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The forming of a relativistic partially electromagnetic planar plasma shock

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Introduction

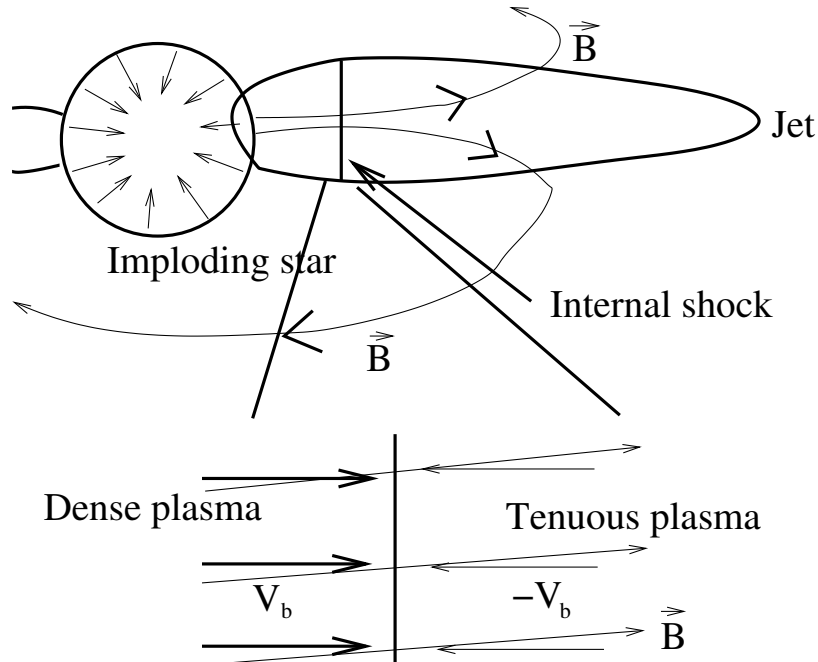
- Gamma-ray bursts are energetic eruptions at cosmological distances
- Source process of long gamma-ray bursts: Massive supernovae
- Origin of gamma ray flash: Ultra-relativistic jet
- Process yielding gamma rays: Synchrotron radiation
- What do we not know:
 - (1) Which process accelerates electrons to ultra-relativistic speeds ?
 - (2) How are the strong magnetic fields generated ?

Possible mechanism: Filamentation instability at internal shocks.

Problem: Weak electron acceleration and 'weak' small-scale \mathbf{B}
- Here: We consider shocks due to a more powerful wave

Internal shock model

- Imploding strongly magnetized star results in compact object
- Magnetic field and angular momentum conservation constrain plasma flow: Jets may escape along magnetic poles.
- The jets may reach Lorentz factors of hundreds
- Time dependent jet source: Jet density and speed varies \Rightarrow Internal shocks



Assumptions:

Two plasma clouds collide,

Relative speed: $v = 0.9c$,

Density ratio: 10,

Quasi-parallel magnetic field,

Each slab consists of equal numbers

of ions and electrons: Mass ratio 400

Magnetic energy = 0.008 Kinetic energy

Particle-in-cell simulation: Maxwell-Lorentz equations

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}, \quad \nabla \times \mathbf{B} = \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} + \mu_0 \mathbf{J} \quad (1)$$

$$\nabla \cdot \mathbf{B} = 0, \quad \nabla \cdot \mathbf{E} = \rho / \epsilon_0, \quad \frac{d\mathbf{p}}{dt} = e (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \quad (2)$$

Simulation strategy: \mathbf{v}_b is plasma flow velocity and \mathbf{B}_0 initial magnetic field

- Use $\mathbf{B}_0 \cdot \mathbf{v}_b \neq 0$ to suppress waves with \mathbf{k} oblique / perpendicular to \mathbf{v}_b
 \Rightarrow We can use 1D PIC simulations
Test the suppression with 2D simulations
- Use $|\mathbf{B}_0 \times \mathbf{v}_b| \neq 0$ to trigger new waves

2D PIC simulation in x-y plane: Impact of flow-aligned magnetic field B_x

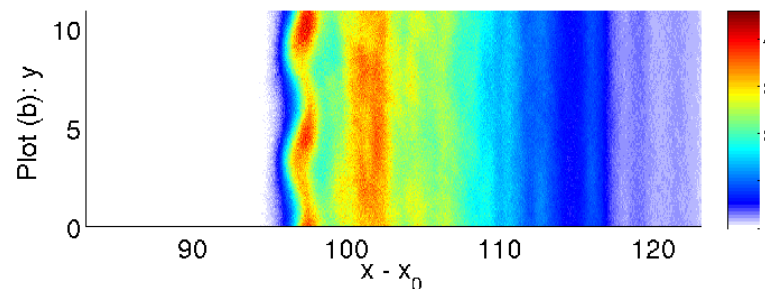
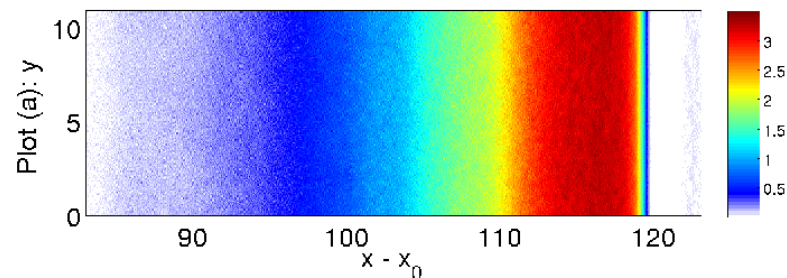
Initial contact boundary at $t = 0$: $x - x_0 = 0$. Dense slab moves to the right.
Position in units of $\lambda_e = c/\omega_p$

Filamentation instability modulates B_z : Both figures show $\log_{10}|B_z|$:

Upper plot: Strong flow-aligned magnetic field

Lower plot: No flow-aligned magnetic field

Flow-aligned magnetic field enforces planarity \Rightarrow 1D geometry

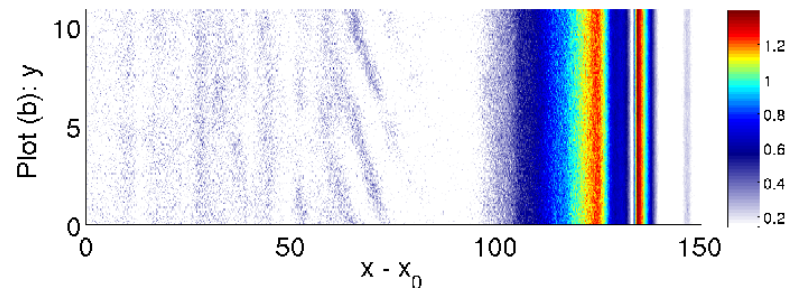
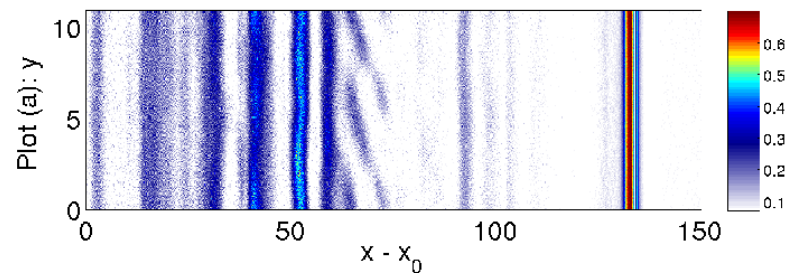


2D PIC simulation in x-y plane: Electric fields

Position in units of $\lambda_e = c/\omega_p$. Flow-aligned \mathbf{B}_0 present

Upper plot: $|E_x|$ parallel to \mathbf{v}_b : Electrostatic field

Lower plot: $|E_y + iE_z|$: Electromagnetic field

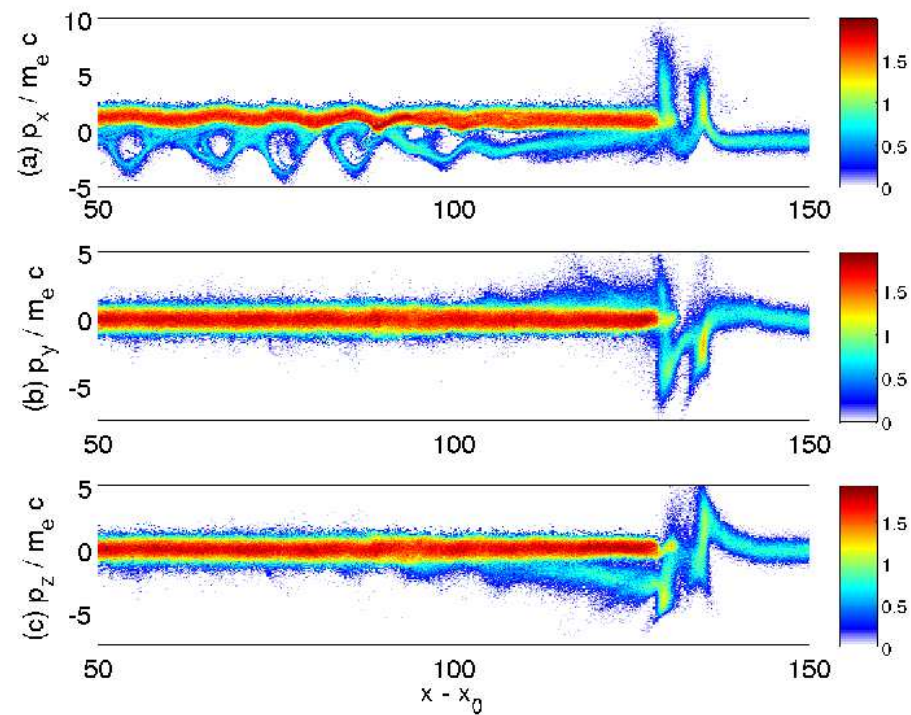


Mode at leading edge of plasma slab: Mixed polarity

Modes further downstream: Quasi-electrostatic polarity

Projected electron phase space distributions: Early time

Plasma flow along x-direction. Position is in units of $\lambda_e = c/\omega_p$

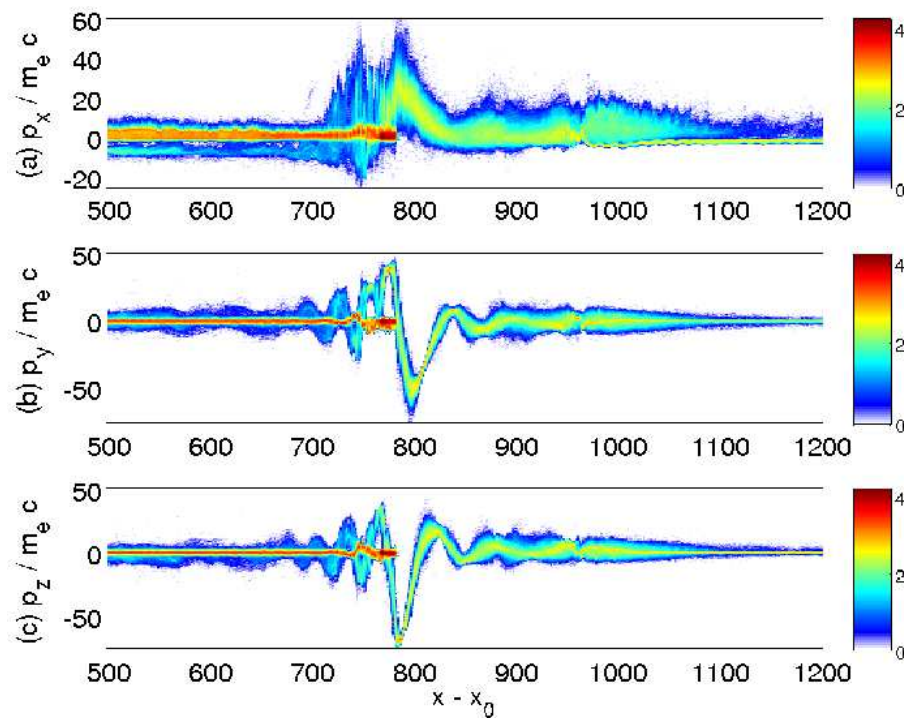


Electromagnetic structure at slab front: 3D momentum oscillation

Electrostatic structures downstream: Electron phase space holes

Projected electron phase space distributions: Later time

Plasma flow along x-direction. Position is in units of $\lambda_e = c/\omega_p$

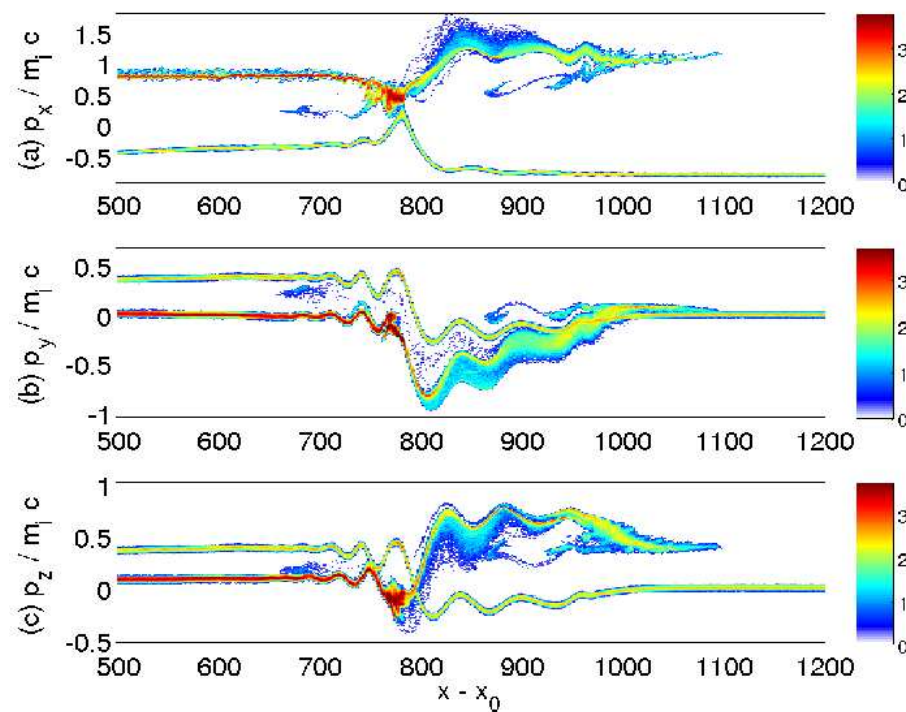


Momentum oscillations at slab front increase.

Relativistic electron mass is not small compared to the ion mass!

Projected ion phase space distributions: Later time

Plasma flow along x -direction. Position is in units of $\lambda_e = c/\omega_p$

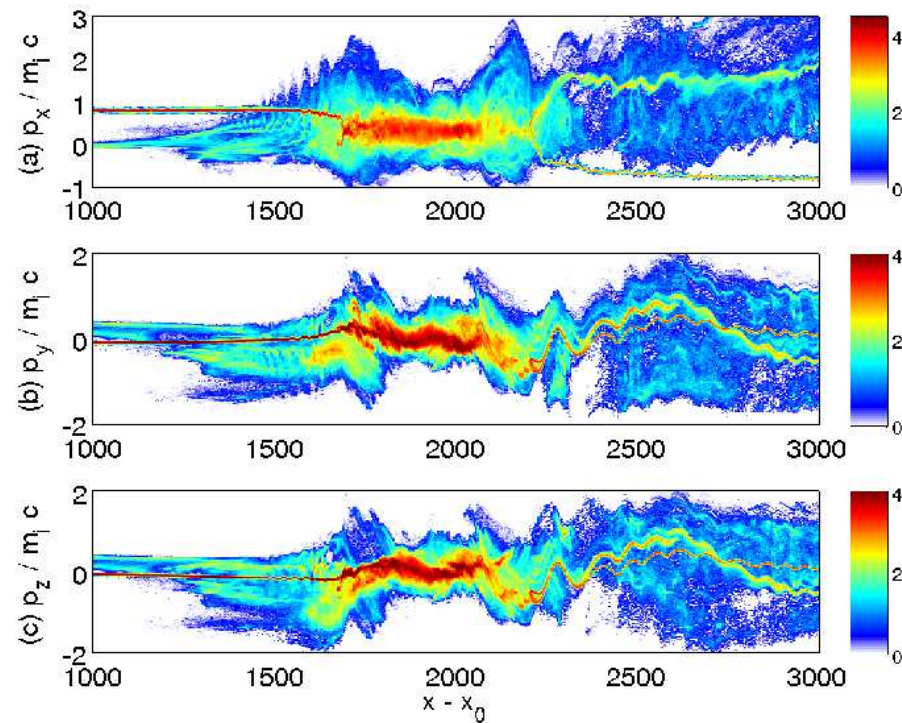


The ions of both slabs react: Strong momentum modulation at $x - x_0 = 780$

Note: Ions of dense slab with $x - x_0 > 780$ are not shock-reflected

Projected ion phase space distributions: Final time

Plasma flow along x-direction. Position is in units of $\lambda_e = c/\omega_p$



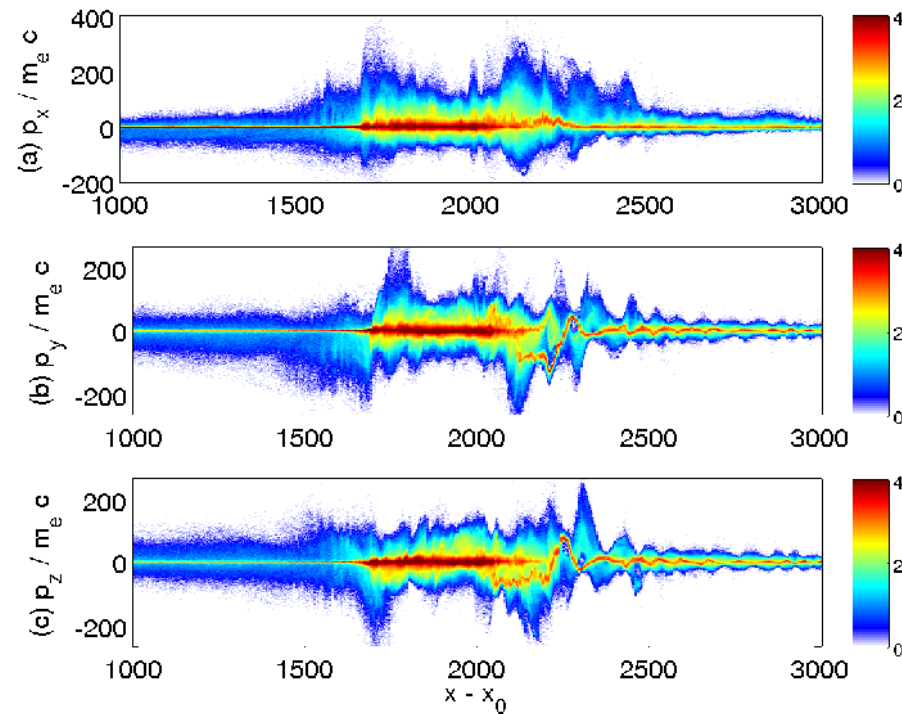
Between $1600 < x - x_0 < 2100$: forming downstream

Net flow of downstream: asymmetric forward / reverse shocks

Shock-reflected ion beam at $2300 < x - x_0$.

Projected electron phase space distributions: Final time

Plasma flow along x-direction. Position is in units of $\lambda_e = c/\omega_p$



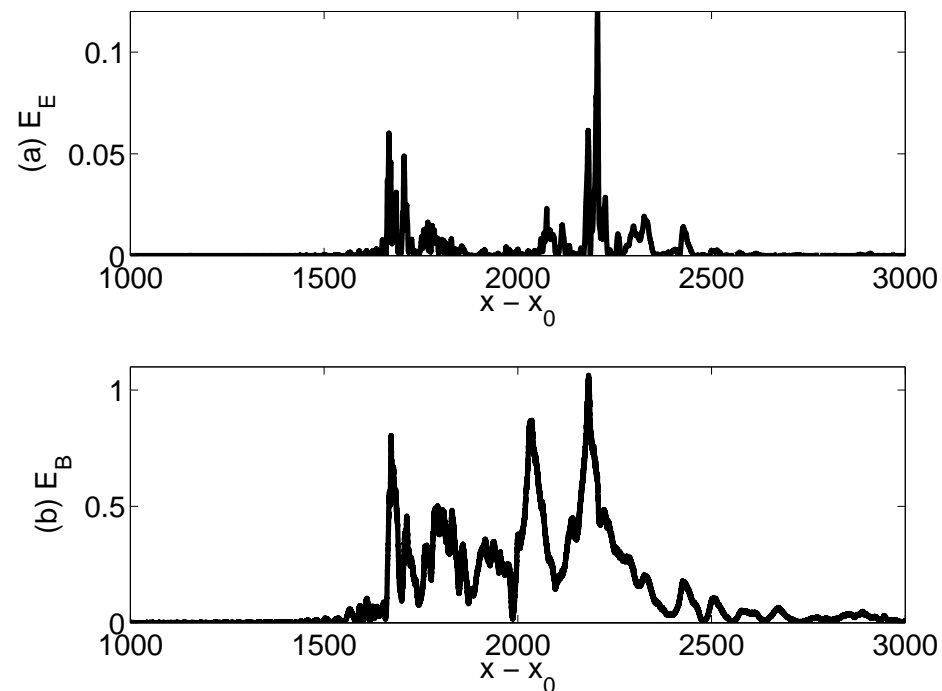
Peak electron Lorentz factor: $400 \sim m_i/m_e$

Relativistically hot electrons in 'downstream': Probably energy equi-partition between electrons and ions

Electric E_E and magnetic E_B energy densities: Final time

Position is in units of $\lambda_e = c/\omega_p$

$E_E = \epsilon_0 E^2$ and $E_B = B^2/2\mu_0$. Units: initial average plasma energy density



Energy equi-partition in downstream plasma also between plasma and **B**!

Time / energy scales in physical units:

- Simulation runtime: $\omega_p t \approx 5400$, where ω_p is plasma frequency for box-averaged electron number density $n_e \approx 130/cm^3$.

Time in physical units: 8 milliseconds

- Jet density n_e not known: However, time scales with $\sqrt{n_e}$ (robust)
- Internal shock moves in jet frame. Jet Lorentz factor $\approx 400 \Rightarrow$ Shock development in 3-4 seconds in Earth frame
- Electrons reach $\gamma \approx const m_i / m_e (?) \Rightarrow$ GeV in jet frame. *const* depends on shock collision speed.
 \Rightarrow Lorentz-boosted $\gamma \approx 1.5 \times 10^6$ or TeV energy in Earth frame.
- Size of structure in jet frame $10^3 c / \omega_p \approx 500$ km. In Earth frame 1 km.

Discussion

- A flow-aligned magnetic field can stabilize the plasma against waves with \mathbf{k} oblique or perpendicular to flow velocity vector.
Required $|\mathbf{B}|$ rises fast with $\gamma(\mathbf{v}_b)$: Only practical for internal shocks
- A weak perpendicular magnetic field triggers a powerful structure of mixed polarity, probably an oblique whistler
- The perpendicular magnetic field is amplified and it reaches an energy comparable to the mean plasma kinetic energy.
- A shock forms: Electrons and ions get accelerated / heated
- Note: During its nonlinear evolution, the shock structure may filament, which is not represented by our simulation. The plasma temperature may suppress this?!
- Assuming a Lorentz factor of 400 of a gamma-ray burst jet: Variability of electron energies on TeV and second scales in Earth frame
- Good news: Plasma instabilities can, in principle, provide the particle acceleration and magnetic field amplification required to explain the prompt gamma ray burst emissions.