



*The Abdus Salam
International Centre for Theoretical Physics*



1854-14

Workshop on Grand Unification and Proton Decay

22 - 26 July 2007

MSGUTs at 25: back to Limbo?

Charan AULAKH
*Panjab University
Chandigarh, India*

MSGUTs at 25 : back to Limbo ?

C. S. Aulakh

(Panjab Univ, Chandigarh)

- MSGUTs : A brief bi(bli)o-graphy
- SO(10) Fermion Fitting Frenzy
- Bloom to Doom : **MSGUT Seesaw failure**
- **Saving the MSGUT**
- New Minimal Susy GUT : Back to Limbo ?
- **RG Thresholds : Generic $\tau_P^{d=5} \gg 10^{33\text{yrs}}$ yrs**
- Pleromal Condensation : Liberation from Limbo ?

MSGUTs : A brief bi(bli)o-graphy -I

Structural Aspects : SSB,Spectra,RG Flow

- BIRTH (1982) : $210 + 10 + 126 + \overline{126}$ SO(10) Susy
GUT CSA, Mohapatra ; Clark, Kuo, Nakagawa.
- BAPTISM 1993 : D.G. Lee : Symmetry Breaking and Mass
Spectra in Minimal Susy SO(10) Unified Theory
- BAR-MITZVAH 2003 : Parameter Counting, Analytic SSB
CSA, Bajc, Melfo, Senjanovic, Vissani (BMSV) (2003,2004);
Spectra CSA Girdhar (2003,2004); BMSV (2004) ; Fukuyama,
Ilakovac, Kikuchi, Meljanac, Okada(2004).
- YOUTH : Threshold Effects Meaningful : CSA, Girdhar(2004);
Apposite (High M_X, M_t ..) : CSA, Garg(2005,2006) *The New
MSGUT.*

MSGUTs : A brief bi(bli)o-graphy -II

Angst and Bloom : Fermion Spectra and Predictivity

- Seminal idea for SO(10) Fermion Masses : $\mathbf{10} + \overline{\mathbf{126}} \Rightarrow$ predictive for M_ν ? ! Babu, Mohapatra(1992)
- Angst : Large θ_{PMNS} failures : **First Type I fit : Complex!** Matsuda,Koide, Fukuyama,Nishiura (2002)
BLOOM Bajc, Senjanovic, Vissani(2003) : **Type II**
 $\Rightarrow m_b - m_\tau \Leftrightarrow large \theta_{PMNS} : \mathbf{FFF}$;
 3 Generation. Goh Mohapatra Ng + Nasri (2003,4).
- Bertolini,Frigiero, Malinsky(2004,2005)Realistic Type II +/- **120**; Babu,Macesanu(2005) (Almost) Realistic Type I, II.
- Datta,Mimura, Mohapatra(04/05):
120+ < CP > + Type II optimal

MSGUTs : A brief bi(bli)o-graphy -III

Doom and **Rebirth** : Falsification and reinvention

- Intimations of Mortality : M_ν always too small hep-ph/0506291
C.S.A *MSGUTs From germ to bloom : Towards Falsifiability and beyond* ; BMSV (hep-ph/0511352): 'x' best scan parameter .
- hep-ph/0512224 **Global Proof C.S.A, S.K. Garg** *MSGUT : From Bloom to Doom.*
- **Confirmed Heartbreak** ph-0605006, **Bertolini, Schwetz, Malinsky**
- **10, 120** $\gg \overline{126}$ Type I evades no-go CSA hep-ph/0602132, hep-ph/0607252 .
- Accurate Type I 10, 120 $\gg \overline{126}$ Realistic Fits : W. Grimus and H. Kühbock hep-ph/0607197, hep-ph/0612132. **Non predictive !**

VIRTUES OF SO(10) UNIFICATION

- $\{Q_L, L_L, u_L^c, d_L^c, l_L^c \oplus \nu_L^c\} \equiv 16$: Tight and complete !
- NATURAL HOME TO BOTH SEESAWS
 $\vec{\Delta}_R(1, 3, -2), \vec{\Delta}_L(3, 1, 2) \subset \overline{126}$:

$$M_{B-L} \sim \langle \vec{\Delta}_R \rangle_{SM=0} \Rightarrow M_{\nu^c} \Rightarrow M_{\nu}^I$$

$$\frac{v_W^2 M'_{B-L}}{M_{B-L}^2} \sim \langle \vec{\Delta}_L \rangle_{Y=2, T_{3L}=-1} \Rightarrow M_{\nu}^{II}$$

- SO(10) FM Higgs

$$16 \otimes 16 = 10 \oplus 120 \oplus 126 \Rightarrow 16 \cdot 16 \cdot (10 + 120 + \overline{126})$$

- SO(10) AM Higgs (**R-PARITY PROTECTED! LSP STABLE**):
 $45 \oplus 54 \oplus 126 \oplus \overline{126}$ OR $210 \oplus 126 \oplus \overline{126} \Rightarrow MSGUT$

Guts OF MSGUT

- **AM Higgs** : $\langle \mathbf{210}(\Phi_{ijkl}), \overline{\mathbf{126}}(\overline{\Sigma}_{ijklm}) \mathbf{126} \rangle \Rightarrow$
Susy $SO(10) \longrightarrow MSSM$
- **FM Higgs** : $\mathbf{10}$ -plet(\mathbf{H}_i) $\overline{\mathbf{126}}$ dual (AM-FM) : $v_{EW}, M_\nu^{I,II}$
- $3 \times \mathbf{16} : \Psi_A (A = 1, 2, 3)$ **MATTER** (including $\bar{\nu}_L^A$).
 $\mathbf{16} = (4, 2, 1) + (\bar{4}, 1, 2) \quad ; \quad \mathbf{4} = [3, 1, \frac{1}{3}] + [1, 1, -1]$
 $(4, 2, 1) = (Q_\alpha, L_\alpha) \quad \quad (\bar{4}, 1, 2) = (\bar{Q}_{\dot{\alpha}}, \bar{L}_{\dot{\alpha}})$
- $SU(3) \times U(1)_{B-L} \times SU(2)_R \times SU(2)_L \subset SU(4) \times SU(2)_R \times SU(2)_L \subset SO(10)$
 $Q_e = T_{3L} + T_{3R} + \frac{B-L}{2}$

MSGUT SSB-I : VEVS

- **Superpotential**

$$\begin{aligned}
 W &= m \, 210^2 + \lambda \, 210^3 + M \, 126 \cdot \overline{126} + \eta \, 210 \cdot 126 \cdot \overline{126} \\
 &+ 10 \cdot 210(\gamma \, 126 + \bar{\gamma} \, \overline{126}) \\
 &+ M_H \, 10^2 + h_{AB} \, 16_A \cdot 16_B + f'_{AB} \, 16_A 16_B
 \end{aligned}$$

Superpotential Parameters : **(25) Minimal !!** ABMSV(2003)

- **GUT scale VEVS : $SO(10) \rightarrow MSSM$**

$$\begin{aligned}
 \langle (15, 1, 1) \rangle_{210} &: \langle \phi_{abcd} \rangle = \frac{a}{2} \epsilon_{abcdef} \epsilon_{ef} \\
 \langle (15, 1, 3) \rangle_{210} &: \langle \phi_{ab\tilde{\alpha}\tilde{\beta}} \rangle = \omega \epsilon_{ab} \epsilon_{\tilde{\alpha}\tilde{\beta}} \\
 \langle (1, 1, 1) \rangle_{210} &: \langle \phi_{\tilde{\alpha}\tilde{\beta}\tilde{\gamma}\tilde{\delta}} \rangle = p \epsilon_{\tilde{\alpha}\tilde{\beta}\tilde{\gamma}\tilde{\delta}} \\
 \langle (10, 1, 3) \rangle_{\overline{126}} &: \langle \overline{\Sigma}_{\hat{1}\hat{3}\hat{5}\hat{8}\hat{0}} \rangle = \bar{\sigma} \quad ; \quad \langle (\overline{10}, 1, 3) \rangle_{126} : \langle \Sigma_{\hat{2}\hat{4}\hat{6}\hat{7}\hat{9}} \rangle = \sigma
 \end{aligned}$$

MSGUT SSB-III : Analytic Solution : 1 Complex Modulus

- D Terms : $|\sigma| = |\bar{\sigma}|$
- F Terms : **SSB completely analyzable !!** 4 eqns \Rightarrow **Cubic in**
 $x = -\lambda\omega/m : \xi = \frac{\lambda M}{\eta m}$. (ABMSV 2003)
 $8x^3 - 15x^2 + 14x - 3 = -\xi(1-x)^2$
- Units : $\frac{m}{\lambda}$
 $\tilde{a} = \frac{(x^2+2x-1)}{(1-x)}$; $\tilde{p} = \frac{x(5x^2-1)}{(1-x)^2}$; $\tilde{\sigma}\tilde{\bar{\sigma}} = \frac{2}{\eta} \frac{\lambda x(1-3x)(1+x^2)}{(1-x)^2}$
- At Special Points : Quadratic/Linear e.g :
 - * $SU(5) \times U(1) : p = a = -\omega = -m_{\Phi}/3\lambda ; \sigma = 0$
 - * $SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} : p = \omega = \sigma = 0 ;$
 $a = -m_{\Phi}/\lambda$

Spectra and Control Parameter x

- ξ/x **Crucial Control Parameter**
 $x \rightarrow \xi$ **1 to 1!!** Trade ξ for x :: **3 FOLD GAIN !!**
 :SCAN OVER x -plane for fixed values of slow parameters.
- Chiral GUT scale spectra : 52 MSSM multiplet sets,
 26 MSSM types : 18 unmixed , 8 mixed : 504 Fields
 CSA, Girdhar(2003) ; Fukuyama, Ilakovac, Kikuchi, Mejanac,
 Okada (2004), BMSV (2004), CSA Girdhar(2004)
 Complete gauge, spinor couplings , Clebsches : CSA Girdhar
 (2002) (2004)
- Spectra \Rightarrow RG including Threshold effects etc. CSA, Girdhar
 (2004), CSA, Garg(2005/6)

Light Doublets and $m_{q,l}$

- Doublet Masses CSA, Girdhar (2003) : **10, $\overline{126}$, 126, 210**

$$\mathcal{H} = \begin{pmatrix} -M_H & +\bar{\gamma}\sqrt{3}(\omega - a) & -\gamma\sqrt{3}(\omega + a) & -\bar{\gamma}\bar{\sigma} \\ -\bar{\gamma}\sqrt{3}(\omega + a) & 0 & -(2M + 4\eta(a + \omega)) & 0 \\ \gamma\sqrt{3}(\omega - a) & -(2M + 4\eta(a - \omega)) & 0 & -2\eta\bar{\sigma}\sqrt{3} \\ -\sigma\gamma & -2\eta\sigma\sqrt{3} & 0 & -2m + 6\lambda(\omega - a) \end{pmatrix}$$

- $\bar{U}^T \mathcal{H} U = Dg(m_H^{(1)}, m_H^{(2)}, \dots); h^{(i)} = U_{ij} H^{(j)} ; \bar{h}^{(i)} = \bar{U}_{ij} \bar{H}^{(j)}$
- Fine Tune $M_H \Leftarrow \text{Det}\mathcal{H} = 0 \Rightarrow$ Light Doublets $H^{(1)}, \bar{H}^{(1)}$

$$E \ll M_X \quad : \quad \begin{aligned} h^{(i)} &\rightarrow \alpha_i H^{(1)} & ; & \alpha_i = U_{i1} \\ \bar{h}^{(i)} &\rightarrow \bar{\alpha}_i \bar{H}^{(1)} & ; & \bar{\alpha}_i = \bar{U}_{i1} \end{aligned}$$

- $\mathcal{H}\alpha = 0 \quad ; \quad \bar{\alpha}^T \mathcal{H} = 0 \quad \Rightarrow \alpha, \bar{\alpha}.$
(ABMSV(2003), BMSV(2004), CSA, Garg(2006))

FERMION MASSES IN SO(10)

- Data for GUT To Explain :

Measured(17) : $m_{q,l}, \theta_i^{CKM}, \delta^{CKM}, \Delta m_\nu^2, \theta_{12,23}^{PMNS}$

Bounded: $\theta_{13}^{PMNS} < .15$

- Awaited (4) : $M_\nu, \delta^{PMNS}, \alpha_{1,2}^{PMNS}$

- Yukawa couplings : $h = h^T, f = f^T, g = -g^T$

$$W = \mathbf{16}_A \times \mathbf{16}_B \cdot (h_{AB}\mathbf{10} + f_{AB}\overline{\mathbf{126}} + g_{AB}\mathbf{120})$$

- MSGUT : only $\mathbf{10} + \overline{\mathbf{126}}$ Dirac masses at M_X

$$m^u = v(\hat{h} + \hat{f})$$

$$m^\nu = v(\hat{h} - 3\hat{f})$$

$$m^d = v(r_1\hat{h} + r_2\hat{f})$$

$$m^l = v(r_1\hat{h} - 3r_2\hat{f})$$

- Seesaw masses :

$$\begin{aligned}
 M_\nu^I &= vr_4 \hat{n} \\
 M_\nu^{II} &= 2vr_3 \hat{f} \\
 \hat{n} &= (\hat{h} - 3\hat{f})\hat{f}^{-1}(\hat{h} - 3\hat{f})
 \end{aligned}$$

- Babu and Mohapatra (1992) : $\mathbf{10} \oplus \overline{\mathbf{126}} \Leftrightarrow m_{q,l} \Rightarrow$
Predictive in the Neutrino Sector ?! : failure (1992,93,94..)
- Matsuda, Koide , Fukuyama, Nishiura (2002): Successful Type I , large θ^{PMNS} fit. Requires CP violation!

Type II: BM -BSV FITTING FRENZY

- Bajc, Senjanovic, Vissani (2003) Large PMNS mixing angle
 $b - \tau$ unification connection

$$M_{\nu}^{II} \sim f \langle \Delta_L \rangle \sim (M_d - M_l) \sim m_{\tau} \begin{pmatrix} \epsilon^2 & \epsilon^2 \\ \epsilon^2 & \frac{(m_b - m_{\tau})}{m_{\tau}} \end{pmatrix} \Rightarrow$$

$$\text{MSSM} : m_b \simeq m_{\tau}(M_X) \Rightarrow \theta_{23}^{PMNS} \simeq 1$$

- Goh Mohapatra Ng : Type II : 3 generations , Real/Complex :
Good Fits except $\delta^{CKM} > \frac{\pi}{2}$.
- Bertolini, Malinsky (2004)(Type II, $\oplus 120$) ; Babu Macesanu
(2005)(Type I and II) **Good Angle and Ratio Fits. !!**
- Datta Mimura, Mohapatra(2004/5) **120**, $\langle CP \rangle$, Type II:
parameters reduced and generic fits excellent. $d = 5$ proton
decay controllable by cancellations

MSGUT DOOM

- Type I ,Type II generic fits : freedom to choose r_1, r_2, r_3, r_4 assumed. M_ν scale, Relative strength of Type I / Type II assumed. **NOT JUSTIFIED IN MSGUT !**
- In MSGUT magnitude and relative strength of seesaw masses fixed !! Fit fully specified : is it viable ??
- **NO !!** CSA (2005), CSA, Garg (2005)
Seesaw masses ($v^2/M_X^0 = (1.7 \times 10^{-3} eV)$)

$$M_\nu^I = (1.7 \times 10^{-3} eV) \sin \beta F_I \hat{n}$$

$$M_\nu^{II} = (1.7 \times 10^{-3} eV) \sin \beta F_{II} \hat{f}$$

- $F_{I,II}$ known and bounded by $10^{\sim 1}$ so M_ν too small.

$$F_I = \frac{10^{-\Delta_x}}{2\sqrt{2}} \frac{\gamma g}{\sqrt{\eta\lambda}} |p_2 p_3 p_5| \sqrt{\frac{z_2}{z_{16}}} \sqrt{\frac{(1-3x)}{x(1+x^2)}} \frac{q'_3}{p_5}$$

$$F_{II} = 10^{-\Delta_x} \frac{2\sqrt{2}\gamma g}{\sqrt{\eta\lambda}} \frac{|p_2 p_3 p_5|}{(x-1)} \sqrt{\frac{z_2}{z_{16}}} \sqrt{\frac{(x^2+1)}{x(1-3x)}} \frac{(4x-1)q_3^2}{q'_3 q_2 p_5}$$

- **Demo (real ξ)** : CSA(2005-May)
- **Proof using x** : CSA,Garg (2005-December)
- **Checked**, Bertolini, Schwetz, Malinski(2006-April)
- Type II fit $\Rightarrow \hat{f}_{II} \ll \hat{n} = (\hat{h}(\hat{f})^{-1}\hat{h})_{II} \Rightarrow$ Type II \ll Type I
: **Compensation impossible !:**
- Typical Type I fits $\Rightarrow \hat{n} \sim .5 \Rightarrow (M_\nu^I)_{max} < 10^{-3} eV$ (Including all viable singular points) $\Leftrightarrow F_I < 1$

Saving MSGUTs

- $\mathbf{10} \oplus \overline{\mathbf{126}}$ FM Higgs irreps \Rightarrow Type I , Type II Seesaw failure :
 $\oplus \mathbf{120}$ -plet \Rightarrow ???
- $\oplus \mathbf{120}$ perturbation : Bertolini Malinsky, Datta Mimura
 Mohapatra (Spontaneous CP and Type II) ; $g_{AB} = -g_{BA}$:
- **NEW SCENARIO** : $h \oplus g \gg f \Rightarrow (m_{q,l}, \theta_q^i, \delta_c)$. **120** not a
 perturbation but zeroth order contribution.

$\mathbf{120} \supset (\mathbf{15}, \mathbf{2}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{2}, \mathbf{2}) \Rightarrow$ Novel Georgi-Jarlskog ($m_\mu(M_X) \approx 3m_s(M_X)$).

- $f \ll h, g \Rightarrow$ Type I boosted !! ($\hat{n} \sim \hat{f}^{-1}$) !
- $h, g \sim 1 \gg f \Rightarrow M_{\nu^c} \ll M_X$: Characteristic feature!!
- Viable m_f , CKM , Δm_ν^2 , PMNS ?? : **Yes!**

Guts of NMSGUT

- Decomposition **120**-plet w.r.t $SU(4) \times SU(2)_L \times SU(2)_R$

$$\begin{aligned}
 O_{ijk}(120) &= O_{\mu\nu}^{(s)}(10, 1, 1) + \overline{O}_{(s)}^{\mu\nu}(\overline{10}, 1, 1) + O_{\nu\alpha\dot{\alpha}}{}^{\mu}(15, 2, 2) \\
 &+ O_{\mu\nu\dot{\alpha}\dot{\beta}}^{(a)}(6, 1, 3) + O_{\mu\nu}^{(a)}{}_{\alpha\beta}(6, 3, 1) + O_{\alpha\dot{\alpha}}(1, 2, 2)
 \end{aligned}$$

- AM SSB unmodified, 26 MSSM multiplet types same.

$$\begin{aligned}
 W_{120} &= M_O 120 \cdot 120 + k 10 \cdot 120 \cdot 210 + \rho 120 \cdot 120 \cdot 210 \\
 &+ \zeta 120 \cdot 126 \cdot 210 + \bar{\zeta} 120 \cdot \overline{126} \cdot 210 + g_{[AB]} 16_A \cdot 16_B \cdot 120
 \end{aligned}$$

- Parameter Counting : Complex Case

$$M_O, k, \rho, \zeta, \bar{\zeta}, g_{AB} : (1 + 1 + 1 + 2 + 3) \times 2 - 1 = 15 \oplus 25 \quad (old) = 40$$

(Minimal No Longer ?)

- **Too Hasty** : Spontaneous CP violation only ? \Rightarrow All Superpot couplings Real, phases from vevs (\Rightarrow *Complex x!!*)

$$OLD : g, m, M, M_H, \lambda, \eta, \gamma, \bar{\gamma}, h_{AB}, f_{AB} : 8 + 3 + 6 = 17$$

$$NEW : M_O, k, \rho, \zeta, \bar{\zeta}, g_{AB} : 5 + 3 = 8$$

$$TOTAL : 25 \text{ *I.E one less than MSGUT*}$$

- Yukawa couplings to MSSM fermions :

$$m^u = v(\hat{h} + \hat{f} + \hat{g})$$

$$m_\nu = v(\hat{h} - 3\hat{f}) + (r_5 - 3)\hat{g}$$

$$m^d = v(r_1\hat{h} + r_2\hat{f} + r_6\hat{g})$$

$$m^l = v(r_1\hat{h} - 3r_2\hat{f} + (\bar{r}_5 - 3r_6)\hat{g})$$

$$\hat{g} = 2ig\sqrt{\frac{2}{3}}(\alpha_6 + i\sqrt{3}\alpha_5)\sin\beta \quad ; \quad \hat{h} = 2\sqrt{2}h\alpha_1\sin\beta$$

- **New Baryon Decay Channels** : $P[3, 3, \pm\frac{2}{3}]$, $K([3, 1, \pm\frac{8}{3}] \subset 120$

Can the $\overline{126}$ sub dominant scenario work in the NMSGUT ?

YES !

REAL CORE SCENARIO C.S.A (2006)

- Semi-Realistic 3 Generation Model C.S.A(June 2006) : Perturb around 23 sector Core : Good Charged Fermion fit \oplus One Large PMNS \oplus large \hat{n}

The eigenvalues of \hat{h} , \hat{f} , \hat{g} , \hat{n} are (note highly boosted \hat{n})

$$\begin{aligned}
 \hat{h} & : \mathbf{.518} \quad ; \quad .0277 \quad ; \quad 1.92 \times 10^{-5} \\
 \hat{f} & : \mathbf{1.33 \times 10^{-4}} \quad ; \quad 1.11 \times 10^{-4} \quad ; \quad 0.171 \times 10^{-4} \\
 r'_5 \hat{g} & : \mathbf{\pm 0.122} \quad ; \quad 0 \\
 \hat{n} & : \mathbf{113.8} \quad ; \quad 20.045 \quad ; \quad 1.97 \times 10^{-5}
 \end{aligned}$$

\Leftrightarrow Complex necessary ! But Phases not perturbative :

REALISTIC SPONTANEOUS CP VIOLATION FITS

- Grimus Kühbeck (July 2006) : Spontaneous CP violation : All Superpot couplings Real. Downhill Simplex Method : Accurate fit.
- Fit I ; Ad-hoc $Z_2 \Rightarrow f_{12} = f_{23} = g_{13} = 0$, 21 free parameters fit 18 observables

$$\begin{aligned}
 \hat{h} & : 0.58 \quad ; \quad -0.0213 \quad ; \quad 0.000375 \\
 \hat{f} & : 0.105 \quad ; \quad 0.021 \quad ; \quad 0.00033 \\
 r'_5 \hat{g} & : \pm 0.65 \quad ; \quad 0 \\
 \hat{n} & : 31.19 \quad ; \quad 5.996 \quad ; \quad 1.045 \\
 \delta^P & = .21 \quad ; \quad \alpha_1^P = 3.174 \quad ; \quad \alpha_2^P = 0.0023
 \end{aligned}$$

- Grimus Kühbeck Fit II, December 2006 Even better fit with only 18 parameters (No Z_2 symmetry but 6 phases fixed in maximally CP violating way in 120 sector vevs only)

$$\begin{aligned} \hat{h} & : \quad .473 \quad ; \quad .00037 \quad ; \quad 8.15 \times 10^{-5} \\ \hat{f} & : \quad 2.45 \times 10^{-3} \quad ; \quad 1.49 \times 10^{-3} \quad ; \quad 5.8 \times 10^{-5} \\ r'_5 \hat{g} & : \quad \pm .108 \quad ; \quad 0 \\ \hat{n} & : \quad 220.035, 39.867, 7.974 \\ \delta^P & = \quad .0347 \quad ; \quad \alpha_1^P = .0111 \quad ; \quad \alpha_2^P = .0034 \end{aligned}$$

- Z_2 and Phase fixing are ad hoc : 4 parameter freedom remains in reserve to fit measured $\delta^{PMNS}, \alpha_{1,2}^{PMNS}, M_\nu$.
- Similar Inverted Hierarchy fit with even larger \hat{n}
- Clearly of the $\overline{126}$ subdominant type : $\hat{h} > \hat{r}'_5 \hat{g} \gg \hat{f} \sim$ and \hat{n} larger by a factor $> 20 - 400$! So little constraint from GUT coefficients.

MSGUT RG Analysis

CSA Girdhar (2004), CSA (2005), CSA Garg (2005,2006)

- *Are the one loop values of $\alpha_G(M_X)$, $\text{Sin}^2\theta_W$ and M_X generically stable against superheavy threshold corrections ?*
- Hall(Weinberg) : MSSM / Broken SO(10) matching:

$$\frac{1}{\alpha_i(M_S)} = \frac{1}{\alpha_G(M_X)} + 8\pi b_i \ln \frac{M_X}{M_S} + 4\pi \sum_j \frac{b_{ij}}{b_j} \ln X_j - 4\pi \lambda_i(M_X)$$

Match Point : $M_i = M_V = M_X$ Mass of lightest $\Delta B \neq 0$
mediating $[3, 2, \pm \frac{5}{3}]$ (X-type) gauge bosons

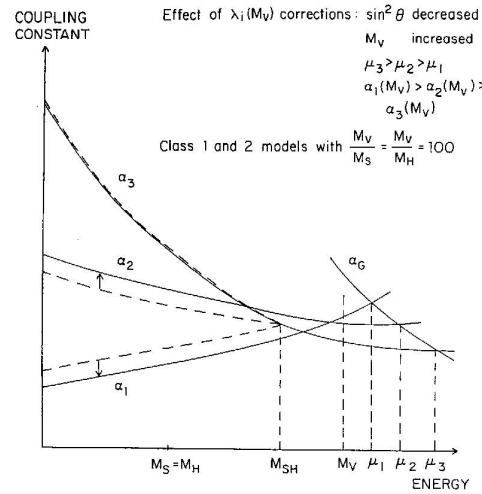


Fig. 3. Unification plot for class 1 and 2 models: $M_V > M_H = M_S$. The dashed lines show the evolution of the two-loop coupling constants $\alpha_i(\mu)$ when $\lambda_i(\mu)$ is neglected, that is with a boundary condition $\alpha_i(M_{SH}) = \alpha_G(M_{SH})$. The full curves show the evolution of $\alpha_i(\mu)$ when all second-order corrections are included. The arrows show the displacement of α_1 and α_2 due to the contributions of $\lambda_i(M_V)$ to $\sin^2 \theta$. The curves are drawn for a fixed α_{QED} and α_s input at $\bar{\mu}$, but are not drawn to scale. The position of the unification points at μ_i (although not their orderings) depends on the details of the model.

Figure 1:

Unification Stability : $\Delta\{(\log_{10} M_X, \sin^2 \theta_W(M_S), \alpha_G^{-1}(M_X))\}$

- SO(10) perturbative $\oplus \lambda, \eta, \gamma, \bar{\gamma}, G_N$ loop neglect \oplus data accuracy :

$$\begin{aligned} |\Delta_G| &= |\Delta(\alpha_G^{-1}(M_X))| \leq 10 \\ 2 > \Delta_X &= \Delta(\text{Log}_{10} M_X) \geq -1 \\ |\Delta_W| &= |\Delta(\sin^2 \theta_W(M_S))| < .02 \end{aligned}$$

- Threshold + 2 Loop (-.08,.0026,-.546) Corrections :

$$\begin{aligned} \Delta_X &= -.0583 + .0167 \sum_{M'} (5\bar{b}'_1 + 3\bar{b}'_2 - 8 \sum_{M'} \bar{b}'_3) \text{Log}_{10} \frac{M'}{M_X} \\ \Delta_W &= .00264 - .00024 \sum_{M'} (4\bar{b}'_1 - 9.6\bar{b}'_2 + 5.6\bar{b}'_3) \text{Log}_{10} \frac{M'}{M_X} \\ \Delta_G &= -.3895 + .01832 \sum_{M'} (5\bar{b}'_1 + 3\bar{b}'_2 + 12\bar{b}'_3) \text{Log}_{10} \frac{M'}{M_X} \end{aligned}$$

- MSGUT 504 heavy Fields (NMSGUT 624 heavy fields)
 $\sum_{M'}$ \Rightarrow Large threshold effects ?? Dixit, Sher(1989) : *Futility of High Precision SO(10) Calculations* .
 CSA, Girdhar (2004) Calculated spectra \Rightarrow well defined, consistent perturbative fine structure at M_X to 1-loop architecture.
- $\xi = \lambda M / \eta m \leftrightarrow x$ only “fast ” spectral control parameter.
- $\Delta^{th} \sim \log(\lambda, \eta, \gamma, \bar{\gamma})$
- * $\lambda, \eta \ll 1 \Rightarrow \Delta_G \ll 0 \Rightarrow \alpha_G$ explosion !! $\Rightarrow \lambda, \eta \sim 1$ (exact unimportant).
- Mass parameters : Overall scale : $m_{210} \sim M_X$; M_H tuned , M_{126} in ξ .

$$|m| = 10^{16.25 + \Delta_x} \frac{|\lambda|}{g \sqrt{4|\tilde{a} + \tilde{w}|^2 + 2|\tilde{p} + \tilde{w}|^2}} \text{GeV}$$

Large M_X Natural ?

- **Generic problem of Susy GUTs** : $\tau_P^{d=5, \Delta B \neq 0} < 10^{33}$ yrs
already near conflict with $M_X \sim 10^{16.25}$ GeV.
- **Raising M_X with threshold corrections.....** Bajc, Senjanovic (2006)
 - (a) Artificial cancellations to raise $\tau_P^{d=5, \Delta B \neq 0}$ unnatural. **Radical solution: Raise M_X by threshold effects to $> \sim 10^{18}$ GeV**
!! Shown possible in toy model with M_3, M_8 free (rest neglected)
 - (b) $M_X \sim M_P \Rightarrow$ (Ovrut, Raby) dispense with extra GUT singlet sector, use GUT MSSM singlets for Susy breaking. **!!**
- **NMSGUT** : All thresholds calculated : $M_X > 10^{17.25}$ GeV
generic in MSGUTs **!!**

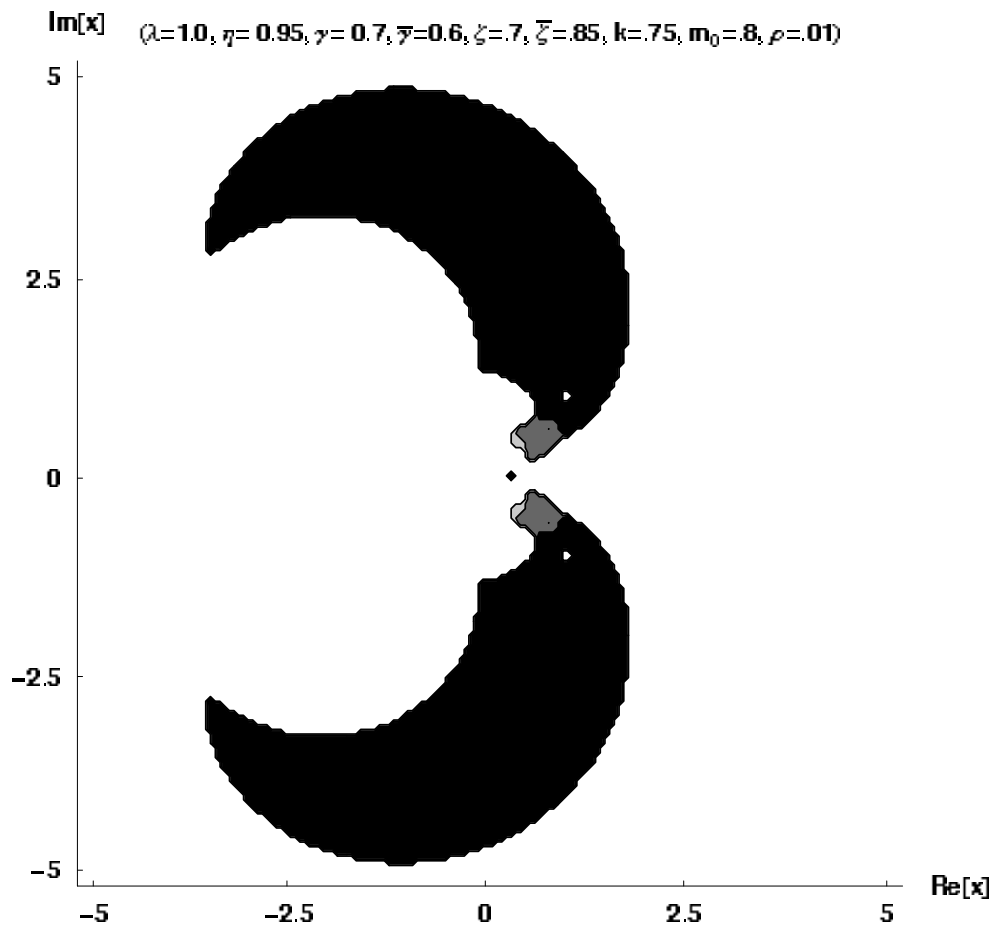


Figure 2: Typical NMSGUT : Regions of the x -plane compatible with the unification constraints : darkest regions have $2 \geq \Delta_X > 1$ (corresponding to $10^{18.25} > M_X > 10^{17.25} \text{GeV}$), the next darkest $1 \geq \Delta_X > 0$ the lightest shade $0 \geq \Delta_X > -1$ and the white regions are disallowed.

NMSGUT RG Features

- Spont CP violation requires complex branch $x_+(\xi)$
- On Spontaneous CP solution line, $\Delta_X > 0.2$: M_X always raised !
- $x_+(\xi)$: $M_X < 10^{17.25}$ exceptionally near $\xi \sim 4$ only !
- All masses follow M_X through $m \sim M_X$: Lightest Baryon violating triplets in all sectors $t[3, 1, \pm \frac{2}{3}]$, $P[3, 1, \pm \frac{2}{3}]$, $K[3, 1, \pm \frac{8}{3}]$ raised above $10^{16.5} GeV \Rightarrow d = 5$ decay operators innocuous.
- $\overline{126}$ vev also raised above $10^{16} GeV$! Very Small $\overline{126}$ Yukawa couplings necessary!! Another seesaw scissor between m_ν and M_X !
- Landau Pole of MSGUTs : Huge SO(10) beta Fns $\bar{b} > 137$!!
 $\Rightarrow \Lambda \sim M_X$! Gauge/Planck strong coupling. **SQUEEZE HERE !!**

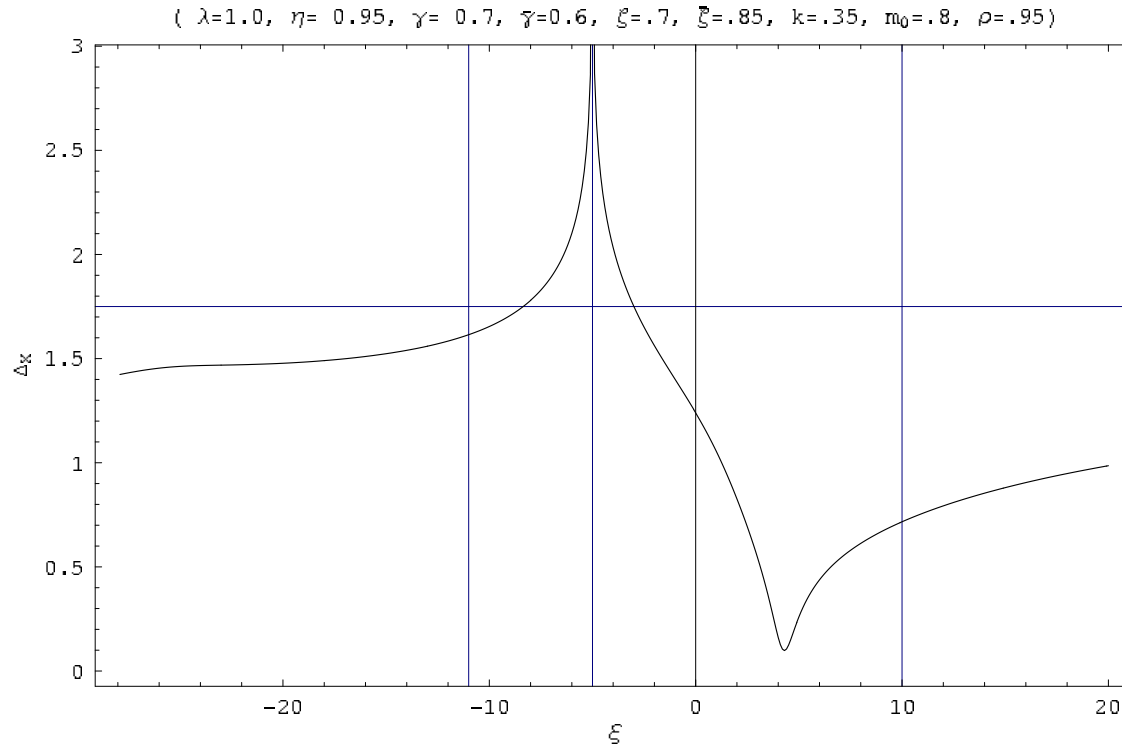


Figure 3: Plot of Δ_X against ξ on the CP violating solution branch $x_+(\xi)$ at representative allowed values of the diagonal parameters. Spike due to $C[8, 2, \pm 1]$ massless exactly at $\xi = -5$

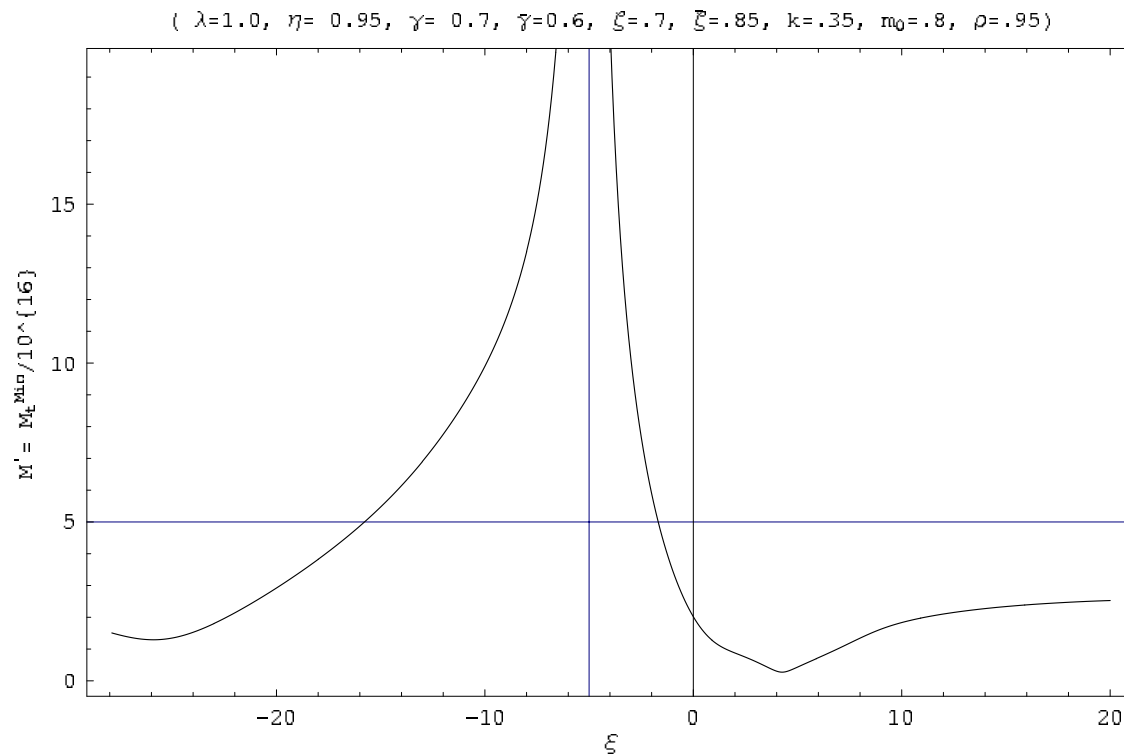


Figure 4: Plot of M_t^{min} , the lightest triplet of MSSM type $[3, 1, \pm \frac{2}{3}]$, against ξ on the CP violating solution branch $x_+(\xi)$ at representative allowed values of the diagonal parameters. Units of $10^{16} GeV$.

Taming Asymptotic Strength

- SU(2) Toy model CSA(2002): $\mathbf{5}$ plet $b_0 = 10 - 6 = 4 \Rightarrow$
Asymptotically Strong : Landau pole at $\mu = \Lambda \sim m e^{\frac{2\pi^2}{g^2(m)}}$
- Supersymmetry in UV \Rightarrow Apply Holomorphy techniques !
- UV Dynamical symmetry breaking $SU(2) \rightarrow U(1)$ due to condensation of Coset gauginos and Φ in ULTRAVIOLET

$$\langle \lambda^+ \lambda^- \rangle \sim \langle S = W^2 / 32\pi^2 \rangle = \left(\sqrt{\frac{3}{10}} \frac{1}{\lambda} \right)^5 \Lambda^3$$

$$\Phi = \sqrt{\frac{3}{10}} \frac{\Lambda}{\lambda^2} \text{Diag}(1, 1, -2)$$

- Vev Independent of Superpotential mass parameter !

Dynamically Breaking out of Limbo ? : Speculative Wish list

- **Coset Gaugino Condensate** Calculable GUT dynamical ssb by UV Susy SO(10) gaugino/chiral condensation. Gauginos in coset G/H condense preserving H, Chiral multiplet vevs break $G \rightarrow H$. Condensates related via Konishi anomaly and calculable using Seibergistics
- **Konishi problem for 10,16,120** Susy breaking and/or quantum condensates of composite operators **16, 10, 120** may be required to satisfy Konishi Anomaly constraints.
- **Dynamical Scale generation** DSB scale arises from RG flow as UV cutoff of flow. No need for mass scales in Superpot ?
- **Susy Breaking** : Could MSSM singlets in GUT allow metastable susy breaking with $\sqrt{F} \preceq 10^{12}$ GeV ?

- **Doublet masses** : In absence of Superpotential mass parameters light doublet pair with masses M_I^2/M_X may arise naturally and get vevs by RSB.
- **Induced Gravity** Λ_X Supersymmetric Physical Cutoff set by Landau pole : evades no go arguments against Induced Gravity due to CC (Λ^4) and Newton's constant (Λ^2) ambiguities.
- **Dual Unification** Quarks with hearts(G-GUT UV tangles) dual to monopoles of \tilde{G} : asymptotically strong FM yukawas dual to asymptotically weak \tilde{G} ??

Conclusions

- SO(10) NMSGUT is fully compatible with all known FM data and also probably with remaining FM data when available.
- Proton Decay scales are naturally raised
- Falsifiability problematic ! But early days yet !
- Manic/genial UV behaviour : Killer Pandora or Cornucopia ?