



The Abdus Salam  
International Centre for Theoretical Physics



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**Advanced School on Synchrotron and Free Electron Laser Sources  
and their Multidisciplinary Applications**

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**Ultrafast VUV and soft X-ray pulses  
(production by harmonic generation and  
features)**

M.B.Danailov

*Sincrotrone  
Trieste*

# Ultrafast VUV and soft X-ray pulses

## (production by harmonic generation and features)

M.B.Danailov  
Synchrotron-Trieste

M.B.Danailov, ICTP School on  
Synchrotron Radiation 2008

# OUTLINE

Introduction

Some basics

HG in crystals : where do we stop

Low-order HG in Gases

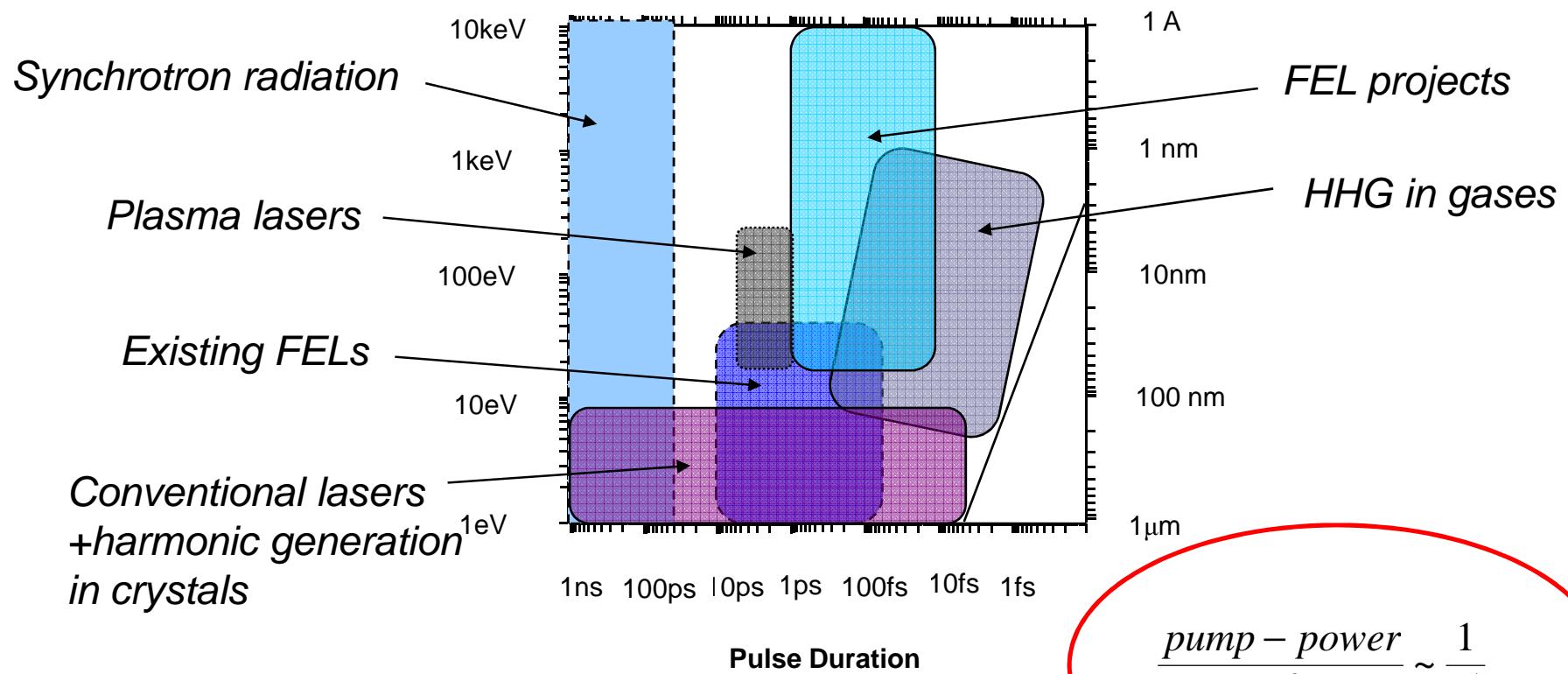
High order HG in Gases (HHG)

Trends in HHG

Features of the HHG light

# INTRODUCTION

Main sources of laser-like beams/pulses in the sub-180 nm range



# Harmonic generation



Regimes:

1. Peak power density from  $10^3$  to  $10^{13}$  W/cm<sup>2</sup> - **weak perturbation limit**

Nonlinear polarisation :

$$\vec{P} = \epsilon_0 (\chi^{(1)} \vec{E} + \chi^{(2)} \vec{E}^2 + \chi^{(3)} \vec{E}^3 + \dots)$$

Phase matching:

$$n\mathbf{k}_\omega = \mathbf{k}_{n\omega}$$

In NL crystals :

- PM by birefringence
- $\chi^{(2)} \sim 10^{-12}$  m/V

efficiency of SHG ( $2\omega$ )~50% , THG( $3\omega$ )~20%,... FHG( $5\omega$ )~1%

Limits:

- transparency region : 6.9 eV BBO, ~8eV KBBF , ~10eV SBBO
- No phase matching for SHG , mixing with longer wavelengths

Shortest wavelengths: 157 nm , FHG of Ti: sapphire in KBBF

130 nm , SHG (not in PM!) in SBBO

# Low-order HG in gases

Features:

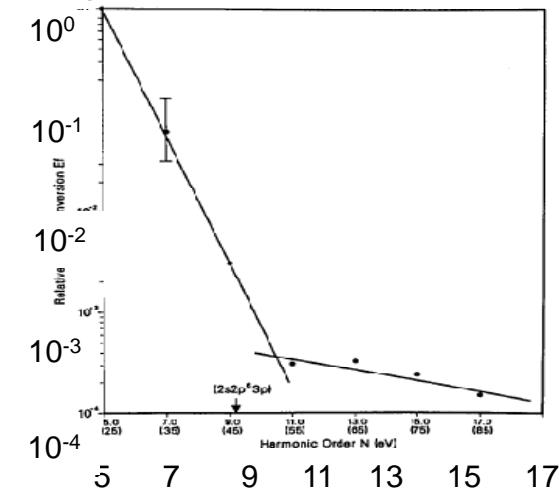
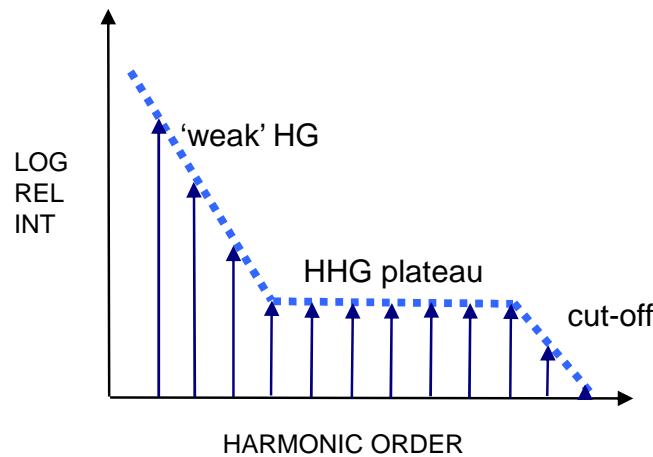
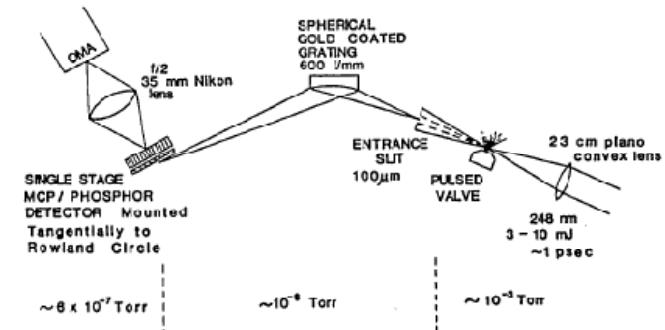
- Transmission in the VUV-EUV
- Odd harmonics only
- Low nonlinear susceptibility

$$\eta = \frac{P_3}{P_1} = \frac{3\pi^2}{\epsilon_0^2 c^2 \lambda_1^4} N^2 [\chi_{\lambda_3}^{(3)}]^2 P_1^2 |\Phi|^2 \quad (\text{in SI units})$$

- Regions where  $\Delta k \sim 0$  (or small enough) can be found by adjusting gas mixture and focusing conditions
- Feasible for THG in the EUV starting with laser wavelength in the deep UV Excimer or Third harmonic YAG : 3% efficiency in generating 118.2 nm (10.5 eV) in gas cell with mixture Xe:Ar;  
Tunable source (Nd:YAG harmonic+dye) for tunable THG in gas jets
  - >  $10^{-4}$  efficiency in generating 70- 100 nm ( $\sim 18 - 10$  eV)
  - > Could be used down to 63 nm ( $\sim 20$  eV) by use of Ti:sapphire harmonics in BBO as a source to generate  $\sim 1 \mu\text{J}$  per pulse (2 to  $5 \times 10^{11}$  ph/pulse)

# HHG in gases

At very high intensities ( $>10^{14} \text{ W/cm}^2$ )  
the weak perturbation limit breaks ->plateau in  
the harmonic conversion efficiency



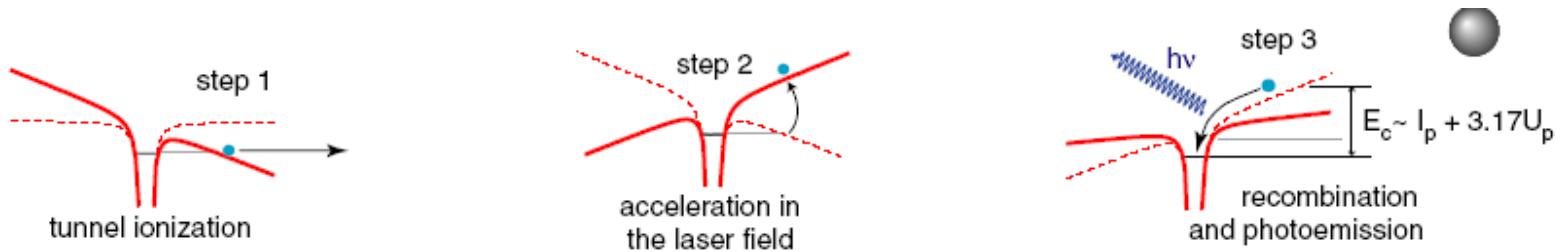
From McFerson et al, JOSA B 4 (1987), 595

# HHG in gases

## Theoretical Description:

-Semi-classical: The three-step model of HHG

Corkum Phys.Rev.Lett.71 (1994); Kulander et al Proc.SILAP III, ed. B.Piraux (Plenum), 95-110.



->Correctly predicts most of the observed features

$$\text{Cutoff: } h\nu_{\max} = I_p + 3.2U_p, \text{ where } U_p = e^2 E^2 / (4m\omega^2) = 9.33 \times 10^{-14} I_f \lambda_f^2$$

$\uparrow$   
 $eV$      $\uparrow$   
     $W/cm^2$        $\mu m$

-Fully quantum-mechanical treatment  
Lewenstein et al, Phys.Rev.A 49 (1994), 2117

$$\Phi_q = q\omega t_f - S(p_{st}, t_i, t_f)$$

# HHG in gases

## Directions for parameter improvement

- A. Phase-matching: standard scheme-> focusing in a gas-cell/jet and pressure optimization
  - 1. HG in waveguide (hollow fibre)
  - 2. Corrugated waveguide (QPM)
  - 3. Multiple gas jets (QPM)
  - 4. Counter-propagating beam (QPM)
  - 5. Non-adiabatic self-phase matching (HHG with very short pulses)
  - 6. Use of gas mixtures
- B. Long wavelength excitation for increasing cut-off (pump source development)
- C. Selective harmonic enhancement:
  - HHG with temporally shaped pulses
  - Bi-harmonic fields
- D. Wavelength tuning:
  - OPA pump
  - Use of 'blue' shift with changing gas pressure
  - Selection of a bandwidth from a continuum

# HHG in gases

## A1. Phase matching in guided wave HHG

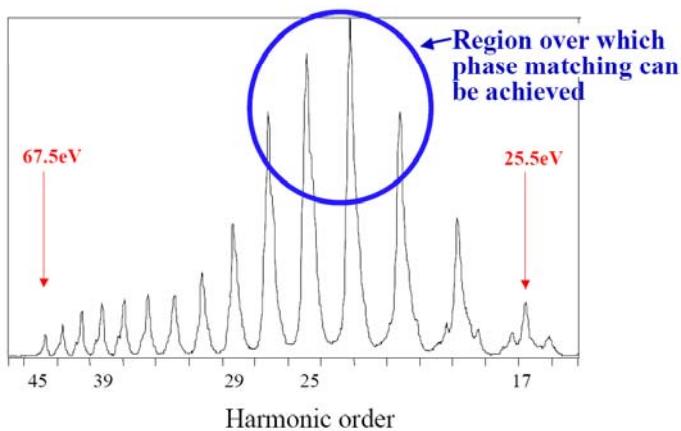
Phase mismatch

$$\Delta k = qk_f - k_q = \Delta k_{gas} + \Delta k_{wg} + \Delta k_{plasma}$$

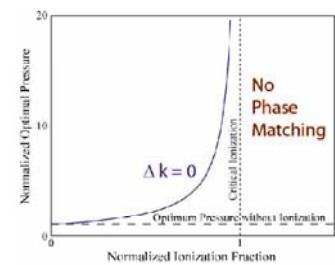
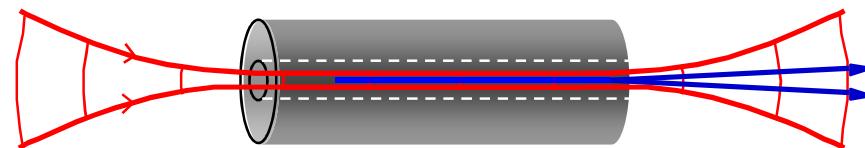
Fundamental

$$k = \frac{2\pi}{\lambda} \left( 1 + N_a \delta(\lambda) - \frac{1}{2} \left[ \frac{U_{nm} \lambda}{2\pi a} \right]^2 - \frac{1}{2} \frac{N_e r_e \lambda^2}{\pi} \right)$$

vacuum      gas      waveguide      ionization



Hollow fibre



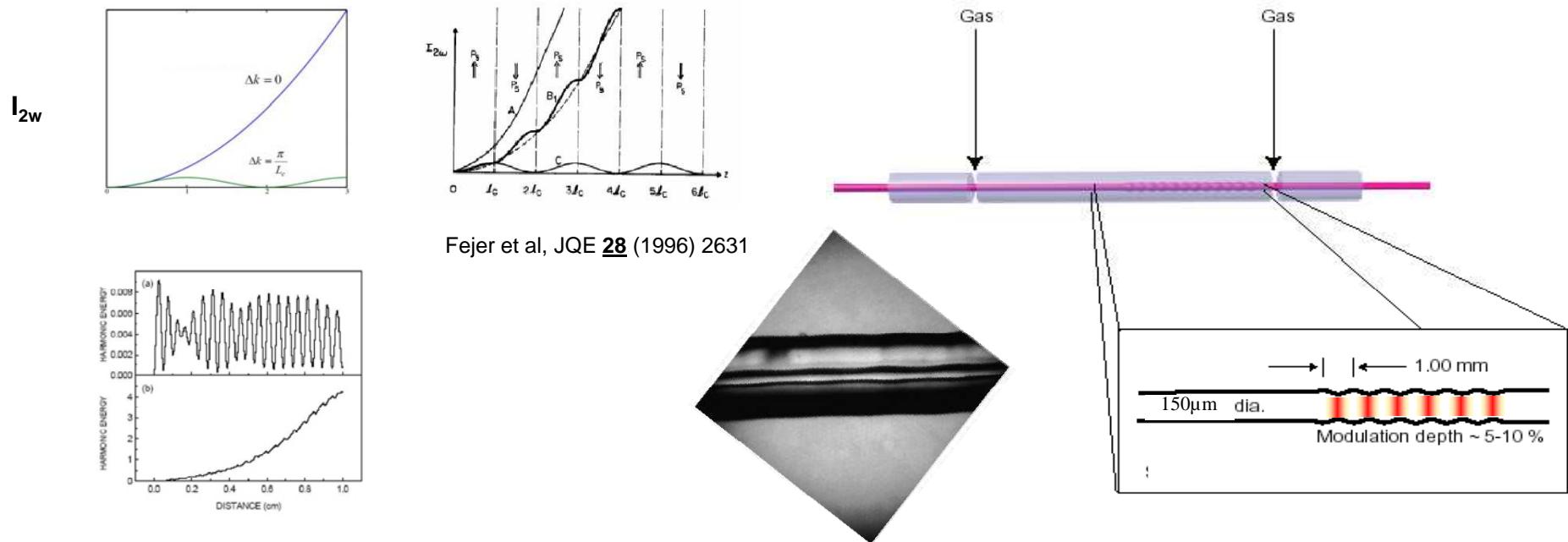
C. Durfee et al., Opt Lett 22, 1565 (1997)

Critical ionization: 0.5%, 1%, 5%  
For He, Ne and Ar

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# HHG in gases

## A.3. Quasi-Phase Matching (QPM) in waveguide HHG

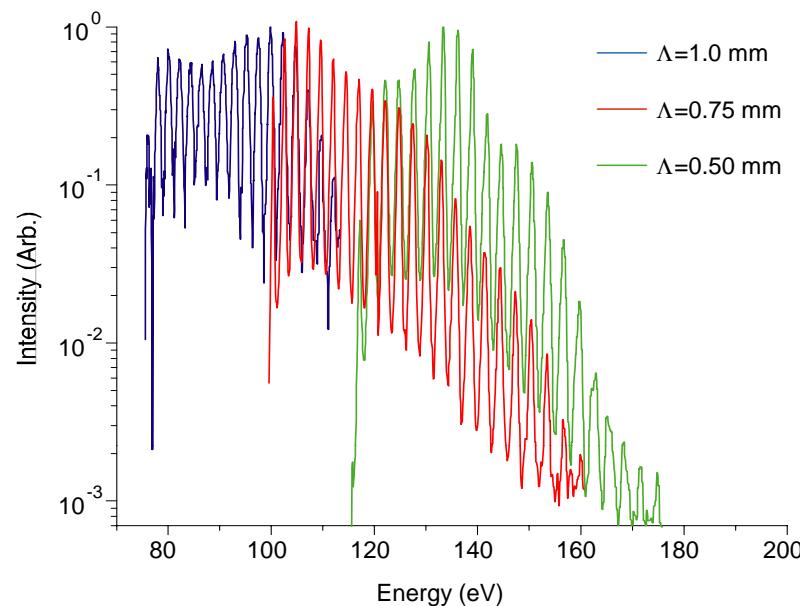


I.P.Christov et al, *OptExpress* **7** (2000), 362

A. Paul et al, *Nature* **421** (2003), 51

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# HHG in gases

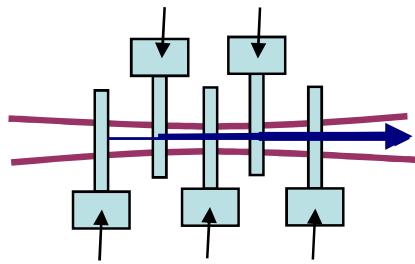


Cut-off shift to higher energy by QPM in He, driving pulse 25 ps,  
Peak intensity  $\sim 5 \times 10^{14} \text{ W/cm}^2$ ,

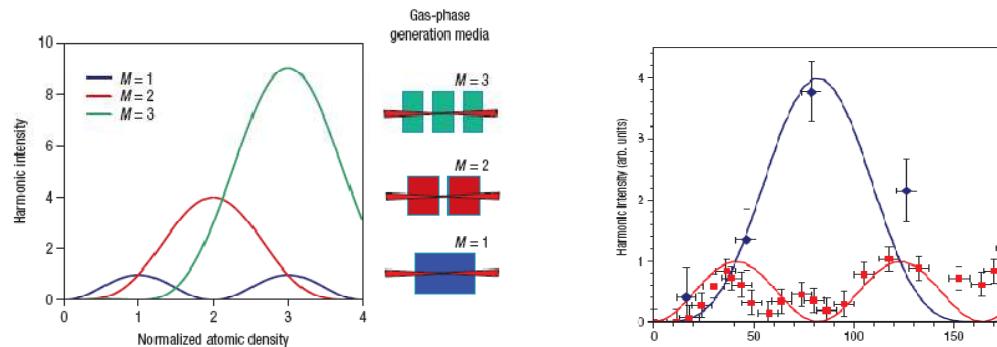
A. Paul et al, *Nature* **421** (2003) 51

# HHG in gases

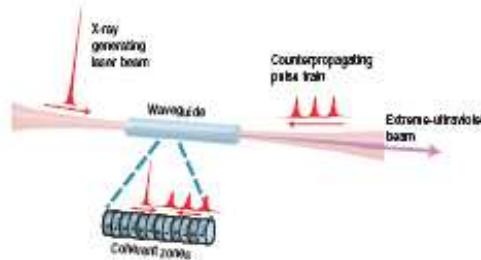
## A.3. QPM using multiple gas jets



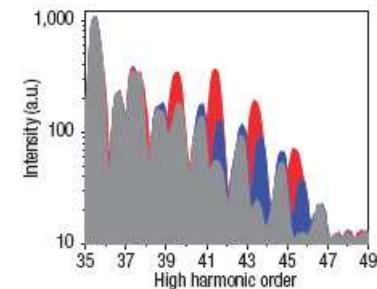
J.Seres et al, *Nature Phys* **3** (2007), 878



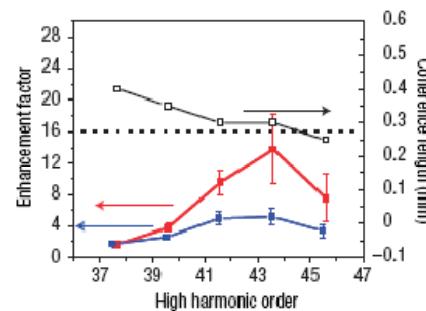
## A.4. QPM using counter-propagating pulse/beam



X.Zhang et al, *Nature Phys* **3** (2007), 274



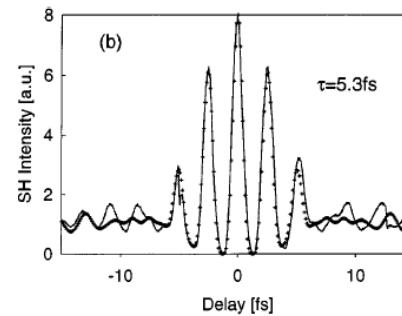
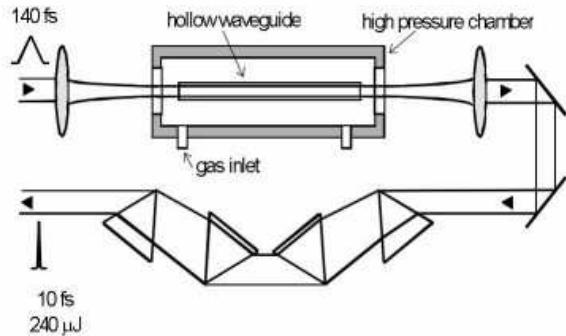
HHG with no (grey), one (blue) and two (red) c-prop pulses



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# HHG in gases

## A.4. Use of very short pulses: non-adiabatic regime, non-adiabatic self-phase matching (NSPM)

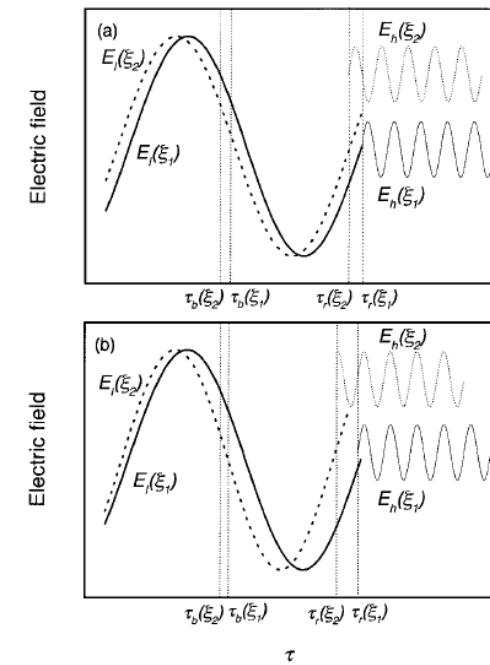


M. Nisoli et al, *Opt. Lett.* **22**, (1997) 522

Approach for generation of few-cycle fundamental pulse (~5 fs at 800 nm)  
proposed at Politecnico di Milano and Viena

NSPM: very short pulses focused to  $0.2-1 \times 10^{16} \text{ W/cm}^2$ ;  
proposal and numerical simulations: Tempea et al, *Phys Rev Lett* **84** (2000) 4329  
Experimental results : E.Seres et al, *Phys Rev Lett* **92** (2004), 163002

Laser source: 5 fs, 300  $\mu\text{J}$  , focused to 30-40  $\mu\text{m}$   
Medium: thin jet (0.5 mm), 0.5 bar



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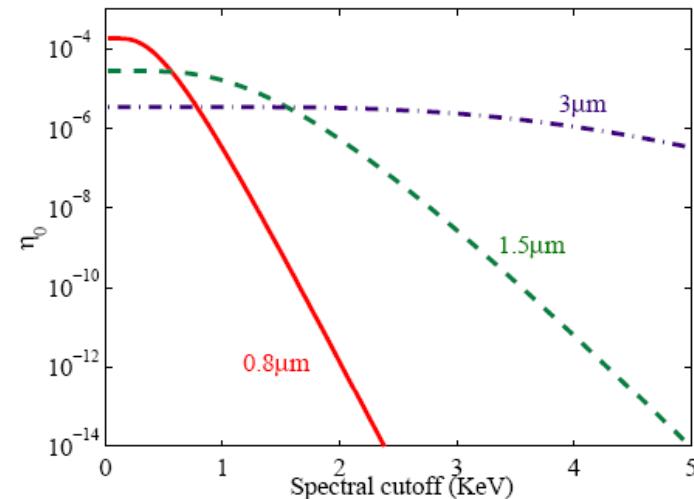
# HHG in gases

- B. Increase wavelength of excitation
  - cutoff increase expected

$$hv_{\max} \sim I_p + I_L \lambda^2$$

Needs development of high energy parametric amplifier systems in the  $\mu\text{m}$  region

Problem: loss of efficiency !

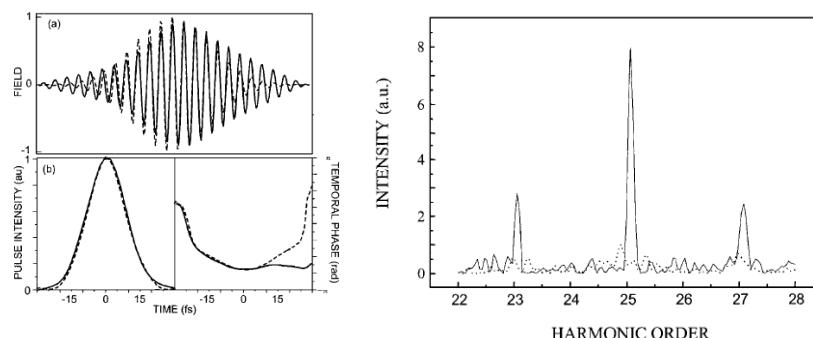


A. Gordon et al, Opt. Express 13, 2941-2947 (2005)

# HHG in gases

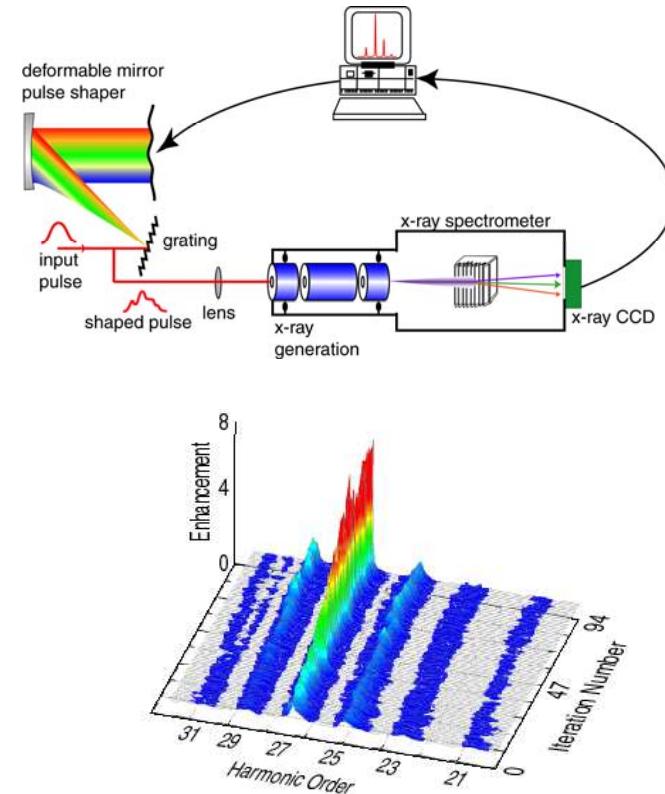
## Temporal pulse shaping

a. Optimization of harmonic yield for a given harmonic order : very small changes in the driving pulse temporal phase induce substantial enhancement



Theory : Christov et al, PRL **86**  
(2001), 5458

b. Quantum path control using CEO phase control *Phys.Rev.A* **73** (2006), 053408



*Bartels et al*, Nature **406** (2000) 164

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# HHG in gases

## PARAMETERS

### Pulse energy

- Above 1 $\mu$ J from 40 to 80 nm
- 10-100 nJ in the 10-40 nm range

Laser source: Ti:saphire at 800 nm

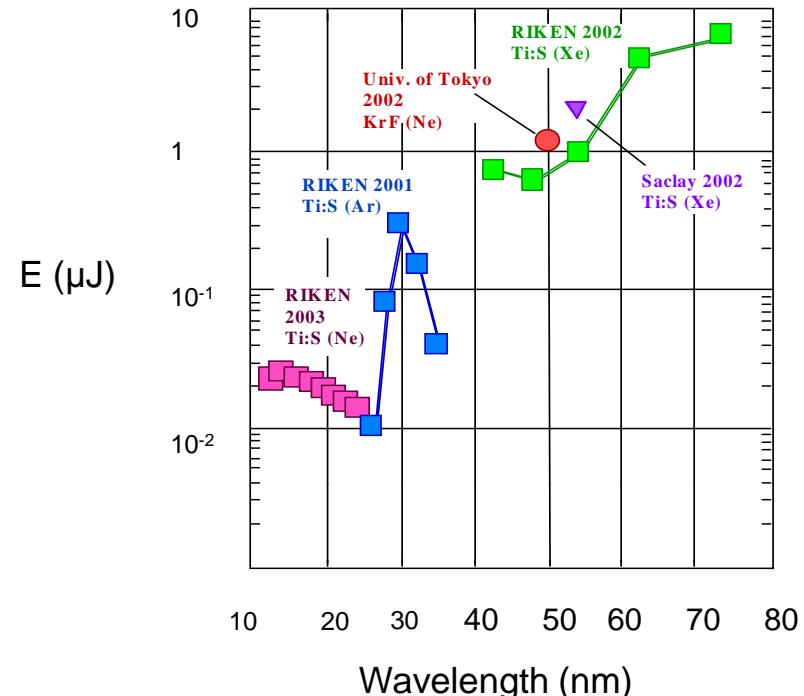
For low rep rate high-energy regime:

$E_p \sim 30\text{-}50 \text{ mJ}$ ,  $t_p \sim 30\text{-}50 \text{ fs}$ , rep rate  $\sim 10 \text{ Hz}$

Geometry: loose focusing ( $f_l \sim 2\text{-}5 \text{ m}$ )

For low-medium energy HHG:

$E_p \sim 2\text{-}3 \text{ mJ}$ ,  $t_p < 30 \text{ fs}$ ,  $\sim 1\text{KHz}$ , sharper focusing  $f_l < 1\text{m}$



# HHG setup at Elettra

## LASER SOURCE PARAMETERS:

*Ti:Sapphire laser system*

- Coherent® Legend® amplifier

$$\lambda_0 \approx 798 \text{ nm}$$

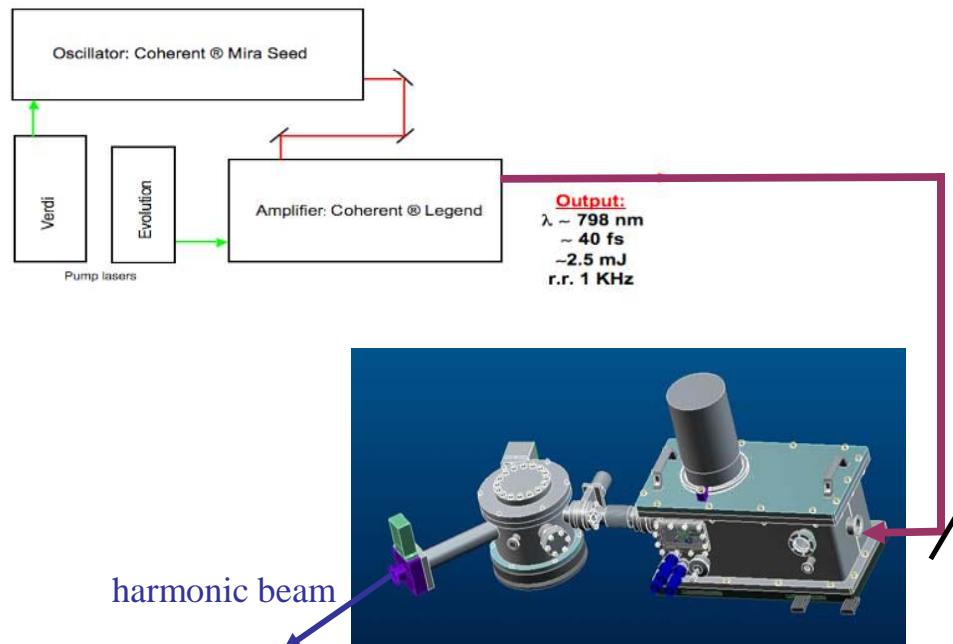
$$\text{Pulse energy} \approx 2.1 \text{ mJ}$$

$$\tau \approx 50 \text{ fs}$$

Upgrade in progress: pulse compression in hollow fibre

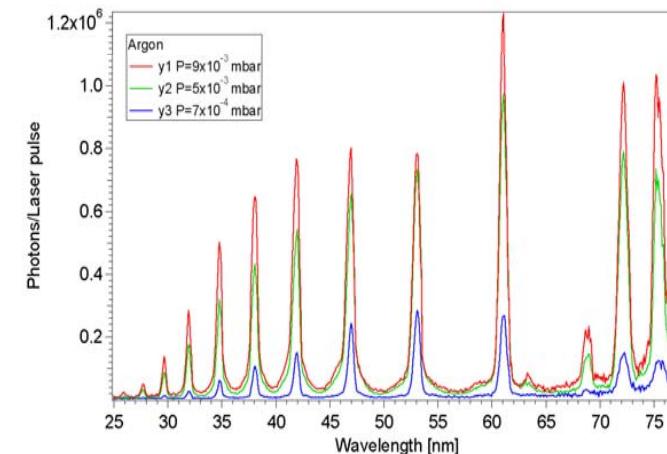
Amplifier Repetition Rate: 1 KHz

μm



## MONOCHROMATOR SPECIFICATIONS:

- Grating:  
576 grooves/mm  
1000 mm radius  
blazed profile  
gold-coated
- Source-grating distance: 450 mm
- Grating-slit distance: 350 mm
- Subtended angle: 135°
- Al filter thickness: 200 nm



Slide by B.Ressel,  
group of F.Parmigiani at Elettra

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# HHG in gases

## PARAMETERS

### Max photon energy

$10^2$ - $10^3$  ph/s within 10% bw at **1.3 keV**

( J.Seres et al, Nature 433 (2005), 596);

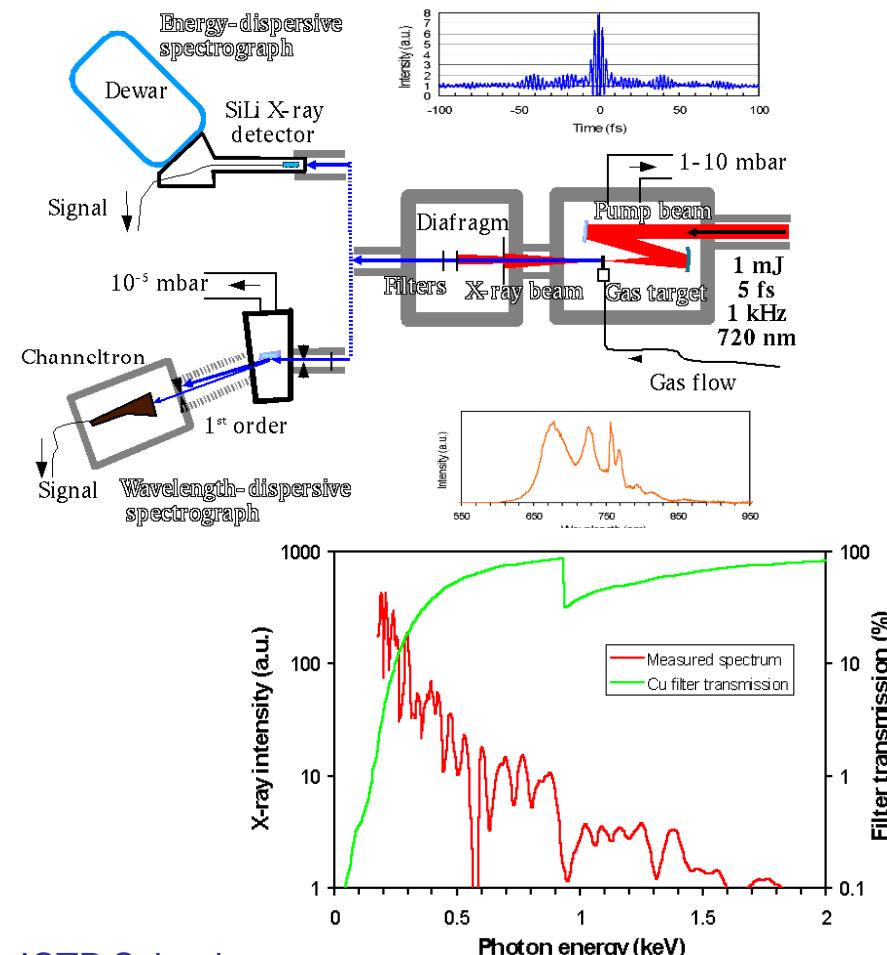
$2 \times 10^5$  ph/s at **700 eV**

$2 \times 10^7$  ph/s at **280 eV**

$1 \times 10^8$  ph/s at **200 eV**

$5 \times 10^8$  ph/s at **100 eV**

(E.Seres et al, PRL 92 (2004), 163002)



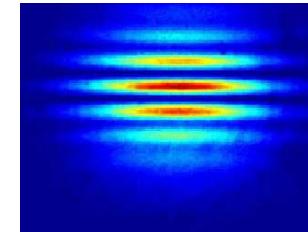
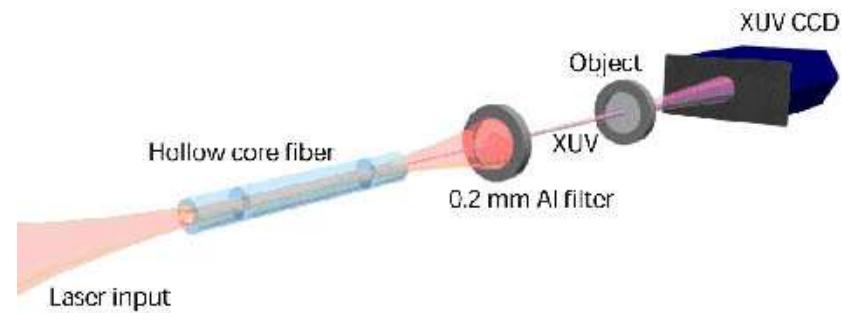
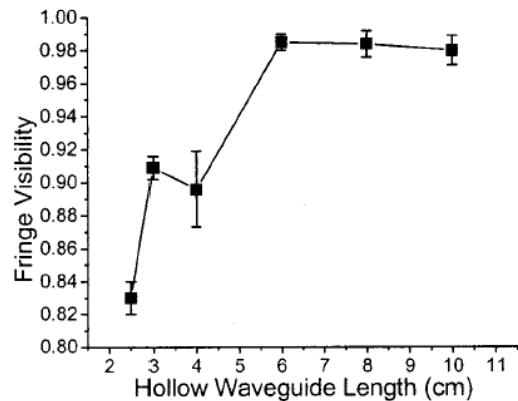
# HHG in gases

## Parameters

Spatial coherence – depends strongly  
on the generation scheme

Nearly 100% fringe visibility with 3 to 5 segment  
hollow-fibre filled with Ar, 40 Torr, harmonic  
order 23-39 (36-45 eV)

A.Libertun et al, Appl Phys Lett **84** (2004), 3903



Setup and Young fringes produced at  
13 nm by the Kapteyn-Murnane group  
(drawing from H.Kapteyn's home  
page)

# HHG in gases

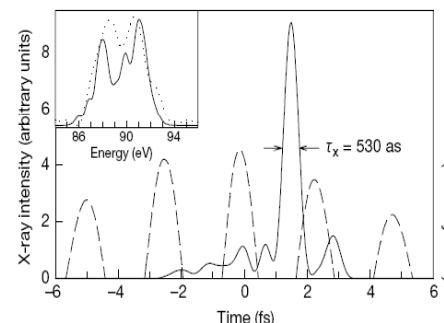
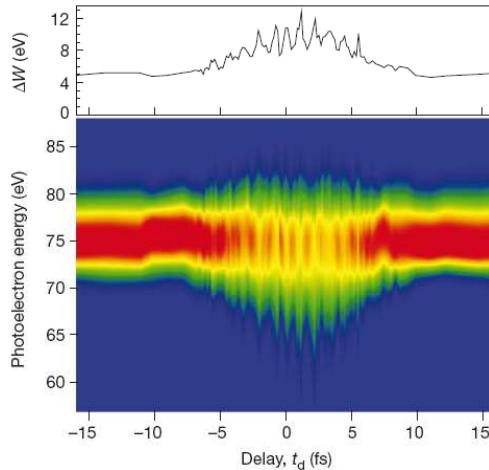
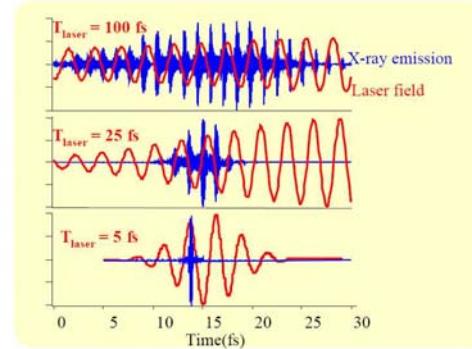
## Parameters

Temporal properties: burst of sub-fs spikes separated by half cycle of the fundamental; can be isolated by a monochromator

Attosecond pulse generation

Two approaches:

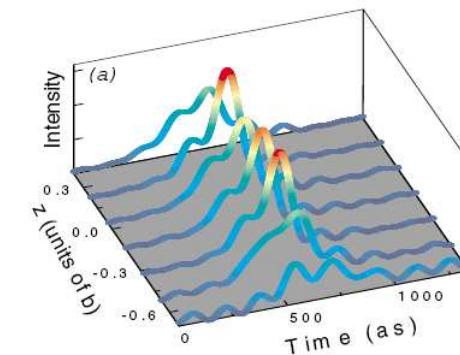
1. Isolation of single as peak by using a few-cycle IR pulse and selecting the cutoff of HHG in a thin jet



Hentschel et al, *Nature* **414**  
(2001) **504**

2. Generation of attosecond pulse train , if the harmonics in the plateau are phase locked . IR source: 45 fs, 40 mJ; gas jet: 1 mm Ne

Christov et al, Phys.Rev.Lett **78**  
(1997) **1251**



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Mariesse et al, Phys Rev Lett **93**  
(2004), 163901