



*The Abdus Salam*  
**International Centre for Theoretical Physics**



**SMR.1751 - 3**

Fifth International Conference on  
**PERSPECTIVES IN HADRONIC PHYSICS**  
Particle-Nucleus and Nucleus-Nucleus Scattering at Relativistic Energies

**22 - 26 May 2006**

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**TDAs: a new tool to study exclusive reactions**

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These are preliminary lecture notes, intended only for distribution to participants



# TDAs : a new tool to study exclusive reactions

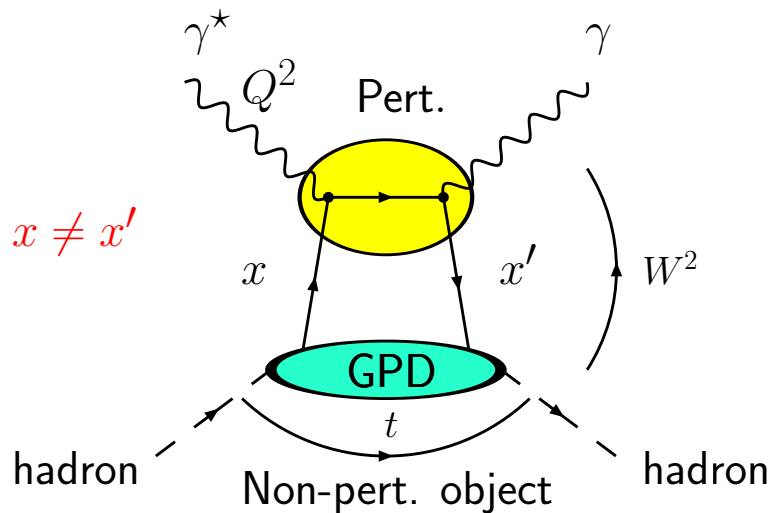
Conference on Perspectives in Hadronic Physics  
22-26 May 2006, ICTP Trieste Italy

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CPhT, École Polytechnique & PTF, Liège

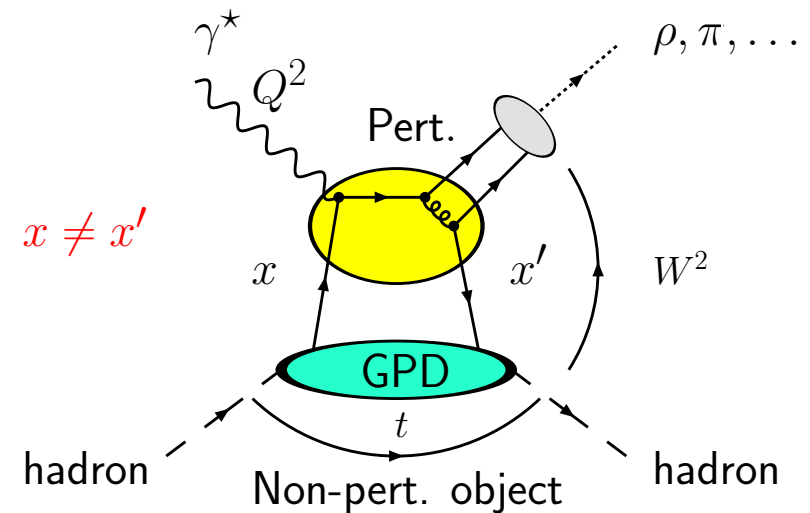
in collaboration with B. Pire and L. Szymanowski

# Reminder on Generalised Parton Distributions

## DVCS

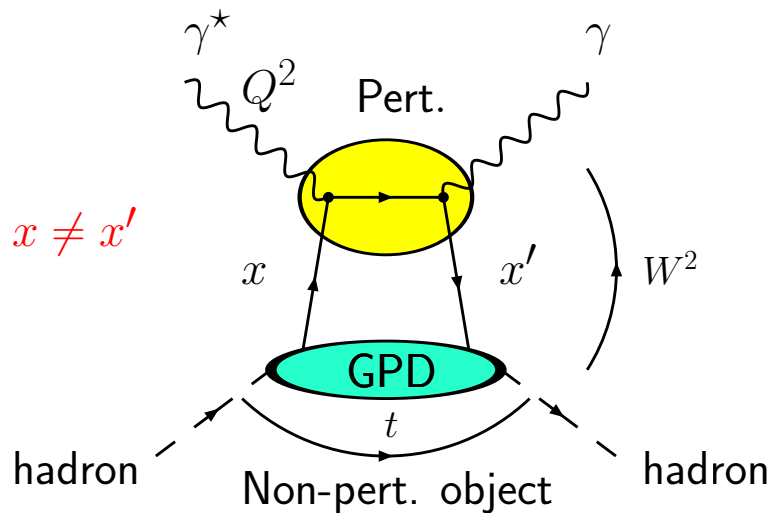


## Mesons Production

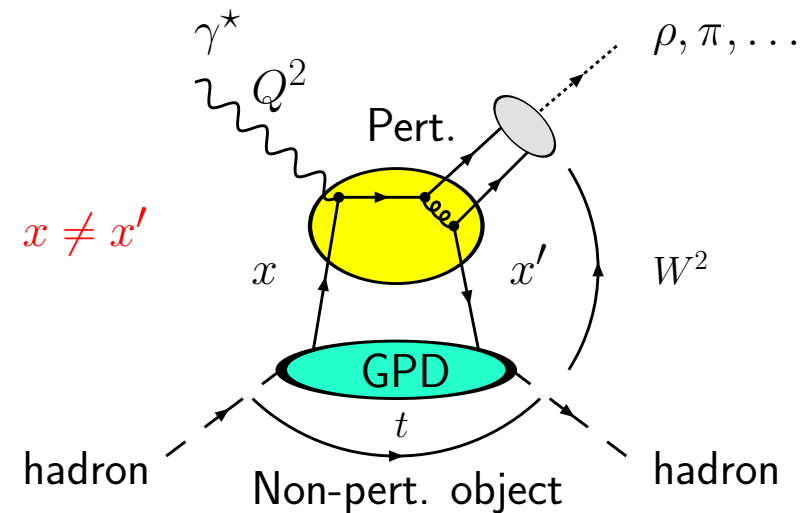


# Reminder on Generalised Parton Distributions

## DVCS



## Mesons Production



⇒ **Factorisation** between the hard part (perturbatively calculable) and the soft part (non-perturbative) **demonstrated** for

$$Q^2 \rightarrow \infty, x_B = \frac{Q^2}{Q^2 + W^2} \text{ fixed and } t \ll \text{fixed}$$

# TDAs : transition distribution amplitudes

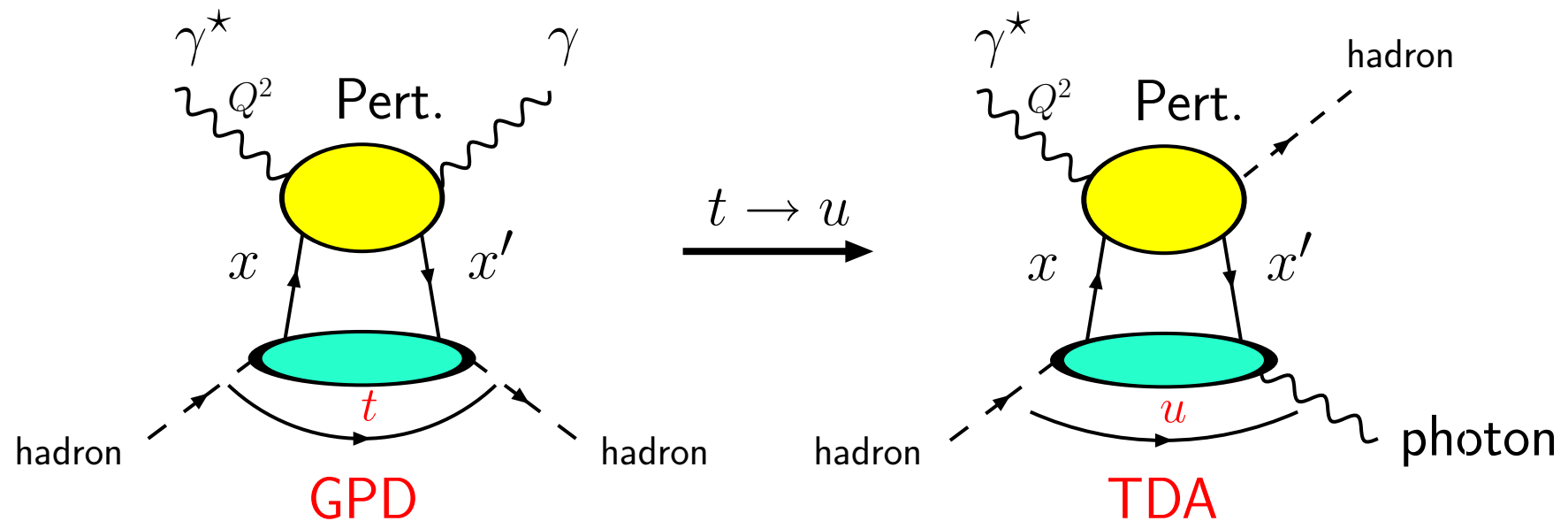
B. Pire, L. Szymanowski, PRD 71 :111501,2005 ; PLB 622 :83,2005.

⇒ For  $u \ll \text{DVCS}$ , the non-perturbative part does not describe anymore a  $H \rightarrow H$  transition, but rather  
a hadron-photon or baryon-meson transition.

# TDAs : transition distribution amplitudes

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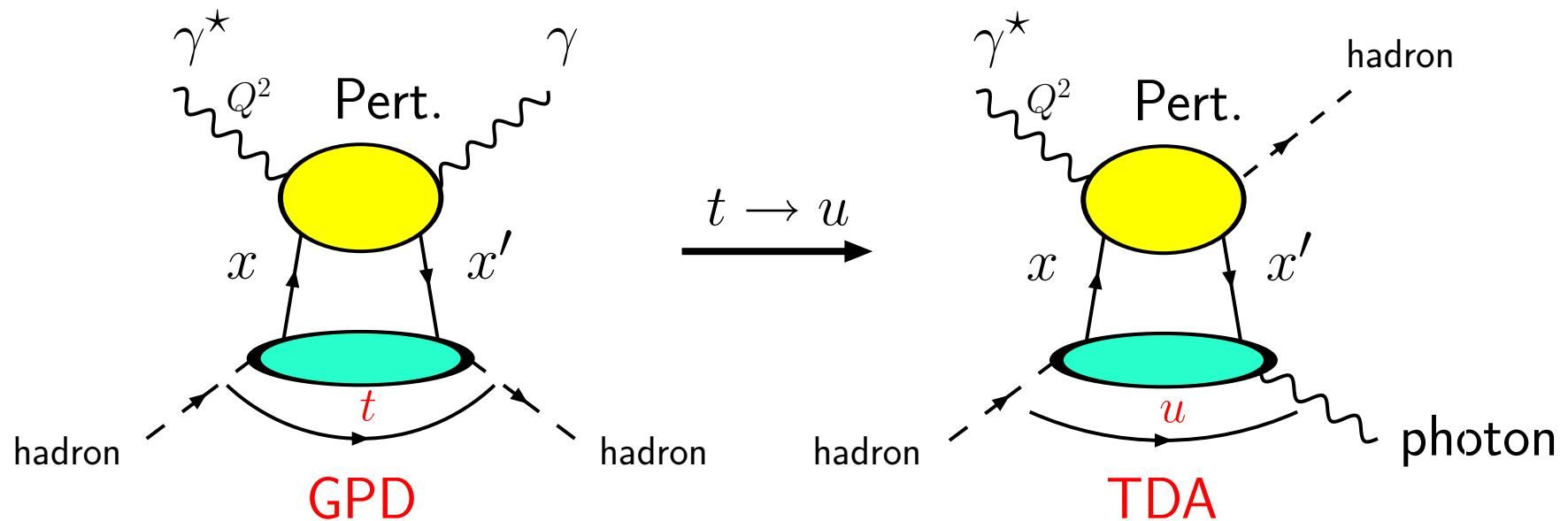
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# TDAs : transition distribution amplitudes

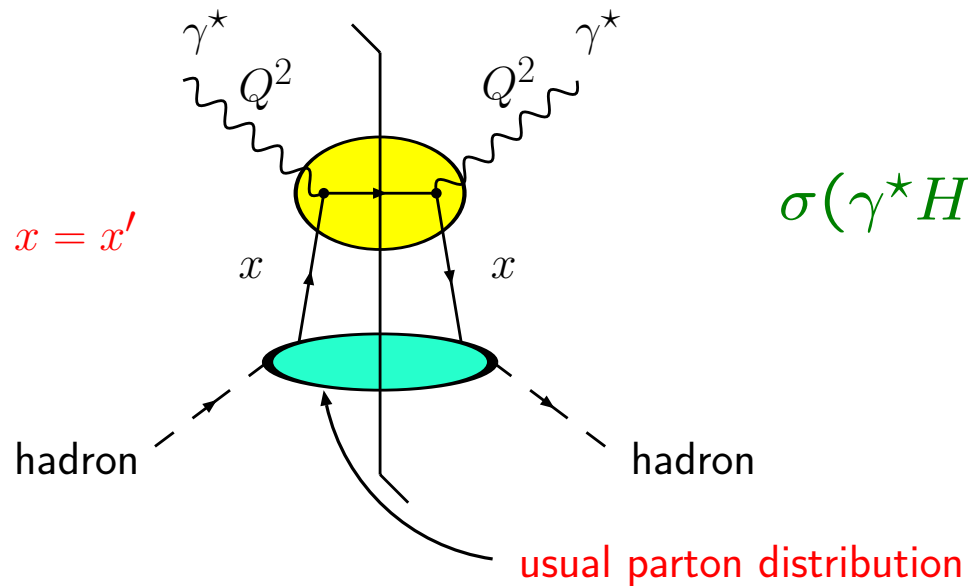
B. Pire, L. Szymanowski, PRD 71 :111501,2005 ; PLB 622 :83,2005.

⇒ For  $u \ll \text{DVCS}$ , the non-perturbative part does not describe anymore a  $H \rightarrow H$  transition, but rather a hadron-photon or baryon-meson transition.



⇒ The same occurs in  $p\bar{p} \rightarrow \gamma\gamma^*$  reactions at  $t \ll (\text{GSI})$   
⇒ and in  $\gamma\gamma^* \rightarrow \pi\pi$  reactions at  $t \ll$  (through  $e^+e^-$  collisions )

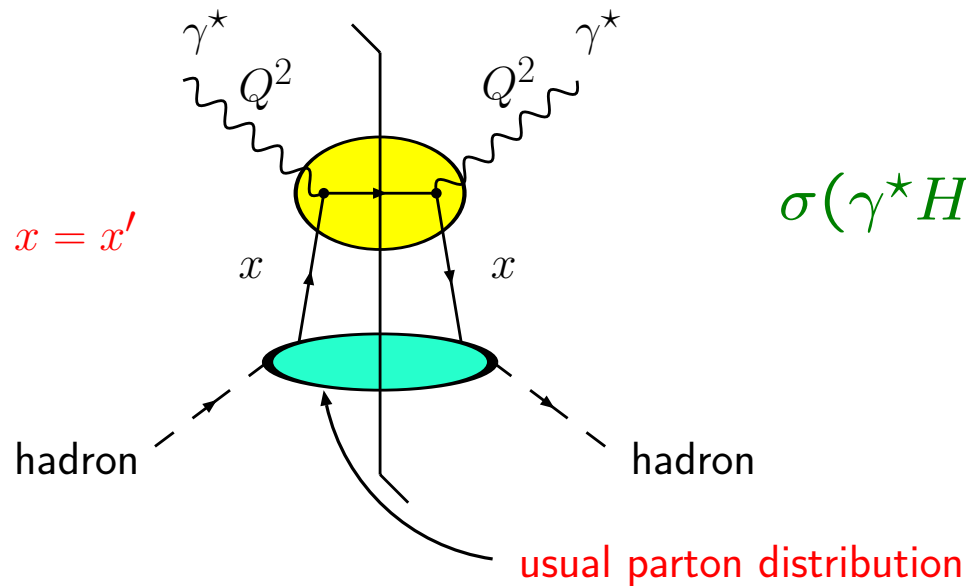
# GPD in terms of *usual* parton distributions



$$\sigma(\gamma^* H \rightarrow X) \propto \Im m(\mathcal{A}^{diag}(\gamma^* H \rightarrow \gamma^* H))$$



# GPD in terms of *usual* parton distributions



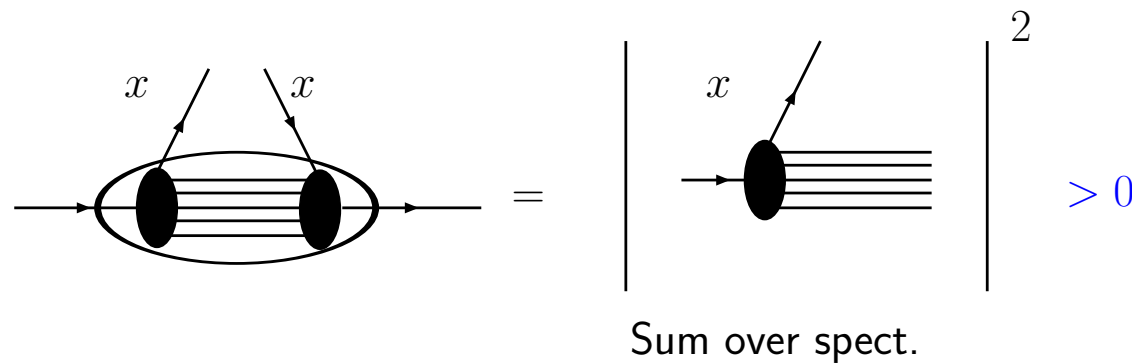
$$\sigma(\gamma^* H \rightarrow X) \propto \Im m(\mathcal{A}^{diag}(\gamma^* H \rightarrow \gamma^* H))$$

$$= \left| \text{Sum over spect.} \right|^2 > 0$$

Sum over spect.

⇒ The PDFs give the **probability** to find, within the hadron, a parton with a **momentum fraction**  $x$ .

# GPD in terms of *usual* parton distributions



The diagram illustrates the relationship between a Generalized Parton Distribution (GPD) and a Parton Distribution Function (PDF). On the left, a GPD is represented by a hadron (an oval) with two partons (black ovals) inside. Two incoming lines, each labeled  $x$ , point to the partons. A horizontal line with an arrow enters the hadron from the left, and another horizontal line with an arrow exits to the right. This is followed by an equals sign. On the right, a PDF is shown as a single parton (black oval) with an incoming line labeled  $x$ . A horizontal line with an arrow enters the parton from the left, and several horizontal lines exit to the right. This is enclosed in a square with vertical bars on the left and right sides. A superscript 2 is placed above the right vertical bar. To the right of the square is a blue  $> 0$ . Below the square is the text "Sum over spect."

⇒ The PDFs give the **probability** to find, within the hadron, a parton with a **momentum fraction**  $x$ .

# GPD in terms of *usual* parton distributions

$$\begin{array}{c} x \neq x' \\ x \quad x' \\ p \quad p' \end{array} \quad \text{Diagram} = p \quad \text{Diagram} \times \left[ p' \quad \text{Diagram} \right]^*$$

The diagram on the left shows a hadron with two partons, one with momentum fraction  $x$  and the other with  $x'$ , where  $x \neq x'$ . The hadron has momentum  $p$  and the partons have momenta  $p$  and  $p'$ . The diagram on the right shows the same hadron with two partons, one with momentum fraction  $x$  and the other with  $x'$ , where  $x = x'$ . The hadron has momentum  $p$  and the partons have momenta  $p$  and  $p'$ . The diagram on the right is the complex conjugate of the diagram on the left.

⇒ The GPDs possess an interpretation at the **amplitude** level and provide with information about **correlations between quarks**

$$\begin{array}{c} x \quad x \\ \text{Diagram} \end{array} = \left| \begin{array}{c} x \\ \text{Diagram} \end{array} \right|^2 > 0$$

Sum over spect.

The diagram on the left shows a hadron with two partons, both with momentum fraction  $x$ . The hadron has momentum  $p$  and the partons have momenta  $p$  and  $p'$ . The diagram on the right shows the same hadron with two partons, both with momentum fraction  $x$ . The hadron has momentum  $p$  and the partons have momenta  $p$  and  $p'$ . The diagram on the right is the square of the diagram on the left, summed over the spectator partons.

⇒ The PDFs give the **probability** to find, within the hadron, a parton with a **momentum fraction  $x$** .

# Interpretation of the TDAs

$$p \rightarrow \text{box}(x, x') \rightarrow p' = p \rightarrow \text{vertex}(x) \times \left[ \text{vertex}(x') \rightarrow p' \right]^*$$

⇒ The **mesonic** TDAs possess an interpretation at the **amplitude** level and provide with information on **how a meson looks like photon**

**whereas**

$$p \rightarrow \text{box} \rightarrow p' = p \rightarrow \text{vertex} \times \left[ \text{vertex} \rightarrow p' \right]^*$$

⇒ The **baryonic** TDAs rather provide information on **how one can find a meson or a photon in it**

# TDAs vs GPDs : meson case

|                                                                                           | GPDs                                                               | TDAs                                                                       |
|-------------------------------------------------------------------------------------------|--------------------------------------------------------------------|----------------------------------------------------------------------------|
| <b>Matrix elements</b>                                                                    | $\langle M(p')   \Phi^\dagger(z) \Phi(0)   M(p) \rangle$           | $\langle \gamma(p', \varepsilon)   \Phi^\dagger(z) \Phi(0)   M(p) \rangle$ |
| <b>Diagonal limit</b><br>$\xi \rightarrow 0, t \rightarrow 0$                             | <b>GPDs <math>\rightarrow</math> PDFs</b><br>$H^q(x, 0, 0) = q(x)$ | <b>N/A</b>                                                                 |
| <b>Sum rules : <math>\int dx</math></b><br><b><math>\rightarrow</math> local operator</b> | $\int dx H(x, \xi, t) = F(t)$                                      | $\int dx T(x, \xi, t) = F_{A \rightarrow B}(t)$                            |

⇒ In view of the sum rules, both GPDs and TDAs are such that their integral on  $x$  is **independent of  $\xi$  !**

⇒ possible modelling of the TDAs through double distributions  
(cf. Radyushkin)

## Example : $\gamma \rightarrow \pi$ TDAs

JPL, B. Pire, L. Szymanowski, PRD 73 :074014,2006.

There are **4** leading-twist helicity amplitudes for  $\gamma \rightarrow q\bar{q}\pi$

→ **4 TDAs :  $A$ ,  $V$ ,  $T_1$  and  $T_2$**

$$\int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle \pi^-(p_{\pi^-}) | \bar{d}(-\frac{z}{2}) [\dots] \gamma^\mu u(\frac{z}{2}) | \gamma(p_\gamma, \varepsilon) \rangle \Big|_{z^+=0, z_T=0} = \frac{1}{P^+} \frac{i e}{f_\pi} \epsilon^{\mu\varepsilon P \Delta_\perp} V^{\pi^-}(x, \xi, t)$$

$$\int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle \pi^-(p_{\pi^-}) | \bar{d}(-\frac{z}{2}) [\dots] \gamma^\mu \gamma^5 u(\frac{z}{2}) | \gamma(p_\gamma, \varepsilon) \rangle \Big|_{z^+=0, z_T=0} = \frac{1}{P^+} \frac{e}{f_\pi} (\varepsilon \cdot \Delta) P^\mu A^{\pi^-}(x, \xi, t),$$

$$\begin{aligned} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle \pi^-(p_{\pi^-}) | \bar{d}(-\frac{z}{2}) [\dots] \sigma^{\mu\nu} u(\frac{z}{2}) | \gamma(p_\gamma, \varepsilon) \rangle \Big|_{z^+=0, z_T=0} \\ = \frac{e}{P^+} \epsilon^{\mu\nu\rho\sigma} P_\sigma \left[ \varepsilon_\rho T_1^{\pi^-}(x, \xi, t) - \frac{1}{f_\pi} (\varepsilon \cdot \Delta) \Delta_{\perp\rho} T_2^{\pi^-}(x, \xi, t) \right] \end{aligned}$$

## Example : $\gamma \rightarrow \pi$ TDAs

### ⇒ Sum Rules :

$$\Rightarrow \pi^\pm : \int_{-1}^1 dx \left\{ \frac{A^{\pi^\pm}}{V^{\pi^\pm}} \right\} (x, \xi, t) = \frac{f_\pi}{m_\pi} F_{\left\{ \begin{smallmatrix} A \\ V \end{smallmatrix} \right\}}^{\pi^\pm}(t)$$

$F_A$  et  $F_V$  are measured (cf. PDG)

$$\Rightarrow \pi^0 : \int_{-1}^1 dx \left( Q^u V_u^{\pi^0}(x, \xi, t) + Q^d V_d^{\pi^0}(x, \xi, t) \right) = f_\pi F_{\pi^0 \gamma^* \gamma}(t)$$

**NB : Sum rule for  $A^{\pi^0}$**

→  $\pi^0 \rightarrow Z^0 \gamma \rightarrow \nu \bar{\nu} \gamma$  (not measurable) or

→  $\pi^0 \rightarrow Z^0 \gamma \rightarrow \ell^+ \ell^- \gamma$  (with huge background from the electromagnetic process) ;

## Example : $\gamma \rightarrow \pi$ TDAs

For  $G = (A, V)$ ,  $G^{(0)}(x, \xi) \equiv \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(x - \beta - \xi\alpha) f(\beta, \alpha)$  with  $f(\beta, \alpha) = q(\beta)h(\beta, \alpha)$

and a profile function  $h^{(b)}(\beta, \alpha) = \frac{\Gamma(2b+2)}{2^{2b+1}\Gamma^2(b+1)} \frac{[(1-|\beta|)^2 - \alpha^2]^b}{(1-|\beta|)^{2b+1}}$ .

( $b$  characterises the strength of the  $\xi$ -dependence.)



## Example : $\gamma \rightarrow \pi$ TDAs

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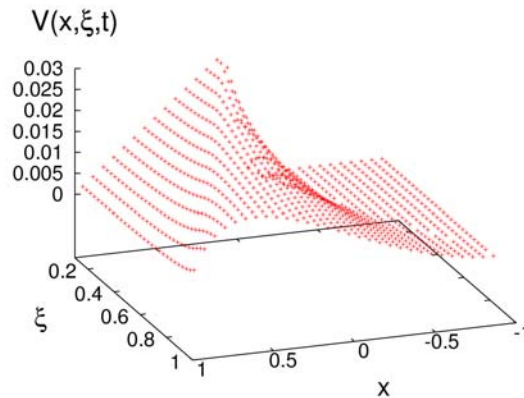
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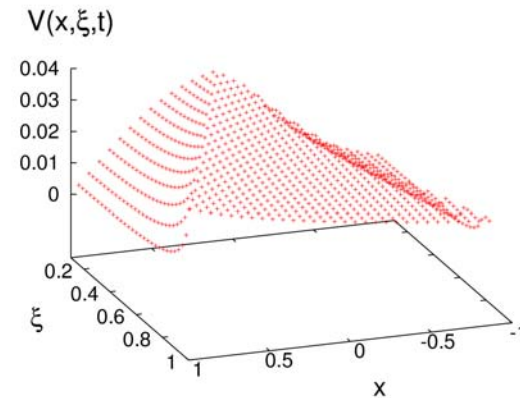
The  $t$ -dependence is implemented to get the sum rule :

$$G(x, \xi, t) = G^{(0)}(x, \xi) \cdot \frac{f_\pi}{m_\pi} F_G(t) .$$

Setting  $b = 1$  and taking the  $\beta$ -dependence of  $q$  to be  $q(\beta) = 2(1-\beta)\theta(\beta)$ .



This Model (1)

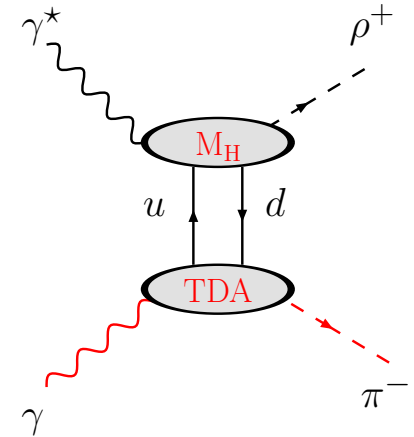


Tiburzi's Model (2)

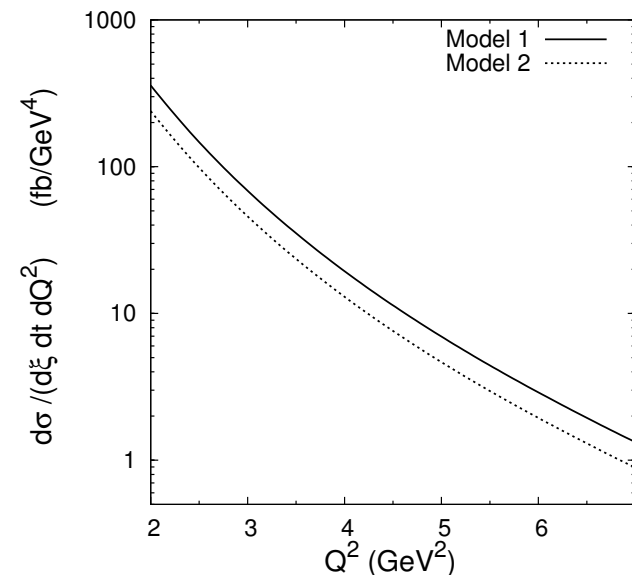
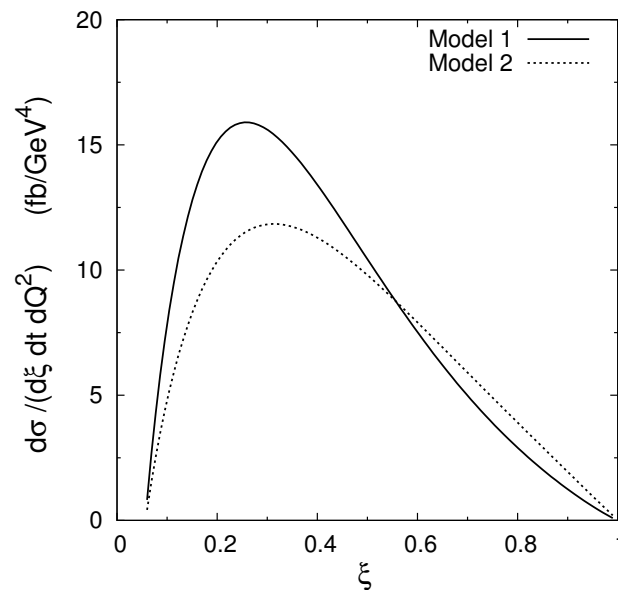
# $\gamma \rightarrow \pi$ TDAs : Application

## ➔ $\rho - \pi$ pair production at small $t$

- ➔ cross section for  $e \gamma \rightarrow e' \rho \pi$
- ➔  $\pi$  flies in the direction of the  $\gamma$   
( $\leftrightarrow \sim 180^\circ$  between  $\rho$  and  $\pi$  or large  $W$ )
- ➔ Complementary kinematics compared to GDAs
- ➔ No Bremßstrahlung

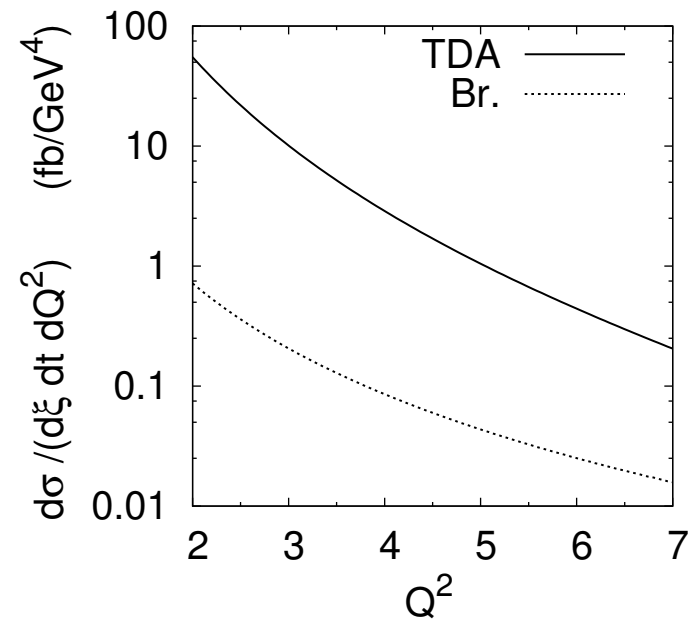
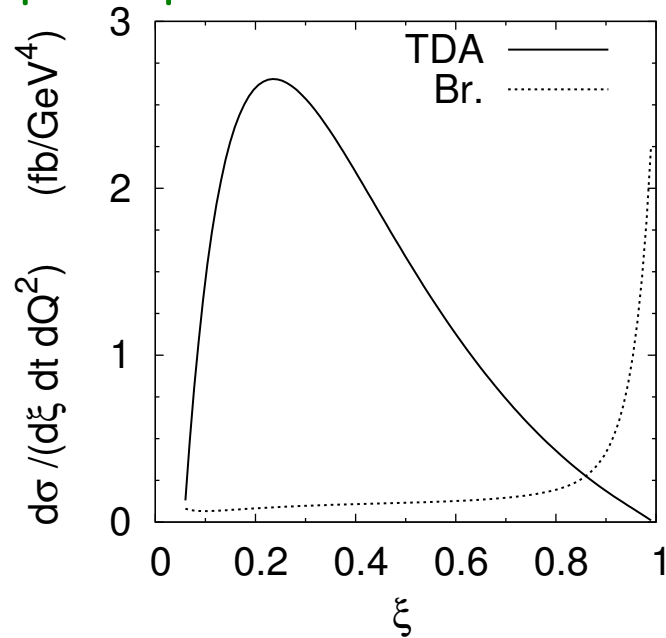


➔  $s_{e\gamma} = 40 \text{ GeV}^2$ ,  $t = -0.5 \text{ GeV}^2$ ,  $Q^2 = 4 \text{ GeV}^2$  and  $\xi = 0.2$



# $\gamma \rightarrow \pi$ TDAs : Application

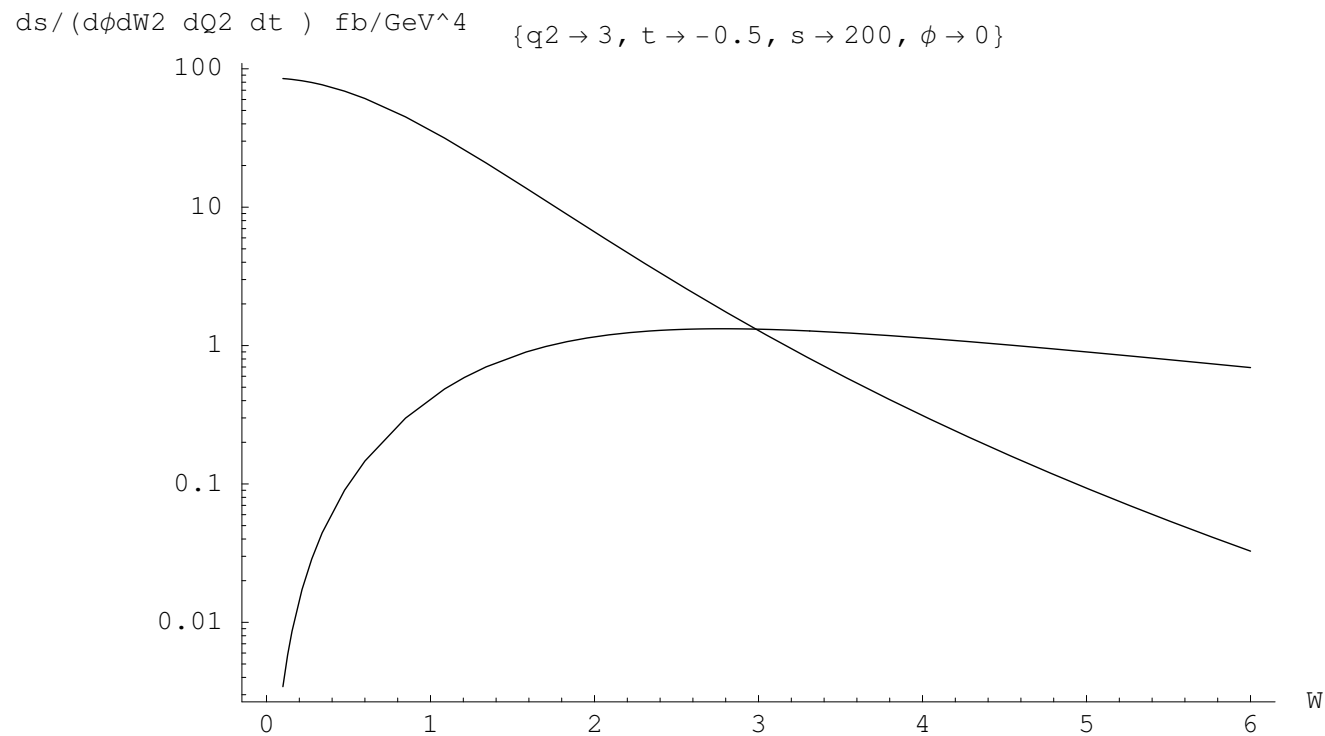
➡  $\pi - \pi$  pair production at small  $t$



➡ Any measurement of  $e\gamma \rightarrow e'\pi^0\pi^0$  would provide with information on the Axial Transition Form factor  $F_A^{\pi^0}$ .

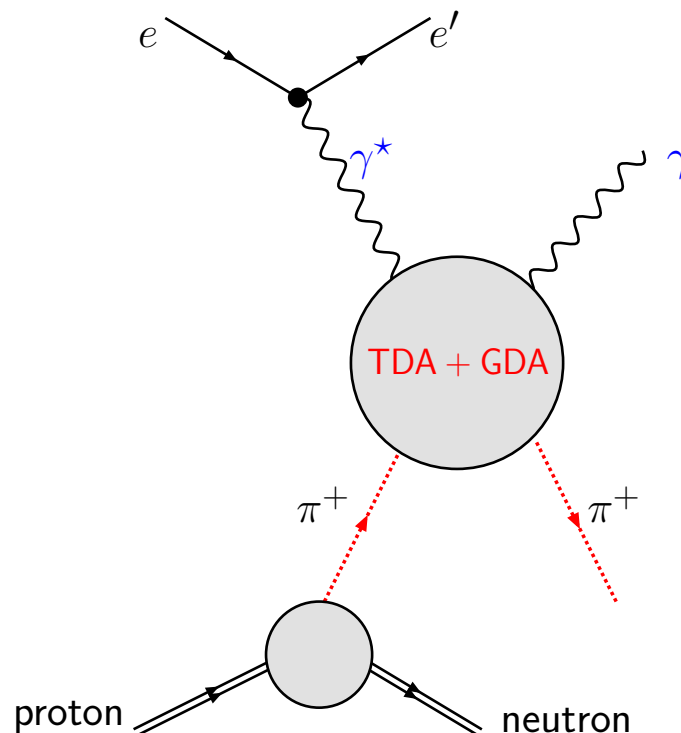
# TDAs vs GDAs

➔ Expected behaviour :  $\frac{\sigma_{TDA}}{\sigma_{GDA}} \rightarrow \frac{t}{Q^2} \frac{W^2}{Q^2}$



## DVCS on pion

- ⇒ To be analysed by HERMES through :  $ep \rightarrow e'\gamma\pi^+n$
- ⇒ Non-trivial kinematics ; DVCS subset of  $2 \rightarrow 4$  process
  - ⇒ Cannot trivially distinguish between the small  $t$  (GPD) and small  $u$  (TDA) regions



## TDAs : baryonic case

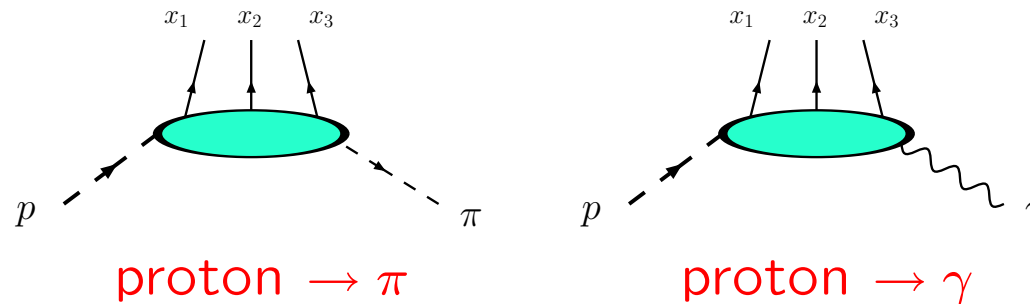
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- ⇒ Both for Baryon  $\rightarrow$  Meson and Baryon  $\rightarrow$  photon,  
3 quarks should be exchanged in the  $t$ -channel

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- ⇒ Both for Baryon  $\rightarrow$  Meson and Baryon  $\rightarrow$  photon,  
3 quarks should be exchanged in the  $t$ -channel



- ⇒ More than the two regions ERBL and DGLAP
- ⇒ In principle, one has Sum rules  
 $\rightarrow \xi$ -independence of the moments of the TDA
- ⇒ Triple distributions ?
  - ⇒ Diquark picture and double distribution ?

would suit some regions only ?

- ⇒ Closest object : Baryon Distribution Amplitude :  $\rightarrow$  SOFT LIMIT ?

# $p \rightarrow \pi$ : parametrisation

$\Rightarrow p \rightarrow \pi$  (at Leading twist accuracy)

$\Rightarrow \Delta_T = 0$  : **3 TDAs** ( $3 \times p(\uparrow) \rightarrow uud(\uparrow\uparrow\downarrow) + \pi$ )

(similar to Baryon DAs)

**TDA**

**DA**

$$4\langle\pi^0|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p\rangle \propto$$

$$4\langle 0|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p\rangle \propto$$

$$\left[ V_1^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} C)_{\alpha\beta}(N)_\gamma + \right. \\ A_1^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} \gamma^5 C)_{\alpha\beta}(\gamma^5 N)_\gamma - 3 \\ \left. T_1^{\pi^0}(x_i, \xi, \Delta^2)(\sigma_{\rho P} C)_{\alpha\beta}(\gamma^\rho N)_\gamma \right]$$

$$\left[ V(x_i)(\not{p} C)_{\alpha\beta}(\gamma^5 N)_\gamma + \right. \\ A(x_i)(\not{p} \gamma^5 C)_{\alpha\beta} N_\gamma + \\ \left. T(x_i)(i\sigma_{\rho p} C)_{\alpha\beta}(\gamma^\rho \gamma^5 N)_\gamma \right]$$



# $p \rightarrow \pi$ : parametrisation

$\Rightarrow p \rightarrow \pi$  (at Leading twist accuracy)

$\Rightarrow \Delta_T = 0$  : **3 TDAs** ( $3 \times p(\uparrow) \rightarrow uud(\uparrow\uparrow\downarrow) + \pi$ )

(similar to Baryon DAs)

**TDA**

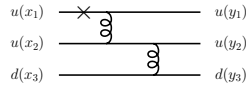
**DA**

$$\begin{aligned}
 4\langle\pi^0|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p\rangle &\propto 4\langle 0|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p\rangle \propto \\
 &\left[ V_1^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} C)_{\alpha\beta}(N)_\gamma + \right. \\
 &\quad A_1^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} \gamma^5 C)_{\alpha\beta}(\gamma^5 N)_\gamma - 3 \\
 &\quad \left. T_1^{\pi^0}(x_i, \xi, \Delta^2)(\sigma_{\rho P} C)_{\alpha\beta}(\gamma^\rho N)_\gamma \right] \\
 &\left[ V(x_i)(\not{p} C)_{\alpha\beta}(\gamma^5 N)_\gamma + \right. \\
 &\quad A(x_i)(\not{p} \gamma^5 C)_{\alpha\beta} N_\gamma + \\
 &\quad \left. T(x_i)(i\sigma_{\rho p} C)_{\alpha\beta}(\gamma^\rho \gamma^5 N)_\gamma \right]
 \end{aligned}$$

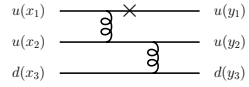
$\Rightarrow \Delta_T \neq 0$  : **8 TDAs** ( $\frac{1}{2} \times 2 \times (2 \times 2 \times 2) \times 1$ )

$$\begin{aligned}
 4\langle\pi^0(p_\pi)|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p(p_1, s)\rangle &= -\frac{f_N}{2f_\pi} \times \\
 &\left[ V_1^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} C)_{\alpha\beta}(N)_\gamma + V_2^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} C)_{\alpha\beta}(\not{\Delta}_T N)_\gamma \right. \\
 &\quad + A_1^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} \gamma^5 C)_{\alpha\beta}(\gamma^5 N)_\gamma + A_2^{\pi^0}(x_i, \xi, \Delta^2)(\not{P} \gamma^5 C)_{\alpha\beta}(\not{\Delta}_T \gamma^5 N)_\gamma \\
 &\quad - 3T_1^{\pi^0}(x_i, \xi, \Delta^2)(\sigma_{\rho P} C)_{\alpha\beta}(\gamma^\rho N)_\gamma + T_2^{\pi^0}(x_i, \xi, \Delta^2)(\sigma_{\Delta_T P} C)_{\alpha\beta}(N)_\gamma \\
 &\quad \left. + T_3^{\pi^0}(x_i, \xi, \Delta^2)(\sigma_{\mu P} C)_{\alpha\beta}(\sigma^{\mu\Delta_T} N)_\gamma + T_4^{\pi^0}(x_i, \xi, \Delta^2)(\sigma_{\Delta_T P} C)_{\alpha\beta}(\not{\Delta}_T N)_\gamma \right] \quad (1)
 \end{aligned}$$

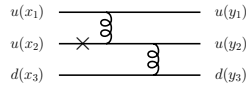
$$\bar{p}p \rightarrow \gamma^* \pi^0 \text{ at } \Delta_T = 0$$



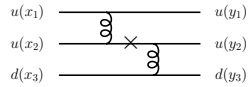
$$\frac{4}{3} \frac{\mathcal{V} + \mathcal{T}}{(2\xi - x_1 + i\epsilon)^2 (x_3 + i\epsilon) (1 - y_1)^2 y_3}$$



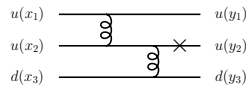
$$0$$



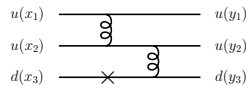
$$-\frac{4}{3} \frac{\mathcal{T}}{(x_1 + i\epsilon) (2\xi - x_2 + i\epsilon) (x_3 + i\epsilon) y_1 (1 - y_2) y_3}$$



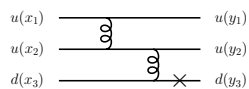
$$\frac{4}{3} \frac{\mathcal{V}}{(x_1 + i\epsilon) (2\xi - x_3 + i\epsilon) (x_3 + i\epsilon) y_1 (1 - y_1) y_3}$$



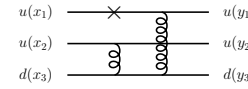
$$-\frac{4}{3} \frac{\mathcal{V}}{(x_2 + i\epsilon) (2\xi - x_3 + i\epsilon) (x_3 + i\epsilon) y_2 (1 - y_1) y_3}$$



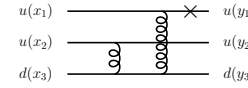
$$0$$



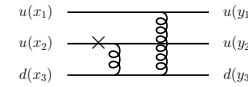
$$-\frac{2}{3} \frac{\mathcal{V}}{(2\xi - x_3 + i\epsilon)^2 (1 - y_3)^2} \left( \frac{1}{(x_1 + i\epsilon) y_1} + \frac{1}{(x_2 + i\epsilon) y_2} \right)$$



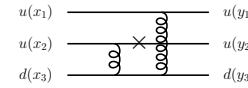
$$0$$



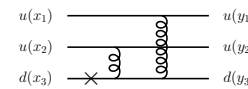
$$\frac{2}{3} \frac{\mathcal{V} + \mathcal{T}}{(2\xi - x_1 + i\epsilon)^2 (x_2 + i\epsilon) (1 - y_1)^2 y_2}$$



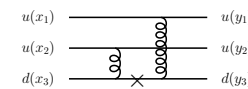
$$\frac{2}{3} \frac{\mathcal{V} + \mathcal{T}}{(2\xi - x_1 + i\epsilon)^2 (x_2 + i\epsilon) (1 - y_1)^2 y_2}$$



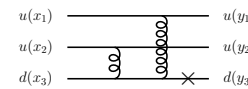
$$0$$



$$\frac{1}{3} \frac{\mathcal{V}}{(x_1 + i\epsilon) (x_2 + i\epsilon) (2\xi - x_3 + i\epsilon) y_1 (1 - y_1) y_2}$$



$$-\frac{1}{3} \frac{\mathcal{T}}{(x_1 + i\epsilon) (2\xi - x_1 + i\epsilon) (x_2 + i\epsilon) y_1 (1 - y_2) y_2}$$



$$\frac{1}{3} \frac{\mathcal{V}}{(x_1 + i\epsilon) (x_2 + i\epsilon) (2\xi - x_1 + i\epsilon) x_3 y_1 y_2 (1 - y_3)}$$

$$\mathcal{M}^\mu = -ie_p \bar{v}(k, \lambda) \gamma^\mu \gamma^5 u(p, s) \frac{f_N^2}{2f_\pi} \frac{(4\pi\alpha_S(Q^2))^2}{54 Q^4} \int_{1+\xi}^{-1+\xi} d^3x \int_0^1 d^3y \sum_{\alpha=1}^{14} T_\alpha(x_i, y_j) \quad (2)$$

$$\text{with } \mathcal{V}(x_j, y_i, \xi, t) = [V(y_i) - A(y_i)] \cdot [V_1(x_j, \xi, t) - A_1(x_j, \xi, t)] \quad \mathcal{T}(x_j, y_i, \xi, t) = -12[T(y_i)] \cdot [T_1(x_j, \xi, t)].$$

# $p \rightarrow \gamma$ : parametrisation

$\Rightarrow p \rightarrow \gamma$  (at Leading twist accuracy)

$\Rightarrow \Delta_T = 0$  : 4 TDAs

$(3 \times p(\downarrow) \rightarrow uud(\uparrow\uparrow\downarrow) + \gamma(\downarrow) \text{ and } p(\downarrow) \rightarrow uud(\downarrow\downarrow\downarrow) + \gamma(\uparrow))$

In the elm gauge  $\varepsilon.n = 0$  :

$$4\langle\gamma(p_\gamma)|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p(p_1,s)\rangle = f_N \times$$

$$\left[ V_1^\varepsilon(x_i, \xi, \Delta^2)(\not{p}C)_{\alpha\beta}(\not{\varepsilon}N^+)_\gamma \right.$$

$$+ A_1^\varepsilon(x_i, \xi, \Delta^2)(\not{p}\gamma^5 C)_{\alpha\beta}(\gamma^5 \not{\varepsilon}N^+)_\gamma$$

$$+ T_1^\varepsilon(x_i, \xi, \Delta^2)(\sigma_{p\mu}C)_{\alpha\beta}(\sigma^{\mu\varepsilon}N^+)_\gamma$$

$$\left. + T_2^\varepsilon(x_i, \xi, \Delta^2)(\sigma_{p\varepsilon}C)_{\alpha\beta}(N^+)_\gamma \right]$$

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$\Rightarrow \Delta_T \neq 0$  16 TDAs  $(\frac{1}{2} \times 2 \times (2 \times 2 \times 2) \times 2)$

$$4\langle\gamma(p_\gamma)|\epsilon^{ijk}u_\alpha^i(z_1n)u_\beta^j(z_2n)d_\gamma^k(z_3n)|p(p_1,s)\rangle = f_N \times$$

$$\left[ V_1^T(\varepsilon.\Delta_T)(\not{p}C)_{\alpha\beta}(N^+)_\gamma + V_1^\varepsilon(\not{p}C)_{\alpha\beta}(\not{\varepsilon}N^+)_\gamma + V_2^T(\varepsilon.\Delta_T)(\not{p}C)_{\alpha\beta}(\not{\Delta}_T N^+)_\gamma + V_2^\varepsilon(\not{p}C)_{\alpha\beta}(\sigma^{\Delta_T\varepsilon}N^+)_\gamma + \right.$$

$$A_1^T(\varepsilon.\Delta_T)(\not{p}\gamma^5 C)_{\alpha\beta}(\gamma^5 N^+)_\gamma + A_1^\varepsilon(\not{p}\gamma^5 C)_{\alpha\beta}(\gamma^5 \not{\varepsilon}N^+)_\gamma + A_2^T(\varepsilon.\Delta_T)(\not{p}\gamma^5 C)_{\alpha\beta}(\gamma^5 \not{\Delta}_T N^+)_\gamma + A_2^\varepsilon(\not{p}\gamma^5 C)_{\alpha\beta}(\gamma^5 \sigma^{\Delta_T\varepsilon}N^+)_\gamma +$$

$$T_1^T(\varepsilon.\Delta_T)(\sigma_{p\mu}C)_{\alpha\beta}(\gamma^\mu N^+)_\gamma + T_1^\varepsilon(\sigma_{p\mu}C)_{\alpha\beta}(\sigma^{\mu\varepsilon}N^+)_\gamma + T_2^T(\varepsilon.\Delta_T)(\sigma_{p\mu}C)_{\alpha\beta}(\sigma^{\mu\Delta_T}N^+)_\gamma + T_2^\varepsilon(\sigma_{p\varepsilon}C)_{\alpha\beta}(N^+)_\gamma +$$

$$\left. T_3^T(\varepsilon.\Delta_T)(\sigma_{p\Delta_T}C)_{\alpha\beta}(N^+)_\gamma + T_3^\varepsilon(\sigma_{p\Delta_T}C)_{\alpha\beta}(\not{\varepsilon}N^+)_\gamma + T_4^T(\varepsilon.\Delta_T)(\sigma_{p\Delta_T}C)_{\alpha\beta}(\not{\Delta}_T N^+)_\gamma + T_4^\varepsilon(\sigma_{p\varepsilon}C)_{\alpha\beta}(\not{\Delta}_T N^+)_\gamma \right]$$

## Conclusions

- ⇒ **Transition Distribution Amplitudes**  
give new information on hadrons
- ⇒ **Need non-perturbative inputs**
- ⇒ **Need precise data expected from**
  - ⇒ **GSI**
  - ⇒ **JLab**
  - ⇒ **Hermes**
  - ⇒ ***B*-factories**