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SUSY-breaking in proton decay

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# SUSY breaking in proton decay ....high scale remnants

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# SUSY GUTs

- Understanding the fermion quantum numbers leads to GUTs.
- Gauge couplings also unify.. SUSY GUTs even better.
- Family symmetries can give understanding of masses and mixings.
- Neutrino seesaw is naturally present.
- LSP, lepto-baryogenesys...
- Higgs hierarchy problem solved (the large one).

However:

- In SUSY: proliferation of parameters (and models...).
- In GUTs: proton should decay.



# So proton is not forever (?)

Baryon number nonconservation a natural consequence of Grand-Unified Theories. Probed up to  $\sim 10^{33-34}$ y:



... different channels from different operators.

#### **D=6 operators** [Weinberg, Wilczek Zee '79]



Four-fermions operators: (doublets q, l; singlets  $u^c, d^c, e^c, \nu^c$ )  $O_{\text{gauge}} \sim g^2 M_G^{-2} (\bar{q} u^c \bar{l} d^c), \quad g^2 M_G^{-2} (\bar{q} u^c \bar{q} e^c),$   $O_{\text{higgs}} \sim y^2 M_H^{-2} (q q q l), \quad y^2 M_H^{-2} (u^c u^c d^c e^c).$ The decay width is very sensitive to  $M_G, M_H$ :  $\Gamma_p \simeq m_p^5 |\mathcal{M}|^2 \sim g^4 / M_G^4.$ E.g. for  $M_G, M_H \sim 10^{13-15}$  GeV, these are dangerous:  $\tau_p \sim 10^{25-33}$  y.

### **Recall GUT vs SUSY GUT**



#### SM GUT

#### MSSM GUT

SUSY GUT gives one-shot unification of gauge couplings, in addition to protecting from other issues.

It also sets the GUT scale to  $10^{16}$  GeV, making the D=6 operators safe.



## With SUSY new operators [Weinberg '82]

With supersymmetry GUT is better, but there are new D=5 and D=4:

Most dangerous are D=4 three-superfield operators:

 $UDD^c$ ,  $QLD^c$ ,  $E^cLL$ 

These are happily eliminated by R-parity ( $\Phi \rightarrow -\Phi$ ). This is automatic with some fields content or may be imposed by hand.

■ Then there are D=5 operators, mediated by triplet higgsino *T*:





#### **D=5 operators** [Weinberg, Sakai Yanagida '82]

... two fermions - two scalars

 $O_{\rm higgsino} \sim y^2 M_H^{-1}(\tilde{q} \, q \, \tilde{q} \, l), \quad y^2 M_H^{-1}(\tilde{u}^c \, u^c \, \tilde{d}^c \, e^c).$ 

After dressing they act as D=6:



But are suppressed only by  $M_G m_{SUSY}$ , and give  $\tau_p \sim 10^{28}$  y.

They are very model dependent [e.g. Bajc Filiever-Perez Senjanovic '02] and in many models can be suppressed

[Coughlan et al '85, Babu Barr '93; Berezhiani F.N. '05]

### **D=4 operators?**

One may ask whether there are also D=4 operators, four-scalars.

$$O_{\rm D=4} \sim g^2(\tilde{q}^* \, \tilde{u}^c \, \tilde{l}^* \, \tilde{d}^c), \quad g^2(\tilde{q}^* \, \tilde{u}^c \, \tilde{q}^* \, \tilde{e}^c),$$

... they are unsuppressed, and  $\tau_p \sim 10^{-10} \, \mathrm{s}$  !?

... and they will be allowed, if scalar partners are discovered at LHC!

We know also that they are already in the lagrangian above GUT: they are the D-terms of the heavy gauge fields:

$$\mathcal{L}_{\mathrm{D-term}} = \sum_{A,i} g^2 \left| \phi_i^* \tau_A \phi_i \right|^2.$$

 $\phi_i = \text{sfermion multiplets} \qquad (\text{e.g. } \phi_{10} = (\tilde{u}^c, \tilde{q}, \tilde{e}^c), \phi_{\overline{5}} = (\tilde{d}^c, \tilde{l}) \text{ in SU(5)})$  $\tau_A = \text{GUT gauge generators} \qquad (\text{among them } \tau_X \text{ and } \tau_Y \text{ in SU(5)})$ 

What happens to these terms at low energy?

# SUSY protects

#### Decoupling theorem should work...hence:



Cancellation of D=4 ensured only by SUSY, where all g are equal.

Therefore the discovery of scalar partners will tell us that: GUT will require SUSY in order to protect us from D=4 operators.

However SUSY is actually broken...so?

## Proton decay in broken SUSY

We expect partial cancellations, in particular nonzero D=4 operators due to soft terms in the theory: [Derendinger Savoy '82, Sakai '83]

$$\sim g^2 \frac{m_S^2}{M_G^2} \phi \phi^* \phi \phi^*$$

Dressing (double!) gives four-fermions operators:

$$\sim g^2 \frac{m_S^2}{M_G^2} \frac{\alpha^2}{(4\pi)^2 m_{\tilde{g}}^2} \psi \psi^* \psi \psi^*$$



with same strenght as D=6!

$$\sim g^2 \frac{1}{M_G^2} \psi \psi^* \psi \psi^*$$

(but loop factor...)

How to check their relevance and dependence on soft terms?

#### The calculation...

... is doable in superfields: Chiral  $\Phi = \{\Phi_I\}$ ; Gauge  $V = V_A T_A$ .

 $\mathcal{L} = \int d^4\theta \left[ \Phi^{\dagger} X e^{2gV} \Phi \right] + \text{superpotential} + \text{gauge kinetic term}$ 

Soft masses are in  $X_{IJ} = (1 - m_I^2 \theta^2 \overline{\theta}^2) \delta_{IJ}$ . Expand  $V \dots$ 

$$\simeq \int d^4\theta \Big[ \Phi^{\dagger} X \Phi + 2J_A V_A + M_{AB}^2 V_A V_B + \cdots \Big] \qquad J_A = g \Phi^{\dagger} X T_A \Phi ,$$
$$M_{AB}^2 = 2g^2 \Phi^{\dagger} X T_A T_B \Phi$$

... and integrate the broken gauge fields  $V_A$  between light fields  $\Phi_i$ :



#### Four fields operator

$$= \int \mathrm{d}^4\theta \, \frac{g^2}{2g^2 \langle \Phi_H \rangle^{\dagger} T_A T_A \langle \Phi_H \rangle} \frac{X_i X_j}{X_H} \Big( \Phi_i^{\dagger} T_A \Phi_i \Big) \Big( \Phi_j^{\dagger} T_A \Phi_j \Big)$$

The soft terms enter via  $X_i$ ,  $X_H$  and via  $\langle \Phi_H \rangle$ , that also has a nonzero F-term  $\langle \Phi_H \rangle = v_H (1 + f_H \theta^2)$ .

One can parametrize the result as

$$= \int \lambda_6 \left( 1 + \boldsymbol{\xi} \theta^2 + \boldsymbol{\xi}^{\dagger} \bar{\theta}^2 + \boldsymbol{\omega}_{ij} \theta^2 \bar{\theta}^2 \right) \left( \Phi_i^{\dagger} T_A \Phi_i \right) \left( \Phi_j^{\dagger} T_A \Phi_j \right) \mathrm{d}^4 \theta \,,$$

where  $\lambda_6 = g^2/M_A^2$  is the standard D=6 coupling.

The SUSY breaking coefficients are in general:

$$\xi = -f_H$$
,  $\omega_{ij} = -m_i^2 - m_j^2 + m_H^2 + |f_H|^2$ .

We found standard D=6 plus new D=5 and D=4 operators



#### **New operators**

D=6, 5, 4:



give three competing effects:

$$\lambda_6 \qquad \lambda_6 \, 2\xi \frac{\alpha_3}{4\pi} L(m_{\tilde{q}}, m_{\tilde{g}}) \qquad \lambda_6 \, \omega \frac{\alpha_3}{4\pi} \frac{\alpha_2}{4\pi} [L(m_{\tilde{q}}, m_{\tilde{g}})]^2$$

# Loop factor



Loop function L with  $m_{\tilde{q}}$  from 0.1 to 2 TeV (upper to lower).

Present limits allow  $m_{\tilde{q}} \sim 100 \text{ GeV}$  when  $m_{\tilde{g}} \gtrsim 500 \text{ GeV}$ . In this region the loop factor is almost maximal,  $L \simeq 5 \text{ TeV}^{-1}$ , and one gets:

$$\lambda_6 \left( 1 + \frac{\xi}{10 \,\mathrm{TeV}} + \frac{\omega}{(30 \,\mathrm{TeV})^2} \right)$$

L

Quite large susy-breaking coefficients are needed  $\sim 10 \text{ TeV}!$ 

## SU(5) example

$$W(\Sigma) = M_{\Sigma}(1 - B_{\Sigma}\theta^{2}) \operatorname{tr} \Sigma^{2} + \frac{1}{6}\lambda_{\Sigma}(1 - A_{\Sigma}\theta^{2}) \operatorname{tr} \Sigma^{3},$$
$$\langle \Sigma \rangle = v_{\Sigma} \left[ 1 + (A_{\Sigma} - B_{\Sigma})\theta^{2} \right] \lambda_{24}, \qquad v_{\Sigma} = 8\sqrt{15} \frac{M_{\Sigma}}{\lambda_{\Sigma}}.$$

Soft terms are  $A_{\Sigma}$ ,  $B_{\Sigma}$ , plus all soft masses.  $(\Sigma \in \mathbf{24}_H)$ 

Proton decay can proceed via  $\Phi_{10}\Phi_{10}\Phi_{\bar{5}}\Phi_{\bar{5}}$  or  $\Phi_{10}\Phi_{10}\Phi_{10}\Phi_{10}\Phi_{10}$  and the standard D=6 coupling is:  $\lambda_6(G) = g_5^2/M_A^2$ , with  $M_A^2 = 5 g_5^2 v_{\Sigma}^2/12$ . For the new operators we have:

$$\begin{aligned} \xi &= B_{\Sigma} - A_{\Sigma} \\ \omega_{10\,\overline{5}} &= -m_{10}^2 - m_{\overline{5}}^2 + m_{\Sigma}^2 + |B_{\Sigma} - A_{\Sigma}|^2 \\ \omega_{10\,10} &= -2m_{10}^2 + m_{\Sigma}^2 + |B_{\Sigma} - A_{\Sigma}|^2 , \end{aligned}$$

Squark masses  $m_{10}$ ,  $m_{\overline{5}}$  should be small, but:

Could one have large  $m_{\Sigma}^2$ ,  $A_{\Sigma}$  or  $B_{\Sigma}$ ? ... large  $B_{\Sigma}$  is not forbidden.

#### Large $B_{\Sigma}$ easier than $A_{\Sigma}$

#### **Hierarchy:**

$$W_H(\Sigma, H, \bar{H}) = M_H(1 - B_H \theta^2) \bar{H} H + \lambda_H (1 - A_H \theta^2) \bar{H} \Sigma H.$$

After the SU(5) breaking, we find  $\mu(1-B_{\mu}\theta^2)H_uH_d$ , with

$$\mu = M_H - \frac{3}{\sqrt{60}} \lambda_H v_{\Sigma}, \qquad \mu B_\mu = \frac{3}{\sqrt{60}} \lambda_H v_{\Sigma} (A_{\Sigma} - B_{\Sigma} - A_H + B_H) + \cdots.$$

... two fine tunings needed in general, but ok.

**Runnings:** 

 $B_{\Sigma}$  never appears

$$16\pi^{2} \frac{\mathrm{d}}{\mathrm{d}t} A_{\Sigma} = \frac{63}{20} A_{\Sigma} \lambda_{\Sigma}^{2} + 3A_{H} \lambda_{H}^{2} - 30 g_{5}^{2} m_{\tilde{g}_{5}}$$
$$16\pi^{2} \frac{\mathrm{d}}{\mathrm{d}t} B_{\Sigma} = \frac{21}{10} A_{\Sigma} \lambda_{\Sigma}^{2} + 2A_{H} \lambda_{H}^{2} - 20 g_{5}^{2} m_{\tilde{g}_{5}}.$$

Finite corrections! e.g.:

$$\delta B_{\mu} \sim \frac{\lambda_H^2}{(4\pi)^2} \boldsymbol{B}_{\boldsymbol{\Sigma}}, \qquad \delta m_{\tilde{g}} \sim \frac{g_5^2}{(4\pi)^2} \boldsymbol{B}_{\boldsymbol{\Sigma}},$$

## ...effect of heavy higgses soft terms

Large  $A_{\Sigma}$ ,  $m_{\Sigma}^2$  enter the RG of higgs masses  $m_{H_{u,d}}^2$ : can destabilize electroweak breaking and whole picture of low energy SUSY.

On the other hand, a large  $B_{\Sigma}$  of SU(5) is allowed:

- Hierarchy problem a bit harder, but anyway to be tuned, in minimal SU(5). Usual group-theoretical mechanisms take care.
- *B*-terms never enter (ruin) the running of any quantity.
- Finite corrections are negligible as far as  $B_{\Sigma} < 50\text{-}100 \text{ TeV}$ .

Effects on proton decay are:

$$\tau_{SOFT}^{-1} = \tau_{SUSY}^{-1} \left( 1 + \frac{B_{\Sigma}}{10 \,\mathrm{TeV}} + 0.1 \left| \frac{B_{\Sigma}}{10 \,\mathrm{TeV}} \right|^2 \right)^2$$

So  $B_{\Sigma}$  may be < 50-100 TeV and still affect proton decay.



Shaded regions represent current and 10-years *hoped* limits on the  $p \rightarrow \pi^0 e^+$  partial lifetimes, from Water-Cerenkov detectors. Dashed lines represent the limit of too large  $B_{\Sigma}$ .

 $B_{\Sigma}$  negative  $\sim -10$  TeV will suppress the decay rate, while  $B_{\Sigma}$  positive may enhance the rate by one order of magnitude.

## **Running down from GUT**

When one renormalizes the D=6, 5, 4 operators from the GUT to SUSY scale, they mix among themselves due to gaugino soft masses. We computed these effects using soft RG techniques [Kazakov '97]. Starting from the supersymmetric anomalous dimensions:

$$\frac{\lambda_6(S)}{\lambda_6(G)} = \prod_{\text{gauge groups}} \left(\frac{\alpha_{(i)}(S)}{\alpha_{(i)}(G)}\right)^{-\frac{\gamma_6(i)}{b_{(i)}}} \simeq 3 \qquad \text{[Ibanez, Munoz '84]}$$

we promote  $\alpha$  to superfields,  $(1 + m_{\tilde{g}}\theta^2 + m_{\tilde{g}}\bar{\theta}^2 + m_{\tilde{g}}^2\theta^2\bar{\theta}^2)\alpha$ , and get:

$$4\pi \frac{\mathrm{d}}{\mathrm{d}t} \begin{pmatrix} \lambda_6 \\ \lambda_6 \xi \\ \lambda_6 \xi^{\dagger} \\ \lambda_6 \omega \end{pmatrix} = \sum_{\text{gauge groups}} \gamma_6 \alpha \begin{pmatrix} 1 & 0 & 0 & 0 \\ m_{\tilde{g}} & 1 & 0 & 0 \\ m_{\tilde{g}}^* & 0 & 1 & 0 \\ 2|m_{\tilde{g}}|^2 & m_{\tilde{g}}^* & m_{\tilde{g}} & 1 \end{pmatrix} \begin{pmatrix} \lambda_6 \\ \lambda_6 \xi \\ \lambda_6 \xi^{\dagger} \\ \lambda_6 \omega \end{pmatrix},$$

Since  $m_{\tilde{g}} \ll \xi$ ,  $\omega \Rightarrow$  running is small in this scenario.

# Conclusions, SUSY-GUT interplay

In SUSY GUT, there are soft SUSY-breaking terms in heavy sector:

■ New operators of D=4,5 arise in proton decay.

When dressed they contribute as standard D=6 ones.

- Dressing loop is enough to suppress them for standard soft terms.
- However, soft terms in the heavy higgs sector may be large, and they enter only in proton decay.
- They may definitely suppress also the gauge mediated decay, or even enhance it, bringing it into the region of future sensitivity!

Experimentally: probing high lifetimes in different channels useful! Theoretically: we need *complete* theories of GUT+SUSY mediation!



#### Thanks!

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#### Thanks!

## SUSY superfield decoupling

Chiral fields can be split:  $\{\Phi_I\} \rightarrow \{\Phi_H, \Phi_A, \Phi_i\}$ :

- Some heavy fields  $\Phi_H = \langle \Phi_H \rangle$ , in "Superunitary" gauge. [Fayet '76]
- Goldstones  $\Phi_A$  are eaten by  $V_A$ ;
- $\langle \Phi_H \rangle$  give mass to gauge bosons:

$$M_{AB}^2 = 2g^2 \langle \Phi_H \rangle^{\dagger} T_A T_B \langle \Phi_H \rangle X_H \sim M_G^2 ,$$

• while light fields  $\Phi_i$  remain in the current  $J_A = g \Phi_i^{\dagger} T_A \Phi_i X_i$ .

Decoupling theorem works easy in superfield formalism: An effective, four-fields, D-term is at least D=6:

$$\frac{1}{M_G^2} \int (\Phi_i \Phi_i^{\dagger} \Phi_j \Phi_j^{\dagger}) \,\mathrm{d}^4\theta \,.$$

and D=6 does not contain  $\phi\phi^*\phi\phi^*$ , it only contains  $\phi\Box\phi^*\phi\phi^*$  etc...

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## Loop integral

One fermion and two scalars in the loop:

$$L(m_1, m_2, m_3) = m_3 \frac{m_1^2 m_2^2 \log \frac{m_1^2}{m_2^2} + m_2^2 m_3^2 \log \frac{m_2^2}{m_3^2} + m_1^2 m_3^2 \log \frac{m_3^2}{m_1^2}}{(m_1^2 - m_2^2) (m_1^2 - m_3^2) (m_2^2 - m_3^2)}$$

$$= \frac{1}{m_3} \frac{\frac{m^2}{m_3^2} - 1 - \log \frac{m^2}{m_3^2}}{\left(\frac{m^2}{m_3^2} - 1\right)^2} \quad \text{for } m_1 = m_2 = m$$

with  $m_{1,2}$  squark masses and  $m_3$  the gaugino mass.

