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Fifth International Conference on  
**PERSPECTIVES IN HADRONIC PHYSICS**  
Particle-Nucleus and Nucleus-Nucleus Scattering at Relativistic Energies

**22 - 26 May 2006**

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### **Testing Radiative Energy Loss at RHIC and the LHC**

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These are preliminary lecture notes, intended only for distribution to participants

Fifth International Conference on PERSPECTIVES IN HADRONIC PHYSICS:  
Particle-Nucleus and Nucleus-Nucleus Scattering at Relativistic Energies  
ICTP, Trieste, May 22nd-26th 2006

*Testing radiative energy loss  
at RHIC and the LHC*

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See the talks by F. Arleo, N. Bianchi, D. d'Enterria, B. Z. Kopeliovich,  
H. J. Pirner, J. W. Qiu, C. A. Salgado and U. A. Wiedemann

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1. Motivation.

2. Model.

*With Andrea Dainese (Padova),*

3. Results for RHIC.

*Carlos A. Salgado and Urs A. Wiedemann (CERN),  
Phys. Rev. D71 (2005) 054027 (hep-ph/0501225).*

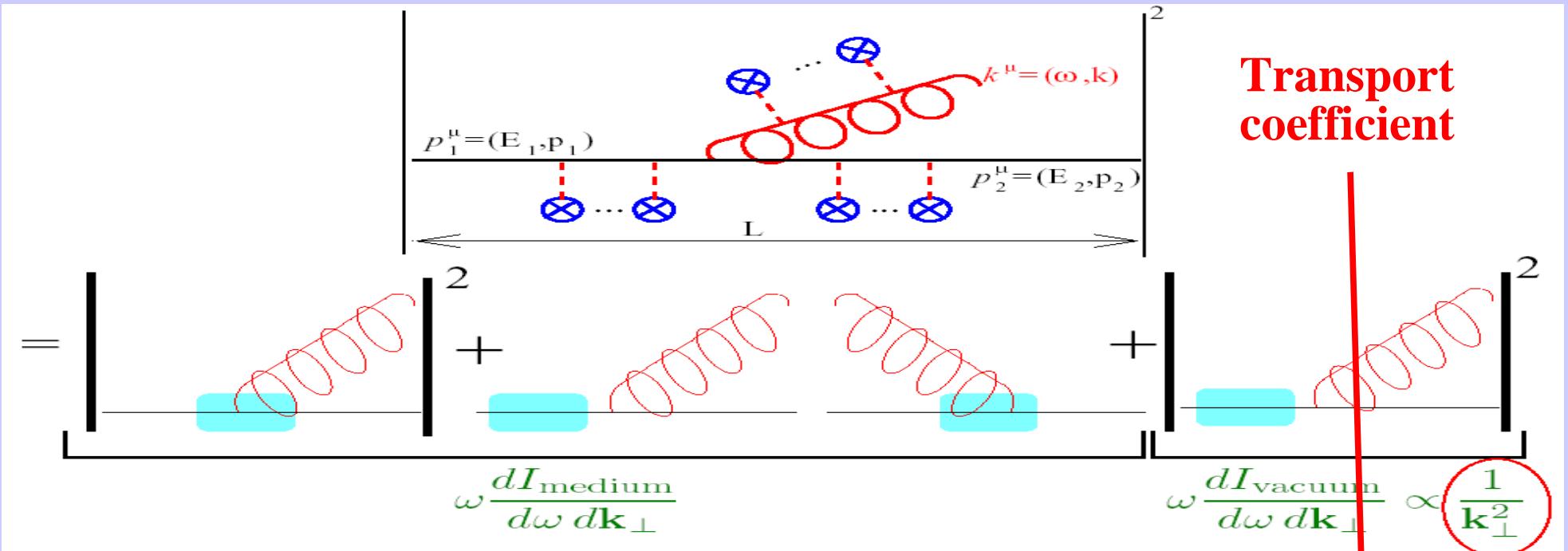
4. Results for the LHC.

*With the former plus Matteo Cacciari  
(Paris VI), hep-ph/0511257  
(Phys. Lett. B in press).*

5. Single electrons at RHIC.

# 1. Motivation (I):

(Baier et al '00; Kovner et al '03; Gyulassy et al '03)



The BDMPS(-GLV-ZW-WZ) formalism describes this in pQCD: interference of production and re-scatterings of the radiated gluon leading to

$$\Delta E \simeq \int d\omega \omega \frac{dI}{d\omega} \propto \alpha_s C_R \omega_c = \alpha_s C_R \hat{q} L^2 / 2 \quad n(z) \sigma(r) \propto \hat{q}(z) r^2$$

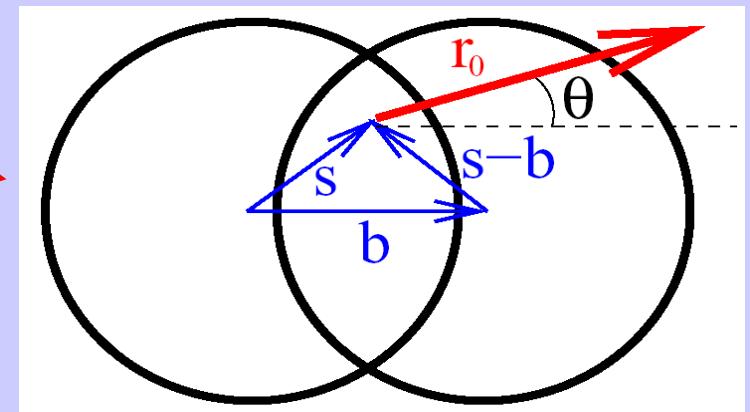
→ Interference and mass effects:  $\exp \left( -\Delta z \frac{k_\perp^2 + x^2 m^2}{2\omega} \right), \quad x = \frac{\omega}{E} \ll 1$

## 1. Motivation (II):

**It has become the ‘canonical’ explanation for the suppression of leading particle spectra at large  $p_T$  and  $y=0$ :**

- Magnitude of the suppression:  $n(z)\sigma(r)$ .
- Dependence of the suppression with centrality and azimuth:  $L^2$ .
- Disappearance of back-to-back correlations: NP  $\sigma(r)$ , tangential emission?

$$R_{AB}(p_T) = \frac{\left. \frac{dN_{\text{medium}}^{AB \rightarrow h}}{dp_T dy} \right|_{y=0}}{\langle N_{\text{coll}}^{AB} \rangle \left. \frac{dN_{\text{vacuum}}^{pp \rightarrow h}}{dp_T dy} \right|_{y=0}}$$



**To further test it and constrain parameters:**

- High  $p_T$  particle correlations, jet shapes and multiplicities.

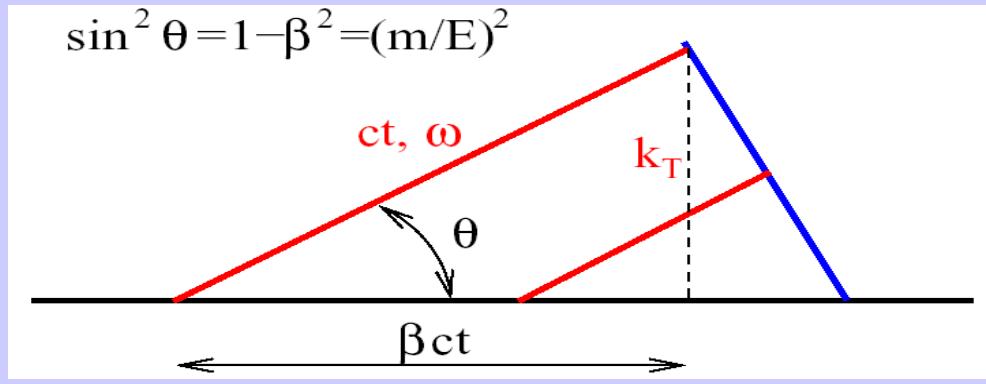
**Genuine prediction of this approach:**

$$\Delta E(g) > \Delta E(q) > \Delta E(Q)$$

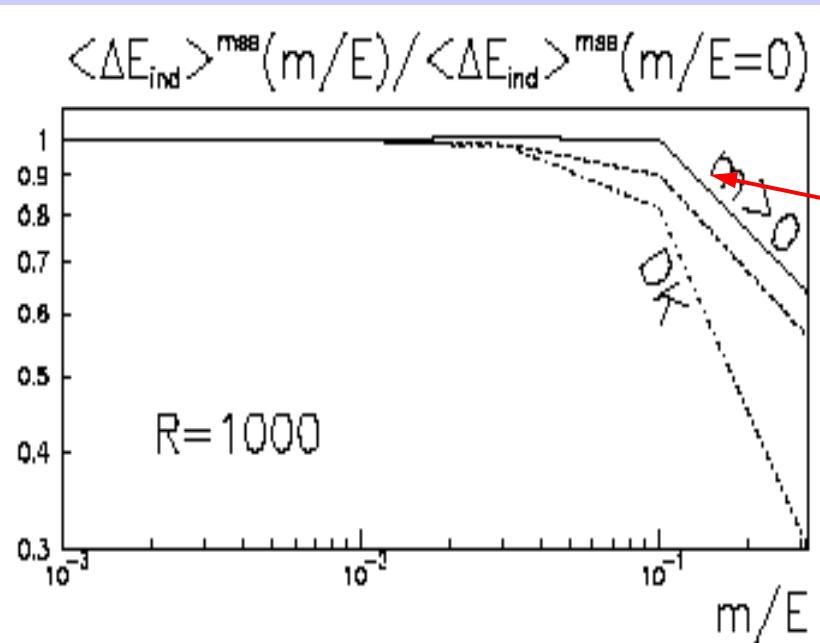
↑ color charge    ↑ mass effect

## 1. Motivation (III):

- Massive partons radiate less in the vacuum: **dead cone effect**, postulated for the medium (*Dokshitzer-Kharzeev '01*).
- Technically: rescattering+dead cone (*Djordjevic et al '03; Zhang et al '03; Armesto et al '03*).



- Heavy-to-light ratios  $R_{D,B/h} = R_{AA}^{D,B}/R_{AA}^h$ : sensitive to** (*Armesto et al '05*)



- **Color-charge dependence** (g to light hadrons important, increases  $R_{D,B/h}$ ).
- **Mass dependence** (Q radiate less, increases  $R_{D,B/h}$ ).
- Detailed behavior of the partonic  $p_T$  spectrum (softer for Q, increases  $R_{D,B/h}$ ) and fragmentation functions (harder for Q, decreases  $R_{D,B/h}$ ).

## 2. Model (I):

Standard LO pQCD (PYTHIA):

$$\frac{dN_{\text{medium}}^{AB-h}}{dp_T dy} \Big|_{y=0} = \sum_{i,j} \int dx_i dx_j d(\Delta E/E) dz_k f_{i/A}(x_i) f_{j/B}(x_j) \\ \times \frac{d\hat{N}^{ij-k}(p_{T,k} + \Delta E)}{dp_{T,k} dy} \Big|_{y=0} \frac{P(\Delta E/E, R, \omega_c, m/E)}{z_k^2} D_{k \rightarrow h}(z_k)$$

### Quenching weights

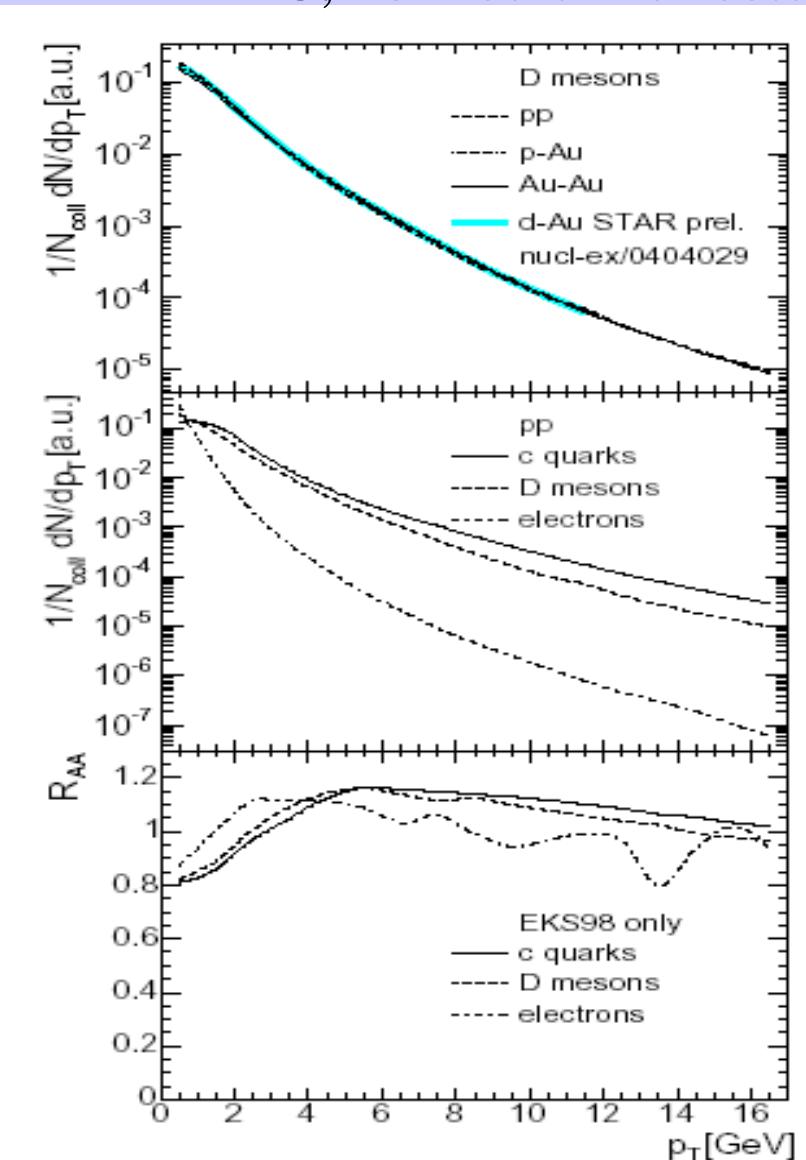
([www.pd.infn.it/~dainesea/qwmassive.html](http://www.pd.infn.it/~dainesea/qwmassive.html)):

probability for medium energy loss,  
they contain a no-eloss contribution.

- CTEQ4L pdf's, EKS98.
- All channels into account.
- Ff into D (B) and semileptonic e-decays.
- RHIC: tune to STAR D-meson data.
- LHC: tune to NLO pQCD calculation.

*Testing radiative energy loss at RHIC and the LHC*

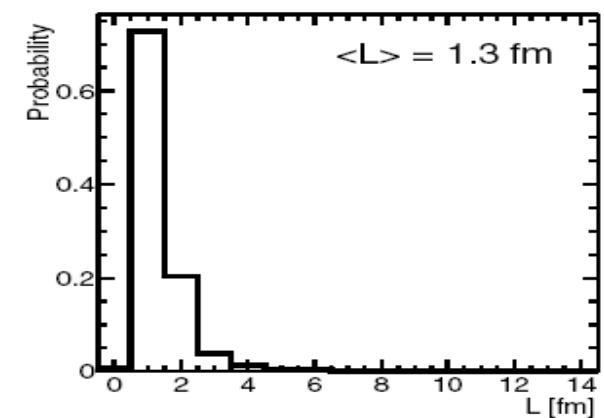
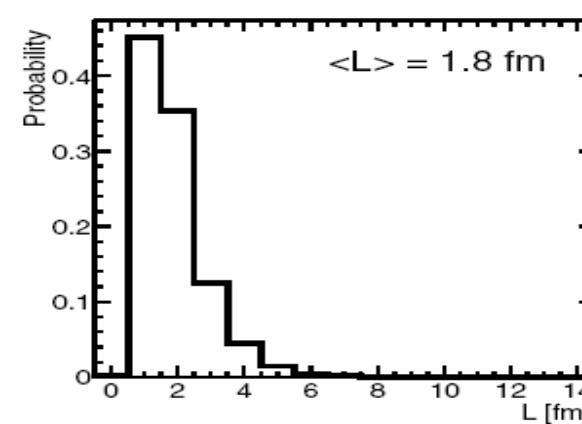
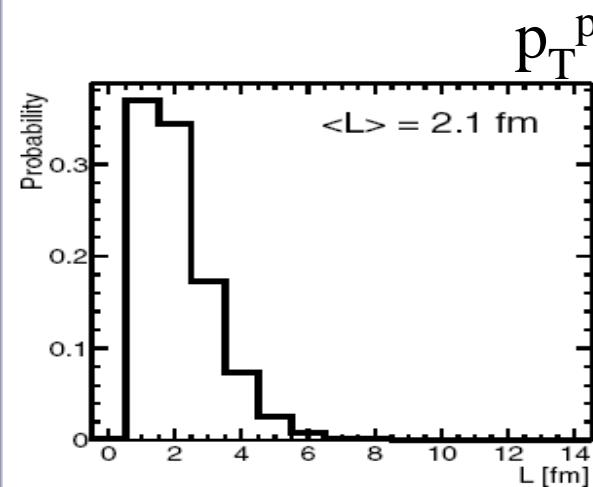
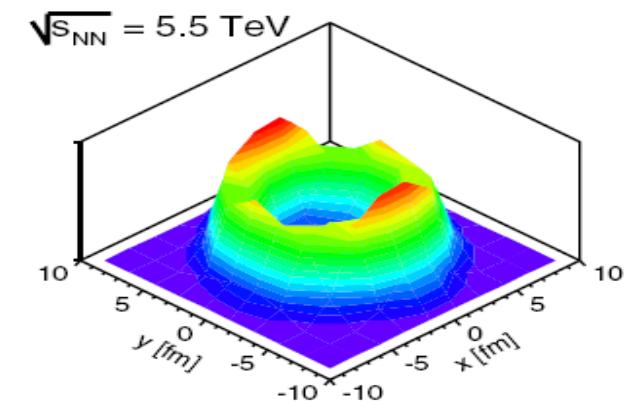
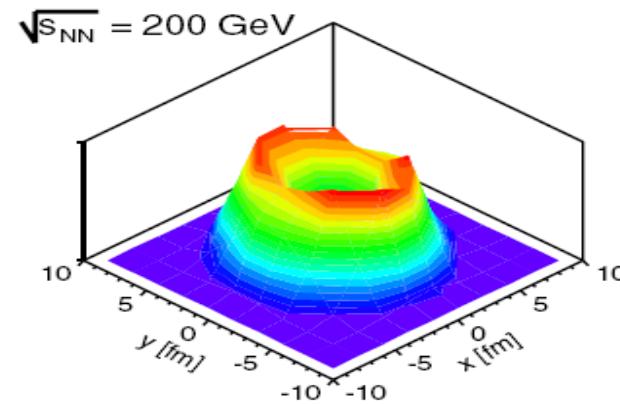
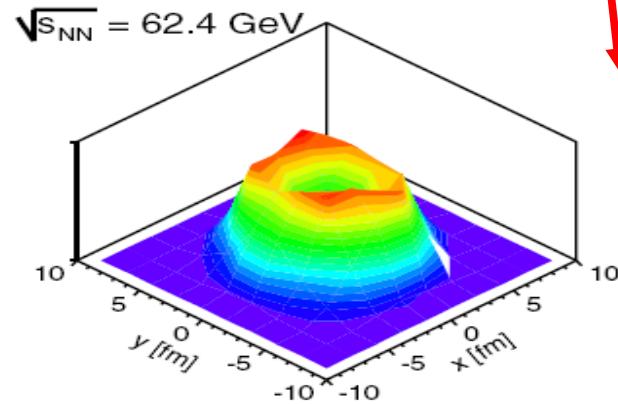
RHIC, no medium effects

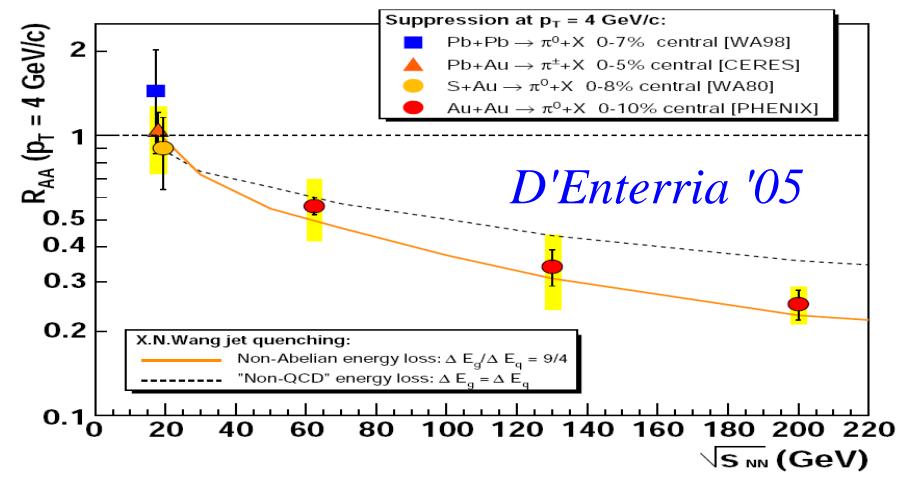
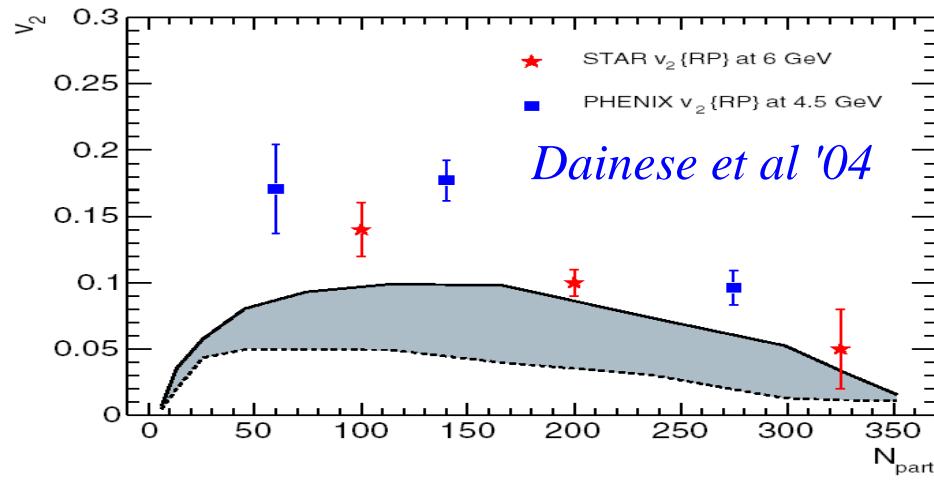
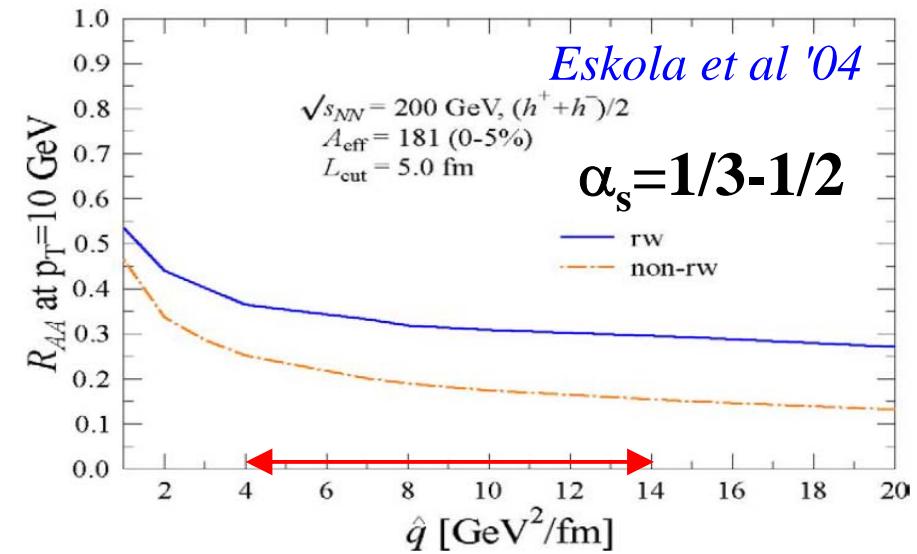
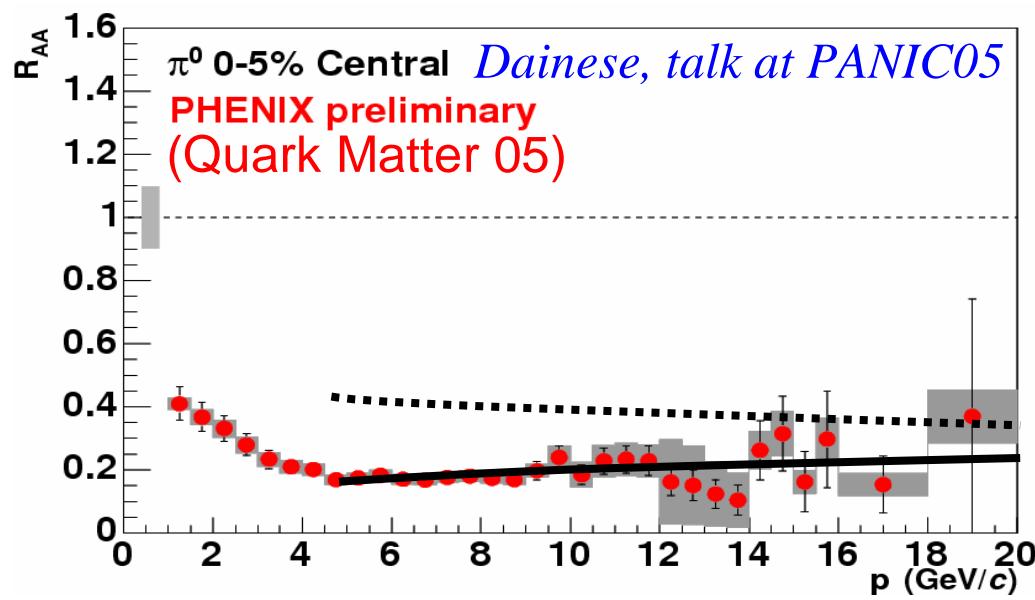


## 2. Model (II):

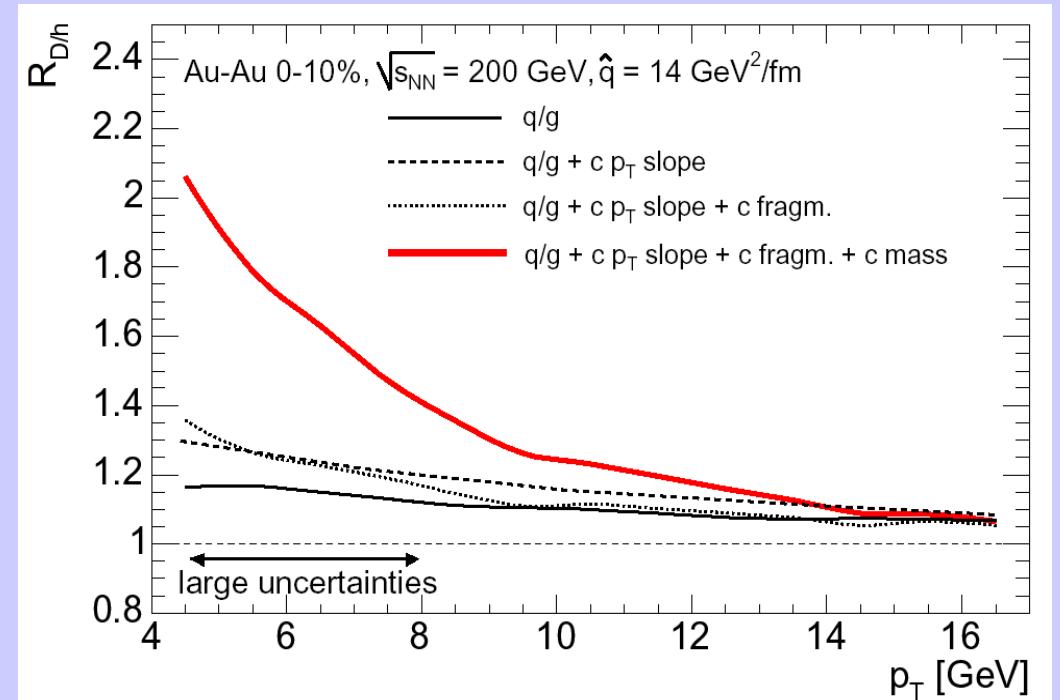
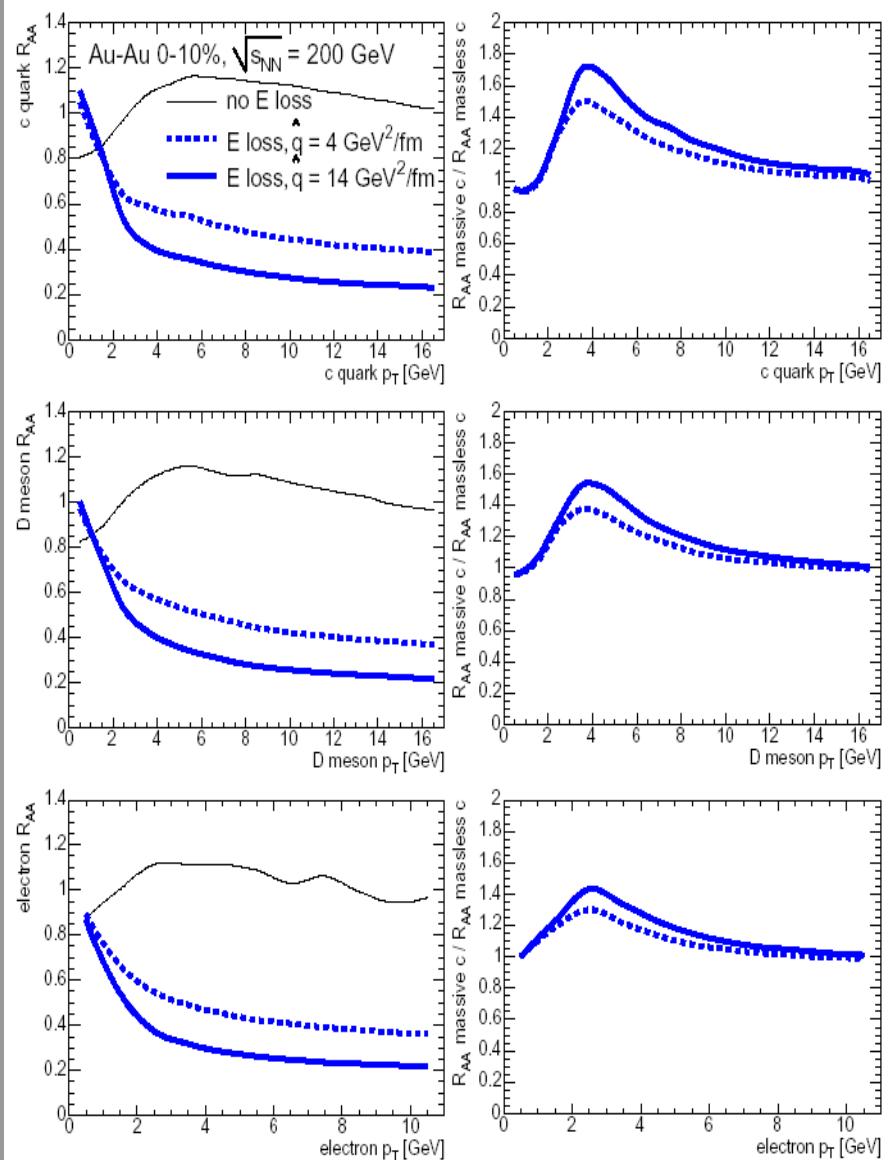
(Dainese et al '04, '05; Eskola et al '04)

Detailed modeling of geometry.





### 3. Results for RHIC:

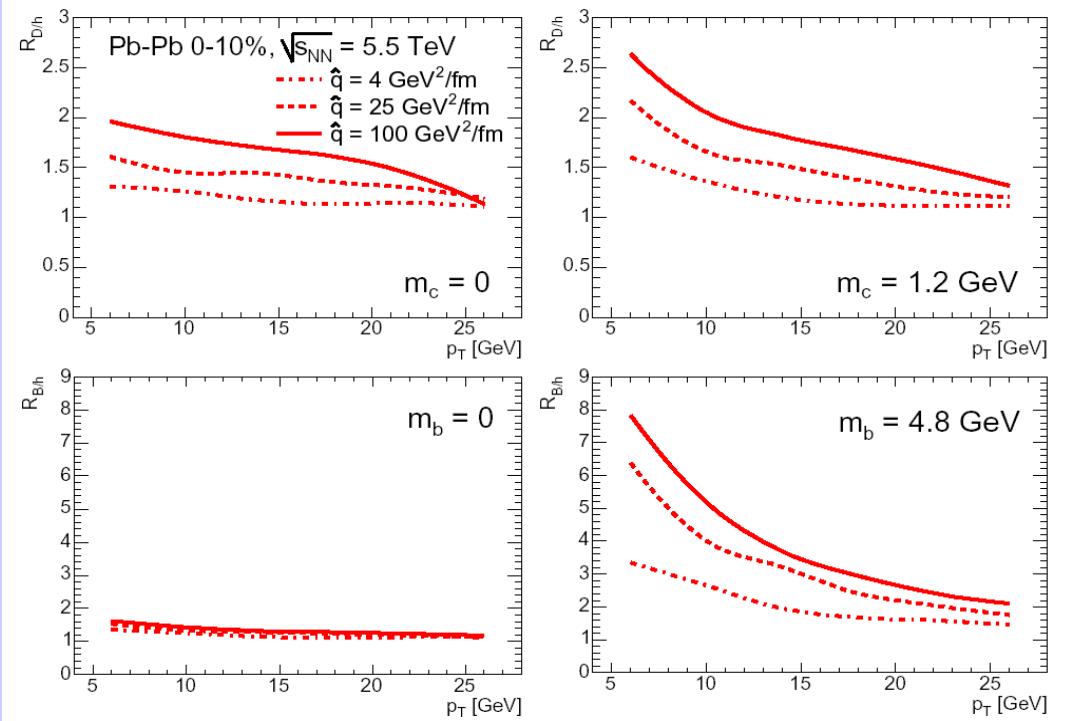
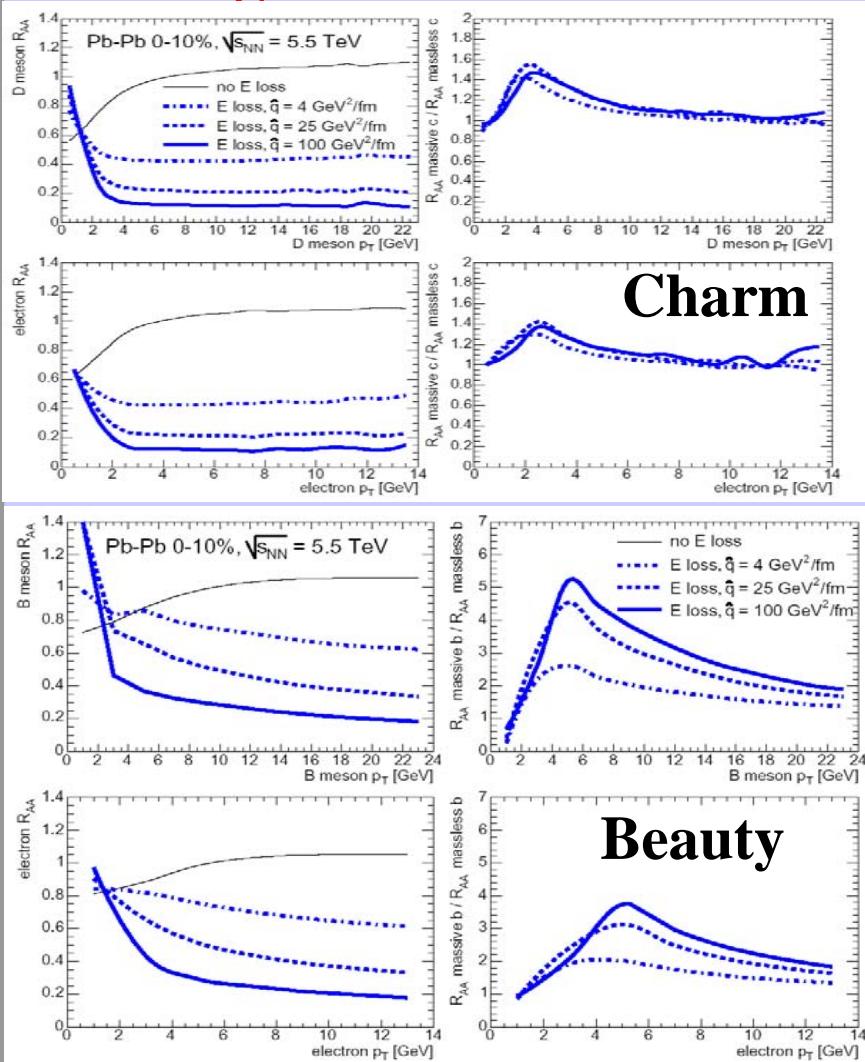


$$R_{D/h} = R_{AA}^D / R_{AA}^h \quad (\text{Dokshitzer-Kharzeev '01}).$$

- q/g difference affects all  $p_T$ .
- Mass effects sizeable for  $p_T < 12 \text{ GeV}$ .
- Look at  $7 < p_T < 12 \text{ GeV}$ .

## 4. Results for the LHC:

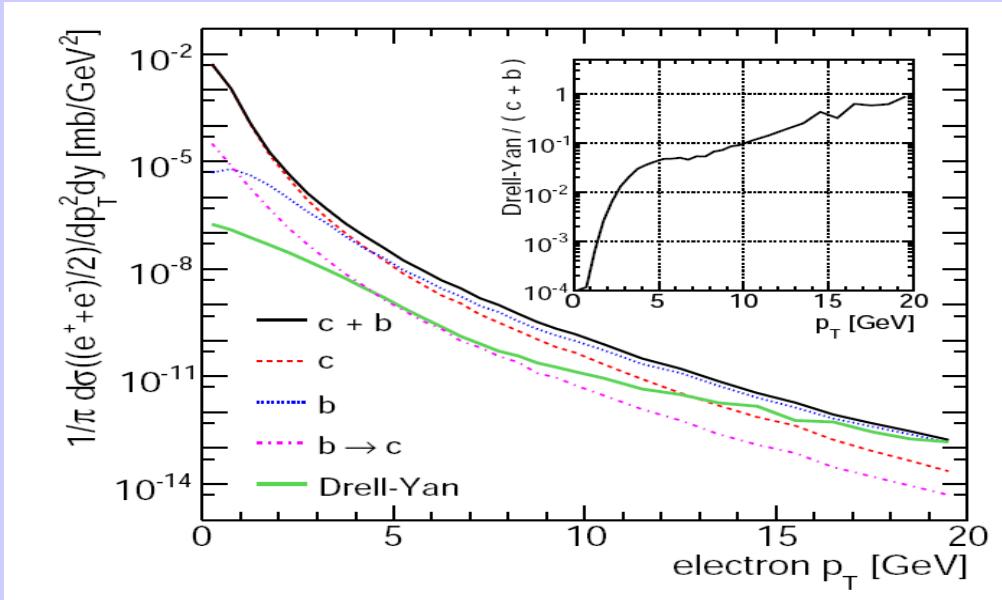
Transport coefficient (density) scaled by multiplicity: factor 2.5 to 7  
larger at the LHC than at RHIC (Armesto et al '04, Eskola et al '04).



- Small difference between massless c and b.
- $10 < p_T < 20$  GeV: charm sensitive to color ( $g$  at low  $x$ ), bottom to mass.

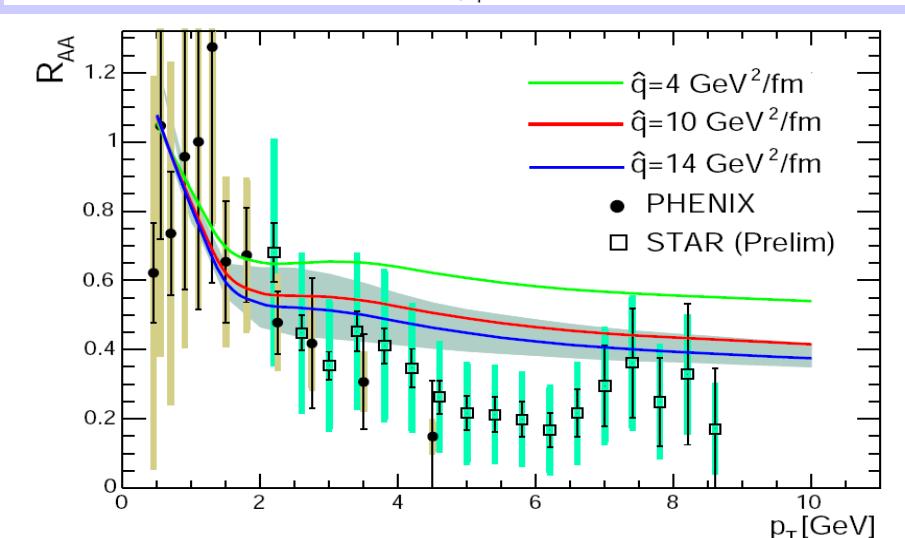
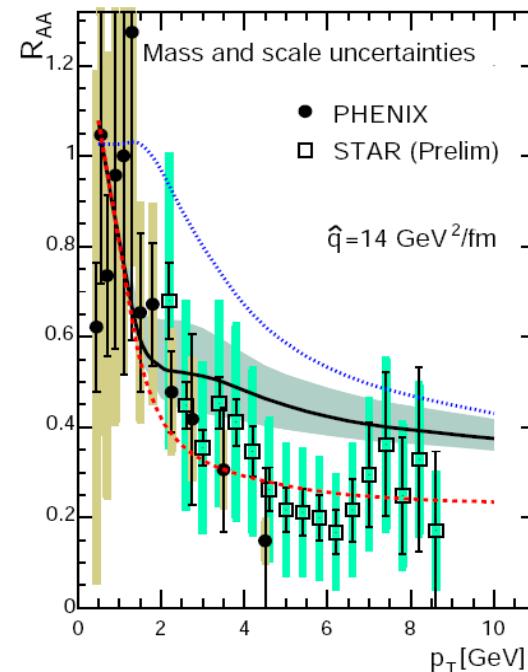
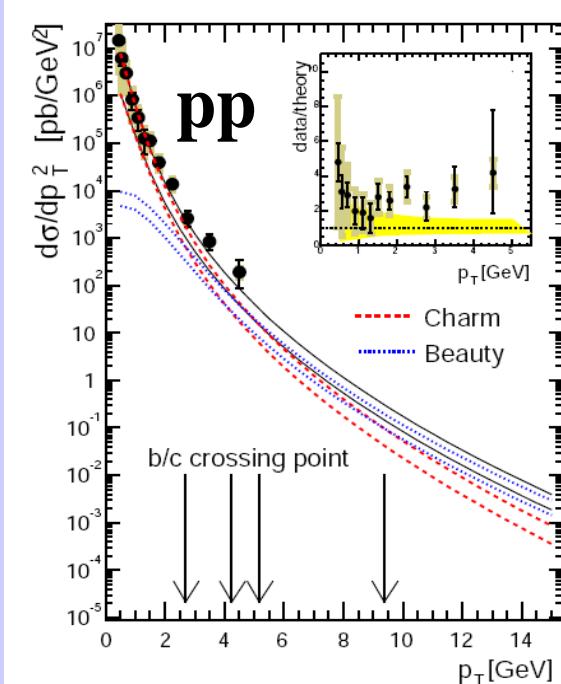
# 5. Single electrons at RHIC (I):

- RHIC data in AuAu: non-photonic electron spectra (measured - cocktail - conversion: *PHENIX '06; STAR '05*), weak correlation in  $p_T$  with parent D, and other contributions (B's) (*Djordjevic et al '05; '06; Armesto et al '05*).
- Heavy flavor: FONLL (*Cacciari et al '98; '01; '05*) partonic spectra supplemented with radiative loss via quenching weights plus FONLL fragmentation:  
 \* Uncertainties (mass and scale variation).

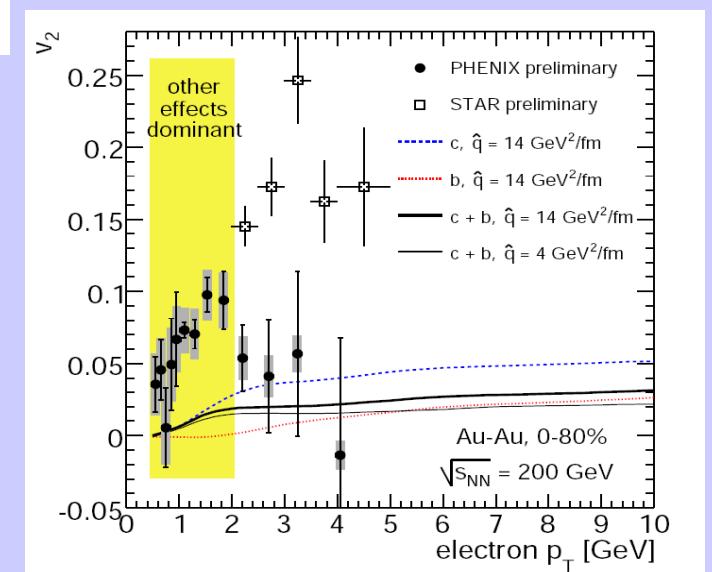


- DY: PYTHIA tuned to NLO (*Gavin et al '95*), it may become important for  $p_T > 10$  GeV.
- A 10% contribution from DY may influence  $R_{\text{AuAu}}^e$  as much as 0.1.

## 5. Single electrons at RHIC (II):



- pp data underestimated by FONLL (*Cacciari et al '05*).
- Suppression in AuAu compatible with c only.
- Variations in  $\hat{q}$  ~ uncertainties.
- $v_2$  compatible with data (*PHENIX '05*).



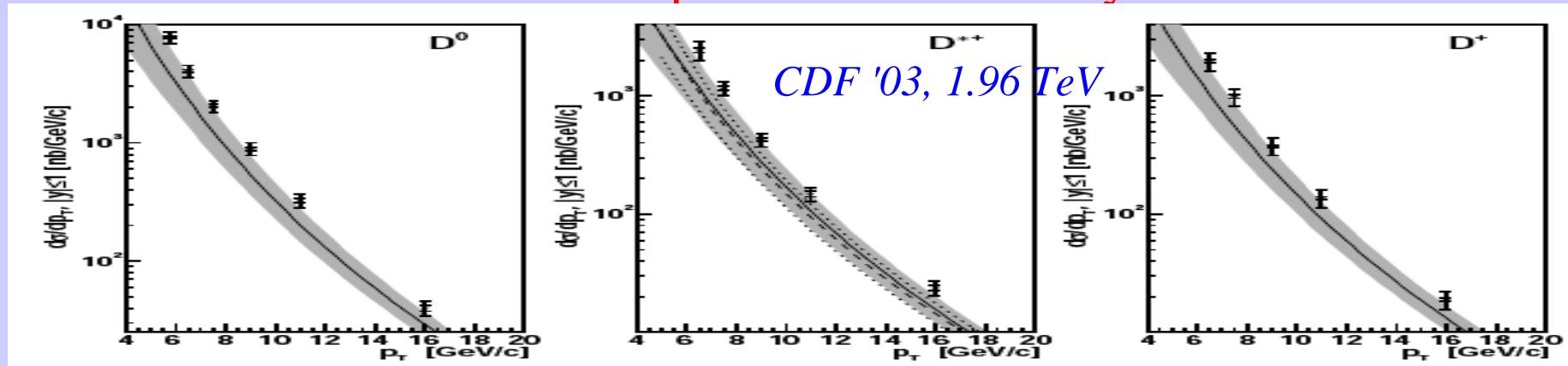
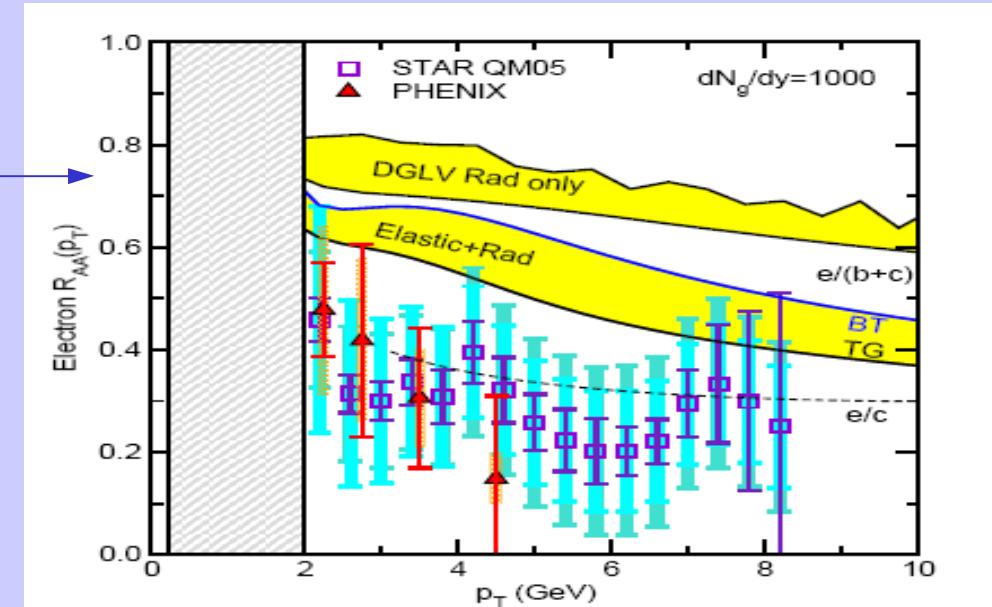
## 5. Single electrons at RHIC (III):

If  $R_{\text{AuAu}}^e < 0.4$  in the range  $5 < p_T < 10 \text{ GeV}$ :

- Strong interaction of  $Q$  with the medium; hadronization inside, elastic scattering? (Djordjevic *et al* '06, Hees *et al* 05, Teaney *et al* '05).

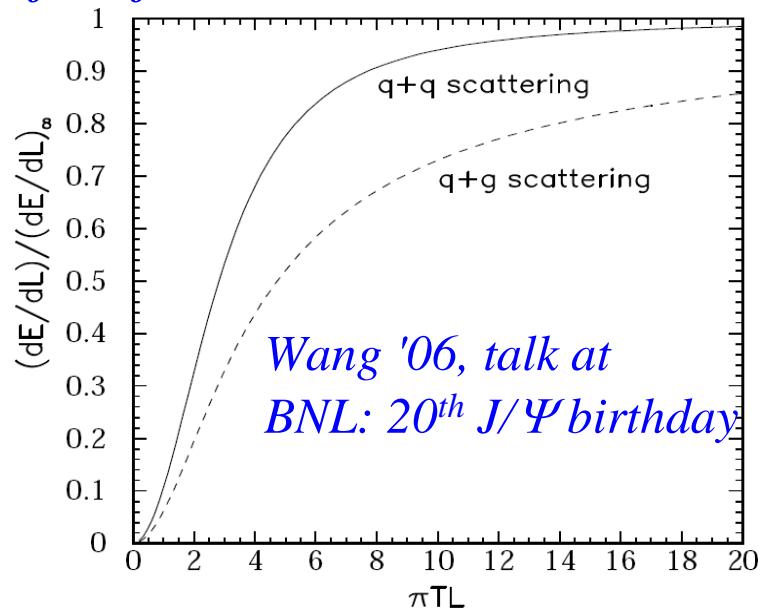
- Larger transport coefficient?  
(but upper bound to come, hopefully, from correlations (PHENIX '05; STAR '06)).

- How well do we control the production of heavy flavors at RHIC?



# Note: elastic scattering

- Historically considered << than radiative eloss (*Bjorken '82; Gyulassy-Braaten-Thoma '91*).
- *Mustafa '05; Djordjevic et al '06; Alam et al '06*: new interest due to single electron data, idea extended from heavy to light flavors.
- *Peigne et al '05*: elastic eloss strongly reduced due to finite L.
- *Djordjevic '06*: effect of finite interaction time (L) negligible.



- *Wang '06*: elastic and inelastic elosses in the same multiple scattering formalism. For **light** flavors:

$$\Delta E_{\text{rad}}/\Delta E_{\text{el}} \sim 3.14 \alpha_s LT \ln(EL/11) \sim 22$$

for  $E=10 \text{ GeV}$ ,  $T=0.2 \text{ GeV}$ ,  $L=6 \text{ fm}$ ,  $\alpha_s=0.3$

## 6. Conclusions:

- Heavy flavors constitute an experimentally accessible testing ground for our understanding of radiative energy loss.
- Both at RHIC and at the LHC heavy-to-light ratios offer solid possibilities to check the formalism like those presented here.
- Single electrons in AuAu at RHIC may demand other effects like elastic scattering, hadronization in medium, strong interactions,...

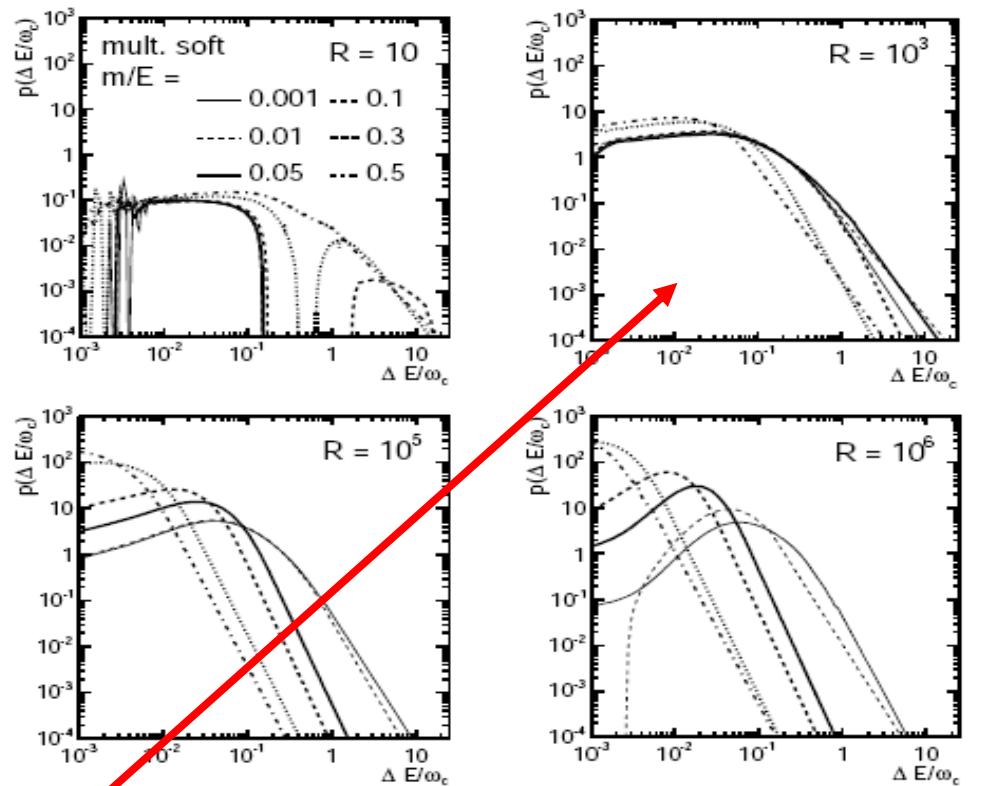
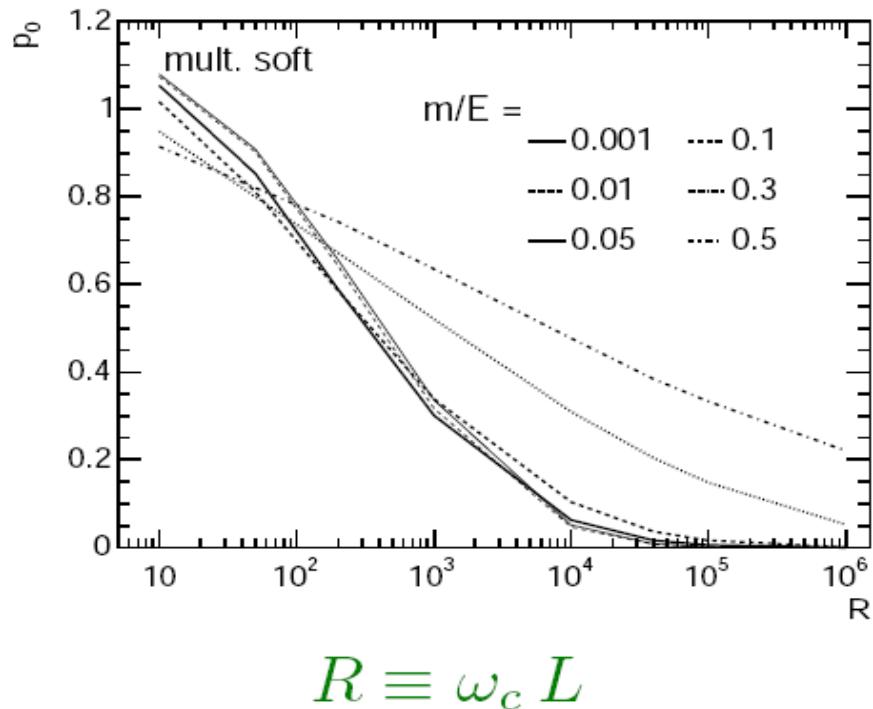
**BUT**

**experimental data are not inconsistent with radiative loss.**

- Clarification of this issue will demand (at RHIC and at the LHC):
  - \* pp/dAu reference to be controlled.
  - \* If possible, data for mesons, not only for electrons.
- Further work needed: energy constraints, consideration of virtualities, ..., crucial for associated particle production.

# *Backup I: quenching weights*

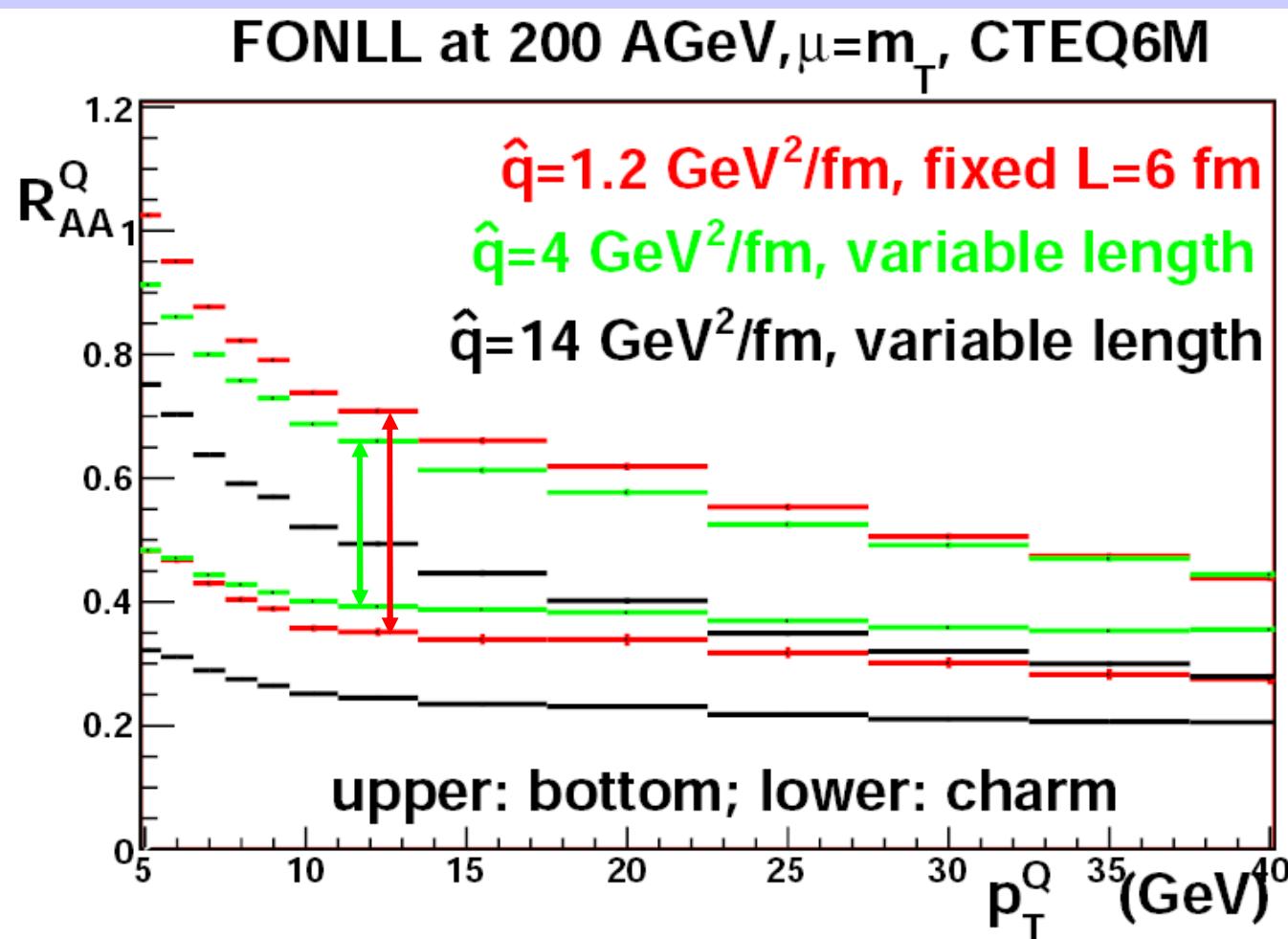
probability of no-energy loss



Mass effect smaller for smaller  $R = \hat{q} L^3 / 2$ , so smaller for smaller lengths.

# *Backup II: fixed vs. variable L*

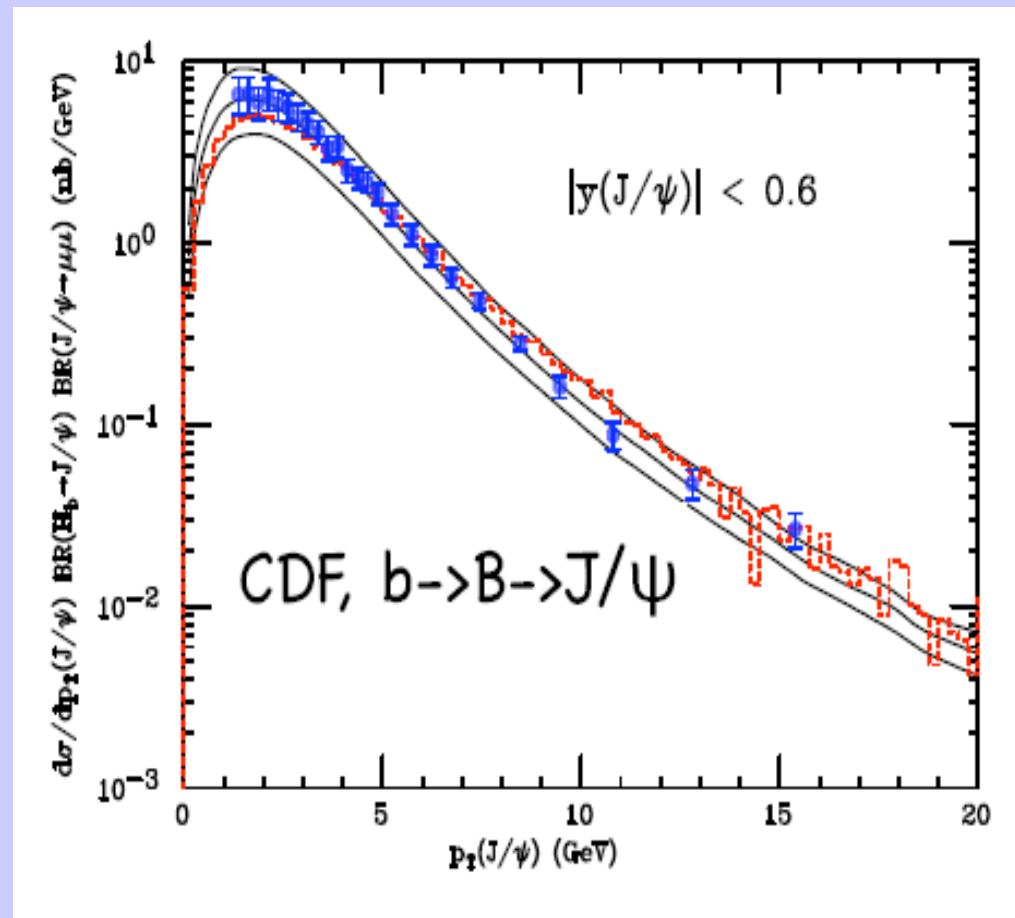
To try to understand a disagreement with Djordjevic et al '05



- $m_c = 1.5 \text{ GeV}$ ,  
 $m_b = 4.75 \text{ GeV}$ ; no fragmentation.
- $\hat{q}=1.2 \text{ GeV}^2/\text{fm}$  with fixed  $L=6 \text{ fm}$  reproduce  $R_{AA}(0-10\%) \sim 0.2$  for pions.
- A large fixed length produces a larger effect of the mass on the loss: mass effect small for small  $L$ .

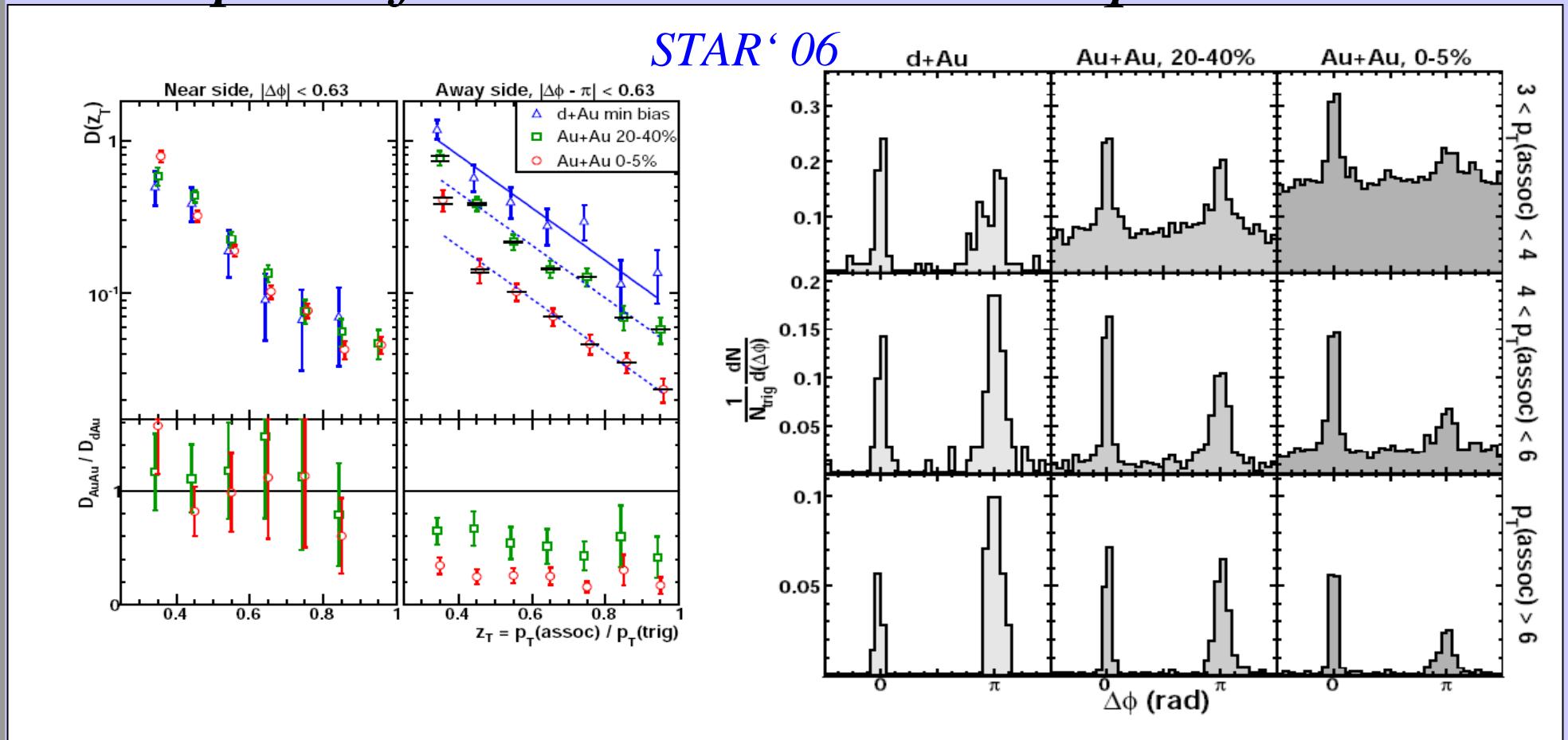
# Backup III: bottom in FONLL

Cacciari et al '03; '04



Reasonable description of  $b$  production.

# *Backup IV: further constraints on $q\bar{q}$*



Tangential emission (*Dainese '05*); associated spectra not yet understood.