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School on Pulsed Neutrons: Characterization of Materials

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Neutron Sources & Scattering Techniques (5)

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Introductory Lecture:

Basics Concepts in Neutron Scattering Techniques and Neutron Sources (5)

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Basics Concepts in Neutron Scattering Techniques and Neutron Sources

Part 5

Design Considerations for Neutron Sources

Neutron Sources for Neutron Scattering

- Neutron scattering instruments can be designed to work in continuous mode or in time of flight mode.
- There is no one instrument that can cover most of the \underline{Q} - ω space with sufficient resolution and flexibility.
- Instruments have varying requirements with respect to spectral properties and time structure.
- This is why instrument and source designers have come to interact ever more closely in conceiving new systems (not so in the early days of reactor development).



Neutron Yield of Different Nuclear Reactions

Nuclear process	Example	Neutron yield	Heat release (MeV/n)
D-T in solid target	400 keV deuterons on T in Ti	4*10 ⁻⁵ n/d	10 000
Deuteron stripping	40 MeV deuterons on liquid Li	7*10 ⁻² n/d	3 500
Nuclear photo effect from e ⁻ -bremsstrahlung	100 MeV e ⁻ on ²³⁸ U	5*10 ⁻² n/e ⁻	2 000
⁹ Be (d,n) ¹⁰ Be	15 MeV d on Be	1 n/d	1 000
⁹ Be (p,n;p,pn)	11 MeV p on Be	5*10 ⁻³ n/p	2 000
Nuclear fission	fission of ²³⁵ U by thermal neutrons	1n/fission	180
Nuclear evaporation (spallation)	800 MeV p+ on ²³⁸ U on Pb	27 n/p 17 n/p	55 30

Development of Neutron Sources ("Top of the Line")



Visualisation of the Spallation and Fission Processes



Cascade particles have energies up to the incident proton energy and can cause evaporation reactions in other nuclei

In contrast to fission, spallation cannot be self sustaining!

Fission neutrons must be moderated (slowed down to thermal energies) to cause fission in other nuclei

Neutron Spectra from Different Nuclear Reactions







- 1 Reactor core
- 2 Heavy water reflector
- 3 Reactor pool
- 4 Primary cooling system
- 5 secondary cooling system
- 6 heavy water system
- 7 Control rod drive
- 8 Heat exchanger
- 9 Primary coolant pump
- 10 Pool drain tank

Functional Principles of a Nuclear Reactor

Steady state research reactors work by consumption of thermal neutrons (moderation needed)



Reactor kinetics

Rate of change of the neutron population, if mean generation time is τ (τ is of the order of μ s!) dn (τ = 1) 1

$$\frac{dn}{dt} = n(k-1) \cdot \frac{1}{\tau},$$

Accounting for delayed neutron precursors produced at a fraction $\beta = \sum_i \beta_i$ with a mean decay constant $\overline{\lambda}$ at concentration $C = \sum_i C_i$

$$\frac{dn}{dt} = n \cdot \frac{k(1-\beta)-1}{\tau} + \overline{\lambda} \cdot C$$
$$\frac{dC}{dt} = -\overline{\lambda} \cdot C + k \cdot \beta \cdot \frac{n}{\tau}$$

Can be affected through k(t) by insertion or removal of absorbing material because $1/\overline{\lambda}$ is if the order of seconds.

 β is of the order of 0.6% in U²³⁵ and 0.2% in Pu²³⁹. This shows why a continuous reactor based U²³⁵ is easier to control than one based on Pu²³⁹, although Pu²³⁹ has a higher neutron yield per fission (2.9 vs. 2.4)

Reactor kinetics (cntd.)

Introducing

The quantity
$$\rho(t) = \frac{k(t) - 1}{k(t)} = 1 - \frac{1}{k(t)}$$
 is called "reactivity"

- the number of neutrons per fission v,

- the normalised generation time $\ell = \frac{\tau}{k}$
- the neutron production rate $P = \frac{1}{\nu} \cdot \frac{n}{\ell}$ (proportional to the reactor power)

one obtains from ρ (*t*) :

$$\frac{dP}{dt} = \frac{dn}{dt} \cdot \frac{dP}{dn} = P \cdot \frac{\rho(t) - \beta}{\ell} - \frac{\overline{\lambda} \cdot C}{\ell \cdot \nu}$$
$$\frac{dC}{dt} = -\overline{\lambda} \cdot C + \beta \cdot P \cdot \nu$$

A system is called *delayed critical* if ρ (*t*) =0; and *prompt critical* if ρ (*t*) = β

A system which exceeds prompt criticality can only be controlled in the time average \Rightarrow pulsed reactor

Pulsed operation of a fission reactor by periodic variation of ρ

Time between pulses:

$$\frac{dP_b}{dt} \stackrel{!}{=} 0$$
with $\epsilon(t) = \rho(t) - \beta$ (deviation from prompt criticality

$$P_b = \frac{\overline{\lambda} \cdot C}{|\epsilon_0| \cdot \nu}$$

- \Rightarrow Power between pulses determines neutron background
 - \rightarrow should be low
 - \rightarrow Small concentration of delayed neutron precursors and high fission yield are desirable for pulsed reactor $\Rightarrow \frac{239}{100}$ Pu is the preferred fuel

Pulsing is accomplished by sudden insertion of reactivity

- \rightarrow by moving part of the fuel (IBR-30, 30kW_{av} cooling problem)
- \rightarrow by moving parts of the reflector (IBR-2, 2MW_{av})





TRIGA-Reactors

- TRIGA reactors use a mixture of about 12 wt% of low enriched (20%) uranium in a fuel matrix of ZrH_{1.6}.
- Moderation to sustain the chain reaction thus occurs primarily in the fuel.
- Moderation becomes insufficient if the fuel temperature increases (prompt negative temperature coefficient of reactivity, aided by the Doppler effect in the ²³⁸U).
- In the case of a sudden insertion of reactivity (withdrawal of the control rod) the fuel heats up and the reactor shuts down within milliseconds.
- Although up to 10 MW average power are possible in TRIGA reactors, most of them operate in the 250 kW – 1MW regime.
- Pulsing up to 250 MW (40 ms pulses) is possible but is limited to 12 p/h.
- TRIGA reactors are useful tools for training and speciality research.

Summary on Fission Reactors

- Fission reactors are the strongest sources of thermal, cold and hot neutrons in the time average and will remain so for the foreseeable future (RHF at ILL: $\Phi_{th} = 1.5 \ 10^{15}$ at 56 MW_{th}).
- Their development has reached its limits due to heat removal problems from the fuel.
- Use of highly enriched uranium is getting increasingly difficult due to proliferation problems.
- Fission reactors are basically cw; apart from several TRIGA reactors (usually not run in a pulsed mode) only one pulsed reactor (IBR-2, 2 MW,5 Hz) is in operation for neutron scattering.
- Deployment of new fission reactors has slowed down considerably since the advent of pulsed spallation neutron sources.

Spallation Neutron Sources

Arguments used in their favour

- No criticality issues
- No actinide waste
- Proliferation safe
- Advantage by exploiting time structure
- Less heat per neutron than other nuclear processes
- High degree of design flexibility (accelerator and target system)

• But

- Demanding shielding issues
- Extra complexity by need for accelerator
- More distributed radioactivity (e.g. in cooling loops and shielding)

Principal Target-Moderator-Reflector Arrangement



The **target** should be optimised for neutron generation and coupling into the moderators

The **moderators** are designed according to users' needs for best output intensity at the desired neutron energy and time structure

The **reflector** serves to enhance the neutron output from the moderator at minimum adverse effect on time structure

The **beam tubes** are arranged such as to avoid direct view on the target to minimize high energy neutron and γ contamination

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Spallation Neutron Sources with P_b>100kW

Source and	Type of	Proton	Pulse	Aver.	Type of	Peak	Time av.	Status
location	accelerator	energy	frequency	beam	target	thermal	thermal	
		(Gev)	(Hz)	power		flux*	flux*	
				(MW)		$(cm^{-2}s^{-1})$	$(cm^{-2}s^{-1})$	
SINQ,	cyclotron	0.57	contin.	0.6	solid, Pb rods	6×10^{13}	6×10^{13}	operating
СН					liquid, PbBi	1×10^{14}	$1 10^{14}$	demonstrated
ISIS,	synchrotron	0.8	50	0.16	solid, vol.	2.3×10^{15}	$2x10^{12}$	operating
UK					cooled, Ta			
MLNSC,	linac plus	0.8	20	0.08	solid, vol.	2.3×10^{15}	1×10^{12}	operating
USA	PSR				cooled, W			
ESS,	linac plus 2	1.33	-50-	5	liquid metal	$\frac{2 \times 10^{17}}{10^{16}}$	2.5×10^{14}	deferred
EU	compressors		16 2/3		(Hg)	1x10 ¹⁰	$3x10^{14}$	
SNS,	linac plus	1	60	1,4	liquid metal	$2x10^{16}$	$8x10^{13}$	under
USA	compressor				(Hg)			commissioning
AUSRTON	synchrotron	1.6	10	0.5	solid, edge	$4x10^{16}$	$6x10^{12}$	proposed
Austria					cooled W,			
JSNS-1	synchrotron	3	25	1	liquid metal	1×10^{16}	$8x10^{12}$	under
Japan					(Hg)			commissioning
JSNS-2	2-ring	3	50	5	liquid metal	$2x10^{17}$	2.5×10^{14}	proposed
Japan	synchrotron				(Hg)			
MMF	linac	0.6		0.6	solid, vol.			commissioning
RUS	(plus comp)				cooled W			(low power)

* typical maximum values; precise figures vary, depending on type of moderator

Spallation Neutron Sources – General Aspects (1)



lead targets

different energy groups for a 20 cm diameter lead target bombarded by protons of 2 GeV

Choice of proton energy



Arguments for higher proton energy:

Easier to accelerate to higher energy than to increase current (in particular with circular accelerators)

Radiation damage in target and window materials scales roughly with number of protons, not with beam power



Primary Neutron Spectra and Moderation by H



Spallation Neutron Sources – General Aspects (4)

High Energy Neutron Shielding

Dose at angular position θ relative to the beam subtending a solid angle Ω to the source with different shielding materials of attenuation lengths λ_i

 $D(\theta) = \Omega \int dE \{ \Phi(E,\theta)^* F(E)^* B(E) \Pi_i [exp(-s_i/\lambda_i)],$

- $\Phi(\mathsf{E}, \theta)$ source particle spectrum in direction Ω
- F(E) flux-to-dose conversion factor
- B(E) buildup factor
- $\begin{aligned} \Pi_i \left[exp(-s_i/\lambda_i) \right] & \text{dose reduction by} \\ & \text{stretches } s_i \text{ of different materials} \\ & \text{with attenuation lengths } \lambda_i \,. \end{aligned}$

Bottom line:

Higher proton energy gives increased neutron yield <u>per proton</u>, but adds to shielding problems (accelerator issue)



Accelerator Drivers for Neutron Sources

- **Synchrotron plus linac**: good solution to obtain high energy at relatively low cost; yields short pulses naturally; intensity limited by injection energy; rep-rate limited (60 Hz), but not a problem.
- Compressor ring plus linac: allows high intensity due to full energy injection; cost relatively high; might run at higher rep-rate (multiple target stations).
- Linac alone: long pulse or cw; high power possible; high cost
- **Cyclotron**: essentially cw; good performance record; cascade may be required for high energy; av. current up to 2 mA demonstrated; 5-10 mA deemed possible; comparatively low cost.
- **FFAG** (Fixed Field Alternating Gradient Synchrotron): often proposed, now under development at KEK; short pulses; high rep-rate (400 Hz) possible; rep-rate reduction by pulse stacking (?); cost comparable to cyclotron (?)
 - \Rightarrow Hope for the future

Neutron Moderation (1)

- Moderation of neutrons occurs by collisions with moderator atoms
- In each collision a constant fraction of the energy is lost
- "Logarithmic energy decrement":

$$\xi = InE_1 - InE_2 \begin{cases} = 1 \text{ for } A = 1 \\ \approx 2/(A+2/3) \text{ for } A > 1 \end{cases}$$
 A is the atomic number of the moderator atom

- Number of collisions x required to slow down from energy E_0 to E_f

 $x = 1/\xi^* ln(E_0/E_f)$ for $= E_0 2MeV$ and $E_f = 1 eV$: $x = 14.5/\xi$

Parameter	Element						
	H	D	Be	С	0	Hg	Pb
A	1	2	9,01	12,01	16	200,6	207,19
$\sigma_{\rm fr}~(10^{-24}~{ m cm^2})$	20,51	3,40	6,18	4,73	3,75	26,53	11,01
ρ (g/cm³) ^(*)	0,07	0,163	1,85	2,3	1,13	13,55	11,3
$\Sigma_{\rm fr} = N^* \sigma_{\rm fr} \ (\rm cm^{-1})$	0,86	0,17	0,76	0,55	0,16	1,08	0,36
۳	1,000	0,725	0,206	0,158	0,120	0,010	0,010
x (2MeV→1eV)	, 14,5	20,0	70,3	92,0	121,0	1460,1	1507,9

Neutron Moderation (2)



The time t_i between collisions and therefore the number of neutrons present in a certain velocity interval is inversely proportional to the neutron velocity, v_i .

 $t_i = \Lambda/v_i = 1/(\Sigma_{fr} * v_i)$ or $t_i * v_i = \Lambda \approx \text{const}$ in the slowing down regime (>1eV)

This means that, in the slowing down regime the spectral neutron flux I(E), which is the *product of the neutron density and their velocity*, is proportional to v² or :

The slowing down process (cntd.)

In small moderators, where losses during slowing down are significant, or if absorption plays a role, one obtains

 $<I(E)_{sd}> = I(E_0)^*(E_0/E)^{(1-\alpha)} = [E^*I(E)]_{Eo}^*(1/E)^*(E/E_0)^{\alpha}$

 E_0 is a reference energy (usually 1eV) and α depends on absorption in and leakage from the moderator during the slowing-down process. For non-reflected moderators α is of the order of 0.2, but can be significantly affected, by a *reflector.*

In a large moderator, a "Maxwellian" flux distribution develops when thermal energies are reached, which depends on the moderator temperature:

 $\Phi(\mathsf{E})_{\mathsf{M}} = \Phi_{\mathsf{th}} \, \mathsf{E}/(\mathsf{k}_{\mathsf{B}}\mathsf{T}_{\mathsf{eff}})^2 \exp\left(-\mathsf{E}/(\mathsf{k}_{\mathsf{B}}\mathsf{T}_{\mathsf{eff}})\right)$

 $\Phi_{\rm th}$ is the thermal neutron flux integral

 $k_{\rm B} = 0,08866165 \text{ meV/K}$ is Boltzman's constant

 T_{eff} is the effective moderator temperature, which is somewhat higher than the physical temperature

the physical temperature

Neutron Moderation (4)

Thermalisation

The transition between the slowing-down regime and the thermal equilibrium spectrum at about $5kT_{eff}$ is usually taken into account by a switch function $\Delta_1(E)$, by which the slowing down spectrum is multiplied. A frequently used formula is $\Delta_1 = 1/(1+5 k_B T_{eff})^5$

The full representation of the spectrum, then reads:



Neutron Moderation (5)

Characterisation of moderators

The slowing down power

 $\zeta^*\Sigma_{s}$

determines the rate (distance) at which neutrons are slowed down in a moderator.

The moderating ratio $\zeta^* \Sigma_s / \Sigma_a$ is a measure for the thermal neutron flux integral relative to the flux at one eV

 Σ_{a} is the mean macroscopic absorption cross section

Moderator	Density (g/cm ³)	ζ*Σ _s (cm⁻¹)	$\zeta^* \Sigma_s / \Sigma_a$
H ₂ O	1.00	1.35	71
D ₂ O (pure)	1.10	0.176	5670
D ₂ O (99.8%)	1.10	0.178	2540
Graphite	1.6	0.060	192
Beryllium	1.83	0.158	143

For a mixture of N nuclei:

$$\overline{\zeta} = (1/\Sigma_{s}) \sum_{i=1}^{i=N} \Sigma_{s,i} \zeta_{i}$$

Neutron Moderation (6)

Slowing down of a neutron pulse

Since, in the slowing down regime (>0.5 eV for room temperature moderators) $t_i = \Lambda/v_i = 1/(\Sigma_{fr}v_i)$ or $t_i v_i = \Lambda \approx \text{const}$ The time it takes to slow a neutron down to the velocity v is essentially determined by the processes near that velocity

$$\begin{array}{lll} \mbox{Time to slow down to v: } v^*t_s = (1+2/\gamma)^*\gamma/(\xi^*\Sigma_{fr}) & = 1 & \mbox{for } A=1 \\ \mbox{Standard deviation: } v^*\Delta t_s = (1+2/\gamma)^{1/2}\gamma/(\xi^*\Sigma_{fr}) & \mbox{with } \gamma & = 1 & \mbox{for } A=1 \\ \mbox{FWHM: } v^*\Delta t_{1/2} = 3/(\xi^*\Sigma_{fr}) & \mbox{with } \gamma & \approx 4/(3A) & \mbox{for } A>1. \end{array}$$

Material	Density	\sum_{s} (cm ⁻¹)	ξ	γ	$v \cdot t_s$ (cm)	$v \cdot \Delta t_s$ (cm)	$v \cdot t_{1/2}$ (cm)
H ₂ O	1	1.5	0.92	0.99	2.17	1.25	2.4
CH ₄	0.94	1.8	0.9	0.98	1.84	1.05	2.0
D_2O	1.1	0.35	0.51	0.56	14.3	6.71	14.2
Be	1.7	0.75	0.21	0.15	13.6	3.61	7.9
C	1.8	0.43	0.16	0.11	30.7	7.0	16.0
Fe	7.9	0.75	0.035	0.024	77.1	8.4	19.2
H ₂ (liqu)	0.07	0.86	1.0	1.0	3.47	1.05	2.16

Neutron Moderation (6)

Slowing down of a neutron pulse (cntd.)

As the neutrons approach thermal equilibrium with the moderator the pulse can be analysed in terms a slowing down and a storage component



The life time of the storage component can be strongly affected by poisoning the moderator and by decoupling it from the reflector



Neutron Moderation (7)

Cold Moderators



Lowering the temperature of a moderator shifts the Maxwellian to lower energies.

This also extends the regime of naturally narrow lines to lower energies

Problems with solid methane:

- difficult to cool
- decomposition by radiation
- spontaneous release of stored energy

Studies for the ISIS-TS2 Moderator System



Neutron Moderation (8)



Short Pulse Neutron Source



Short Pulse-ToF-Technique



Short vs. Long Pulse Operation

Example: bypass ESS compressors



Simply omitting the compressor ring and associated pulse chopping necessary for injection into the ring would result in a 1.2ms long pulse of 10% of the peak intensity of the short pulse source

A higher flux level in the LP moderator (perhaps up to 2x) can be obtained by an optimised design

Long Pulse Neutron Source



Utilisation of Long Pulse Sources

- The most straight forward use of an LPSS is to employ instruments similar to a cw source but gate the detectors to allow data collection only when the "good" neutrons arrive. While using the full time average flux this reduces the background by orders of magnitude.
- More elaborate concepts to use an LPSS exist but in general require advanced and expensive instrument infrastructure
 - multiple chopper systems (ca 1 M\$/beam line)
 - complex neutron guide systems
 - in-shield neutron optics
 - etc.
- LPSS-beam lines will generally be longer than on SPSS
- The need for beam line shielding is generally higher on LPSS instruments
- The peak flux used is lower than on SPSS

Utilisation of Long Pulse Sources

Pulse Shaping by Choppers on a Long Pulse Source





Multiple Wavelengths from a coupled moderator of a pulsed source



Summary on Spallation Neutron Sources

- There exists a very high degree of flexibility in the design and use of spallation neutron sources.
- Choices will often depend on existing boundary conditions; even small facilities have been shown to perform very well.
- Currently the available technology allows to build spallation neutron sources up to a few MW of beam power, which makes it possible to match modern research reactors also in time average flux.
- By properly exploiting the time structure of pulsed sources much better use can be made of the primary neutrons produced than on cw sources.
- Probably there is no clear answer as to which time structure is to be preferred at a given time average power.
- Often, however, the very high efficiency of instruments on pulsed sources is due to the use of very large detector banks.
- The field of source and instrument development is still wide open!

Basics Concepts in Neutron Scattering Techniques and Neutron Sources

That's it! Thank you for your patience!