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School on Pulsed Neutrons: Characterization of Materials

15 - 26 October 2007

Surfaces and Thin Films

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Surfaces and Thin Films

23. October 2005 Hartmut Zabel Ruhr University Bochum, Germany

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Surfaces, Interfaces and Thin Films For fundamental properties in the area of magneto- and spintronics









- 1. X-ray reflectivity
- 2. Neutron reflectivity
- 3. Polarized neutron reflectivity (PNR)
- Methods
- Instrumentation
- Examples
- 4. Case study: do we still need neutrons?





1. X-ray and neutron reflectivity







Index of refraction for EM waves



 $\sqrt{\epsilon(\omega)} = n(\omega) =$ fractive index \Rightarrow optics





X-ray refractive index

Refractive Index:

$$n^{2}(\omega) = 1 + \frac{4\pi\rho_{A}e^{2}}{m_{e}}\sum_{i}\frac{f_{i}}{\omega_{i}^{2} - \omega^{2} + i\gamma}$$

For x-ray's, the refractive index is always smaller than 1:

$$n(\lambda) = 1 - \frac{r_0}{2\pi} \rho_e \lambda^2$$
$$\approx 1 - 10^{-5} < 1$$

Adding dispersion and absorption correction:





Plot of δ and β for CoO





http://www-cxro.lbl.gov/optical_constants/getdb2.html 7



Critical angle for total reflection

Since n < 1, total reflection occurs at:

$$\frac{\cos\alpha_c}{\cos0} = \cos\alpha_c = n$$

For all angles $\alpha < \alpha_c$ the wave can not penetrate into the medium, but at α_c there is an evanescent wave travelling along the interface







Critical Scattering Vector

Scattering vector is defined as:

$$Q = \frac{4\pi}{\lambda} \sin \alpha = 2k \sin \alpha$$

Accordingly the critical scattering vector is:

The critical scattering vector is no more a function of the wavelength. It is entirely determined by the property of the material and in particular by the electron density ρ_{e} .





Fresnel reflectivity

For
$$Q_z < Q_c$$
: R = 1,
For $Q_z > Q_c$: R = R_f

The reflectivity drops with Q⁴, for scattering vectors Q >> Q_c . This applies for perfectly flat interfaces.







Fresnel reflectivity for Si





http://sergey.gmca.aps.anl.gov/



Reflectivity from a thin layer: Kiessig fringes







Reflectivity from a double layer









Reflectivity from a multilayer







Reflectivity and Bragg range







Electron density profile from reflectivity data





Back transformation from reflectivity data to electron densities and thickness profiles is the ultimate goal. However, the back transformation is not always uniquely possible.





Reflectivity with surface roughness







Smooth and rough surfaces







Off-specular scattering from rough interfaces



Perfectly specluar surface, 100% reflection, mirror image



Perfectly rough surface, 100% diffuse scattering, projector wall



Partially reflecting and scattering from rough surface





Reflectivity of rough surface

Master formular yields for a Gaussian roughness a damped Fresnel reflectivity:

$$R(Q_z) = R_F(Q_z) \exp(-Q_z^2 \sigma^2)$$

 $R_F(Q_z)$ is the Fresnel reflectivity of the ideal surface. Roughness adds a damping factor, similar to the Debye-Waller factor:







Diffuse Scattering

Scattering function in the Born approximation:

$$S(\vec{Q}) = \int \langle \rho(0)\rho(R) \rangle e^{i\vec{Q} \cdot \vec{R}} d^3R$$

Pair correlation function:

$$G(\vec{R}) = \left\langle \left(\rho(0) - \left\langle \rho(0) \right\rangle \right) \left(\rho(\vec{R}) - \left\langle \rho(\vec{R}) \right\rangle \right) \right\rangle$$
$$= \left\langle \rho(0) \rho(\vec{R}) \right\rangle - \left\langle \rho(0) \right\rangle \left\langle \rho(\vec{R}) \right\rangle$$
$$= \left\langle \rho(0) \rho(\vec{R}) \right\rangle - \left\langle \rho(0) \right\rangle^{2}$$

Inserting:

$$S_{tot}(\vec{Q}) = \langle \rho(0) \rangle^2 \int e^{i\vec{Q} \cdot \vec{R}} d^3 R + \int C(\vec{R}) e^{i\vec{Q} \cdot \vec{R}} d^3 R$$

Specular Reflection Diffuse Scattering
$$= S_{spec}(\vec{Q}) + S_{diff}(\vec{Q})$$





Height-height correlation function



Height-height correlation function for a single self-affine, fractal surface:

$$C(R) = \langle z(0)z(R) \rangle = \sigma^2 \exp[-(R / \xi)]^{2h}$$

 $\sigma = \text{rms roughness}$ $\xi = \text{cut-off length:}$ for R > ξ , interface appears smooth, for R < ξ , interface appears rough, fractal behavior $S_{diff}(\vec{Q}) = \frac{\exp(-Q_z^2 \sigma^2)}{Q_z^2} \times \int [\exp(Q_z^2 C(R)) - 1] \exp(iQ_{\parallel}R) d^2R$

S.K. Sinha, E.B. Sirota, S. Garoff, and H.B. Stanley, Phys. Rev. B 38 2297 (1988³²)



Specular and off-specular scattering





J. Als-Nielsen and Des McMorrow, Wiley, 2001



Transverse scans

Transverse scan from an FePt film on GaAs





A. Nefedov et al. J. Phys.: Condens. Matter 14, 12273 (2002)





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Refractive index for neutrons

Snell's law for specular reflection:



$$n = \frac{\sin \gamma_0}{\sin \gamma_t} = \frac{\left|\vec{k}_t\right|}{\left|\vec{k}_i\right|}$$

QM potential step for the z-component of the kinetic energy:







Combining both

$$n^{2} = \frac{\sin^{2} \gamma_{0}}{\sin^{2} \gamma_{t}} = \frac{\left|\vec{k}_{t}\right|^{2}}{\left|\vec{k}_{i}\right|^{2}} = \frac{E_{t}}{E_{i}} = \frac{E_{i} - V_{n}}{E_{i}} = 1 - \frac{4\pi}{k_{i}^{2}} N_{A} b_{coh}$$

 N_A = nuclei number density b_{coh} = coherent scattering length of nuclei A Notice that n ≤ 1, only for $b_{coh} \ge 0$ Total reflection only for $b_{coh} \ge 0$

$$Q_{c} = \frac{4\pi}{\lambda} \sin \alpha_{c} = \sqrt{4k^{2}(1-n^{2})} = \sqrt{16\pi N_{A}b_{coh}}$$
$$Q_{c} \propto \sqrt{N_{A}b_{coh}}$$





Example: Neutron reflectivity from a non-magnetic, infinite thick and flat sample



For $Q_z < Q_c$: R = 1, only for b >0, i.e. for coherent scattering length.





Neutron Reflectivity



Film thickness
Interface roughness
Density profiles







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Polarized Neutron Reflectivity: The four cross-sections







Quantum mechanical description of the scattering process

1D optical potential:

$$V = \frac{2\pi\hbar^2}{\underbrace{m}_{\text{nuclear part}}} N_A b - \underbrace{\vec{\mu} \cdot \vec{B}}_{\text{magnetic part}}$$

Schrödinger equation:

$$\left[-\frac{\hbar^2}{2m}\nabla^2+V\right]\Psi(z)=E\Psi(z)$$

N_A: atomic number density

b: coherent neutron scattering length

$\vec{\mu}$: neutron magnetic momentum

$\vec{\mu} = \gamma \mu_N \boldsymbol{\hat{\sigma}}$

 μ_{N} : nuclear magneton

- γ = -1.913: gyromagnetic ratio
- $\hat{\sigma}$: Pauli spin operator

$$\sigma_{\perp} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}; \quad \sigma_{\parallel} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}; \quad \sigma_{z} = \begin{pmatrix} 0 & -\mathbf{i} \\ \mathbf{i} & 0 \end{pmatrix}$$





Polarized Reflectivity



r₊: reflection amplitudes





Reflectivity and Asymmetry

$$R^{+} = R^{++} + R^{+-}$$

$$R^{-} = R^{--} + R^{-+}$$

$$R^{+} - R^{-} = R^{++} - R^{--}$$

$$R^{+} + R^{-} = R^{++} + R^{--} + R^{+-} + R^{-+}$$

• Spin Asymmetry

$$SA = \frac{R^{+} - R^{-}}{R^{+} + R^{-}} = \frac{R^{++} - R^{--}}{R^{++} + R^{--} + R^{+-} + R^{-+}}$$





Reflectivity and Asymmetry of single Fe - layer

1.6x10 **Reflectivities:** 1.2x10SLD [A SLD + 8.0x10 SLD -0.1 4.0x10 Reflectivity 1E-3 R^+ and R^- 600 800 1000 1200 400 z [Å] 1E-4 fit to R + fit to R -1E-5 1.0 Spin Asymmetry : 0.8 Spin Asymmetry 0.6 - $SA = \frac{R^+ - R^-}{R^+ + R^-}$ 0.4 0.2 --0.2 -SA • Fit to SA -0.4 0.02 0.04 0.06 0.08 0.10





0.12

Q [Å ⁻¹]


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Instrumention: two types

- Angle dispersive
- monochromatic beam
- scanning of $\boldsymbol{\theta}$
- Wavelength dispersive
- White beam
- TOF method,
- fixed $\boldsymbol{\theta}$









Polarizer, analyzer, spin flipper







Schematics: neutron reflectometer with complete polarization analysis



This part is identical for angle dispersive and wavelength dispersive instruments





³He Spin-Filter for the spin analysis of diffuse scattering



³He spin-filter technique is very useful for the polarization analysis of offspecular scattering. Compared to solid-state analyzer, the spin-filter covers a wider angular range and is free of small angle scattering.





The ADAM Reflectometer at the ILL







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Nuclear and magnetic density profile in (GaMn)As



B.J. Kirby et al. Phys. Rev. B 69 (2004) 081307





PNR from model-spinstructures in magnetic multilayers



AF case: NR of Fe(2ML)/V(13ML)above and below $T_N = 100K$



Antiferromagnetic coupling below the Néel temperature Intensity = M^2



V. Leiner, K. Westerholt, A. M. Blixt, H. Zabel and B. Hjörvarsson: Physical Review Letters, **91**, 037202 (2003)



Three steps to FM sample analysis

1. Align sample with easy axis parallel to Y-axis

2. Go to saturation and then back to remanence

3. Rotate sample in remanence by 90°. Now the NSF reflectivity is only nuclear, and the SF reflectivity is only magnetic.







Nuclear and magnetic density profiles have the same periodicity but different shape.

M. Vadala, K. Zhernenkov, M. Wolff, H. Zabel, August 2006, ADAM reflectometer





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Transverse reflectivity

Transverse scan







Types of magnetic roughness







Domain size: 1 μm (´<< L_)





Simulations from B.P. Toperberg



Single ferromagnetic film in the domain state



G

F. Radu et al. J. Phys.: Condens. Matter 17 (2005) 1711



Magnetic roughness in Co/Cu superlattices



- $1\!\!\!/_2$ order AF peak, only diffuse peak \Rightarrow small domain size
- weak out-of-plane correlation, gradient in periodicity





Transverse scans across half-order AF peak



$$S_{Diff}(Q) = DW \int d^2 \vec{r} e^{i\vec{Q}_{\parallel}\cdot\vec{r}} \left[s + m + sm\right]$$

s = structural roughness m =domain distribution roughness sm =cross term contains magnetic roughness

Diffuse scattering due to:

- domain size distribution
- orientational domain distribution
- Lorentzian profile changes into Gaussian profile with increasing domain size
- Diffuse scattering diminishes in high fields





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PNR from patterned films





Courtesy K. Theis-Bröhl, Bochum



PNR from patterned films: domains



α_i (deg)

Non-spin-flip channels

R⁺⁺ Simulation: R⁻⁻

1.5







Courtesy K. Theis-Bröhl, Bochum



PNR from patterned films: domains



R+-

Spin-flip channels

Simulation: R-+









Reciprocal space map from a stripe array



Simulation:





K. Theis-Bröhl, et al. Phys. Rev. B 68, 184415 (2003).



Magnetization reversal parallel to stripes



Average hysteresis and quantitative determination of fluctuations





K. Theis-Bröhl, et al. Phys. Rev. B 71, 020403(R) (2005).



Laterally structured Fe/Cr multilayer

• Fe stripes on AF-Fe/Cr ML Λ =1 µm Ziegenhagen et al., Physica B 335 (2003) 50





- Maps:
- specular PNR
 - (half- and full-order peaks)
- off-specular diffuse scattering
- Bragg sheets
- first-order lateral Bragg diffraction

Measurements @ FRJ2, HADAS





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Analytical tools

- Magneto-optic Kerr effect (MOKE): Vector – magnetometry
- Polarized neutron reflectivity (PNR): Vector – magnetometry
 + depth resolution
- X-ray resonant magnetic scattering (XRMS):
 - Vector magnetometry
 - + depth resolution
 - + element selectivity
 - + time resolution





Longitudinal vector - MOKE





Kerr angle
$$\theta_{K}^{x} \sim m_{x} = \left| \vec{m} \right| \cos \chi$$

 $\theta_{K}^{y} \sim m_{y} = \left| \vec{m} \right| \sin \chi$









$$\frac{m_x}{m_y} = \frac{\cos \chi}{\sin \chi} = \frac{\theta_K^x}{\theta_K^y}$$
$$\chi = \operatorname{arc} \operatorname{cot} \left(\frac{\theta_K^x}{\theta_K^y} \right)$$
$$\frac{\left| \vec{M} \right|}{\left| \vec{m} \right|_{x,sat}} = \frac{\theta_K^x}{\theta_K^{x,sat}} \frac{1}{\cos \chi}$$





Two limiting cases









Magnetization reversal of a stripe array



MCD for ferromagnetic metals







MCD for ferromagnetic metals

Transmission

Absorption for right circular polarisation

Difference signal, MCD

Energy A_2 A_3 σ_{tot} =r

Total absorption, σ_{tot}





Spin and orbital moments from sum rules






From absorption to reflection



X-ray magnetic scattering (XRMS)

$$f = \left(\mathbf{e}_{f}^{*} \cdot \mathbf{e}_{i} \right) \left\{ -r_{e}Z + \frac{3}{8\pi} \lambda \left[F_{1}^{1} + F_{-1}^{1} \right] \right\}$$

Charge scattering (non-resonant and resonant)

$$+ i \left(\mathbf{e}_{f}^{*} \times \mathbf{e}_{i} \right) \cdot \hat{\mathbf{m}} \frac{3}{8\pi} \lambda \left[F_{1}^{1} - F_{-1}^{1} \right]$$

$$1^{\text{st}} \text{ order in } \mathbf{M} \to \text{Circular Dichroism}$$

$$+ \left(\mathbf{e}_{f}^{*} \cdot \hat{\mathbf{m}} \right) \left(\mathbf{e}_{i}^{*} \cdot \hat{\mathbf{m}} \right) \frac{3}{8\pi} \lambda \left[2F_{0}^{1} - F_{1}^{1} - F_{-1}^{1} \right]$$

$$2^{\text{nd}} \text{ order in } \mathbf{M} \to \text{Linear Dichroism}$$

Resonant magnetic scattering





Fe/Cr superlattices: resonant magnetic scattering





A.Nefedov, J. Grabis, A. Bergmann, F. Radu and H. Zabel, Superlattices and Microstructures, **37**, 99 (2005)



Fe/Cr superlattices: hysteresis







Element specific reflectivities and hysteresis of EB system

CoO 2.5nm Fe 15 nm Al₂O₃

XRMS after field cooling in H_{FC} = + 2 kOe at 30 K



Hystereses

F. Radu, et al. JMMM 300 (2006) 206





Time scales in magnetic materials



Time resolved reversal XRMS



Time domain: pump probe technique







Precessional dynamics of elemental moments in a ferromagnetic alloy





W. E. Bailey et al. PRB 70 (2004) 172403



Summary: uses of PNR

- Layer resolved magnetization vector
- •Magnetization profile independent of structural/chemical profile
- •Absolute moment evaluation not obscured by substrate effects
- Distinction between different types of magnetization reversal
- •High field measurements
- •Domain distribution, domain sizes, domain walls
- •Ferro- and antiferromagnetic structures
- •Non-collinear magnetism
- Magnetic correlation lengths





Topics for PNR studies

- Quantitative vector magnetometry
- Domain configurations
- Interactions between elements
- Details of remagnetization
 - domain nucleation/ wall movement
 - vs. rotation











Literature

- *T. Brückel, E. Kenzinger*, "Streumethoden zur Untersuchung von "Dünnschichtsystemen", in Vorlesungsmanuskripte des 30. Ferienkurses des Instituts für Festkörperforschung Jülich, 1999.
- *C. Fermon, F. Ott, A. Menelle*, "Neutron Reflectometry" in X-Ray and Neutron Reflectivity: Prinziples and Applications, J. Daillant, A. Gibaud (Eds.), Lecture Notes in Physics, Springer, 1999.
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- *M.R. Fitzsimmons et al.* J. Magn. Magn. Mater. **271**, 103 (2004)
- H. Zabel and K. Theis-Bröhl, J. Phys.: Condens. Matter 15, S505 (2003)
- *H. Zabel*, Materials Today, **8** (2006) 42





Advantages and disadvantages: XRMS

- High flux and large q
- Element specific
- Distinguish L and S
- Cross sections not known
- Indirect probe of the magnetisation
- Measure interference term between charge and magnetism
- Time resolved experiments
- Penetration depth









