



The Abdus Salam
International Centre for Theoretical Physics



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**Advanced School on Synchrotron and Free Electron Laser Sources
and their Multidisciplinary Applications**

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**Ultrafast VUV and soft X-ray pulses
(production by harmonic generation and
features)**

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Ultrafast VUV and soft X-ray pulses

(production by harmonic generation and features)

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Synchrotron Radiation 2008

OUTLINE

Introduction

Some basics

HG in crystals : where do we stop

Low-order HG in Gases

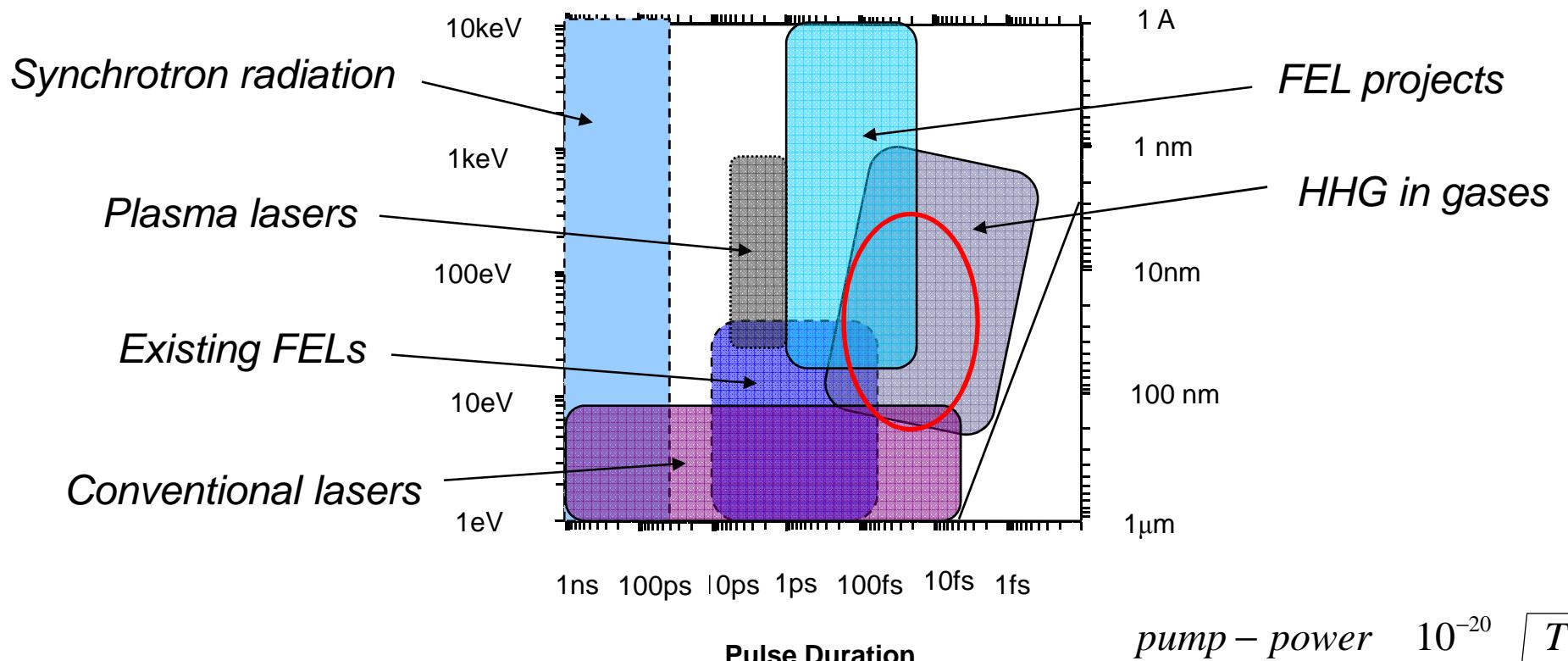
High order HG in Gases (HHG)

Trends in HHG

Features of the HHG light

INTRODUCTION

Main sources of laser-like beams/pulses in the 180-3 nm range



$$\frac{\text{pump-power}}{m^3} \sim \frac{10^{-20}}{\lambda^4 L} \sqrt{\frac{T}{Mn}}$$

Harmonic generation



Regimes:

1. Peak power density from 10^3 to 10^{13} W/cm² - **weak perturbation limit**

Nonlinear polarisation :

$$\vec{P} = \epsilon_0 (\chi^{(1)} \vec{E} + \chi^{(2)} \vec{E}^2 + \chi^{(3)} \vec{E}^3 + \dots)$$

Phase matching:

$$n\mathbf{k}_\omega = \mathbf{k}_{n\omega}$$

In NL crystals :

- PM by birefringence
- $\chi^{(2)} \sim 10^{-12}$ m/V

efficiency of SHG (2ω)~50% , THG(3ω)~20%,... FHG(5ω)~1%

Limits:

- transparency region : 6.9 eV BBO, ~8eV KBBF , ~10eV SBBO
- No phase matching for SHG , mixing with longer wavelengths

Shortest wavelengths: 157 nm , FHG of Ti: sapphire in KBBF (1)

130 nm , SHG (not in PM!) in SBBO

Low-order HG in gases

Features:

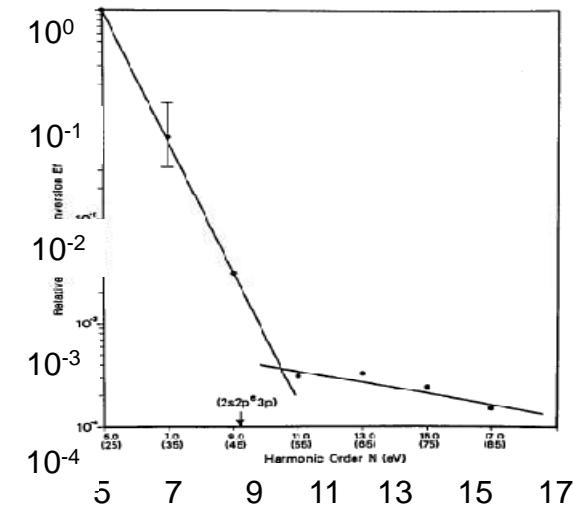
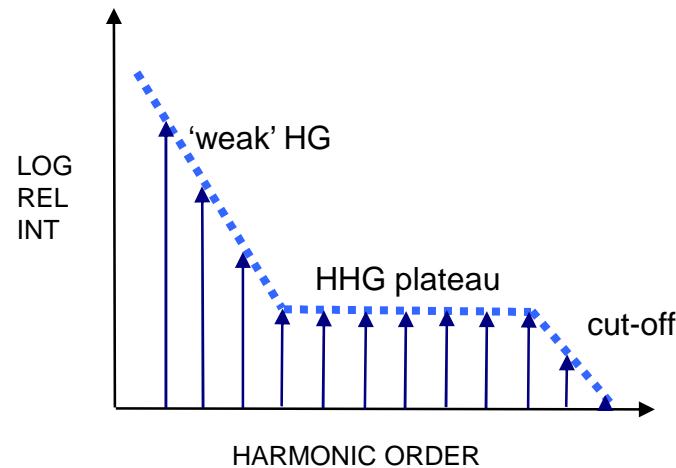
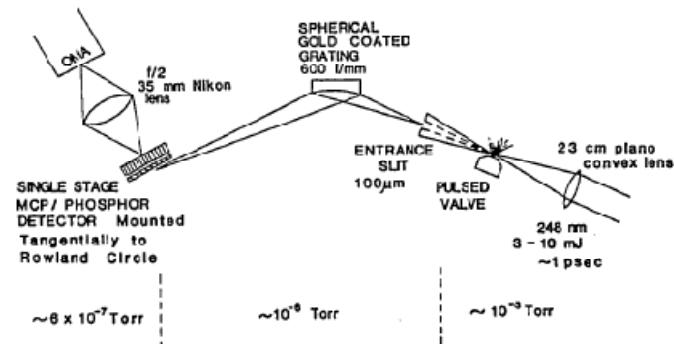
- Odd harmonics only
- Transmission in the VUV-EUV
- Low nonlinear susceptibility

$$\eta = \frac{P_3}{P_1} = \frac{3\pi^2}{\epsilon_0^2 c^2 \lambda_1^4} N^2 [\chi_{\lambda_3}^{(3)}]^2 P_1^2 |\Phi|^2 \quad (\text{in SI units})$$

- Regions where $\Delta k \sim 0$ (or small enough) can be found by adjusting gas mixture and focusing conditions
- Feasible for THG in the EUV starting with laser wavelength in the deep UV Excimer or Third harmonic YAG : 3% efficiency in generating 118.2 nm (10.5 eV) in gas cell with mixture Xe:Ar;
Tunable source (Nd:YAG harmonic+dye) for tunable THG in gas jets
 - > 10^{-4} efficiency in generating 70- 100 nm ($\sim 18 - 10$ eV)
 - > Could be used down to 63 nm (~ 20 eV) by use of Ti:sapphire harmonics in BBO as a source to generate $\sim 1 \mu\text{J}$ per pulse (2 to 5×10^{11} ph/pulse)

HHG in gases

- At very high intensities ($>10^{14} \text{ W/cm}^2$)
- the weak perturbation limit breaks ->plateau in the harmonic conversion efficiency



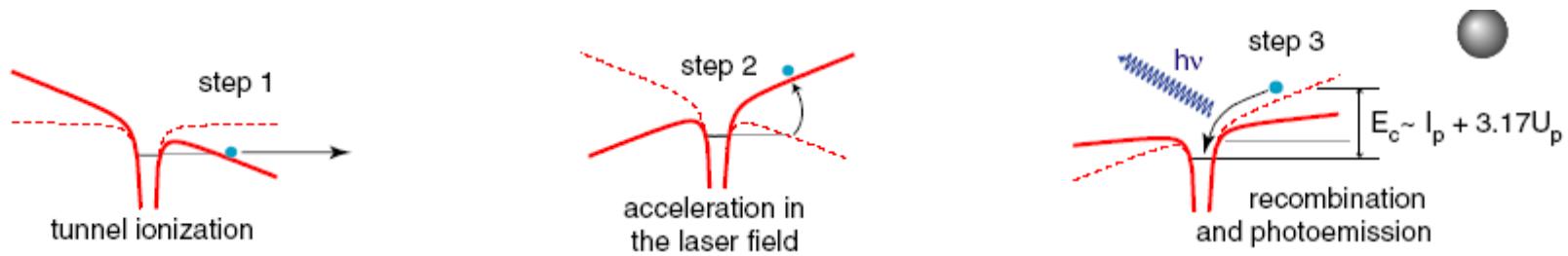
From McFerson et al, JOSA B 4 (1987), 595

HHG in gases

Theoretical Description:

-Semi-classical: The three-step model of HHG

Corkum Phys.Rev.Lett.71 (1994); Kulander et al Proc.SILAP III, ed. B.Piraux (Plenum), 95-110.



->Correctly predicts most of the observed features

Cutoff: $h\nu_{\max} = I_p + 3.2U_p$, where $U_p = e^2 E^2 / (4m\omega^2) = 9.33 \times 10^{-14} I_f \lambda_f^2$

$$\begin{matrix} \uparrow \\ \text{eV} \end{matrix}$$
$$\begin{matrix} \nearrow \\ \text{W/cm}^2 \end{matrix}$$
$$\begin{matrix} \nearrow \\ \mu\text{m} \end{matrix}$$

-Fully quantum-mechanical treatment

Lewenstein et al, Phys.Rev.A 49 (1994), 2117

$$\Phi_q = q\omega t_f - S(p_{st}, t_i, t_f)$$

HHG in gases

Directions for parameter improvement

A. Phase-matching

1. HG in waveguide (hollow fibre)
2. Corrugated waveguide (QPM)
3. Multiple gas jets (QPM)
4. Counter-propagating beam (QPM)
5. Non-adiabatic self-phase matching (HHG with very short pulses)
6. Use of gas mixtures

B. Long wavelength excitation for increasing cut-off (pump source development)

C. Selective harmonic enhancement:

- HHG with temporally shaped pulses
- Bi-harmonic fields

D. Wavelength tuning:

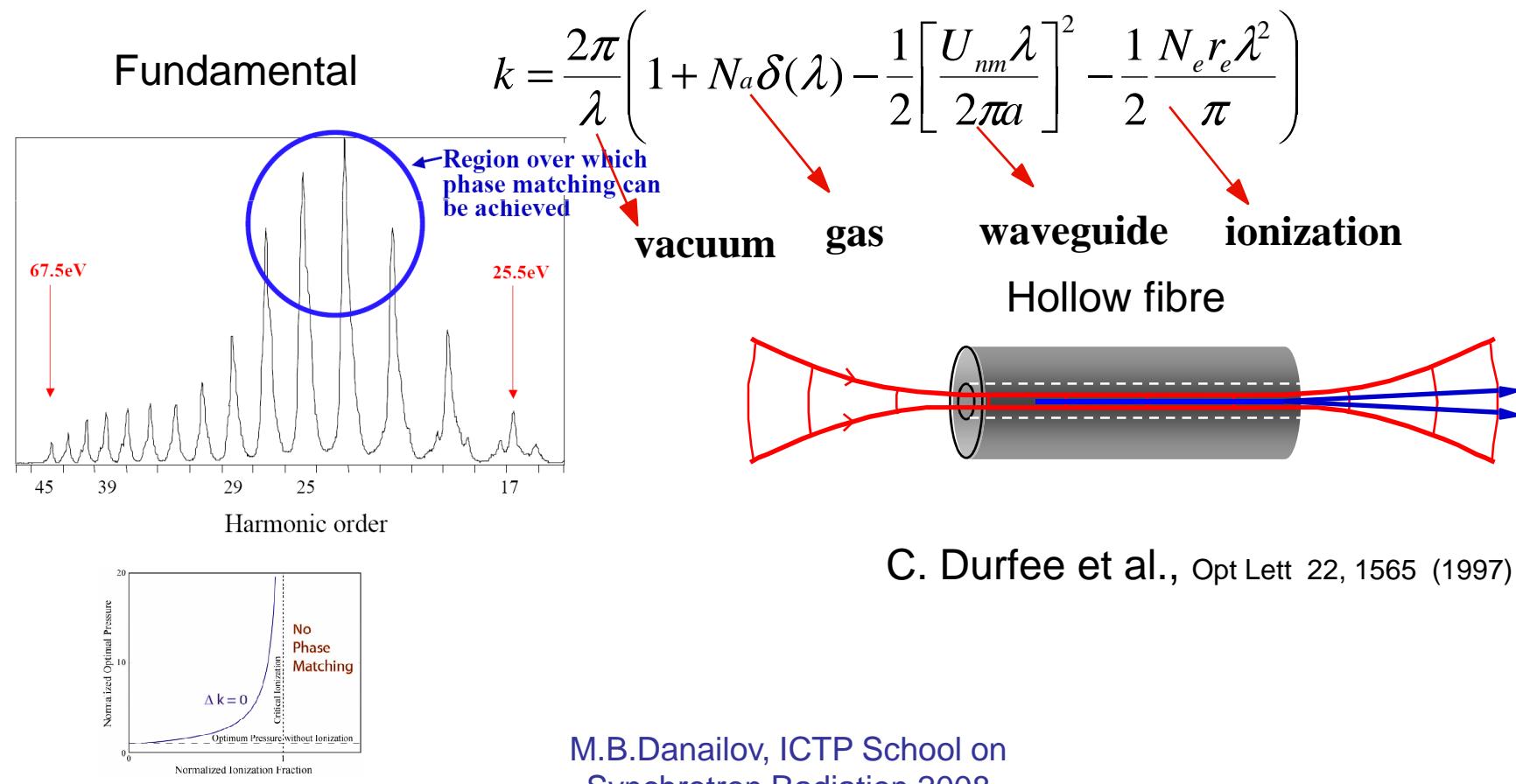
- OPA pump
- Use of 'blue' shift with changing gas pressure

HHG in gases

A1. Phase matching in guided wave HHG

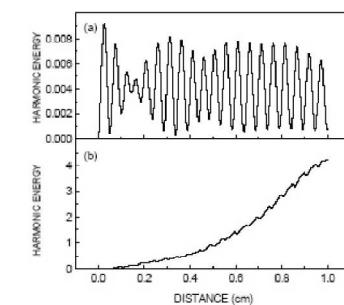
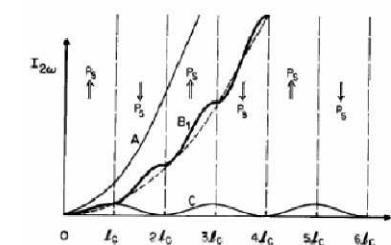
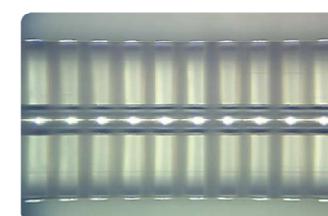
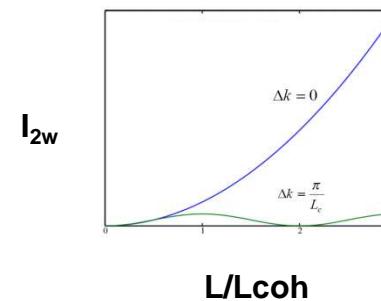
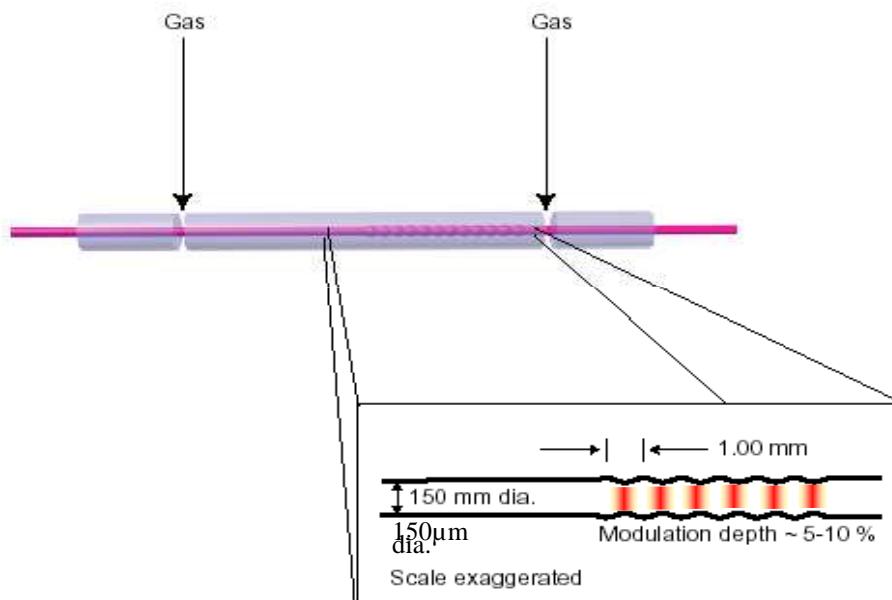
Phase mismatch

$$\Delta k = qk_f - k_q = \Delta k_{gas} + \Delta k_{wg} + \Delta k_{plasma}$$



HHG in gases

A.3. Quasi-Phase Matching (QPM) in waveguide HHG

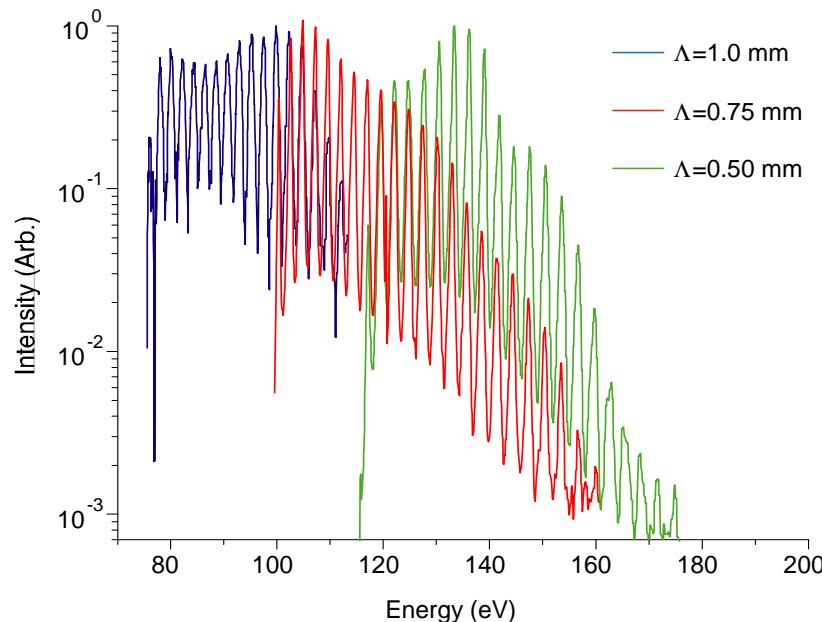


A. Paul et al, *Nature* **421** (2003), 51

I.P.Christov et al, *OptExpress* **7** (2000), 362

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HHG in gases



Cut-off shift to higher energy by QPM in He, driving pulse 25 ps,
Peak intensity $\sim 5 \times 10^{14} \text{ W/cm}^2$,

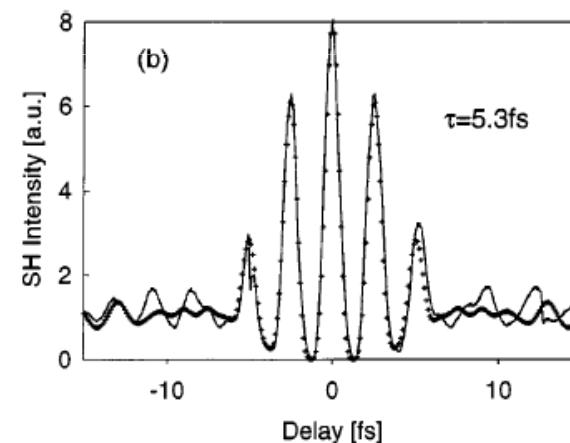
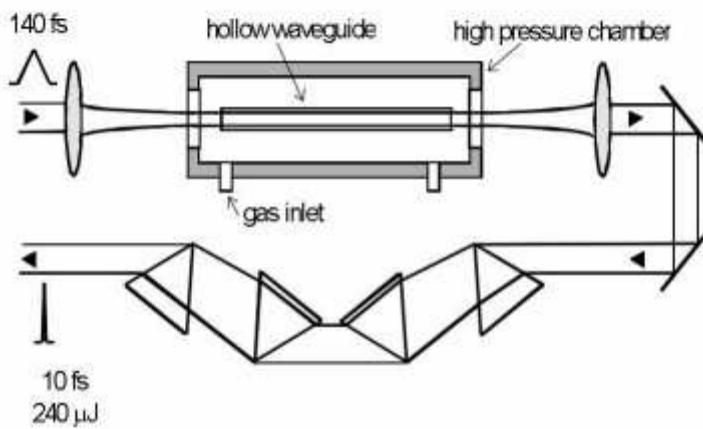
A. Paul et al, *Nature* **421** (2003) 51

HHG in gases

A.4. Use of very short pulses: non-adiabatic regime

Few-cycle fundamental pulse (~5 fs at 800 nm)

(approach for generation proposed at Politecnico di Milano and Viena,
demonstrated 5 fs , 70 μ J)



M. Nisoli et al, Opt. Lett. 22, 522 (1997)

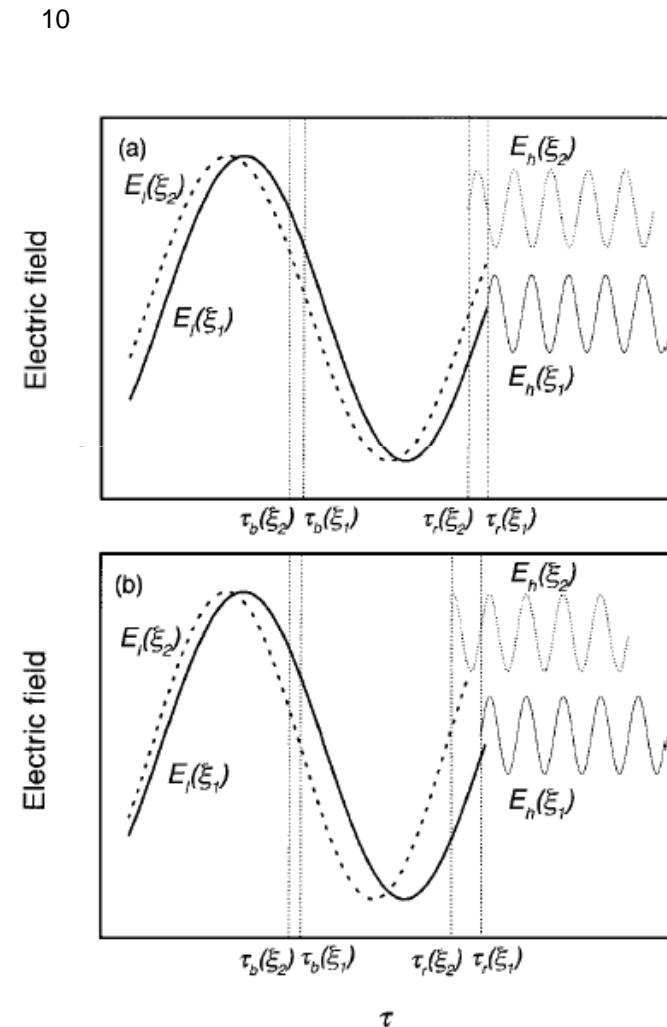
HHG in gases

A.4. Non-adiabatic self-phase matching (NSPM)

Very short pulses focused to $0.2\text{-}1 \times 10^{16} \text{ W/cm}^2$
Proposal and numerical simulations: Tempea et al, *Phys Rev Lett* **84** (2000)4329

Experimental results : E.Seres et al, *Phys Rev Lett* **92** (2004), 163002

Laser source: 5 fs, 300 μJ , focused to 30-40 μm
Medium: thin jet (0.5 mm), 0.5 bar



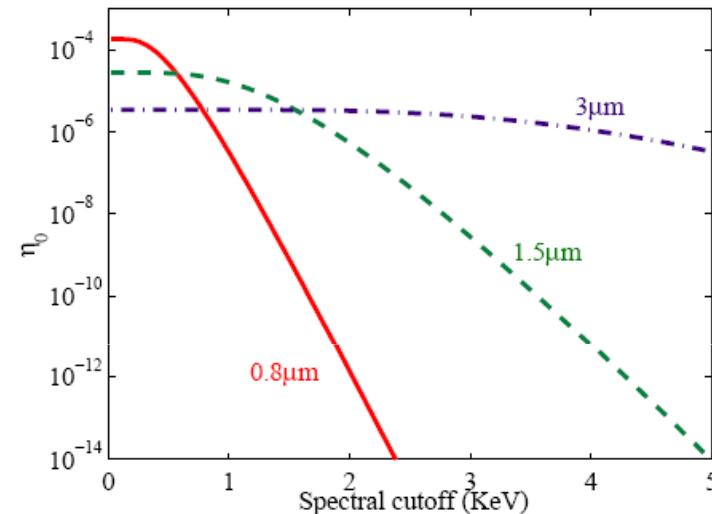
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B. Increase wavelength of excitation

— cutoff increase expected

$$hv_{\max} \sim I_p + I_L \lambda^2$$

Needs development of high
Energy parametric amplifier systems
in the 2 μm
region

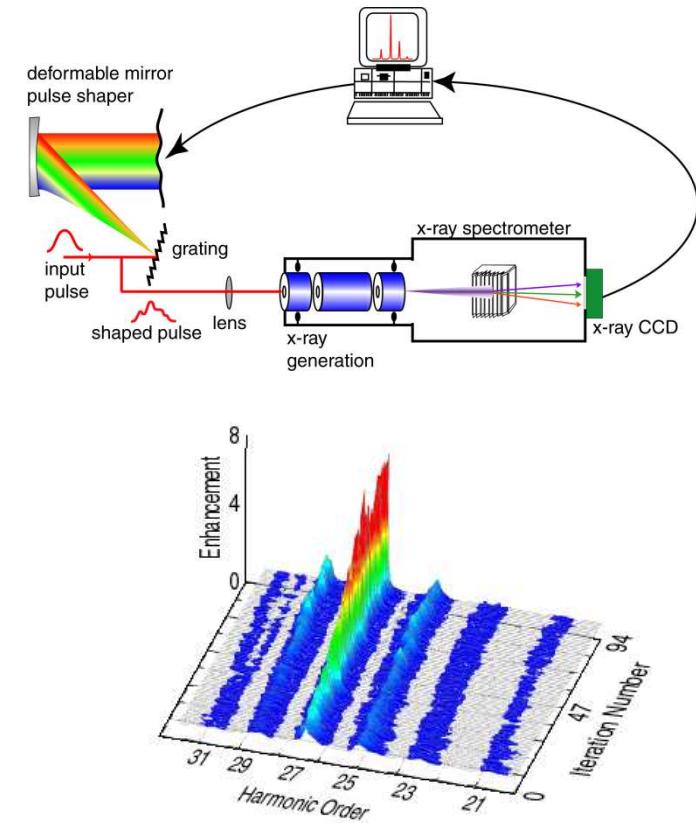
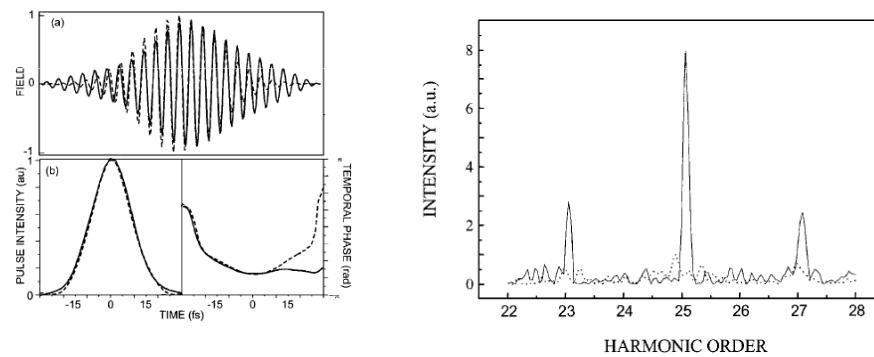


A. Gordon et al, Opt. Express **13**, 2941-2947 (2005)

HHG in gases

Temporal pulse shaping

Optimization of harmonic yield for a given harmonic order : very small changes in the driving pulse temporal phase induce substantial enhancement



Theory : Christov et al, PRL 86 (2001),
5458

Bartels et al, Nature 406 (2000) 164

HHG in gases

PARAMETERS

Pulse energy

- Above 1 μJ from 40 to 80 nm
- 10-100 nJ in the 10-40 nm range

Laser source: Ti:sapphire at 800 nm

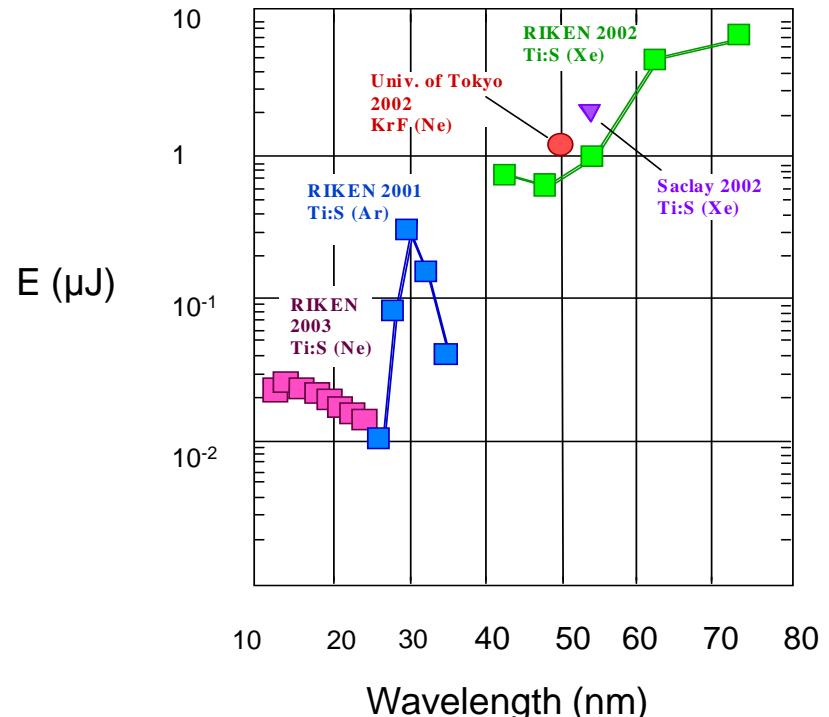
For low rep rate high-energy regime:

$E_p \sim 30\text{-}50 \text{ mJ}$, $t_p \sim 30\text{-}50 \text{ fs}$, rep rate $\sim 10 \text{ Hz}$

Geometry: loose focusing ($f_l \sim 2\text{-}5 \text{ m}$)

For low-medium energy HHG:

$E_p \sim 2\text{-}3 \text{ mJ}$, $t_p < 30 \text{ fs}$, $\sim 1\text{KHz}$, sharper focusing $f_l < 1\text{m}$



HHG setup at Elettra

LASER SOURCE PARAMETERS:

Ti:Sapphire laser system

- Coherent® Legend® amplifier

$$\lambda_0 \approx 798 \text{ nm}$$

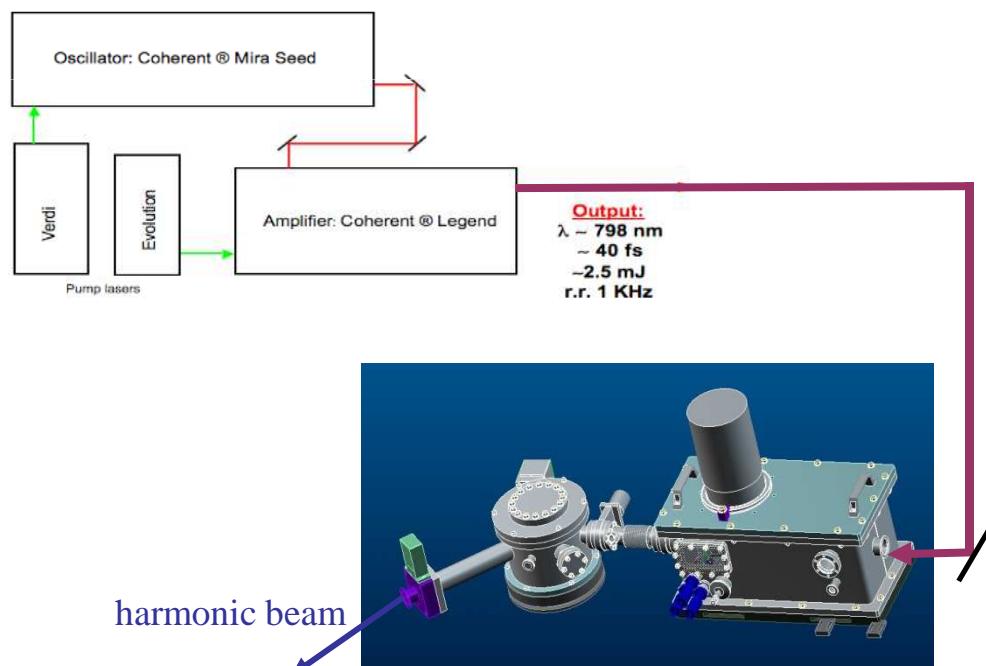
Pulse energy $\approx 2.1 \text{ mJ}$

$$\tau \approx 50 \text{ fs}$$

Upgrade in progress: pulse compression in hollow fibre

Amplifier Repetition Rate: 1 KHz

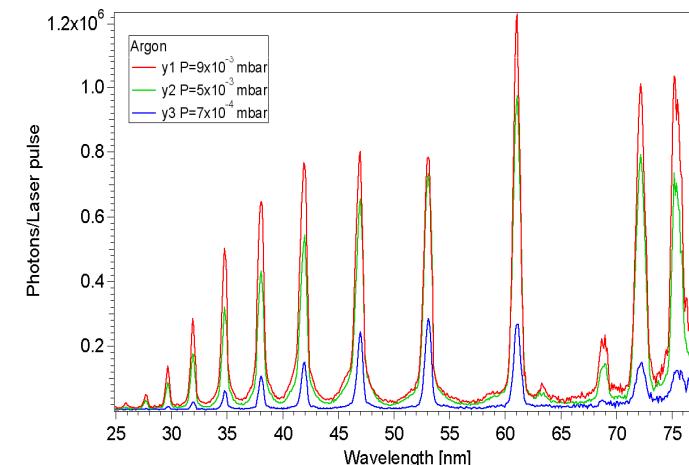
- Beam spot size after 250 mm focusing lens $\approx 40 \mu\text{m}$



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MONOCHROMATOR SPECIFICATIONS:

- Grating:
576 grooves/mm
1000 mm radius
blazed profile
gold-coated
- Source-grating distance: 450 mm
- Grating-slit distance: 350 mm
- Subtended angle: 135°
- Al filter thickness: 200 nm



Slide by B.Ressel ,
group of F.Parmigiani at Elettra

HHG in gases

PARAMETERS

Max photon energy

10^2 - 10^3 ph/s within 10% bw at **1.3 keV**
(J.Seres et al, Nature 433 (2005), 596);

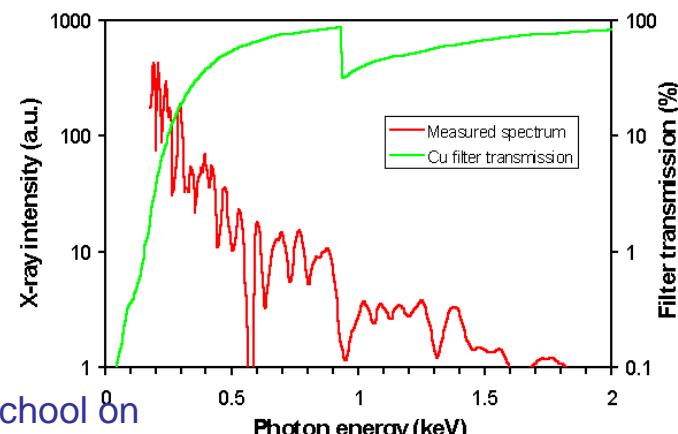
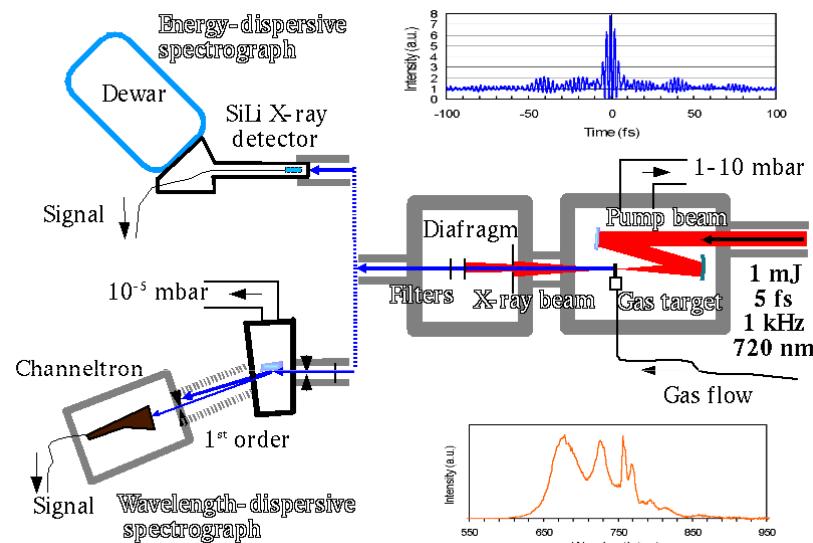
2×10^5 ph/s at **700 eV**

2×10^7 ph/s at **280 eV**

1×10^8 ph/s at **200 eV**

5×10^8 ph/s at **100 eV**

(E.Seres et al, PRL 92 (2004), 163002)



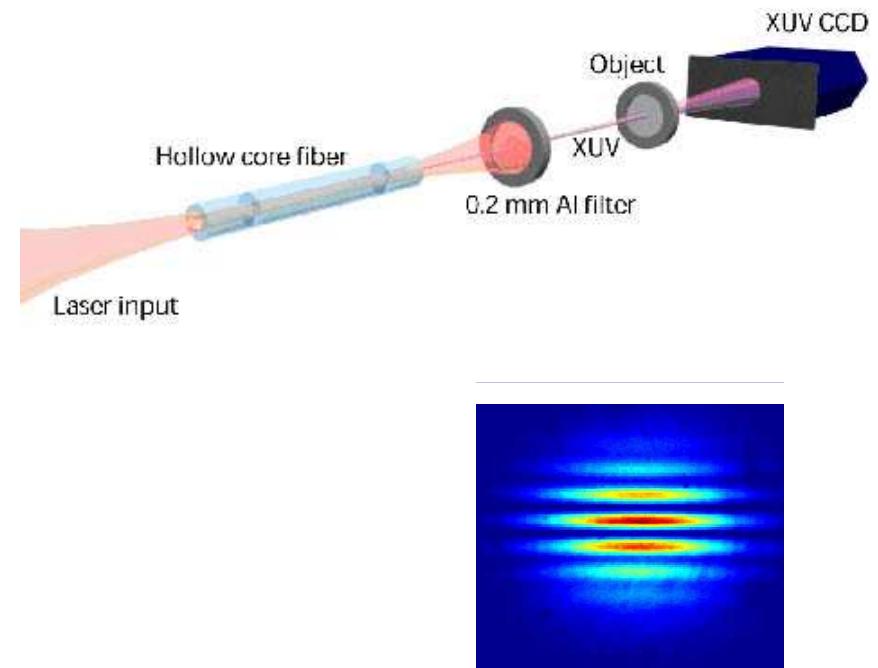
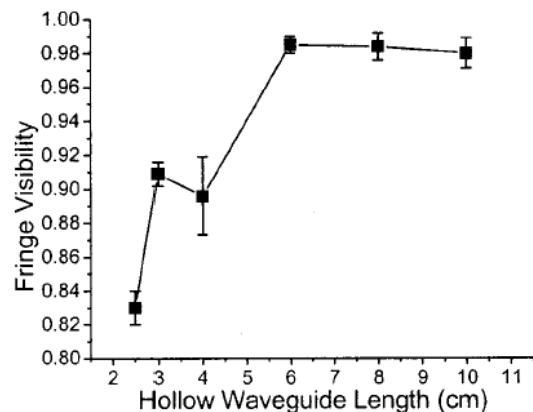
HHG in gases

Parameters

Spatial coherence – depends strongly
on the generation scheme

Nearly 100% fringe visibility with 3 to 5 segment
hollow-fibre filled with Ar, 40 Torr, harmonic
order 23-39 (36-45 eV)

A.Libertun et al, Appl Phys Lett **84** (2004), 3903



Setup and Young fringes produced at
13 nm by the Kapteyn-Murnane group

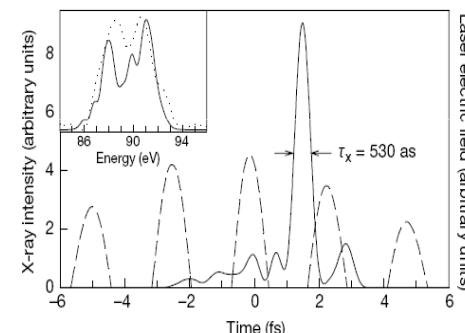
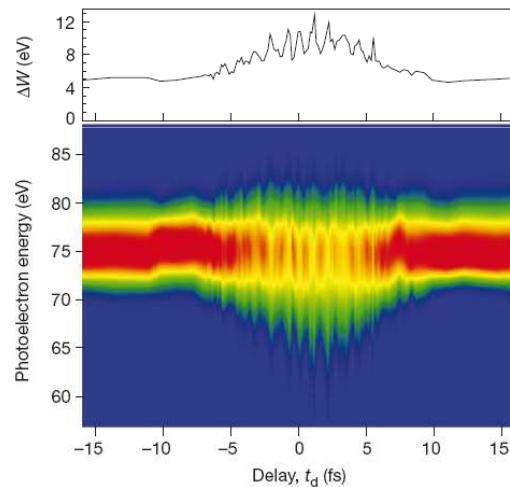
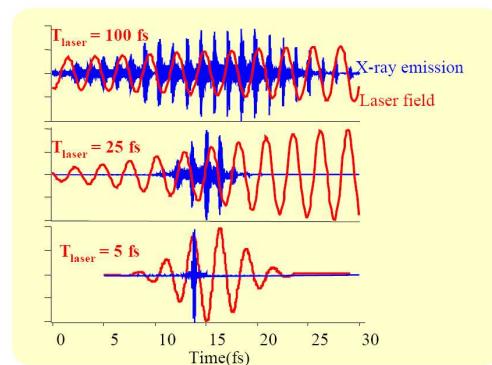
HHG in gases

Parameters

Temporal properties and attosecond pulse generation

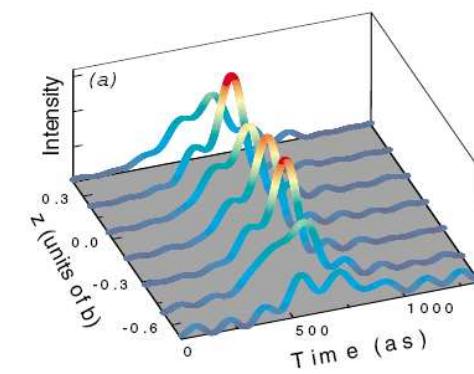
Two approaches:

1. Isolation of single as peak by using a few-cycle IR pulse and selecting the cutoff of HHG in a thin jet



Hentschel et al, Nature **414** (2001) 504

Christov et al, Phys.Rev.Lett **78** (1997)1251



2. Generation of attosecond pulse train , if the harmonics in the plateau are phase locked . IR source: 45 fs, 40 mJ; gas jet: 1 mm Ne

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Mariesse et al, Phys Rev Lett **93** (2004), 163901