



The Abdus Salam  
International Centre for Theoretical Physics



SMR.1824 - 19

**13th International Workshop on  
Computational Physics and Materials Science:  
Total Energy and Force Methods**

**11 - 13 January 2007**

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**Ab-initio theory of alloys:  
New possibilities for materials design**

**Igor A. ABRIKOSOV**  
Linköping University  
Materials Science  
Department of Physics & Measurement Technology  
S-58183 Linköping  
SWEDEN

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These are preliminary lecture notes, intended only for distribution to participants

*AB INITIO THEORY OF ALLOYS:  
NEW POSSIBILITIES FOR MATERIALS DESIGN*



**Igor A. Abrikosov**

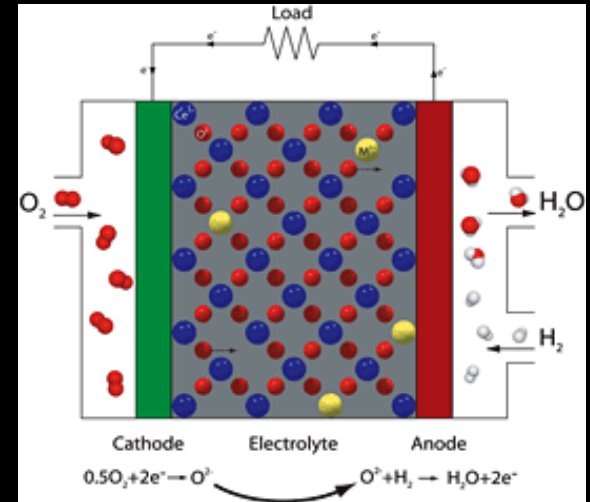
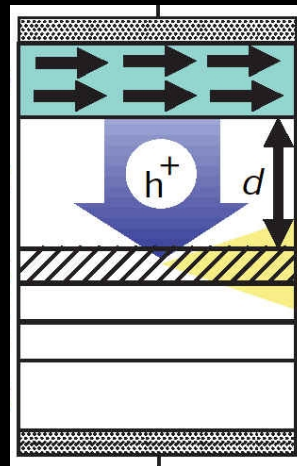
**Theoretical Physics,**

**Department of Physics, Chemistry and  
Biology, Linköping University, Sweden**

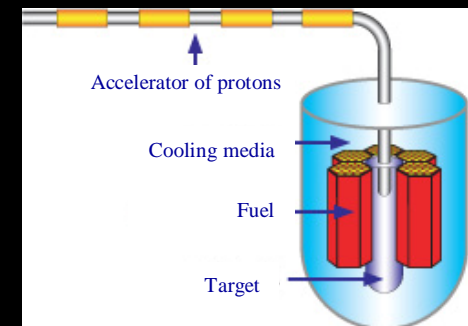
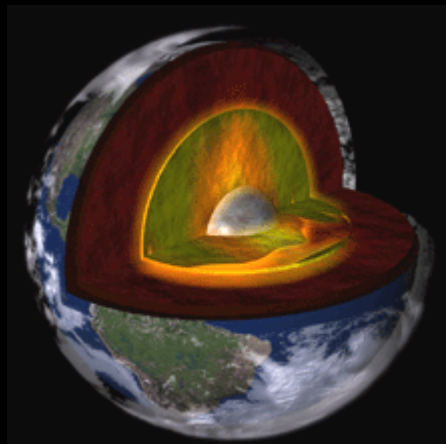
# *COLLABORATION :*



- B. Alling and S. I. Simak, LiU, Sweden
- L. Vitos, D. Andersson, and B. Johansson, KTH, Sweden
- P. Olsson, CAE, France, and J. Wallenius, KTH, Sweden
- N. Skorodumova and O. Peil, UU, Sweden
- A. Karimi, EPFL, Switzerland



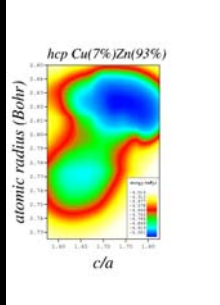
# Alloys



# *CONTENTS :*



- Recent developments in the alloy theory
- Phase stability: a role of the electronic structure  
Mixing and decomposition thermodynamics of nanocomposite hard coating (TiAl)N alloys.  
Anomalous stability of low Cr steels.
- Optimization of the ionic conductivity in doped ceria
- Conclusions



# *INALLOY toolkit*

- Coherent potential approximation:
  - KKR-ASA basis set
  - Exact Muffin-Tin Orbitals (EMTO) basis set
  - Screened Impurity Model for charge fluctuations
  - Model treatment of the local lattice relaxations
- Locally self-consistent Green's function method
- Supercell technique combined with conventional band structure methods using Special Quasirandom Structures
- Multiscale modeling based on Hamiltonians with parameters determined *ab initio*

# *The EMTO method*

Potential:

overlapping MT potential

Kink cancellation equation:

$$[D(\varepsilon) - S(\varepsilon, \mathbf{k})]g(\varepsilon, \mathbf{k}) = 1$$

$D(\varepsilon)$  potential

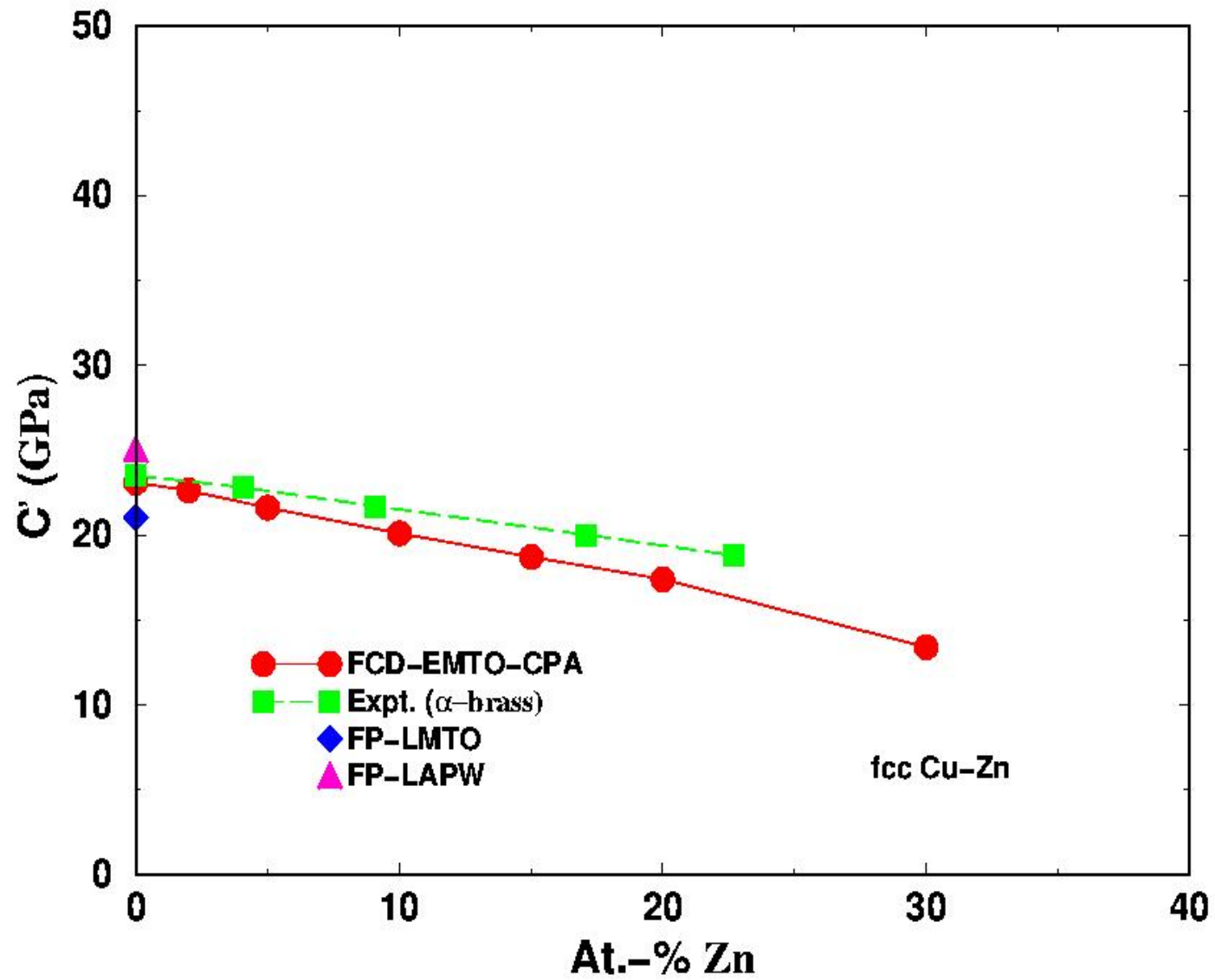
$S(\varepsilon, \mathbf{k})$  slope matrix

Density:

$$n(\mathbf{r}) \sim \langle Z(\varepsilon, \mathbf{r}) g(\varepsilon, \mathbf{k}) Z(\varepsilon, \mathbf{r}) \rangle_{\varepsilon, \mathbf{k}}$$

- **Localized MT orbitals (screened KKR)**
- **Smooth energy dependence of  $S(\varepsilon, \mathbf{k})$**
- **Optimized overlapping MT potential**
- **Proper normalization (CC term)**
- **Accurate Full Charge Density**
- **Accurate kinetic energy**

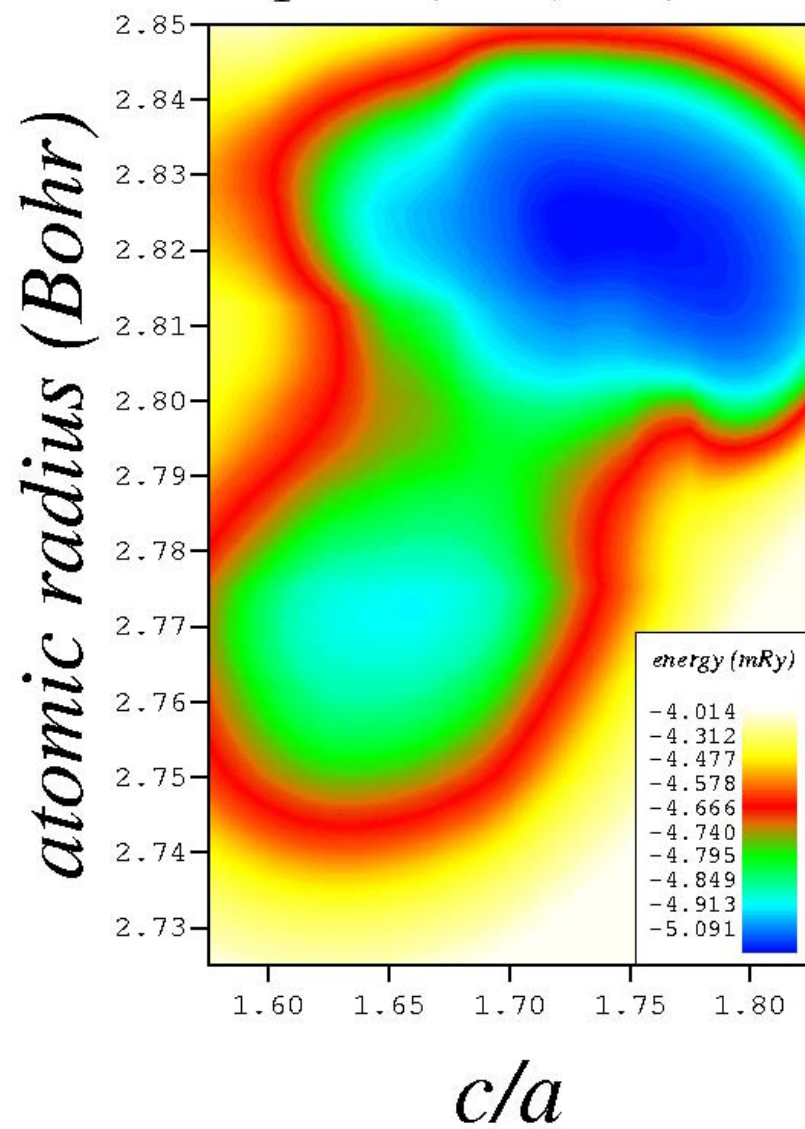
## EMTO-FCD-CPA

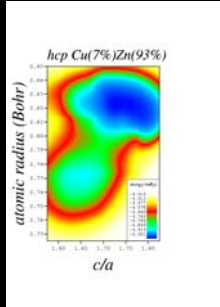


L. Vitos, I. A. Abrikosov, and B. Johansson, Phys. Rev. Lett. **87**, 156401 (2001)



*hcp Cu(7%)Zn(93%)*



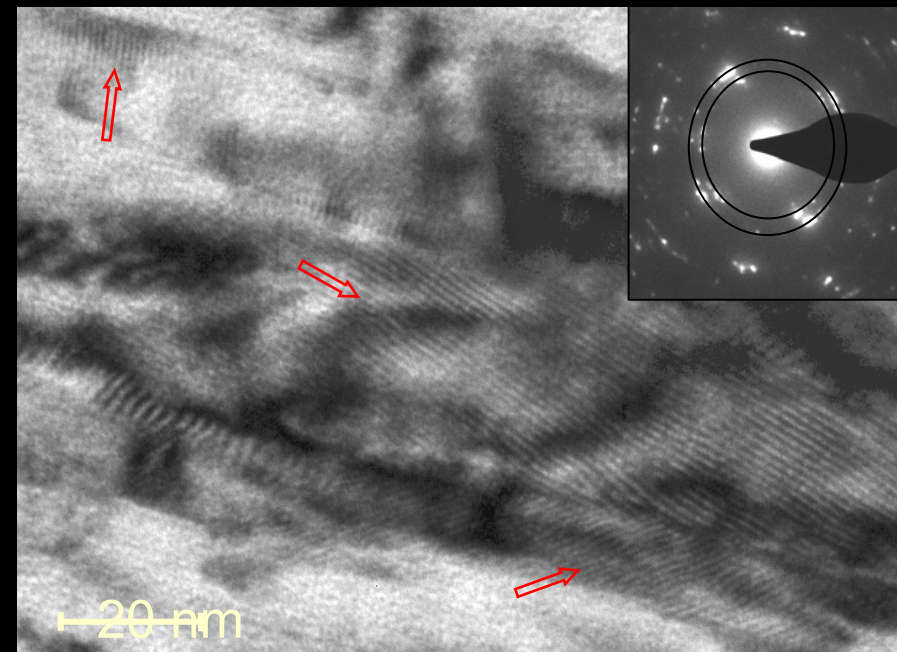


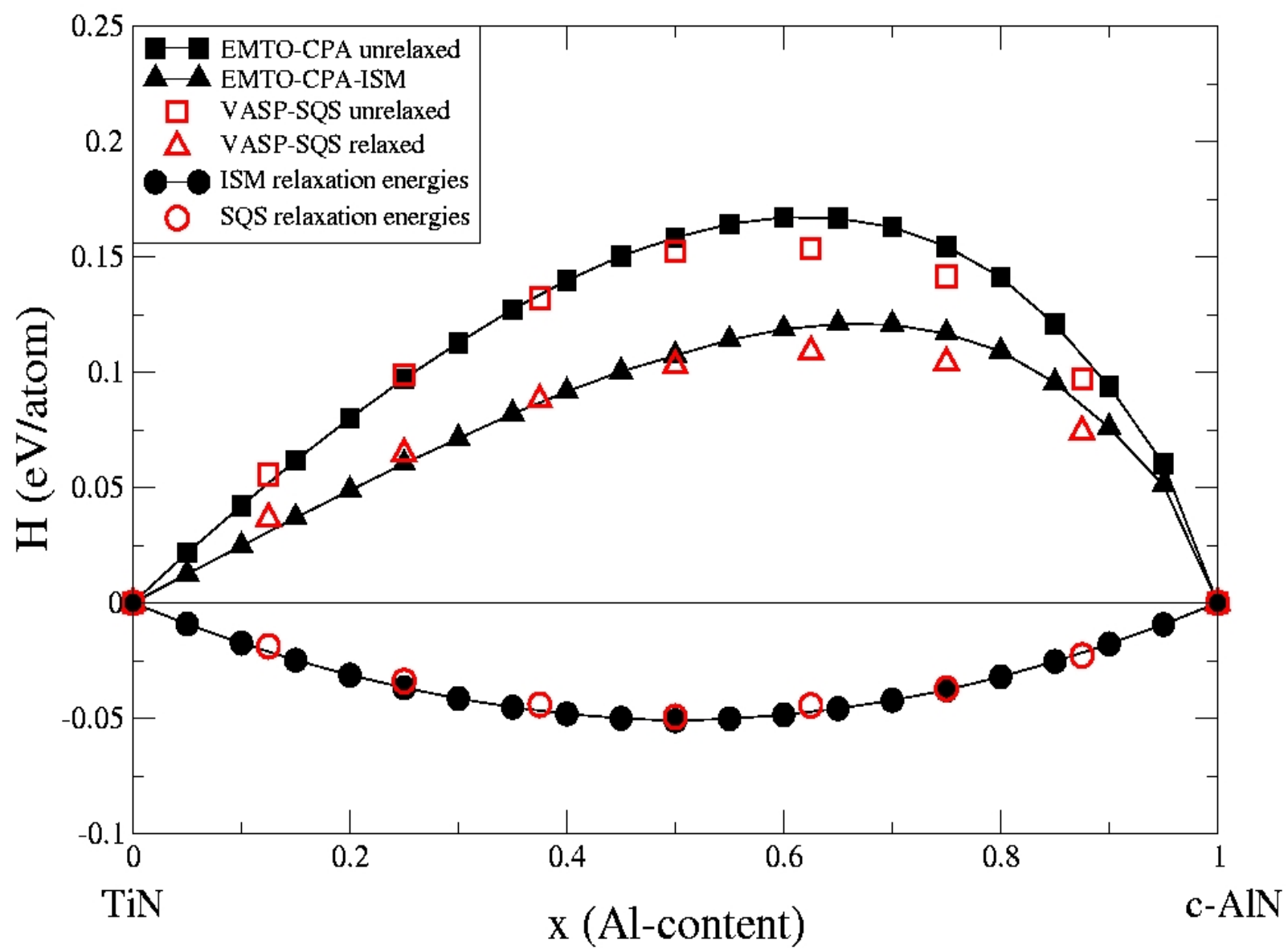
# *INALLOY toolkit*

- Coherent potential approximation:
  - KKR-ASA basis set
  - Exact Muffin-Tin Orbitals (EMTO) basis set
  - Screened Impurity Model for charge fluctuations
  - Model treatment of the local lattice relaxations
- Locally self-consistent Green's function method, (O(N) method for metallic alloys, Phys. Rev. Lett. **76**, 4203 (1996)).
- Supercell technique combined with conventional band structure methods using Special Quasirandom Structures (A. Zunger *et al.*, Phys. Rev. Lett. **65**, 353 (1990)).
- Multiscale modeling based on Hamiltonians with parameters determined *ab initio*

# *Nanocomposite hard coating (Ti-Al)N alloys*

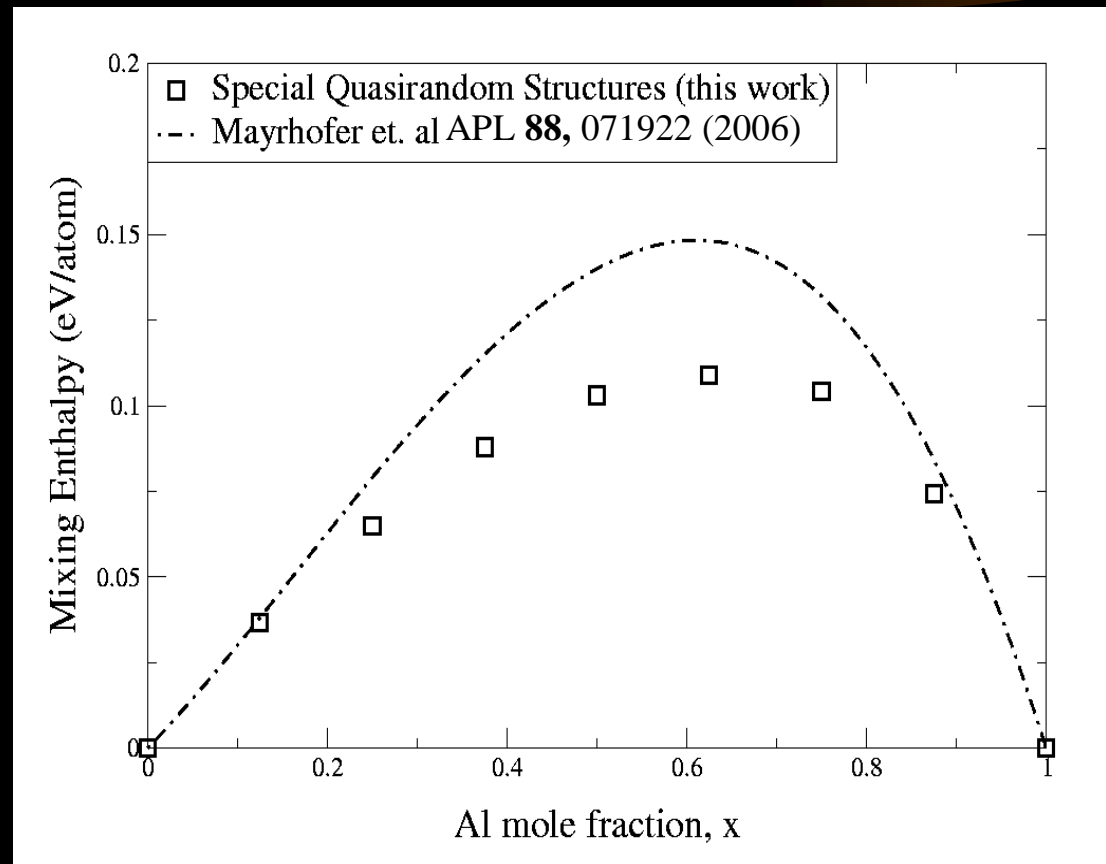
- The new universal high-performance coating (drilling, milling, etc.)
- Increasing Al content leads to very high heat resistance, dry high-speed machining, and increased oxidation resistance
- Spinodal decomposition

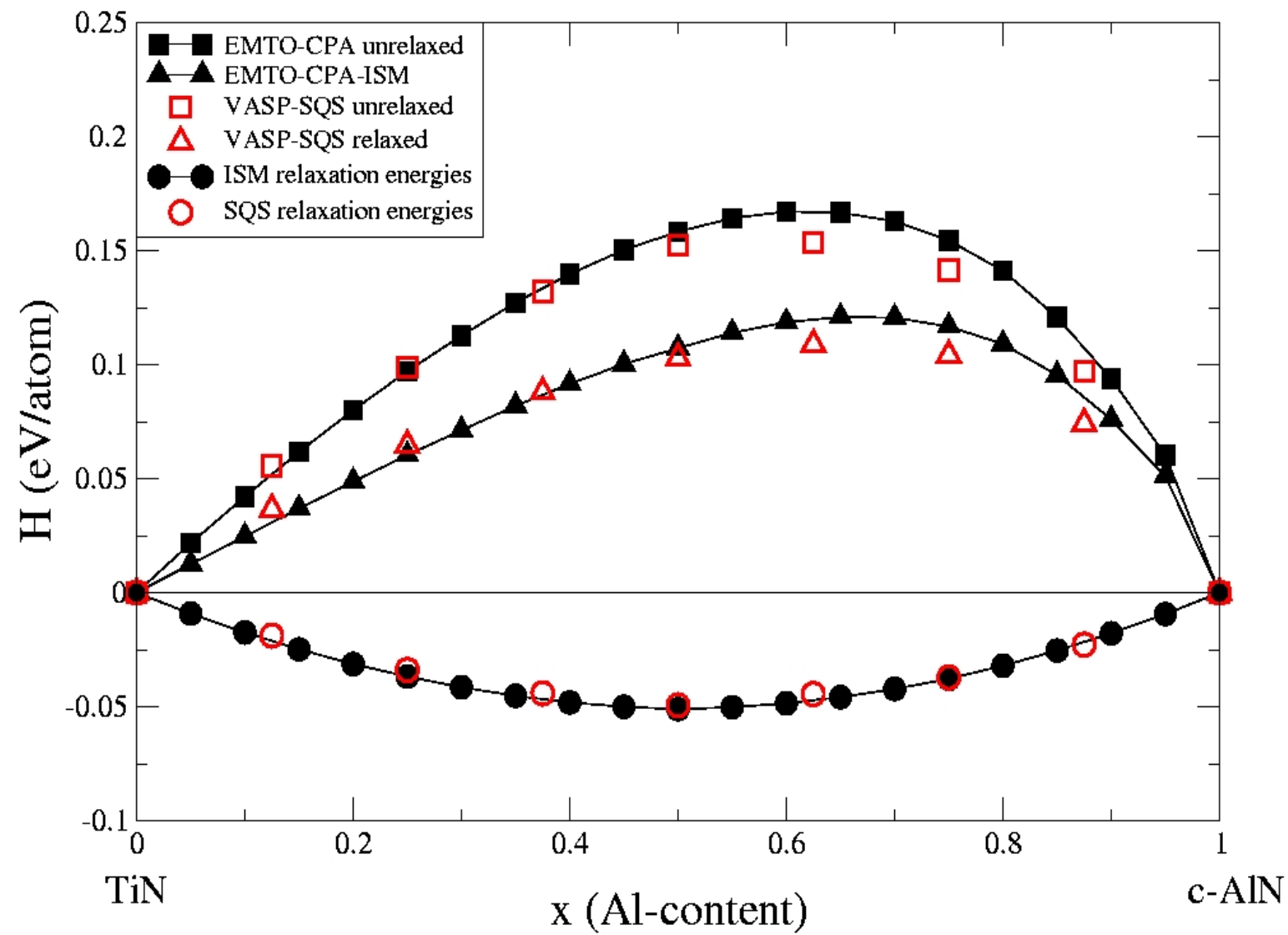


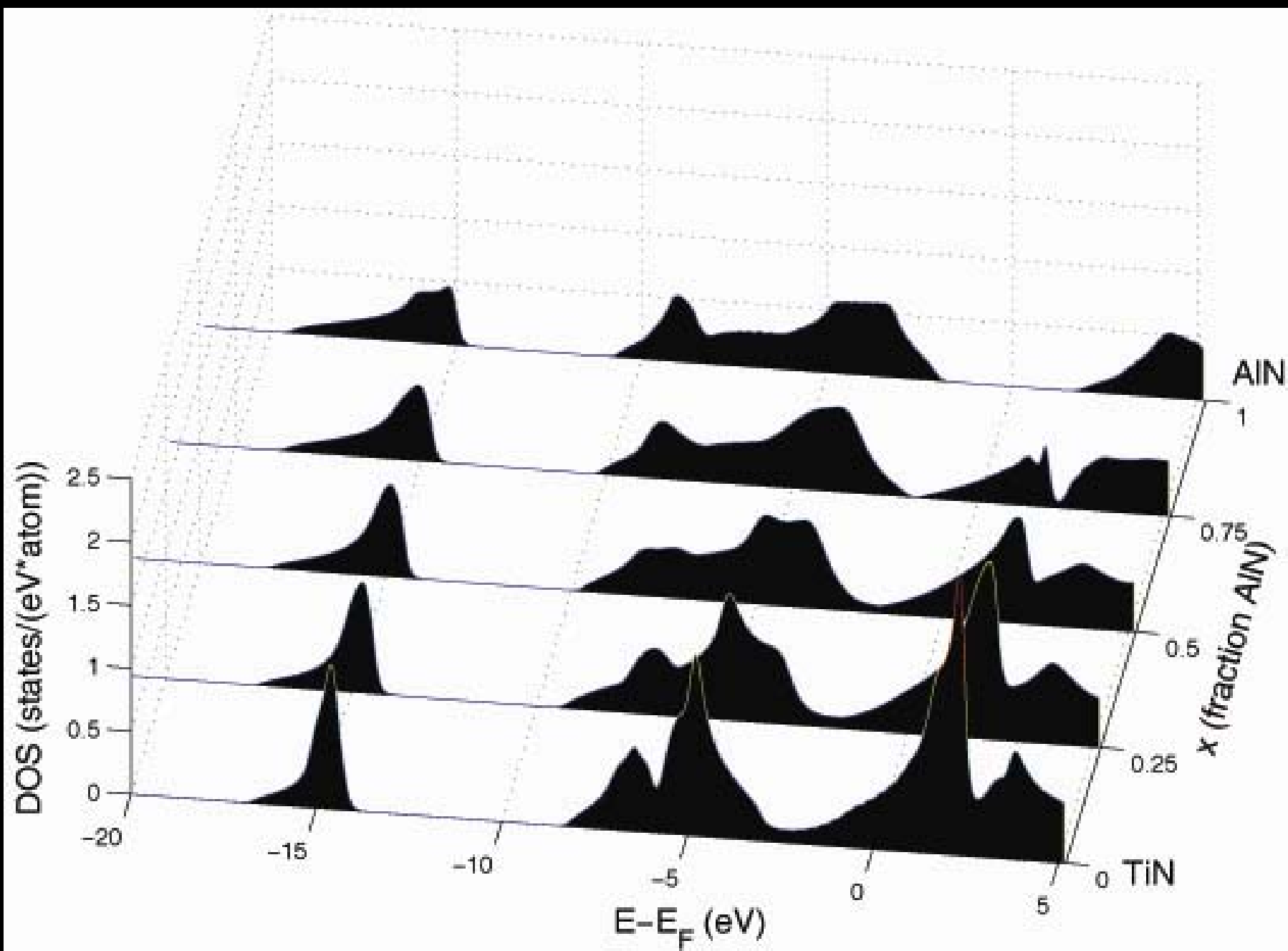


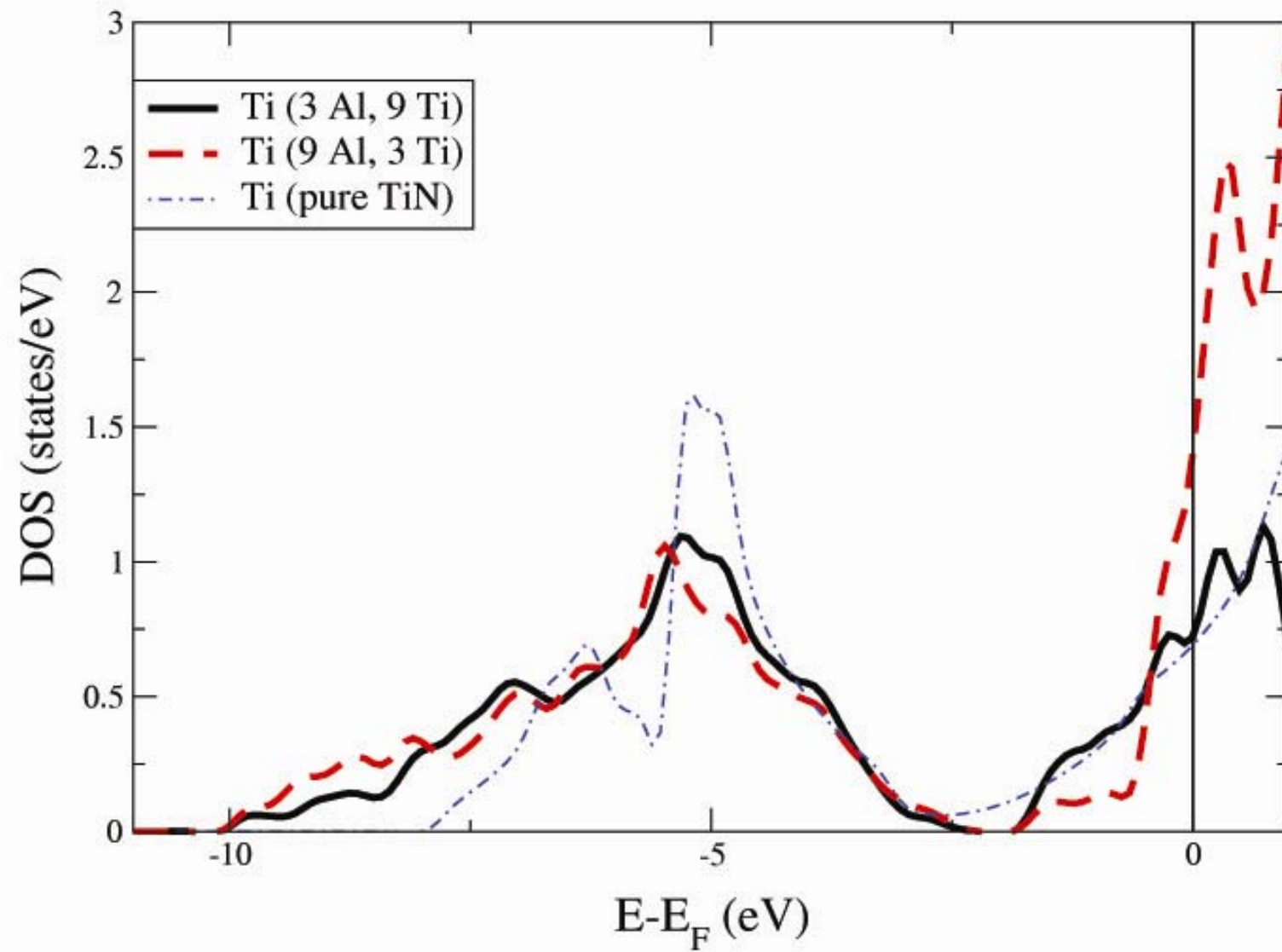
B. Alling, A. V. Ruban, A. Karimi, O. E. Peil, L. Hultman, and I. A. Abrikosov, Phys. Rev. B (in press).

## *Caution: the use of the supercell technique*

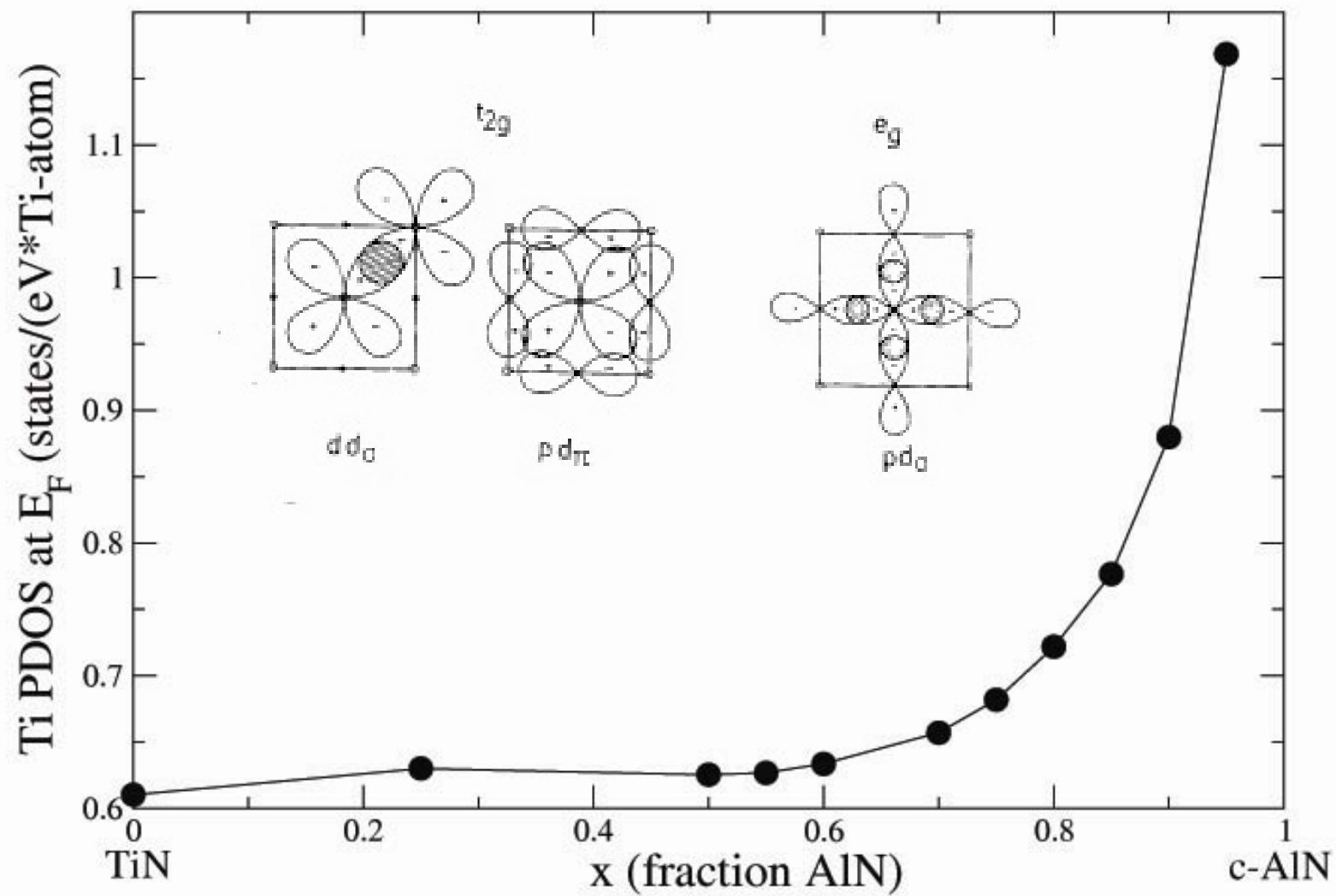


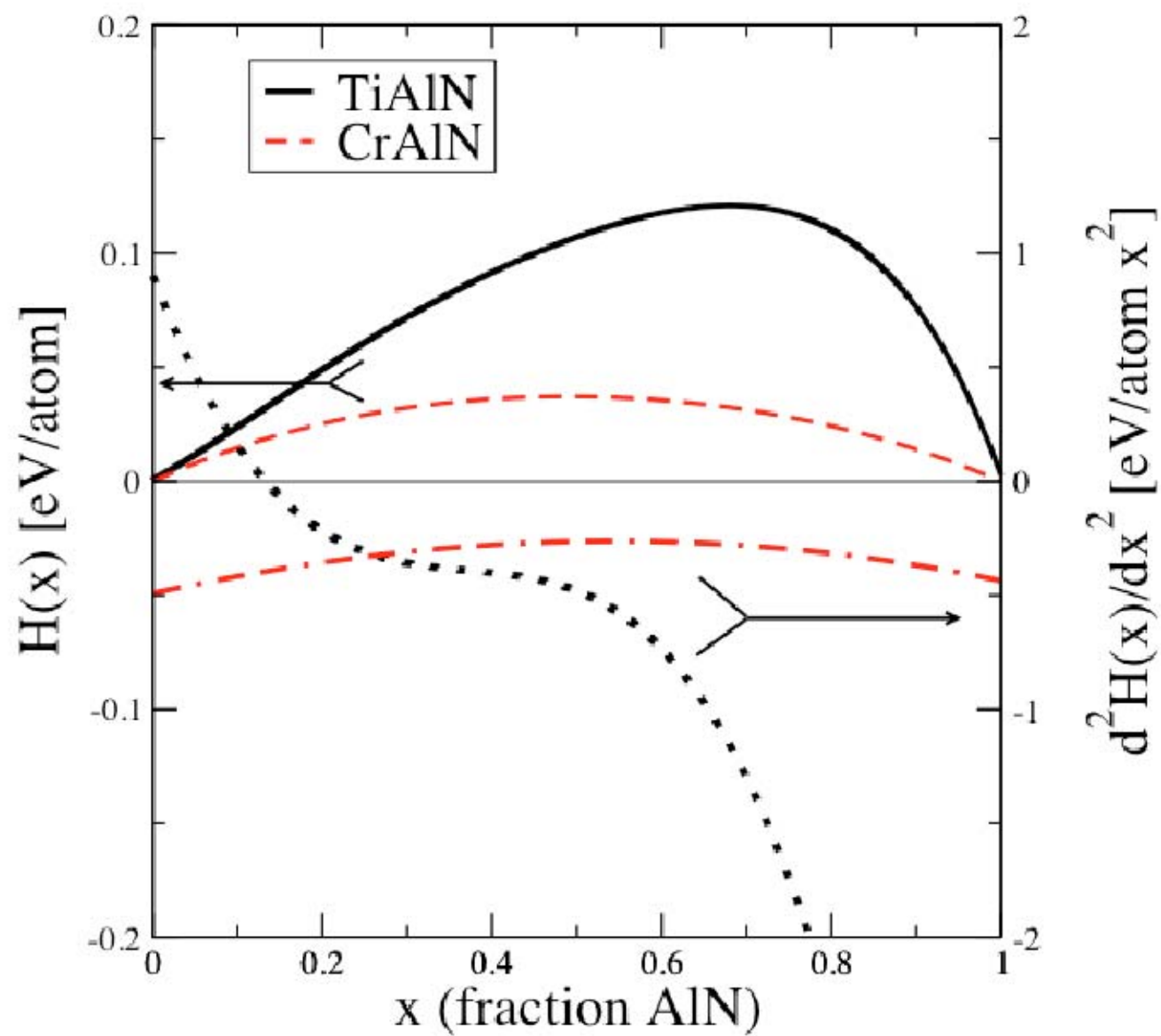






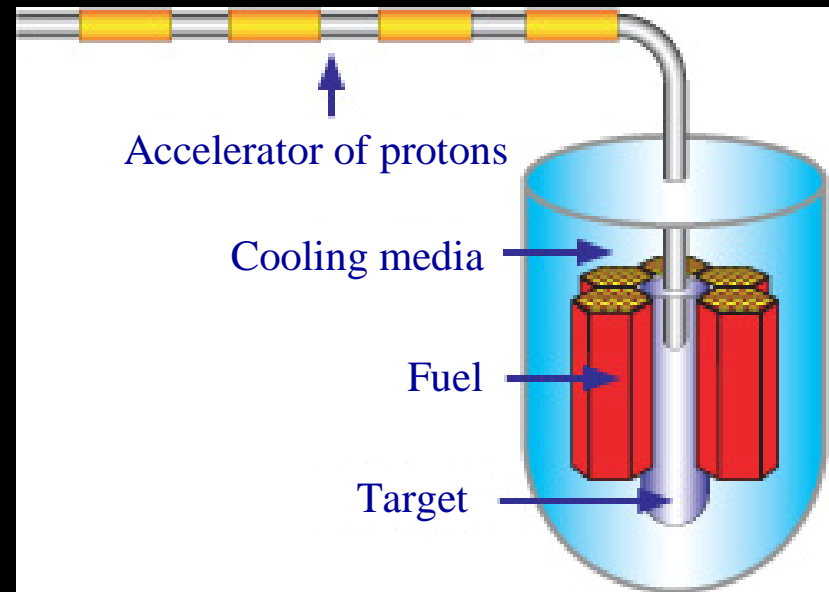




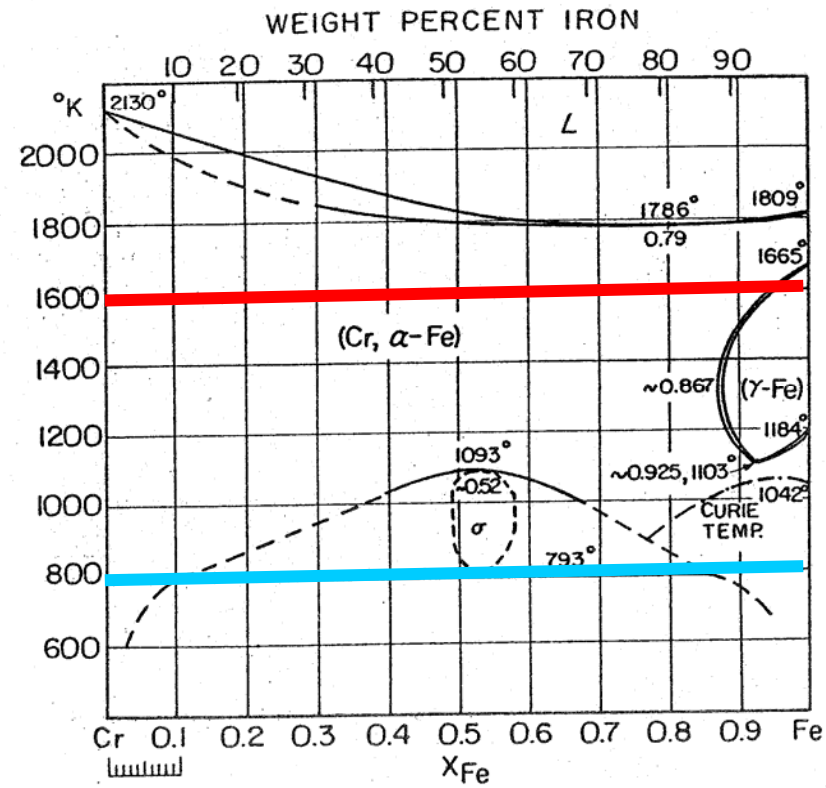


# *Fe-Cr alloys*

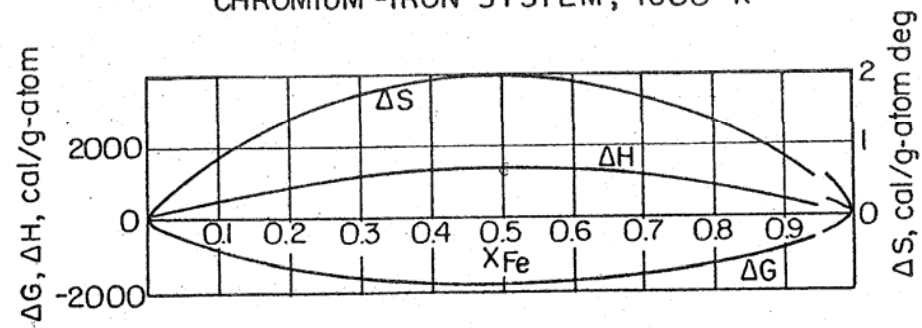
- Are the base for many important industrial steels
- Used as cladding material in fast neutron reactors
- Low Cr steels, up to 10 % Cr, show:
  - anomalous stability
  - resistance to neutron radiation induced swelling
  - corrosion resistance
  - increased ductile to brittle transition temperature

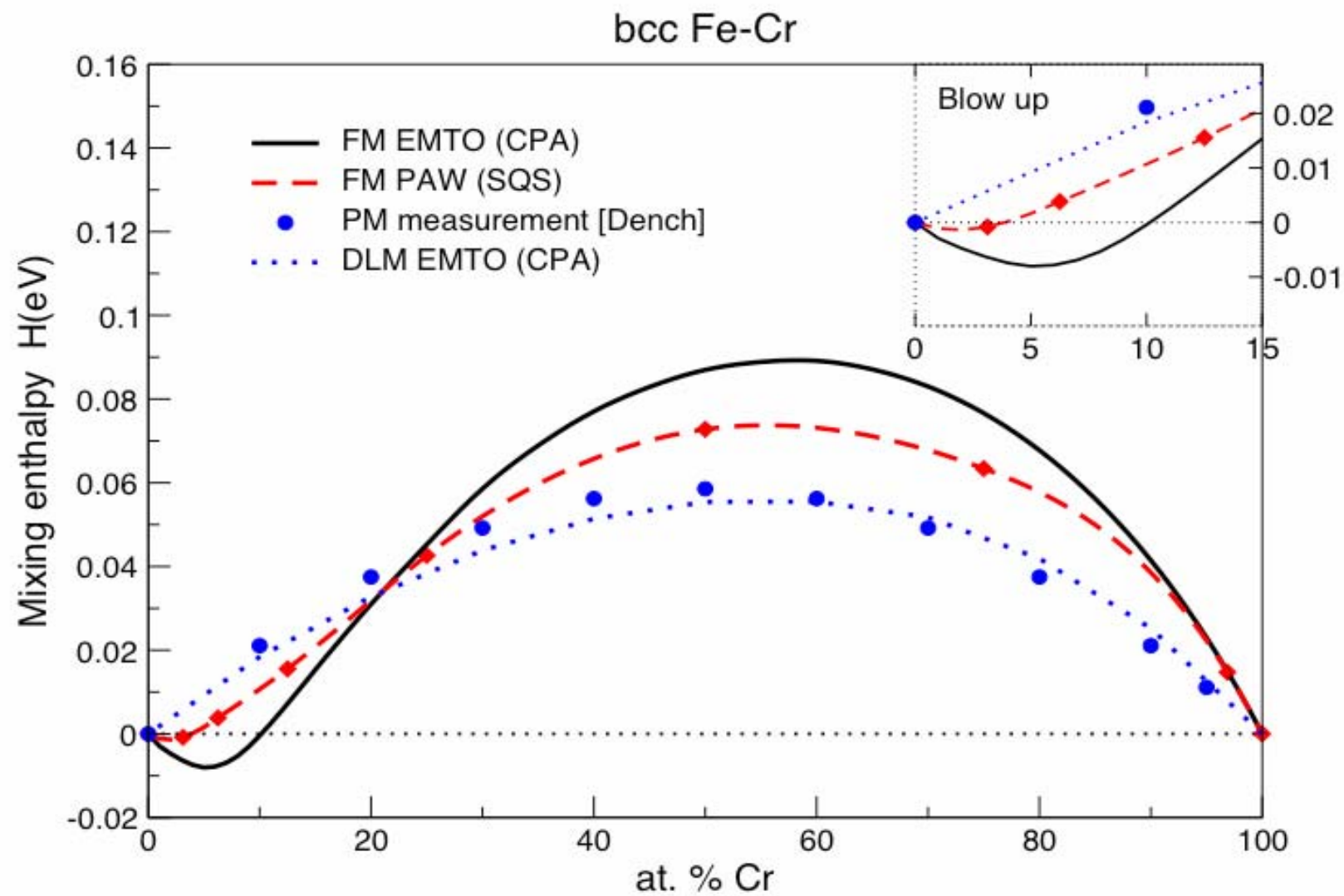


# Cr-Fe

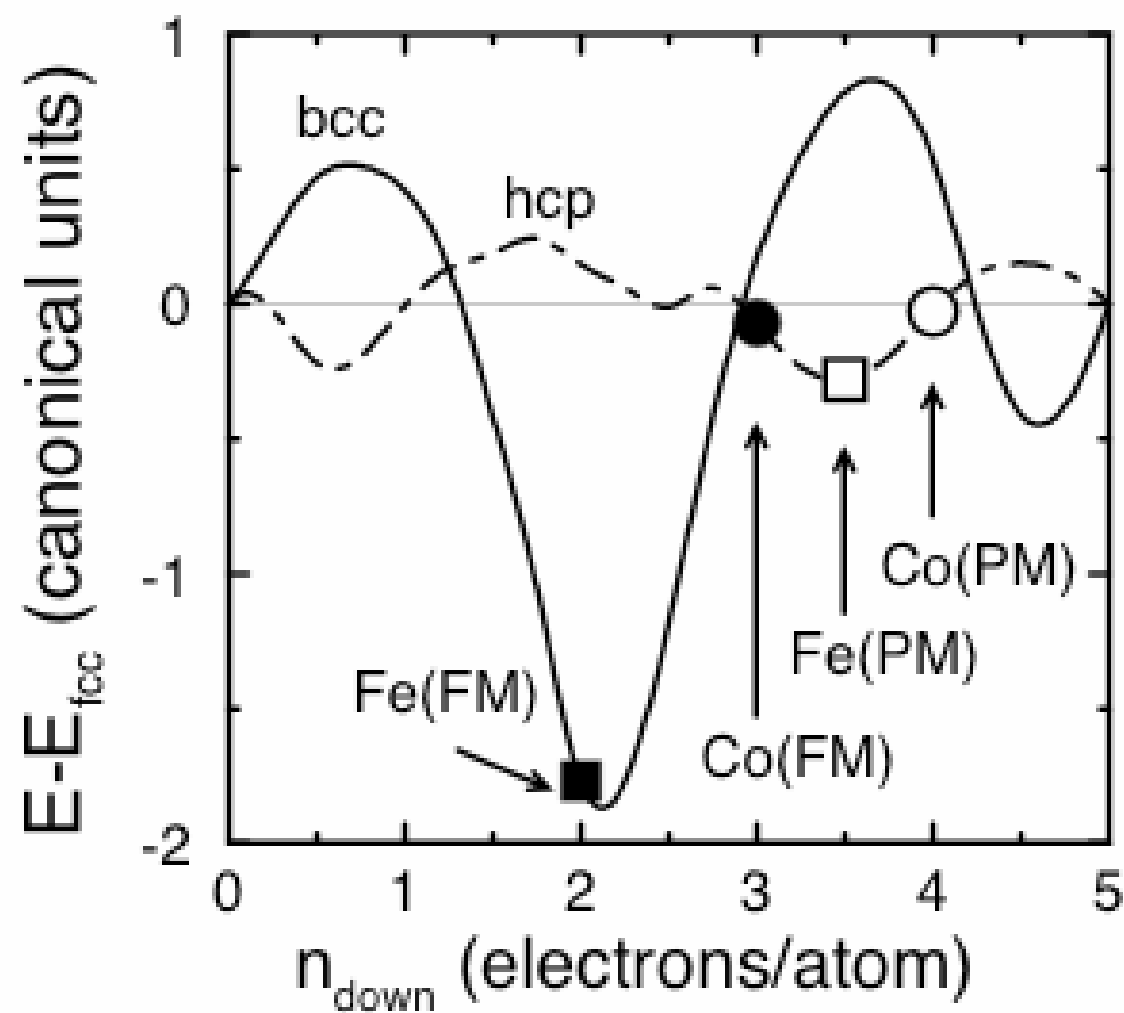


CHROMIUM-IRON SYSTEM, 1600 °K





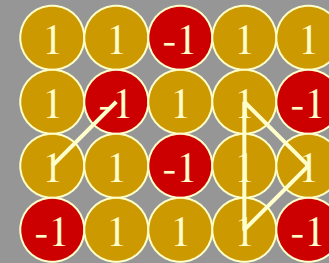
P. Olsson, I. A. Abrikosov, and J. Wallenius, Phys. Rev. B **73**, 104416 (2006)



# *Ising Hamiltonian and effective cluster interactions*

$$\vec{\sigma}_s = \{\sigma_i\} \quad \sigma_i = \begin{cases} 1 & \text{if site } i \text{ is occupied by atom } A \\ -1 & \text{otherwise} \end{cases}$$

$$\langle \sigma_i \sigma_j \rangle^s, \quad \langle \sigma_i \sigma_j \sigma_k \rangle^s, \dots$$



$$\underline{E_{tot}} = \underline{V^{(0)}} + \underline{V^{(1)}} \langle \sigma \rangle +$$

$$\sum_s \underline{V^{(2,s)}} \langle \sigma_i \sigma_j \rangle + \sum_s \underline{V^{(3,s)}} \langle \sigma_i \sigma_j \sigma_k \rangle + \dots$$

# *Calculations of effective interatomic potentials*

## The generalized perturbation method

1. Calculate electronic structure of a random alloy (for example, use the CPA):

$$\underline{g}, t^{A(B)}$$

$$2. E_{one} = E_{one}(c) + \frac{1}{2} \sum_{RR'} V_{RR'} \langle \sigma_i \sigma_j \rangle^{(RR')} \dots$$

-determine a perturbation of the band energy due to small variations of the correlation functions

where the effective interatomic interactions are given by an analytical formula:

$$\underline{V_{RR'} = -\frac{1}{\pi} \int dE \left\{ t_R^A \gamma_{RR'} t_{R'}^B \gamma_{R'R} t_R^A \right\}}$$

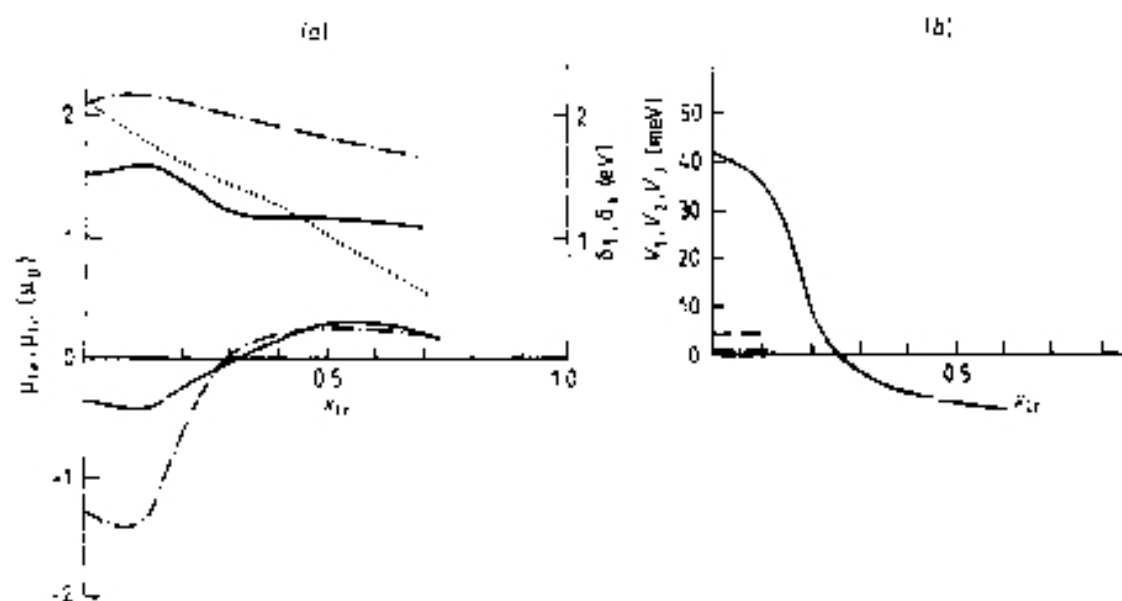


## Chemical sro effects in ferromagnetic Fe alloys in relation to electronic band structure

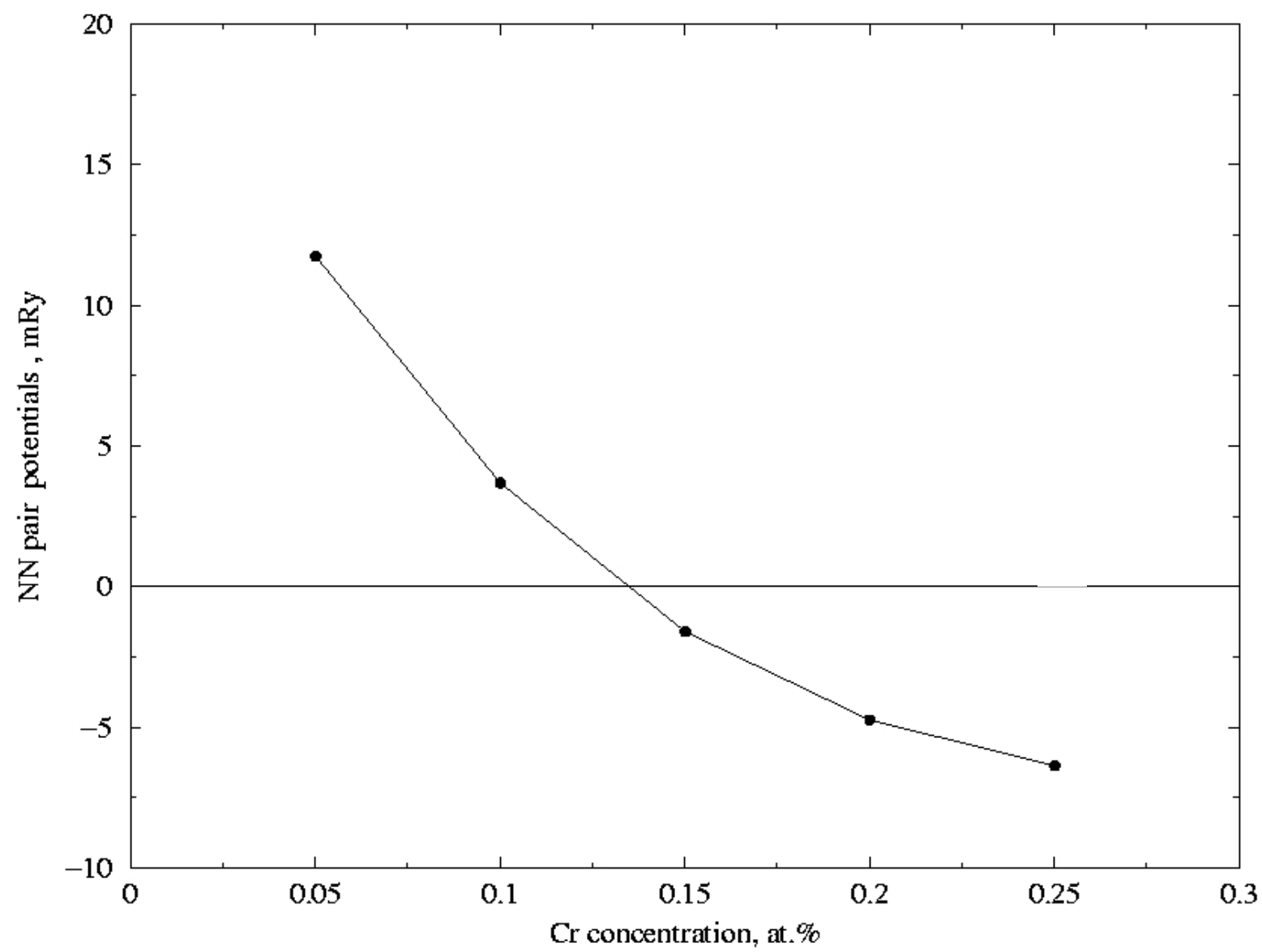
M Héron

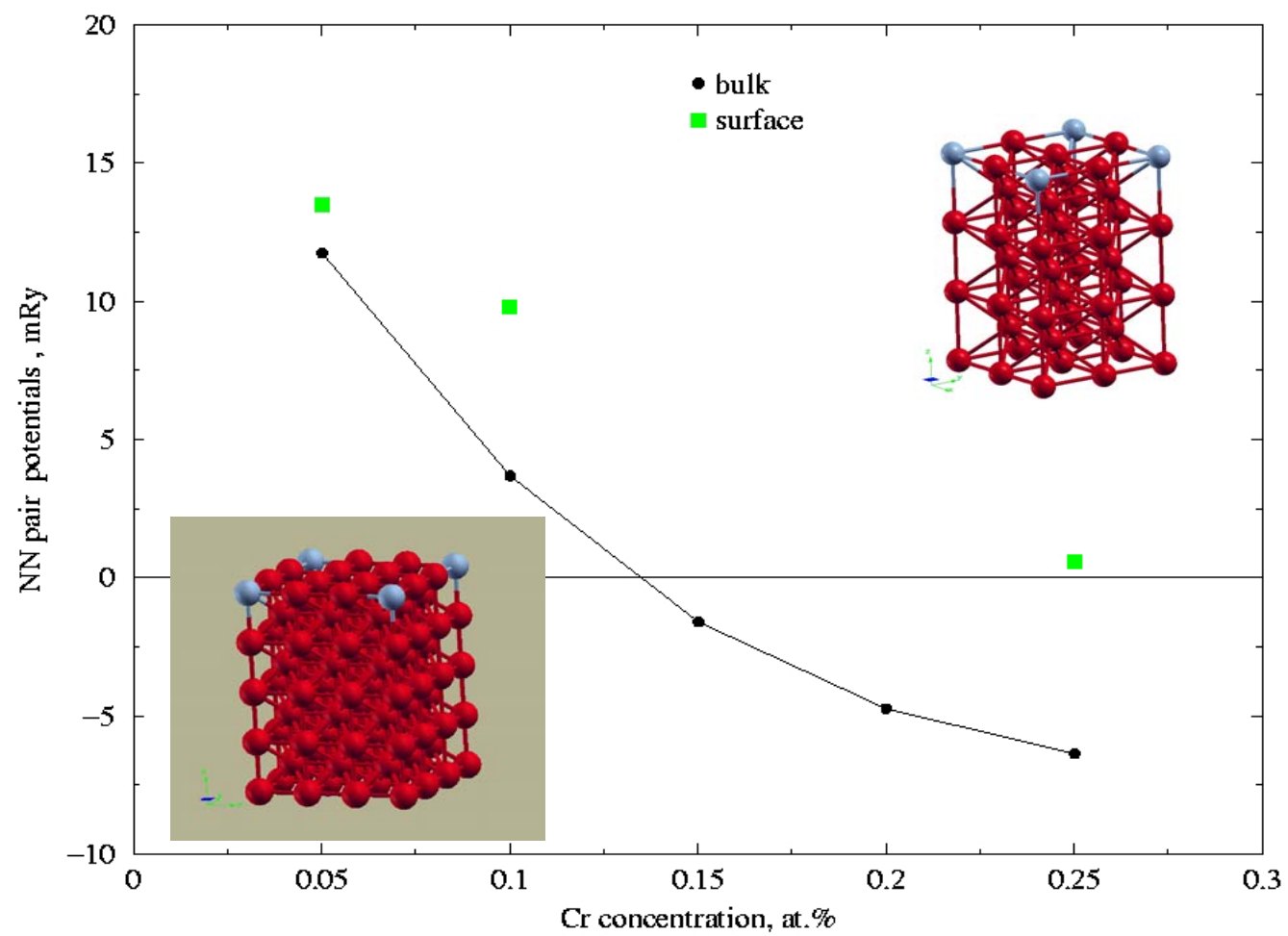
Laboratoire Léon Brillouin, CEN Saclay, 91191 Gif-sur Yvette Cédex, France

Received 3 May 1983



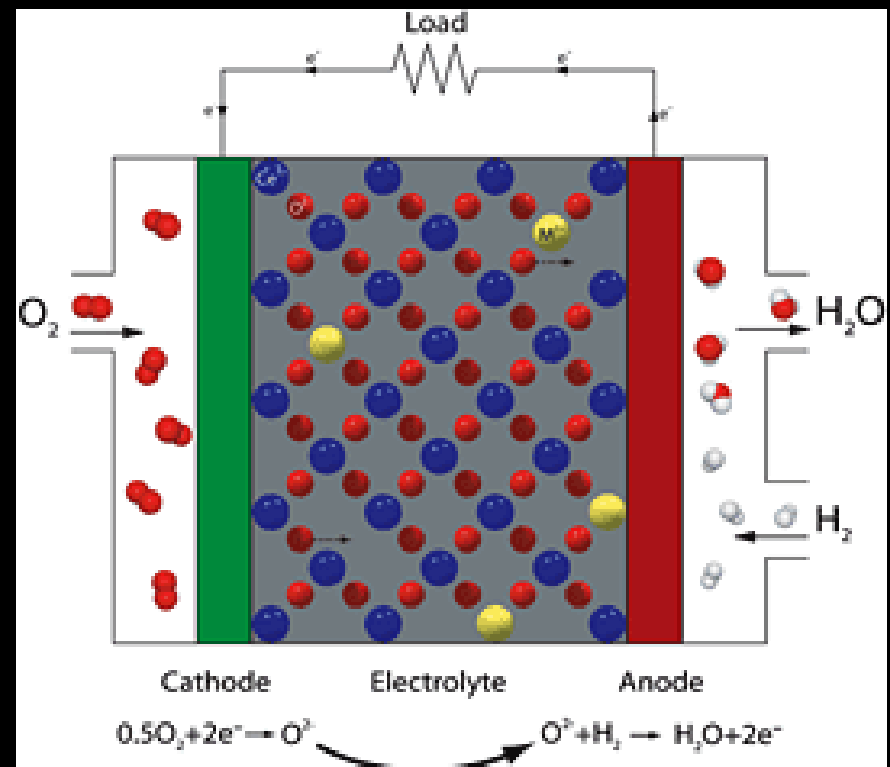
**Figure 2.** FeCr alloys. (a) Calculated curves of the partial  $\mu_{Fe}(x)$  and  $\mu_{Cr}(x)$  (— · —) and total (· · ·) magnetisations, and calculated curves of the energy disorder parameters  $\delta_\sigma$  ( $\sigma = \uparrow, \downarrow$ ) with chromium concentration (—). (b) Calculated variations of the pair potentials with Cr concentration:  $V_1$  (—),  $V_2$  (— · —) and  $V_3$  (· · ·).





# *Optimization of ionic conductivity in doped ceria*

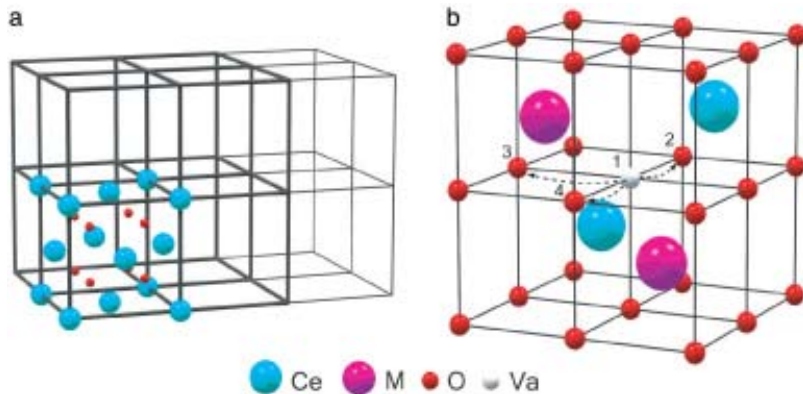
- $\text{CeO}_2$  is known to be good solid electrolyte when it is doped with cations of lower valence than the host cation.
- Attractive electrolyte for solid-oxide fuel cells
- It is important to optimize the ionic conductivity in order to decrease the operation temperature



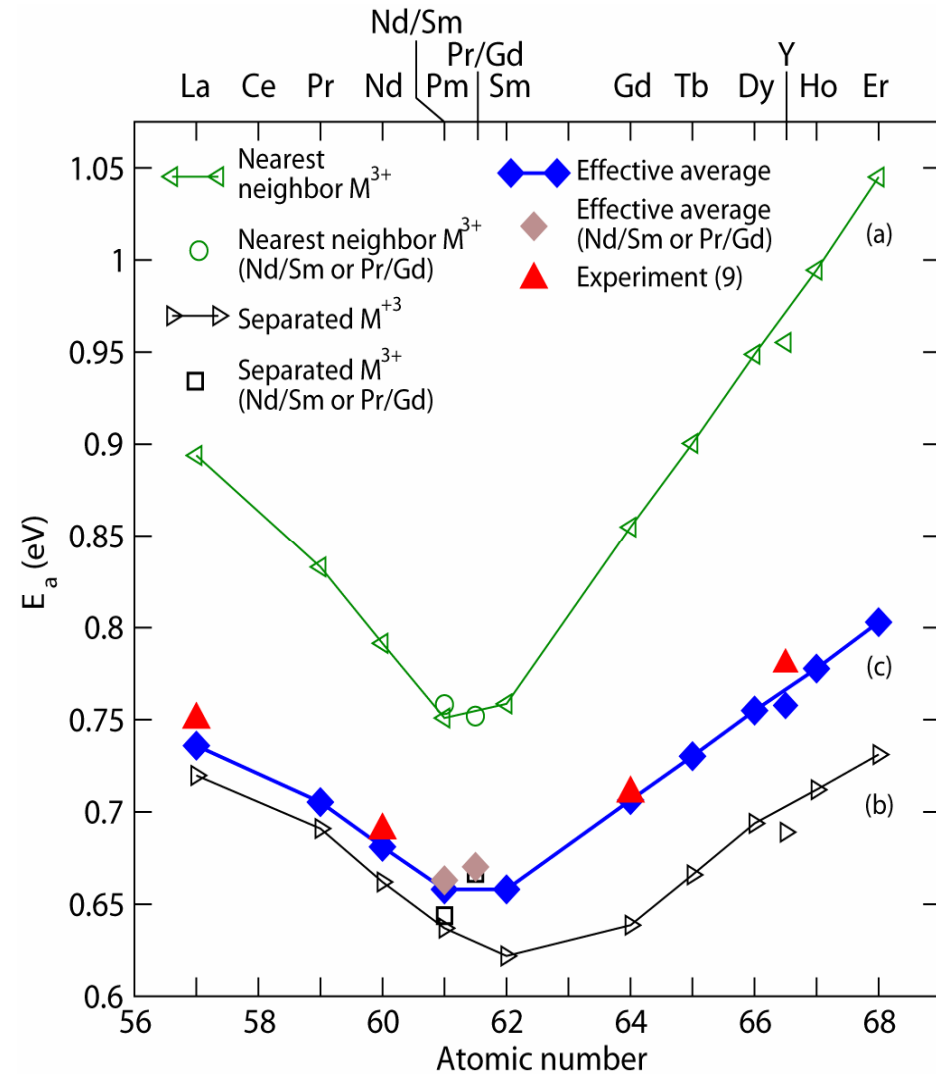
# Activation energy for diffusion

$E_a$  determines the ionic conductivity ( $\sigma$ ):

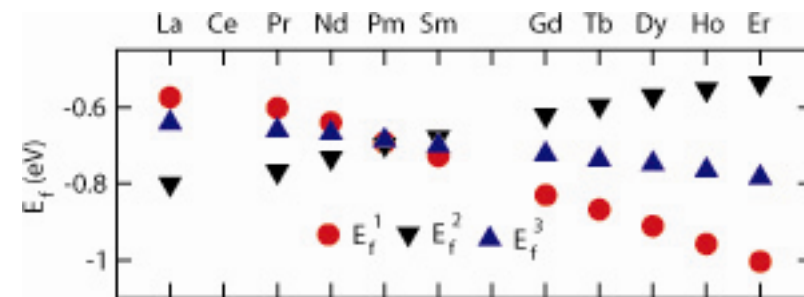
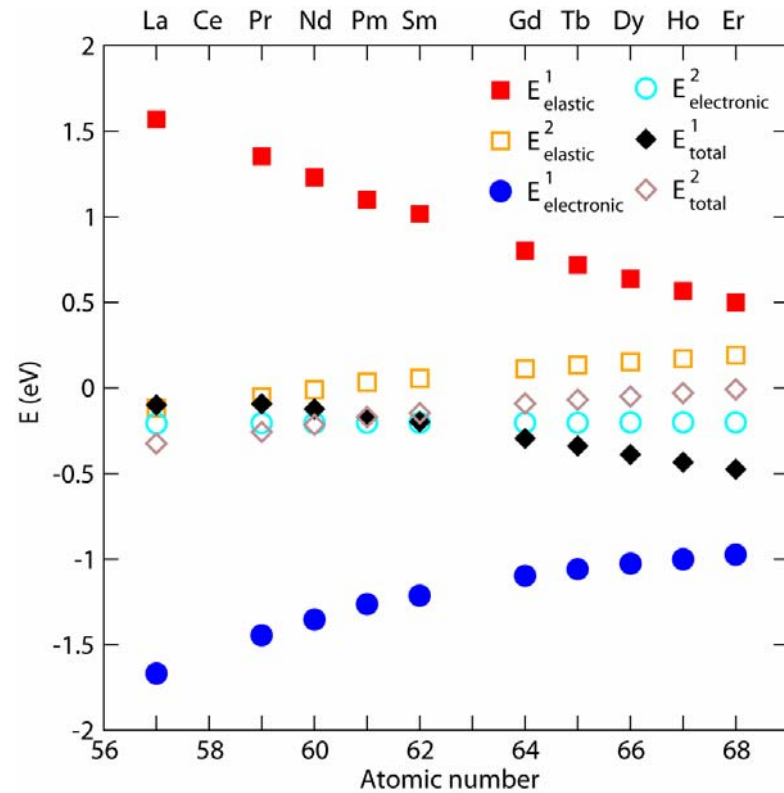
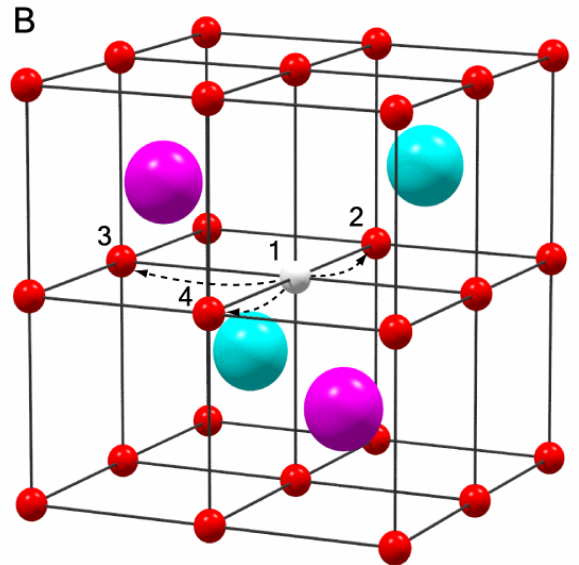
$$\sigma = \sigma_0 / T \cdot \exp\left(-\frac{E_a}{k_B T}\right)$$



$$E_a = E_{ass} + E_m$$



# Defect formation energies



# Activation energy for diffusion

**PATENT COOPERATION TREATY**

From the INTERNATIONAL SEARCHING AUTHORITY

**PCT**

NOTIFICATION OF TRANSMITTAL OF  
THE INTERNATIONAL SEARCH REPORT AND  
THE WRITTEN OPINION OF THE INTERNATIONAL  
SEARCHING AUTHORITY, OR THE DECLARATION

(PCT Rule 44.1)

To:	STENBORG Anders Aros Patent AB P.O. Box 1544 SE-751 45 Uppsala
Date of mailing (day/month/year)	27-12-2006
Applicant's or agent's file reference	FOR FURTHER ACTION See paragraphs 1 and 4 below
Applicant's or agent's file reference	P494PC00
International application No.	International filing date (day/month/year)
PCT/SE2006/050299	29-08-2006
Applicant	
ANDERSSON David et al	

1. ☒ The applicant is hereby notified that the international search report and the written opinion of the International Searching Authority have been established and are transmitted herewith.

**Filing of amendments and statement under Article 19:**  
The applicant is entitled, if he so wishes, to amend the claims of the international application (see Rule 46):

**When?** The time limit for filing such amendments is normally 2 months from the date of transmittal of the international search report.

**Where?** Directly to the International Bureau of WIPO, 34 chemin des Colombettes  
1211 (Geneva 20, Switzerland, Facsimile No.: +41 22 338 82 70

For more detailed instructions, see notes on the accompanying sheet.

2. ☐ The applicant is hereby notified that no international search report will be established and that the declaration under Article 17(2)(a) to that effect and the written opinion of the International Searching Authority are transmitted herewith.

3. ☐ With regard to the protest against payment of (an) additional fee(s) under Rule 40.2, the applicant is notified that:

☐ the protest together with the decision thereon has been transmitted to the International Bureau together with the applicant's request to forward the texts of both the protest and the decision thereon to the designated Offices.

☐ no decision has been made yet on the protest: the applicant will be notified as soon as a decision is made.

4. **Reminders**

Shortly after the expiration of 18 months from the priority date, the international application will be published by the International Bureau. If the applicant wishes to avoid or postpone publication, a notice of withdrawal of the international application, or of the priority claim, must reach the International Bureau as provided in Rules 90bis.1 and 90bis.3, respectively, before the completion of the technical preparations for international publication.

The applicant may submit comments on an informal basis on the written opinion of the International Searching Authority to the International Bureau. The International Bureau will send a copy of such comments to all designated Offices unless an international preliminary examination report has been or is to be established. These comments would also be made available to the public but not before the expiration of 30 months from the priority date.

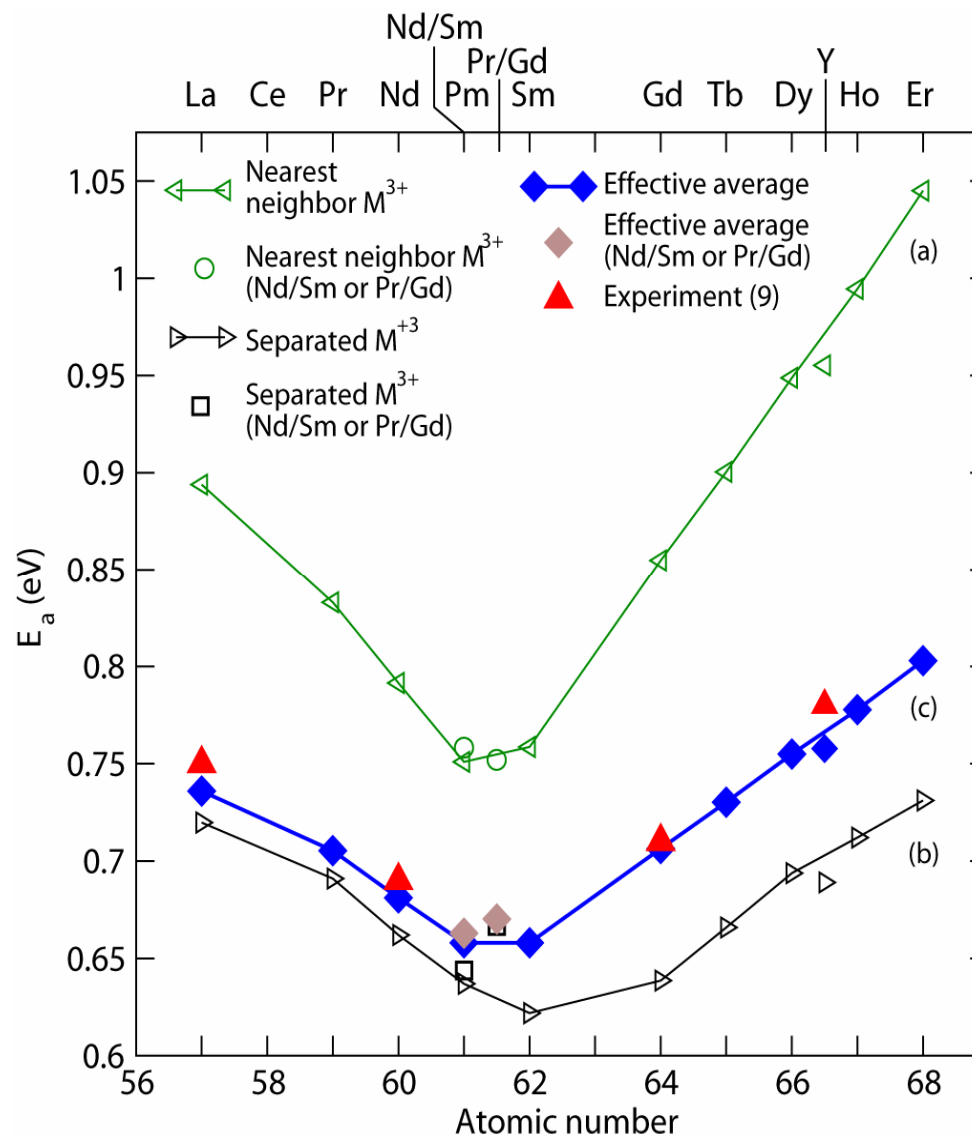
Within 19 months from the priority date, but only in respect of some designated Offices, a demand for international preliminary examination must be filed if the applicant wishes to postpone the entry into the national phase until 30 months from the priority date (in some Offices even later); otherwise, the applicant must, within 20 months from the priority date, perform the prescribed acts for entry into the national phase before those designated Offices.

In respect of other designated Offices, the time limit of 30 months (or later) will apply even if no demand is filed within 19 months.

See the Annex to Form PCT/IB/301 and, for details about the applicable time limits, Office by Office, see the PCT Applicant's Guide, Volume II, National Chapters and the WIPO Internet site.

Name and mailing address of the ISA/ Patent- och registreringsverket Box 5055 S-102 40 STOCKHOLM Facsimile No. 08-067 72 88	Authorized officer  Telephone No. 08-782 25 00
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Form PCT/ISA/220 (October 2005) (See notes on accompanying sheet)



# *CONCLUSIONS :*



- Treatment of the alloying effects within the electronic structure theory can be carried out at different levels and by different methods, depending on the problem at hand, but with certain degree of caution.
- Analysis of the electronic structure allows for the fundamental understanding of the physics behind the technologically relevant phenomena.
- The decomposition in (TiAl)N hard coating alloys with high Al content is enhanced by the increased localization of non-bonding states at transition metal sites.
- Anomalous stability of low Cr steels is determined by the band-filling effects.
- We predicted theoretically new alloy compositions which should optimize the ionic conductivity in doped ceria