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**Higgs Diffractive Production**

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These are preliminary lecture notes, intended only for distribution to participants

# Higgs Diffractive Production

Ivan Schmidt  
Trieste 2006

# Higgs detection

- Unknown mass
- Small production probability and large backgrounds
- Coupling  $\sim$  mass  $\rightarrow$  hard to observe in pp

But :

$$1) \quad |p\rangle = a_1 |qqq\rangle + a_2 |qqqQ\bar{Q}\rangle + \dots$$



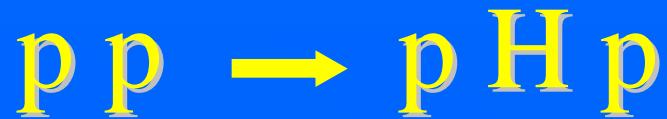
Small (1% probability for c)

$$\sim 1/M^2$$

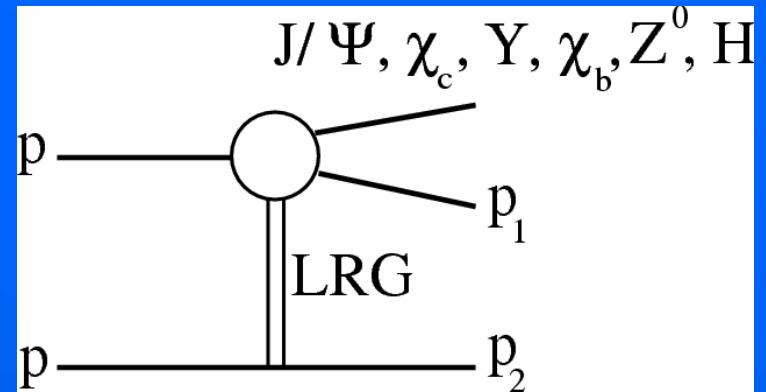
- 2) Reduce backgrounds from multiparticle production



Diffractive production in fragmentation region of one of the protons

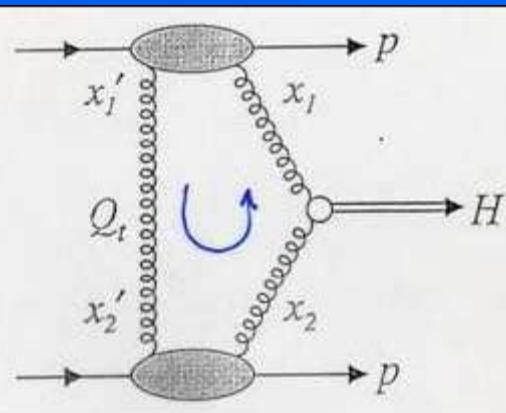


- ✓ Large rapidity gap
- ✓ Missing mass measurement

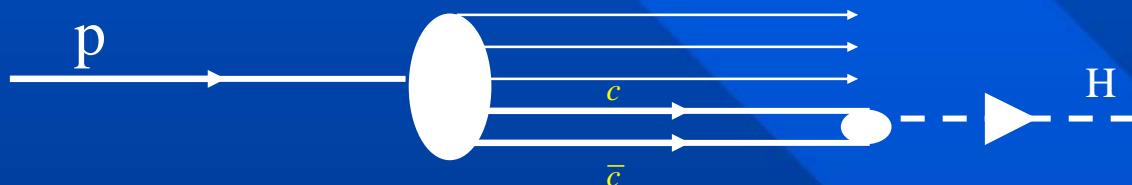


### Concrete possibilities :

1) Central region (MKKRS)



2) Heavy quarks in proton

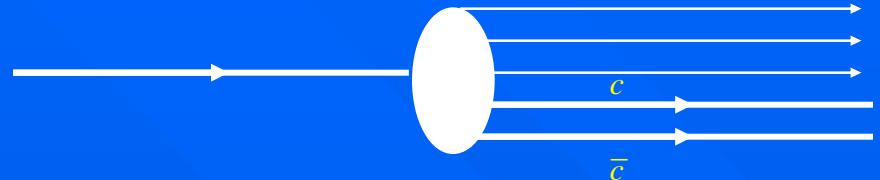


$$x_F \simeq x_c + x_{\bar{c}}$$

large  
 { S. Brodsky  
 B. Kopeliovich  
 J. Soffer  
 I. S.

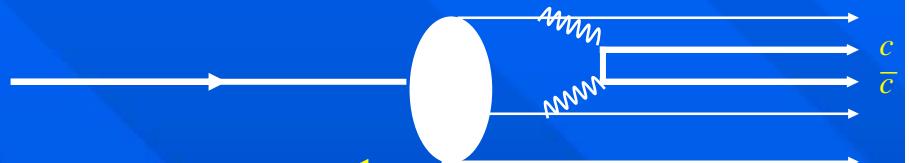
# Large $x_F$ production

1) Non-perturbative (stationary state)



$$\langle r_{c\bar{c}}^2 \rangle = \frac{2}{\omega m_c} \quad \omega = 300 \text{ MeV}$$

2) Perturbative (quantum fluctuation)

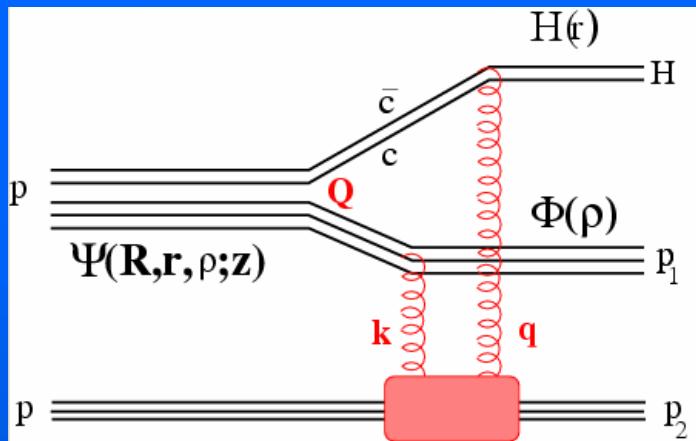


$$\langle r_{c\bar{c}}^2 \rangle = \frac{1}{m_c^2}$$

Experimentally:

DIS data, excess at large  $x_{Bj}$

# Exclusive diffraction calculation



Form factors  $\longleftrightarrow$  (gluon coupling to all quarks)

Vanish as  $q \rightarrow 0$  (suppression)

$$\frac{d\sigma(pp \rightarrow ppH)}{dx_2 d^2p_1 d^2p_2} = \frac{1}{(1-x_2)16\pi^2} |A(x_2, \vec{p}_1, \vec{p}_2)|^2$$

$$\begin{aligned}
 A(x_2, \vec{p}_1, \vec{p}_2) &= \frac{8}{3\sqrt{2}} \int d^2Q \frac{d^2q}{q^2} \frac{d^2k}{k^2} \alpha_s(q^2) \alpha_s(k^2) \delta(\vec{q} + \vec{p}_2 + \vec{k}) \delta(\vec{k} - \vec{p}_1 - \vec{Q}) \\
 &\times \int d^2\tau |\Phi_p(\tau)|^2 [e^{i(\vec{k}+\vec{q})\cdot\vec{\tau}/2} - e^{i(\vec{q}-\vec{k})\cdot\vec{\tau}/2}] \int d^2R d^2r d^2\rho H^\dagger(\vec{r}) e^{i\vec{q}\cdot\vec{r}/2} \\
 &\times (1 - e^{-i\vec{q}\cdot\vec{r}}) \Phi_p^\dagger(\vec{\rho}) e^{i\vec{k}\cdot\vec{\rho}/2} (1 - e^{-i\vec{k}\cdot\vec{\rho}}) \Psi_p(\vec{R}, \vec{r}, \vec{\rho}, z) e^{i\vec{Q}\cdot\vec{R}}. \quad (5)
 \end{aligned}$$

Born

# Calculational steps

1) Factorized form for proton wf

$$\psi_p(\vec{R}, \vec{r}, \vec{\rho}, z) = \psi_{IC}(\vec{R}, z) \psi_{c\bar{c}}(\vec{r}) \psi_{3q}(\vec{\rho})$$

$$\int d^2 R |\psi_{IC}(\vec{R}, z)|^2 = P_{IC}(z) \quad z \approx x_F$$

2) Calculate at t=0 ( $\vec{q} = -\vec{k}$ ), and assume Pomeron-type t-dependence

$$\frac{d\sigma}{d^3 p_1 d^3 p_2} \sim e^{-B(s') p_2^2}$$



3) Replace two-gluon proton vertex by gluon density  $F(x, k^2)$

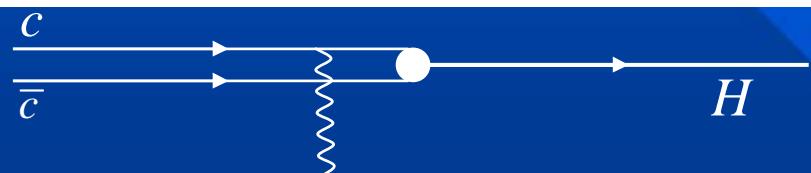


fitted to data



Includes higher  
order corrections

$$\begin{aligned} \frac{d\sigma^{IC}(pp \rightarrow ppH)}{dx_2} &= \frac{32\pi P_{IC}(z)}{9B(s')(1-x_2)} \left| \int \frac{d^2 k}{k^4} \alpha_s(k^2) \mathcal{F}(x, k^2) \right. \\ &\times \int d^2 r H^\dagger(\vec{r}) e^{-i\vec{k}\cdot\vec{r}/2} \left(1 - e^{i\vec{k}\cdot\vec{r}}\right) \Psi_{\bar{c}c}(\vec{r}) \\ &\times \left. \int d^2 \rho \Phi_p^\dagger(\vec{\rho}) e^{-i\vec{k}\cdot\vec{\rho}/2} \left(1 - e^{i\vec{k}\cdot\vec{\rho}}\right) \Psi_{3q}(\vec{\rho}) \right|^2. \end{aligned}$$



Only odd powers of  $\vec{k} \cdot \vec{r}$   
 $\vec{k} \cdot \vec{\rho}$

change of orbital angular momentum

- initial  $\bar{c}c$  in S-wave
  - final  $\bar{c}c$  in P-wave
- H is scalar

(different for  $J/\psi, Z^0$  : P-wave initial state)

## 4) Higgs wavefunction (P-wave)

$$H(\vec{r}) = i \frac{\sqrt{N_c G_F}}{2\pi} m_c \bar{\chi} \vec{\sigma} \chi \frac{\vec{r}}{r} \left[ \epsilon Y_1(\epsilon r) - \frac{ir}{2} \Gamma_H M_H Y_0(\epsilon r) \right] \quad (\text{for } \bar{c}c \text{ and } \bar{b}b)$$

$$H_{\bar{t}t}(\vec{r}) = \frac{\sqrt{N_c G_F}}{2\pi} m_t \bar{\chi} \vec{\sigma} \chi \frac{\vec{r}}{r} \epsilon_t K_1(\epsilon_t r) . \quad (\text{for } \bar{t}t)$$

## 5) $\bar{c}c$ wavefunction

$$\left. \begin{array}{l} \Psi_{\bar{c}c}^{npt}(\vec{r}) = \sqrt{\frac{m_c \omega}{2\pi}} \exp(-r^2 m_c \omega/4) , \\ \Psi_{\bar{c}c}^{pt}(\vec{r}) = \frac{m_c}{\sqrt{\pi}} K_0(m_c r) . \end{array} \right\} \quad (\text{FT of energy denominator})$$

## 6) Relative motion of $\bar{c}c$ and qqq clusters $\psi_{IC}(\vec{R}, z) \rightarrow [P_{IC}(z)]$

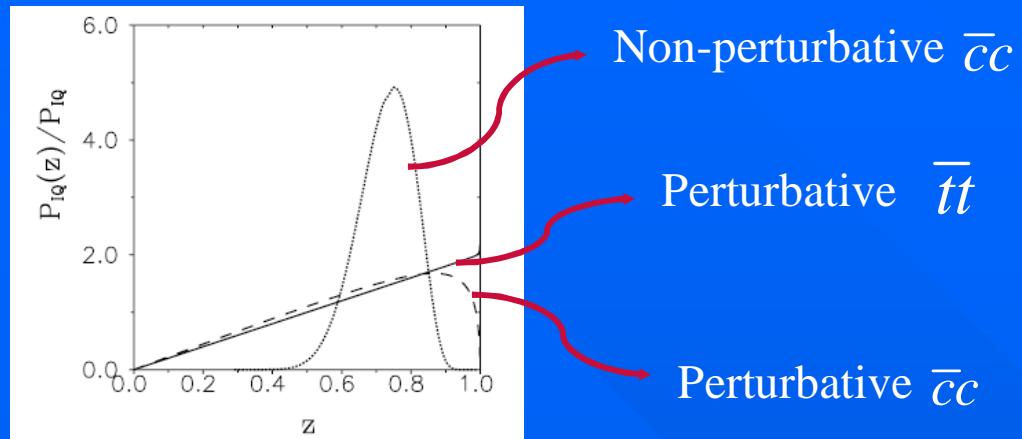
a) Non-perturbative heavy flavors

$$\tilde{\Psi}_{IC}(\vec{Q}, z) = \sqrt{P_{IC}(z)} \left( \frac{1}{\pi \omega \mu} \right)^{3/4} \exp \left( -\frac{\vec{Q}^2}{2\omega \mu} \right)$$

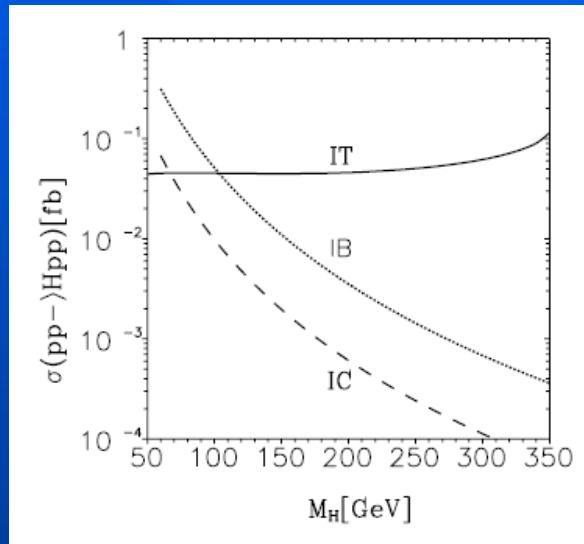
$$\frac{P_{IC}(z)}{P_{IC}} = \frac{1}{\sigma^{IC}(pp \rightarrow ppH)} \frac{d\sigma^{IC}(pp \rightarrow ppH)}{dx_1} = \frac{1}{P_{IC}} \int d^2 Q |\Psi_{IC}(Q, z)|^2$$

b) Perturbative heavy flavors

$$\frac{P_{IQ}(z)}{P_{IQ}} = Nz(1-z) \frac{\left\{ \ln \left[ \frac{|M_H^2 - 4m_Q^2|(1-z)}{4m_Q^2(1-z) + m_p^2 z^2} \right] \right\}^2}{M_H^2(1-z) + m_p^2 z^2}$$



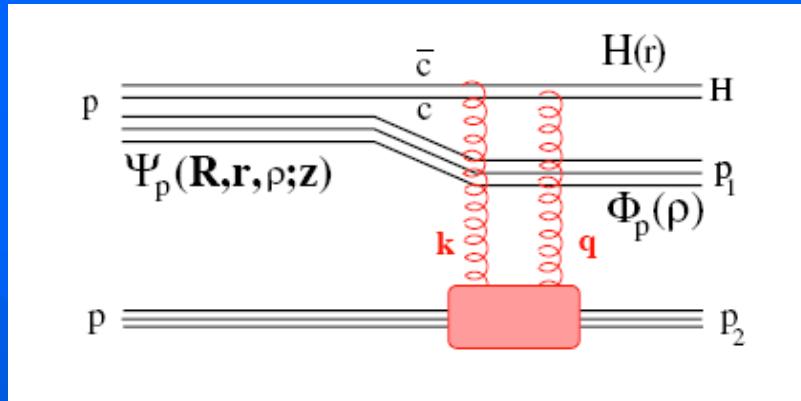
## Final result



- For LHC energy (14 TeV cm)
- Perturbative heavy flavors
- Includes absorptive corrections ( 20% at LHC)
- IT falls for  $M_H > 2m_t \approx 350$  GeV
- Heavy quark probability  $\sim \frac{1}{M_Q^2}$

# Larger cross section

1) From colorless heavy pair



Does not have proton form factor

But

$$\text{Amplitude} \sim \int d^2 r H^+(\vec{r}) \sigma_{\bar{q}q}(r) \psi_{\bar{c}c}(r)$$
$$\sim \frac{1}{M_H^3} \quad \text{suppressed}$$

2) Nuclear enhancement

Not as big as one might think



Stronger absorptive corrections

Factor of  $\sim 10$  for Pb

# Conclusions

- ✓ Heavy quark components  $\rightarrow$  carry high momentum fractions.
- ✓ Higgs production in fragmentation region.
- ✓ Diffractive production  $pp \rightarrow pH\bar{p}$
- ✓ Also possible:  $pp \rightarrow pHX$  ,  $pp \rightarrow HX$  .
- ✓ Difficult detection .