI HERE NOT TO ALLOW FOR e^-e^- CORRELATION, BUT JUST DIFFERENT COUPLING IN $3p^5 3d^5$

**COMPARISON OF
GAS-PHASE AND
SOLID-STATE
SPECTRA**

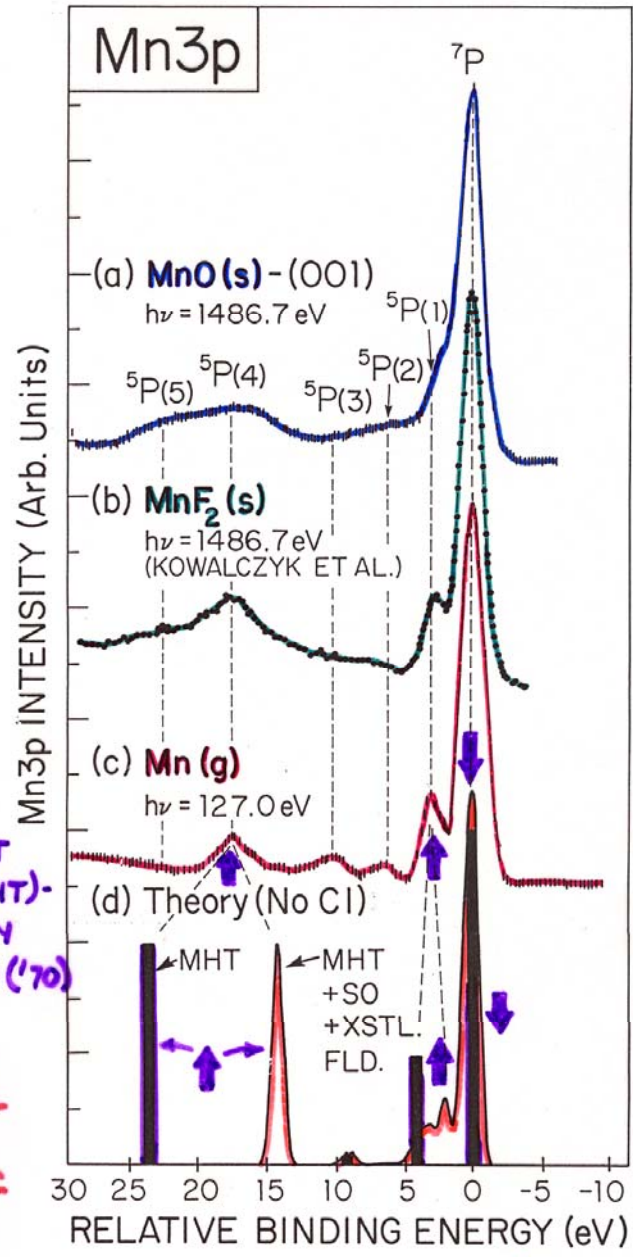
**EXPT. : (a), (b), (d),
HERMSMEIER ET AL.,
PHYS. REV. LETT.
61, 2592 (1988)
(OUR GROUP)**



Correlation
CI effects:
anti-parallel
electrons

THEORY:
BAGUS, FREEMAN,
SASAKI, PHYS. REV.
LETT. 30, 850 (1973)
ATOMIC CONFIG.
INT. IN
 $\text{Mn}^{2+} \dots 3s^2 \dots 3d^5$
 $+ \text{Mn}^{3+} \dots 3s^2 3p^4 3d^6$

**“Basic Concepts of XPS”
Figure 33**



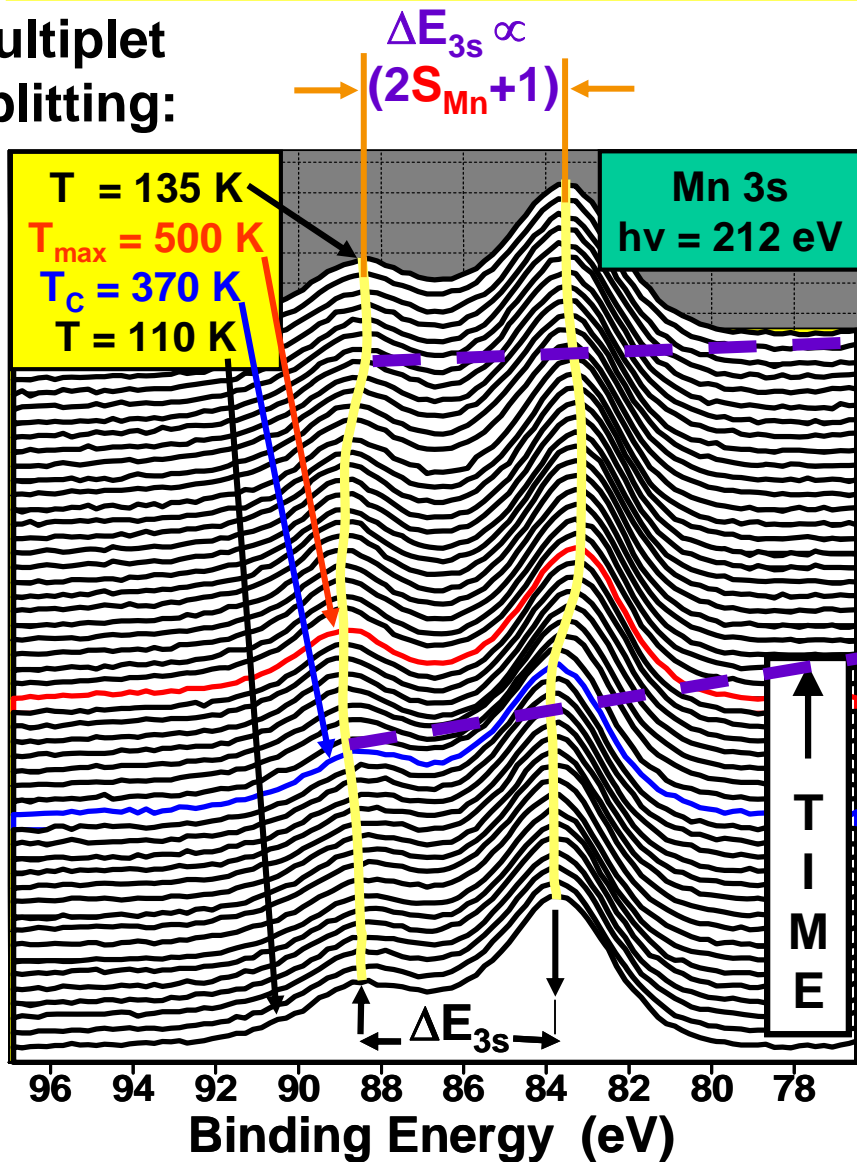
THEORY: NO CI
SIMPLE MULTIPLET HOLE THEORY (MHT)-
FADLEY, SHIRLEY
PHYS. REV. A2, 1109 ('70)
EMPIRICAL
MHT WITH SPIN ORBIT & CRYSTAL FIELD- SUGANO
ET AL., J. PHYS. C
15, 2625 (1982)

HERNSMEIER
ET AL.,
P.R.L. 61, 2592 ('88)

Temperature dependence of Mn3s and O1s spectra in a colossal magnetoresistive (CMR) oxide: $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$

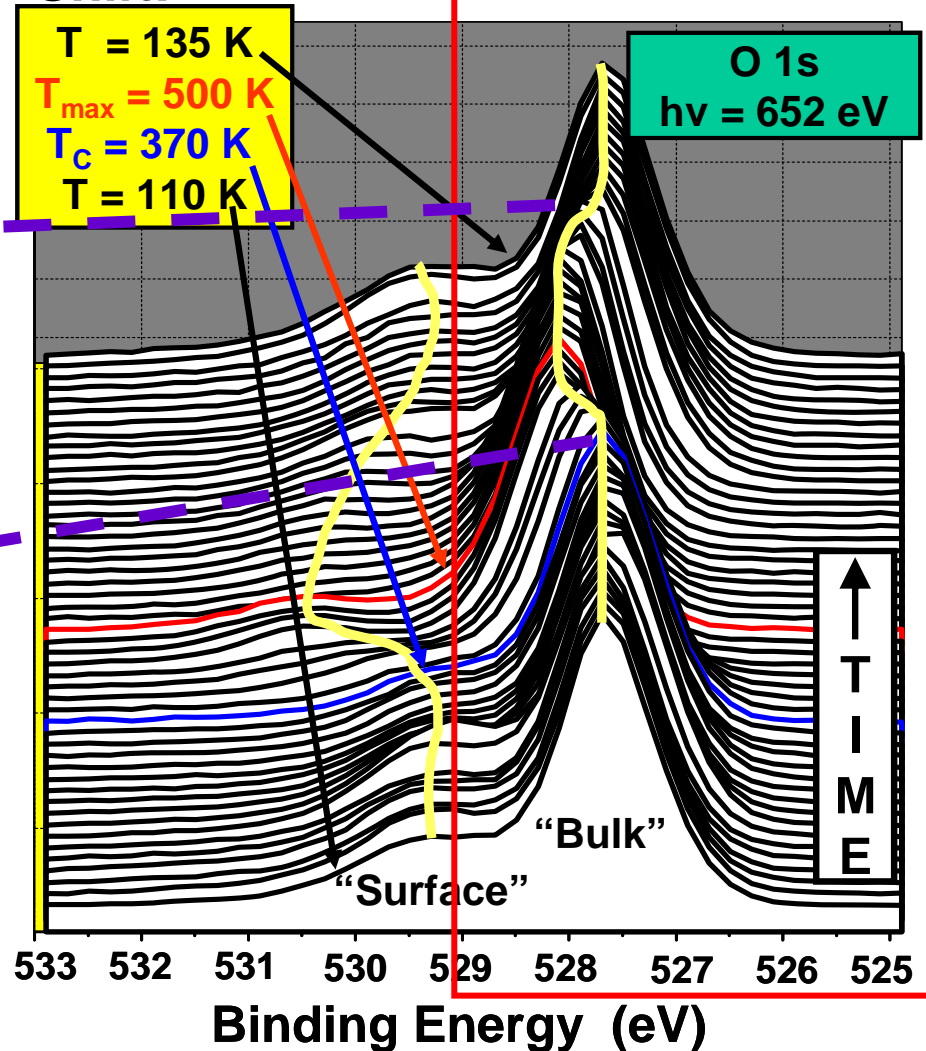
Multiplet Splitting:

Photoelectron Intensity (a.u.)



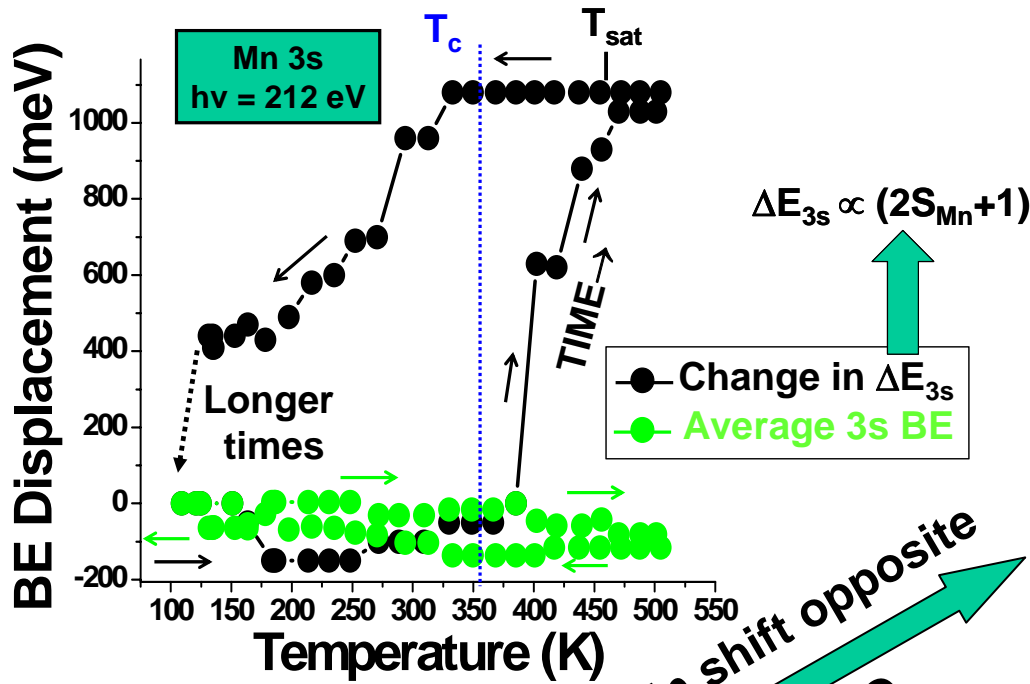
Increase of the Mn3s splitting-reversible

Chemical Shift:

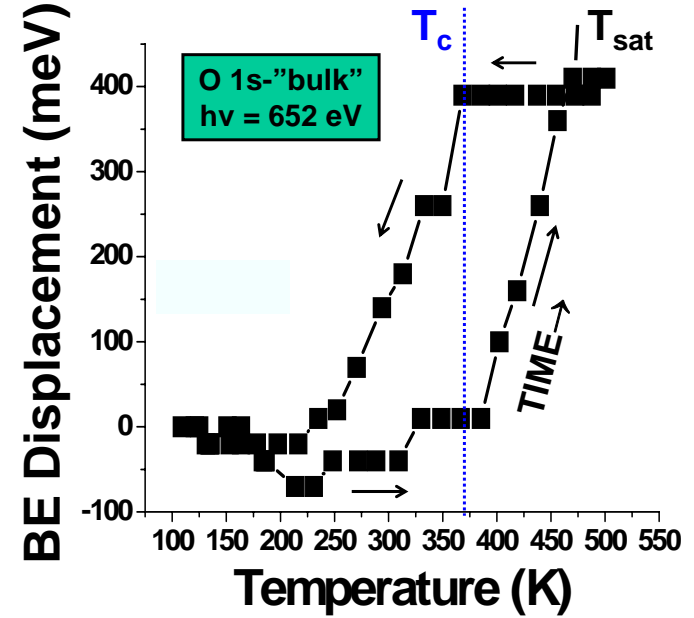


Increase of O1s BE-reversible

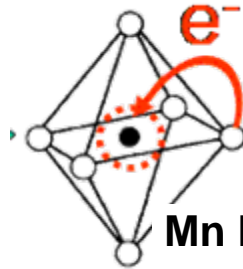
T dependence of Mn 3s binding energies



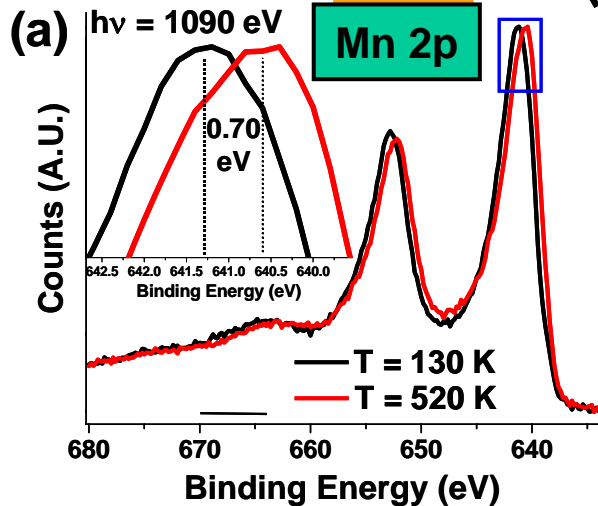
T dependence of bulk O 1s binding energy



Mn shift opposite
to O



O more positive
Mn higher spin,
more negative



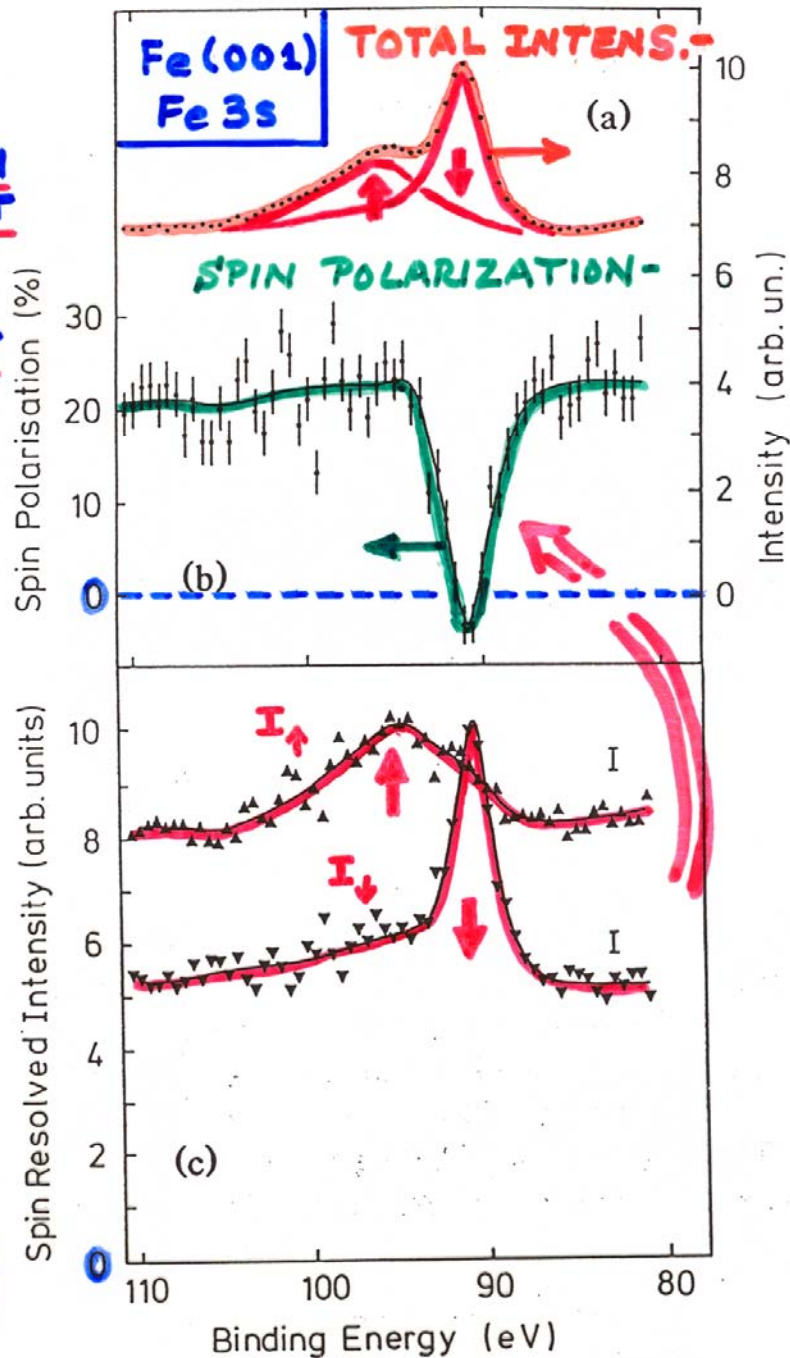
Theory: self-interaction corrected local spin density results for LSMO \rightarrow elongating octahedron makes Mn^{3+} more stable than Mn^{4+}
Banach, Temmerman, PRB 69, 054427 ('04)

Mannella et al., Phys. Rev. Lett. 92, 166401 (2004)

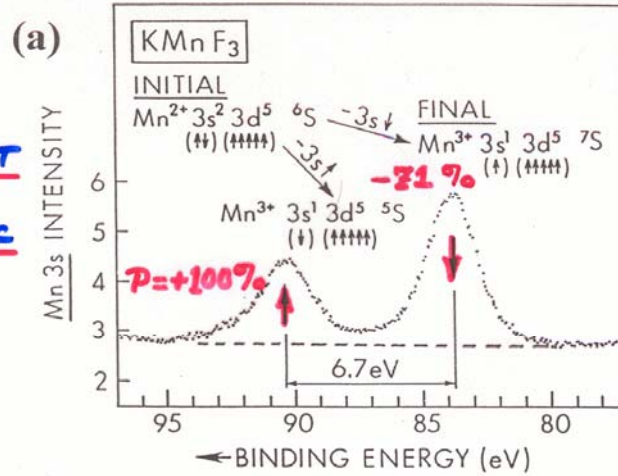
DIRECT
OBSERVATION
OF SPIN-SPLIT
CORE LEVELS
IN A
FERROMAGNET

$$\frac{I_{\uparrow} - I_{\downarrow}}{I_{\uparrow} + I_{\downarrow}}$$

HILLEBRECHT
ET AL.,
PHYS. REV. LETT.
65, 2450 (1990)



①
MULTIPL
ET
IN A
MAGNETIC
ATOM

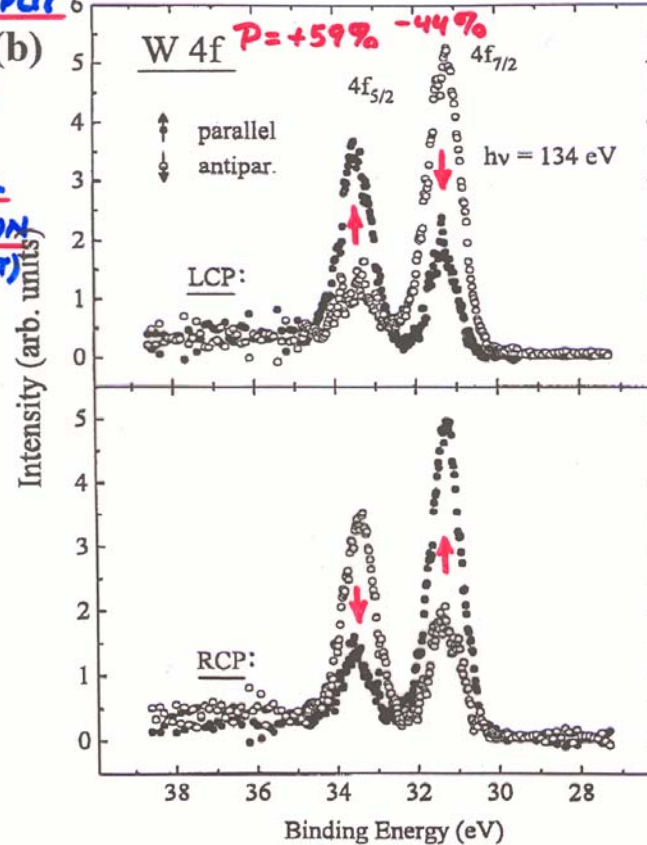


SPIN POLARIZATION
IN CORE SPECTRA

$$P = \frac{I_{\uparrow} - I_{\downarrow}}{I_{\uparrow} + I_{\downarrow}}$$

EXPT. - SINKOVIC
ET AL.
P.R.L. 55,
1227 (1985)

②
SPIN-ORBIT SPLIT
LEVEL
EXCITED
WITH
CIRCULAR
POLARIZATION
(FANO EFFECT)



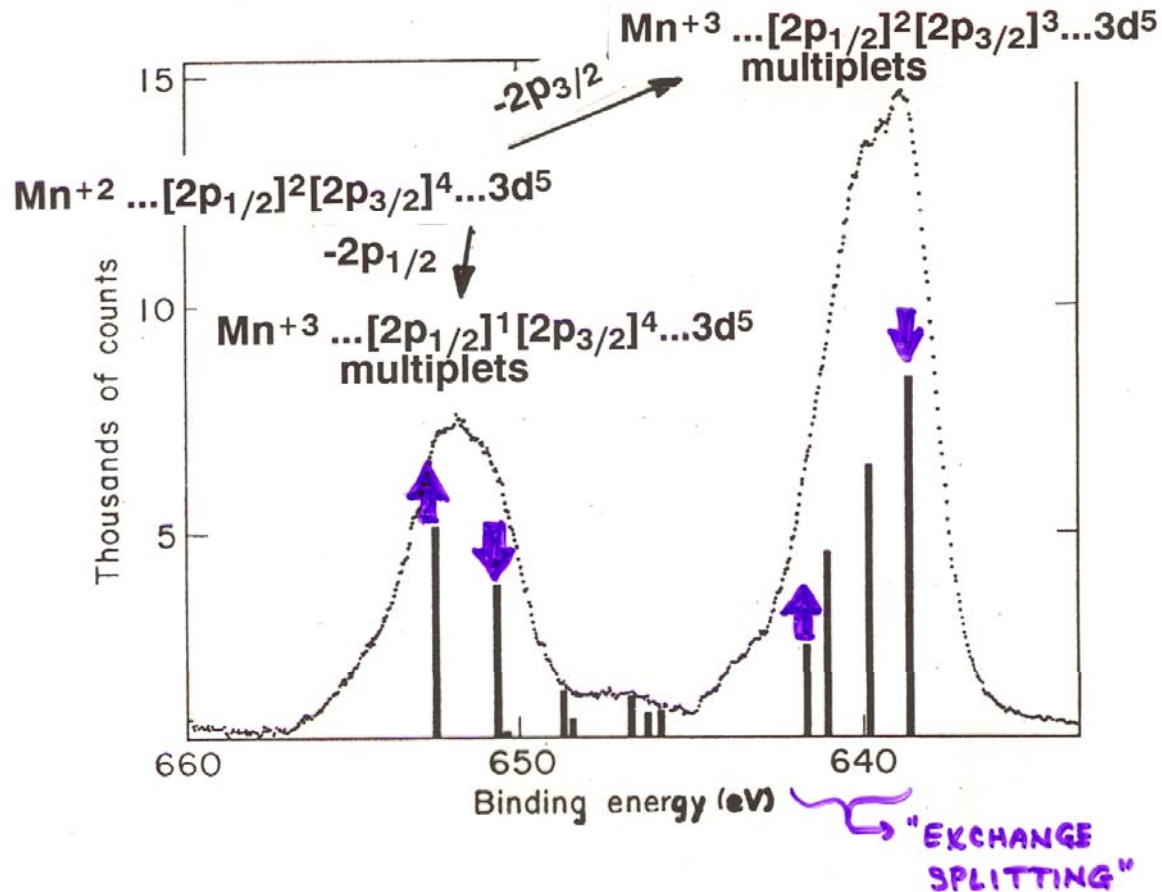
EXPT. - STARK ET
AL.
PRB 53, R10544
(1996)

Spin
internally
referenced
to spin of
each ion

Spin
externally
referenced
to \vec{k}_{hv} and \vec{M}
of sample

**+ MORE COMPLEX MULTIPLETS FOR $L > 0$
WITH SPIN-ORBIT COUPLING:**

Mn 2p emission from MnF_2 :

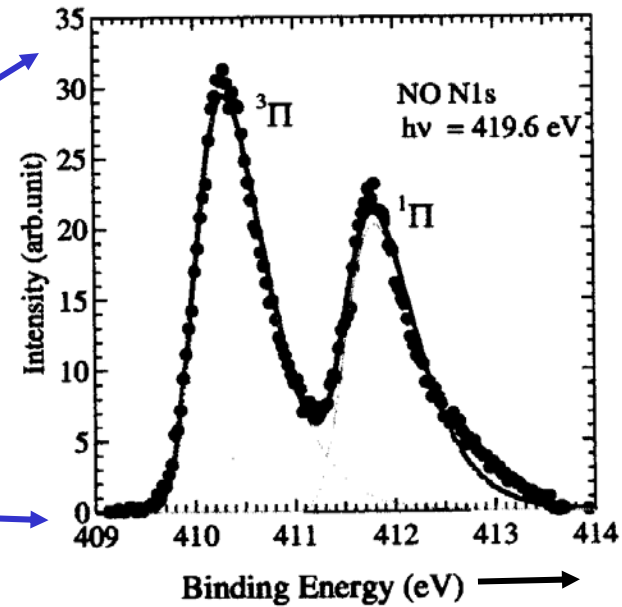
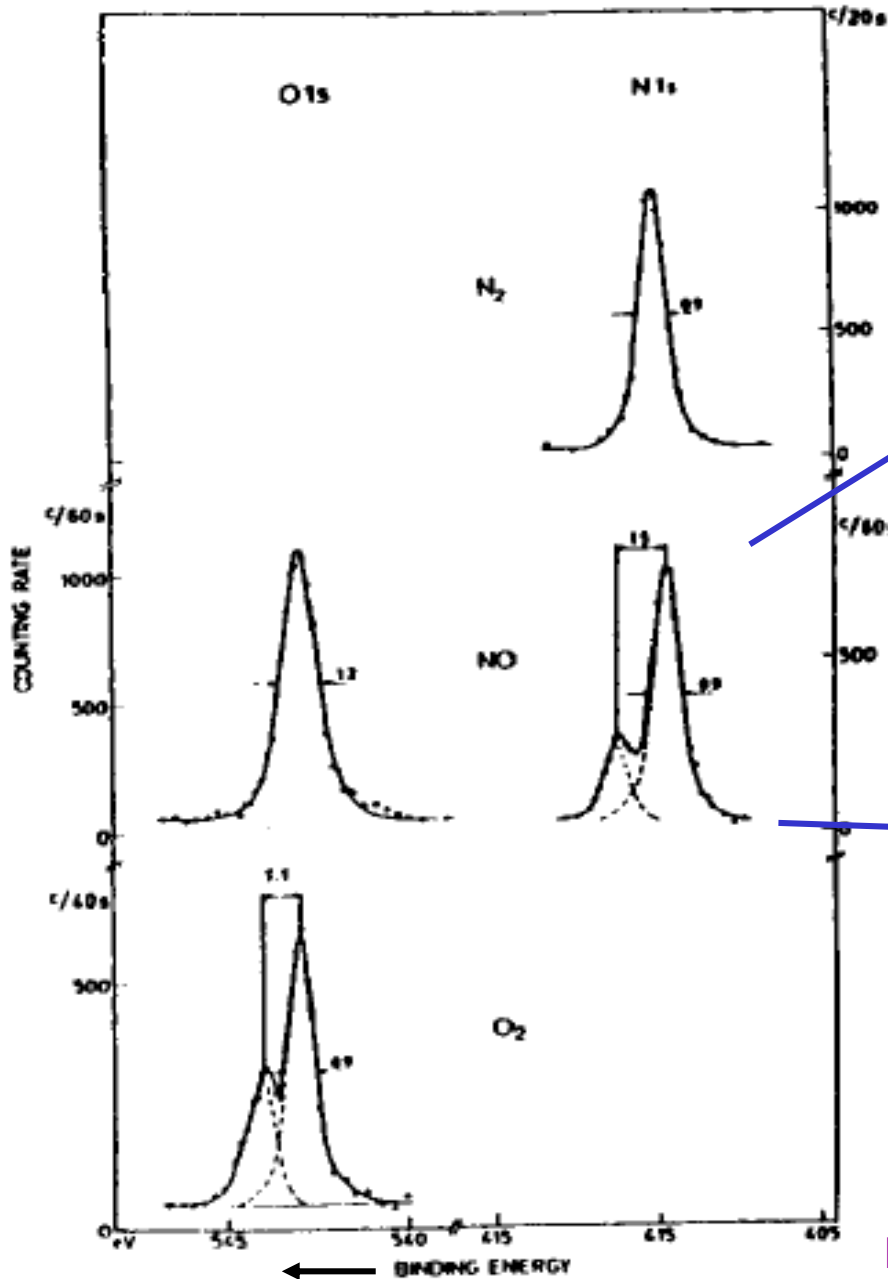


Expt.--Kowalczyk et al., Phys. Rev. B11, 1721 (1975)

Theory--Gupta and Sen, Phys. Rev. B10, 71 (1974)

Park et al., Phys. Rev. B37, 10967 (1988)

MULTIPLETS IN FREE MOLECULES



Hosaka et al., J. Phys. B
36, 4617 (2003), and
earlier theory from
Bagus and Schaefer,
J. Chem. Phys. 55, 1474
(1971)

Fig. 34
Basic Concepts of XPS

Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit

- Core-level chemical shifts: the potential model

- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies

- Multiplet splittings



- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons

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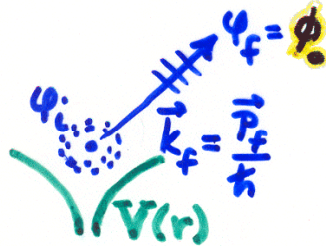
PHOTOELECTRON EMISSION-

BASIC MATRIX ELEMENTS + SELECTION RULES:

● ATOMIC-LIKE (LOCALIZED) STATES \Rightarrow CORE:

PLUS SPIN:

$$\psi_i(\vec{r}) = \psi_{n_i l_i m_i}(r, \theta, \phi) = R_{n_i l_i}(r) Y_{l_i m_i}(\theta, \phi) \begin{cases} \alpha(\sigma) = m_{s_i} = +1/2 = \uparrow \\ \beta(\sigma) = m_{s_i} = -1/2 = \downarrow \end{cases}$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f m_f}^*(\theta, \phi) Y_{l_f m_f}(\theta, \phi) R_{E_f, l_f}(r) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

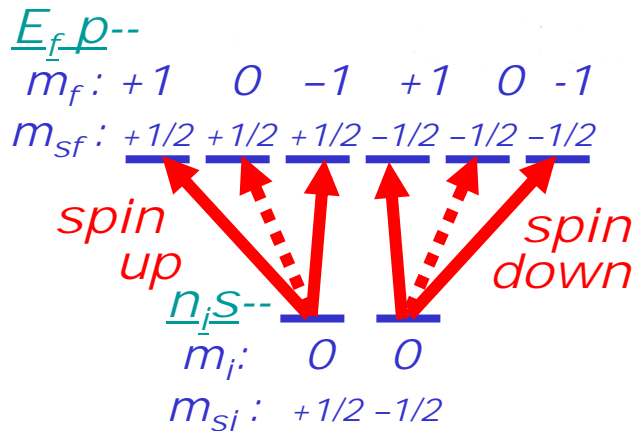
PHASE SHIFT OF l_f WAVE IN $V(r)$

DIPOLE: INT. $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \langle \psi_f | \vec{r} | \psi_i \rangle|^2 \Rightarrow \left\{ \begin{array}{l} \Delta l = l_f - l_i = \pm 1 \\ \text{TWO CHANNELS} \\ \Delta m = m_f - m_i = 0, \pm 1 \\ \text{LINEAR POLAR.} \\ \Delta m = \pm 1, \text{ CIRCULAR POLARIZATION} \end{array} \right.$

EQUIVALENT WITHIN CONSTANT FACTOR



$$\Delta m_s = m_{s_f} - m_{s_i} = 0!$$



FOR A GIVEN $n_i / l_i m_i m_{s_i}$: SUM OVER DEGENERATE INITIAL STATES $m_i m_{s_i}$ AND AVERAGE OVER FINAL STATES $E_f / l_f m_f m_{s_f}$ ACCESSED FROM EACH m_i TO YIELD DIFFERENTIAL SUBSHELL PHOTOELECTRIC CROSS SECTION:

$$d\sigma_{n_i l_i} / d\Omega$$

\propto PROBABILITY PER UNIT SOLID ANGLE OF EXCITING ONE ELECTRON FROM SUBSHELL n_i / l_i INTO THE DIRECTION k_f

• SPIN-ORBIT SPLITTING OF LEVELS:



⇒ EFFECTIVE \vec{B} (NUCLEUS AROUND e^-) $\propto \vec{L}$

$$\hat{H}_{s.o} = \xi(r) \vec{L} \cdot \vec{S}$$

- SPLITS ALL nl LEVELS $2(2l+1)$
 - $nl_j = l + 1/2 \rightarrow 2l+2$
 - $nl_j = l - 1/2 \rightarrow 2l$

• MIXES SPIN + ORBITAL ANGULAR MOM.:

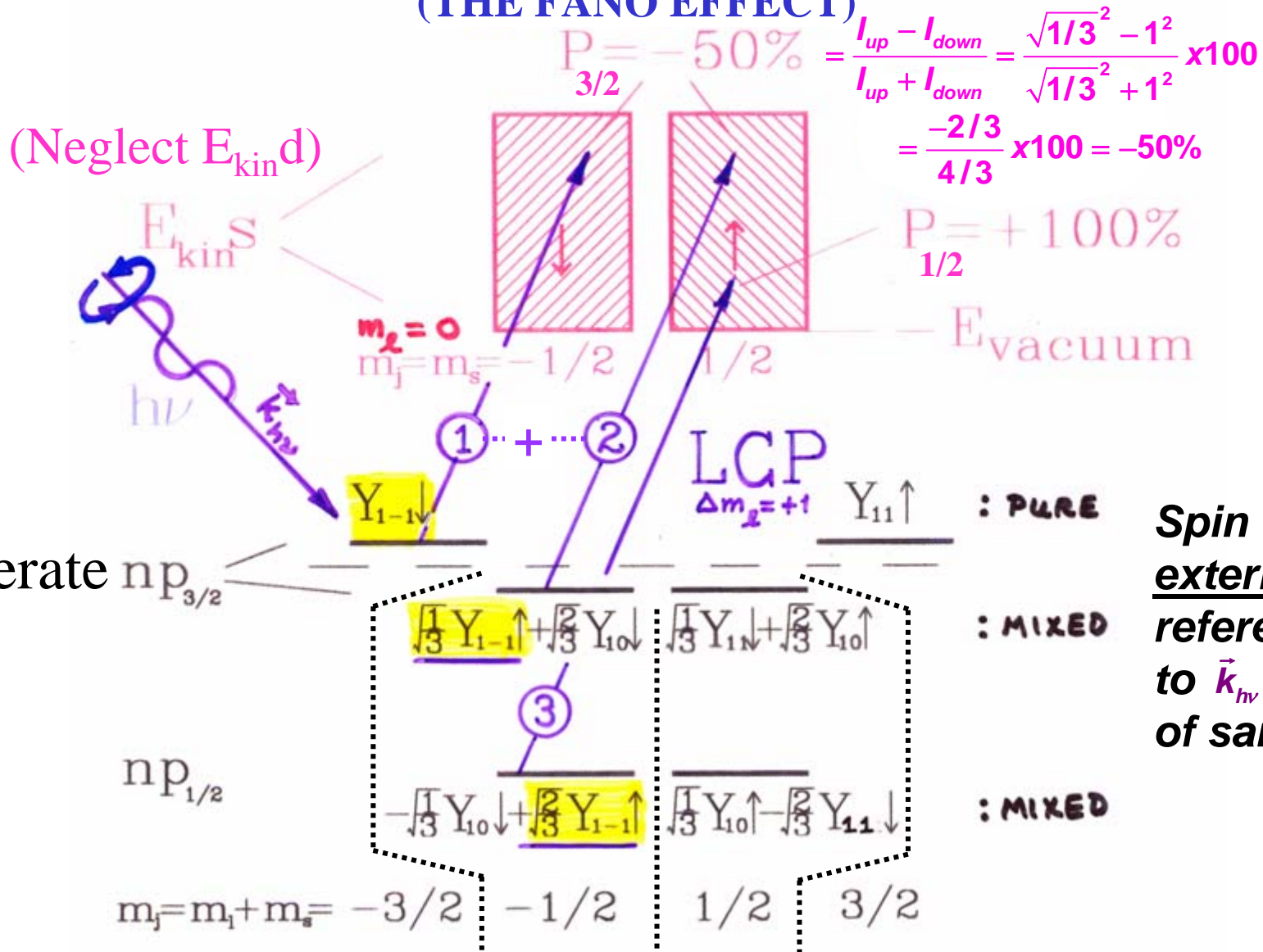
$$\psi_{nljm_j} = C_1 \psi_{nl, m_j - 1/2} \begin{pmatrix} 1 \\ 0 \end{pmatrix} + C_2 \psi_{nl, m_j + 1/2} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

\parallel
 $m_s = +1/2$
 \parallel
 \uparrow

\parallel
 $m_s = -1/2$
 \parallel
 \downarrow

WITH C1 AND C2 TABULATED CLEBSCH-GORDAN OR WIGNER 3j SYMBOLS

PHOTOELECTRON SPIN POLARIZATION FROM CIRCULAR POLARIZATION AND SPIN-ORBIT SPLITTING (THE FANO EFFECT)



**Spin
externally
referenced
to \vec{k}_{hv} and \vec{M}
of sample**

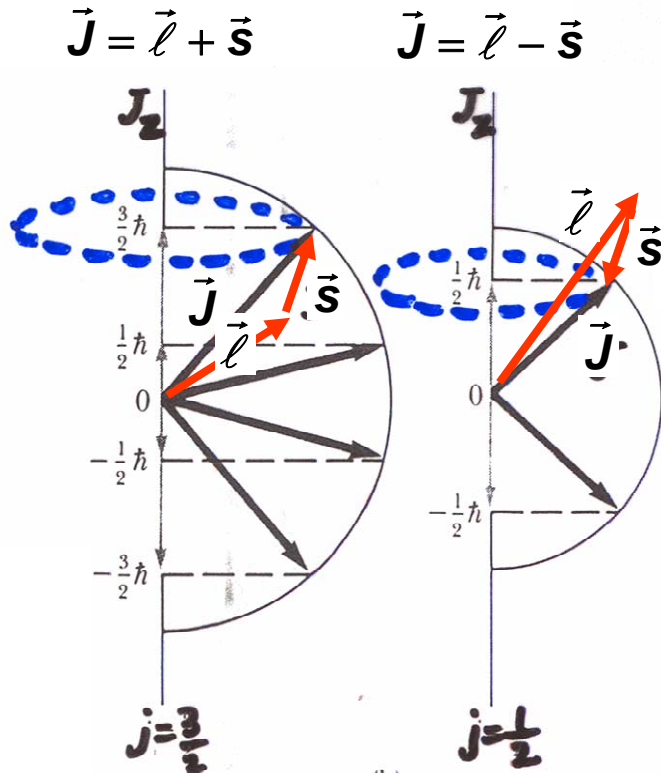
Spin polarization in core photoelectron spectra—expt.



Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
 - Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
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- Various other final state effects providing information in core-level spectra

MCD IN 2p EMISSION - 1-e⁻ THEORY

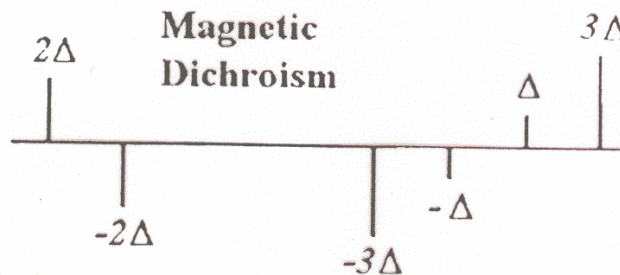
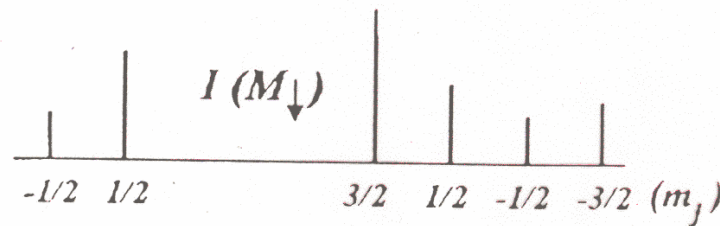
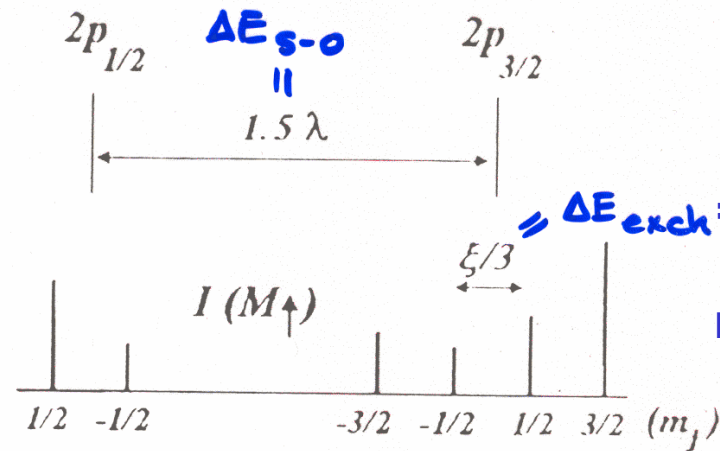


$$|\vec{J}| = \hbar \sqrt{j(j+1)}$$

WITH: $j = \begin{cases} l - 1/2 \\ l + 1/2 \end{cases}$

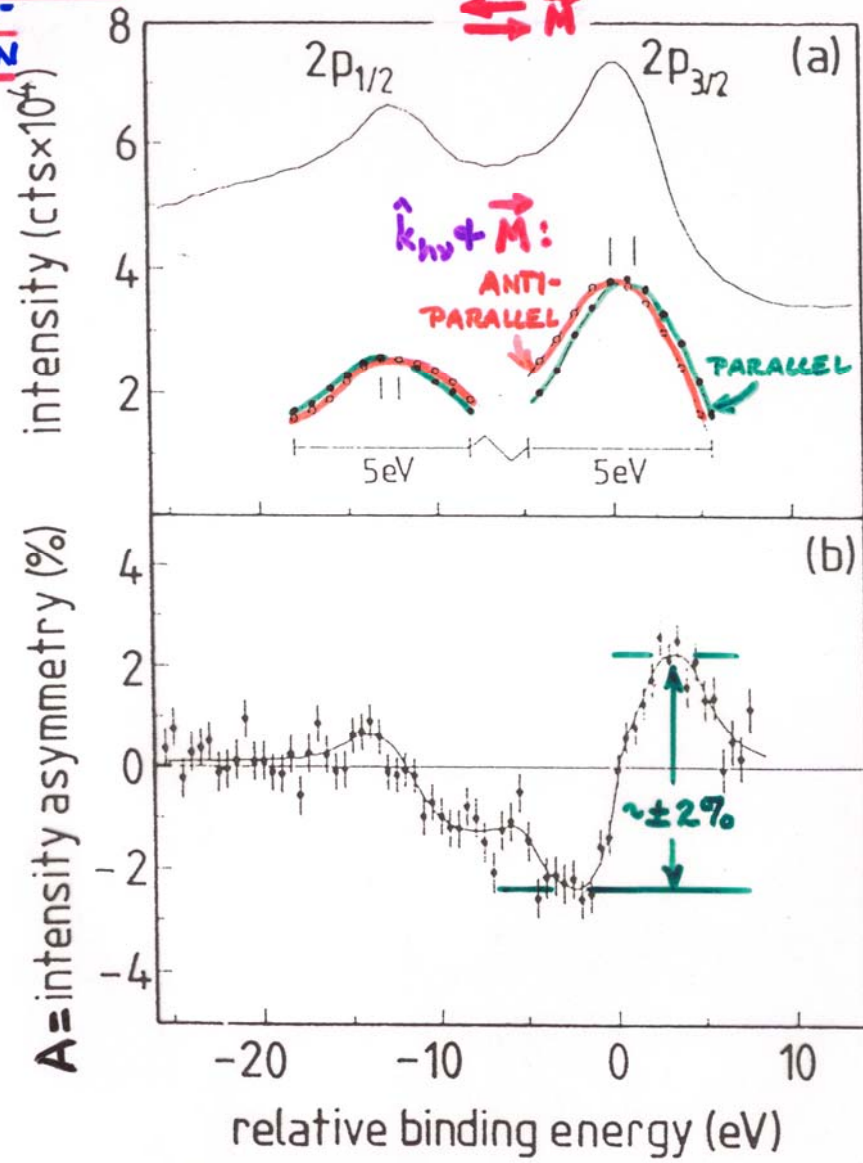
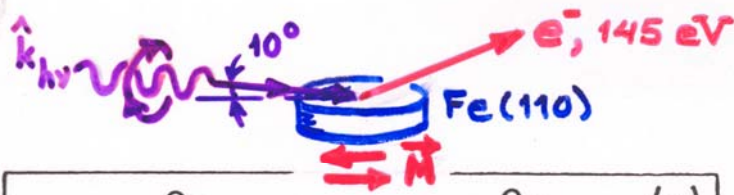
$$J_z = \hbar m_j$$

WITH: $m_j = -j, -j+1, \dots, +j$



MENCKERO,
 P.R. 8 57,
 993 ('98)

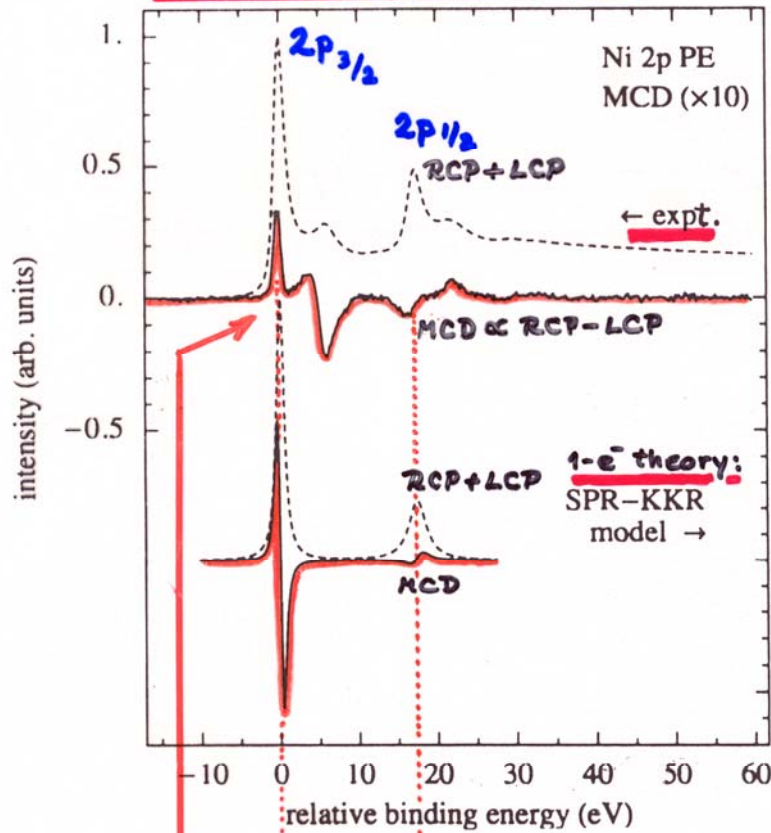
MAGNETIC CIRCULAR DICHROISM IN CORE-LEVEL PHOTOEMISSION



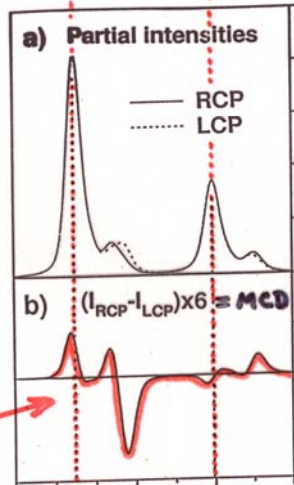
BAUM-GARTEN ET AL., P. R. L. 65, 492 (1990)

\Rightarrow DIFFRACTION EFFECTS WILL BE IMPORTANT HERE ALSO

MCD IN Ni2P EMISSION:



VAN DER LAAN
ET AL., J. PHYS.
COND. MATT.
12, 4275 (2000)

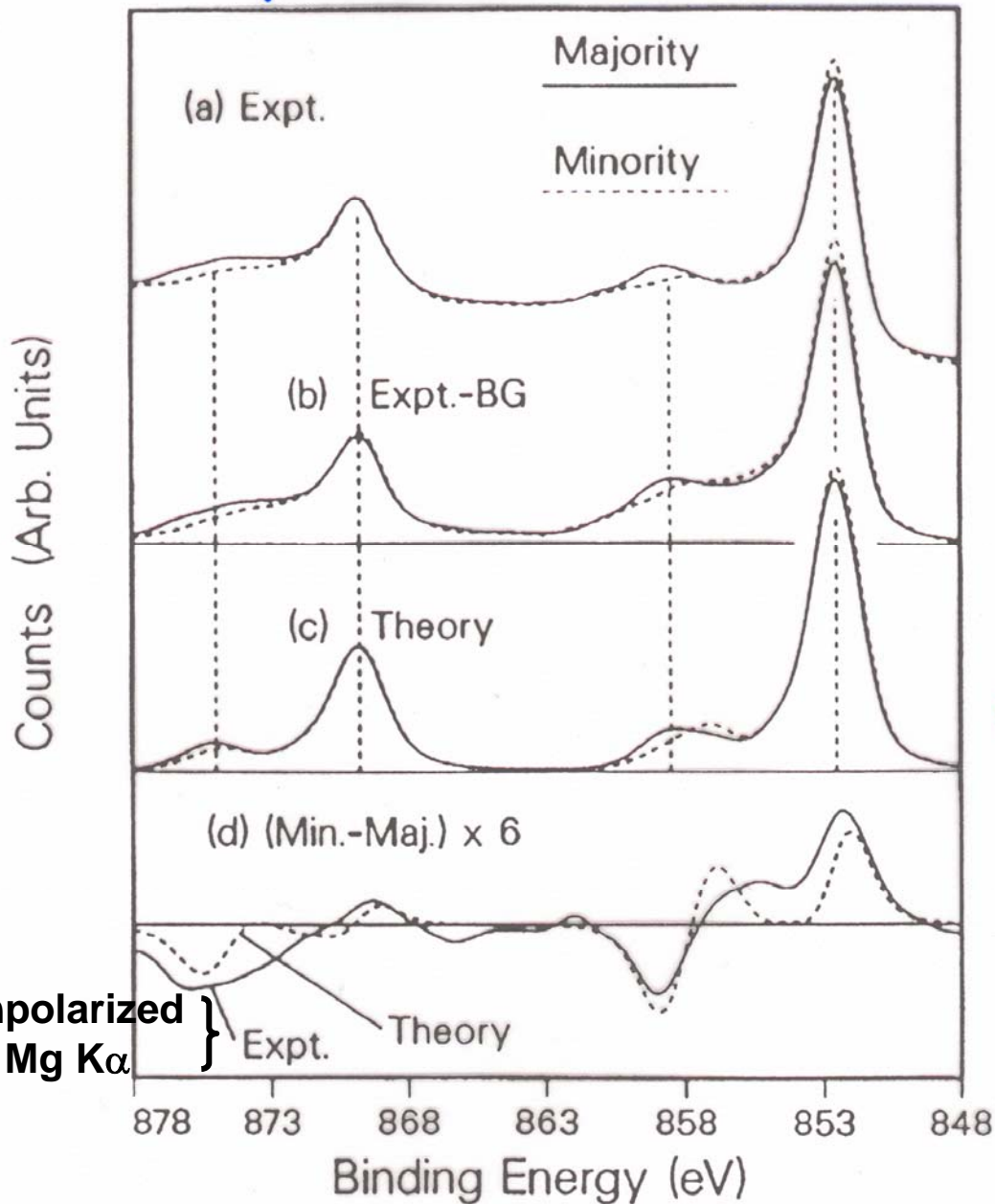


Many-e⁻ theory:
CI, screening

MENCHERO,
PRL 76, 3208 ('96)
PRB 57, 1001 ('98)

MANY- e^- THEORY

Ni2p - SPIN-RESOLVED SPECTRA



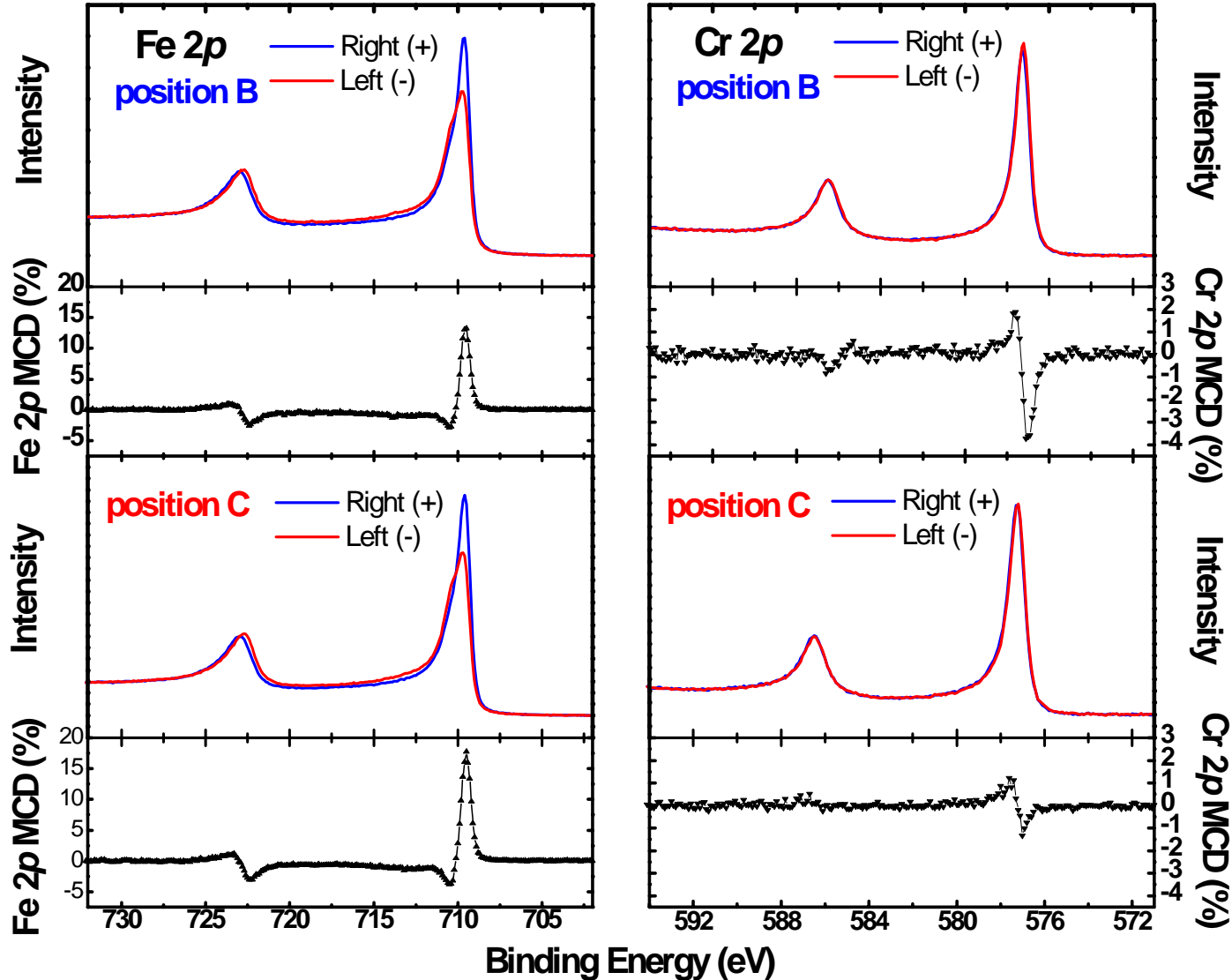
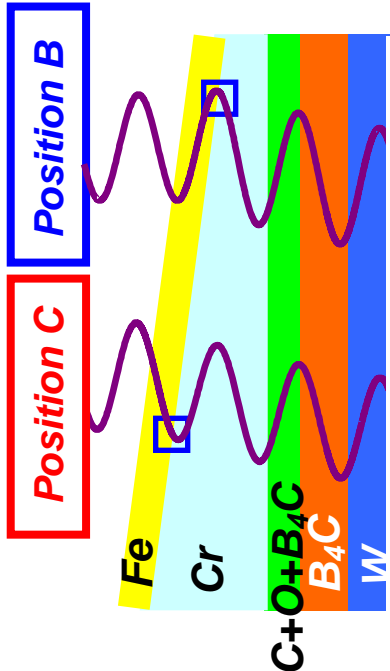
\Rightarrow FORM OF MCD APPROX. OF
 FORM OF SPIN POLARIZATION:
 MCD + POLARIZATION
 DIRECTLY LINKED

MENCHERO
 P.R.L. 76, 3208
 (196)

Application to a buried interface: with standing wave excitation

Fe & Cr 2p MCD Data from wedge (Fe/Cr)+SWG

Cr magnetization is antiparallel to Fe; systematic variation of MCD strengths vs d_{cr}

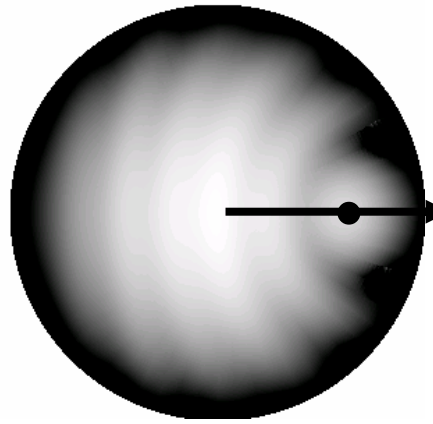
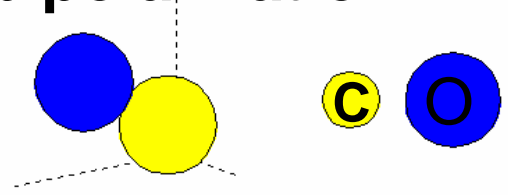


Outline

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- Core-level chemical shifts: the potential model
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- Various other final state effects providing information in core-level spectra

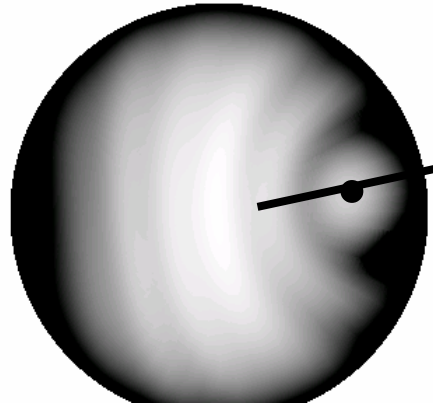
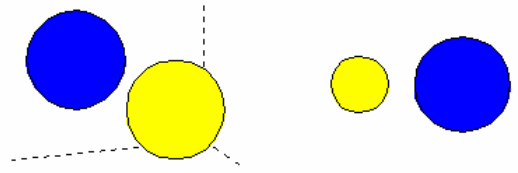
Circular dichroism in angular distributions: C 1s emission from CO, $E_{\text{kin}} = 200$ eV

Linear p polarization:



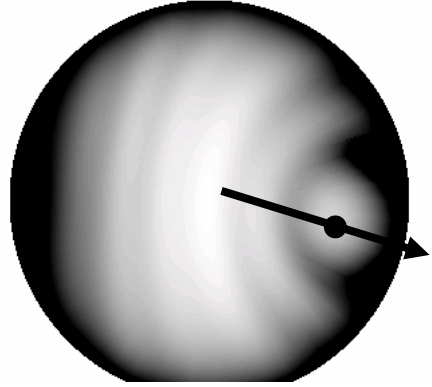
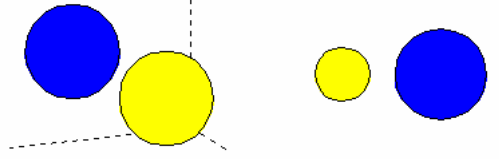
Oxygen forward scattering peak

Right circular polarization:



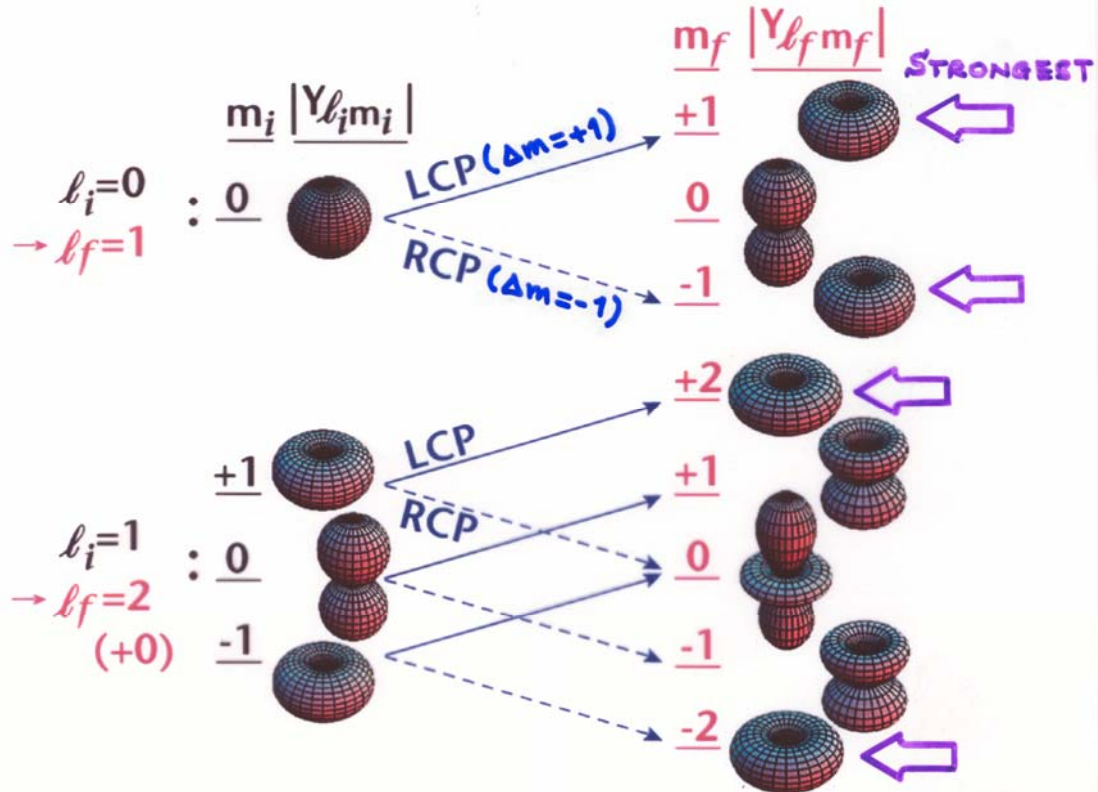
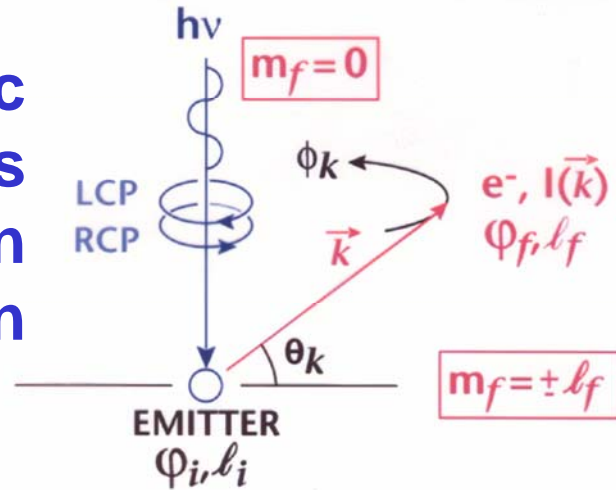
Circular dichroism!
Why?

Left circular polarization:



CIRCULAR DICHROISM IN PHOTOELECTRON ANGULAR DISTRIBUTIONS (CDAD)

Non-magnetic dichroism effects due to photoelectron diffraction

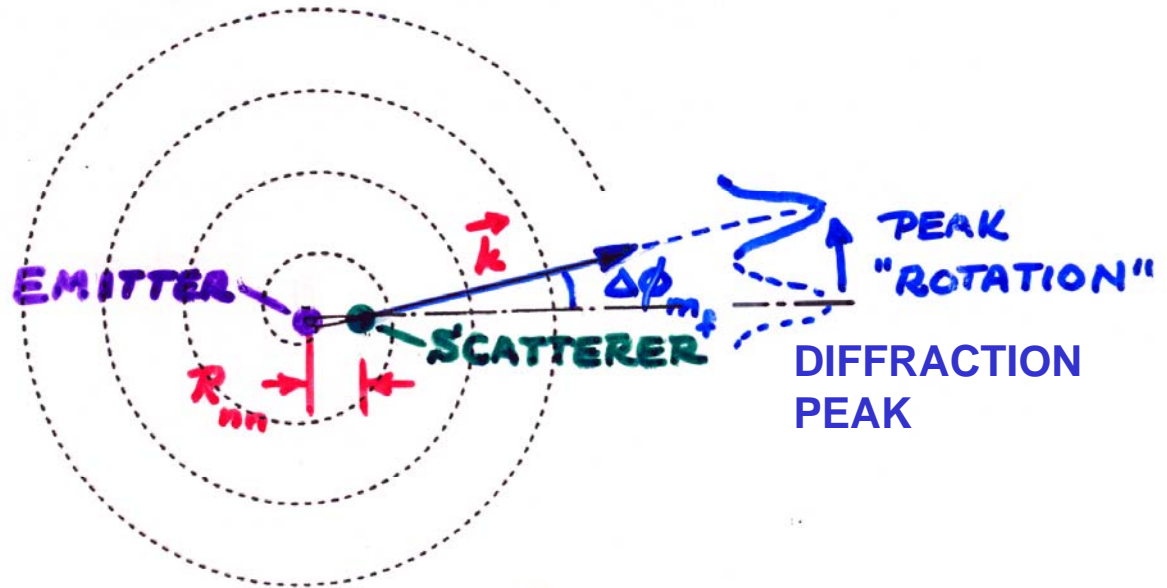


CIRCULAR DICHOISM IN PHOTOELECTRON DIFFRACTION

CONSTANT-PHASE SURFACES OF :

$$\psi_{\text{PHOTOE}}(r, \theta, \phi) \propto \frac{e^{ikr}}{r} \sum_{lm} e^{im_f \phi}$$

Z OUT
OF PLANE



$$\Delta\phi_{m_f} = \frac{m_f}{R_{nn, \parallel} k_{\parallel}}$$

$$\overline{m_f} \approx m_{f, \max}$$

DAIMON ET AL.
JPN. J. APPL. PHYS.
32, L1480 (1993)

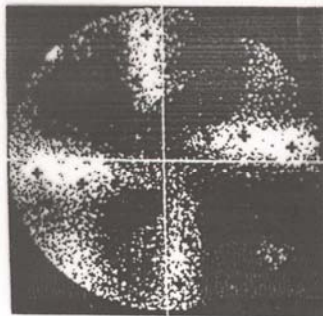
CIRCULAR DICHOISM - NON-MAGNETIC SYSTEMS

Si2p -- 250eV = E_{kin}

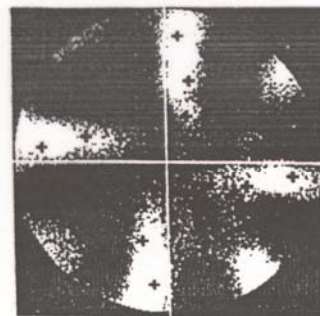
EXPERIMENT



(a) LCP



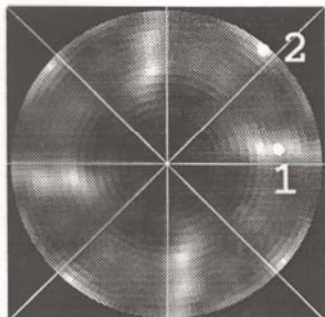
(b) RCP



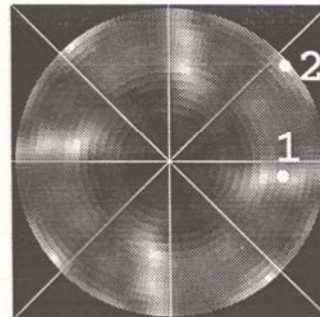
DAIMON ET AL.
JPN. J. APPL. PHYS.
32, L1480 ('93)

THEORY

(c) LCP



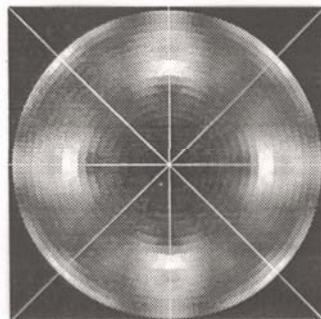
(d) RCP



ILADUWELA ET AL.
P. R. B 50, 6203 ('94)

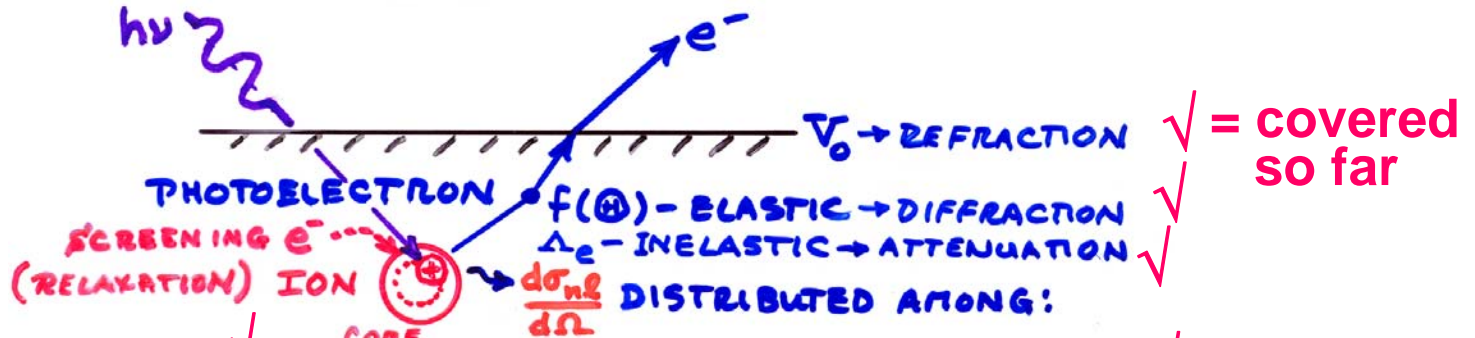


(e) UNPOLARIZED



Outline

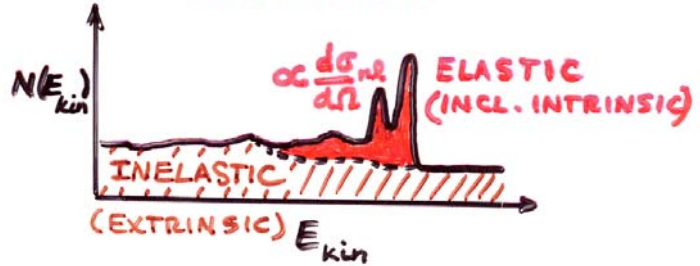
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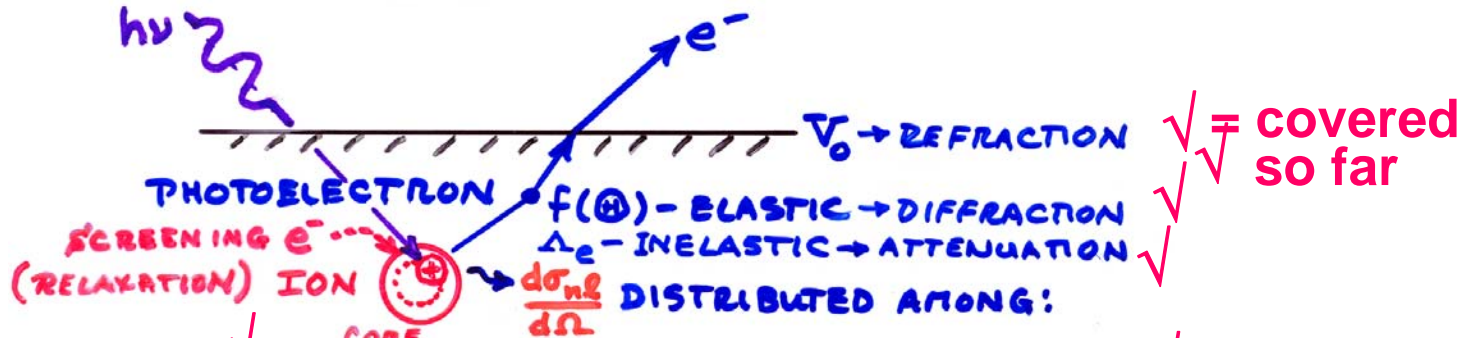


ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- SPIN-ORBIT SPLITTING (EASY) ✓
- + MULTIPLY SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD ✓
- + CORRELATION / CONFIGURATION INTERACTION ✓
- + SHAKE-UP / SHAKE-OFF / e⁻-HOLE ✓
- + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION ✓
- + VIBRATIONAL EXCITATIONS ✓
- + RESONANT PHOTOEMISSION (hv = E_{b, n l}) ✓

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



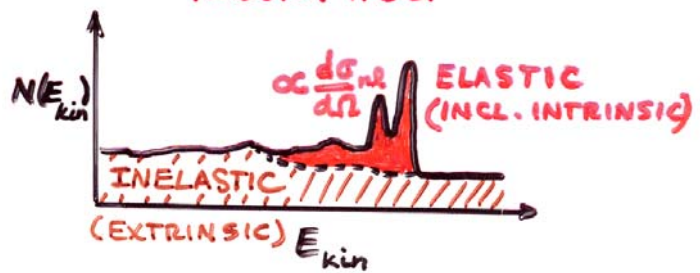


✓ = covered so far

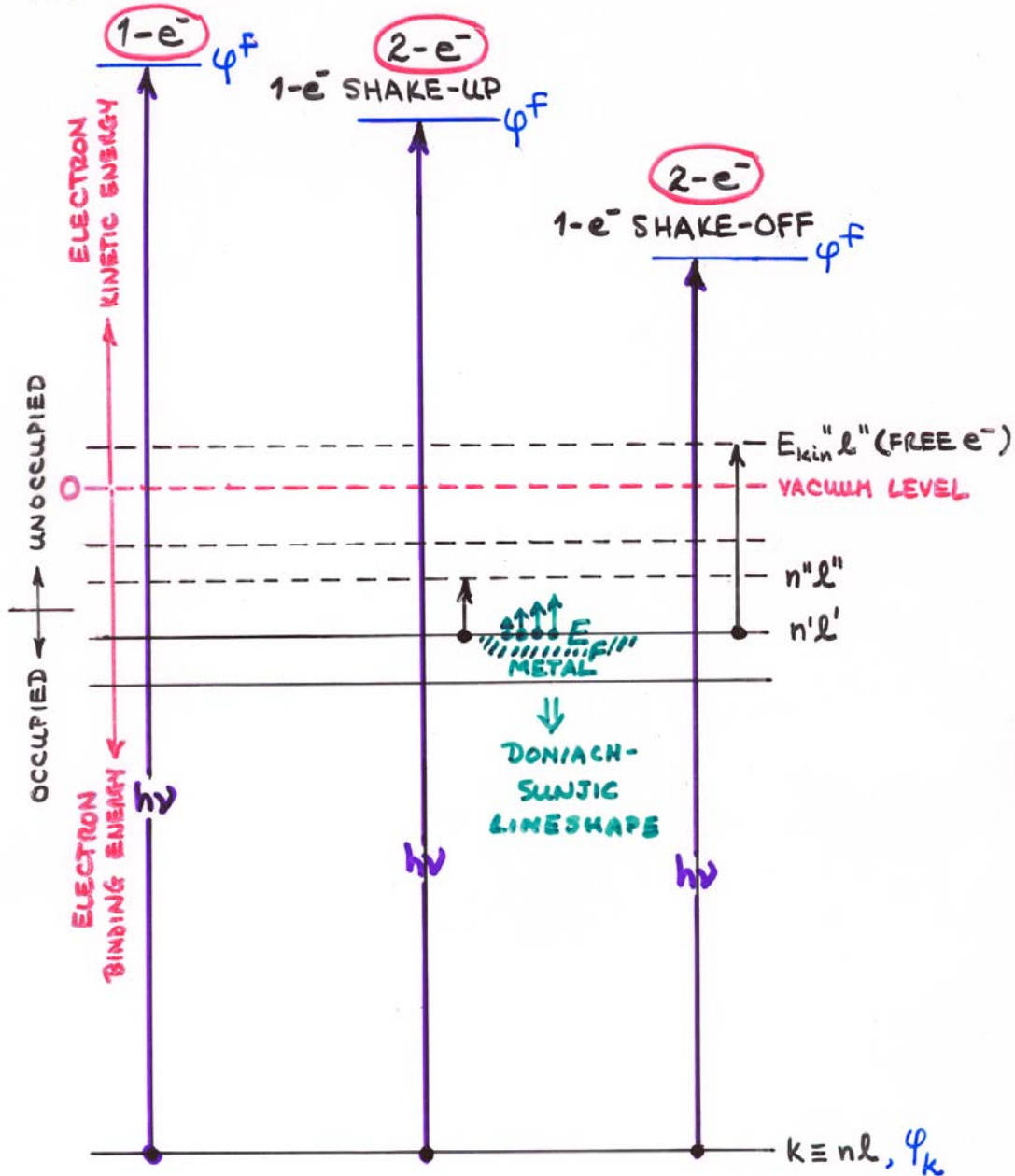
ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- ✓ SCREENING e^- (RELAXATION) ION
- ✓ CORE HOLE $k = n\ell$
- ✓ SPIN-ORBIT SPLITTING (EASY)
- ✓ + MULTIPLY SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD
- ✓ + CORRELATION / CONFIGURATION INTERACTION
- ✓ + SHAKE-UP / SHAKE-OFF / e^- -HOLE ←
- ✓ + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION
- ✓ + VIBRATIONAL EXCITATIONS
- ✓ + RESONANT PHOTOEMISSION ($h\nu \approx E_{b,n\ell}$)

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



TOTAL NO. e^- :



MULTIELECTRON EFFECTS IN CORE EMISSION

INTENSITIES IN PHOTOELECTRON SPECTRA:

- GENERAL: FINAL STATE K (k -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_i^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPPENHEIMER: e^- 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION: $\Psi_k \rightarrow \Psi_f = \text{PHOTO}^-$ (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 |\langle \Psi_e^f(N-1, K) | \Psi_R^i(N-1, K) \rangle|^2$$

$$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_k \rangle|^2 \quad \text{SAME SUBSHELL COUPLING + TOTAL L, S} \rightarrow \text{"MONOPOLE"}$$

↳ NORMAL $\frac{dG_K}{d\Omega}$

- SLATER DETS. FOR $\Psi_{e^-}^f = \det(\Psi_1^f, \Psi_2^f, \dots, \Psi_{k-1}^f, \Psi_{k+1}^f, \dots, \Psi_N^f)$

$$\Psi_R^i = \det(\Psi_1^i, \Psi_2^i, \dots, \Psi_{k-1}^i, \Psi_{k+1}^i, \dots, \Psi_N^i)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 |\langle \Psi_1^f | \Psi_1^i \rangle|^2 |\langle \Psi_2^f | \Psi_2^i \rangle|^2 \dots$$

$$|\langle \Psi_{k-1}^f | \Psi_{k-1}^i \rangle|^2 |\langle \Psi_{k+1}^f | \Psi_{k+1}^i \rangle|^2 \dots |\langle \Psi_N^f | \Psi_N^i \rangle|^2$$

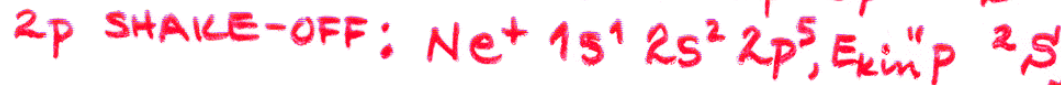
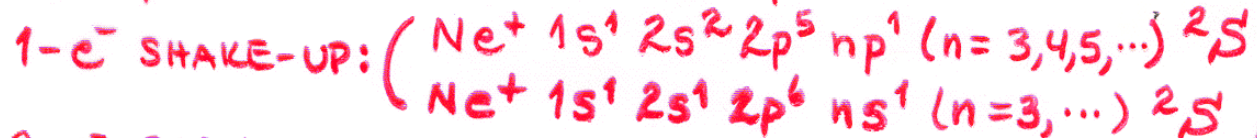
$$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_R \rangle|^2$$

1e- DIPOLE $\rightarrow d\sigma/d\Omega$

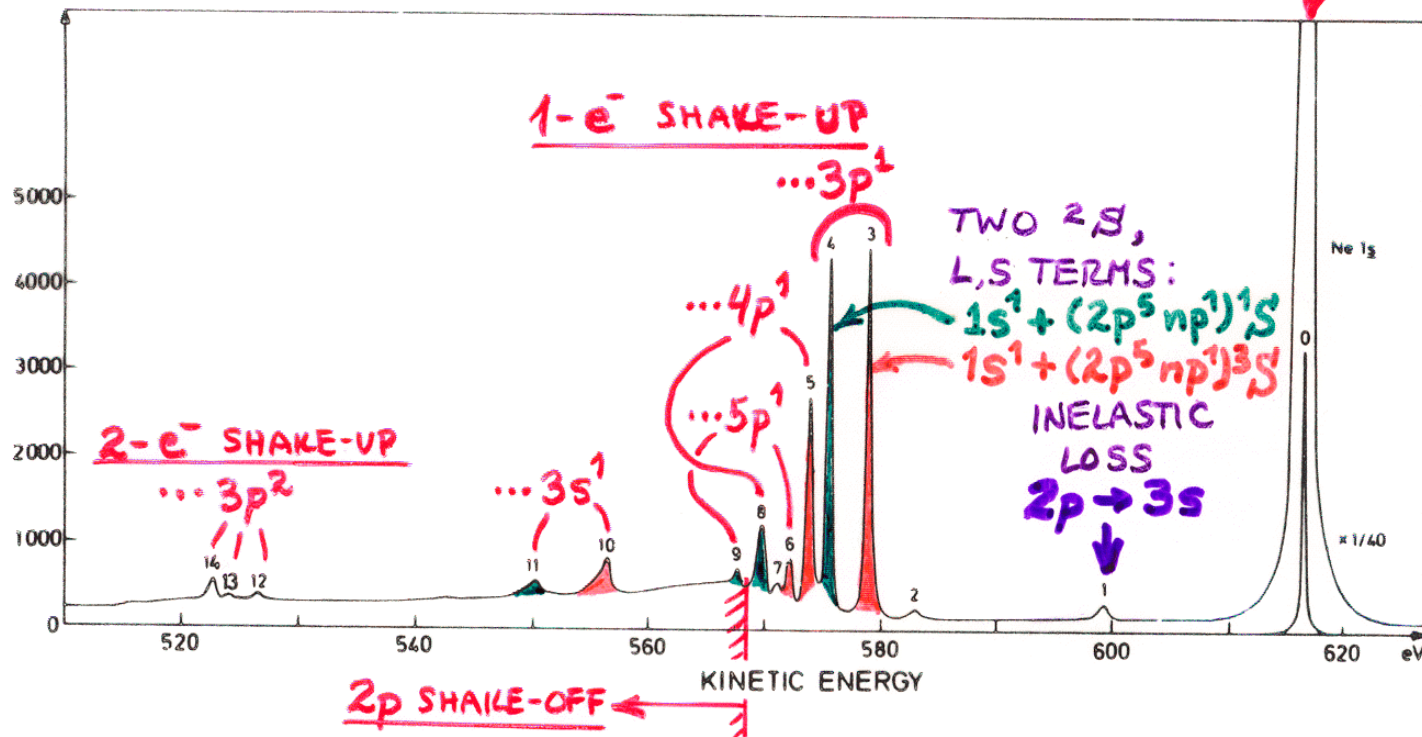
(N-1)e- SHAKE-UP/
SHAKE-OFF \rightarrow
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN Ψ_f ESCAPE

NEON 1S SHAKE-UP/SHAKE-OFF:



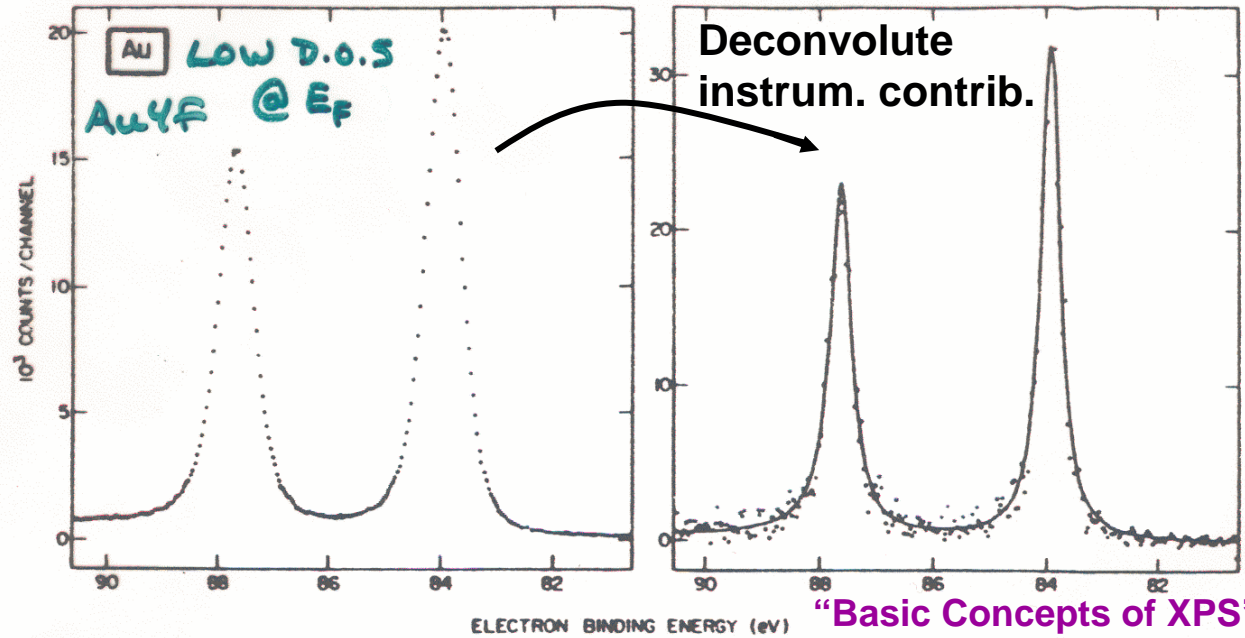
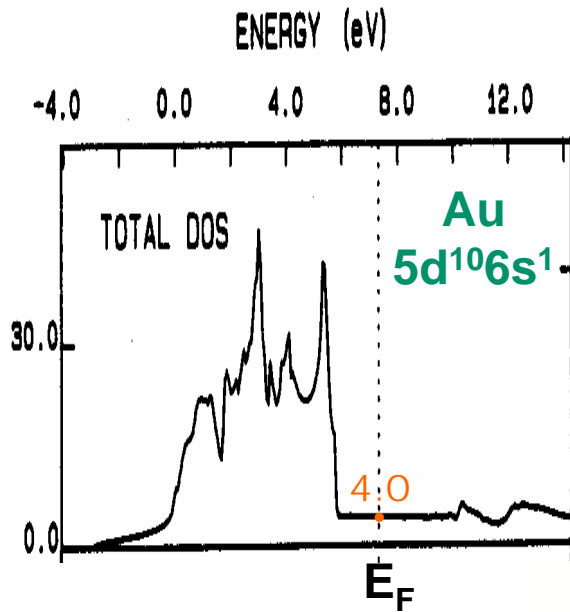
“Basic Concepts of XPS”
Figure 36



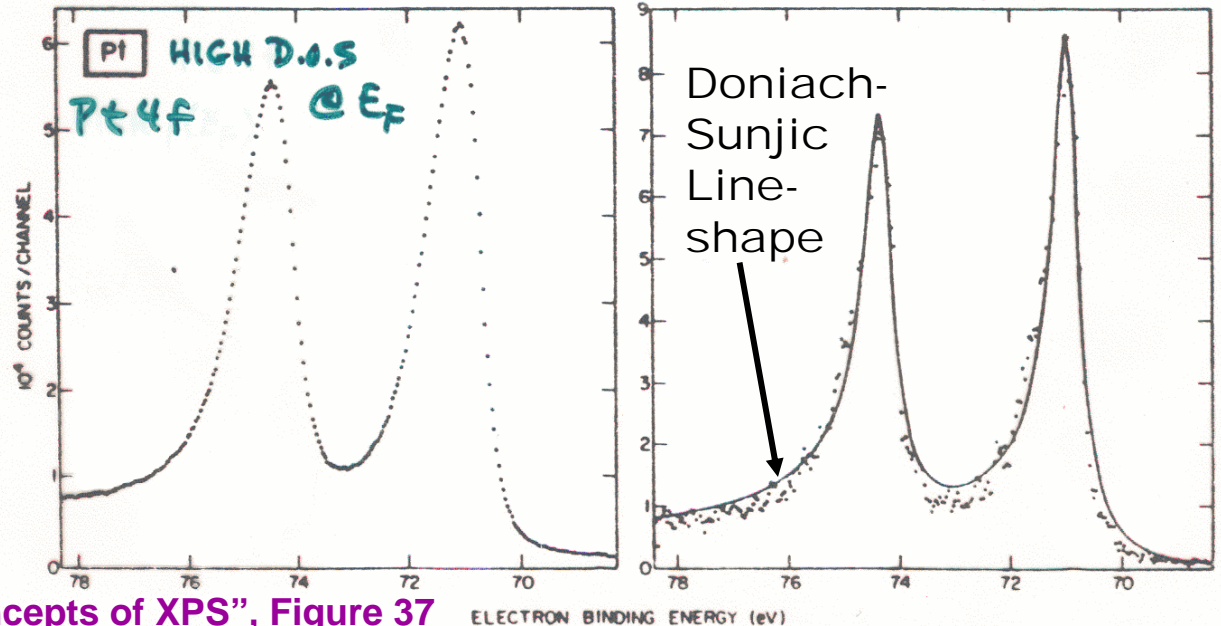
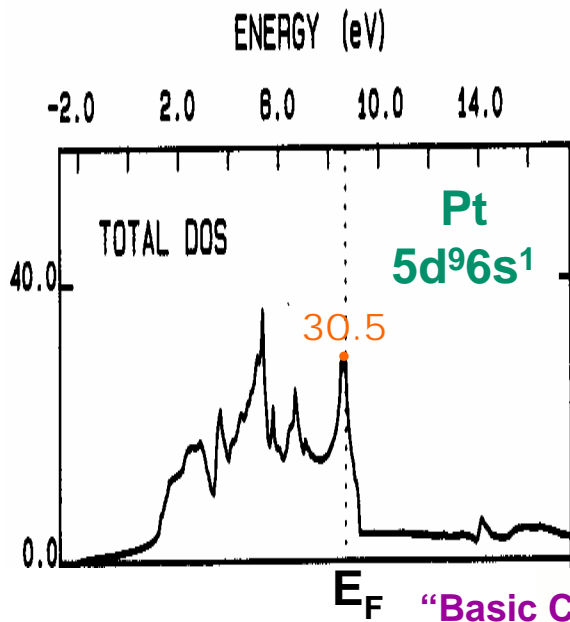
OVERALL: ~12% SHAKE-UP + 16% SHAKE-OFF \approx 28% OF EVENTS

BAND THEORY—D.O.S:

ELECTRON-HOLE EXCITATIONS IN METALS:



“Basic Concepts of XPS”
Figure 10



“Basic Concepts of XPS”, Figure 37

TWO SUDDEN-APPROXIMATION

SUM RULES:

①

{ AVERAGE BINDING ENERGY }

$$= \frac{\sum_{j=1}^{\text{ALL}} I_j E_b^V(k)_j}{\sum_{j=1}^{\text{ALL}} I_j}$$

KOOPMANS'

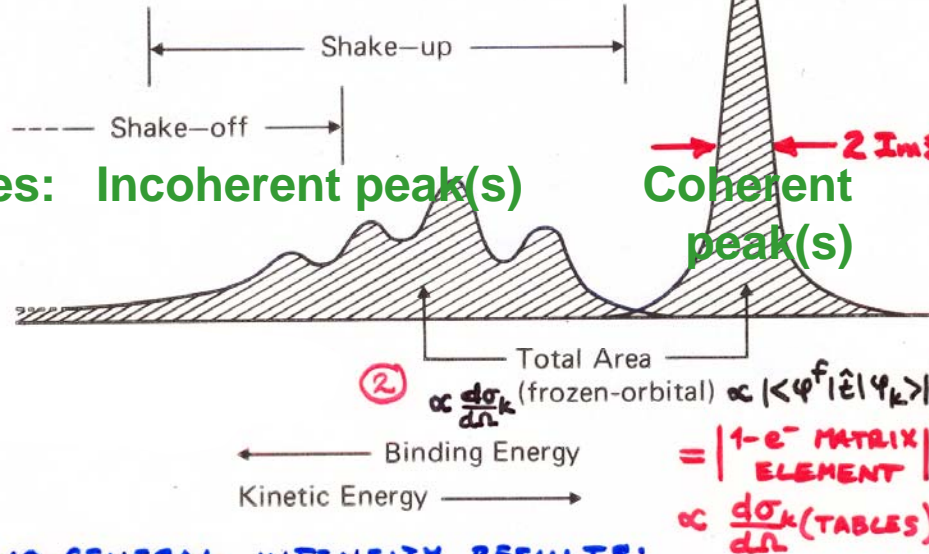
$$= -\epsilon_k$$

Ground-State of Ion = Adiabatic peak

$$E_b^V(k)_1$$

$$\approx \delta E_{\text{relax}} = \text{Re} \Sigma$$

$\Sigma = \text{many-body "self energy"} = \text{Re} \Sigma + i \text{Im} \Sigma$



In valence-band studies: Incoherent peak(s)

Coherent peak(s)

$$\Delta E \tau_{\text{lifetime}} \approx \hbar/2$$

TWO GENERAL INTENSITY RESULTS:

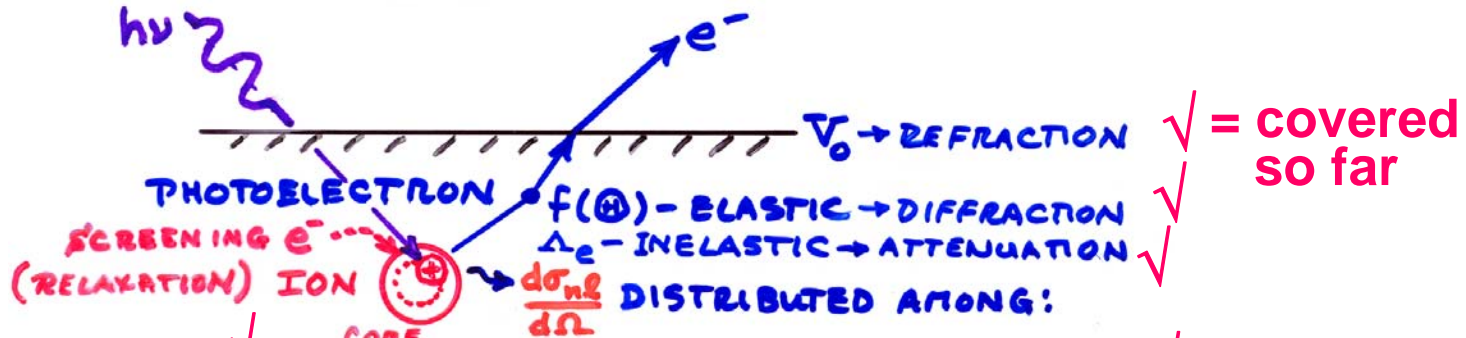
①

$$I_j \propto |\langle \varphi^f(i) | \hat{\epsilon} | \varphi_k(i) \rangle|^2 |\langle \Psi^f(N-1, j) | \Psi_R(N-1) \rangle|^2$$

$k e^- \text{ MISSING}$

Figure 8 -- Schematic illustration of a photoelectron spectrum involving shake-up and shake-off satellites. The weighted average of all binding energies yields the Koopmans' Theorem binding energy $-\epsilon_k$ (sum rule (77)), and the sum of all intensities is proportional to a frozen-orbital cross section σ_k (sum rule (78)). The adiabatic peak corresponds to formation of the ground-state of the ion ($E_b(k)_1 \equiv E_b(K=1)$).

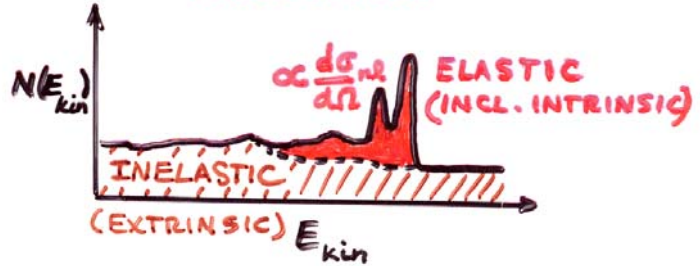
$$\textcircled{2} \text{ (TOTAL SHAKE-UP + SHAKE-OFF) } = 1 - |\langle \Psi^f(N-1, 1) | \Psi_R(N-1) \rangle|^2 \approx 15-25\% \text{ FOR ATOMS/MOLEC.}$$



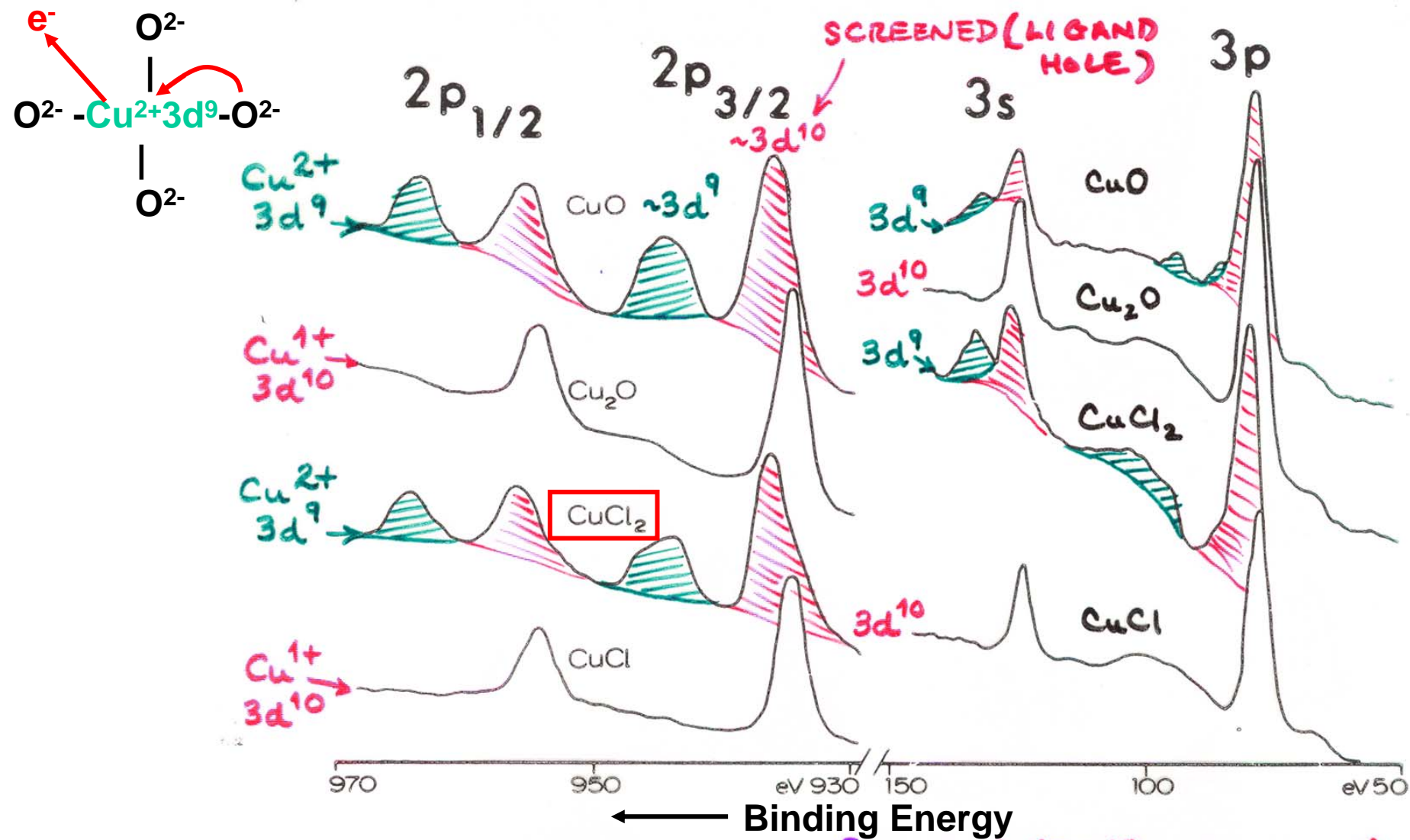
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- + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION ←
- + VIBRATIONAL EXCITATIONS ✓
- + RESONANT PHOTOEMISSION (hv = E_{b, n, l}) ✓

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



SATELLITES & CHARGE-TRANSFER SCREENING



ACTUAL FINAL STATE $\Psi \approx C_1 \phi_1 (3d^{10} - \text{SCREENED}) + C_2 \phi_2 (3d^9 - \text{UNSCREENED})$

“Basic Concepts of XPS”
Figure 38

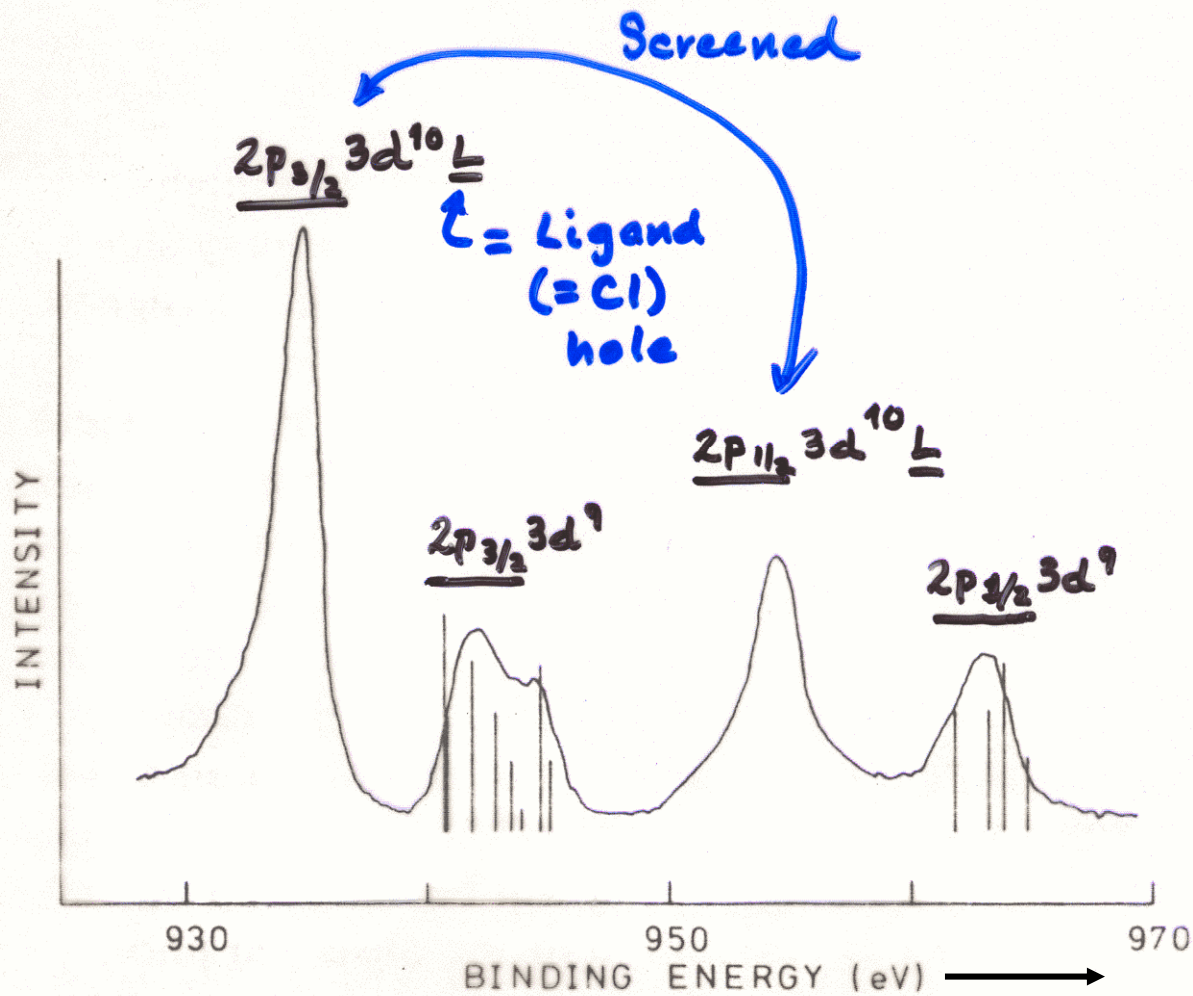


FIG. 2. The Cu 2p spectrum of CuCl₂ together with the expected multiplet splittings, represented by bars, for the $2p 3d^9$ level as calculated and discussed in the text.

VAN DE LAAN
 ET AL., PHYS.
 REV. B 23, 4369
 (1981)

Screening depends on ionicity/covalency → satellite intensities can be used to measure interaction parameters

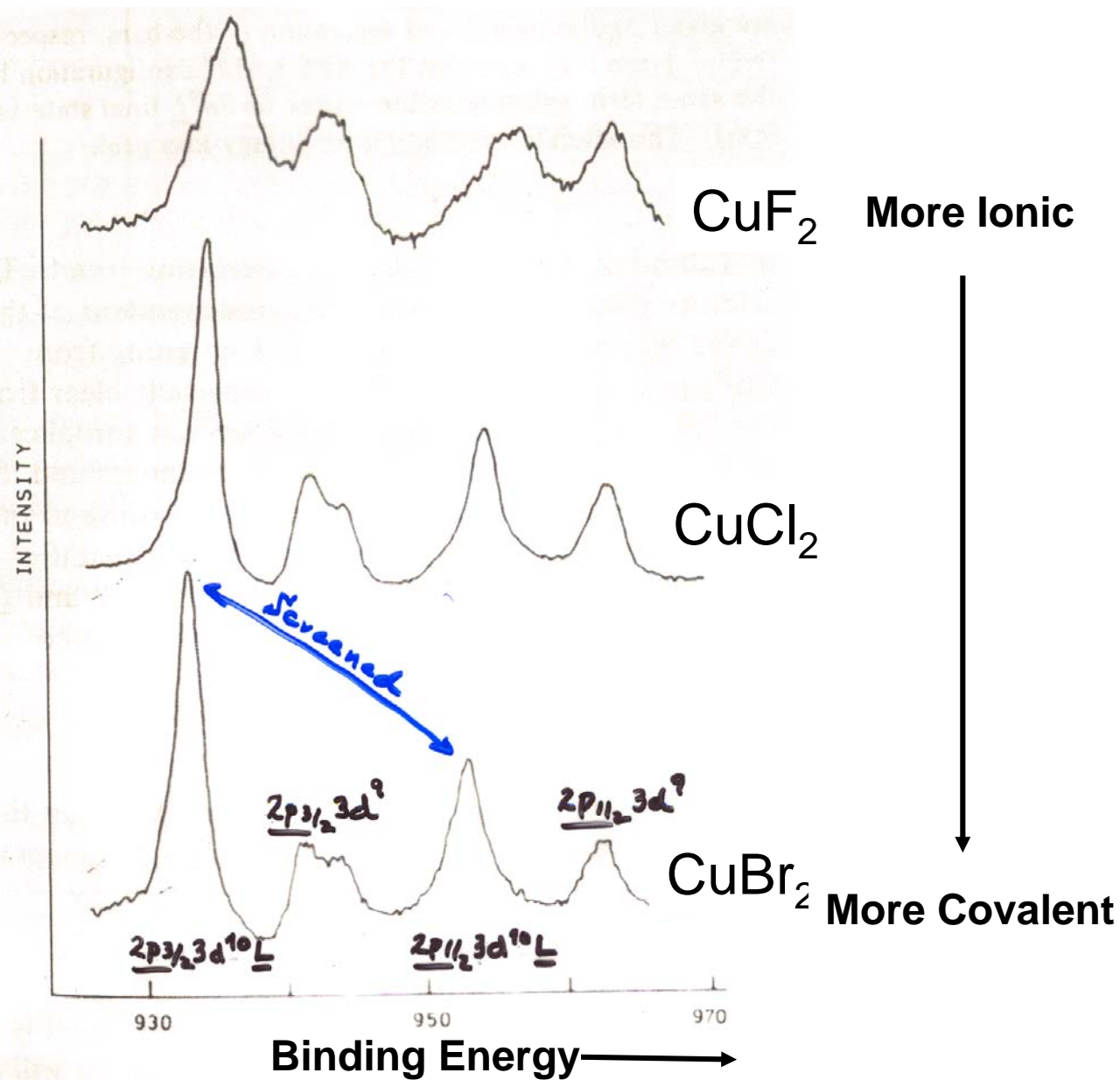


FIG. 1. Cu 2p photoelectron spectra of Cu dihalides. The lines leading to a final state with a ligand hole (\underline{L}) show a chemical shift.

Screening depends on Ionicity/covalency → satellite intensities can be used to measure interaction parameters

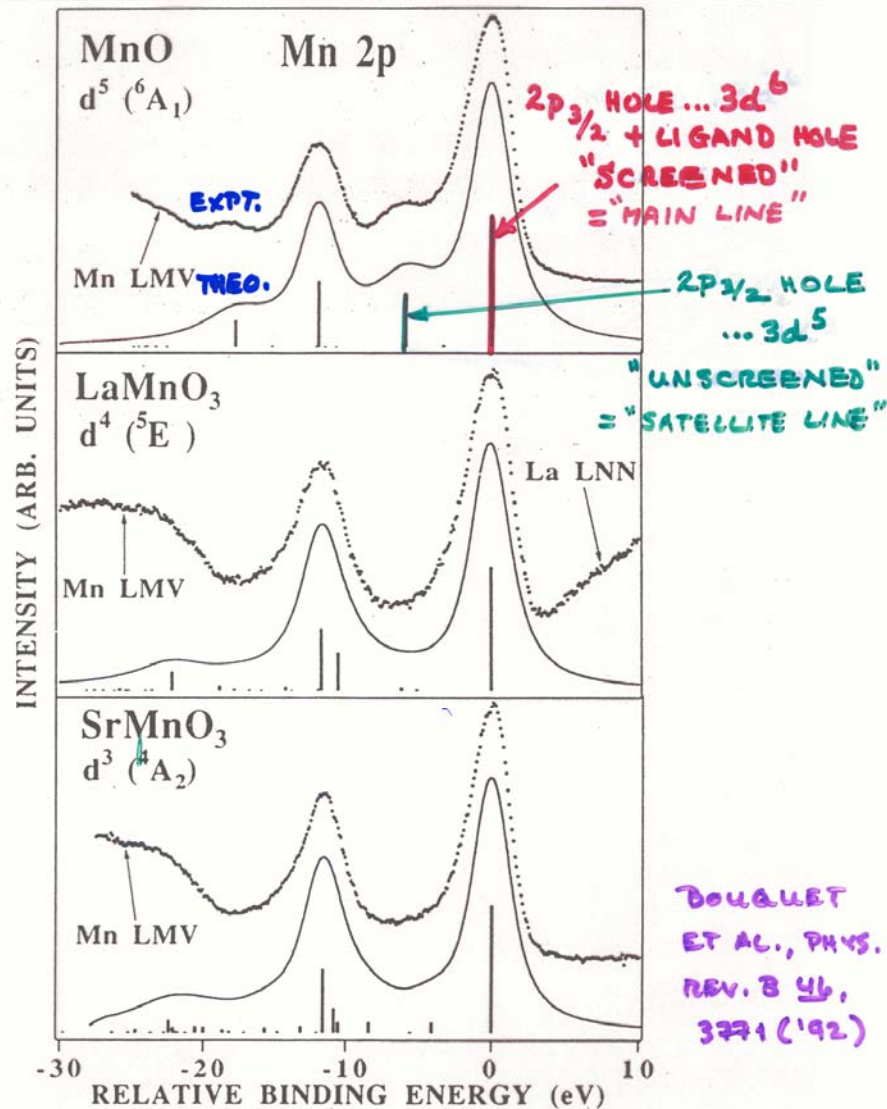
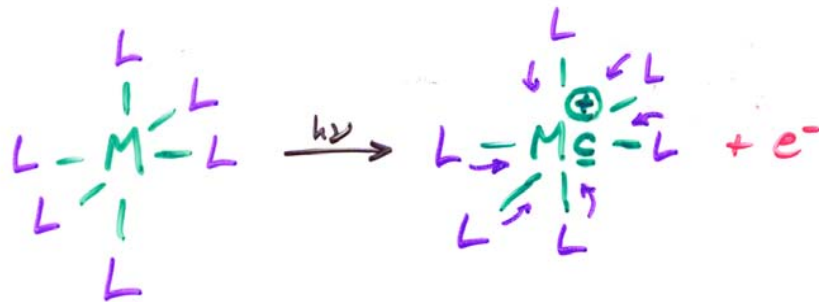


FIG. 1. Theoretical $2p$ core-level XPS spectra (solid line) compared with experimental data (dots) after background subtraction for Mn cations with varying valence. Emission due to the Mn LMV Auger peak is observed on the high-binding-energy side of the $2p_{1/2}$ spin-orbit peak, partially obscuring the $2p_{1/2}$ satellite structure.

CONFIGURATION INTERACTION APPROACH TO SCREENING IN TRANSITION-METAL (RARE-EARTH) COMPOUNDS:

(SUGANO, LARSSON → SAWATZKY, VANDER LAAN, FUJIMORI, OH, ET AL.)



c = CORE HOLE ON METAL

l = VALENCE (?) HOLE ON LIGAND

$$\psi_i = a_0 |d^n\rangle + \sum_m a_m |d^{(n+m)} \underline{l}^m\rangle$$

$$\psi_f = b_0 |c d^n\rangle + \sum_m b_m |c d^{(n+m)} \underline{l}^m\rangle$$

WITH INTERACTIONS OF:

$10Dq$ = CRYSTAL FIELD (OFTEN NEGLECTED)

Δ = LIGAND-TO-METAL CHARGE TRANSF. ENERGY
 $= E(d^{n+1} \underline{l}) - E(d^n)$

U = d-d COULOMB REPULSION ENERGY
 $= E(d^{n-1}) + E(d^{n+1}) - 2E(d^n)$

T = LIGAND p-TO-METAL d HYBRIDIZATION
 $= \langle d_\alpha | \hat{H} | p_\alpha \rangle$ (α = SAME SYMMETRY)

Q = CORE-HOLE-TO-d INTERACTION: $\langle c | \hat{H} | d \rangle \approx J_{cd}$

WITH INTENSITIES FROM SUDDEN APPROX.

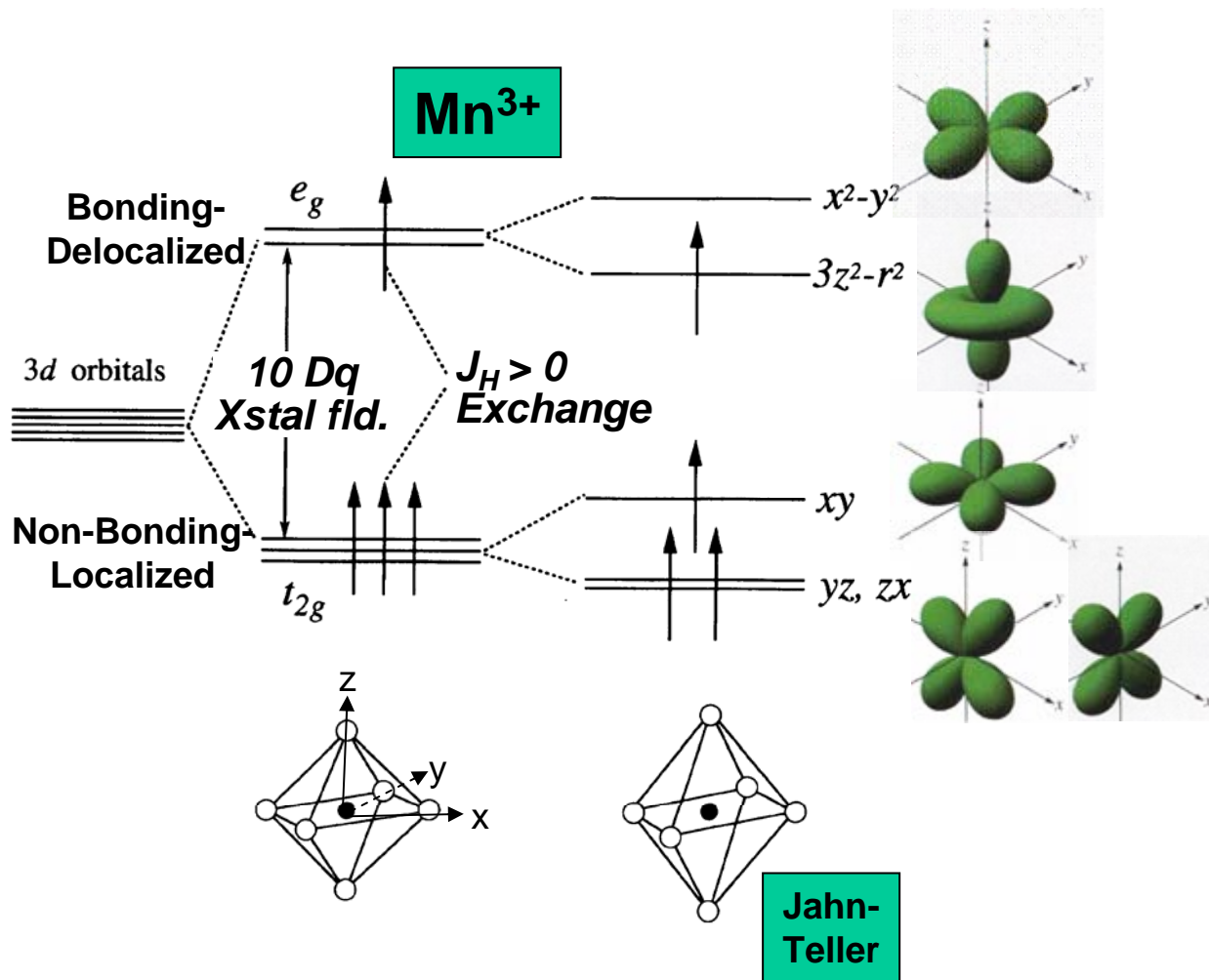
AS:

$$I(E_{kin}) \propto \sum_{f,k} |\langle \psi_f(N-1, k) | \psi_i(N-1, k) \rangle|^2 \delta(h\nu - E_f - E_{kin})$$

\downarrow = c = CORE HOLE

WHERE: $\psi_f(N-1, k) = \psi_i(N \text{ WITH } k \text{ HOLE} = \underline{l})$

E.g.—Crystal field in Mn^{3+} with negative octahedral ligands



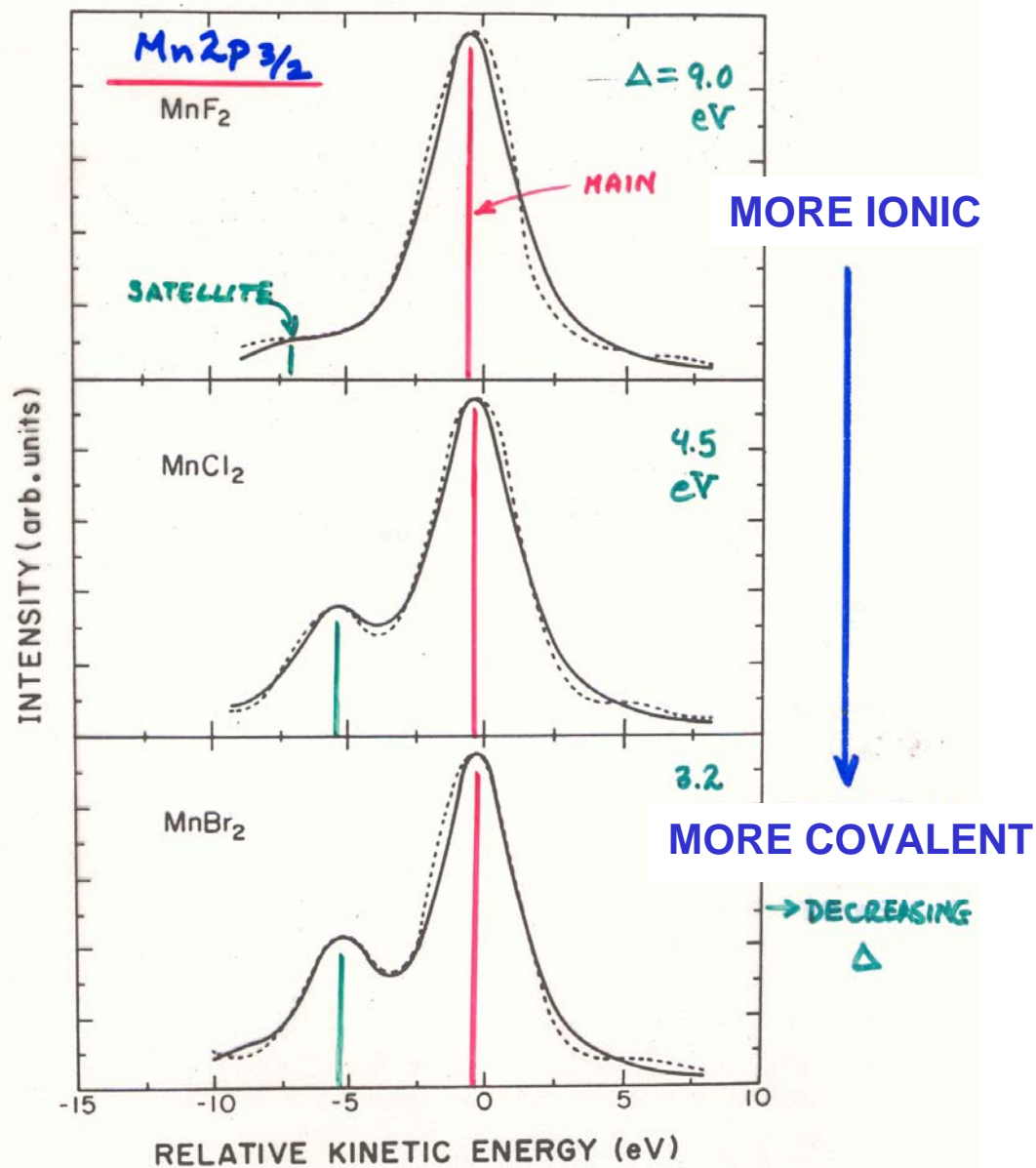
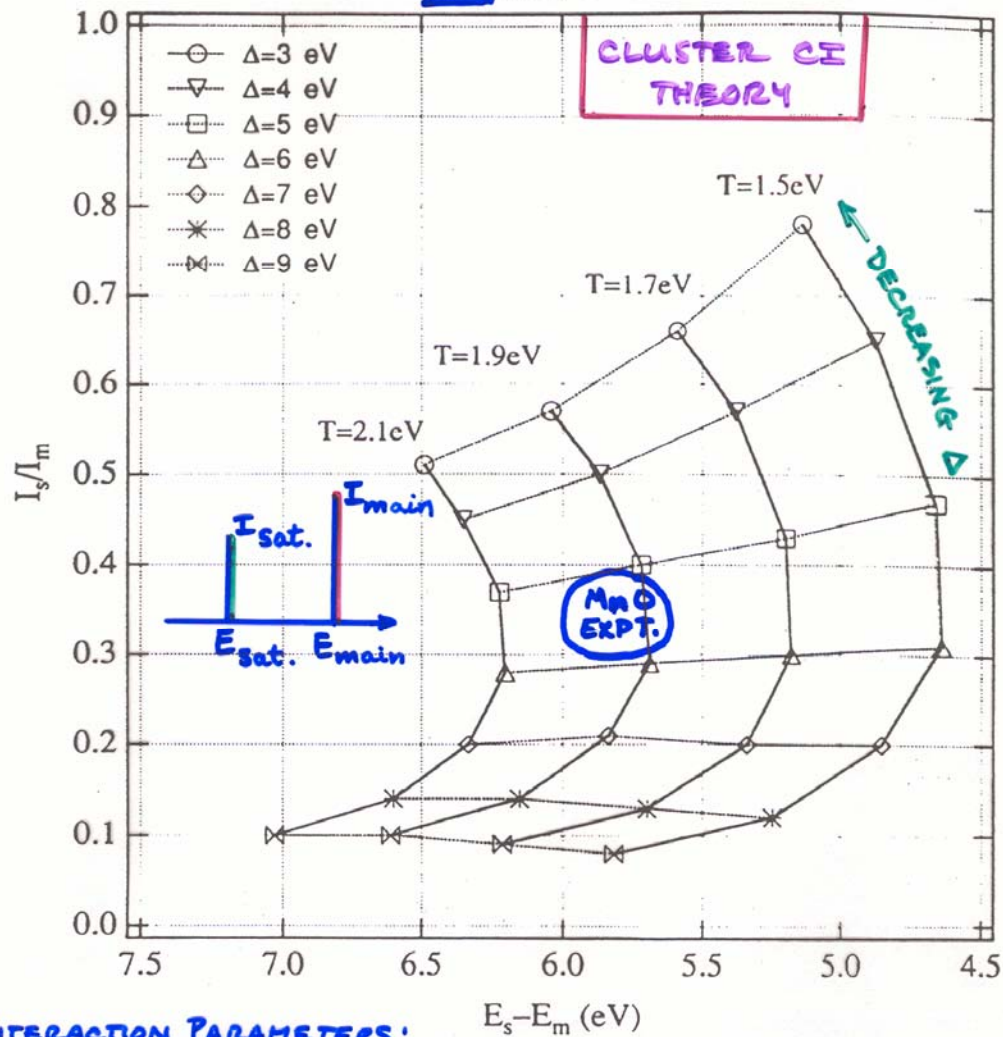


FIG. 6. Fits of the cluster model results with the experimental $2p_{3/2}$ spectra of the manganese dihalides. The parameters used are listed in Table II. A Lorentzian broadening is 2.6–3.0 eV, and a Gaussian broadening of 1.2 eV (FWHM) was used.

ANALYSIS VIA ANDERSON IMPURITY MODEL

$\text{Mn}^{2+}(\text{HS})$ $U=6.0$ eV



INTERACTION PARAMETERS:

$U = 3d-3d$ COULOMB REPULSION ENERGY

$\Delta =$ LIGAND-TO-METAL CHARGE TRANSFER ENERGY

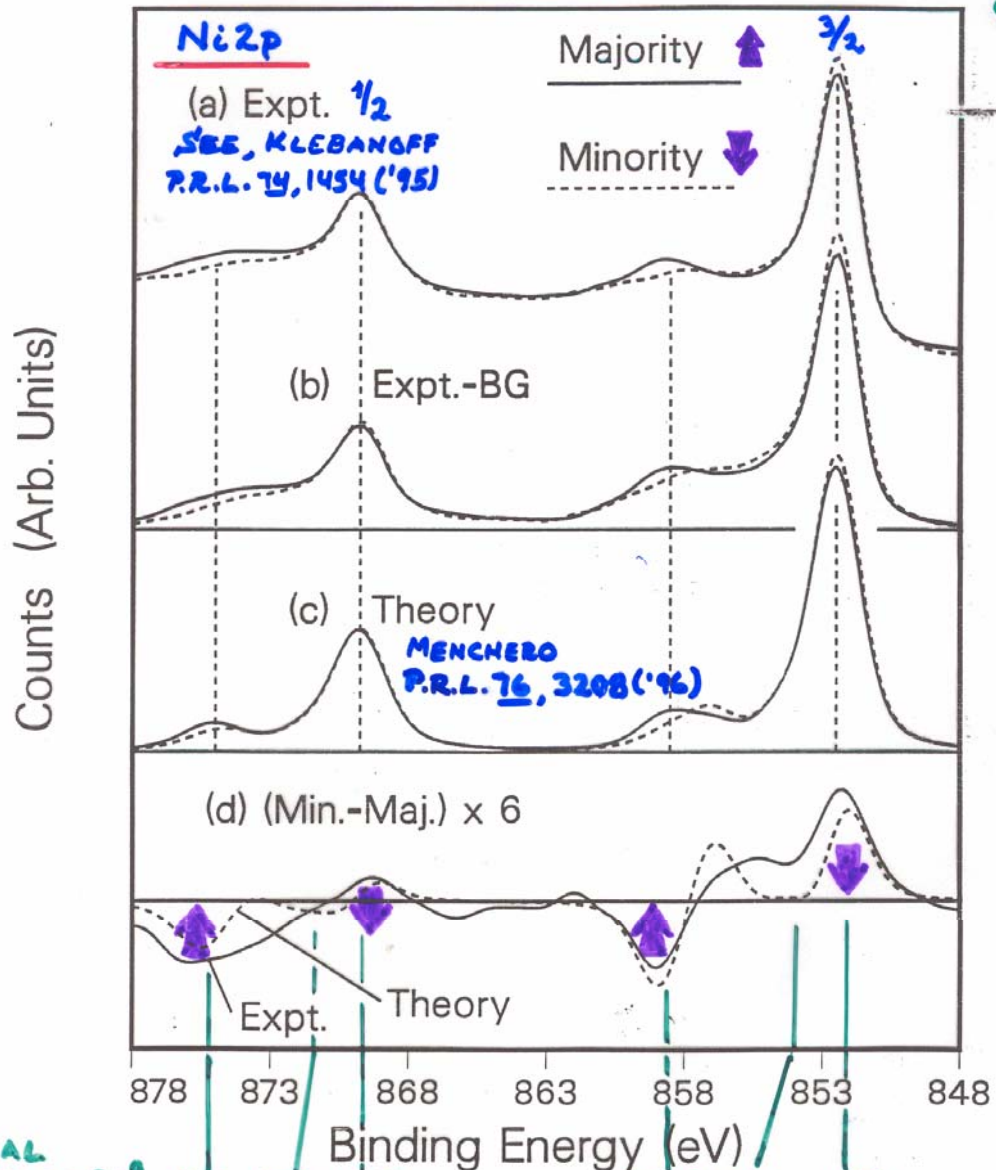
$T =$ LIGAND $p -$ METAL $3d$ HYBRIDIZATION ENERGY

$Q =$ CORE HOLE- $3d$ COULOMB

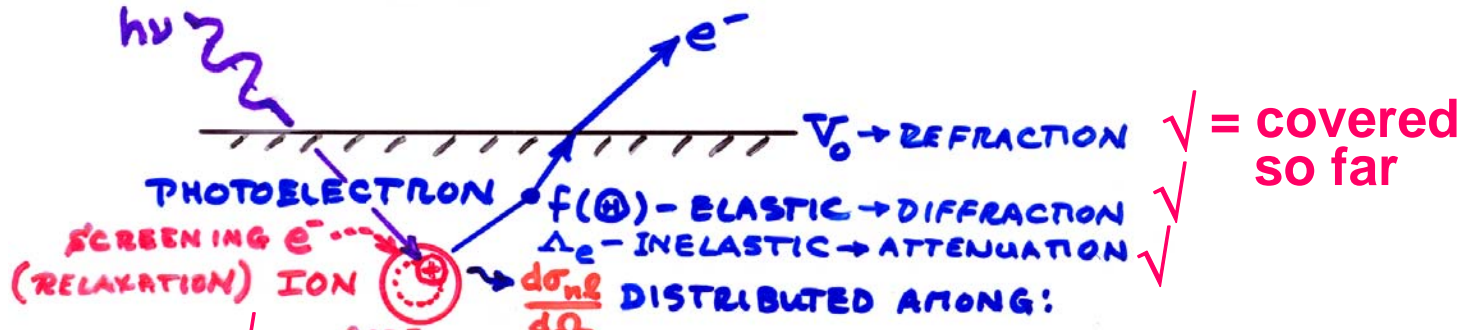
BOUQUET ET AL.,
J. EL. SP. 82, 87 (196)

SPIN-ORBIT SPLITTING + MULTIPLETS + SCREENING IN A METAL: Ni

~15% $3d^8$
43% $3d^9$
42% $3d^{10}$

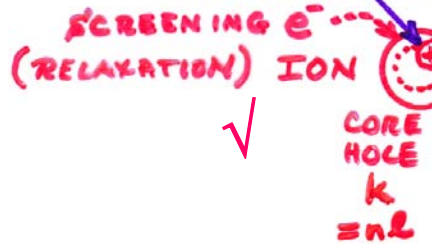


FINAL CONFIG.: $3d^9$ 65% 15% 10% "UNSCREENED" { 65% 15% 10% } "SCREENED"
 $3d^{10}$ 35% 85% 90% { 35% 85% 90% }



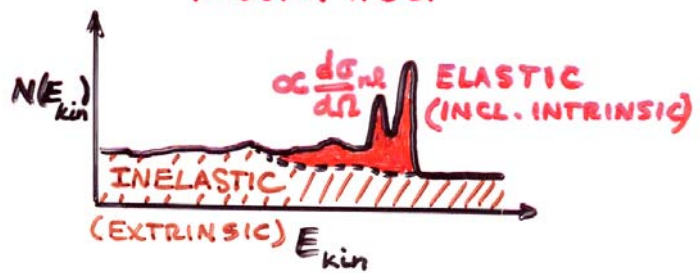
= covered so far

ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS



- + SPIN-ORBIT SPLITTING (EASY)
- + MULTIPLY SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD
- + CORRELATION/CONFIGURATION INTERACTION
- + SHAKE-UP/SHAKE-OFF/ e^- -HOLE
- + SCREENING/NON-SCREENING: CONFIGURATION INTERACTION
- + VIBRATIONAL EXCITATIONS
- + RESONANT PHOTOEMISSION ($h\nu \approx E_{b,n\ell}$)

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



INTENSITIES IN PHOTOELECTRON SPECTRA:

- GENERAL: FINAL STATE K (k -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_i^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPPENHEIMER: e^- 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION: $\Psi_k \rightarrow \Psi_f = \text{PHOTO}^-$ (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 \underbrace{|\langle \Psi_e^f(N-1, K) | \Psi_e^i(N-1, K) \rangle|^2}_{k \text{ MISSING}}$$

$$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_k \rangle|^2 \quad \text{SAME SUBSHELL COUPLING + TOTAL L, S} \rightarrow \text{"MONOPOLE"}$$

\hookrightarrow NORMAL $\frac{dG_K}{d\Omega}$

- SLATER DETS. FOR $\Psi_e^f = \det(\Psi_1', \Psi_2', \dots, \Psi_{k-1}', \Psi_{k+1}', \dots, \Psi_N')$

$$\Psi_e^i = \det(\Psi_1, \Psi_2, \dots, \Psi_{k-1}, \Psi_{k+1}, \dots, \Psi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 \underbrace{|\langle \Psi_1' | \Psi_1 \rangle|^2 |\langle \Psi_2' | \Psi_2 \rangle|^2 \dots |\langle \Psi_{k-1}' | \Psi_{k-1} \rangle|^2 |\langle \Psi_{k+1}' | \Psi_{k+1} \rangle|^2 \dots |\langle \Psi_N' | \Psi_N \rangle|^2}_{\text{}}}$$

$$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_k \rangle|^2$$

1e- DIPOLE $\rightarrow d\sigma/d\Omega$

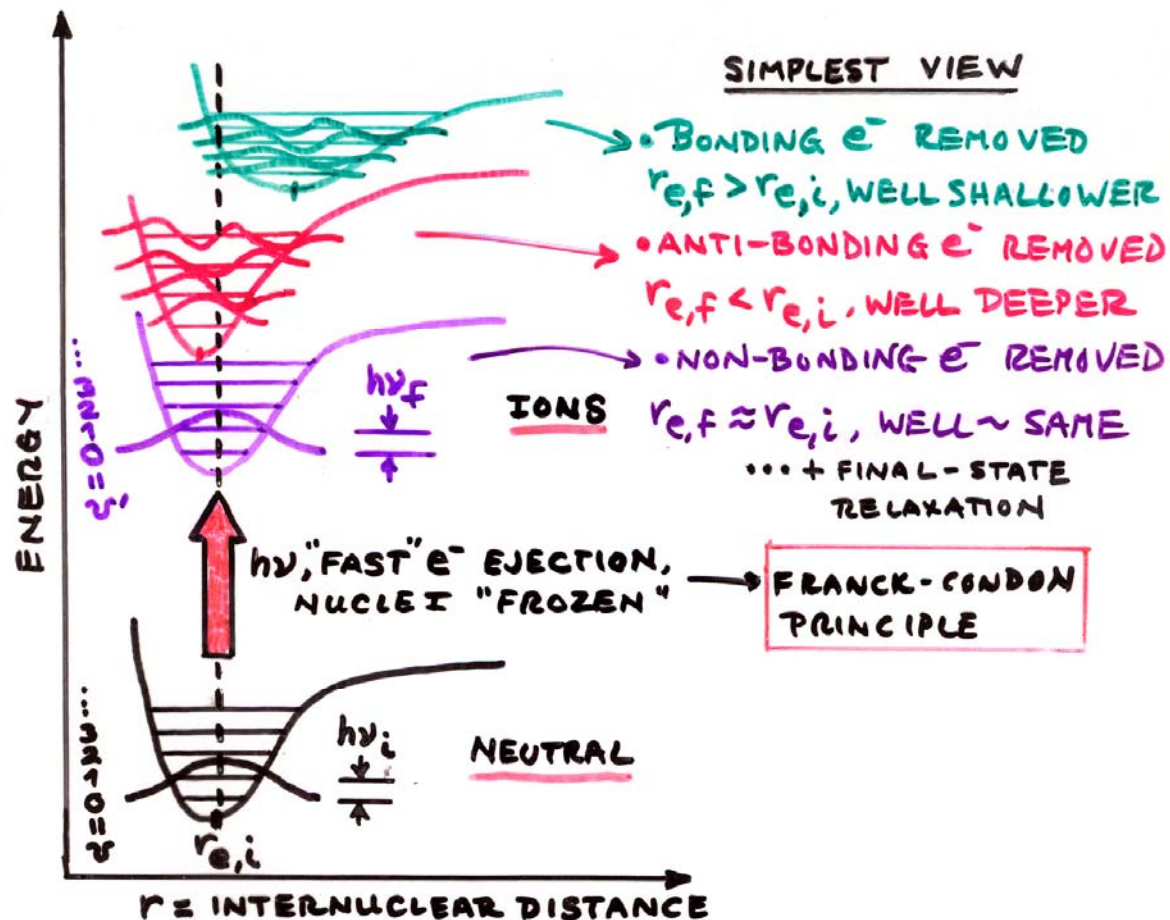
(N-1)e- SHAKE-UP/
SHAKE-OFF \rightarrow
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN Ψ_f ESCAPE

VIBRATIONAL STRUCTURE IN VALENCE-LEVEL (MO) SPECTRA

Diatomic A-B example

(Also applies to core-level emission if equilibrium distance changes on forming core hole)

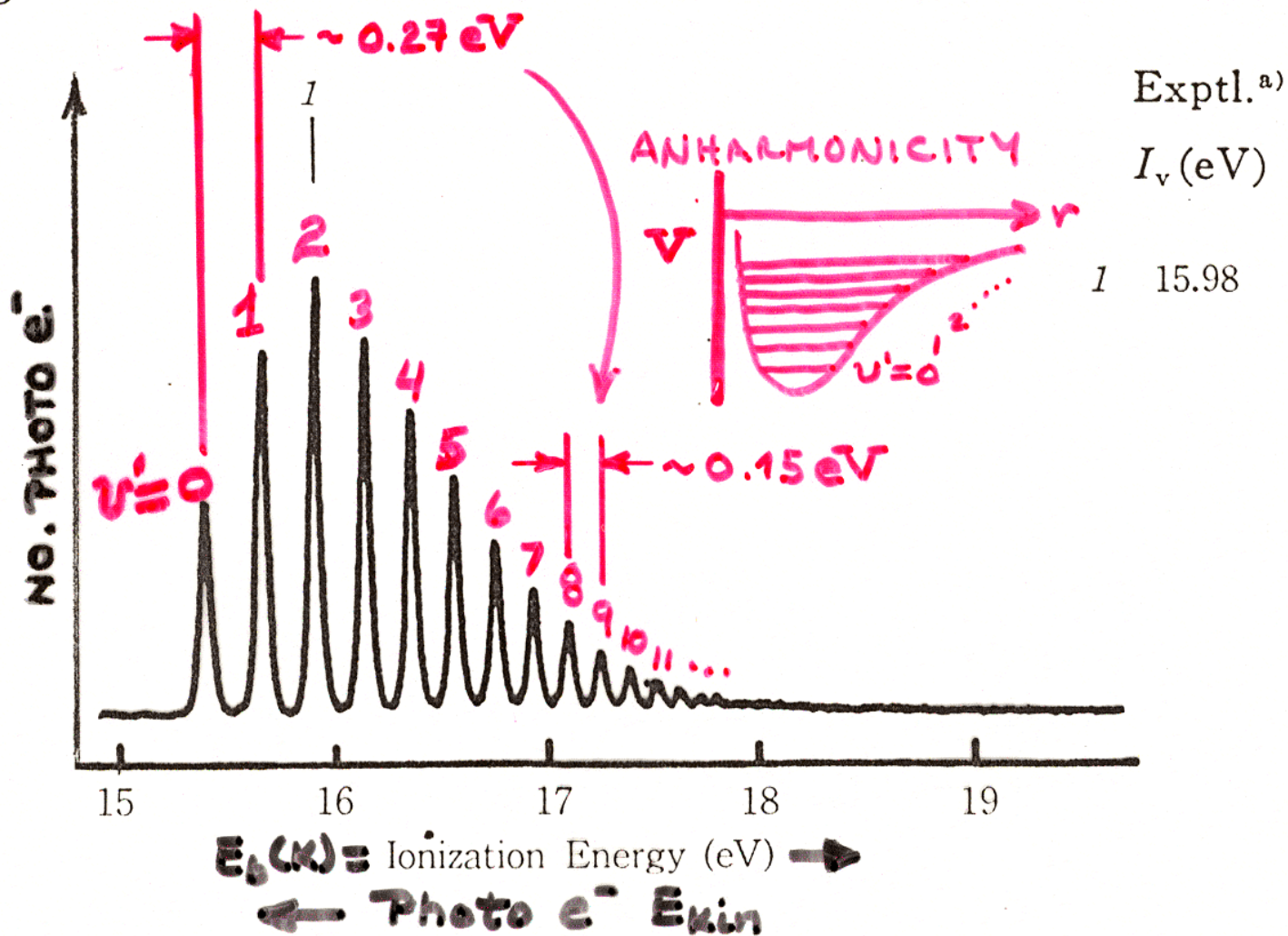


e^- REMOVED	r_e	$h\nu_{\text{VIB}}$	BAND APPEARANCE
BONDING	$r_{e,f} > r_{e,i}$	$h\nu_f < h\nu_i$	<p>$v=0 \rightarrow v'=0$ = "ADIABATIC" "VERTICAL" = MOST INTENSE</p>
ANTI-BONDING	$r_{e,f} < r_{e,i}$	$h\nu_f > h\nu_i$	<p>$v'=0$</p>
NON-BONDING (E.G., LONE PAIR)	$r_{e,f} \approx r_{e,i}$	$h\nu_f \approx h\nu_i$	<p>$v=A$</p>

← I.P. = E_b

VIBRATIONAL STRUCTURE IN VALENCE-LEVEL (MO) SPECTRA

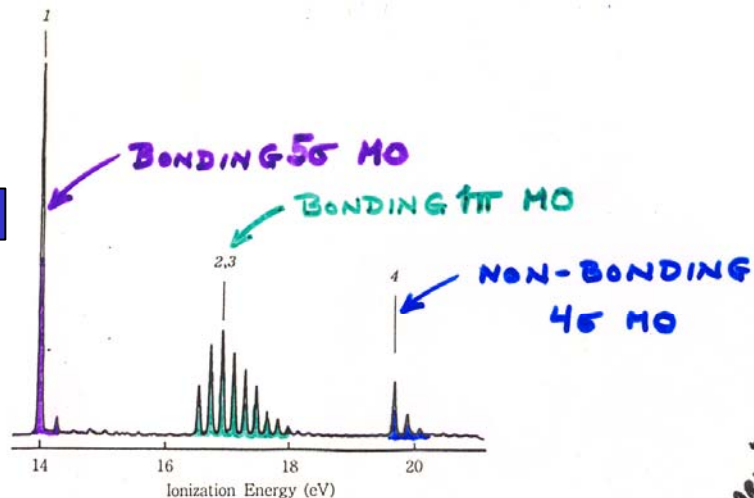
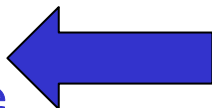
H₂ Hydrogen



(9) CO Carbon Monoxide

UV PHOTOELECTRON SPECTRUM OF CO

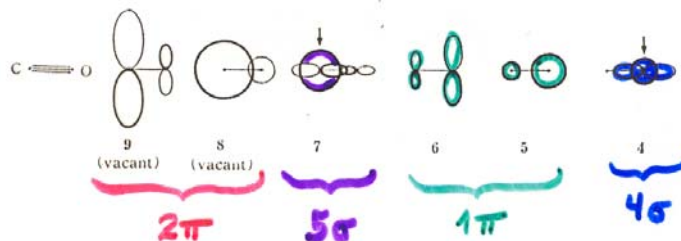
Vibrational fine structure



Exptl. ^{a)} I_v (eV)	Koopmans'		CI FINAL STATE			
	$-\epsilon$ (eV)	SCF MO [6-31 G] ^{b)}	CI (Ionic State) [6-31 G] ^{c)}	E (eV)	State	Configuration
1	14.01	14.99	5σ (7) σ_{CO}	13.11	$1^2\Sigma^+$	0.93(7 ⁻¹) -0.15(6 ⁻¹ , 7 ⁻¹ , 9 ¹) _a -0.15(5 ⁻¹ , 7 ⁻¹ , 8 ¹) _a
2	16.91	17.48	1π (6, 5) π_{bond}	16.69	$1^2\Pi$	0.95(6 ⁻¹) ; 0.95(5 ⁻¹)
3	16.91	17.48				
4	19.72	21.69	4σ (4) n_O	19.29	$2^2\Sigma^+$	0.92(4 ⁻¹) +0.16(6 ⁻¹ , 7 ⁻¹ , 9 ¹) _a +0.16(5 ⁻¹ , 7 ⁻¹ , 8 ¹) _a

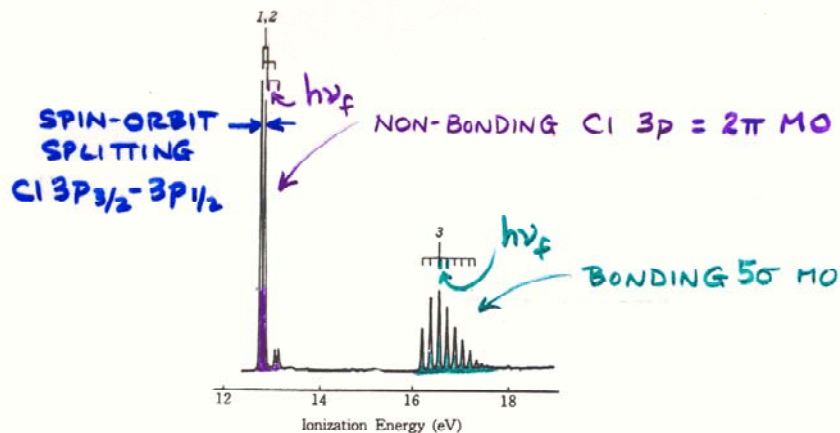
PRIMARY HOLES
RELAX. + CORREL.

- a) The spectrum: this work. The I_v 's: Turner *et al.* (215). See also other works: Turner and May (215 a); Carlson and Jonas (54); Gardner and Samson (104); Edqvist *et al.* (90); Potts and Williams (182 a); and Natalis *et al.* (165).
- b) We used the bond length reported (A 3); symmetry $C_{\infty h}$. $E_{SCF} = -112.6672$ hartree. In 4-31 G calculations, $E_{SCF} = -112.5524$ hartree and $-\epsilon$ (eV) = 14.93, 17.41, 17.41, and 21.60.
- c) CI-IL (9, 8) = 1π. |N| = 0.98 (SCF). The results obtained in other CI levels are given in Appendix B.



Kimura et al.,
"Handbook of Hel
Photoelectron Spectra"

THE UV PHOTOELECTRON SPECTRUM OF HCl



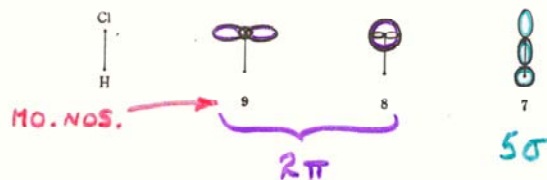
Exptl. ^{a)}	SCF MO [4-31 G] ^{b)}		CONFIG. INT. ON FINAL STATE			
	I_v (eV)	$-\epsilon$ (eV)	MO	Character	\sim Cl (Ionic State) [4-31 G] ^{c)}	
					E (eV) State Configuration	
1	12.75	12.77	2 π (9, 8)	n_{Cl}	11.97 1 2 I	0.98 (9 $^{-1}$); 0.98 (9 $^{-1}$)
2	12.85	12.77				
3	16.28	16.50	5 σ (7)	σ_{HCl}	16.10 1 2 Σ^+	0.98 (7 $^{-1}$)

CI HOLE
WEIGHTING

a) The spectrum: this work. The I_v 's: Frost *et al.* (102). See also other works: Lempka *et al.* (150); Turner *et al.* (215); and Weiss *et al.* (224).

b) We used the bond length reported in Ref. (A 5); symmetry $C_{\infty v}$. $E_{SCF} = -459.5631$ hartree.

c) CI-V: $|N\rangle = 0.99$ (SCF).
 CI-V': E (eV) = 12.01 and 16.11.
 CI-III: E (eV) = 12.60 and 16.79.



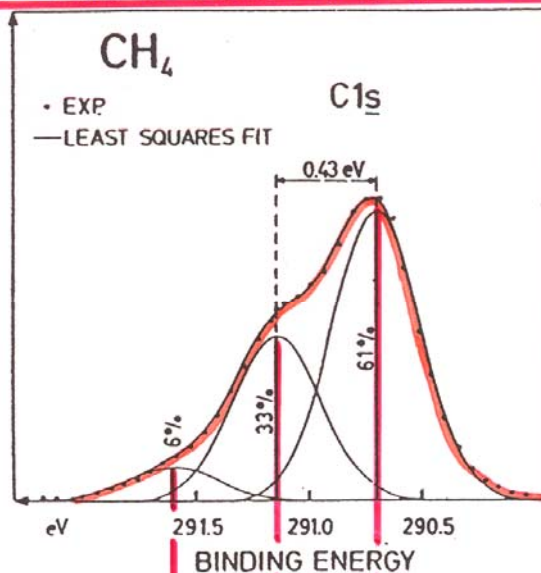
(FROM KIMURA ET AL., "HANDBOOK OF He I PHOTO-ELECTRON SPECTRA OF FUND. ORGANIC MOLECULES")

VIBRATIONAL FINE STRUCTURE IN CORE SPECTRA

MONOCHROMATIZED
LABORATORY
X-RAY SOURCE

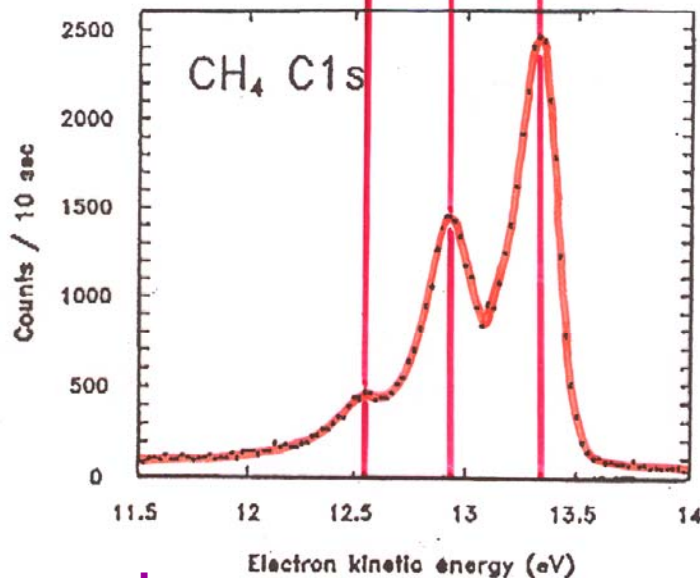
1970
SIEGBAHN,
GELUUS,
ET AL.

“Basic Concepts of XPS”
Figure 40

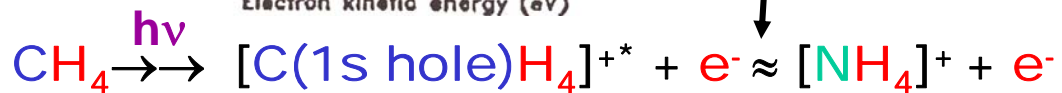


NEW SR
BEAMLINE
AT
BROOK-
HAVEN
(~5-10X
FASTER
@ALS)

1991
BRADSHAW,
KAINDL,
ET AL.

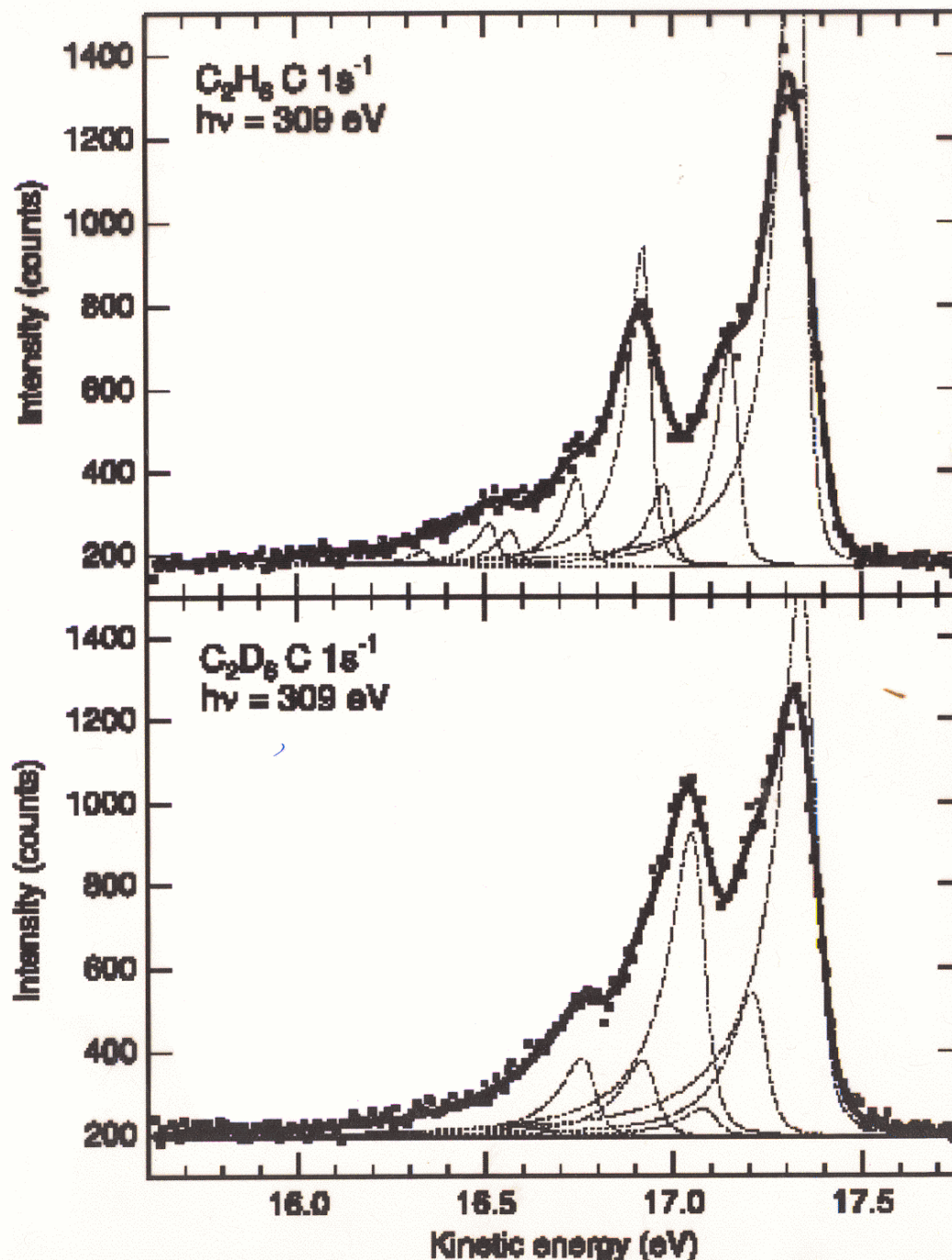


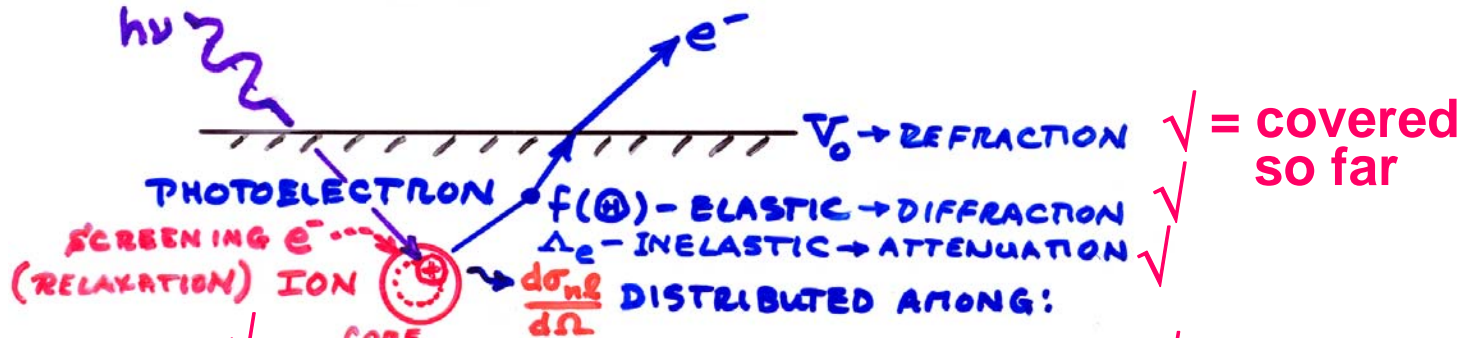
CH distance = 1.10 Å
NH distance = 1.00 Å
Equivalent-core



Vibrational fine structure in C 1s photoemission from ethane: two progressions ν_a at 0.407 eV and ν_b at 0.176 eV and various excitations (ν_a, ν_b)

Rennie et al.,
J. Phys. At. Mol. Opt. Phys. 32, 2691 (1999)



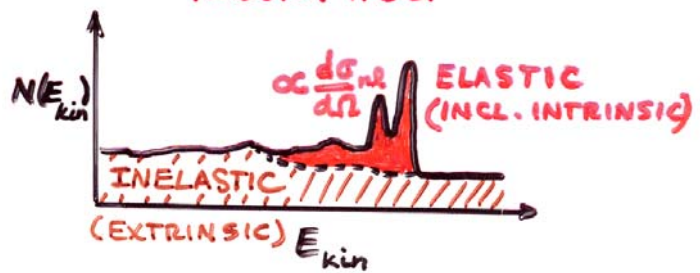


= covered so far

ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- ✓ CORE HOLE $k = n\ell$
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- ✓ + VIBRATIONAL EXCITATIONS
- ✓ + RESONANT PHOTOEMISSION ($h\nu \approx E_{b,n\ell}$)

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



Outline

Surface, interface, and nanoscience—short introduction

Some surface concepts and techniques→photoemission

Synchrotron radiation: experimental aspects

Electronic structure—a brief review

**The basic synchrotron radiation techniques:
more experimental and theoretical details**

Core-level photoemission

Valence-level photoemission

 **Microscopy with photoemission:
All of the above with lateral spatial resolution
of ca. 20 nm, going down to few nm in future
(Next lecturers)**

Thank you for your attention!