



The Abdus Salam
International Centre for Theoretical Physics



SMR.1751 - 60

Fifth International Conference on
PERSPECTIVES IN HADRONIC PHYSICS
Particle-Nucleus and Nucleus-Nucleus Scattering at Relativistic Energies

22 - 26 May 2006

**Final state interaction in $3\text{He}(e'p)d$ and $4\text{He}(e, e'p) 3\text{H}$
within a generalized eikonal approximation**

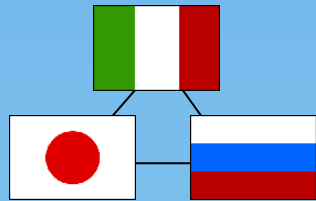
Hiko MORITA
Universita' di Perugia
Dipartimento di Fisica
Via A. Pascoli
06123 Perugia
ITALY

These are preliminary lecture notes, intended only for distribution to participants

ICTP Workshop, Trieste, Italy 23 May, 2006

Hadron Propagation in the Medium

— The Exclusive Process
 $A(e,e'p)B$ in few-nucleon
systems —



H. Morita for

< Perugia-Dubna-Sapporo Collab. >

C. Ciofi degli Atti, M. Alvioli, V. Palli, I. Chiara, Univ. of Perugia

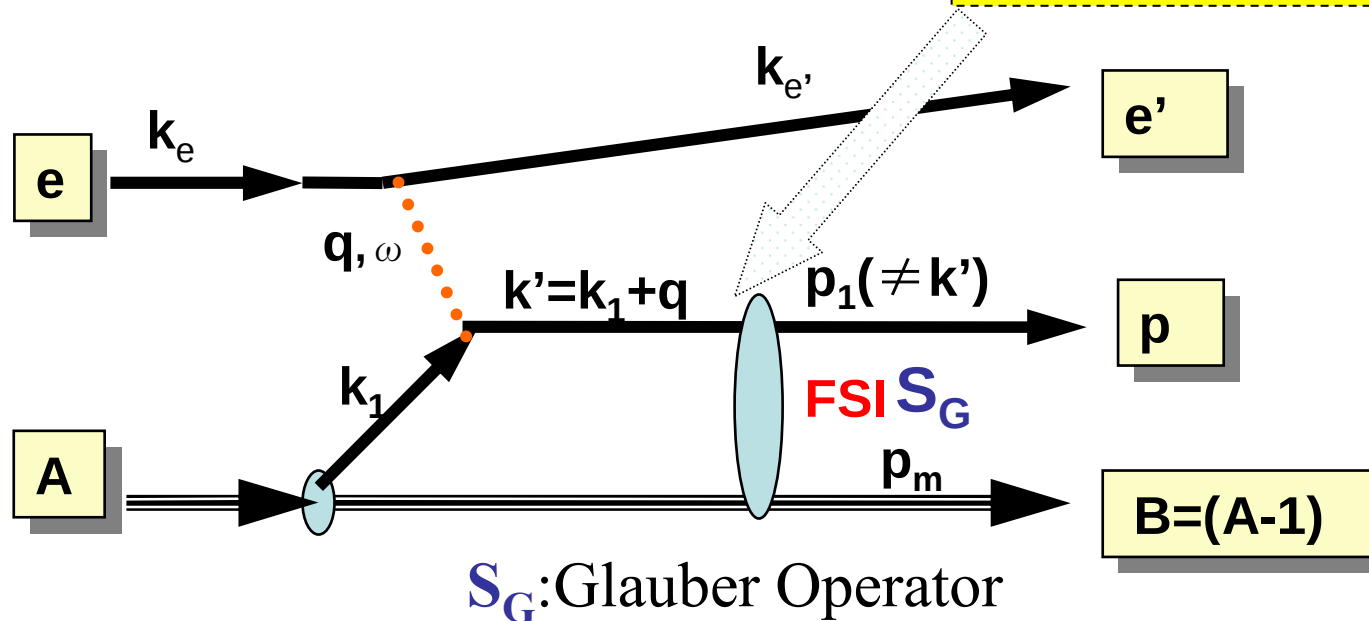
L.P. Kaptari, BLTP JINP, Dubna

H. Morita, Sapporo Gakuin Univ., Sapporo

1. Introduction

$A(e, ep')B$ Reaction

How can we describe the p propagation in medium?



< Subject of this talk >

Study of the (knocked out) p propagation in the process of ${}^3\text{He}(e, e'p)d(pn)$ and ${}^4\text{He}(e, e'p){}^3\text{H}$ reaction.

Outline of my talk

1. Introduction
2. Framework of the calculation for the $A(e,e'p)B$ Reaction -Generalized Eikonal Approximation-
3. Results of ${}^3\text{He}(e,e'p){}^2\text{H}(pn)$ Reaction
4. Results of ${}^4\text{He}(e,e'p){}^3\text{H}$ Reaction
5. Finite Formation Time Effect on ${}^4\text{He}(e,e'p){}^3\text{H}$ Reaction -at higher Q^2 region-
6. Summary

2. Framework of the Calculation for the $A(e,e'p)B$ Reaction

< Cross Section of $A(e,e'p)B$ >

* We use Factorization Ansatz.
(here only unpolarized cross section will be discussed)

$$\frac{d^6\sigma}{d\omega d\Omega_e dp d\Omega_p} = K \sigma_{ep} S_D(p_m, E_m)$$

e-N cross section

nuclear distorted spectral function

If “**B**”(recoil system) is bound state

$$\frac{d^5\sigma}{d\omega d\Omega_e d\Omega_p} = K' \sigma_{ep} |\Phi_D(p_m)|^2$$

nucleon distorted momentum distribution

distorted by FSI

Nuclear Distorted Spectral Function in ${}^3\text{He}(e,e'p){}^2\text{H}(pn)$ process

C. Ciofi degli Atti, L.P. Kaptari, *Phys. Rev.* **C71**, 024005 (2005)

S_G : Glauber operator

${}^3\text{He}(e,e'p){}^2\text{H}$

$$S_D(p_m, E_m) = \sum_f \left| \Psi_D^{M_2^+}(\mathbf{r}) S_G(\mathbf{r}, \boldsymbol{\rho}) \Psi_{{}^3\text{He}}^{M_3}(\mathbf{r}, \boldsymbol{\rho}) d\boldsymbol{\rho} d\mathbf{r} \right|^2$$

$$\times \delta(E_m - (E_D - E_{{}^3\text{He}}))$$

$\Psi_{{}^3\text{He}}^{M_3}$: Pisa Group's w.f. with AV18 pot.

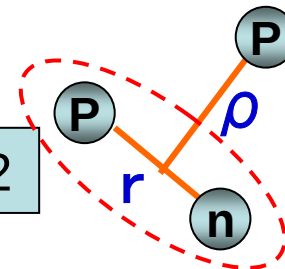
A. Kievsky et al., *Nucl. Phys.* **A551**(1993) 241

${}^3\text{He}(e,e'p)pn$

$$S_D(p_m, E_m) = \sum_f \int \frac{d^3\mathbf{t}}{(2\pi)^3} \left| \int e^{i\mathbf{p}\cdot\mathbf{p}_m} \chi_{\frac{1}{2}s_1}^+ \Psi_{np}^{\mathbf{t}^+}(\mathbf{r}) S_G(\mathbf{r}, \boldsymbol{\rho}) \Psi_{{}^3\text{He}}^{M_3}(\mathbf{r}, \boldsymbol{\rho}) d\boldsymbol{\rho} d\mathbf{r} \right|^2$$

$$\times \delta(E_m - \left(\frac{\mathbf{t}^2}{M_N} - E_{{}^3\text{He}} \right))$$

$\mathbf{t} = (\mathbf{P}_p - \mathbf{P}_n)/2$



Glauber Operator S_G

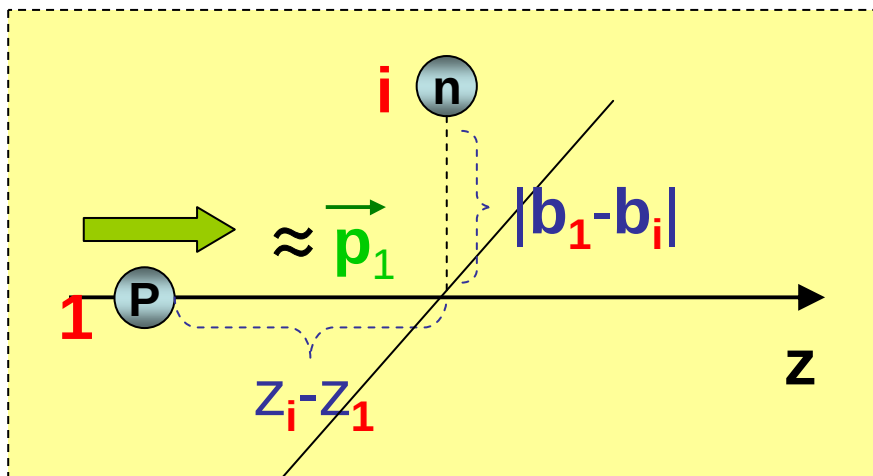
1st nucleon $\rightarrow$ Struck proton

$$S_G = \prod_{i=2}^3 G(1i), \quad G(1i) = 1 - \theta(Z_i - Z_1) \Gamma(\mathbf{b}_1 - \mathbf{b}_i),$$

$$\Gamma(\mathbf{b}) = \frac{\sigma_{\text{tot}} (1 - i\alpha)}{4\pi b_0^2} \exp(-\mathbf{b}^2 / 2b_0^2)$$

Usual Parameterization

$\sigma_{\text{tot}} \leftarrow$ Particle Data Group (<http://pdg.lbl.gov/>)
 $\alpha \leftarrow$ Partial-Wave Analysis Facility
(<http://lux2.phys.va.gwu.edu/>)



<Choice of Z-axis>

$\mathbf{p}_1 \parallel z$

ejected proton's Momentum

not $\mathbf{q}$!!

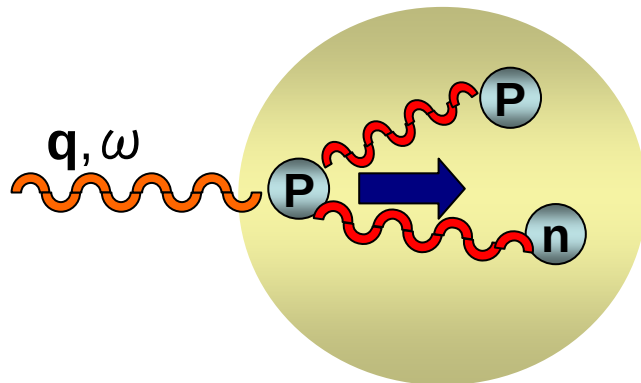


Generalized Eikonal Approximation

L.L.Frankfurt et al., *Phys. Rev.* **C56**, 1124(1997) and M.M. Sargsian et al, *Phys. Rev.* **C71** 044614(2005)

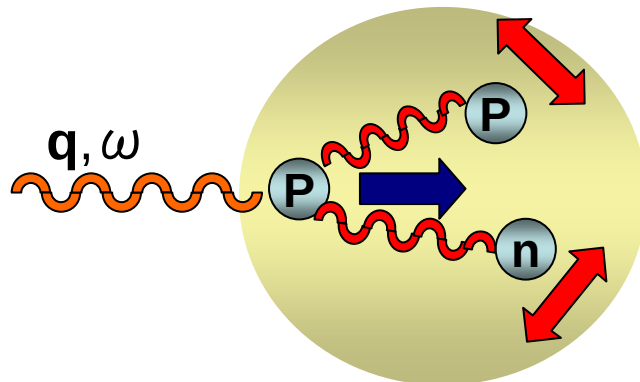
C. Ciofi degli Atti, L.P. Kaptari, *Phys. Rev.* **C71**, 024005 (2005)

Conventional Glauber Approximation



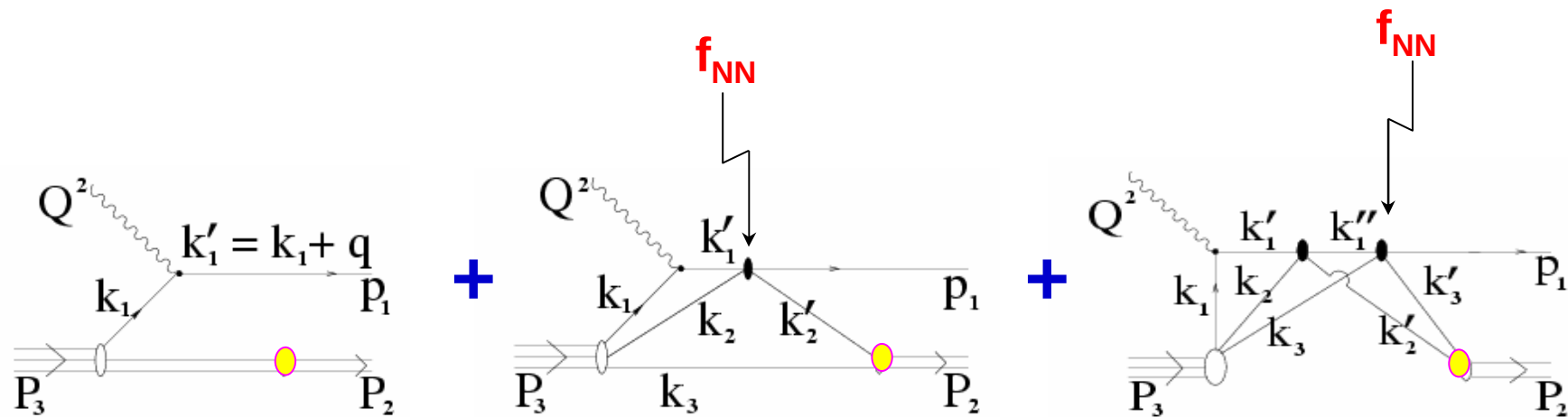
Frozen Approximation

Generalized Eikonal Approximation



Consider the Fermi motion

Diagrammatic representation of the process ${}^3\text{He}(e,e'p){}^2\text{H}(pn)$



PWIA
 $\mathfrak{T}^{(0)}$: **IA** Amplitude

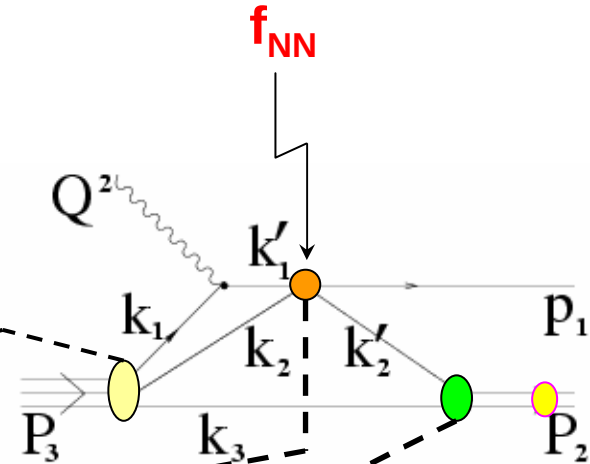
Single resc.
 $\mathfrak{T}^{(1)}$: **Single** Resc. Amp.

Double resc.
 $\mathfrak{T}^{(2)}$: **Double** Resc. Amp.

$$S_D(p_m, E_m) = \frac{1}{2J_{{}^3\text{He}} + 1} \sum_f \left| \sum_{n=0}^2 \mathfrak{T}^{(n)}(M_f, s_1) \right|^2 \delta(E_m - (E_2^f - E_{{}^3\text{He}}))$$

Single Rescattering Amplitude $\mathfrak{T}^{(1)}$

$$S_D(p_m, E_m) = \frac{1}{2J_{^3\text{He}} + 1} \sum_f \left| \sum_{n=0}^2 \mathfrak{T}^{(n)}(M_f, s_1) \right|^2 \delta(E_m - (E_2^f - E_{^3\text{He}}))$$



$$\mathfrak{T}^{(1)} = \int d\tau_{23} \begin{array}{|c|c|c|} \hline G_{\text{He} \rightarrow \text{l}(23)}(k_1, k_2, k_3, s_1, s_2, s_3) & f_{\text{NN}}(p_1 - k_1') & G_{(23) \rightarrow f}^+(k_2', k_3, s_2, s_3) \\ \hline (k_1^2 - M_N^2) & k_1'^2 - M_N^2 & (k_1'^2 - M_N^2) \\ \hline \end{array}$$

$$\langle s_1, s_2, s_3 | \Psi_{^3\text{He}}^{M_3}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \rangle$$

$$\langle s_2, s_3 | \Psi_{23}^{M_{23}}(\mathbf{k}_2, \mathbf{k}_3) \rangle$$

$$\mathfrak{T}^{(1)} \approx \int \frac{d^3\kappa}{(2\pi)^3} \begin{array}{|c|c|c|} \hline \langle s_1 | \Psi_{^3\text{He}}^{M_3}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \rangle & \frac{f_{\text{NN}}(\kappa_{\perp}) / 4M_N |\mathbf{p}_1|}{\kappa_z + \Delta_z + i\varepsilon} & \Psi_{(23)}^f(\mathbf{k}_2', \mathbf{k}_3; S_{23}) \\ \hline \end{array}$$

$$\Delta_z = \frac{E_{\mathbf{k}_1+\mathbf{q}} + E_{\mathbf{p}_1}}{2|\mathbf{p}_1|} E_m \approx \frac{E_{\mathbf{p}_1}}{|\mathbf{p}_1|} E_m$$

Effect of residual nucleon's Fermi motion.

Single Rescattering Amplitude $\mathfrak{T}^{(1)}$ (cont.)

Using the coordinate space representation of the propagator

$$\mathfrak{T}^{(1)} \approx \int \frac{d^3 \mathbf{k}}{(2\pi)^3} \left\langle s_1 \left| \Psi_{^3\text{He}}^{M_3}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \right\rangle \frac{f_{NN}(\kappa_{\perp}) / 4M_N |\mathbf{p}_1|}{\kappa_z + \Delta_z + i\varepsilon} \Psi_{(23)}^f(\mathbf{k}_2', \mathbf{k}_3; S_{23})$$

$$\frac{1}{\kappa_z + \Delta_z + i\varepsilon} = -i \int \theta(z) e^{i(\kappa_z + \Delta_z) \cdot z} dz$$

Finally we get

$$S_D^{(0+1)}(p_m, E_m) = \sum_f \left| \Psi_{23}^{f+}(\mathbf{r}) \left(S^{(0)}(\mathbf{r}, \boldsymbol{\rho}) + S_{GEA}^{(1)}(\mathbf{r}, \boldsymbol{\rho}) \right) \Psi_{^3\text{He}}^{M_3}(\mathbf{r}, \boldsymbol{\rho}) d\boldsymbol{\rho} d\mathbf{r} \right|^2 \\ \times \delta(E_m - (E_{23}^f - E_{^3\text{He}}))$$

$$S^{(0)}(\mathbf{r}, \boldsymbol{\rho}) = 1$$

$$S_{GEA}^{(1)}(\mathbf{r}, \boldsymbol{\rho}) = - \sum_{i=2}^3 \theta(z_i - z_1) e^{i\Delta_z(z_i - z_1)} \Gamma(\mathbf{b}_1 - \mathbf{b}_i)$$

GEA Operator

Double Rescattering Case

$$S_{GEA}^{(2)}(\mathbf{r}, \boldsymbol{\rho}) = [\theta(z_2 - z_1)\theta(z_3 - z_2)e^{-i\Delta_3(z_2 - z_1)}e^{-i(\Delta_3 - \Delta_z)(z_3 - z_1)} + \theta(z_3 - z_1)\theta(z_2 - z_3)e^{-i\Delta_2(z_3 - z_1)}e^{-i(\Delta_2 - \Delta_z)(z_2 - z_1)}] \Gamma(\Delta_z, \mathbf{b}_1 - \mathbf{b}_2) \Gamma(\Delta_z, \mathbf{b}_1 - \mathbf{b}_3)$$

$$\Delta_i = \frac{q_0}{|\mathbf{q}|} (E_{\mathbf{k}_i'} - E_{\mathbf{p}_i}) \quad \Gamma(\Delta_z, \mathbf{b}_1 - \mathbf{b}_i) \equiv e^{i\Delta_z} \Gamma(\mathbf{b}_1 - \mathbf{b}_i)$$

Ref) L.L.Frankfurt et al., *Phys. Rev.* **C56**, 1124(1997)

In the following calculation, we put

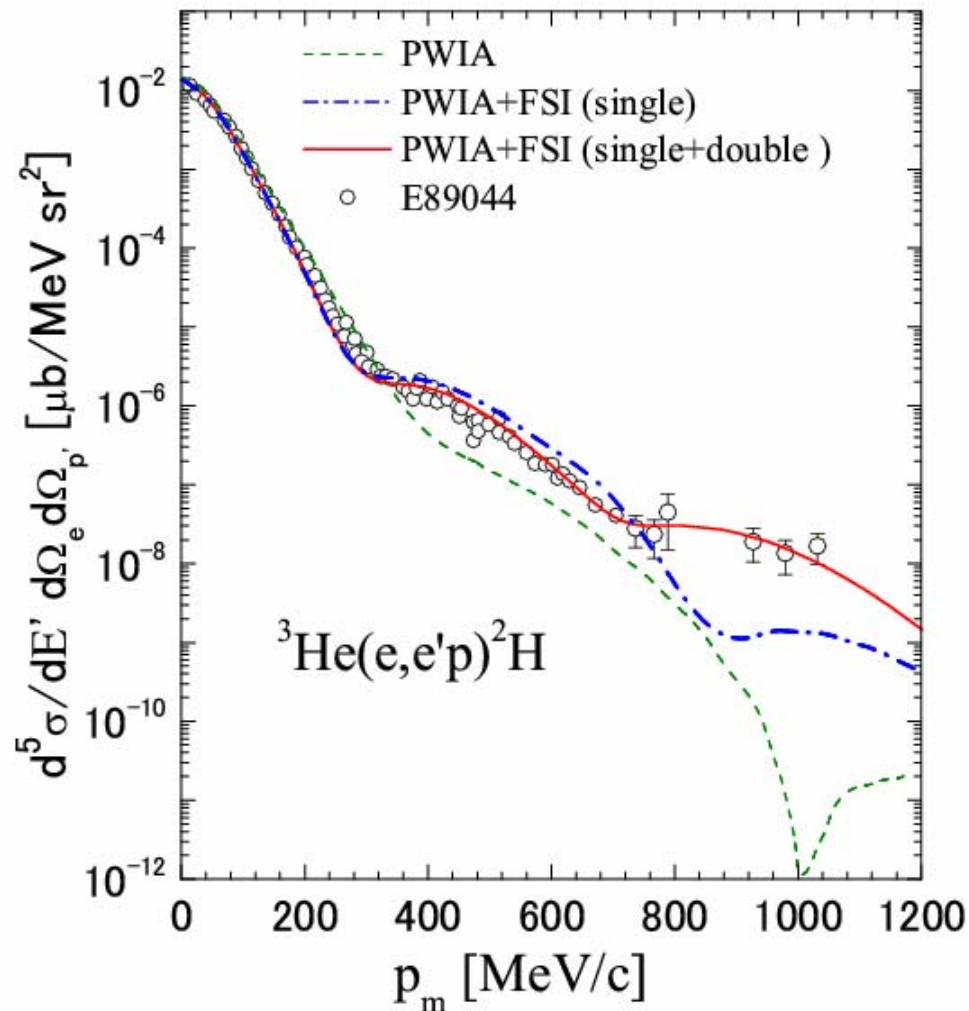
$$\Delta_i = \Delta_z / 2 \quad \text{for the double rescattering}$$

Finally we get the distorted spectral function

$$S_D(p_m, E_m) = \sum_f \left| \Psi_{23}^{f+}(\mathbf{r}) (S^{(0)} + S_{GEA}^{(1)} + S_{GEA}^{(2)}) \Psi_{^3He}^{M_3}(\mathbf{r}, \boldsymbol{\rho}) d\boldsymbol{\rho} d\mathbf{r} \right|^2 \times \delta(E_m - (E_{23}^f - E_{^3He}))$$

3.Results of $^3\text{He}(e,e'p)^2\text{H}(\text{pn})$ Reaction

C. Ciofi degli Atti, L.P. Kaptari, *Phys. Rev. Lett.* **95**, 052502 (2005)



Data: JLab E89044

$$Q^2 \sim 1.55(\text{GeV}/c)^2, x=1$$

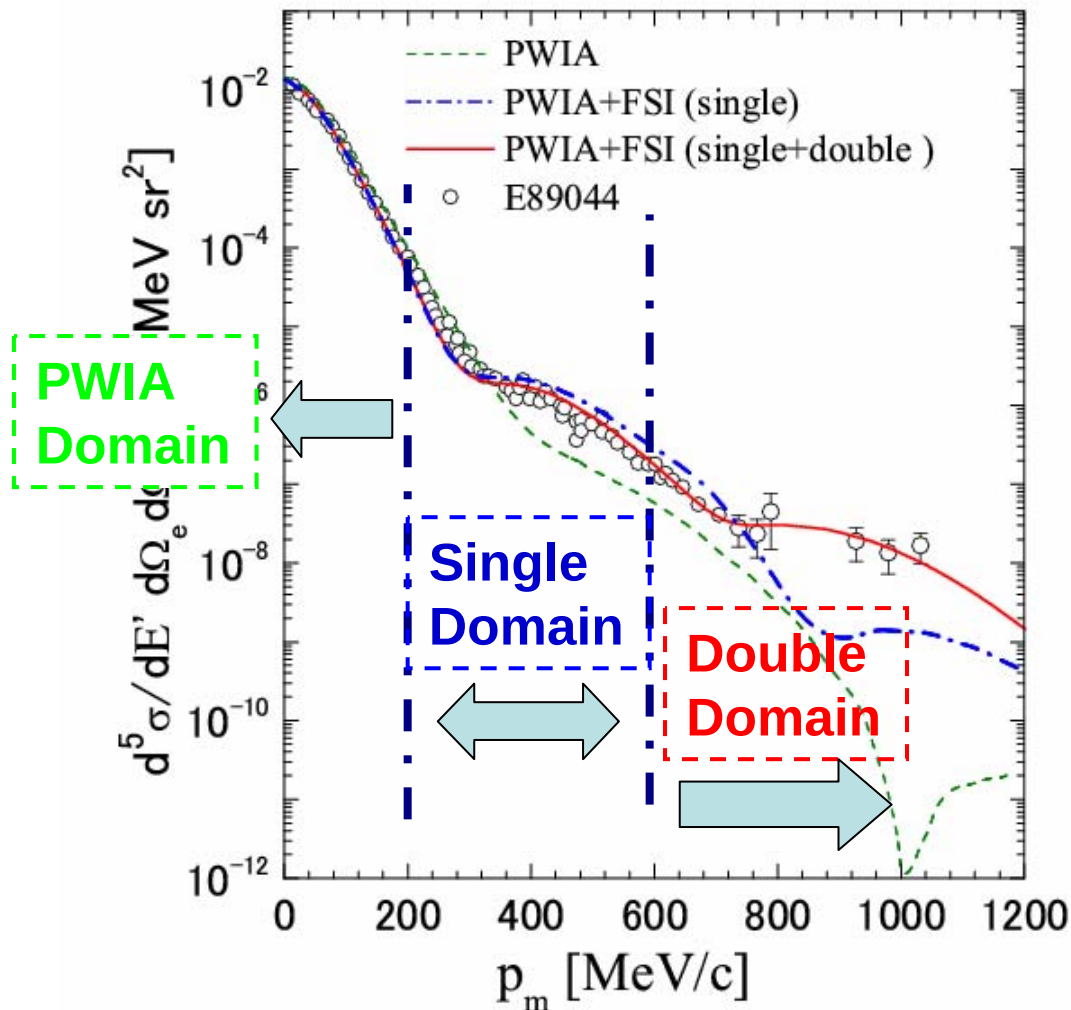
M.M. Rvachev et al., *Phys. Rev. Lett.* **94**(2005) 192302

GEA(GA) Calculation reproduces the data almost perfectly.

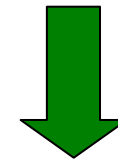
$$|d^5\sigma(\text{GEA}) - d^5\sigma(\text{GA})| \approx \text{a few \%}$$

Multiple Scattering Contributions

C. Ciofi degli Atti, L.P. Kaptari, *Phys. Rev. Lett.* **95**, 052502 (2005)



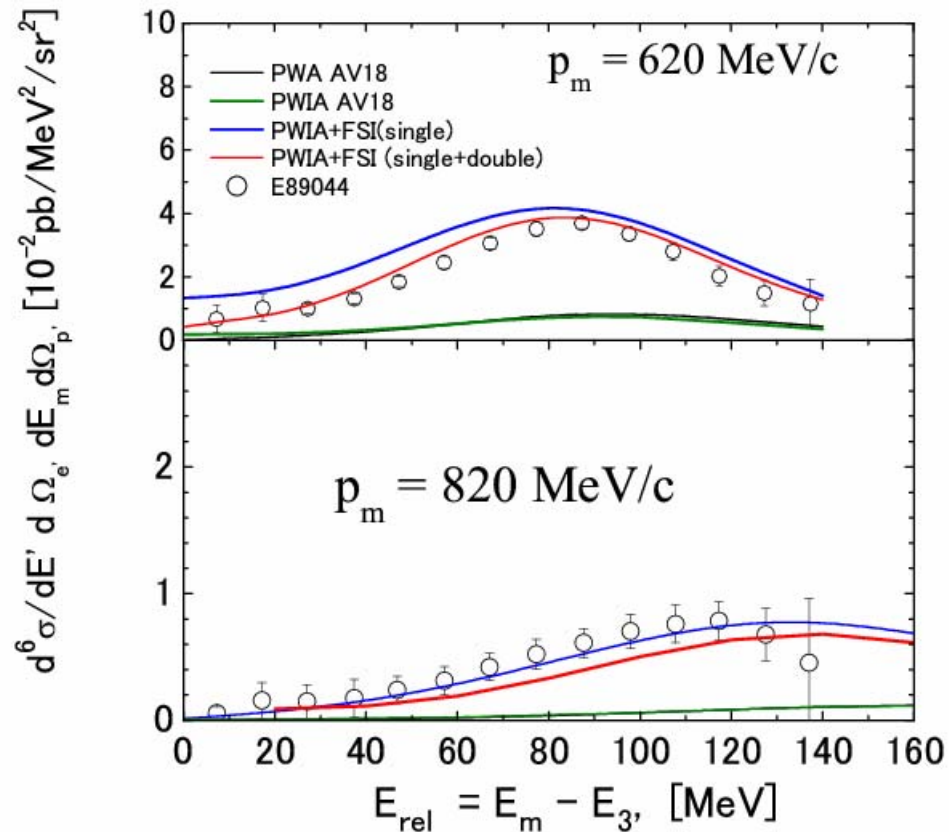
$d\sigma(p_m)$ has
different (three)
slopes



different Multiple
Scattering
Component

Results of $^3\text{He}(e,e'p)pn$

C. Ciofi degli Atti, L.P. Kaptari, *Phys. Rev. Lett.* **95**, 052502 (2005)



Data: JLab E89044

$$Q^2 \sim 1.55 (\text{GeV}/c)^2, x=1$$

F. Benmokhtav et al., *Phys. Rev. Lett.* **94**(2005) 082325

GEA(GA) Calculation
reproduces the data quite
well.



4. Results of $^4\text{He}(e,e'p)^3\text{H}$ Reaction

< Extension to $^4\text{He}(e,e'p)^3\text{H}$ Reaction >

We extend the same calculation as ^3He -case to $^4\text{He}(e,e'p)^3\text{H}$ reaction

But, for the realistic wave function we adopted the **ATMS** method

ATMS method

M. Sakai et al., Prog.Theor.Phys.Suppl.56(1974)108.

H. Morita et al., Prog.Theor.Phys.78(1987)1117.



$\Psi_{^3\text{H}}, \Psi_{^4\text{He}}$:ATMS wave function
NN force :Reid Soft Core

Variational wave function

< Experimental Data >

JLab E97-111: B. Reitz et al., Eur. Phys. J. A S19(2004) 165

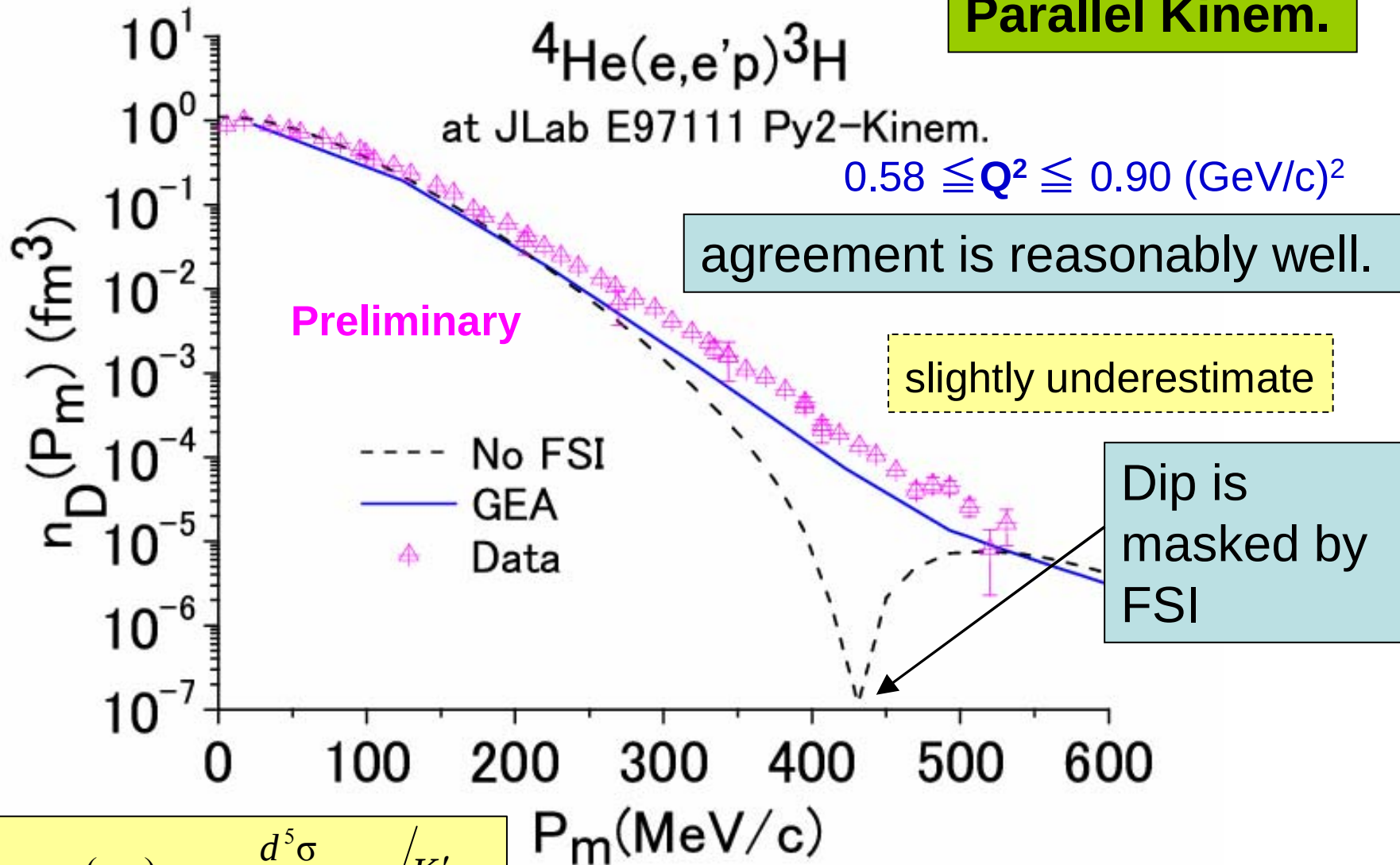
1. **Py2 Kinematics**—Parallel Kinematics

2. **CQ ω 2 Kinematics**—Perpendicular Kinematics



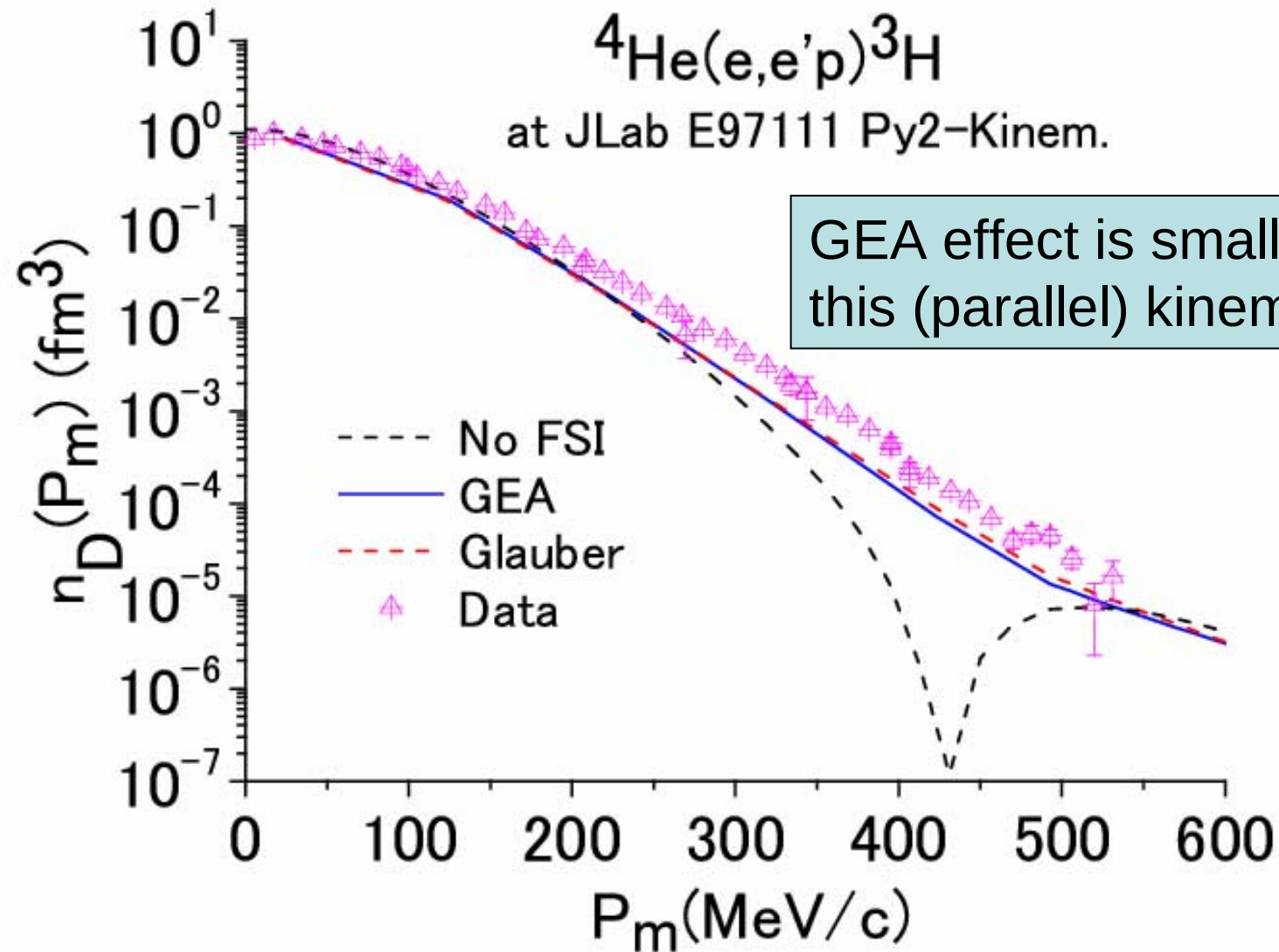
Results at Py2-Kinem.

Parallel Kinem.



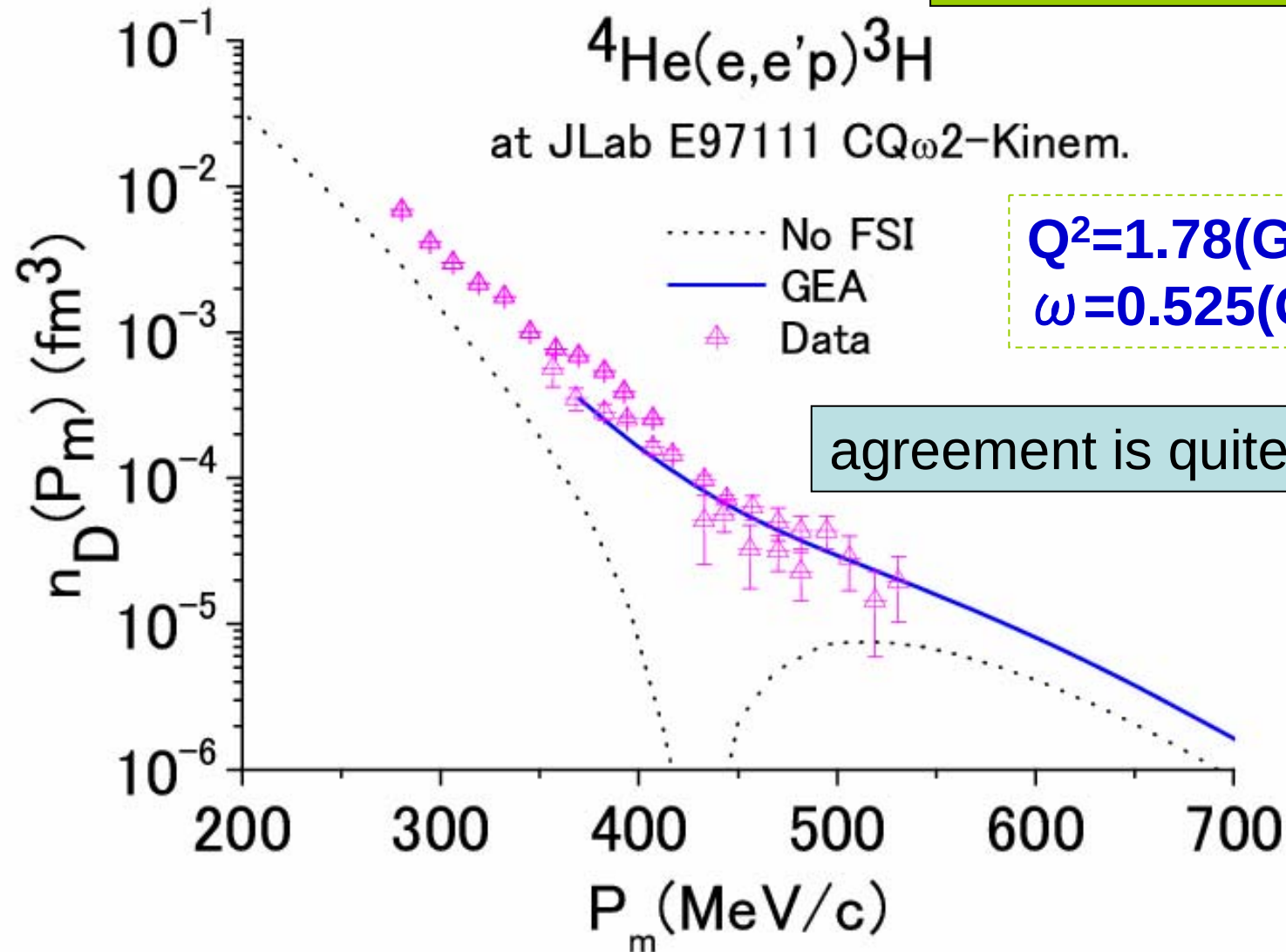
$$n_D(p_m) = \frac{d^5\sigma}{d\omega d\Omega_e d\Omega_p} / K' \sigma_{ep}$$

Effect of the GEA on GA

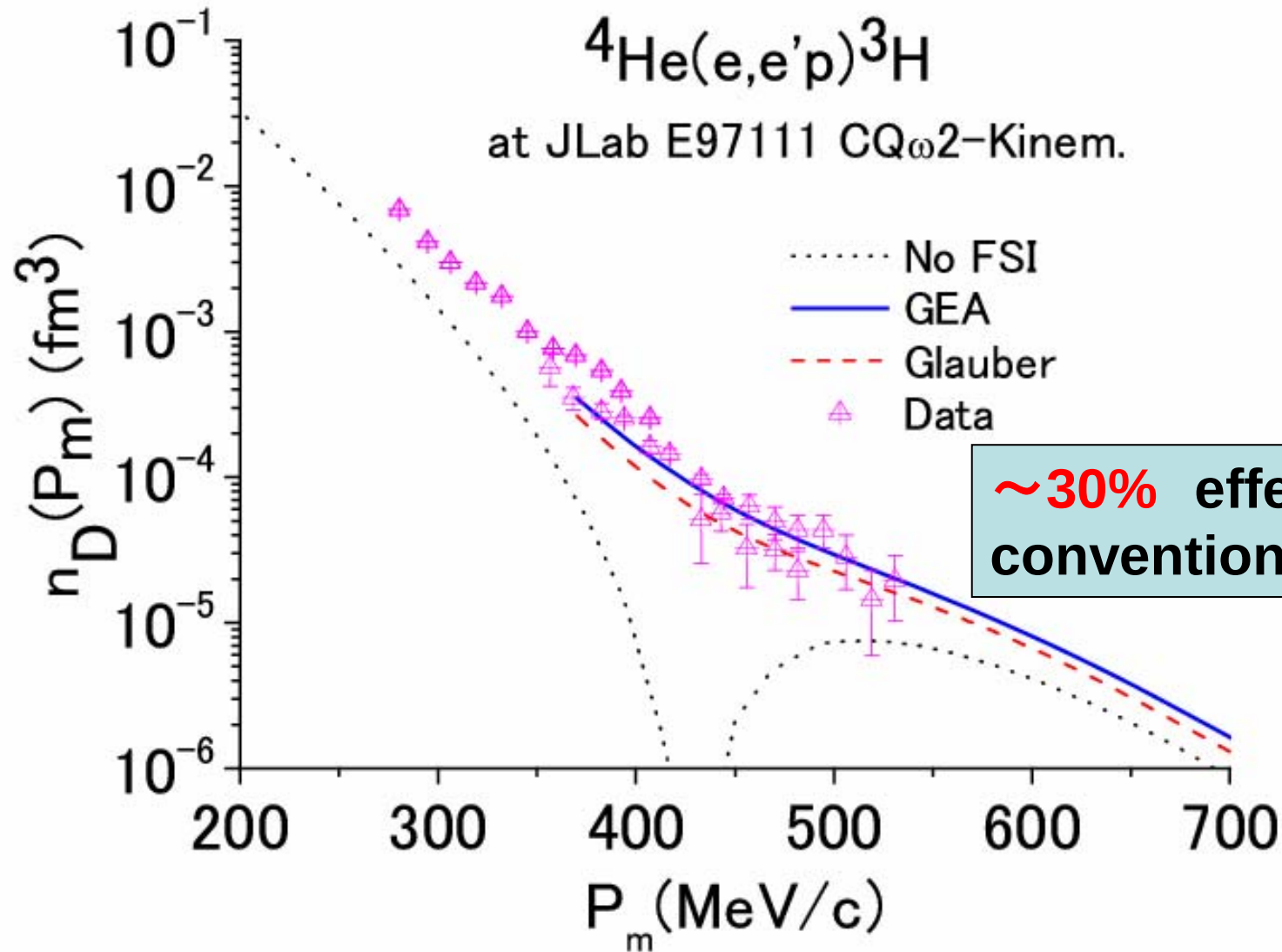


Results at CQ ω 2-Kinem.

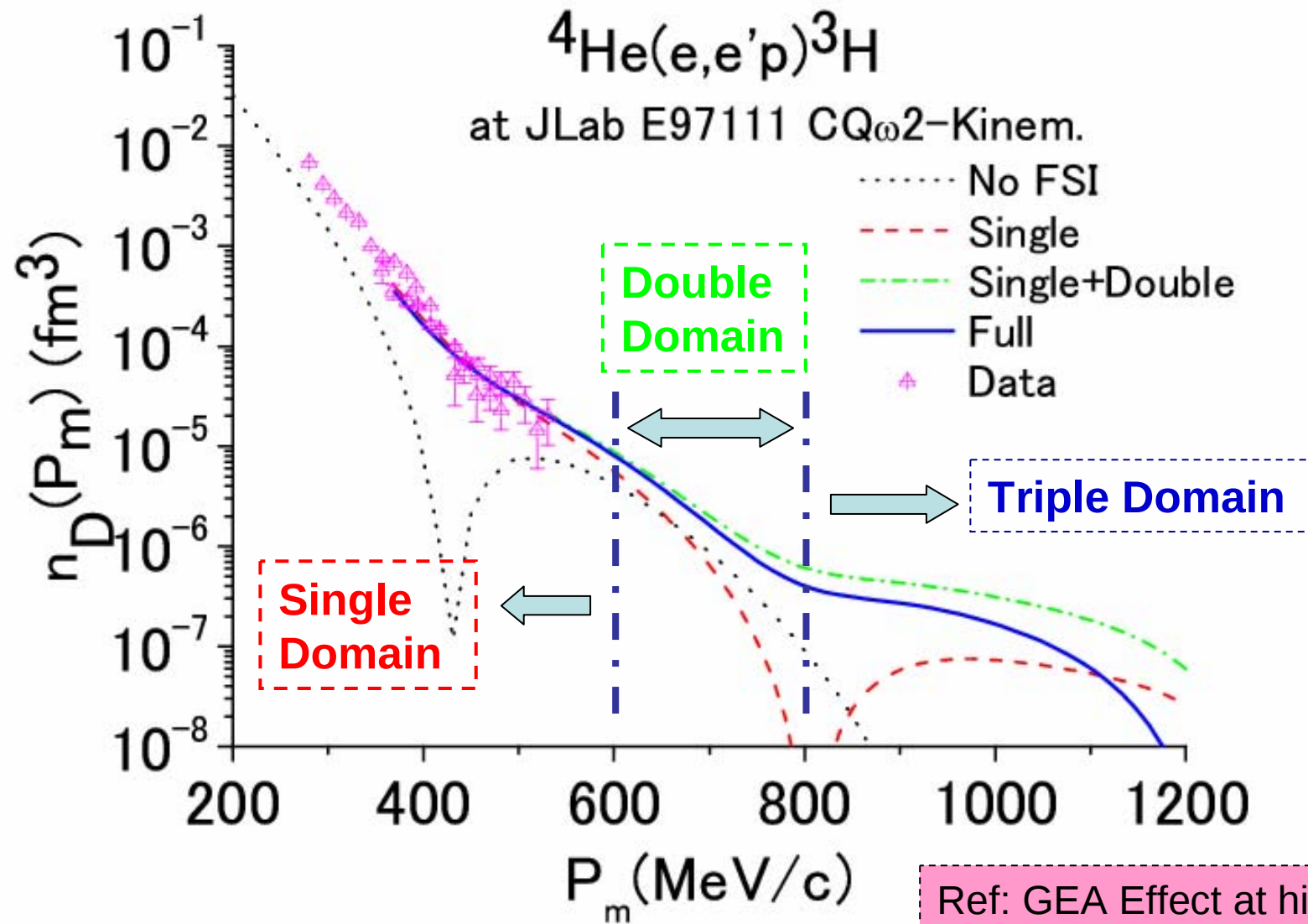
Perpendicular Kinem.



Effect of the GEA on GA

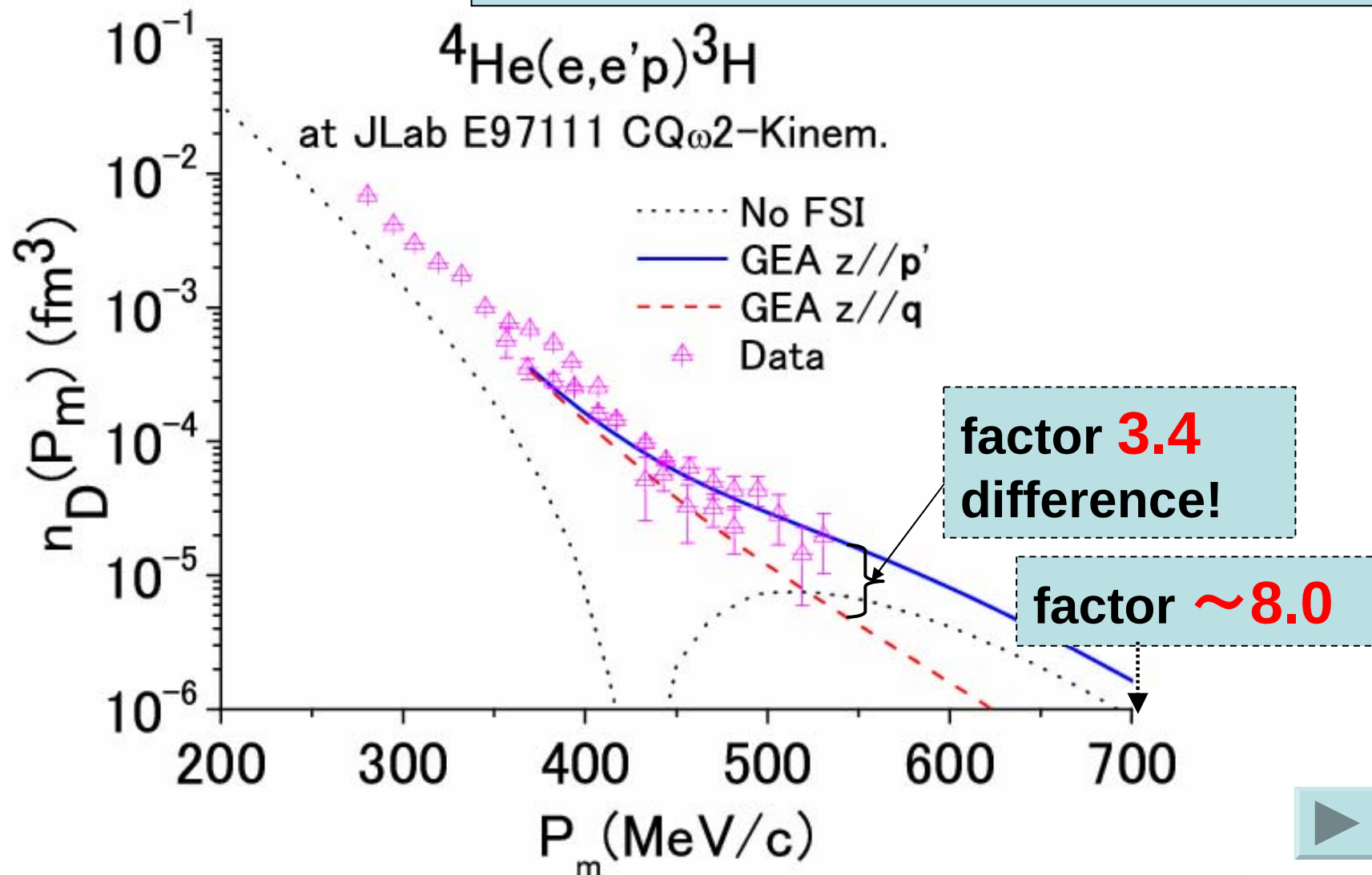


Multiple Scattering Contributions

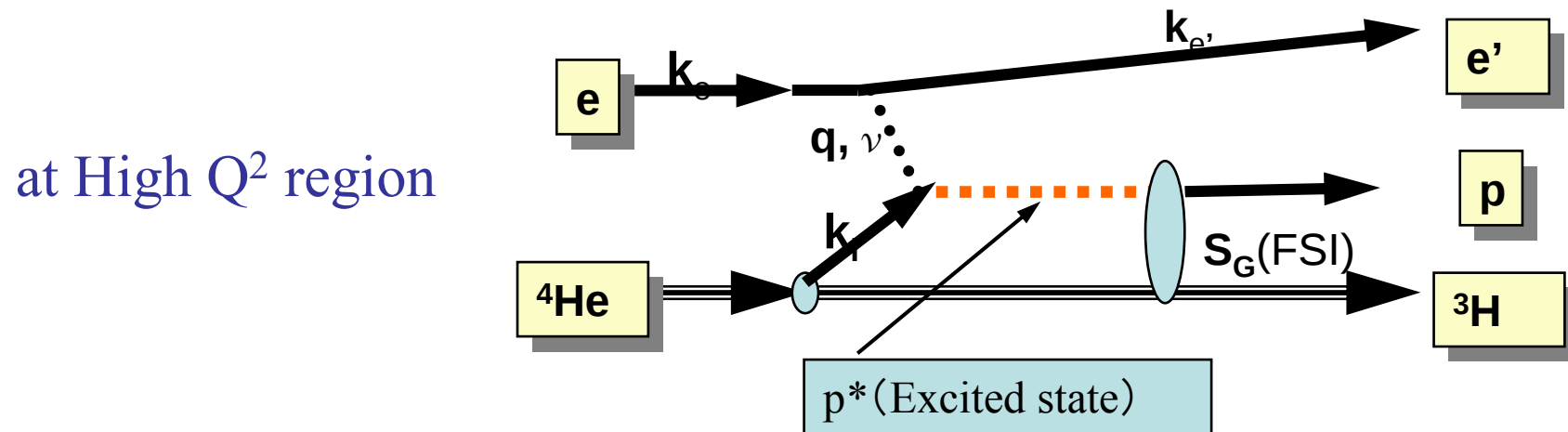


Comment on the choice of Z-axis

correct choice of z-axis is important!



5. Finite Formation Time Effect on ${}^4\text{He}(e,e'p){}^3\text{H}$ Reaction



One must take into account the effect of p^*



Finite Formation Time (**FFT**) effect



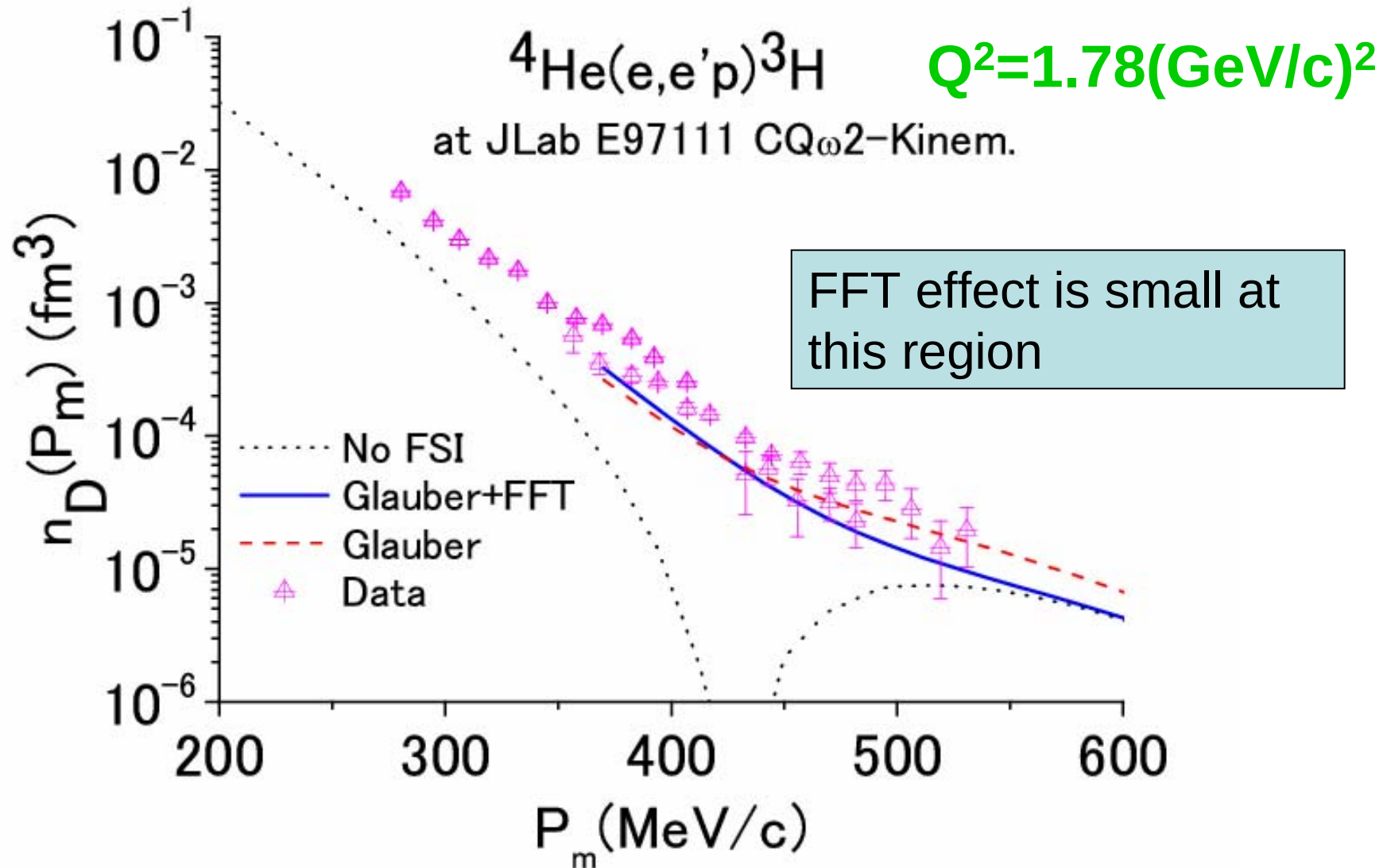
M.A.Braun et al. Phys. Rev. **C62**, 034606(2000)

$$S(\vec{r}_j) = 1 - \boxed{J(z_j - z_1)} \Gamma(\vec{b}_j - \vec{b}_1), \quad \boxed{J(z) = \mathcal{G}(z) \left(1 - \exp\left(-\frac{z}{l(Q^2)}\right)\right)}, \quad \boxed{\text{damping factor}}$$

$$l(Q^2) = \frac{Q^2}{xmM^2} \quad \boxed{\text{Formation length}}$$

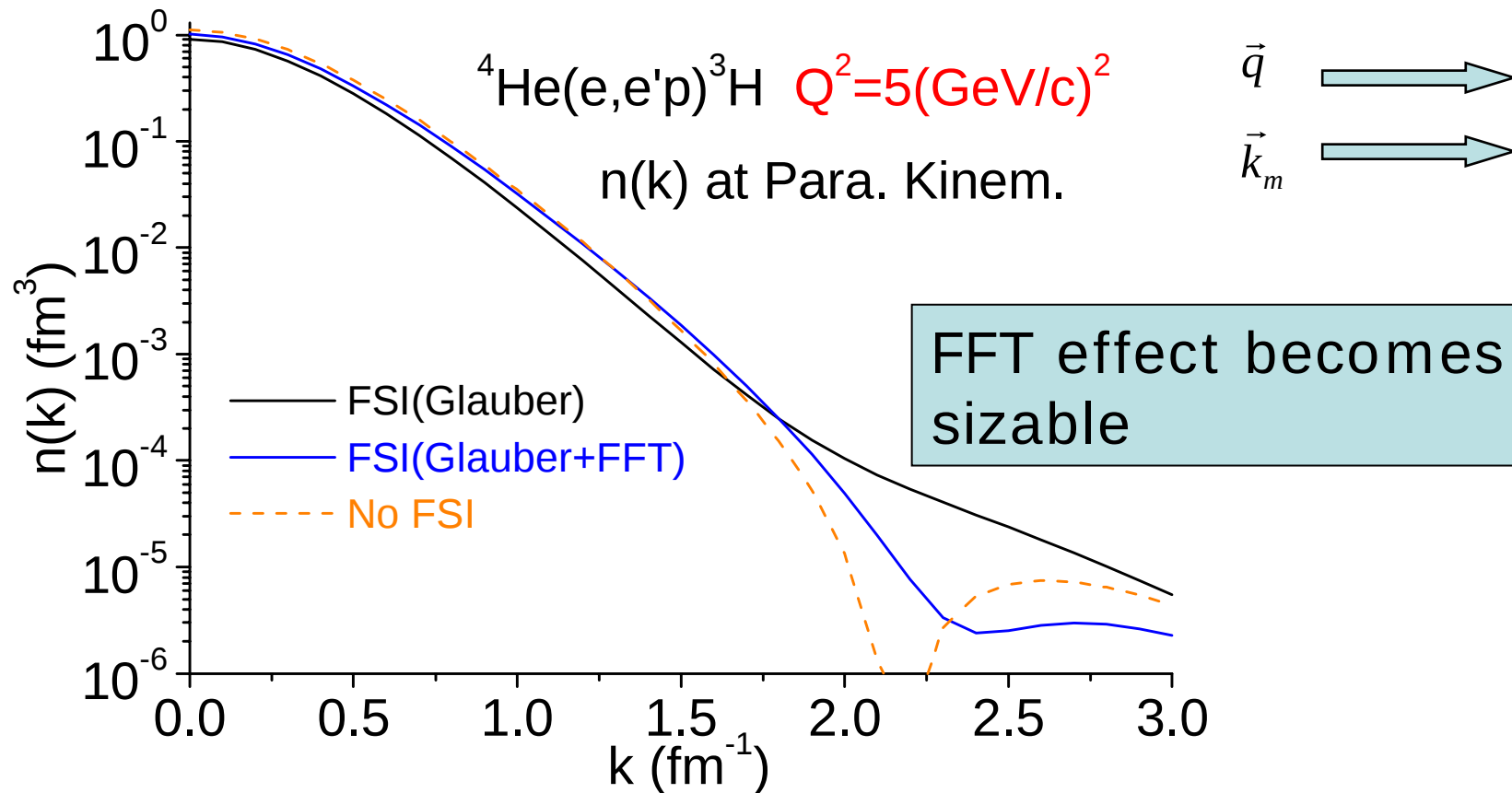
$Q^2 \rightarrow \text{higher, FSI} \rightarrow \text{weaker}$

Effect of the FFT

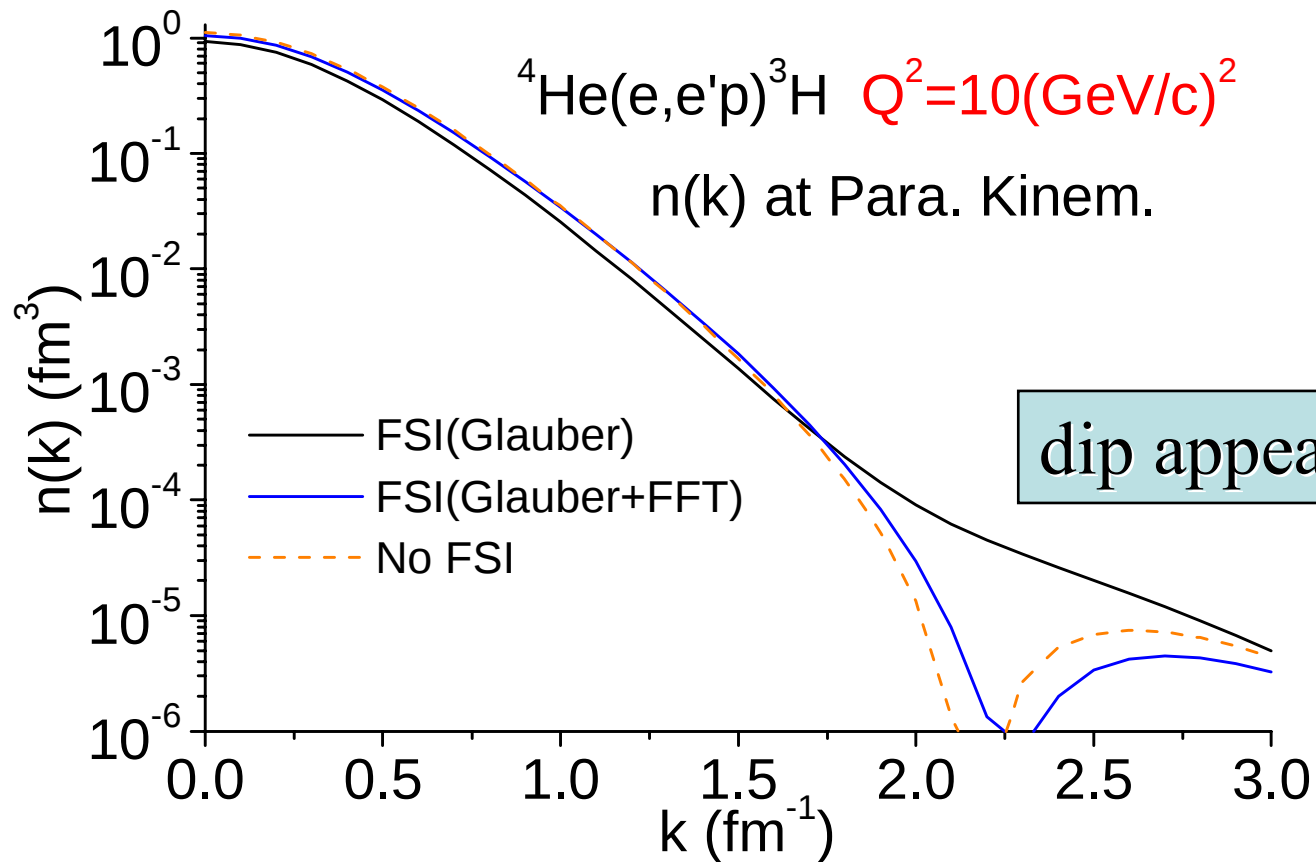


Para. Kinem. at $Q^2=5(\text{GeV}/c)^2$, $x=1$

Parallel Kinematics

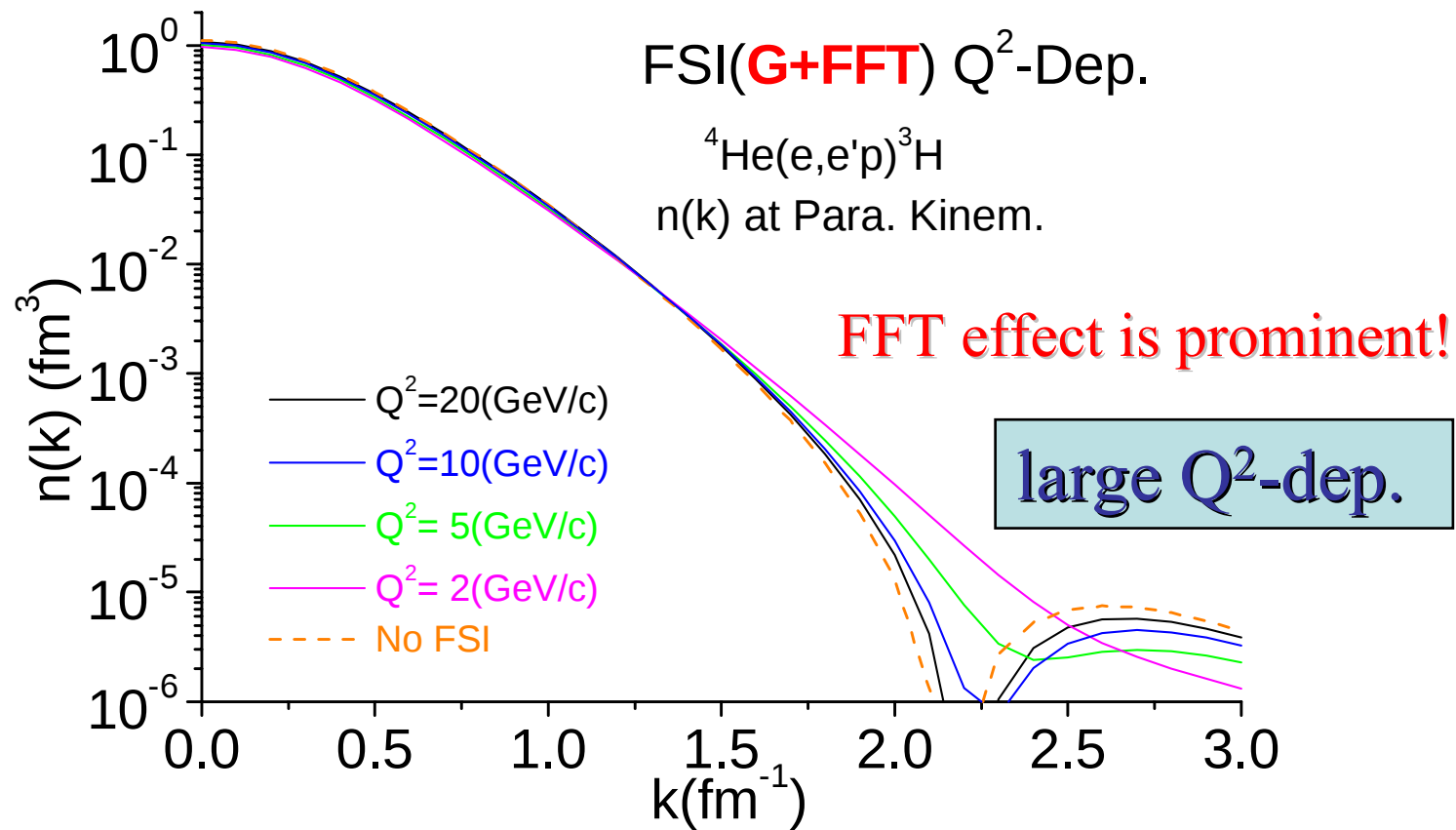


Q^2 -dep. -Parallel Kinem.-
at $Q^2=10(\text{GeV}/c)^2$

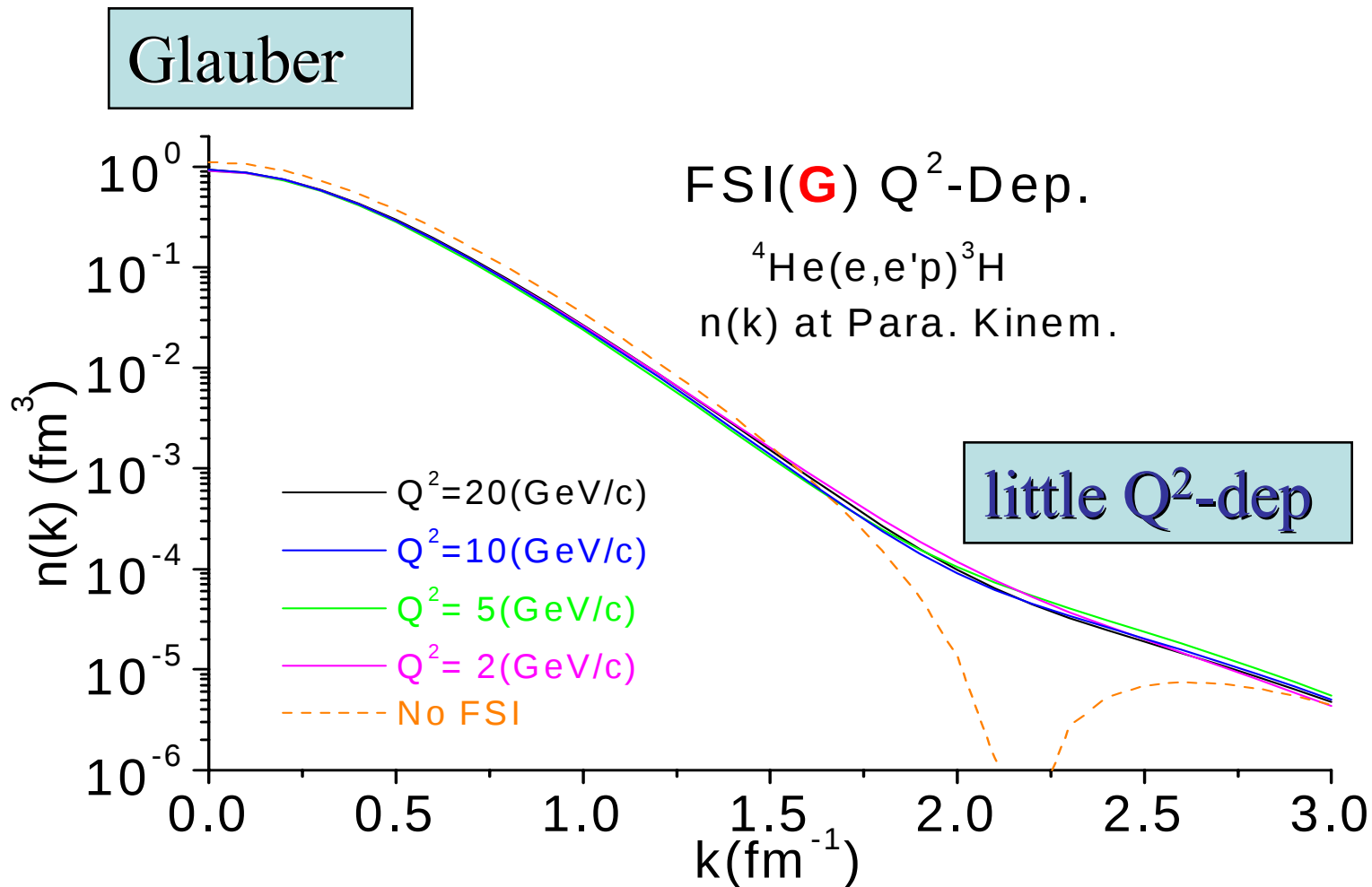


Q^2 -dep. -Parallel Kinem.- Glauber +FFT

Glauber + FFT

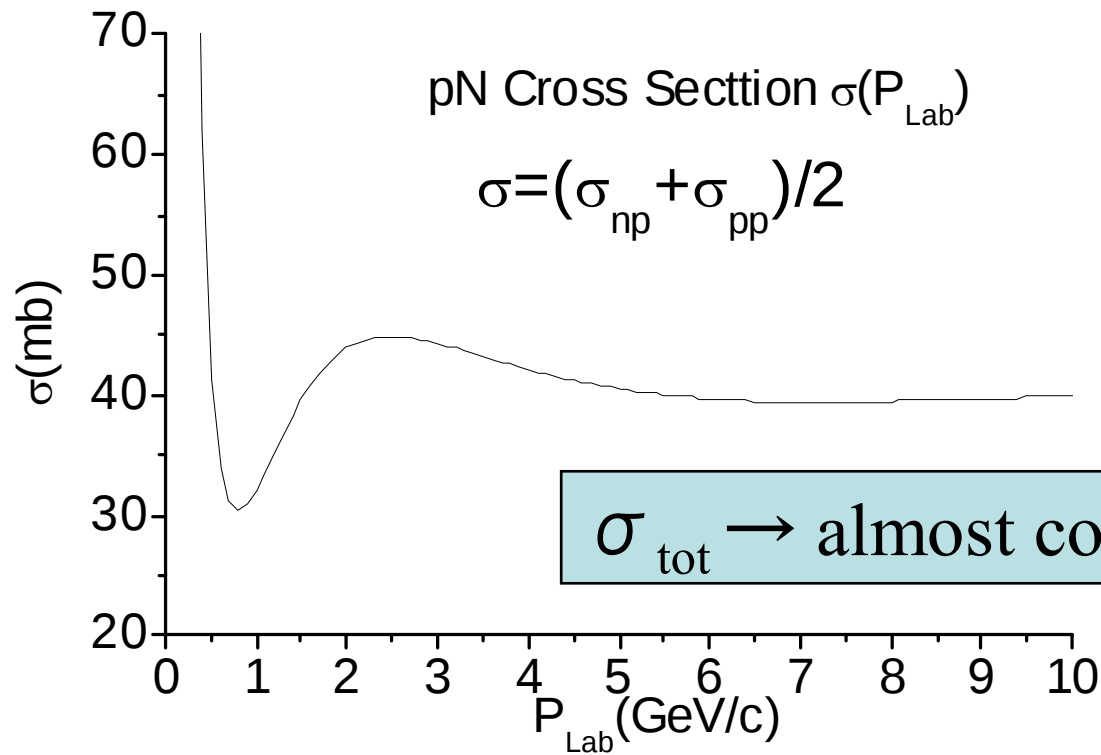
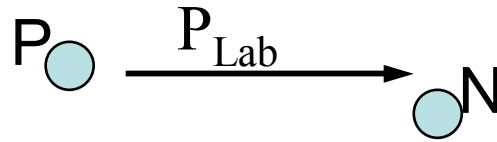


Q^2 -dep. -Parallel Kinem.- Glauber



P_{lab} -dep. of σ_{tot}

σ_{pN}



6. Summary

1. Ability of the GA/GEA to describe the FSI

- Without any free parameter, the data of $^3\text{He}(e,e'p)^2\text{H}(pn)$ and $^4\text{He}(e,e'p)^3\text{H}$ were **well reproduced** by the Glauber/GEA calculation.
- This means that in the energy-momentum range covered by the data, FSI (**propagation of knocked out proton in medium**) can be described within the GA/GEA.
- In the case of $^3\text{He}(e,e'p)^2\text{H}(pn)$, the **effect of GEA** on GA (conventional Glauber approximation) is **rather small** at considered kinematics.
- In the $^4\text{He}(e,e'p)^3\text{H}$ reaction it gives **$\sim 30\%$ effect** at (JLab E97-111) CQ $\omega 2$ kinematics.

Summary -2

2. Multiple Scattering Feature of the GA/GEA

- In the $^3\text{He}(e,e'p)^2\text{H}$ reaction, the p_m -dep. of $d\sigma_{\text{exp}}$ exhibits different slopes ($p_m < 1200(\text{MeV}/c)$), which correspond to **PWIA**, **single** rescattering and **double** rescattering contributions produced by the GA/GEA.
- Such features correspond to the data very well.
- Rather similar features are seen in $^4\text{He}(e,e'p)^3\text{H}$ (theoretical) results, but we also found that the **triple** rescattering starts to contribute at **$p_m > 800(\text{MeV}/c)$** .

Summary -3

3. FFT Effect on $^4\text{He}(e,e'p)^3\text{H}$

- FFT effects are **small** at JLab E97-111 CQ ω^2 Kinematics (**$Q^2=1.78(\text{GeV}/c)^2$**)
- We extend theoretical calculation to higher Q^2 region and found..
- FSI is almost diminished by FFT effect at around **$Q^2 \geq 10(\text{GeV}/c)^2$** region.
- FFT effect will be appeared as a **prominent Q^2 -dep. of $n_D(p_m)$** around dip region ($p_m \sim 2.2(\text{fm}^{-1})$).

Future Developments

- Calculations without factorization are now in progress.
- Under such calculation we will derive each nuclear response functions: R_L, R_T, R_{TT}, R_{TL}
- Then we will calculate A_{TL} (left-right asymmetry) , which is consider to be sensitive to the theoretical prescription.

$$A_{TL} = \frac{\sigma(\varphi = 0^\circ) - \sigma(\varphi = 180^\circ)}{\sigma(\varphi = 0^\circ) + \sigma(\varphi = 180^\circ)} = \frac{v_{TL} \mathcal{R}_{TL}}{v_L \mathcal{R}_L + v_T \mathcal{R}_T + v_{TT} \mathcal{R}_{TT}}$$



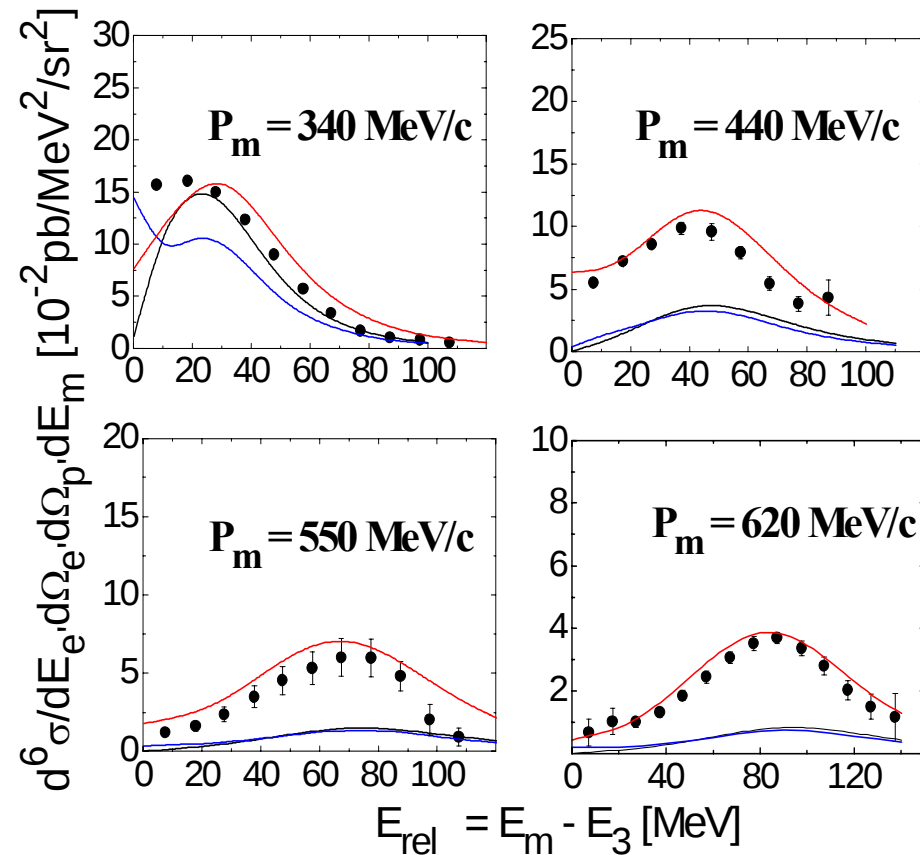
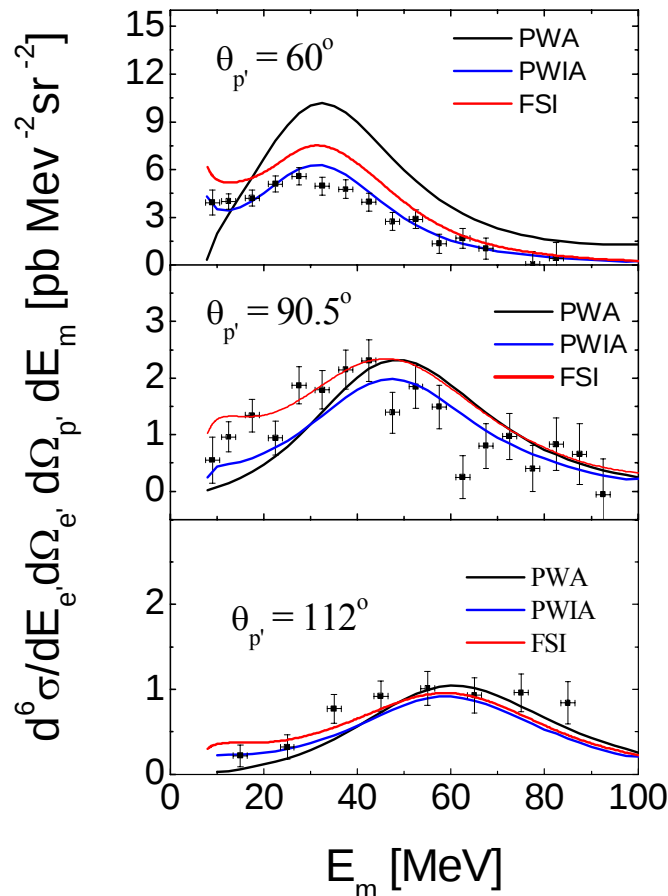
Results of $^3\text{He}(e,e'p)pn$ ②

C. Ciofi degli Atti, L.P. Kaptari, *Phys. Rev. C* **71**, 024005 (2005)

C. Marchand et al., *Phys. Rev. Lett.* **60**(1988) 1703
 $^3\text{He}(e,e'p)pn$ (SACLAY kinem.)

JLAB 89044

— PWA
 — PWIA
 — FSI



ATMS Few-body Wave Function

ATMS method

M. Sakai et al., Prog.Theor.Phys.Suppl.56(1974)108.

H. Morita et al., Prog.Theor.Phys.78(1987)1117.

$$\Psi_{ATMS} = F \cdot \Phi, \quad \Phi : \text{mean-field w.f.} \quad \Phi = \Phi_S \cdot \{S = 0, T = 0\}_A$$

$$F = D^{-1} \sum_{ij} \left(w(ij) - \frac{(n_p - 1)}{n_p} u(ij) \right) \prod_{kl \neq ij} u(kl),$$

$$D = \sum_{ij} \left(1 - \frac{(n_p - 1)}{n_p} u(ij) \right) \prod_{kl \neq ij} u(kl), \quad n_p = A(A-1)/2$$

$w(ij)$: on-shell correlation function

$u(ij)$: off-shell correlation function

Introduction of the State dependence



$$w(ij) = {}^1w_S(ij)\hat{P}^{1E}(ij) + {}^3w_S(ij)\hat{P}^{3E}(ij) + {}^3w_D(ij)\hat{S}_{ij}\hat{P}^{3E}(ij)$$

Euler-Lagrange eq.

$$\delta_u [\langle \psi_{ATMS} | H | \psi_{ATMS} \rangle - E \langle \psi_{ATMS} | \psi_{ATMS} \rangle] = 0$$

δ_u : performed respect to $\{w, u\}$

The radial form of $\{w(r), u(r)\}$ are directly determined from Euler-Lagrange eq.

Results

$V_{NN}(r)$: Reid Soft core V8 model potential

$$\langle H \rangle = -21.2 \text{ MeV}, \quad \langle r^2 \rangle^{1/2} = 1.57 \text{ fm}$$

$$PS = 87.94\%, \quad PS' = 0.24\%, \quad PD = 11.82\%$$

Experimental Data

JLab E97-111: B. Reitz et al., Eur. Phys. J. A S19(2004) 165

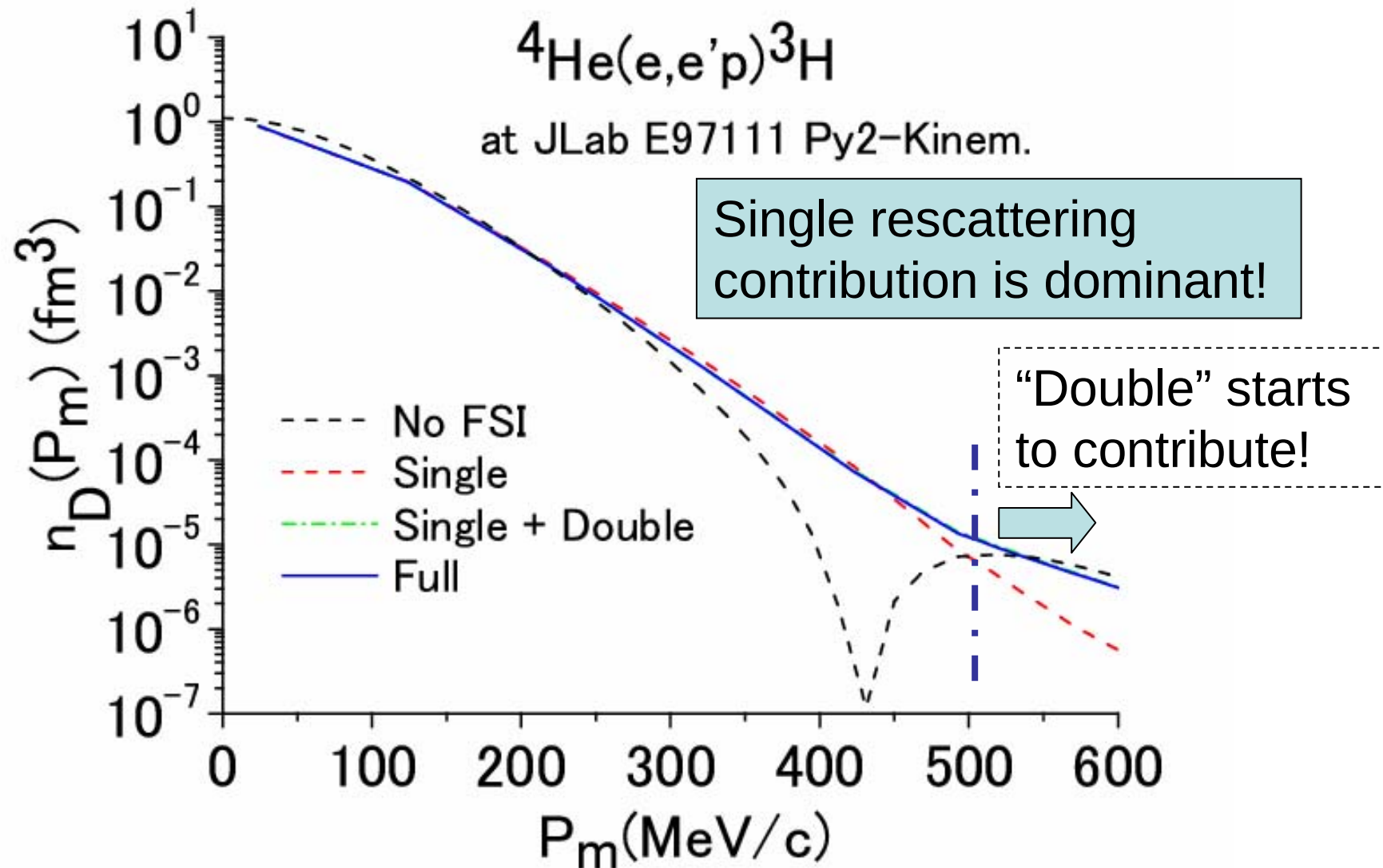


1. Py2 Kinematics—Parallel Kinematics

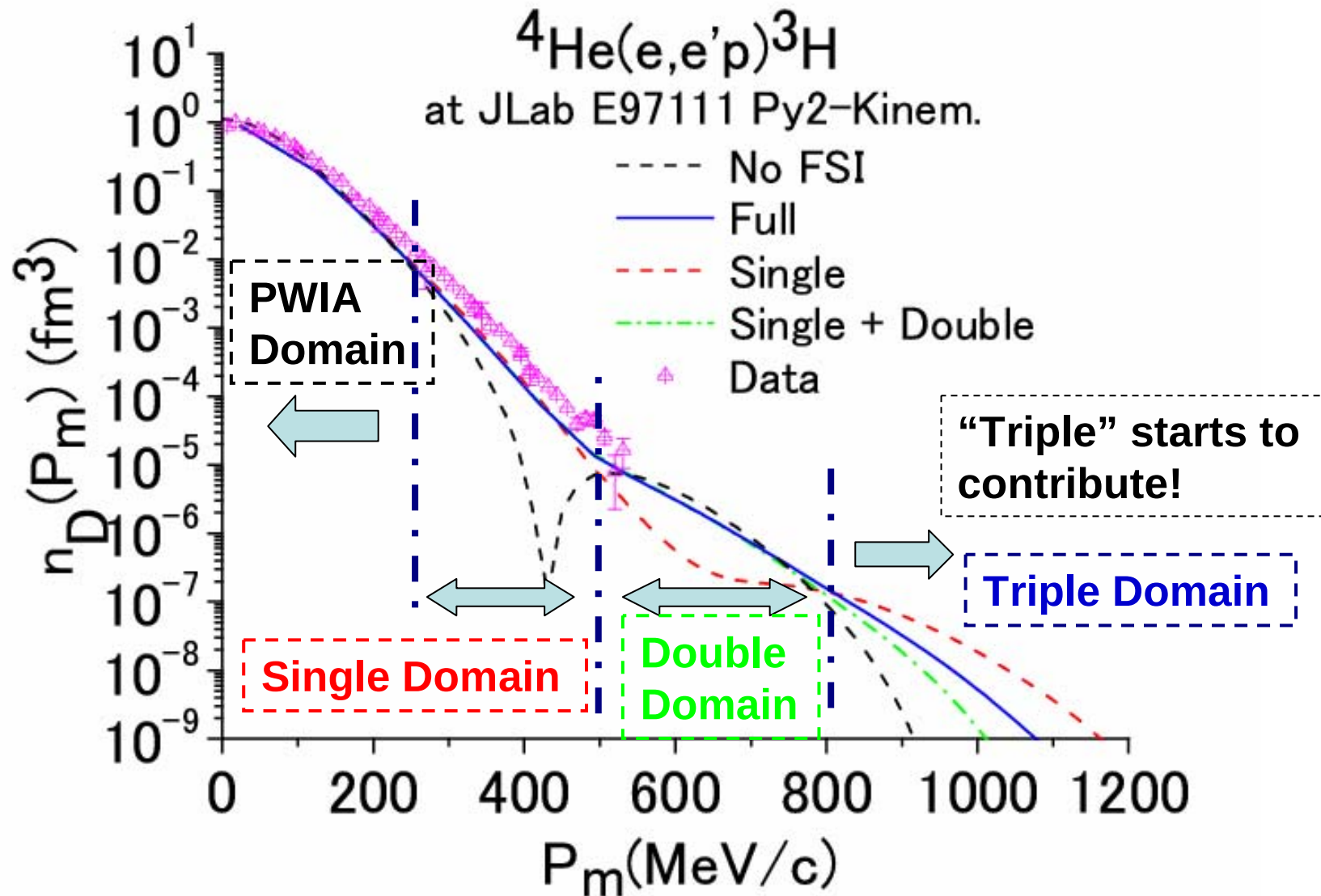
2. CQ ω 2 Kinematics—Perpendicular Kinematics

Kinem.	$E_e(\text{GeV})$	$\omega(\text{GeV})$	$q(\text{GeV}/c)$	$Q^2(\text{GeV}/c)^2$	$p_m(\text{MeV}/c)$
CQ ω 2	3.952	0.525	1.43	1.78	395
CQ ω 2	3.952	0.525	1.43	1.78	446
CQ ω 2	3.952	0.525	1.43	1.78	495
PY2a	3.17	0.537	1.09	0.908	24
PY2b	3.17	0.653	1.14	0.868	124
PY2c	3.17	0.798	1.21	0.818	223
PY2d	3.17	0.985	1.31	0.753	323
PY2e	3.17	1.239	1.48	0.666	423
PY2f	3.17	1.481	1.67	0.582	493

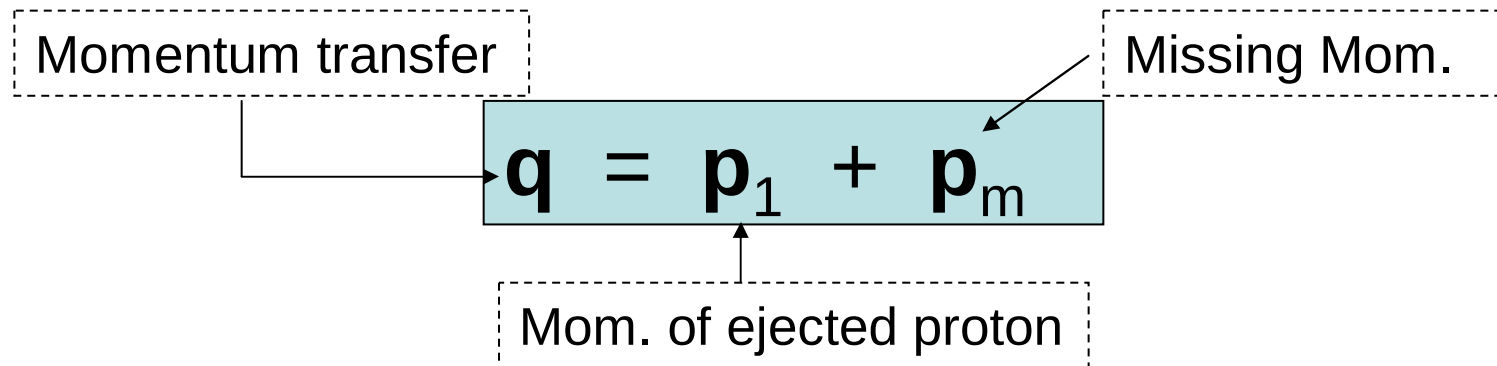
Multiple Scattering Contributions



Multiple Scattering Contributions 2



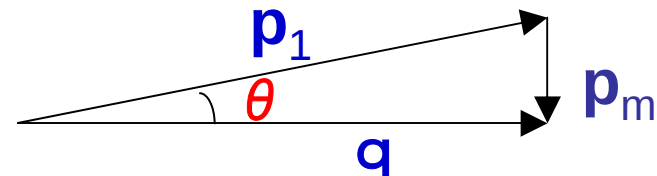
Note: Choice of z-axis



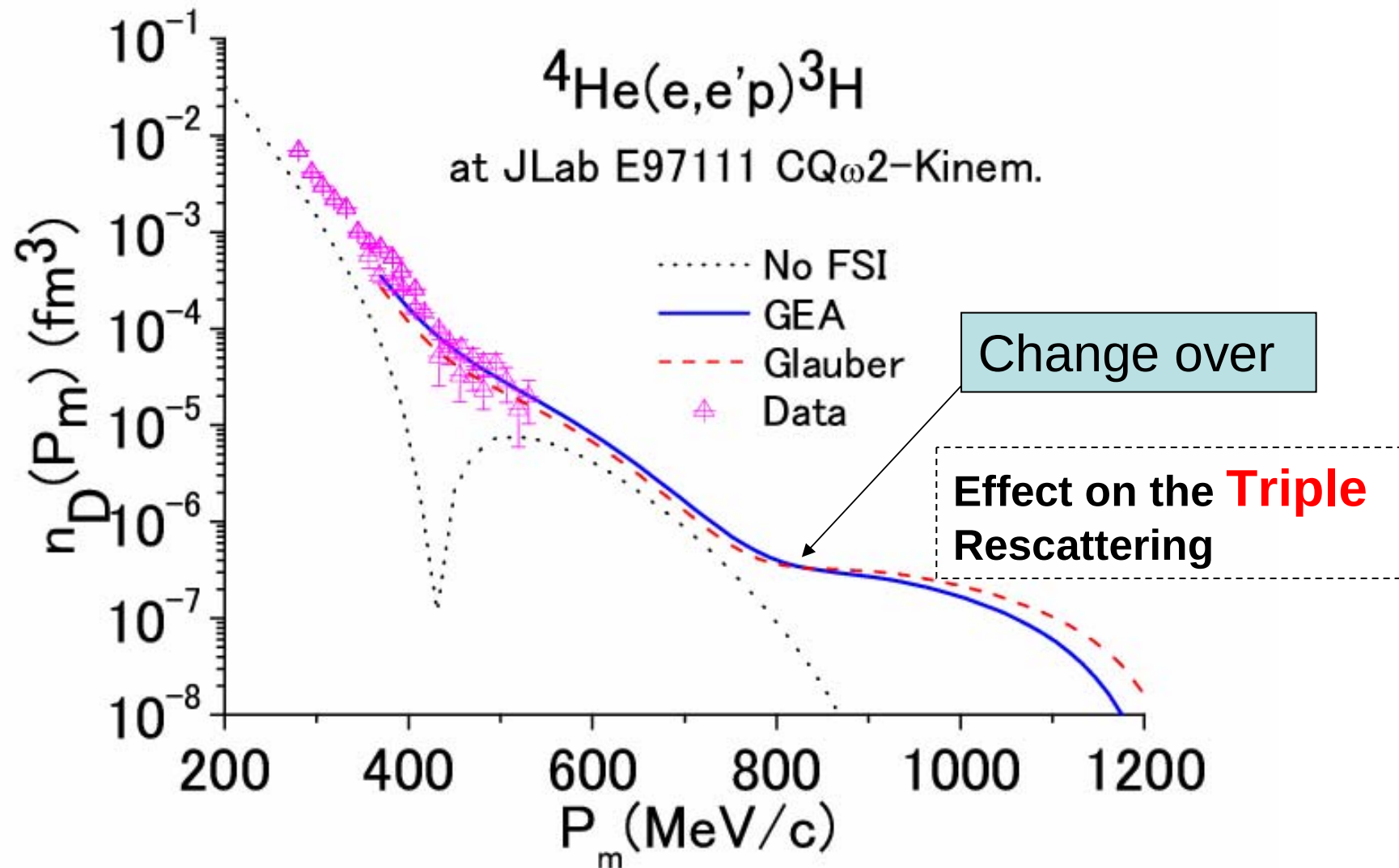
In many cases **q-direction** is taken to be z-axis assuming $\mathbf{q} \gg \mathbf{p}_m$

However, in the Glauber theory z-axis should be the direction of the incident particle
 $\sim \mathbf{p}_1$ direction

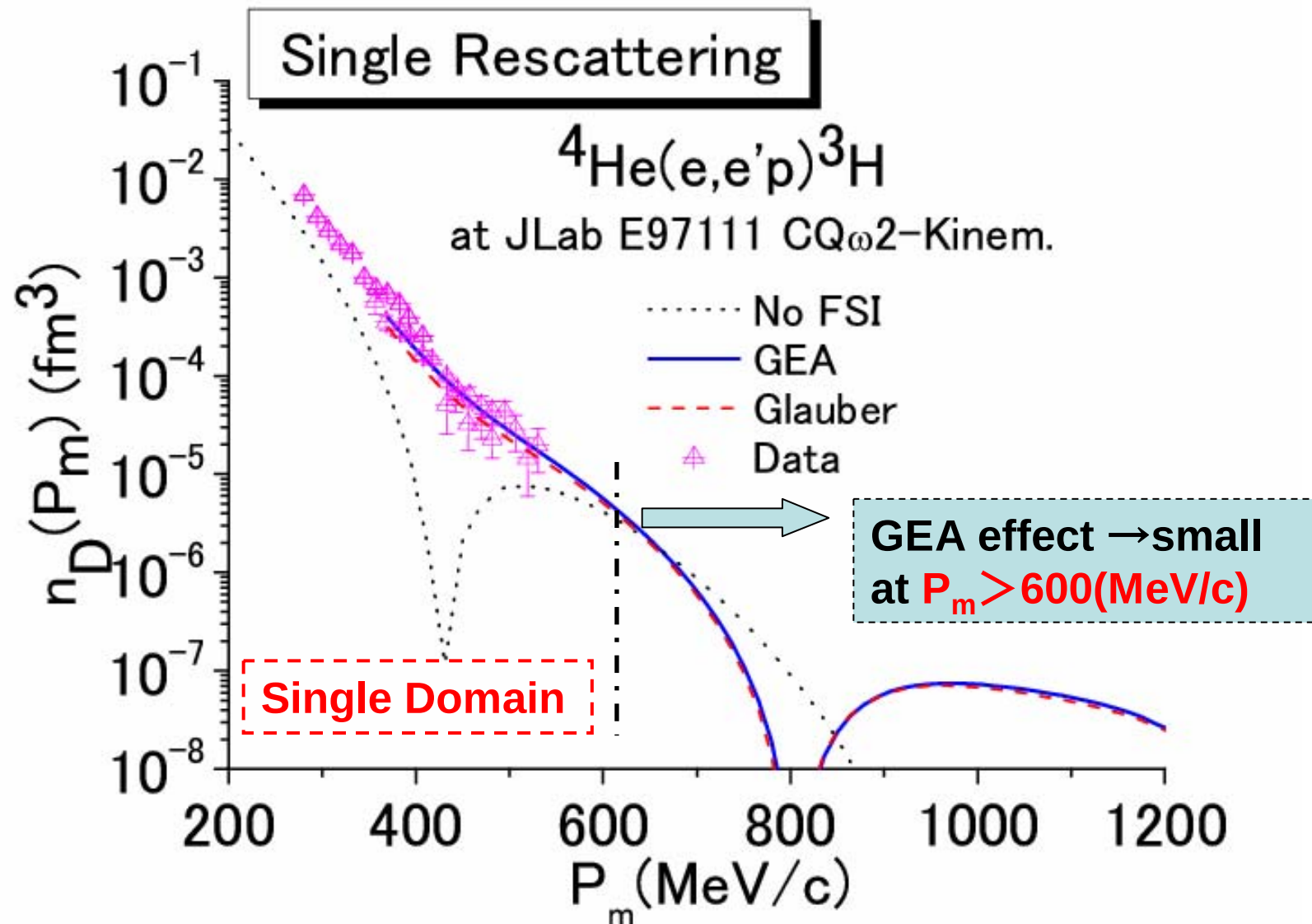
The deviation by θ will make some different results especially at perpendicular kinematics ($\mathbf{q} \perp \mathbf{p}_m$)



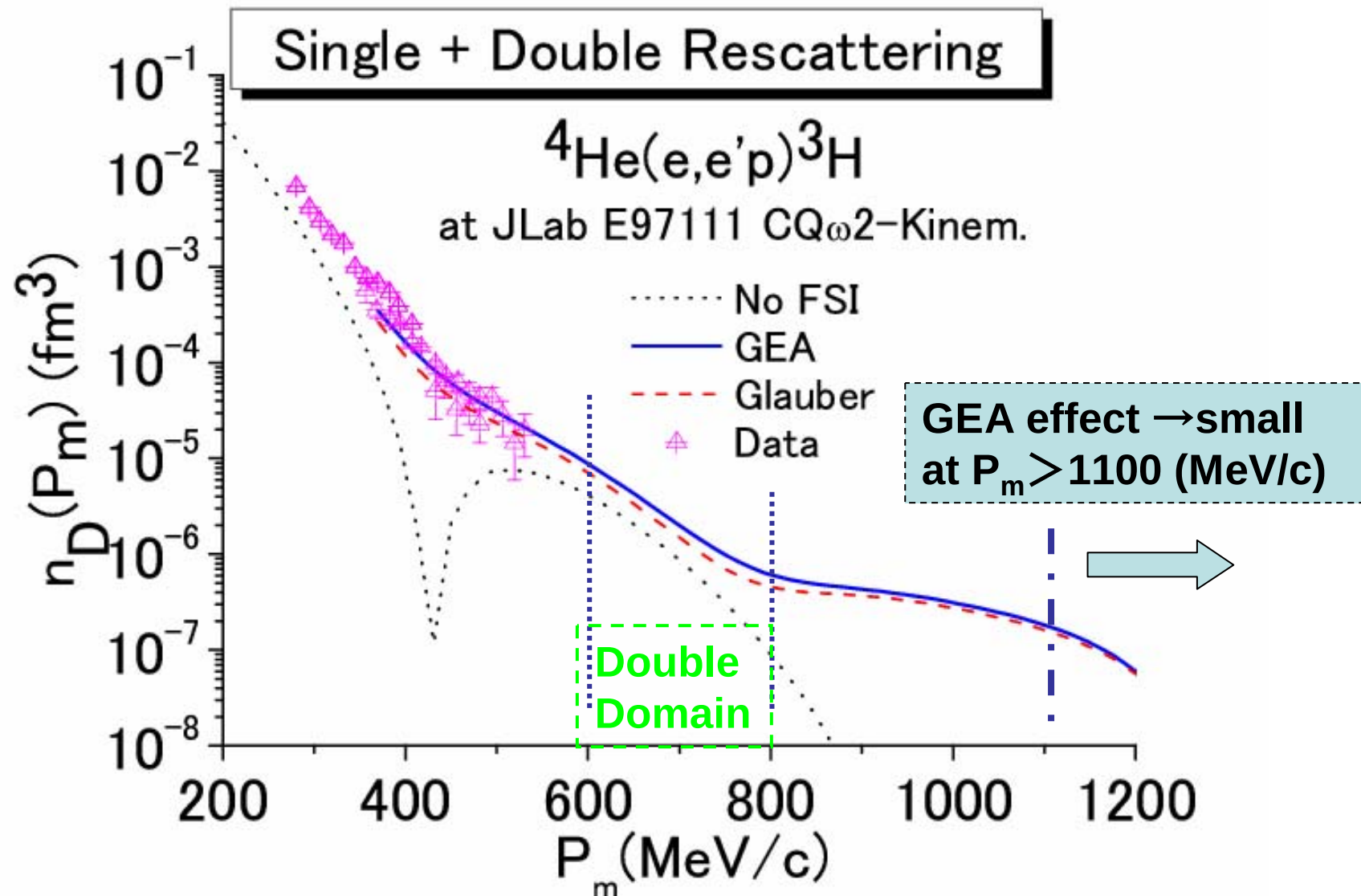
GEA Effect at higher P_m



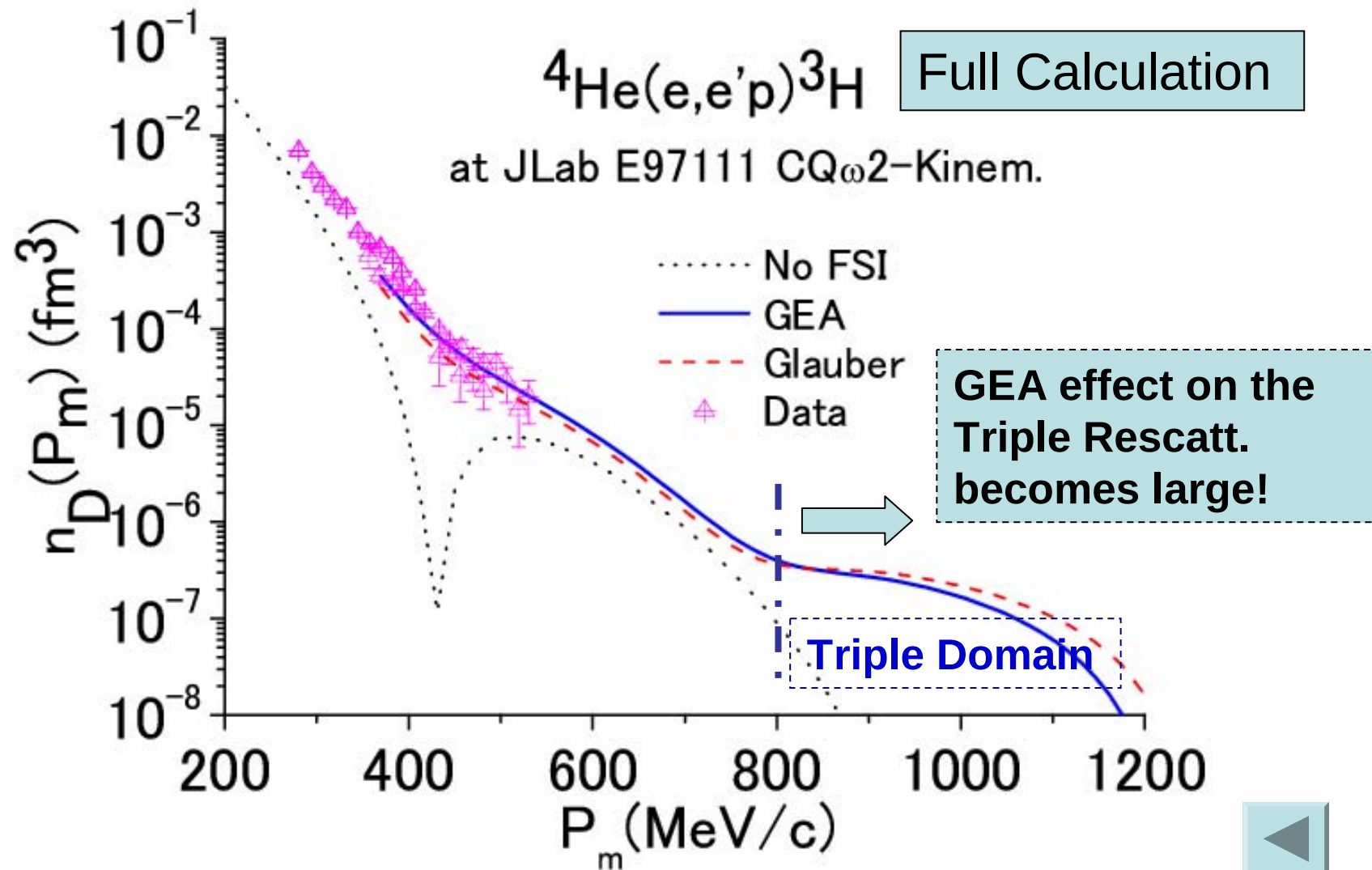
GEA Effect on the Single Rescatt.



GEA Effect on the Double Rescatt.

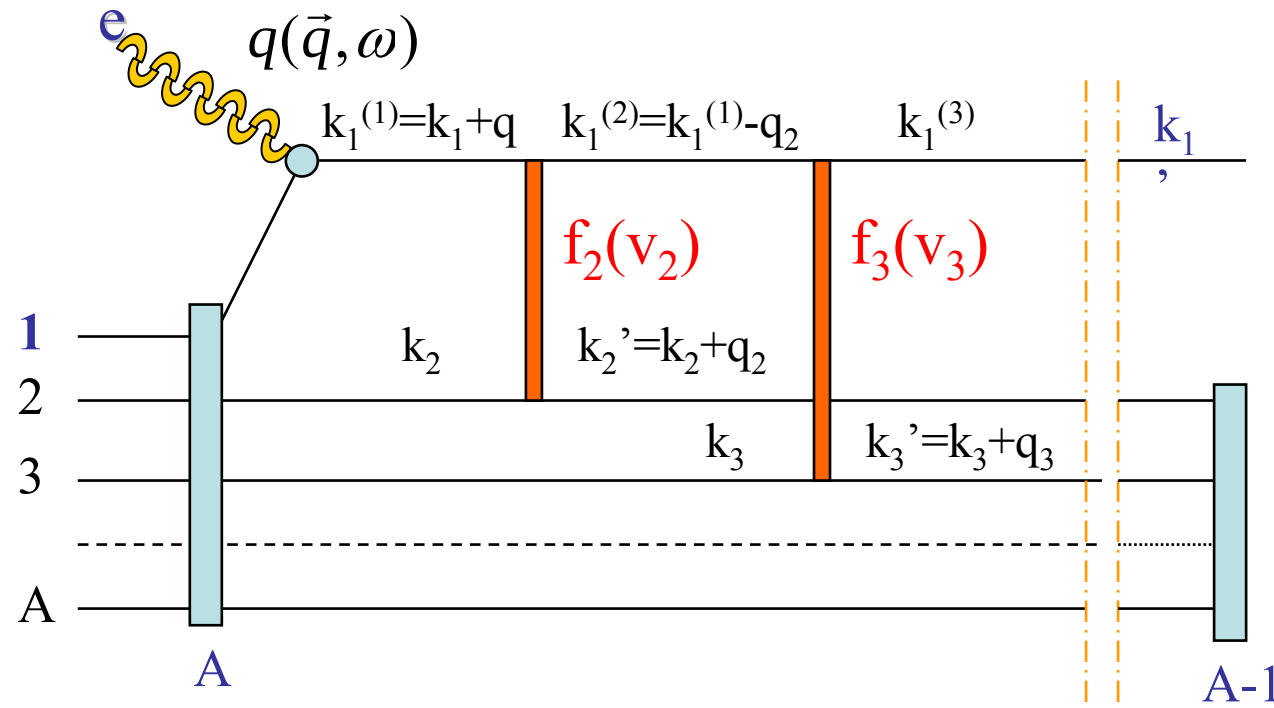


GEA Effect on the Triple Rescatt.



§ 5. Formulation of FFT effect

M.A.Braun et al. Phys. Rev. **C62**, 034606(2000).



Virtuality of particle “1”

$$v_i = (k_1^{(i)})^2 - m^2 = Q^2 \left(\frac{1}{x} - 1 \right) + \frac{Q^2}{xm} \left(\sum_{j=2}^i q_{jz} - k_{1z} \right), \quad Q^2 = \vec{q}^2 - \omega^2, \quad x = Q^2 / (2k_1 \cdot q)$$

m: Nucleon Mass

Bjorken variable

Scattering Amplitude

$$f_j = F(\mathbf{v}_{j-1})F(\mathbf{v}_j)f, \quad f: \text{on-shell Amplitude}$$

$F(\mathbf{v}) \rightarrow$ F.F. for Virtuality
dep.

$$F(0)=1$$

Scattering Matrix

$$S(r_2, r_3, \dots, r_A) = \prod_{j=2}^A S(\vec{r}_j), \quad S(\vec{r}_j) = 1 - J(z_j - z_1) \Gamma(\vec{b}_j - \vec{b}_1)$$

Virtuality dep.

$J(z)$ (Virtuality dep. Factor)

$$J(-z) = -i \int \frac{dv}{2\pi} \frac{F^2(v)}{-v - i0} \exp(i \frac{xmv}{Q^2} z), \quad F^2(v) = \int_0^\infty dv' \frac{v' \tau(v')}{v' - v - i0}$$

$$\int_0^\infty dv \tau(v) = 1$$

$$J(z) = \theta(z) \int_0^\infty dv \tau_1(v) (1 - \exp(-\frac{xmv}{Q^2} z))$$

$$\tau_1(v) = -i \tau(-iv)$$

Here if we take

$$\tau_1(v) \rightarrow \delta(v - M^2), \quad (M^2 = m^{*2} - m^2)$$

M^2 : Average Virtuality

then

$$J(z) = \mathcal{G}(z) \left(1 - \exp\left(-\frac{z}{l(Q^2)}\right)\right),$$

$$l(Q^2) = \frac{Q^2}{xmM^2}$$

Formation length

In the following calculation...

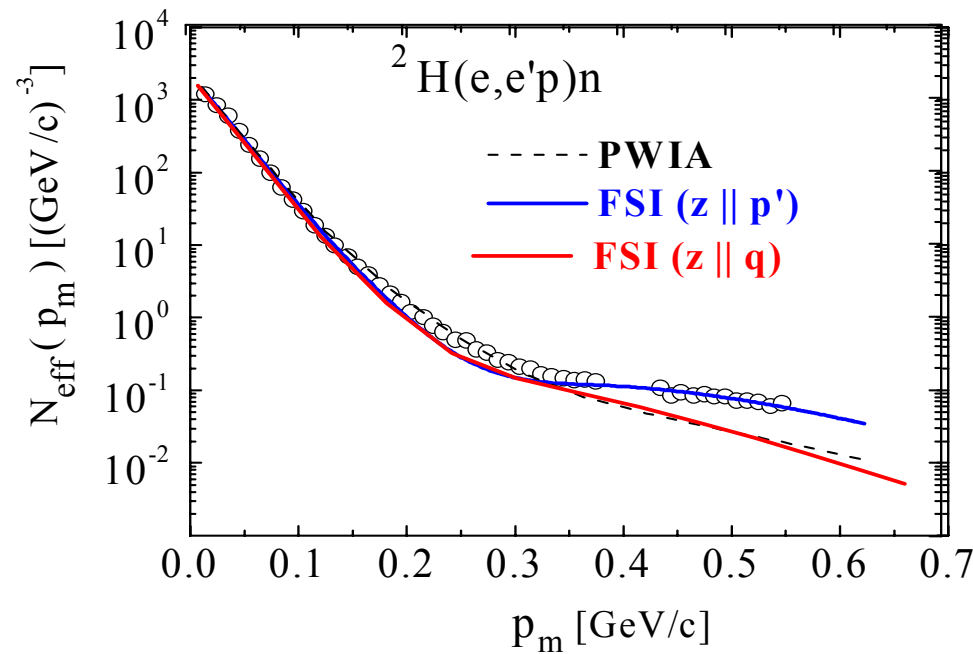
$$M^2 = (m_{Av}^*)^2 - m^2, \quad m_{Av}^* \rightarrow 1.8(\text{GeV}) \quad (\text{Braun et al.})$$



“z-axis” effects

Ref) $^2\text{H}(e,e'p)n$ case

Calculation by L.Kaptari



$\theta_{p_m q}$	$\theta_{p_m p'}$	$p_m [\text{GeV}/c]$
180.0	180.0	0.011
95.1	99.1	0.063
85.5	93.5	0.135
79.2	91.2	0.196
73.8	89.8	0.257
68.7	88.7	0.316
63.9	87.9	0.364
59.3	87.3	0.420
54.9	86.9	0.485
50.6	86.6	0.537
46.0	86.4	0.586
42.4	86.4	0.623
38.5	86.4	0.676

Jlab data (Ulmer *et al.* Phys. Rev. Lett. 89 (2002)) at *perpendicular* kinematics, with:

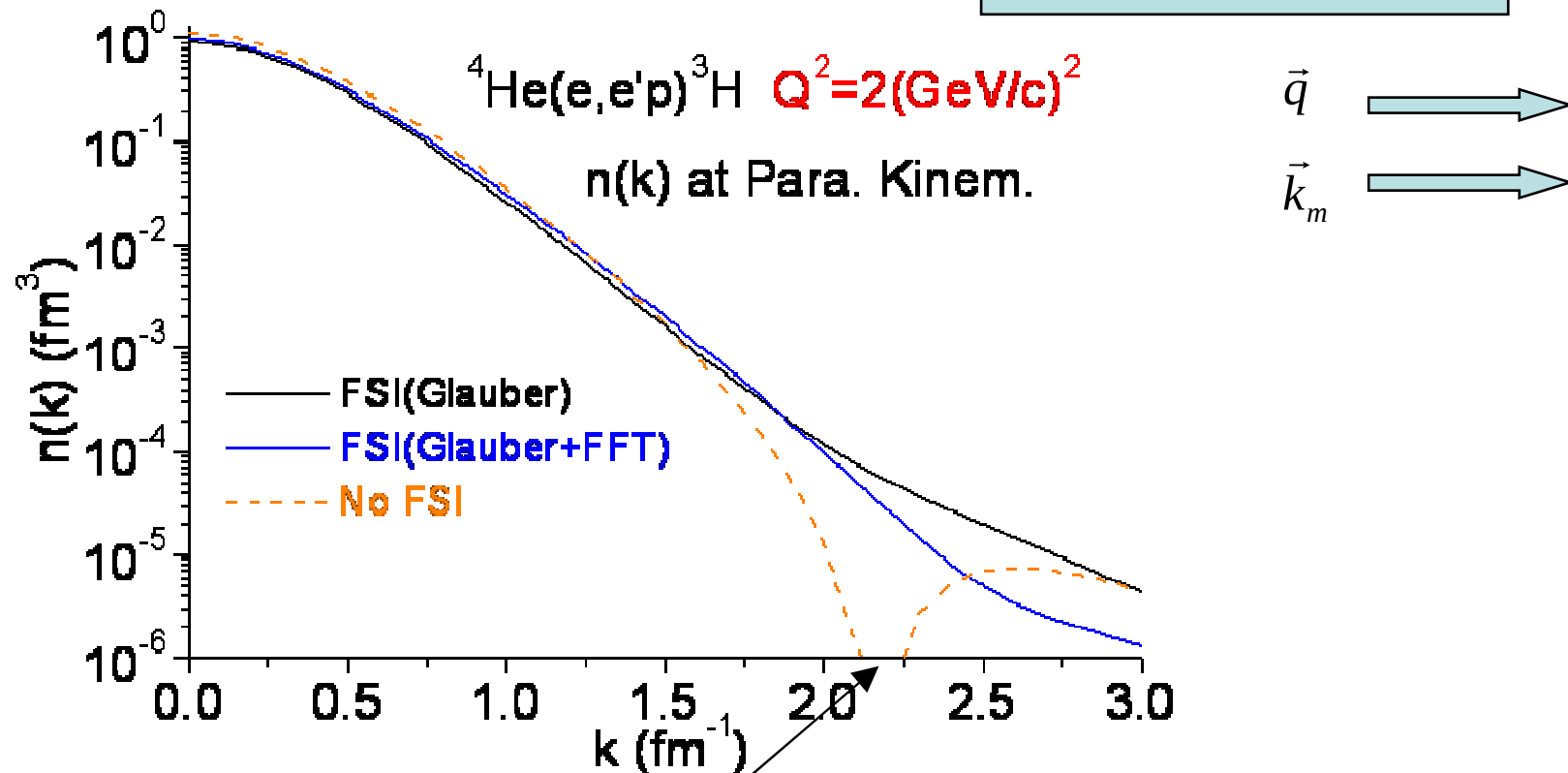
$$Q^2 \simeq 0.665 (\text{GeV}/c)^2, \quad |\mathbf{q}| \simeq 0.7 \text{ GeV}/c, \quad x \simeq 0.96$$

$$N_{eff} = \frac{d^4 \sigma^{exp}}{d\Omega' dE' d\Omega \mathbf{p}_m} [f_{rec} \mathcal{K} \sigma_{cc1}^{eN}]^{-1}$$



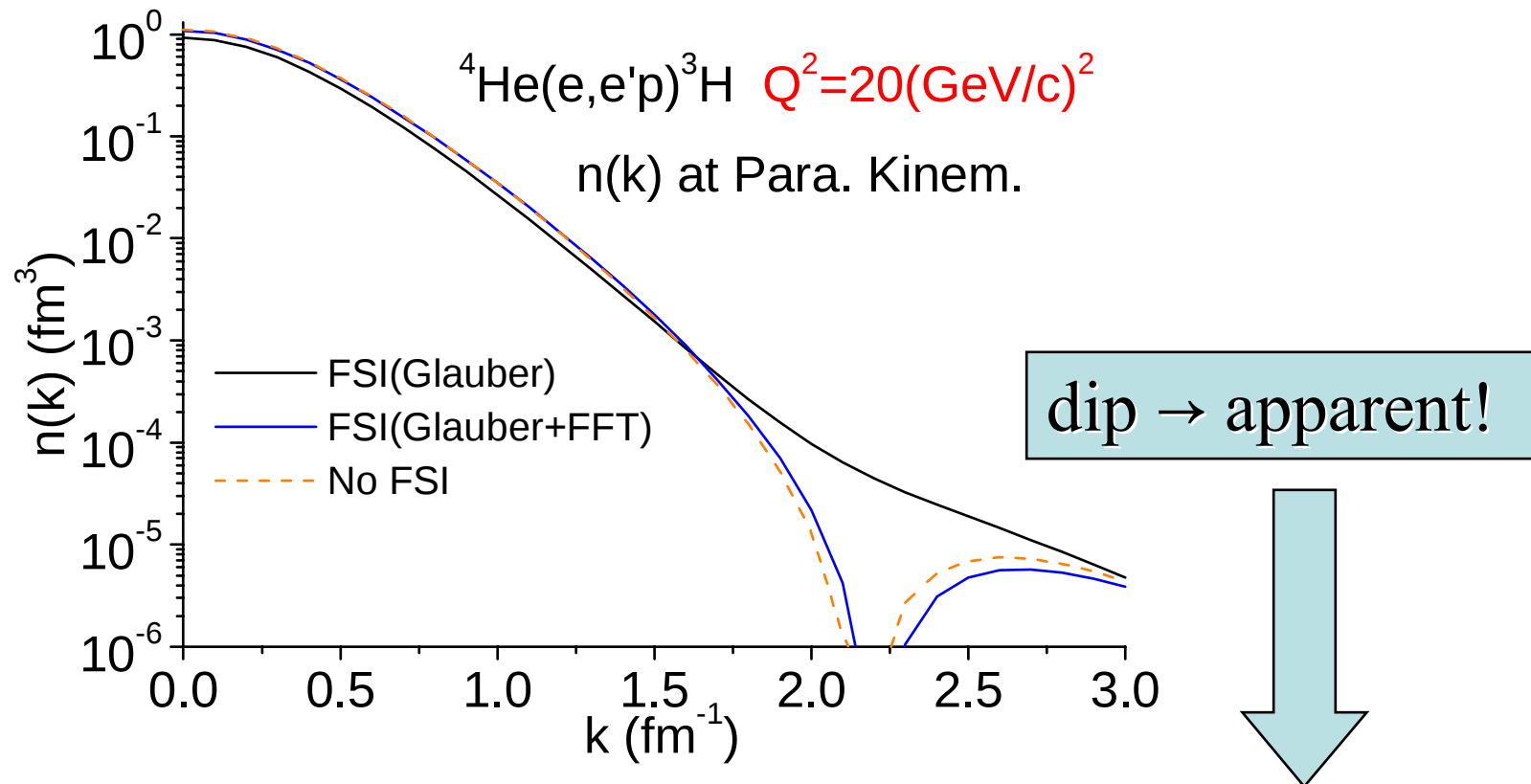
Para. Kinem. at $Q^2=2(\text{GeV}/c)^2$, $x=1$

Parallel Kinematics



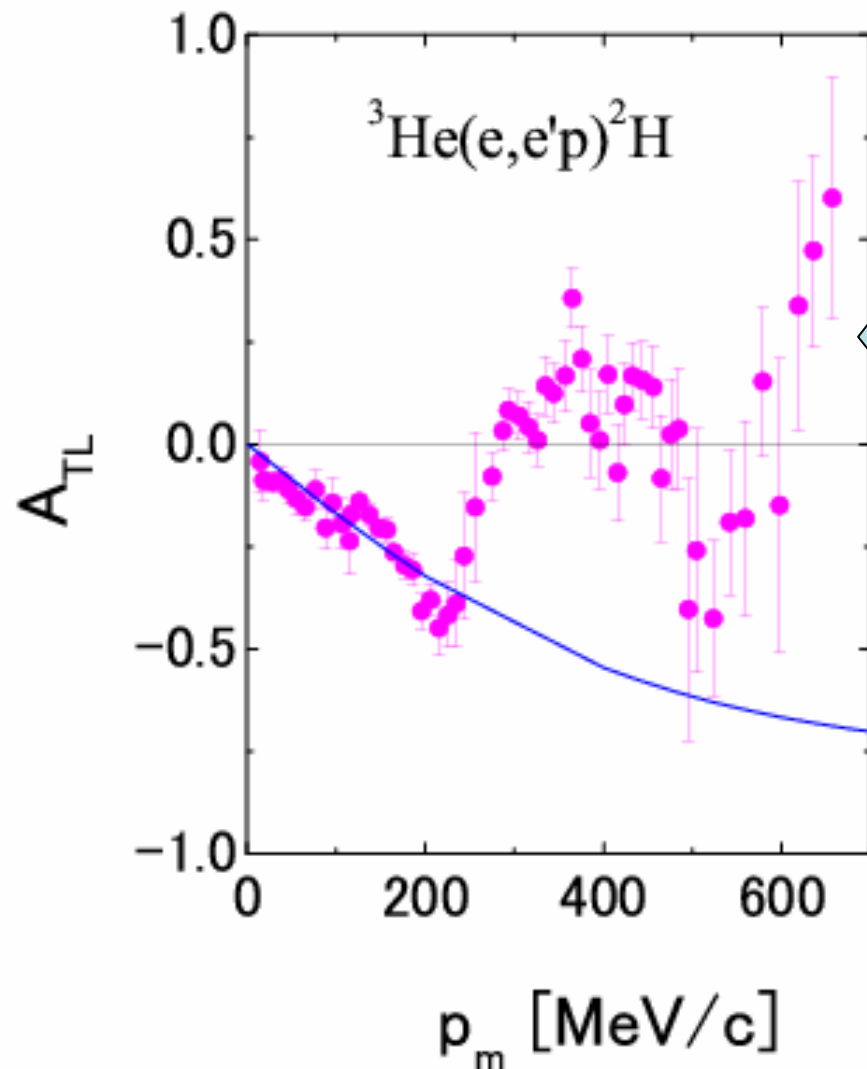
Dip $\rightarrow$ masked by FSI

Q^2 -dep. -Parallel Kinem.- at $Q^2=20(\text{GeV}/c)^2$



FSI → diminished by FFT effect!

A_{TL} within Factorization Calc.



Data

M.M. Rvachev et al.,
Phys.Rev.Lett. **94** (2005) 192302

Factorization calculation
can not reproduce these
structures.

Calculations with no
factorization are now
in progress.



