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Particle-Nucleus and Nucleus-Nucleus Scattering at Relativistic Energies

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**Recent developments in chiral dynamics of
hadrons and hadrons in a nuclear medium**

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These are preliminary lecture notes, intended only for distribution to participants

Recent developments in chiral dynamics of hadrons and hadrons in a nuclear medium

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Unitarized Chiral Perturbation Theory

Skillful combination of the information of the Chiral Lagrangians and unitarity in coupled channels.

- Pioneering work of *Kaiser, Siegel, Waas, Weise 95-97* using Lipmann-Schwinger eq. and input from Chiral Lagrangians as potential.

- Subsequent work

- Inverse Amplitude Method (IAM) \rightarrow $\left\{ \begin{array}{l} \text{Truong} \\ \text{Dobado, Peláez '97} \\ \text{Oller, E.O., Peláez '98} \end{array} \right.$

- (N/D) method \rightarrow $\left\{ \begin{array}{l} \text{Oller, E.O. '99} \\ \text{Oller, Meissner '01} \end{array} \right.$

- Bethe-Salpeter eq. \rightarrow $\left\{ \begin{array}{l} \text{Oller, E.O. '97} \\ \text{Nieves, Ruiz-Arriola '00} \end{array} \right.$

Hosaka, Hyodo ; Lutz, Kolomeitsev, Borasoy, Nijl, Weise

- Applications \rightarrow $\left\{ \begin{array}{l} \text{Ramos, Vicente, Marco, Parreño, Toki, Hirenzaki} \\ \text{Hosaka, Oka, Nacher, Palomar, Jido, Inoue, Roca} \\ \text{Cabrera, Okumura, Takahashi, Mizobe, Chiang} \\ \text{Kamalov, Bennhold, Hernández, García Recio} \end{array} \right.$

Meson-Baryon interaction

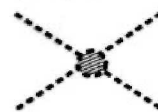
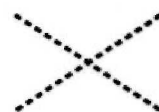
$$\mathcal{L}_1^{(B)} = \langle \bar{B} i \gamma^\mu \nabla_\mu B \rangle - M_B \langle \bar{B} B \rangle + \\ + \frac{D}{2} \langle \bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\} \rangle + \frac{F}{2} \langle \bar{B} \gamma^\mu \gamma_5 [u_\mu, B] \rangle$$

$$u_\mu = i u^\dagger \partial_\mu U u^\dagger \quad ; u^2 = U = e^{i \frac{\sqrt{2}}{f} \Phi}$$

$$\nabla_\mu B = \partial_\mu B + [\Gamma_\mu, B] \quad ; \quad \Gamma_\mu = \frac{1}{2} (u^\dagger \partial_\mu u + u \partial_\mu u^\dagger)$$

$$B(x) \equiv \begin{pmatrix} \frac{1}{\sqrt{2}} \Sigma^0 + \frac{1}{\sqrt{6}} \Lambda^0 & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}} \Sigma^0 + \frac{1}{\sqrt{6}} \Lambda^0 & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}} \Lambda^0 \end{pmatrix}$$

$$\chi \text{ PT: (mesons)} \quad \Phi \equiv \begin{pmatrix} \frac{1}{\sqrt{2}} \pi^0 + \frac{1}{\sqrt{6}} \eta & \pi^+ & \kappa^+ \\ \pi^- & -\frac{1}{\sqrt{2}} \pi^0 + \frac{1}{\sqrt{6}} \eta & \kappa^0 \\ \kappa^- & \bar{\kappa}^0 & -\frac{2}{\sqrt{6}} \eta \end{pmatrix}$$



Successful at low energies

Problems → { Limited energy range of applicability
Cannot deal with resonances

General scheme *Oller, Meissner PL '01* (meson baryon as exemple)

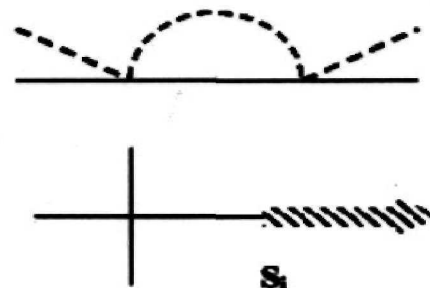
- **Unitarity** in coupled channels $\bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Sigma, \eta\Lambda, K\Xi$, in $S = -1$

$$\begin{aligned} \text{Im}T_{ij} &= T_{il}\sigma_{ll}T_{lj}^* \\ \sigma_l &\equiv \sigma_{ll} \equiv \frac{2Mq_l}{8\pi\sqrt{s}} \\ \sigma &= -\text{Im}T^{-1} \end{aligned}$$

- Dispersion relation

$$\begin{aligned} T_{ij}^{-1} &= -\delta_{ij} \left\{ \hat{a}_i(s_0) + \frac{s-s_0}{\pi} \int_{s_i}^{\infty} ds' \frac{\sigma(s')_i}{(s-s')(s'-s_0)} \right\} + \\ &+ V_{ij}^{-1} \equiv -g(s)_i \delta_{ij} + V_{ij}^{-1} \end{aligned}$$

$g(s)$ accounts for the right hand cut



V accounts for local terms, pole terms and crossed dynamics. V is determined by matching the general result to the χ PT expressions (usually at one loop level)

$$g(s) = \frac{2M_i}{16\pi^2} \left\{ a_i(\mu) + \log \frac{m_i^2}{\mu^2} + \frac{M_i^2 - m_i^2 + s}{2s} \log \frac{M_i^2}{m_i^2} + \frac{q_i}{\sqrt{s}} \log \frac{m_i^2 + M_i^2 - s - 2q_i\sqrt{s}}{m_i^2 + M_i^2 - s + 2q_i\sqrt{s}} \right\}$$

μ regularization mass

a_i subtraction constant

Inverting T^{-1} :

$$T = [1 - Vg]^{-1}V$$

Example 1: Take $V \equiv$ lowest order chiral amplitude

In meson-baryon S -wave

$$[1 - V g] T = V \rightarrow T = V + V g T$$

Bethe Salpeter eqn. with kernel V

This is the method of *E. O., Ramos '98* using cut off to regularize the loops

Oller, Meissner show equivalence of methods with

$$a_i(\mu) \simeq -2 \ln \left[1 - \sqrt{1 + \frac{m_i^2}{\mu^2}} \right] ;$$

μ cut off

$$a_i \simeq -2 \rightarrow \mu \simeq 630 \text{ MeV in } \bar{K} N$$

If higher order Lagrangians not well determined
then fit a_i to the data

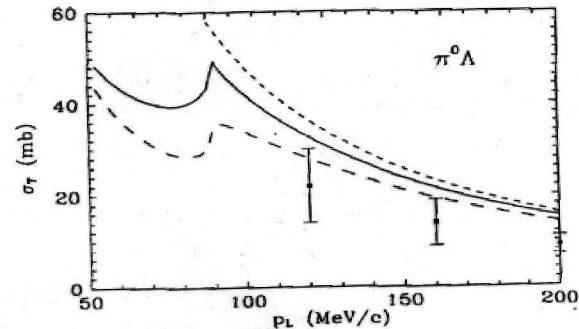
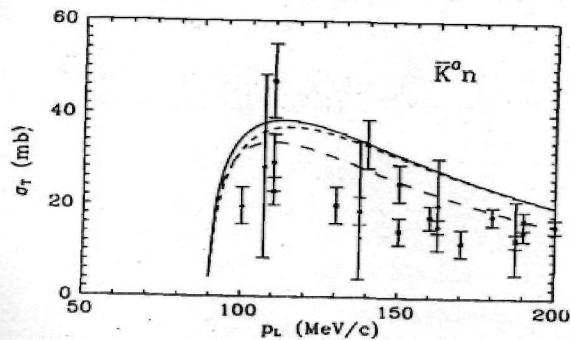
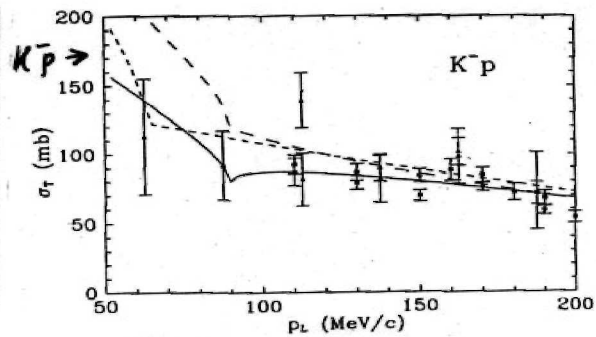
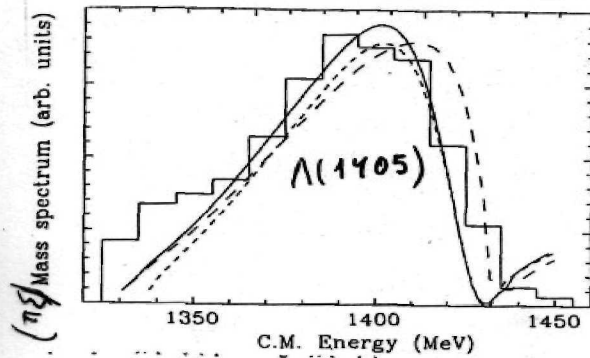
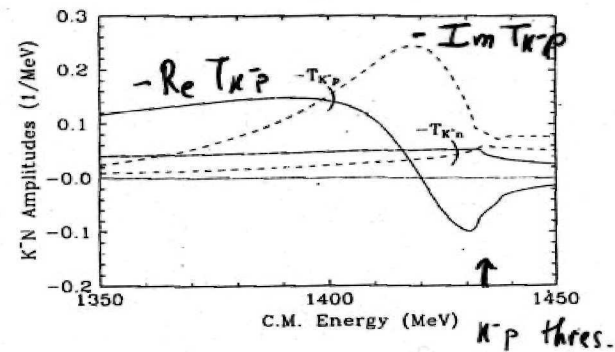
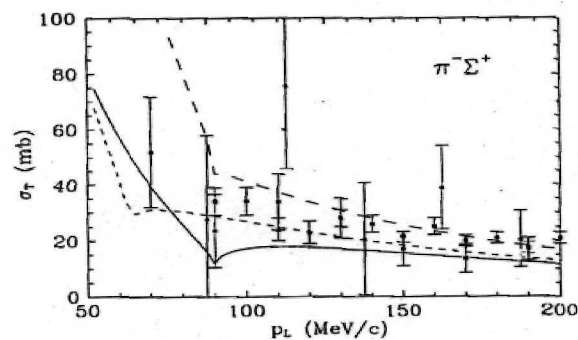
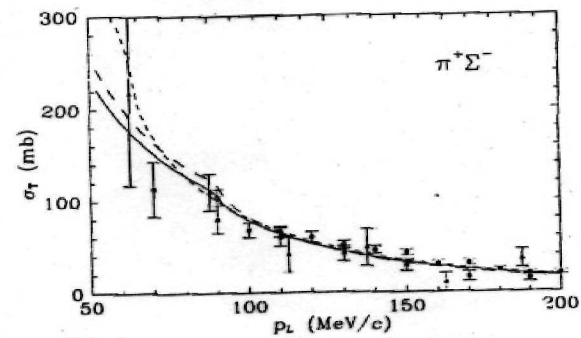
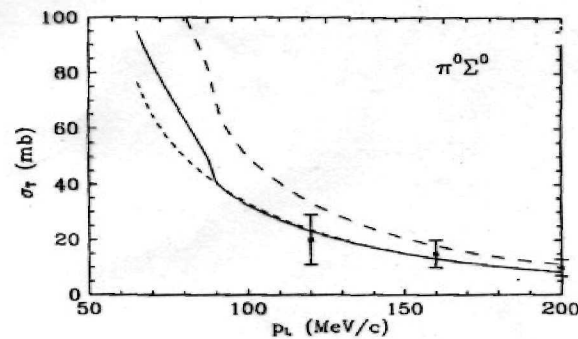
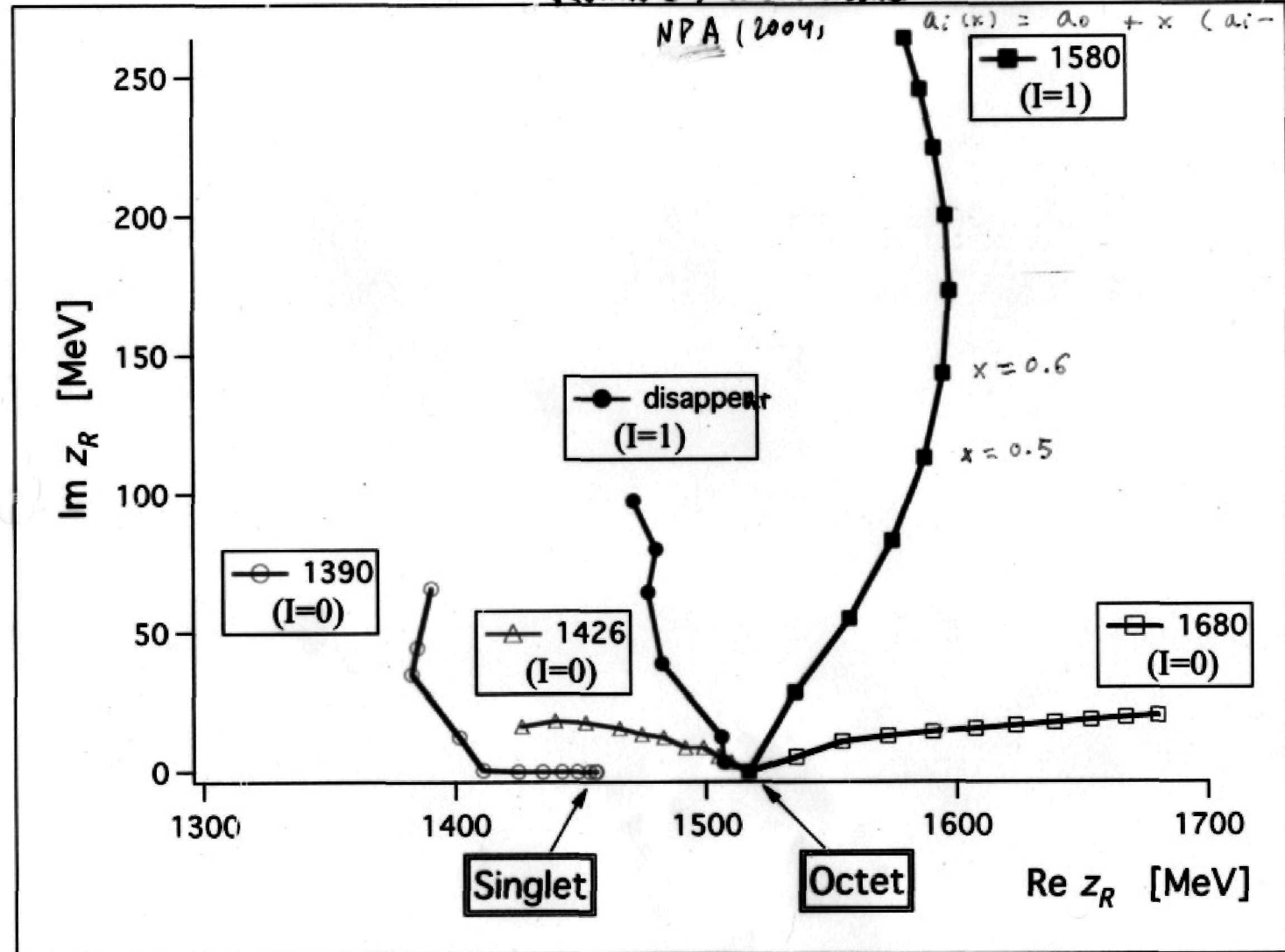


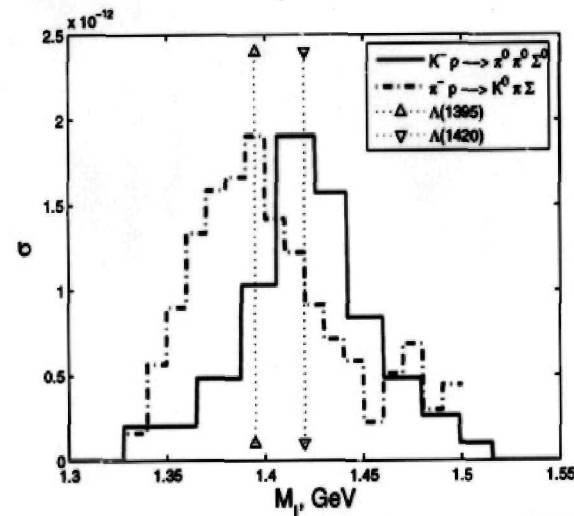
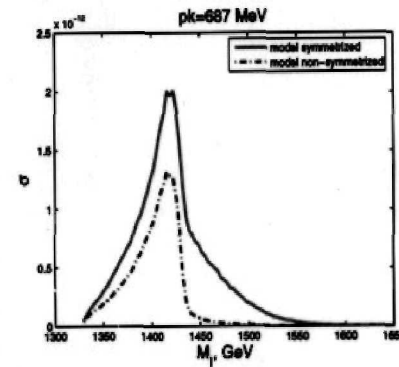
Fig. 5. Same as Fig. 3 for $K^- p \rightarrow \pi^0 \Lambda$.



D. Jido, Oller, E.O. Ramos, U.G. Meissner
 $M_i(x) = M_0 + x(M_i - M_0)$
 $m_i^2(x) = m_0^2 + x(m_i^2 - m_0^2)$
 $a_i(x) = a_0 + x(a_i - a_0)$
 NPA (2004)



Evidence for the two pole structure of the $\Lambda(1405)$



$$\begin{aligned} \Gamma &\approx 30 \text{ MeV} \\ M &\approx 1420 \text{ MeV} \end{aligned}$$

$$\begin{aligned} \Gamma &\approx 65 \text{ MeV} \\ M &\approx 1396 \text{ MeV} \end{aligned}$$

Evidence for the two pole structure of the $\Lambda(1405)$ resonance and the nature of the $\Lambda(1520)$ – p.6/11

Puri, March 2005

V. K. Magas, E. Oset and A. Ramos, **Phys. Rev. Lett.** 2005

$$\mathcal{L} = -i\bar{T}^\mu \not{D} T_\mu \quad (1)$$

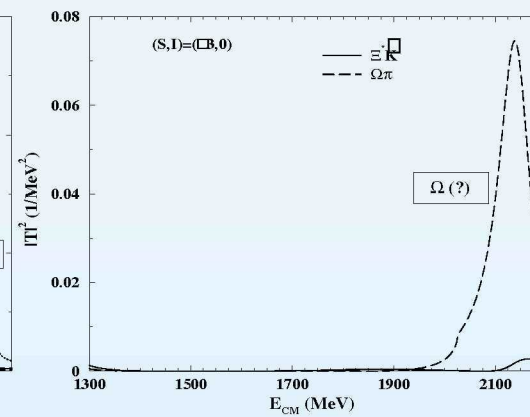
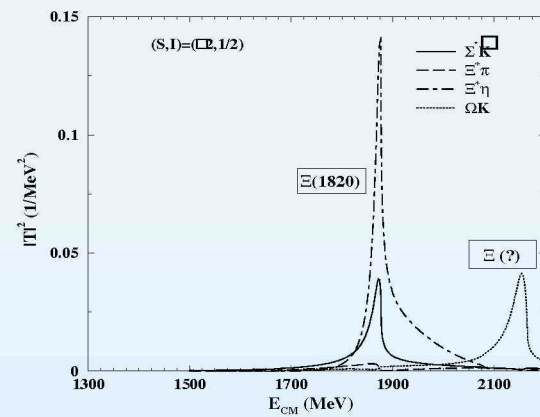
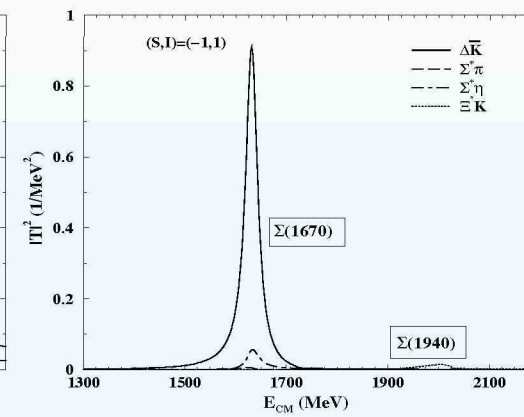
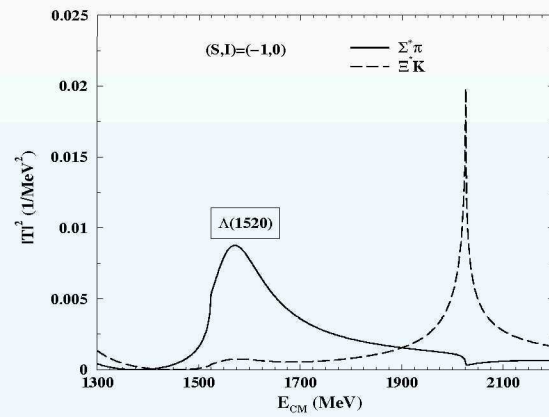
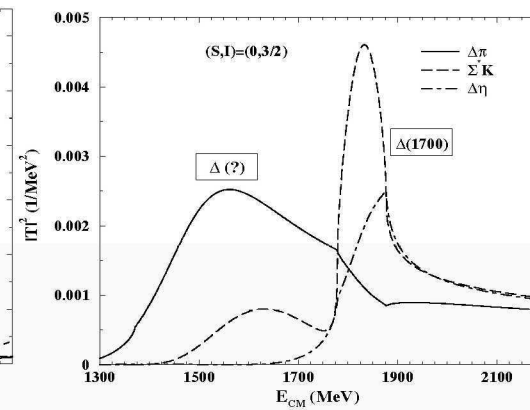
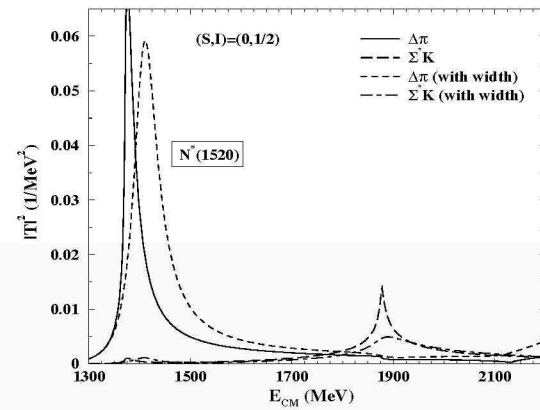
$$\mathcal{D}^\nu T_{abc}^\mu = \partial^\nu T_{abc}^\mu + (\Gamma^\nu)_a^d T_{dbc}^\mu + (\Gamma^\nu)_b^d T_{adc}^\mu + (\Gamma^\nu)_c^d T_{abd}^\mu \quad (2)$$

$$\Gamma^\nu = \frac{1}{2}(\xi \partial^\nu \xi^\dagger + \xi^\dagger \partial^\nu \xi) \quad (3)$$

$$\xi^2 = U = e^{i\sqrt{2}\Phi/f} \quad (4)$$

$$V_{ij} = -\frac{1}{4f^2} C_{ij} (k^0 + k'^0). \quad (5)$$

$$\begin{aligned} |\pi \Sigma^*; I=0\rangle &= \frac{1}{\sqrt{3}} |\pi^- \Sigma^{*+}\rangle - \frac{1}{\sqrt{3}} |\pi^0 \Sigma^{*0}\rangle - \frac{1}{\sqrt{3}} |\pi^+ \Sigma^{*-}\rangle \\ |K \Xi^*; I=0\rangle &= -\frac{1}{\sqrt{2}} |K^0 \Xi^{*0}\rangle + \frac{1}{\sqrt{2}} |K^+ \Xi^{*-}\rangle. \end{aligned} \quad (6)$$



Introduction of the $\bar{K}N$ and $\pi\Sigma$ channels

$\bar{K}N$ and $\pi\Sigma$ couple to $\pi\Sigma(1385)$ in D-wave

$$-it_{\bar{K}N \rightarrow \pi\Sigma^*} = -i\beta_{\bar{K}N} |\vec{k}|^2 \mathcal{C}(1/2 \ 2 \ 3/2; m, M-m) Y_{2,m-M}(\hat{k}) (-1)^{M-m} \sqrt{4\pi}. \quad (7)$$

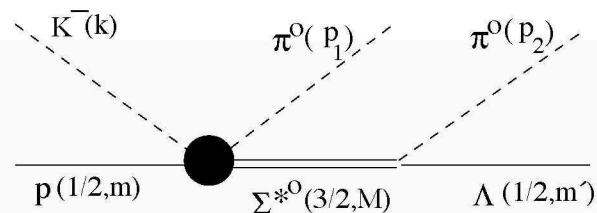
$$-it_{\pi\Sigma \rightarrow \pi\Sigma^*} = -i\beta_{\pi\Sigma} |\vec{k}|^2 \mathcal{C}(1/2 \ 2 \ 3/2; m, M-m) Y_{2,m-M}(\hat{k}) (-1)^{M-m} \sqrt{4\pi}. \quad (8)$$

$$V = \begin{vmatrix} C_{11}(k_1^0 + k_1^0) & C_{12}(k_1^0 + k_2^0) & \gamma_{13} q_3^2 & \gamma_{14} q_4^2 \\ C_{21}(k_2^0 + k_1^0) & C_{22}(k_2^0 + k_2^0) & 0 & 0 \\ \gamma_{13} q_3^2 & 0 & \gamma_{33} q_3^4 & \gamma_{34} q_3^2 q_4^2 \\ \gamma_{14} q_4^2 & 0 & \gamma_{34} q_3^2 q_4^2 & \gamma_{44} q_4^4 \end{vmatrix}, \quad (9)$$

We chose a to get the pole at the physical position. β and γ chosen to reproduce the partial decay widths of the $\Lambda(1520)$ into $\bar{K}N(45\%)$ and $\pi\Sigma(42\%)$ and $\bar{K}N$ phase shifts. From residues at pole $|g_{\pi\Sigma^*}| = 0.91$, $|g_{K\Xi^*}| = 0.29$, $|g_{\bar{K}N}| = 0.54$ and $|g_{\pi\Sigma}| = 0.45$.

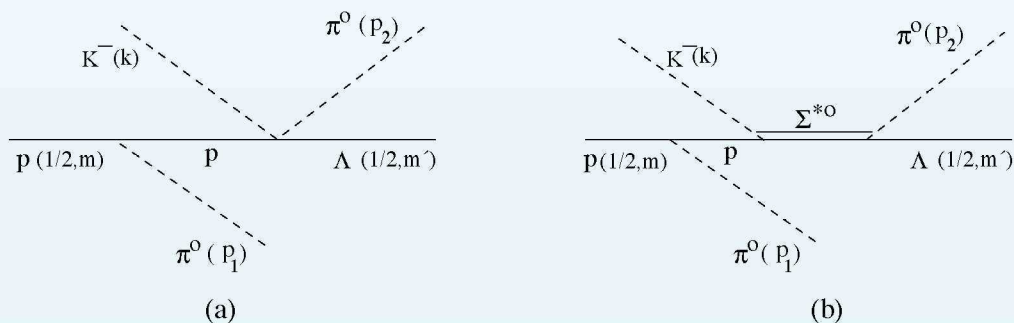
The reaction $K^- p \rightarrow \pi^0 \Sigma^{*0}(1385) \rightarrow \pi^0 \pi^0 \Lambda(1116)$

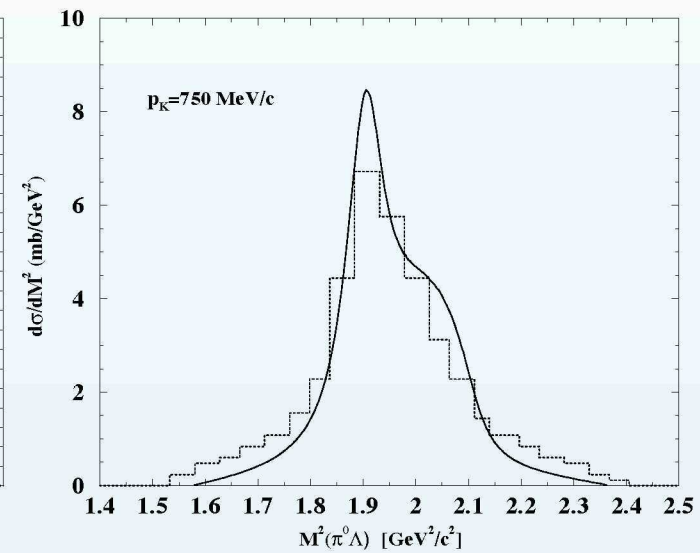
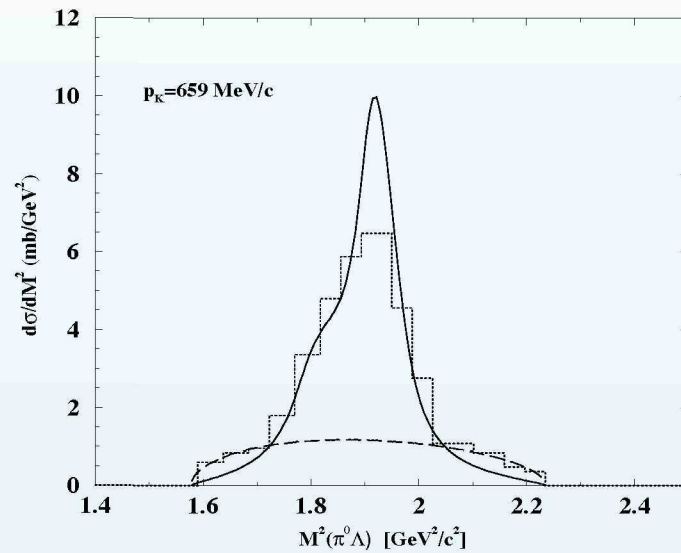
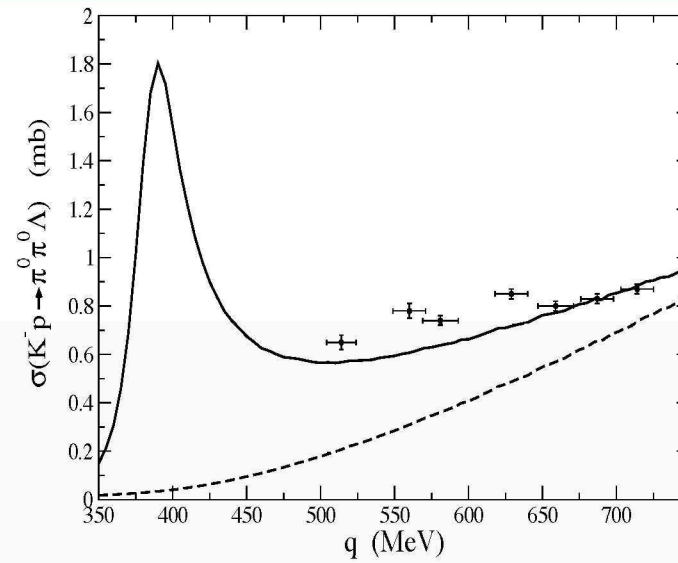
Prakhov...PRD04



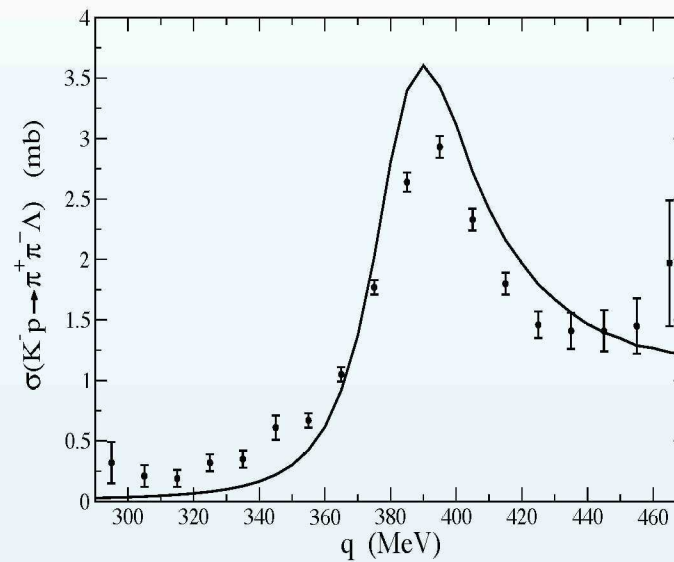
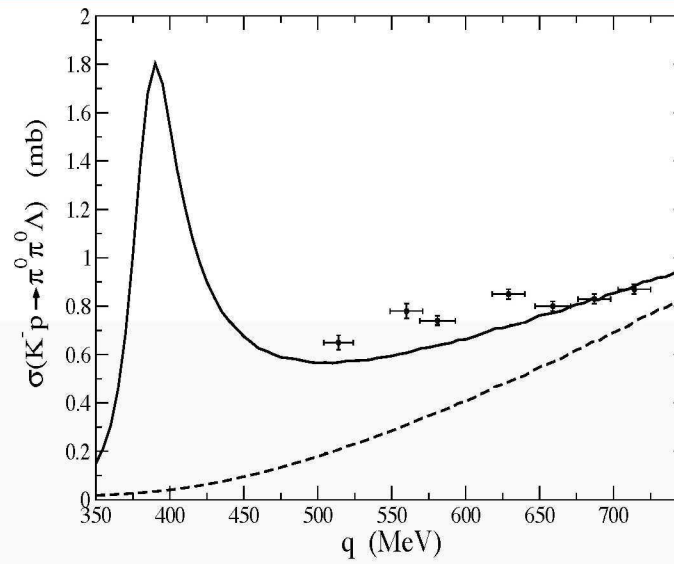
$$-it(\vec{p}_1, \vec{p}_2) = \frac{-iT_{\bar{K}N \rightarrow \pi \Sigma^*}}{3\sqrt{2}} \frac{f_{\Sigma^* \pi \Lambda}/m_\pi}{M_R - M_{\Sigma^*} + i\Gamma_{\Sigma^*}(M_R)/2} \begin{Bmatrix} -2p'_{2z} & m' = +1/2 \\ p'_{2x} + ip'_{2y} & m' = -1/2 \end{Bmatrix}. \quad (10)$$

Conventional scheme for $K^- p \rightarrow \pi^0 \pi^0 \Lambda$





$K^- p \rightarrow \pi^0 \pi^0 \Lambda$, Prakhov,



$K^- p \rightarrow \pi^0 \pi^0 \Lambda$, Prakhov, $K^- p \rightarrow \pi^+ \pi^- \Lambda$, Mast

Hadron in a nuclear medium

Talks of Mosel and Metag tuesday

Good review on the topic

M. Post, S. Leupold and U. Mosel , **Nucl. Phys. A 741 (2004) 81**


I present here examples closely linked to the chiral dynamics of the hadrons

- Kaons in a nuclear medium
- Kaon atoms
- $\Lambda(1520)$ in the medium

One does many body corrections in the $\bar{K}N$ amplitude

$$t(s) \rightarrow \tilde{t}(q, p)_{\substack{K \uparrow \\ N \uparrow}}$$

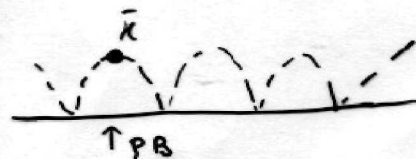
$$\Rightarrow \Pi_{\bar{K}}(q^0, q, p) = 2 \int \frac{d^3 p}{(2\pi)^3} n(\vec{p}) [\tilde{t}_{\bar{K}p}(q, p) + \tilde{t}_{\bar{K}n}(q, p)]$$



$$N \rightarrow \frac{1-n(\vec{p})}{p^0 - E(p) + i\epsilon} + \frac{n(\vec{p})}{p^0 - E(p) - i\epsilon}$$

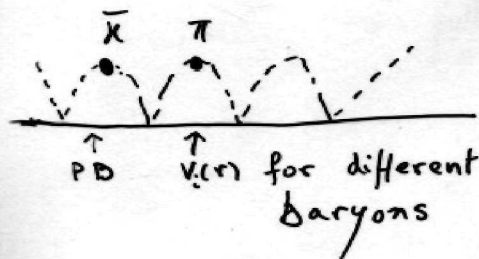
Pauli blocking Koch 94
Waas, Weise 97

Shifts the $\Lambda(1405)$ at higher energies



Selfconsistent use of \bar{K} selfenergy in the loops

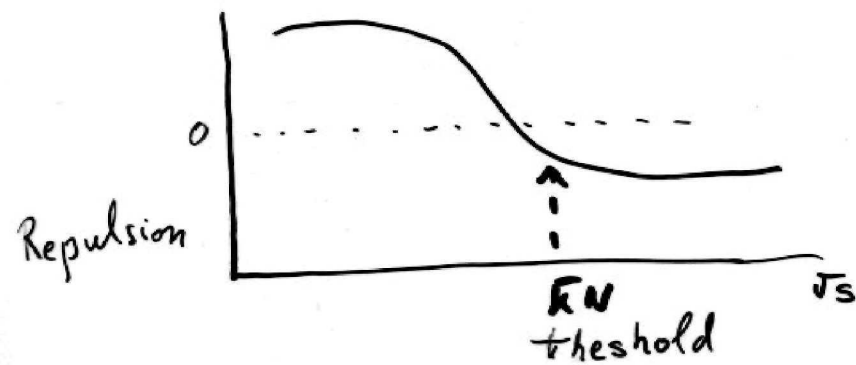
Lutz 98
Brings back the $\Lambda(1405)$ to the free position



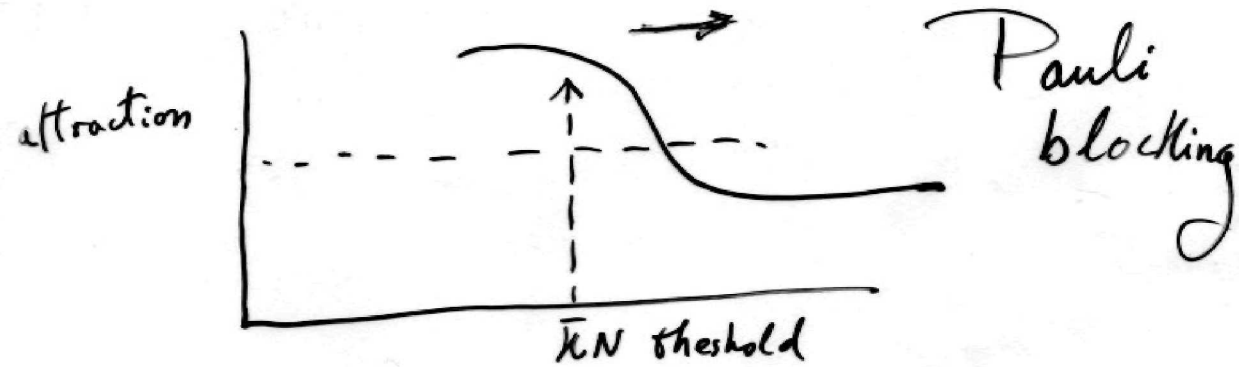
Selfcons. \bar{K} + π selfenergy + mean field baryon potential

Ramos, E.O.
NPA (2000)

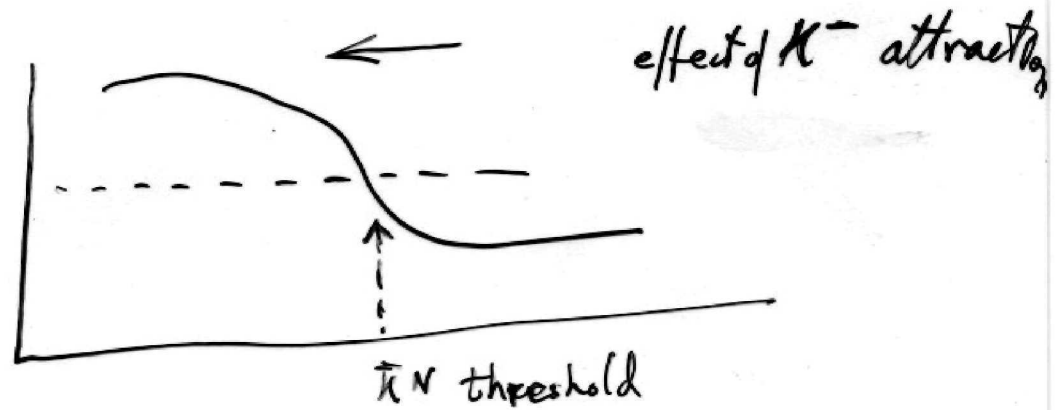
Opens new decay channels and widens spectral function



free
case



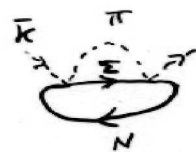
Pauli
blocking



effect of K^- attraction

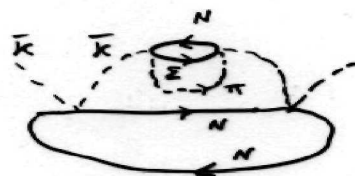
Medium decay channels

Koch
Waas, Weise



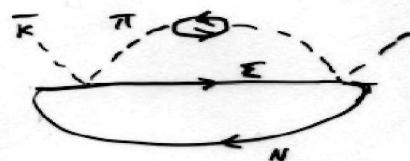
$$\bar{K} \Rightarrow (\Sigma h) \pi, (\Lambda h) \pi$$

Lutz



$$+ \bar{K} \rightarrow (\Sigma h)(p h), (\Lambda h)(p h) \pi$$

Ramos

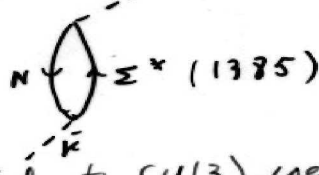
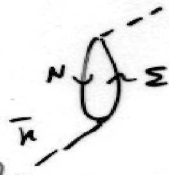


$$+ \bar{K} \rightarrow (\Sigma h)(p h), (\Lambda h)(p h)$$

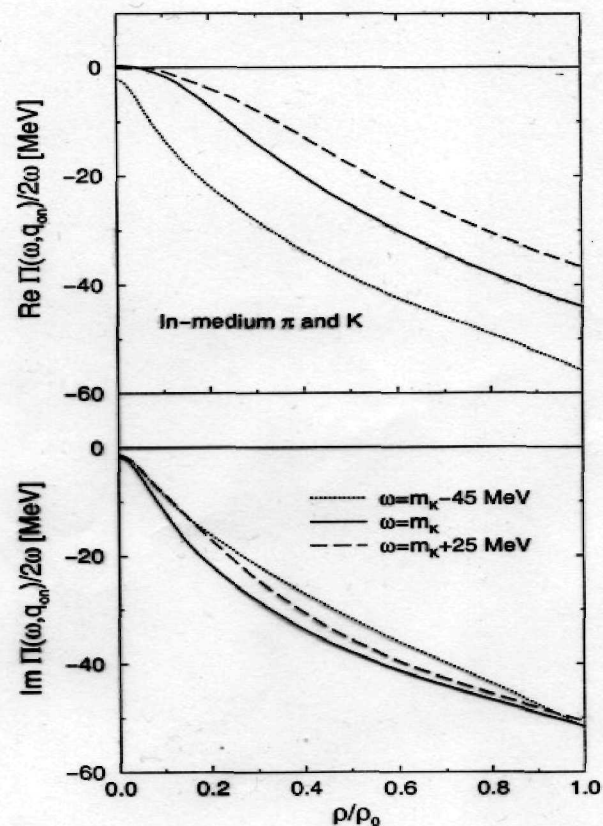


$$+ \text{extra } (\Sigma h)(p h) \pi, (\Lambda h)(p h) \pi$$

In addition we have p-wave \bar{K} selfenergy from Υh excitation



Couplings related to $SU(3)$ with D, F of original chiral Lagrangian



$\text{Re } V_{\text{opt}}$

$\text{Im } V_{\text{opt}} \equiv -\frac{\Gamma}{2}$

FIG. 7. Real (top) and imaginary (bottom) parts of the K^- optical potential as a function of density obtained from the *In-medium pions and kaons* approximation. Results are shown for three different K^- energies: $\omega = m_K - 45$ MeV (dotted lines), $\omega = m_K$ (solid lines) and $\omega = m_K + 20$ MeV (dashed lines).

Similar results in
 Schaffner-Bielich, Koch, Effenberg
 Cieply, Friedman, Gal, Mares NPA 2000
 NPA 2001

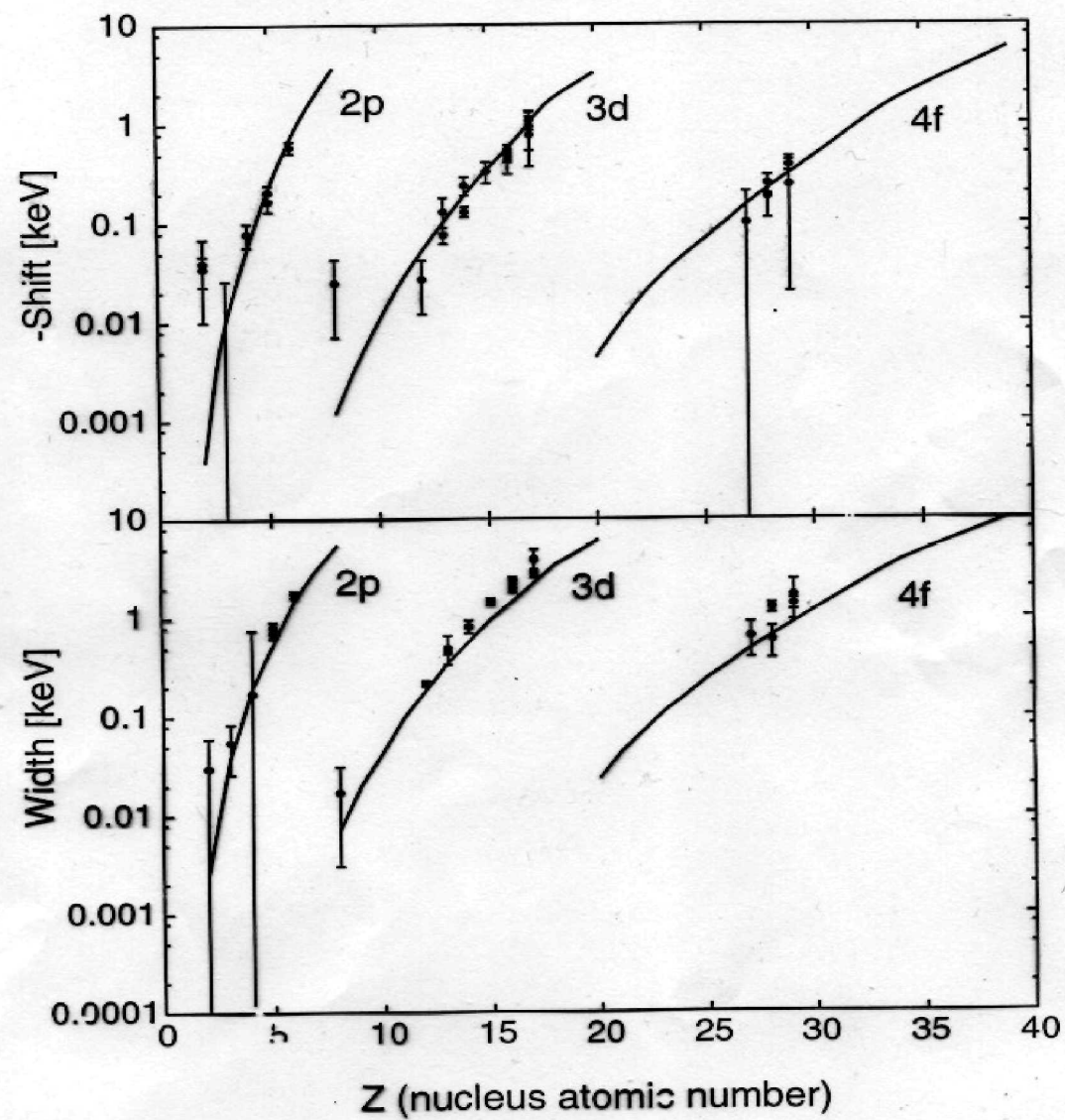
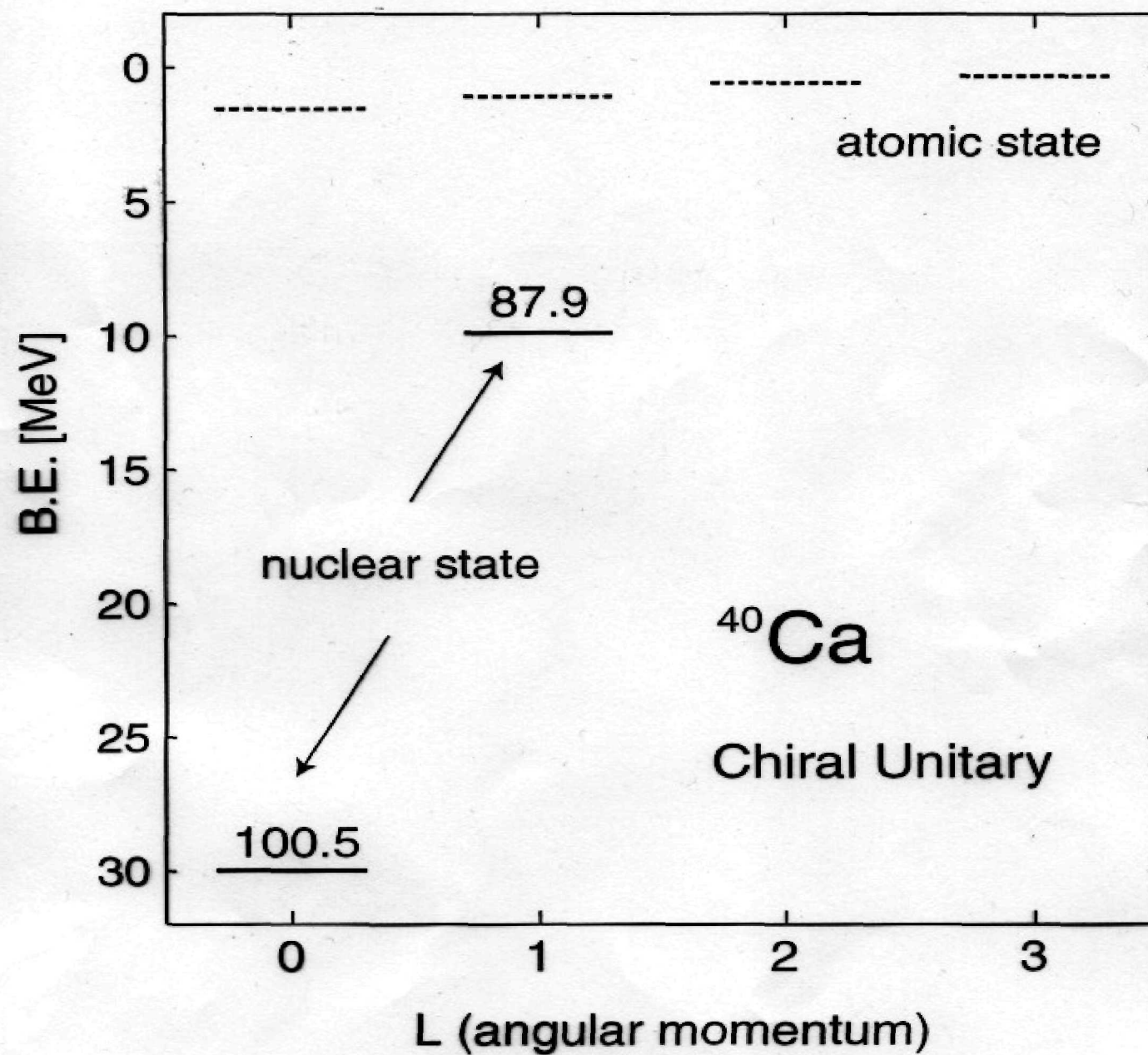


Fig.3



Claims of narrow deeply bound kaon atoms

Akaishi and Yamazaki made rough estimates of the kaon nucleus optical potential ignoring the selfconsistency and predicted **narrow bound states** For the $A=3$ and 4 systems

leads to binding energies of the kaon of the order of 70 MeV with widths around 75 MeV, (from $K^- N \rightarrow \pi \Sigma$).

Next, the nucleus is allowed to shrink to densities $\rho = 10\rho_0$

Then, K^- bound in 3He by 108 MeV and in 4He by 86 MeV

Experimentalist "find" a possible deeply bound K^- state. Suzuki et al. PLB597 (2004)

$K^- {}^4He \rightarrow Sp$, S(3115) Strange tribaryon.

But $l=1$, and if K^- state, $B=195$ MeV

Contradiction with AY with $l=0$ and 108 MeV!!

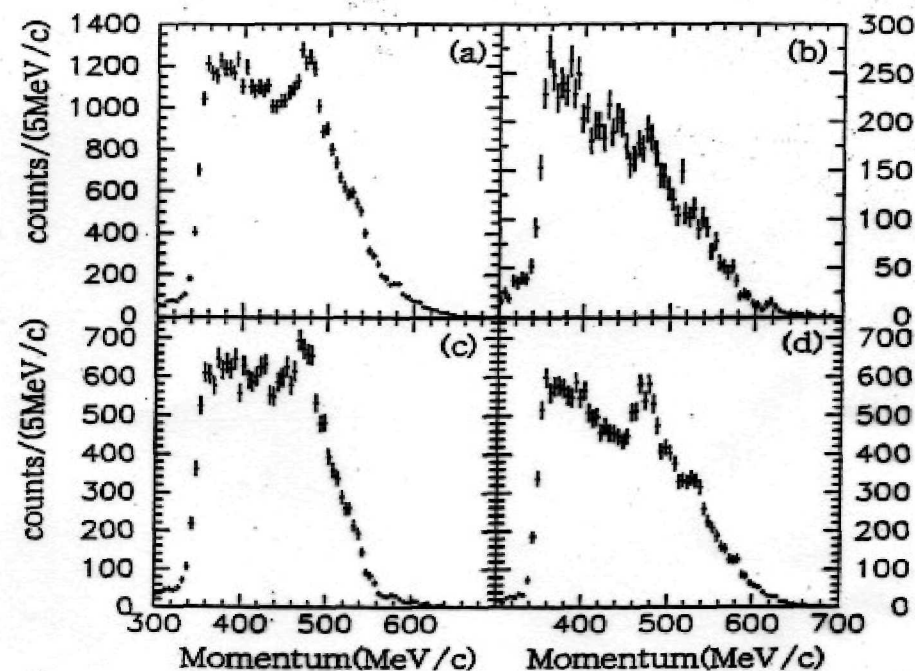


Fig. 5. Proton momentum spectra without energy-loss correction, with cut conditions defined in Fig. 4: (a) with the “ π ”-cut, (b) with the “ p ”-cut, (c) with “fast- π ”-cut, and (d) with “ π ”-cut excluding the fast pions.

The saga continues

AY strike back:

Introduce relativistic corrections (use Klein Gordon equation) (
The chiral theories always did)

some spin orbit corrections

Increase ad hoc the $\bar{K}N$ interaction

B=195 comes out then

At this point the K^- potential in the center of the nucleus has
become 618 MeV!!!

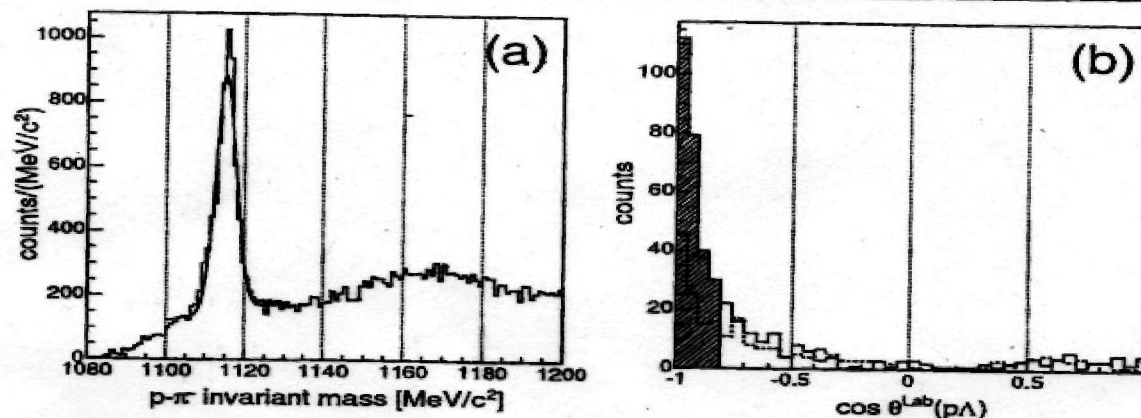
Experimental reconversion: Sato in BadHonnet, PANIC05...
claim the state seen is indeed a K^- bound state.

Discussion of the KEK experiment, Suzuki et al.

- Kaons at rest absorbed: $K^- {}^4\text{He} \rightarrow S p$, They see a peak in the p spectrum around 500 MeV/c.
- Auger emission of the p. Binding energy taken by K^- .
- **Alternative explanation**
 - .. E. O. and H. Toki (2005)
 - .. Many possible conventional mechanisms studied and discarded
- **The one passing all tests**
- $K^- NN \rightarrow \Lambda N$ $p_N = 562 \text{ MeV}/c$
- $K^- NN \rightarrow \Sigma N$ $p_N = 488 \text{ MeV}/c$
The other nucleons left as spectators
- exp. peak seen at $p_p = 475 \text{ MeV}/c$ (some energy loss in thick target)
But what about a peak at $p_p = 562 \text{ MeV}/c$ from $K^- pp \rightarrow \Lambda p$?

FINUDA experiment, M. Agnello et al. PRL 94 (2005)

- K^- absorption at rest from ${}^6\text{Li}, {}^7\text{Li}, {}^{12}\text{C} \dots$
They look for events back to back. Find two peaks in Λp invariant mass: a narrow one at higher energies and a broad one at lower energies. The latter is identified with a bound K^- state.
- Cuts: $p_\Lambda > 300 \text{ MeV}/c$ to eliminate $K^- p \rightarrow \Lambda \pi$
 $|\cos(\theta)| > 0.8$
- **Narrow peak identified as $K^- pp \rightarrow \Lambda p$ removing binding energy**
Broad one at lower energies: "bound K^- state in pp " with $B=115 \text{ MeV}$.
- **Questions:**
where does the binding energy of the kaon go?
Where is the strength if $K^- pp \rightarrow \Lambda p$ exciting the nucleus (largest part)?



(a) Invariant-mass distribution of a proton and a π^- for all the events in which these two particles are observed, fitted with a Gaussian together with a linear background in the invariant-mass range of 1100–1130 MeV/c^2 . (b) Opening angle distribution of a Λ and a proton: solid line, ${}^6\text{Li}$, ${}^7\text{Li}$, and ${}^{12}\text{C}$; dashed line, ${}^{27}\text{Al}$ and ${}^{51}\text{V}$. The shaded area ($\cos\theta^{\text{Lab}} < -0.8$) is selected for the back event.

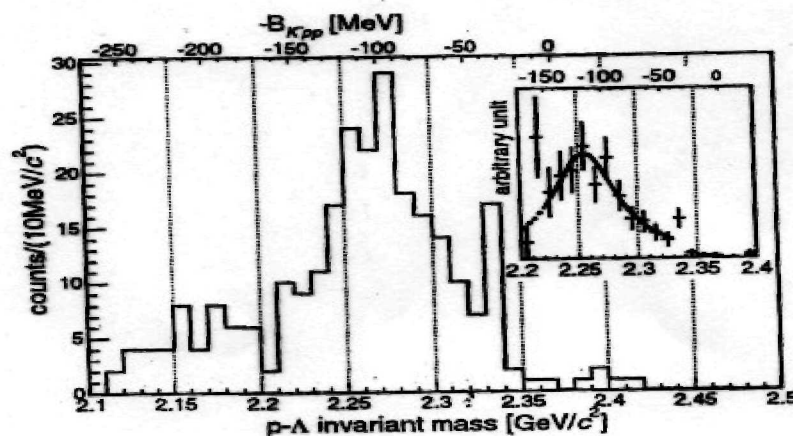
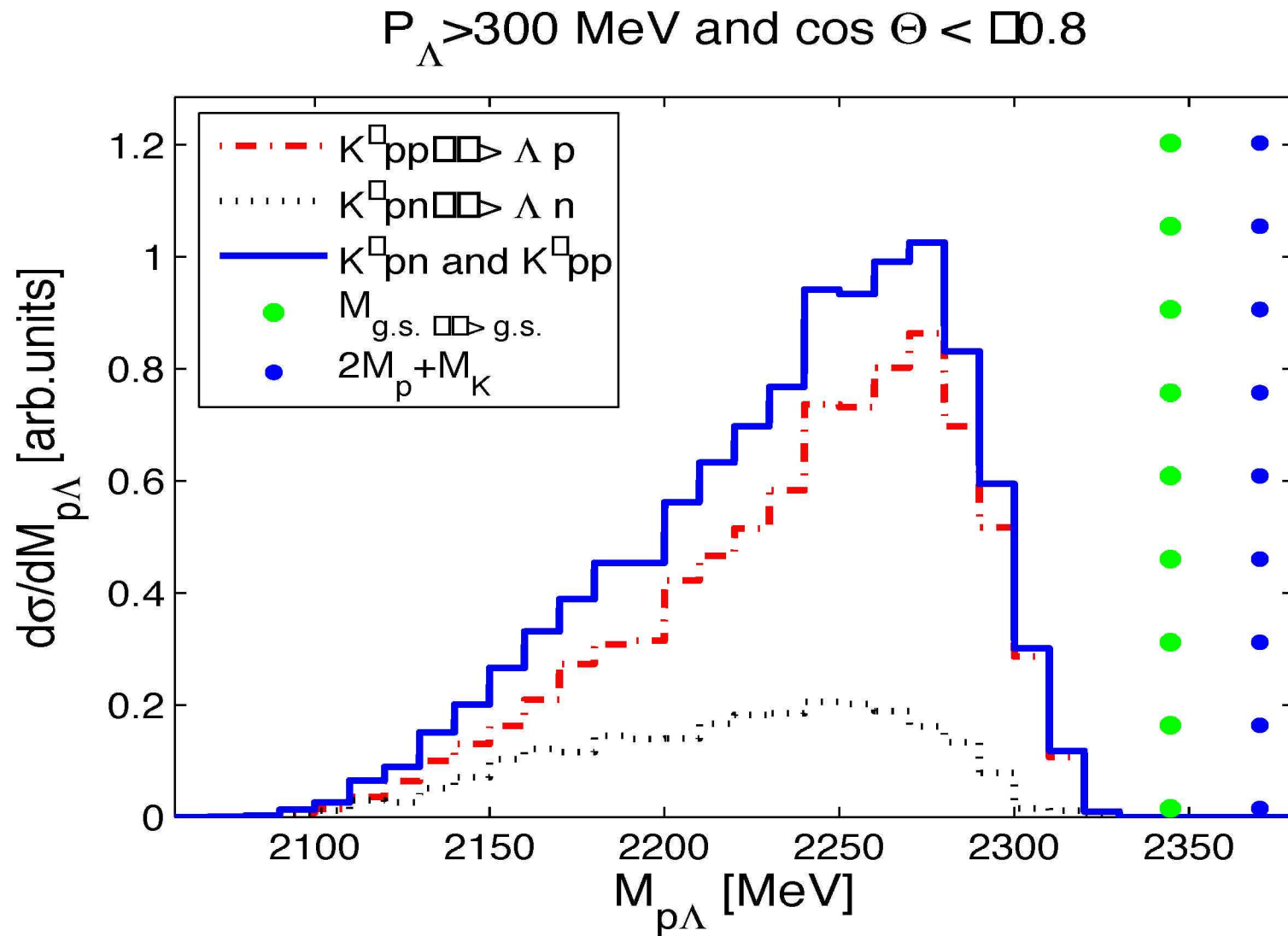


FIG. 3. Invariant mass of a Λ and a proton in back-to-back correlation ($\cos\theta^{\text{Lab}} < -0.8$) from light targets before the acceptance correction. The inset shows the result after the acceptance correction for the events which have two protons with well-defined good tracks. Only the bins between 2.22 and

Our description of the peaks

V. K. Magas, A. Ramos, E. O and H. Toki, (2006)

- We run a computer simulation code for K^- absorption in nuclei by pp and pn pairs:
- $|\Psi(r)|^2$ distribution for K^- peaked around surface of nucleus
- K^- absorbed by pp or pn, with momenta randomly chosen from local Fermi sea.
- energy and momentum conservation including nuclear potential
- Λp , Λn emitted according to phase space
- p, n have further collisions
 - $pN \rightarrow p' N$ $np \rightarrow pn$ (fast n to fast p)
 - done according to $\sigma\rho$ probability per unit length and experimental angular distributions ($\sigma_\Lambda = \frac{2}{3}\sigma_N$)
- Λp invariant mass reconstructed from final events.



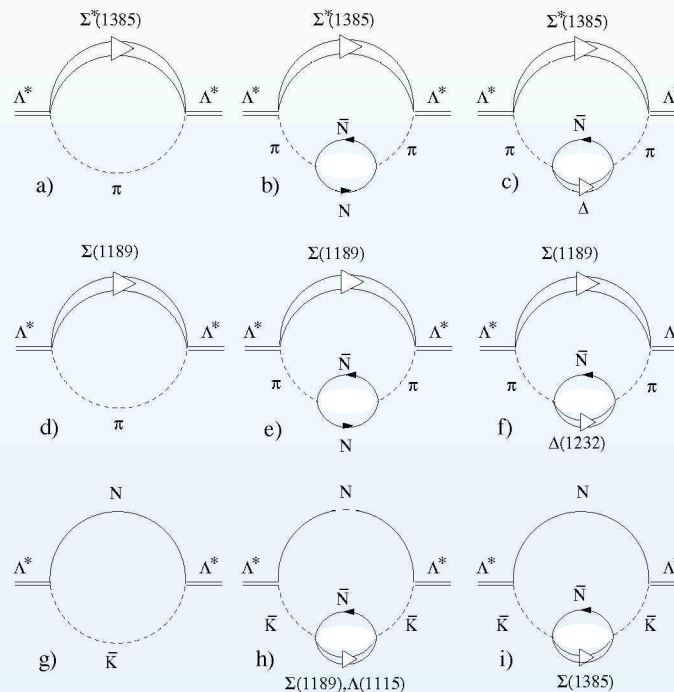
^{12}C Results imposing the experimental angle cut for back to back events, $\cos \Theta_{\vec{p}_{\Lambda}\vec{p}_p} <$

-0.8 , and up to three collisions.

$\Lambda(1520)$ in the nuclear medium

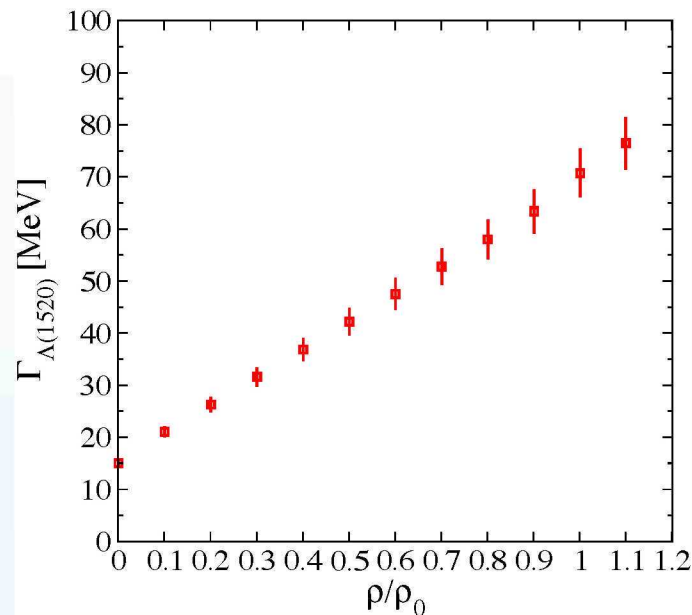
The coupling of the $\Lambda(1405)$ to $\pi\Sigma(1385)$ is very large but decay into this channel practically suppressed because of lack of phase space.

In nuclei a π can excite ph . Plenty of phase space. Large width.

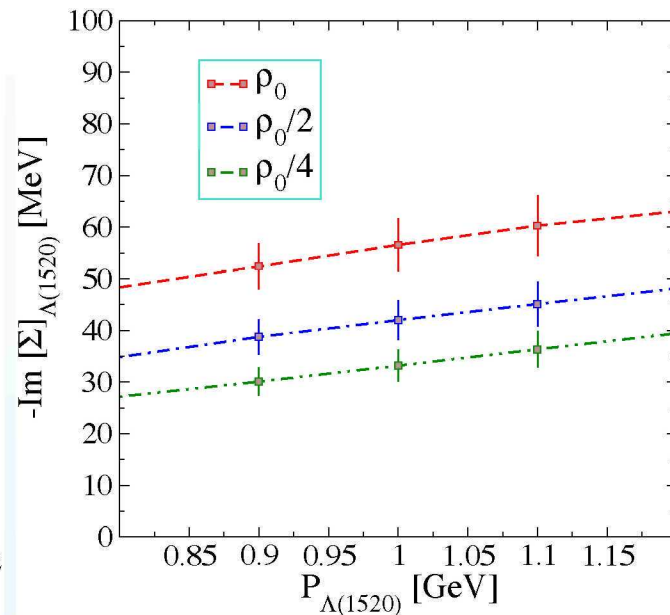


M.Kaskulov and E. O. , Phys Rev C (2006)

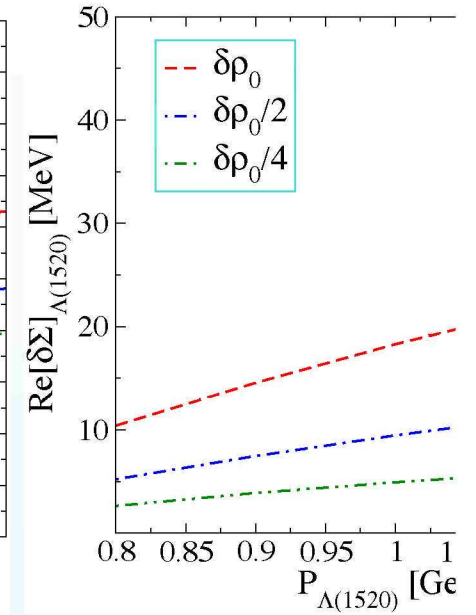
Results for $\Lambda(1520)$ in the nuclear medium



a)



b)



c)

These drastic changes could be observed experimentally suggestion made in **Kaskulov, Roca, E. O, Eur. Phys. J. A (2206)** by looking at the A dependence of the production cross section in

- proton induced $\Lambda(1520)$ production
- photon induced $\Lambda(1520)$ production (in progress at Spring8/Osaka)

Conclusions

- Chiral dynamics is a powerful and ideal tool to face hadron interactions at intermediate energies in free space and in nuclei.
- It has shown as a side effect that some popular resonances qualify as dynamically generated or quasibound states of hadrons.
- It has predicted the existence on new resonances. Evidence for the second $\Lambda(1405)$ recently found.
- Chiral dynamics is important when dealing with hadrons in a nucleus.
- It makes prediction for kaon interaction with nuclei in good agreement with data of Kaon atoms. Predicts deeply bound kaon states but with a large width.
- striking medium effects in some resonances, like the $\Lambda(1520)$

Deeply bound kaon states

- The K^- optical potential on which predictions of narrow deeply bound K^- states was done is overly exaggerated and incomplete in the decay channels.
- The KEK and FINUDA experiment do not have any support for the interpretation of the data as bound kaons except the "theoretical predictions" of the mentioned work.
- We have shown that all the peaks can be interpreted in terms of K^- absorption on pairs of nucleons,
 - in KEK with remnant nucleus as spectator
 - in FINUDA, first peak with remnant nucleus as spectator
 - second peak with nuclear excitation to the continuum
- These mechanisms passed all tests for which there were available data.

Summary of DHD06 Workshop, Kyoto Feb 2006

- Akaishi strikes back, confusion of cut off in field theory and range of interaction. No selfconsistency yet, still $10\rho_0$ density.
- Yamazaki strikes back, makes wrong assumption on final state in $K^- \ ^4\text{He}$ absorption going to $p\Sigma \ nn$ instead of $p\Sigma \ d$ (small recoil energy of d , 10 MeV for 200 MeV/c of Fermi motion). Misses the experimental fact of the narrow signal in FINUDA for K^- absorption without extra final state interaction. Disguised offer of compromise, peaks partly from K^- absorption and partly from production of tribaryon. Compromise rejected: too much coincidence that the peaks appear in all nuclei at the K^- absorption kinematics.
- No help from anybody else of the Japanese community.
- No claims in the experimental talks about deeply bound kaon atoms. Back to tribaryon claim.
- Iwasaki pledge "please understand all this is still preliminary, we are working to understand what happens"
- The paper of 2003 with claims for deeply bound K from the K^- (*at rest*) absorption in $\ ^4\text{He}$, (K^-, n) has been withdrawn.

Summary of DHD06 Workshop, Kyoto Feb 2006

- Y. Yamagata presents calculations of (K^-, p) in flight and concludes that even if there are deeply bound kaon states the signal would be too weak to be seen in present experiments.
- S. Okada (Hayano exp.) presents results for $3d \rightarrow 2p$ X-rays of Kaonic Helium. 2p shift: Old experiments 40 eV, chiral unitary model 0.2 eV, Akaishi potential 11 eV. New experiment compatible with zero with 3-4 eV precision.