



*The Abdus Salam
International Centre for Theoretical Physics*



1936-30

**Advanced School on Synchrotron and Free Electron Laser Sources
and their Multidisciplinary Applications**

7 - 25 April 2008

**Resonant Inelastic X-ray
Scattering**

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Italy*

Resonant Inelastic X-ray Scattering



Filippo Bencivenga



OUTLINE

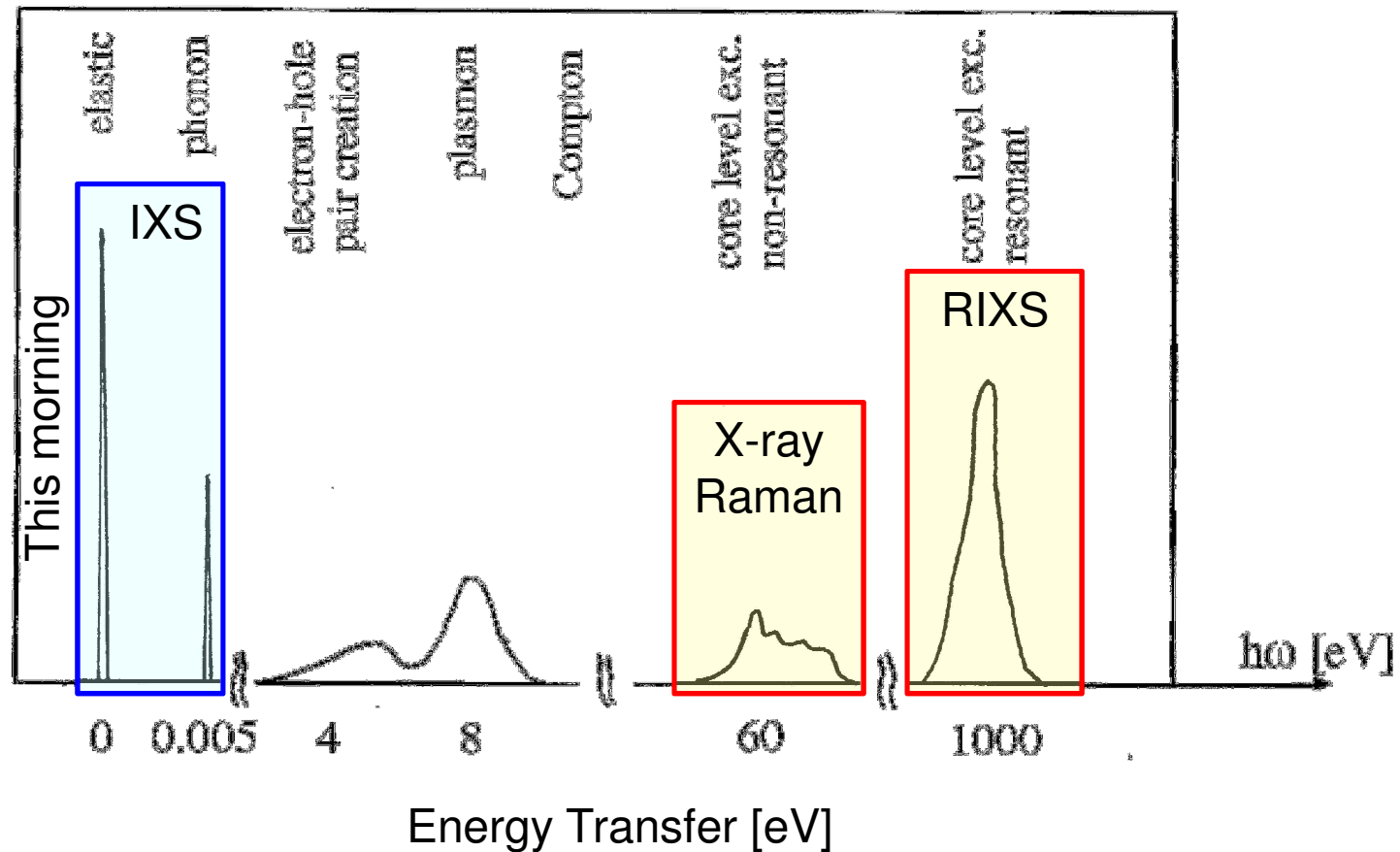
Introduction

Experimental aspects

X-ray Raman Scattering

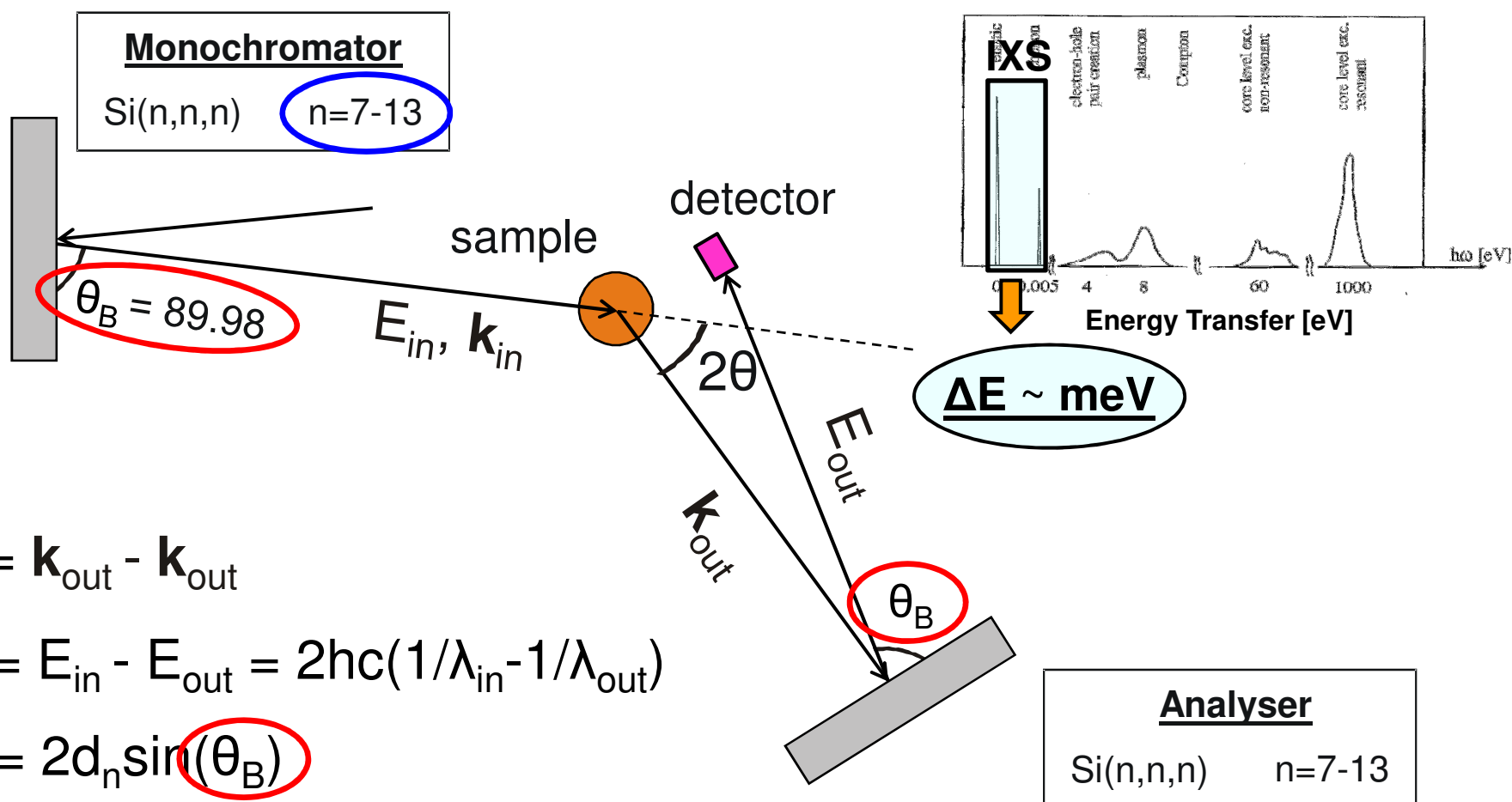
Resonant Inelastic X-ray Scattering

Introduction: inelastic X-ray spectrum



Basic IXS instrumentation

IXS (this morning)



$$\mathbf{k} = \mathbf{k}_{out} - \mathbf{k}_{in}$$

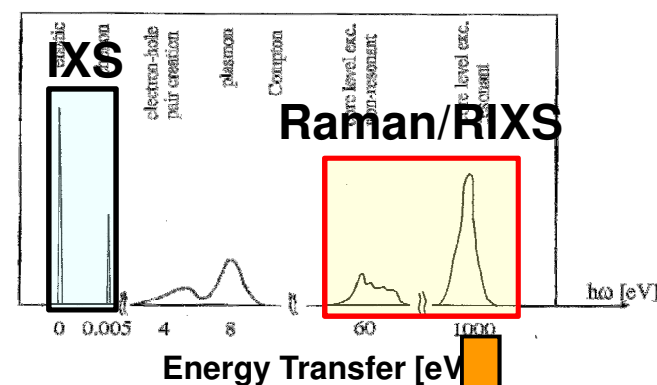
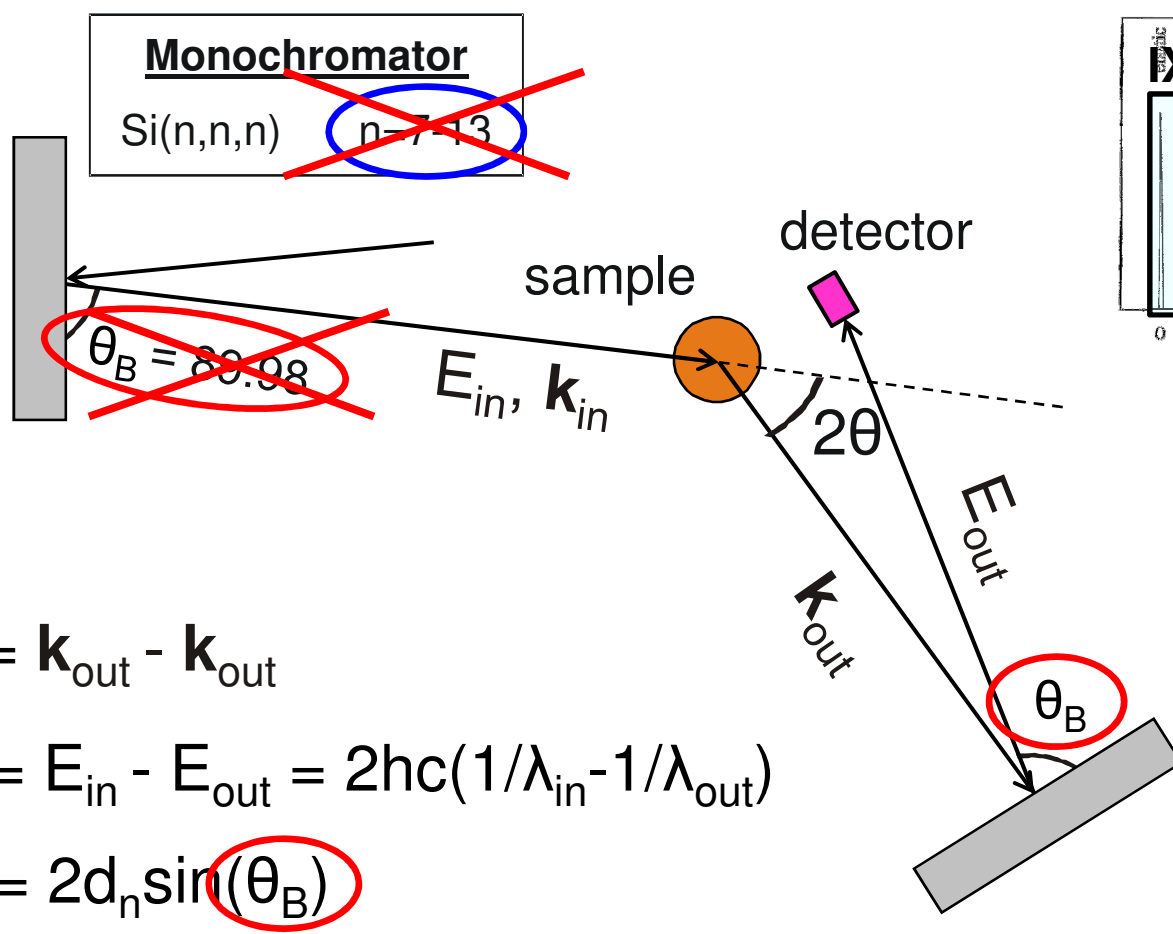
$$E = E_{in} - E_{out} = 2hc(1/\lambda_{in} - 1/\lambda_{out})$$

$$\lambda = 2d_n \sin(\theta_B)$$

backscattering + high order reflections = $\Delta E \sim \text{meV}$

Basic IXS instrumentation

IXS (this morning)



$$\Delta E \sim \text{eV}$$

$$\mathbf{k} = \mathbf{k}_{out} - \mathbf{k}_{in}$$

$$E = E_{in} - E_{out} = 2hc(1/\lambda_{in} - 1/\lambda_{out})$$

$$\lambda = 2d_n \sin(\theta_B)$$

Analyser
Si(n,n,n) n=7-13

~~backscattering~~ + ~~high order reflections~~ = ~~$\Delta E \sim \text{meV}$~~

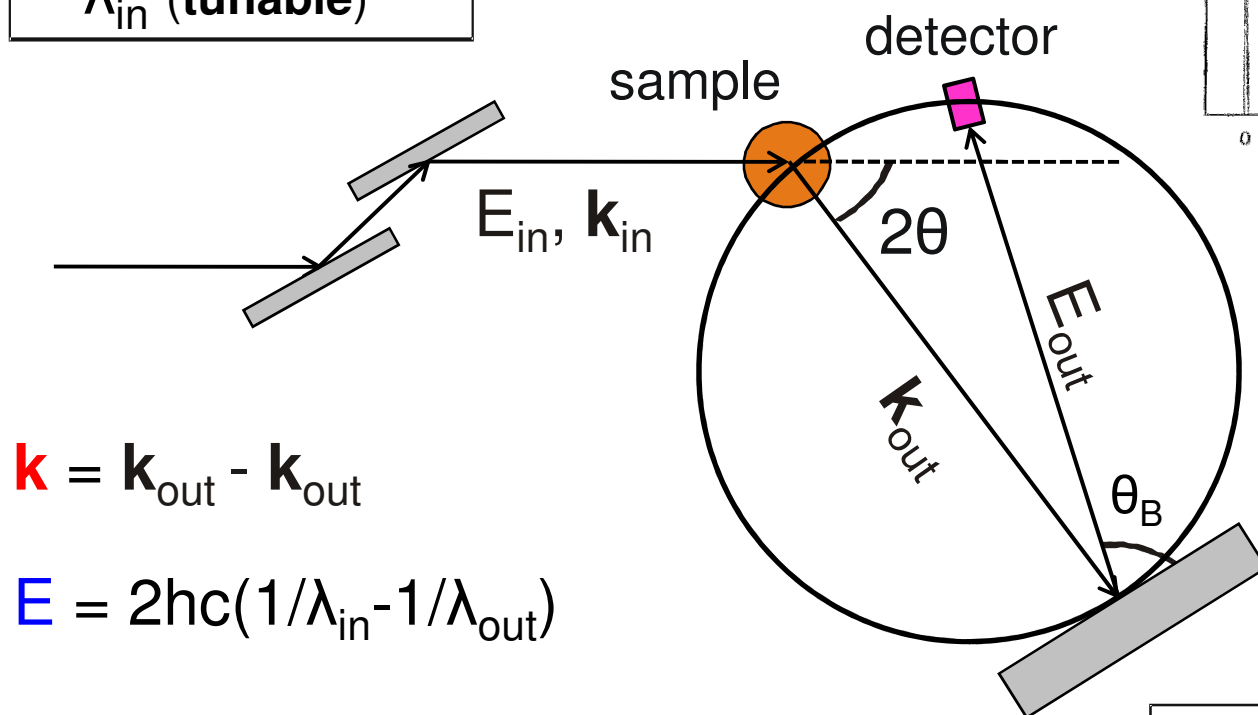
Basic IXS instrumentation

Raman / RIXS

Monochromator

Si(1,1,1); (2,2,0); ...

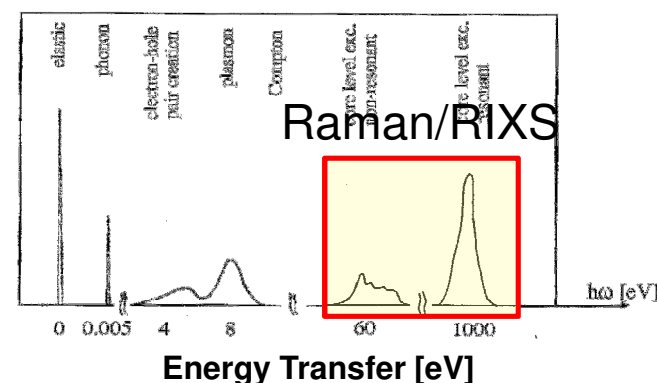
λ_{in} (tunable)



$$\mathbf{k} = \mathbf{k}_{out} - \mathbf{k}_{in}$$

$$E = 2hc(1/\lambda_{in} - 1/\lambda_{out})$$

$$\lambda = 2d_n \sin(\theta_B); \theta_B = 65^\circ \div 90^\circ$$



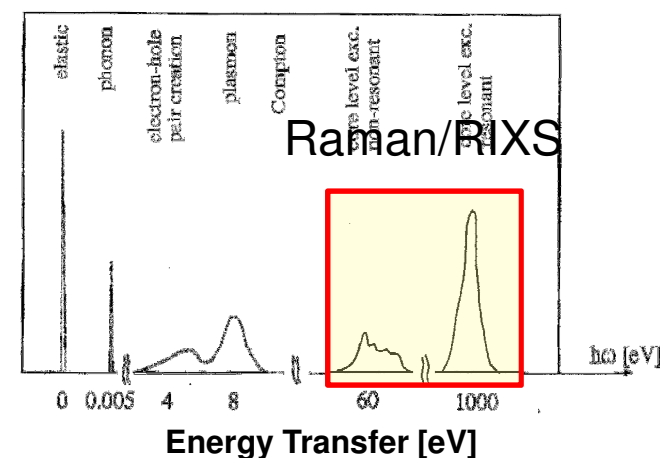
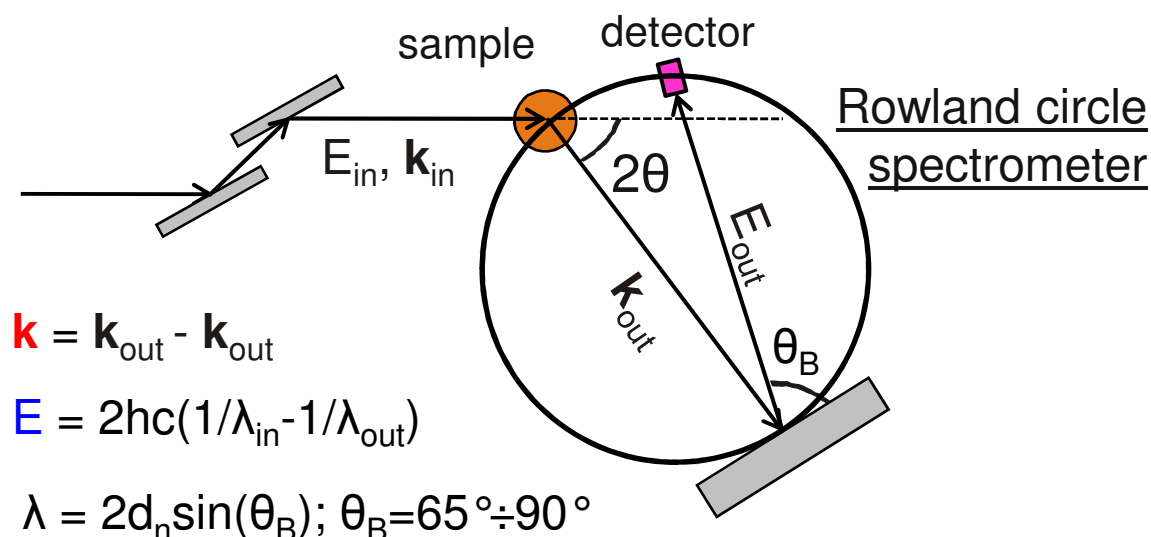
Rowland circle
spectrometer (1 m)

Analyser

Si(h,k,l) λ_{out} (tunable)

Basic IXS instrumentation

Raman / RIXS



Scanning strategy

1. E_{out} fixed, scanning E_{in}
2. E_{in} fixed, scanning E_{out}
(rotating crystal and follow with the detector)
3. Scanning E_{in} and E_{out} keeping E constant

non-resonant IXS, RIXS

RIXS

RIXS

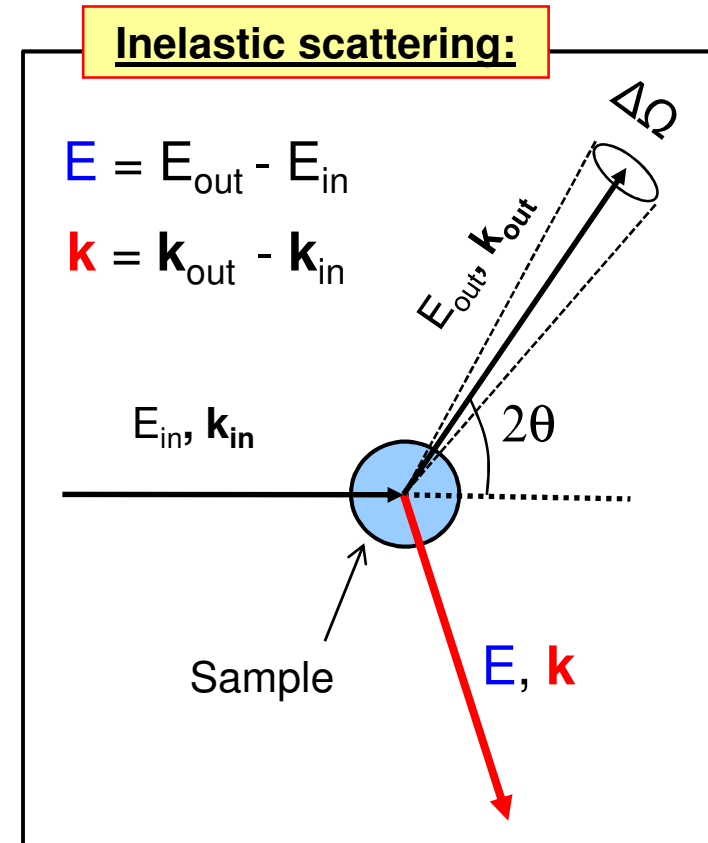
Basic theoretical aspects

$$H_{\text{int}} = (e/m_e c) \sum_j [(e/2c) \mathbf{A}_j \cdot \mathbf{A}_j + \mathbf{A}_j \cdot \mathbf{p}_j]$$

A: vector potential of electromagnetic field

P: momentum operator of the electrons

j: summation over all electrons of the system



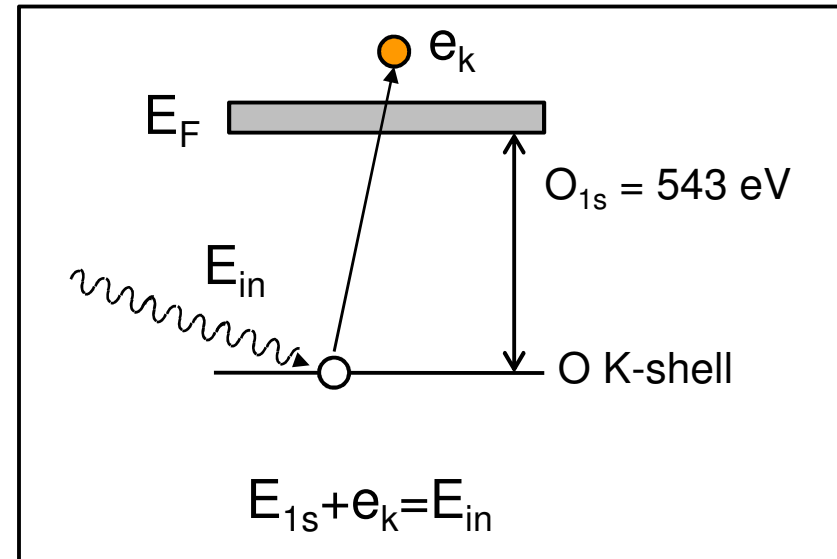
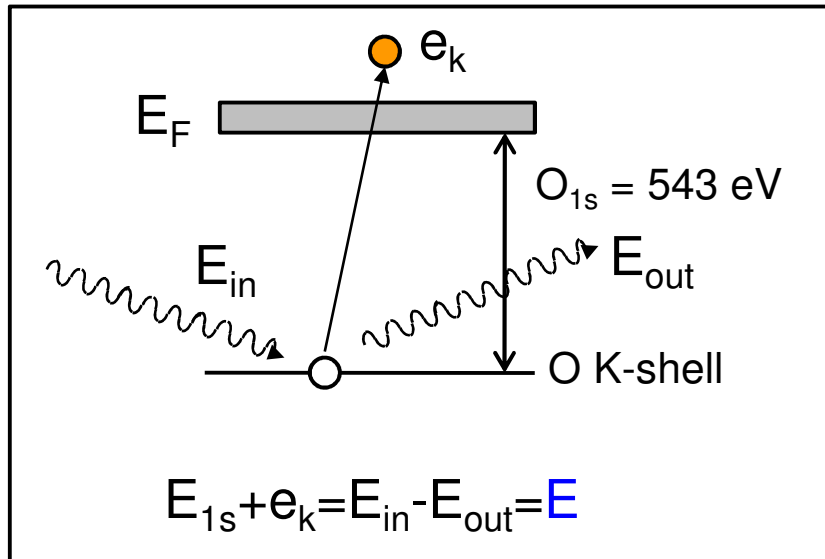
$\mathbf{A} \cdot \mathbf{A} \rightarrow$ non-resonant scattering (example this morning: IXS)

$\mathbf{A} \cdot \mathbf{p} \rightarrow$ resonant scattering, absorption followed by emission

Basic theoretical aspects

Non resonant IXS cross section:

$$\frac{\partial^2 \sigma}{\partial \Omega \partial E} = r_0^2 (\mathbf{\epsilon}_{in} \cdot \mathbf{\epsilon}_{out})^2 (k_{in}/k_{out}) \sum_l |P_l| |\langle l | \exp\{i\mathbf{k} \cdot \mathbf{r}_j\} | F \rangle|^2 \delta(E - E_F + E_l)$$



X-ray absorption cross section (dipolar approximation):

$$\frac{\partial \sigma}{\partial E_{in}} = 4\pi^2 \alpha E_{in} \sum_l |P_l| |\langle l | \mathbf{\epsilon}_{in} \cdot \mathbf{r}_j | F \rangle|^2 \delta(E_{in} - E_F + E_l)$$

Basic theoretical aspects

Non resonant IXS cross section:

$$\frac{\partial^2 \sigma}{\partial \Omega \partial E} = r_0^2 (\boldsymbol{\epsilon}_{\text{in}} \cdot \boldsymbol{\epsilon}_{\text{out}})^2 (k_{\text{in}}/k_{\text{out}}) \sum_l P_l |\langle l | \exp\{i\mathbf{k} \cdot \mathbf{r}_j\} | F \rangle|^2 \delta(E - E_F + E_l)$$



$$\mathbf{k} \cdot \mathbf{r}_j \ll 1 \rightarrow e^{i\mathbf{k} \cdot \mathbf{r}} \sim 1 + i\mathbf{k} \cdot \mathbf{r}_j$$

$\mathbf{k} \cdot \mathbf{r}_j \ll 1 \rightarrow$ Dipolar regime: identical to photon absorption, where:

- i) The momentum transfer ($\mathbf{k}$) plays the role of the photon polarization vector ($\boldsymbol{\epsilon}_{\text{in}}$)
- ii) The energy transfer (E) plays the role of the incident energy (E_{in})

X-ray absorption cross section (dipolar approximation):

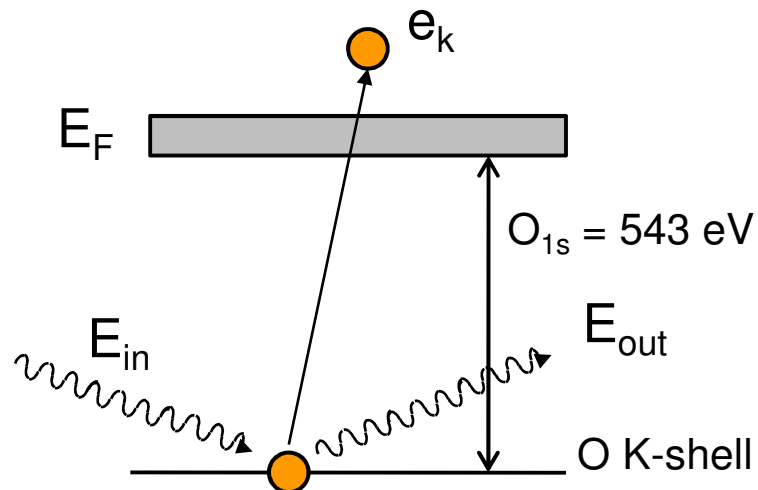
$$\frac{\partial \sigma}{\partial E_{\text{in}}} = 4\pi^2 \alpha E_{\text{in}} \sum_l P_l |\langle l | \boldsymbol{\epsilon}_{\text{in}} \cdot \mathbf{r}_j | F \rangle|^2 \delta(E_{\text{in}} - E_F + E_l)$$

Basic theoretical aspects

Non resonant IXS cross section:

$$\frac{\partial^2 \sigma}{\partial \Omega \partial E} = r_0^2 (\boldsymbol{\epsilon}_{\text{in}} \cdot \boldsymbol{\epsilon}_{\text{out}})^2 (k_{\text{in}}/k_{\text{out}}) \sum_F P_F |\langle I | \exp\{i\mathbf{k} \cdot \mathbf{r}_j\} | F \rangle|^2 \delta(E - E_F + E_I)$$

X-ray Raman Scattering (XRS)



$$E_{1s} + e_k = E_{\text{in}} - E_{\text{out}} = E$$

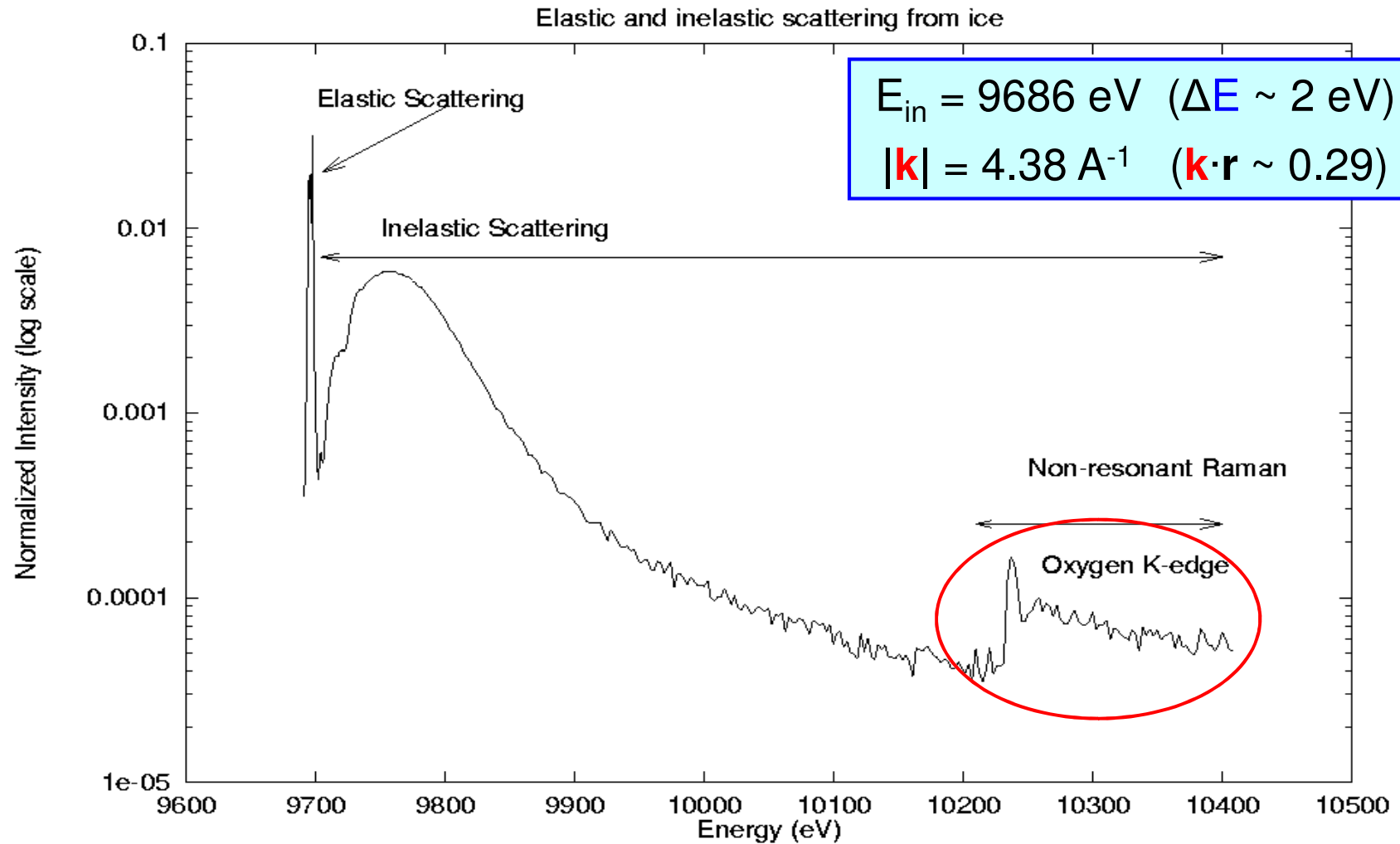
Motivation: element-selective probe for local atomic structure

XRS is alternative to:

- Neutron scattering (with isotopic substitution)
- X-ray (anomalous) scattering
- XANES and EXAFS

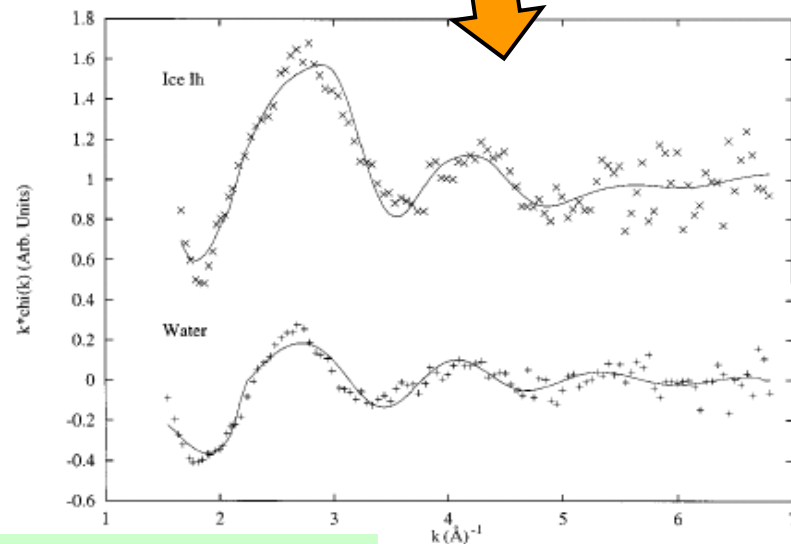
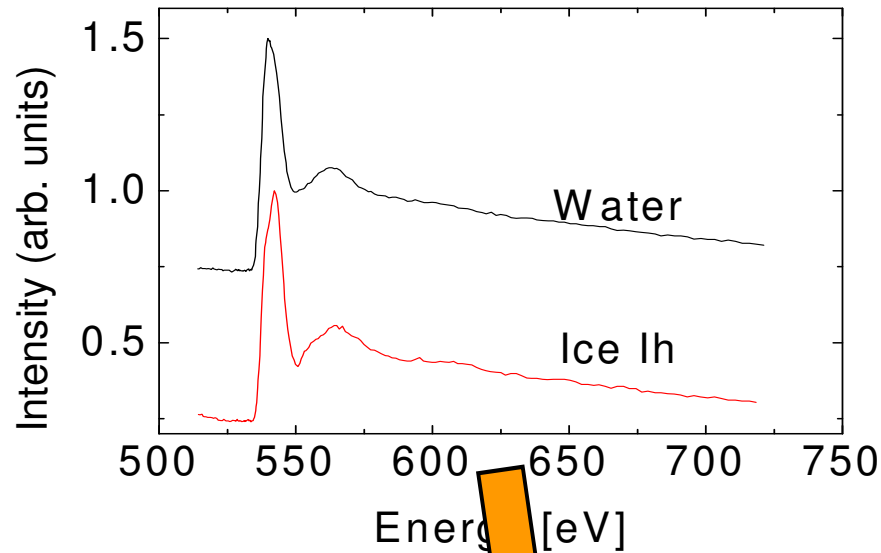
Experimental highlights (XRS)

XRS from O K-edge in water and ice



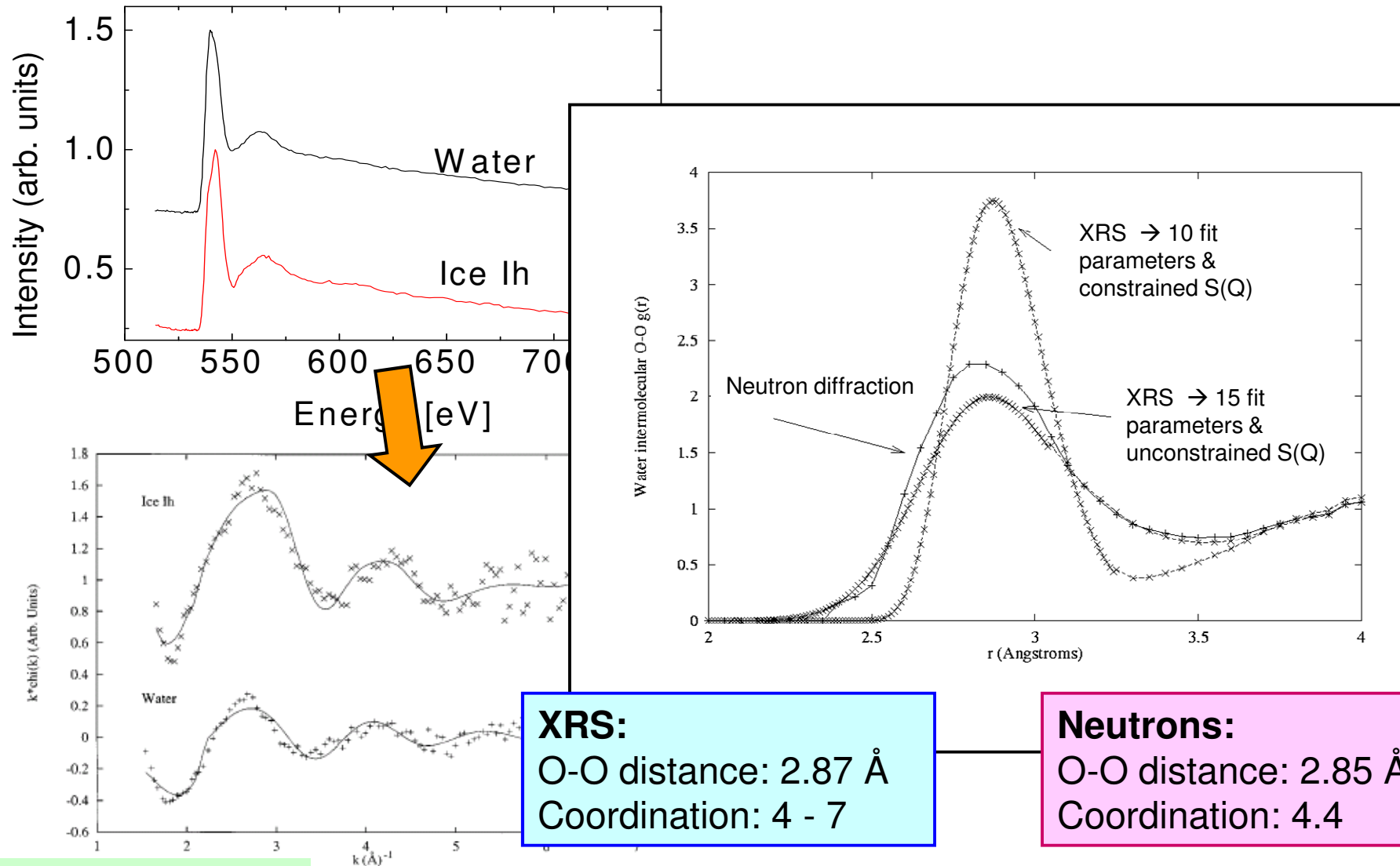
Experimental highlights (XRS)

XRS from O K-edge in water and ice (EXAFS)



Experimental highlights (XRS)

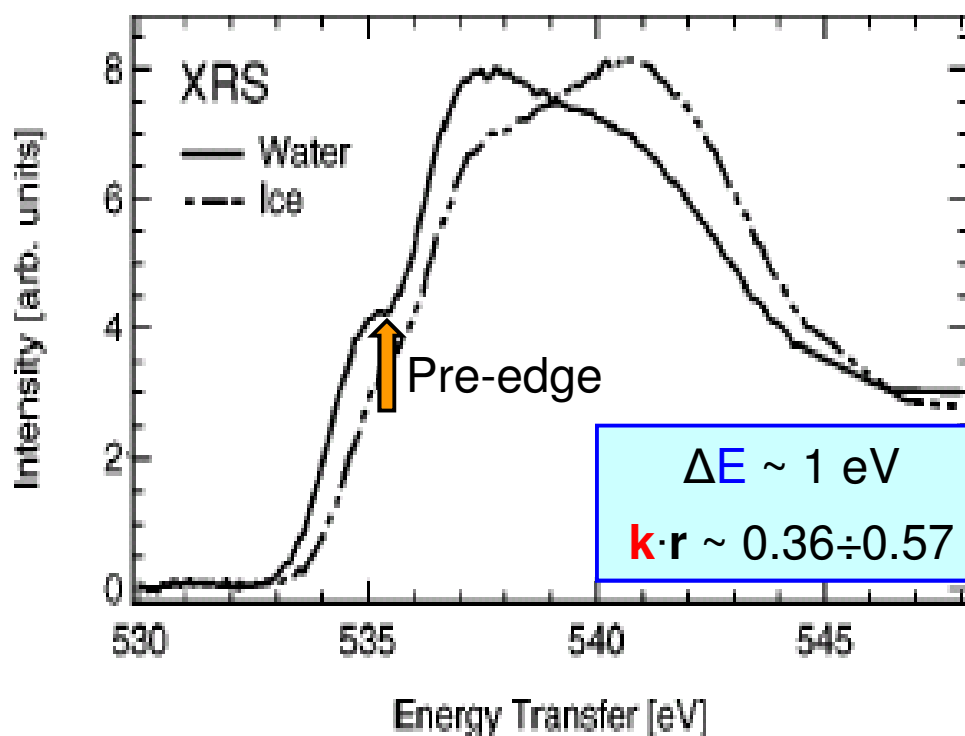
XRS from O K-edge in water and ice (EXAFS)



Experimental highlights (XRS)

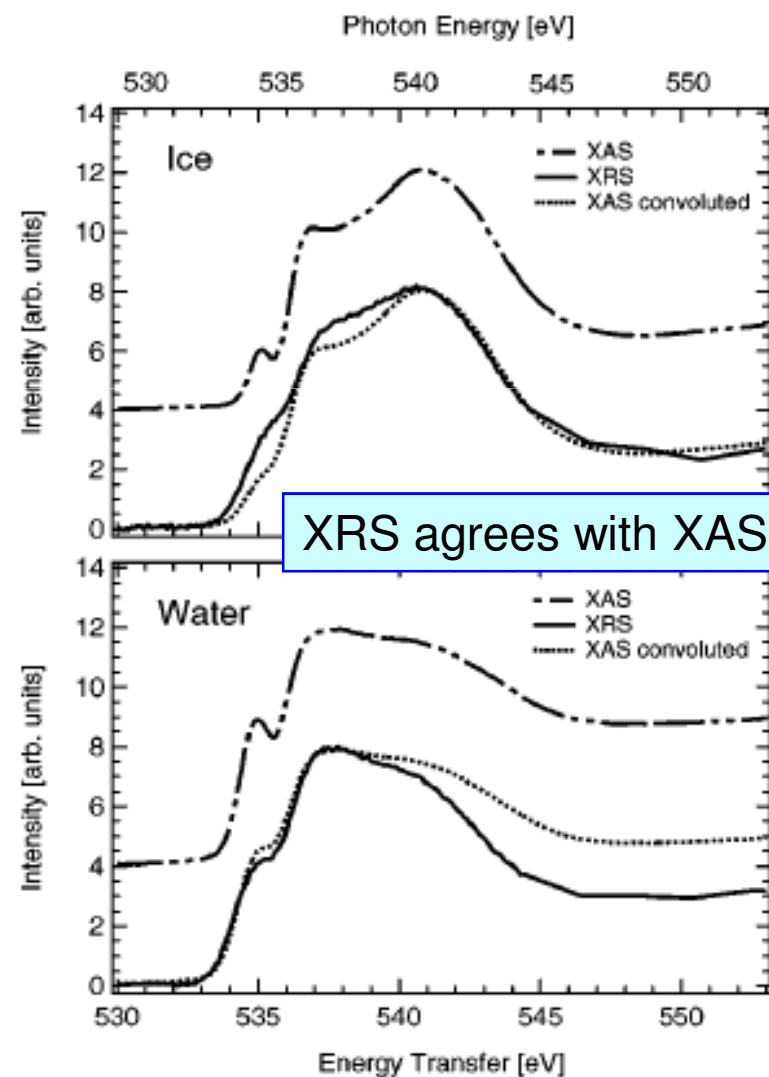
XRS from O K-edge in water and ice (XANES)

XANES sensitive to the number and “type” of hydrogen bonds (HB)



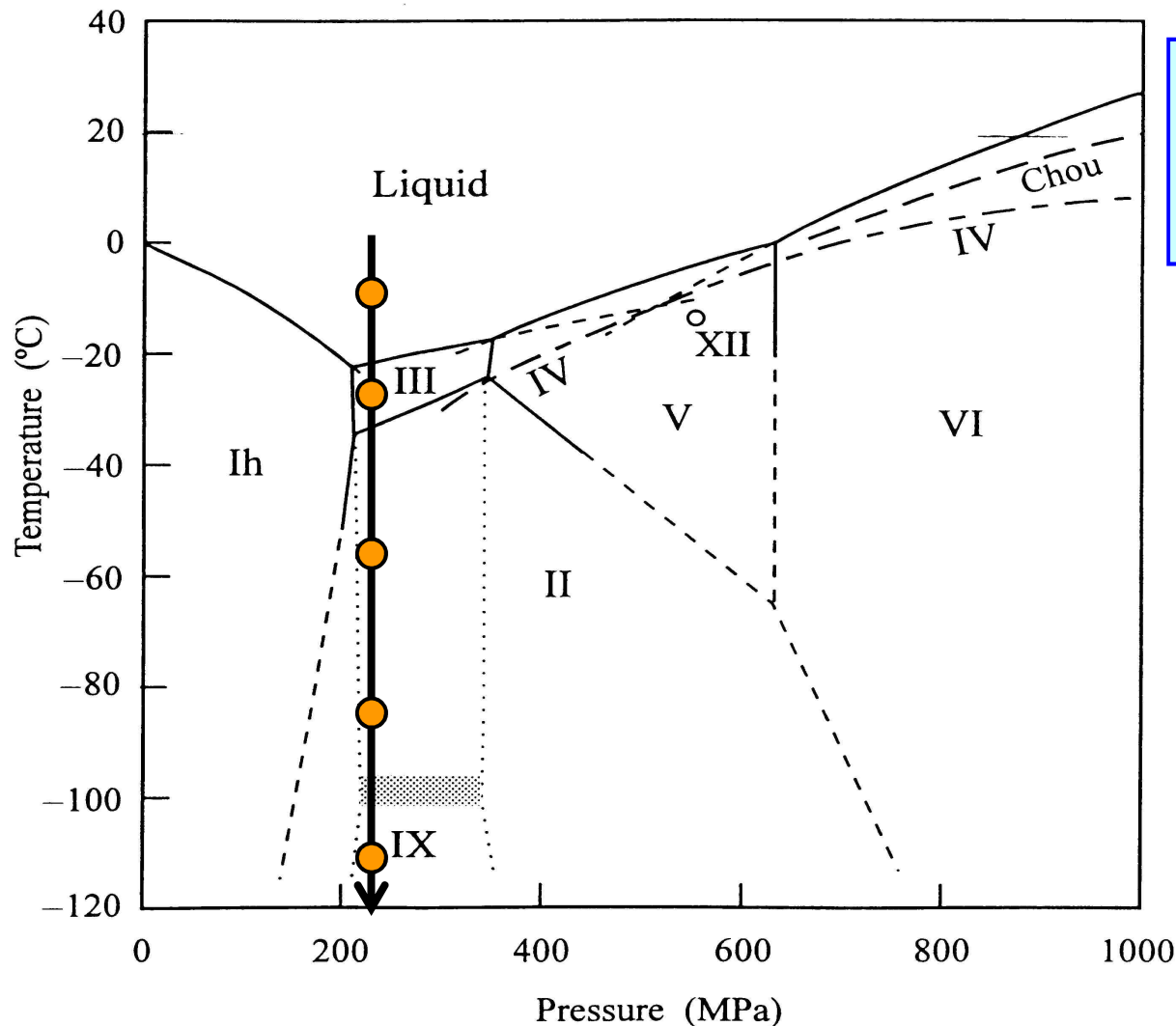
- Pre-edge indicates a large number ($\sim 70\%$) of distorted or broken HB (supported by calculation)

PRB 66, 092107 (2002)



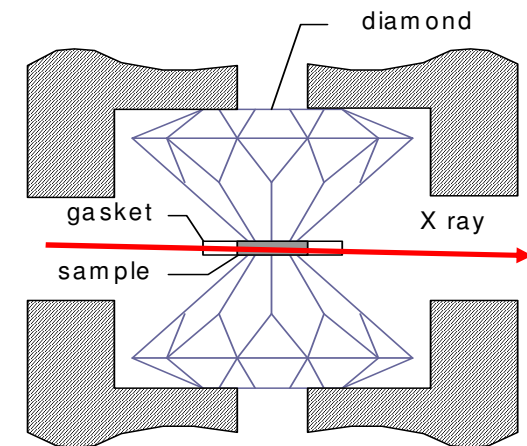
Experimental highlights (XRS)

XRS from O K-edge in ice under high pressure



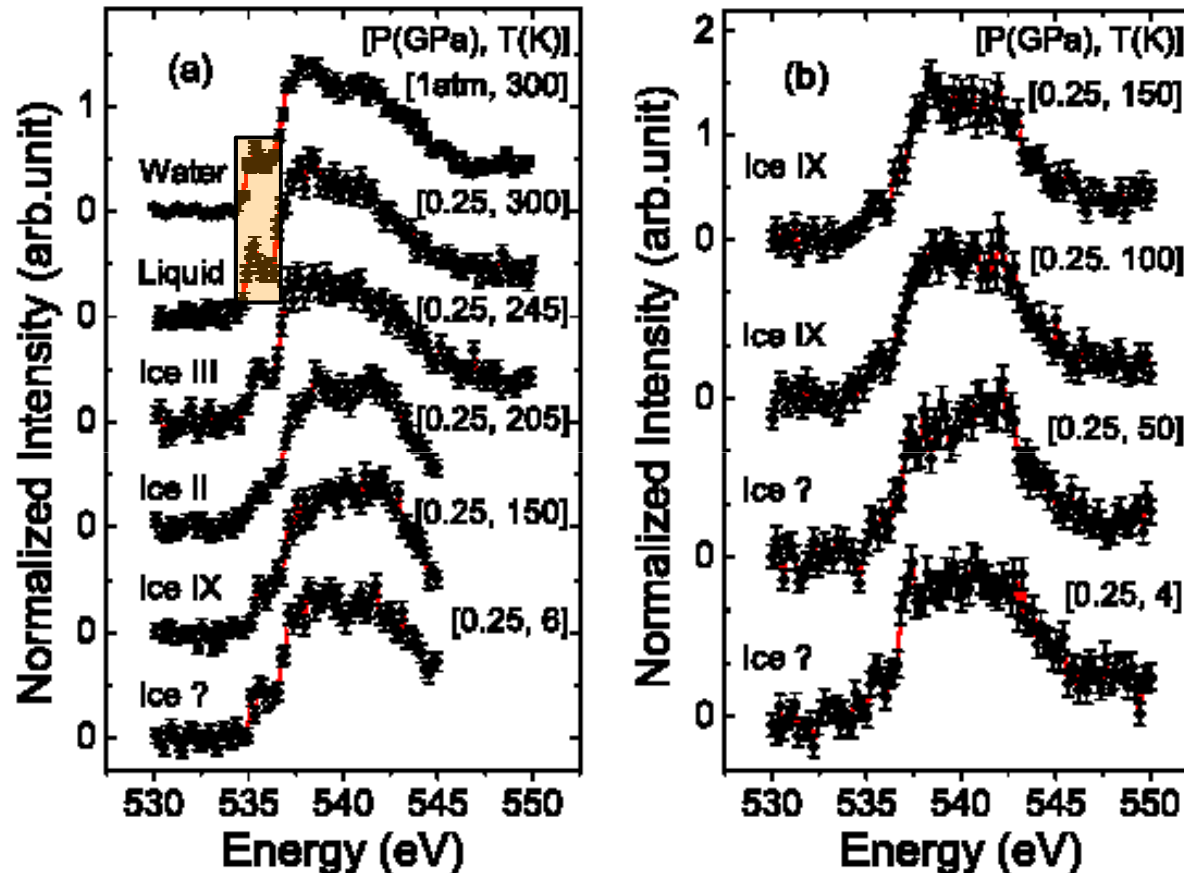
$E_{\text{out}} = 9885 \text{ eV}$
 $(\Delta E \sim 0.2 \div 0.3 \text{ eV})$
 $|\mathbf{k}| \sim 3 \text{ \AA}^{-1} (\mathbf{k} \cdot \mathbf{r} \sim 0.2)$

DAC sample
environment:
hard x-ray needed



Experimental highlights (XRS)

XRS from O K-edge in ice under high pressure



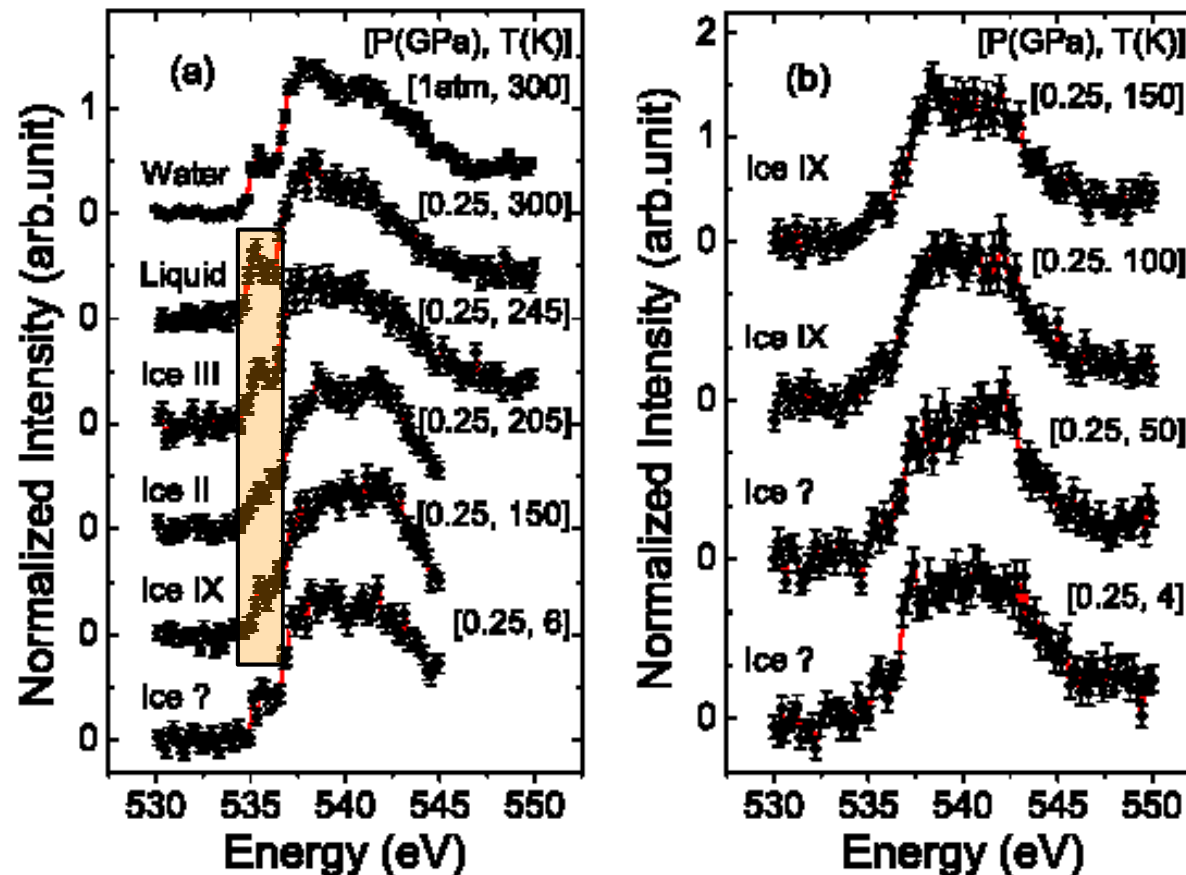
- Slight increase of pre-edge with P (larger HB distortion)
- Increasing order of HB from liquid → Ice III (tetrahedral) → Ice II / IX
- New pre-edge increase @ low-T: new Ice phase?

Observation of spectral changes:

Need of much better statistics and theory to extract quantitative information

Experimental highlights (XRS)

XRS from O K-edge in ice under high pressure



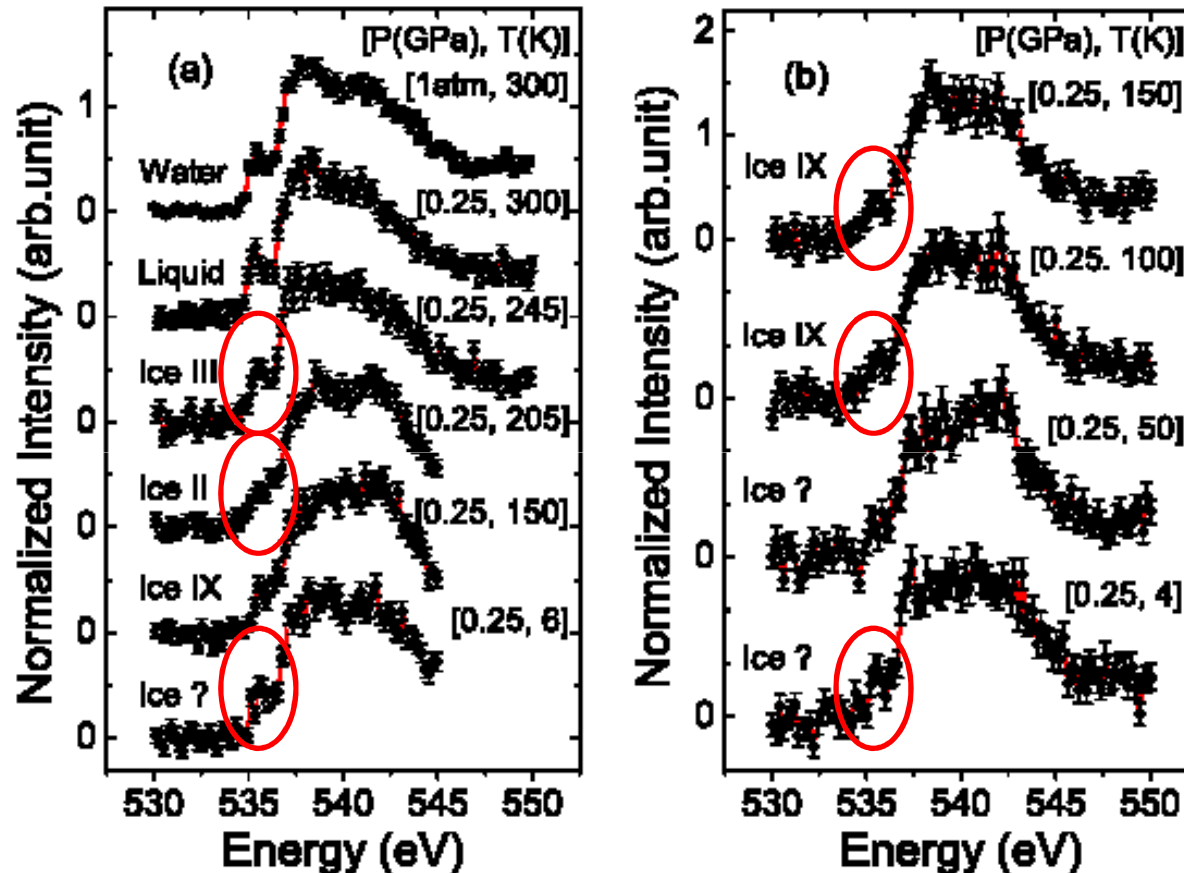
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Observation of spectral changes:

Need of much better statistics and theory to extract quantitative information

Experimental highlights (XRS)

XRS from O K-edge in ice under high pressure



- Slight increase of pre-edge with P (larger HB distortion)
- Increasing order of HB from liquid → Ice III (tetrahedral) → Ice II / IX
- New pre-edge increase @ low-T: new Ice phase?

Observation of spectral changes:

Need of much better statistics and theory to extract quantitative information

Experimental highlights (XRS)

XRS in summary:

Soft x-ray spectroscopy in the hard x-ray regime

Advantages

- “simple” sample environment (high pressure/temperature, etc...)
- bulk sensitive
- access “exotic” final states
- indicated for studying (bulk) Oxygen and Carbon

Drawbacks

- “weak probe” (practically limited to $Z < 14$)
- limited quality for structural analysis (EXAFS)
- reasonable quality in the XANES region

Exploit information in the near-edge region

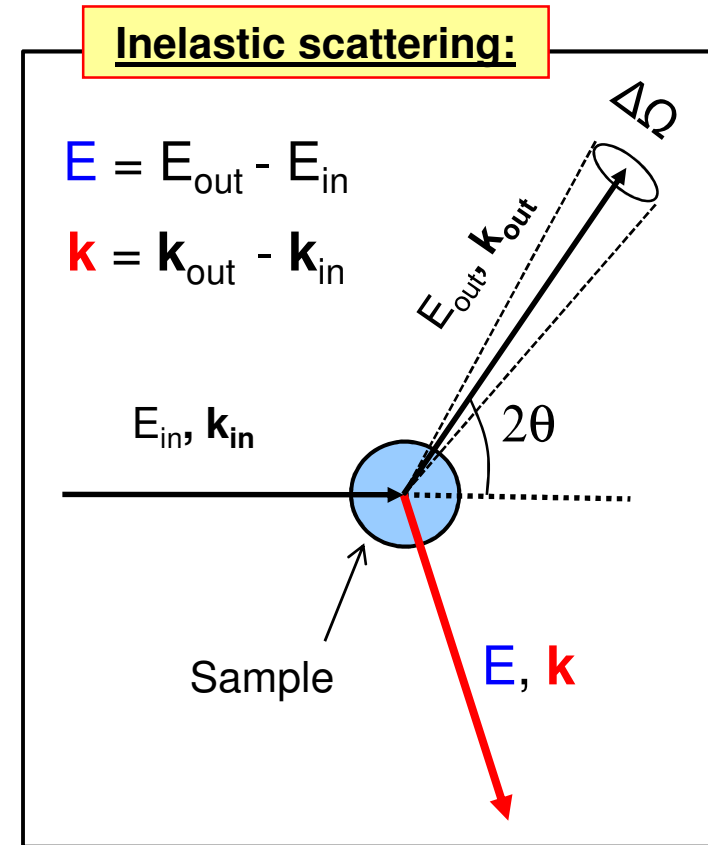
Basic theoretical aspects

$$H_{\text{int}} = (e/m_e c) \sum_j [(e/2c) \mathbf{A}_j \cdot \mathbf{A}_j + \mathbf{A}_j \cdot \mathbf{p}_j]$$

A: vector potential of electromagnetic field

P: momentum operator of the electrons

j: summation over all electrons of the system



$\mathbf{A} \cdot \mathbf{A} \rightarrow$ non-resonant scattering (IXS - XRS)

$\mathbf{A} \cdot \mathbf{p} \rightarrow$ resonant scattering, absorption followed by emission

Basic theoretical aspects

Resonant IXS cross section:

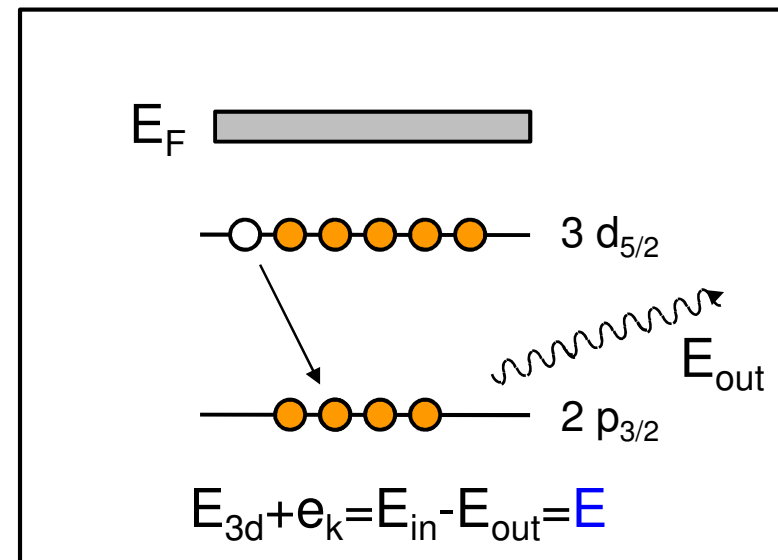
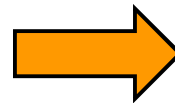
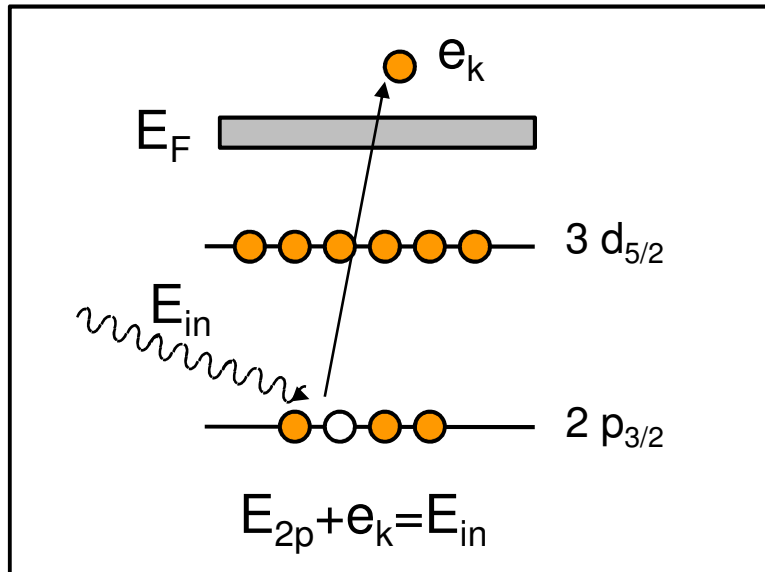
Absorption

$$\frac{\partial^2 \sigma}{\partial \Omega \partial E} \sim \sum_F \left| \sum_n \frac{\langle I | C_k | N \rangle \langle N | C_k^\dagger | F \rangle}{E_N - E_I - E_{in} - i\Gamma_N} \right|^2 \delta(E - E_F + E_I)$$

Emission

Resonant denominator

$$C_k = \sum_j (\boldsymbol{\varepsilon} \cdot \mathbf{p}_j) \exp\{i\mathbf{k} \cdot \mathbf{r}_j\}$$

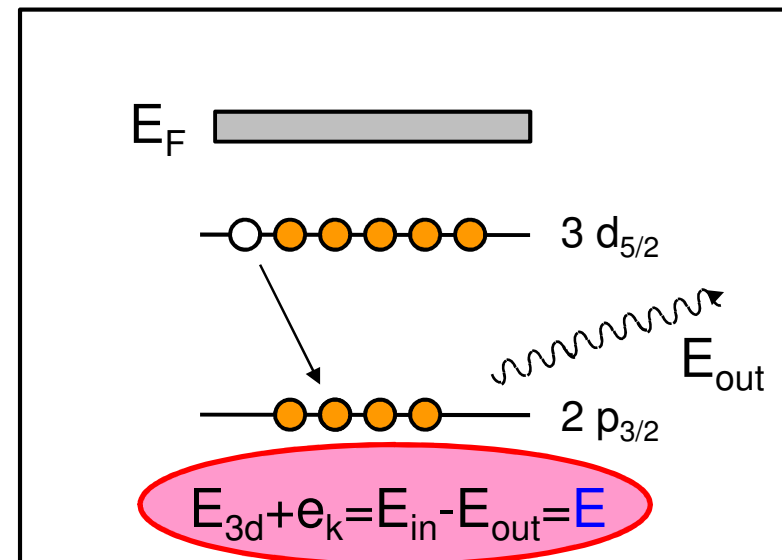
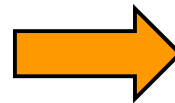
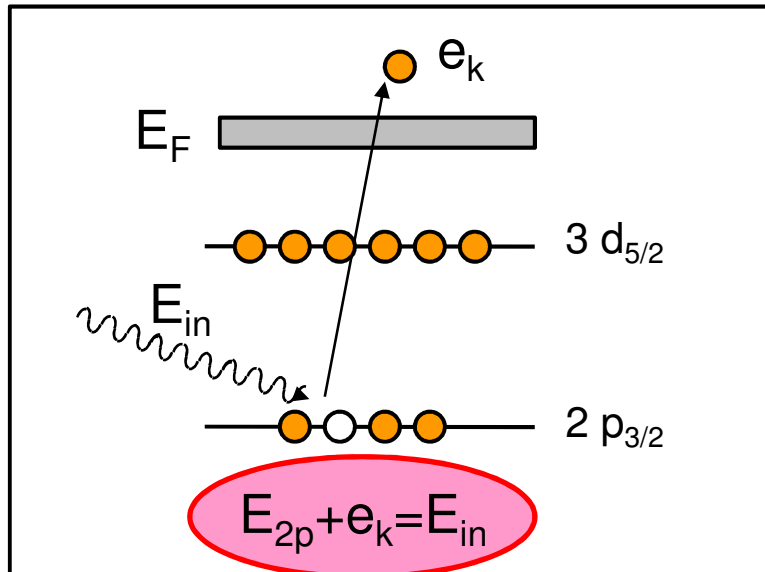


Basic theoretical aspects

Resonant IXS cross section:

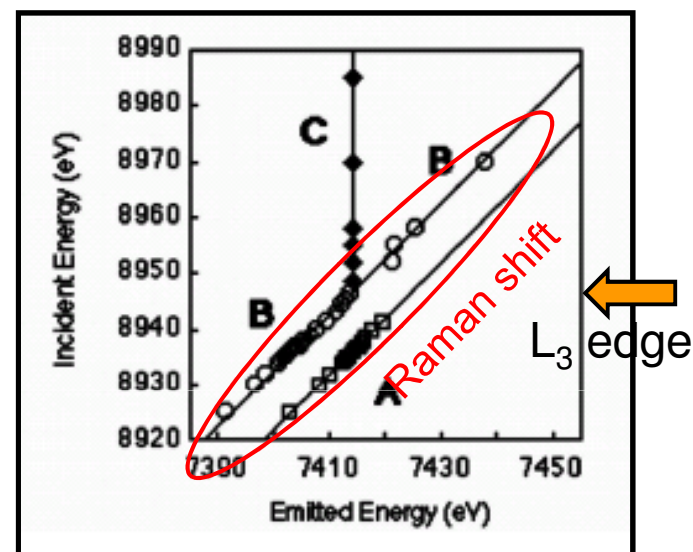
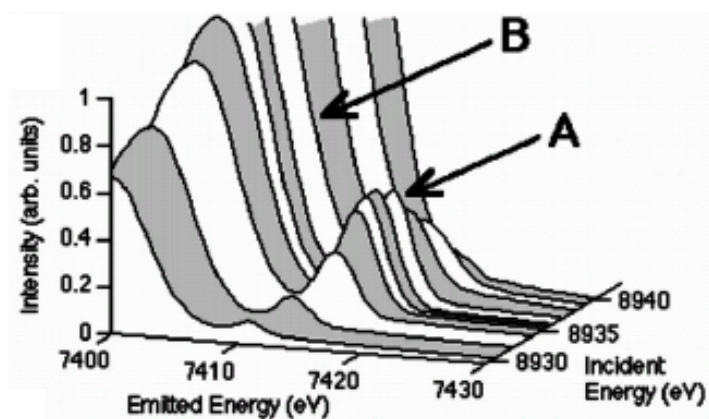
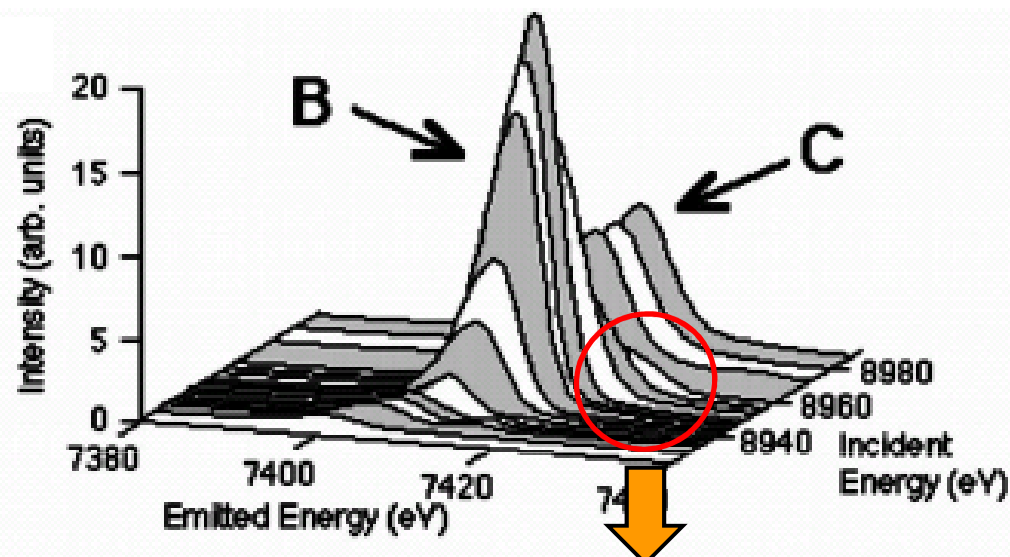
$$\frac{\partial^2 \sigma}{\partial \Omega \partial E} \sim \sum_F \left| \sum_n \frac{\langle I | C_k | N \rangle \langle N | C_k^\dagger | F \rangle}{E_N - E_I - E_{in} - i\Gamma_N} \right|^2 \delta(E - E_F + E_I)$$

Final states for XAS are intermediate for RIXS (resolution $\sim \Gamma_N$)



Experimental highlights (RIXS)

RIXS in Rare-Earths ($\text{Yb}_2\text{Fe}_{14}\text{B}$)

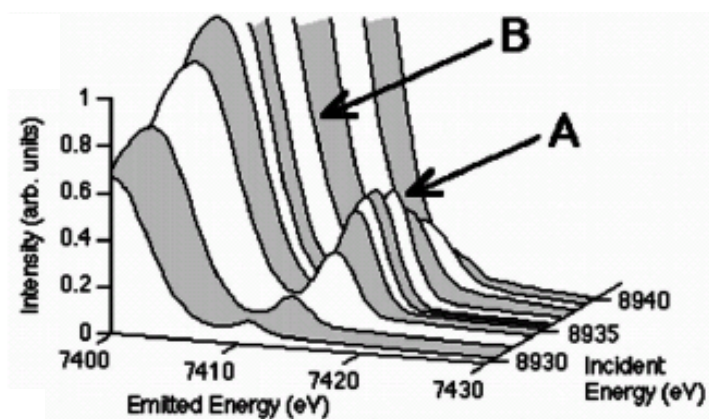
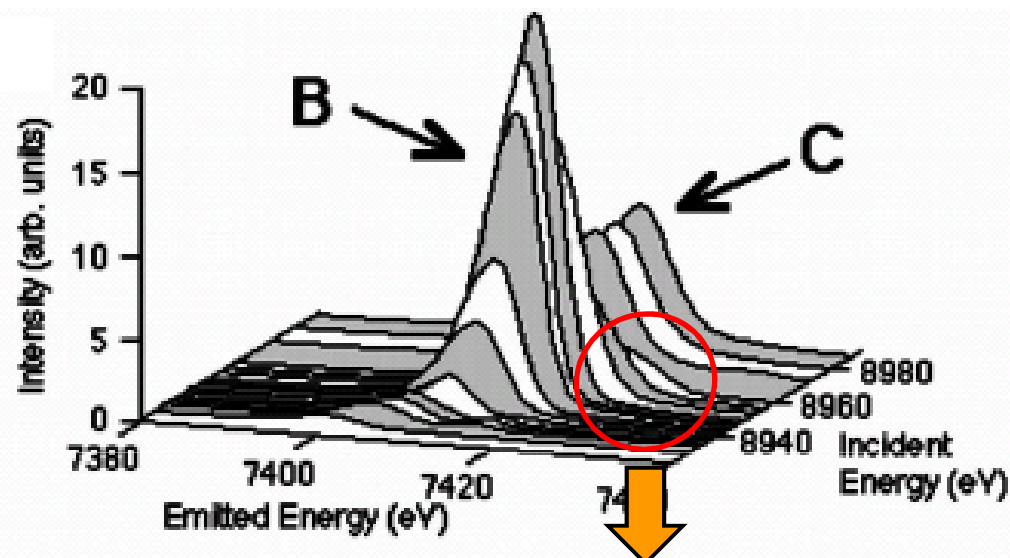


A: very weak, visible in the pre-edge region, observed at constant energy transfer ($E = E_{\text{out}} - E_{\text{in}}$)
B: strong, observed at constant E
C: cannot be separated below edge, above is observed at increasing E

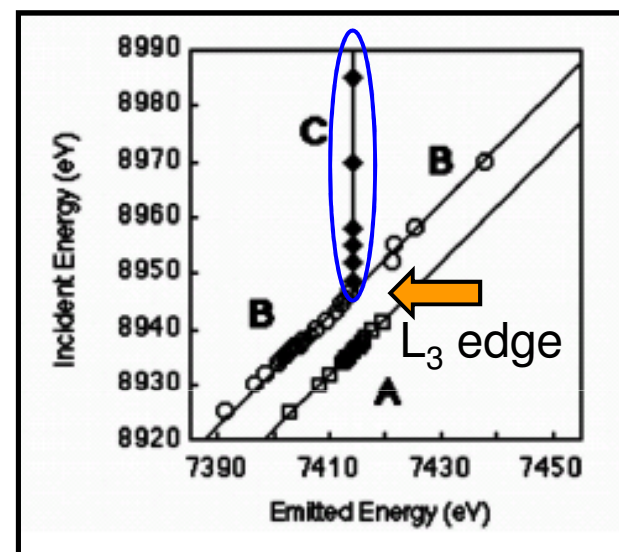
Energy resolution $\sim 3\text{-}7$ eV for Rare-Earths ($\Gamma_{3d} \ll \Gamma_{3d}$)

Experimental highlights (RIXS)

RIXS in Rare-Earths ($\text{Yb}_2\text{Fe}_{14}\text{B}$)



Fluorescence

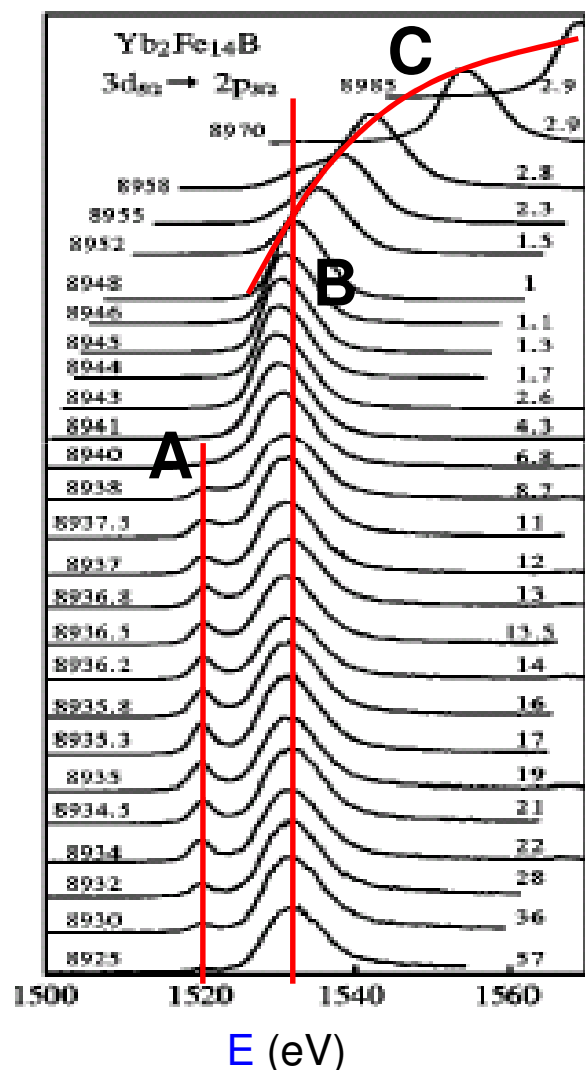


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Energy resolution $\sim 3\text{-}7$ eV for Rare-Earths ($\Gamma_{3d} \ll \Gamma_{3d}$)

Experimental highlights (RIXS)

RIXS in Rare-Earths ($\text{Yb}_2\text{Fe}_{14}\text{B}$)



Ground: $|4f^{13}d^{n^*}\rangle$

A: Quadrupolar: $2p \rightarrow 4f$ channel

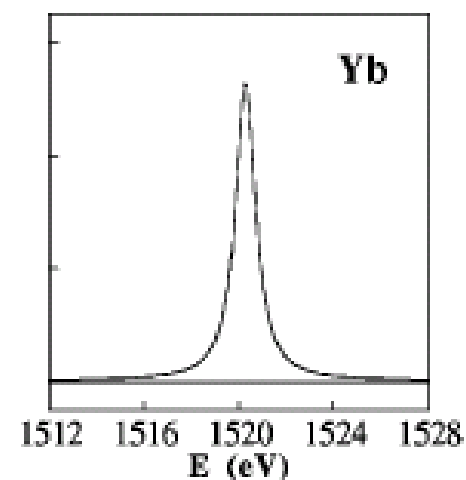
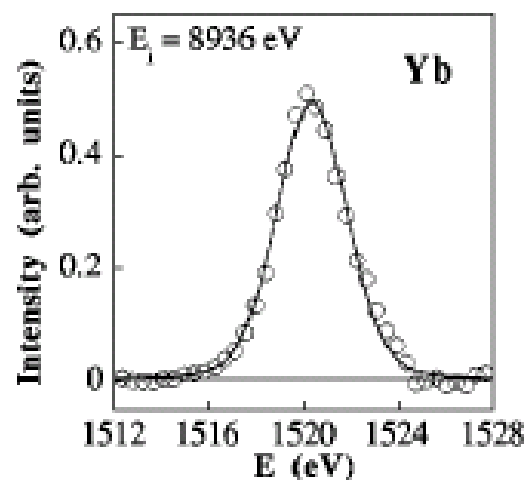
$|N\rangle = |2p^5 4f^{14} 5d^{n^*}\rangle \rightarrow |F\rangle = |3d^9 4f^{14} 5d^{n^*}\rangle$

B: Dipolar: $2p \rightarrow 5d$ channel

$|N\rangle = |2p^5 4f^{13} 5d^{n^*+1}\rangle \rightarrow |F\rangle = |3d^9 4f^{13} 5d^{n^*+1}\rangle$

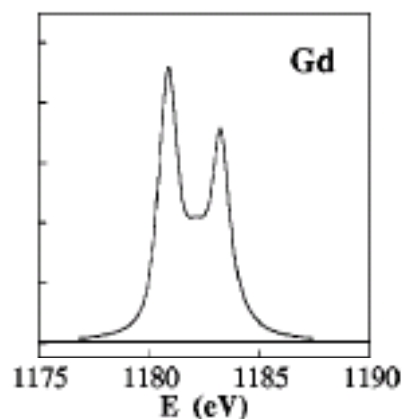
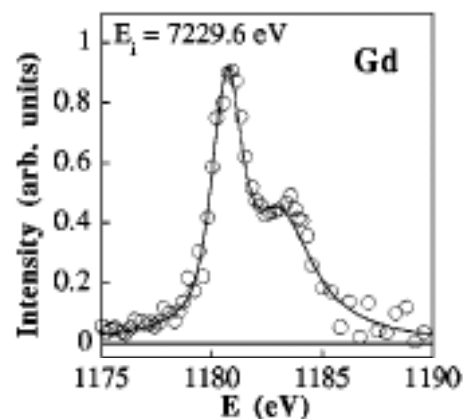
C: $L_{\alpha 1}$ fluorescence: $2p \rightarrow \text{continuum}$

Quadrupolar excitation (A):
agreement calculations



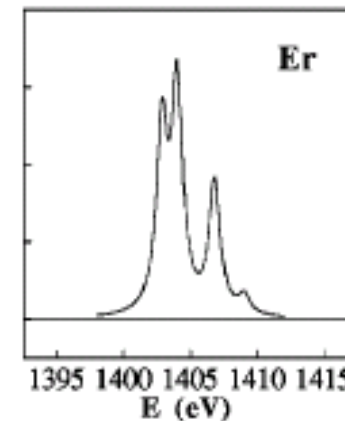
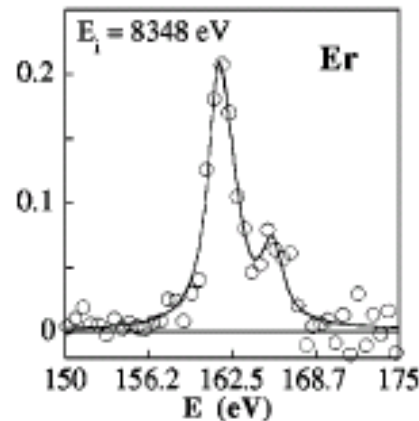
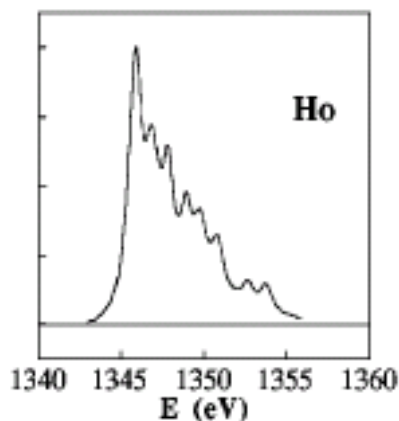
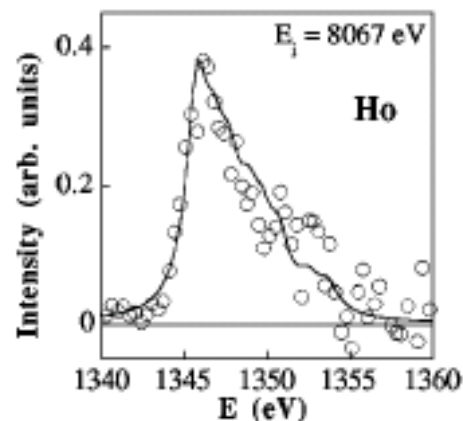
Experimental highlights (RIXS)

RIXS in Rare-Earths (quadropolar $2p \rightarrow 4f$)



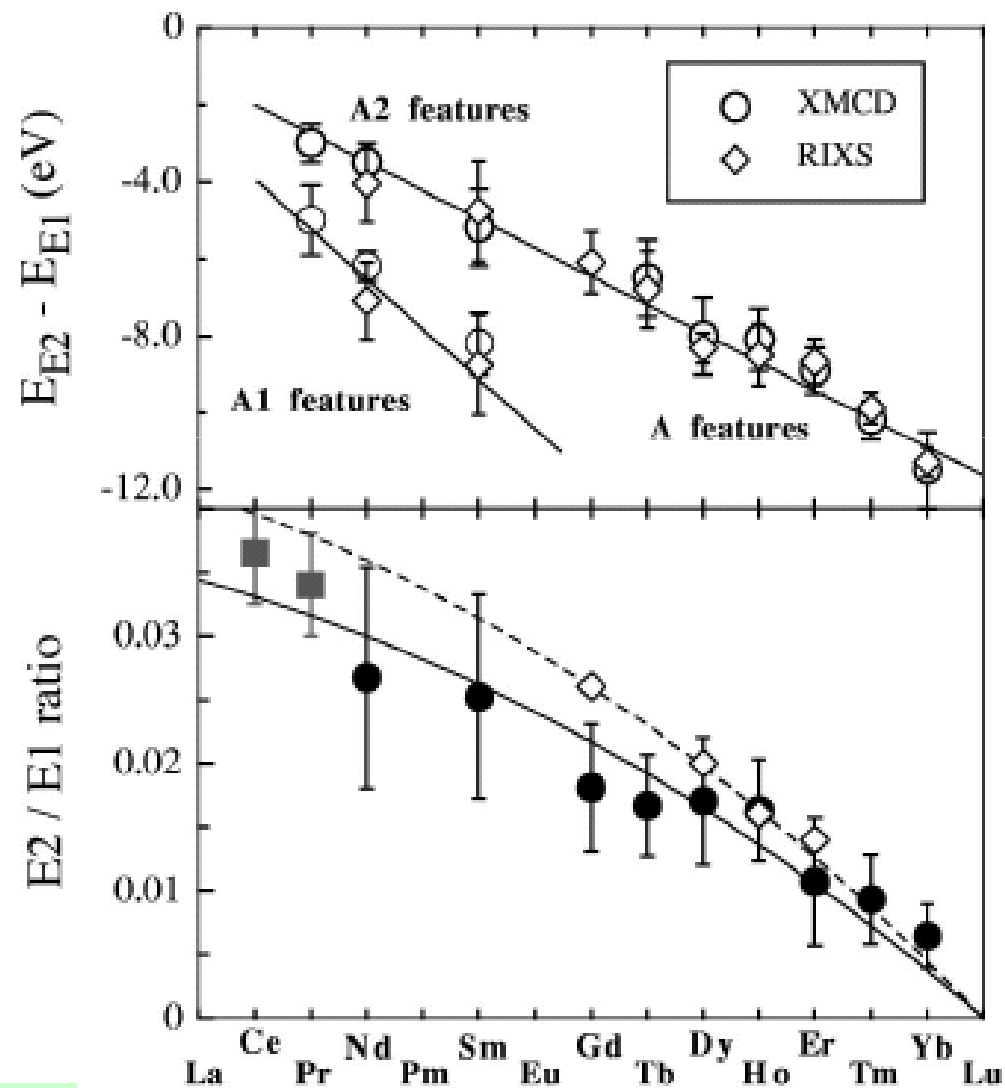
RIXS data vs. Theory:

The shape of quadrupolar $2p \rightarrow 4f$ transition agrees with calculations



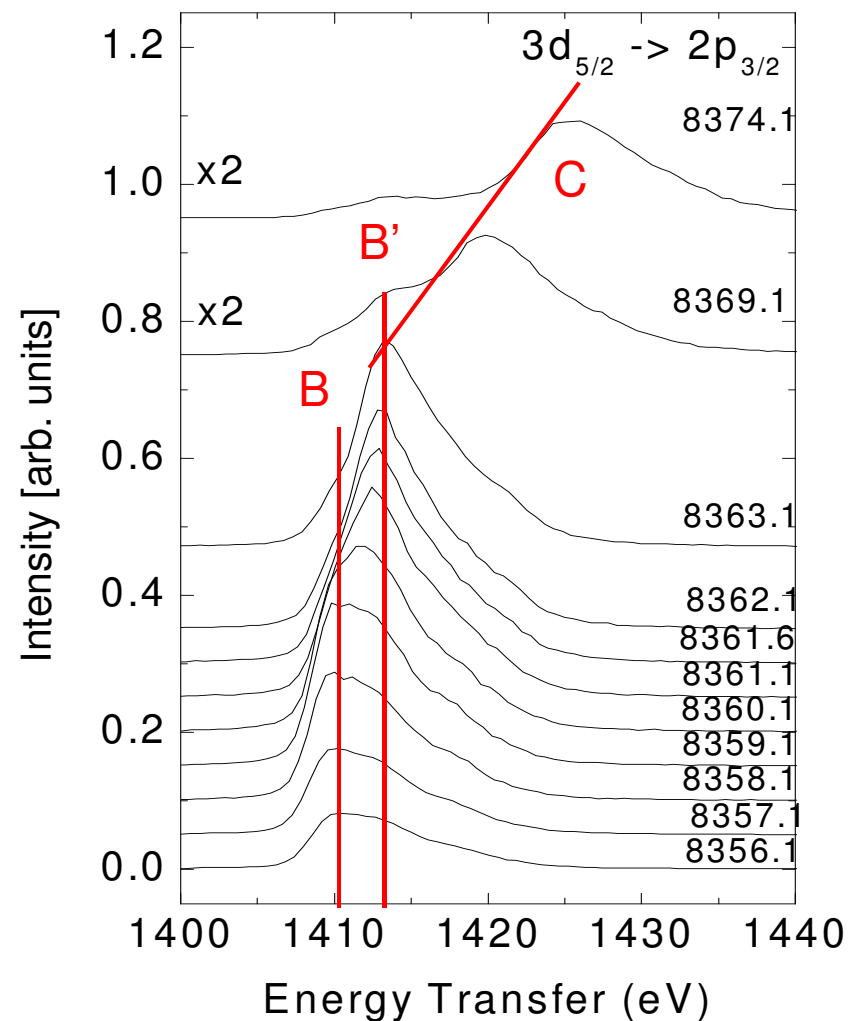
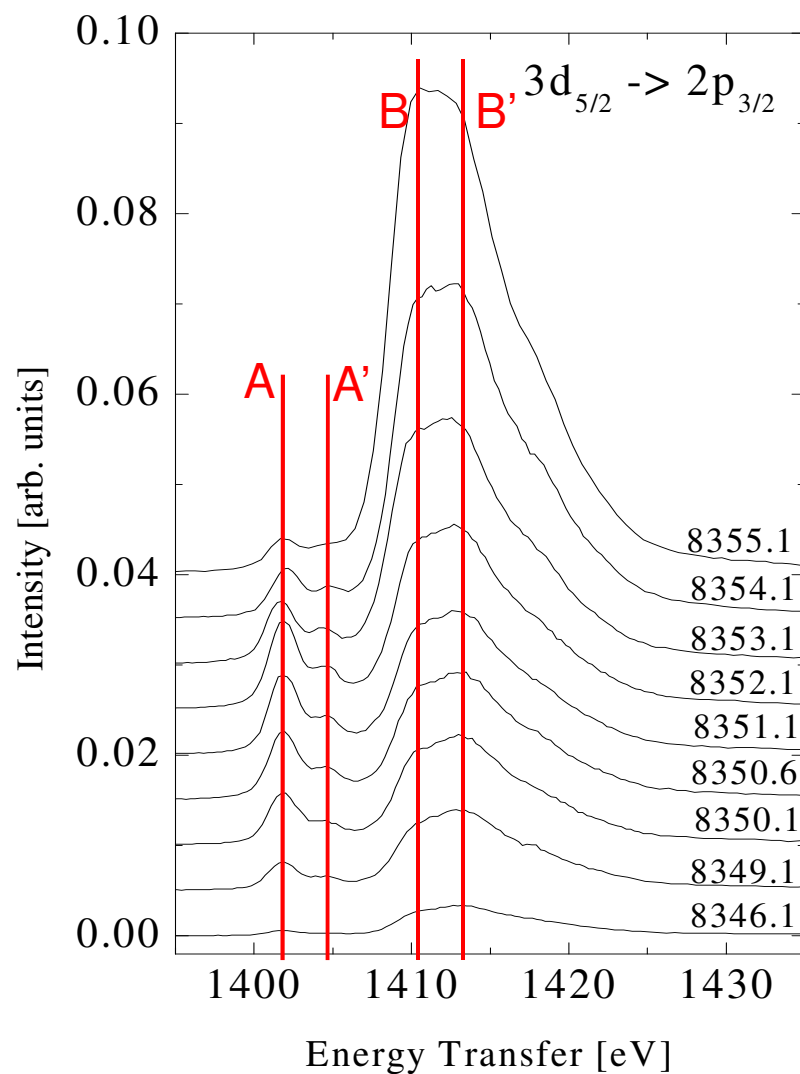
Experimental highlights (RIXS)

RIXS in Rare-Earths (quadropolar $2p \rightarrow 4f$)



Experimental highlights (RIXS)

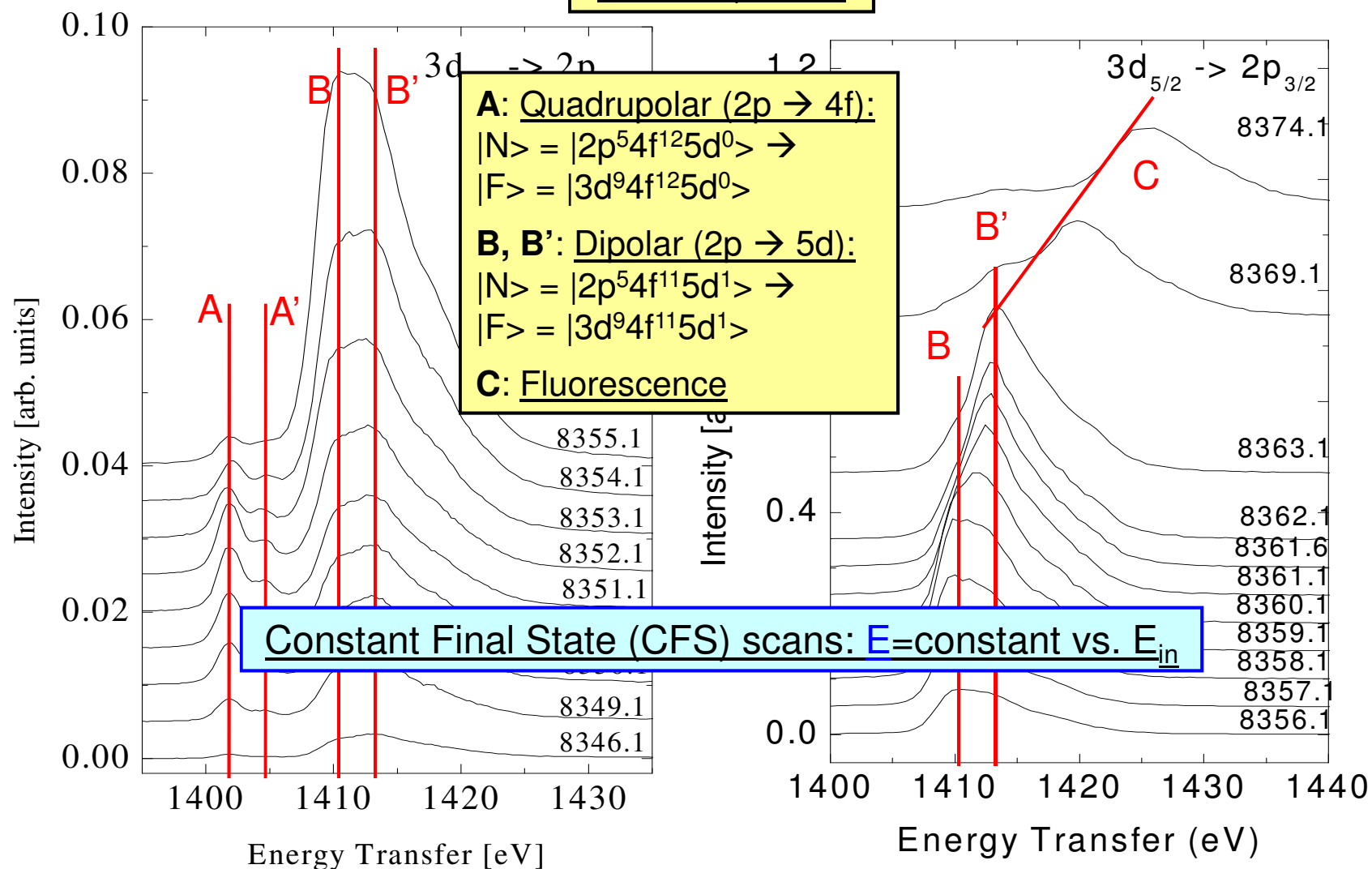
RIXS in Rare-Earths (Er_2O_3)



Experimental highlights (RIXS)

RIXS in Rare-Earths (Er_2O_3)

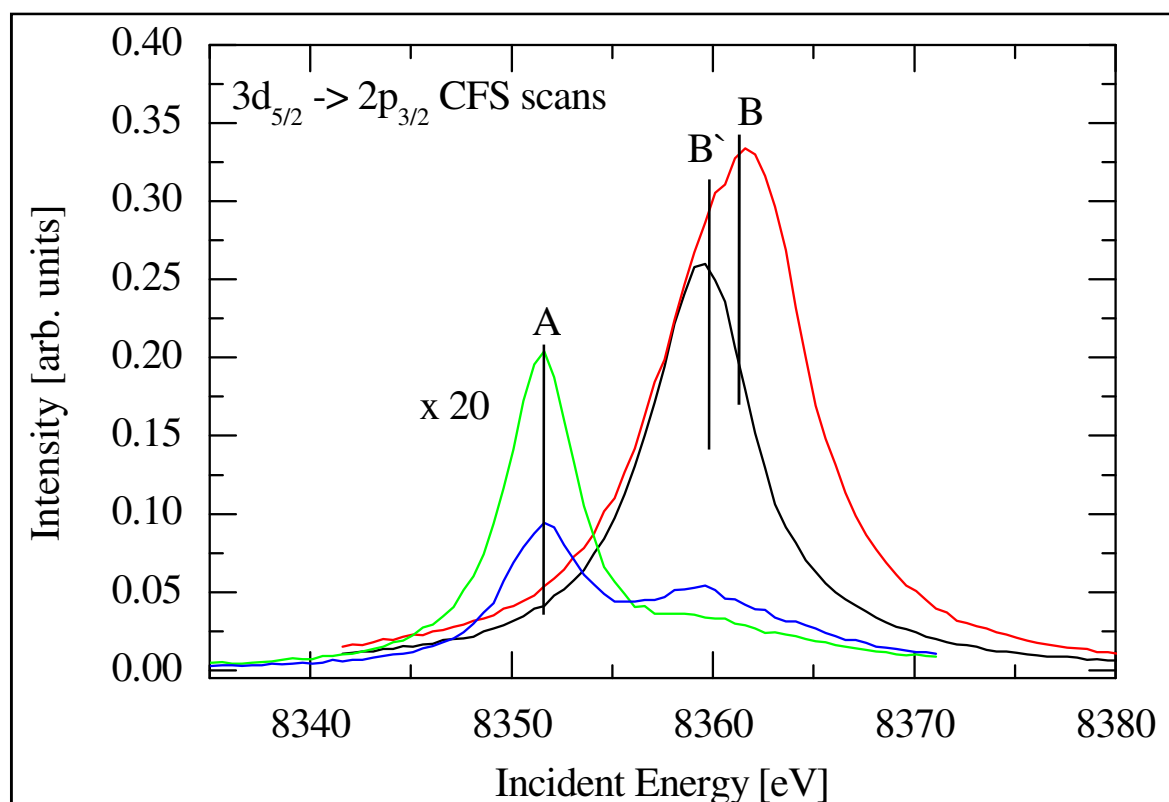
Ground: $|4f^{11}d^0\rangle$



Experimental highlights (RIXS)

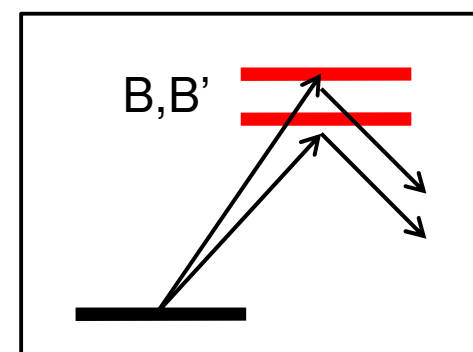
RIXS in Rare-Earths (Er_2O_3)

Constant final state scans: $E = \text{constant}$ & E_{in} through the absorption edge



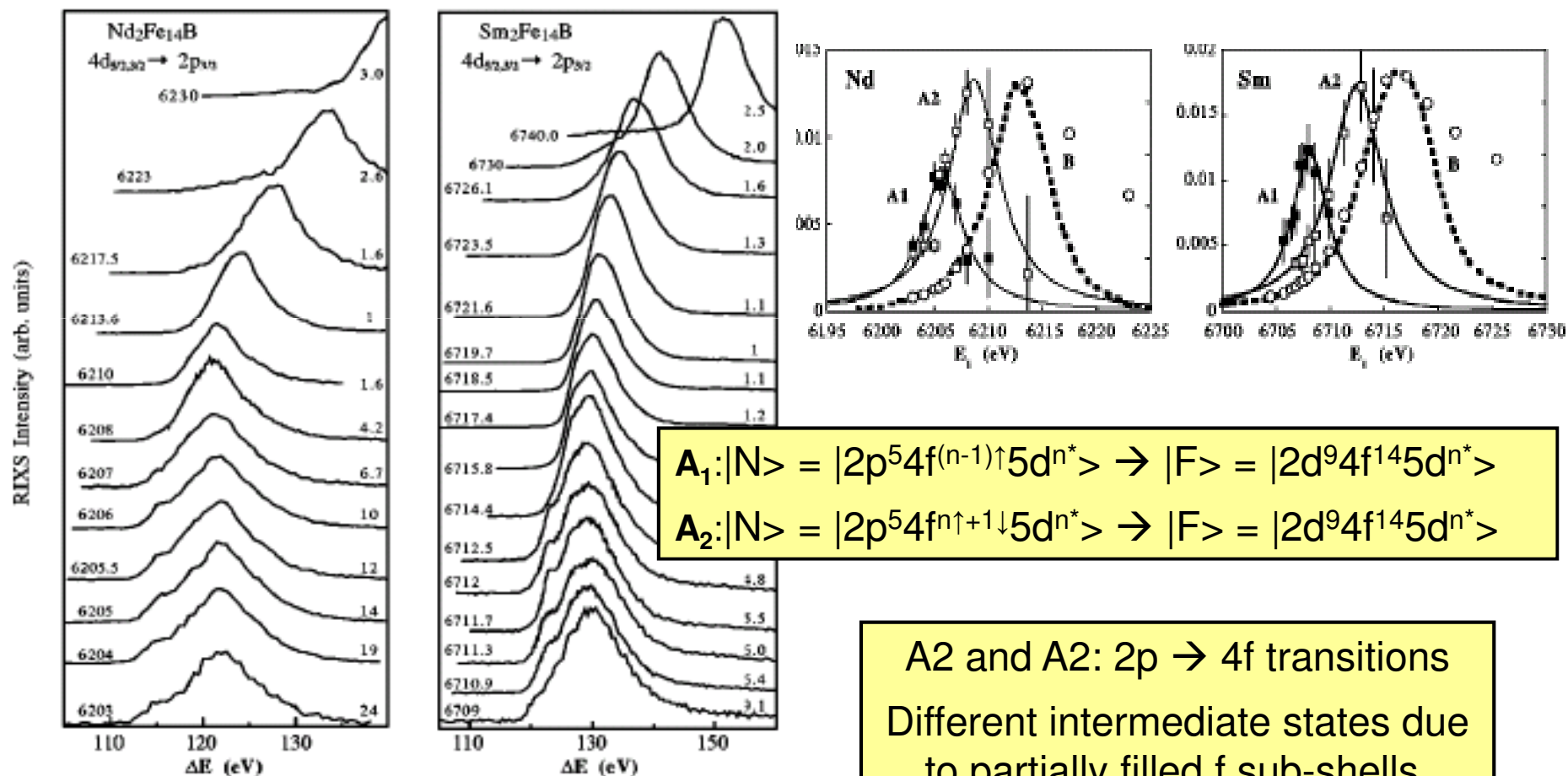
B and B*: $2p \rightarrow 5d$ dipolar transitions. Different intermediate states, cubic field splitting of the 5d states: $\Delta E = 2.3 \text{ eV}$

A and A*: $2p \rightarrow 4f$. Same intermediate state



Experimental highlights (RIXS)

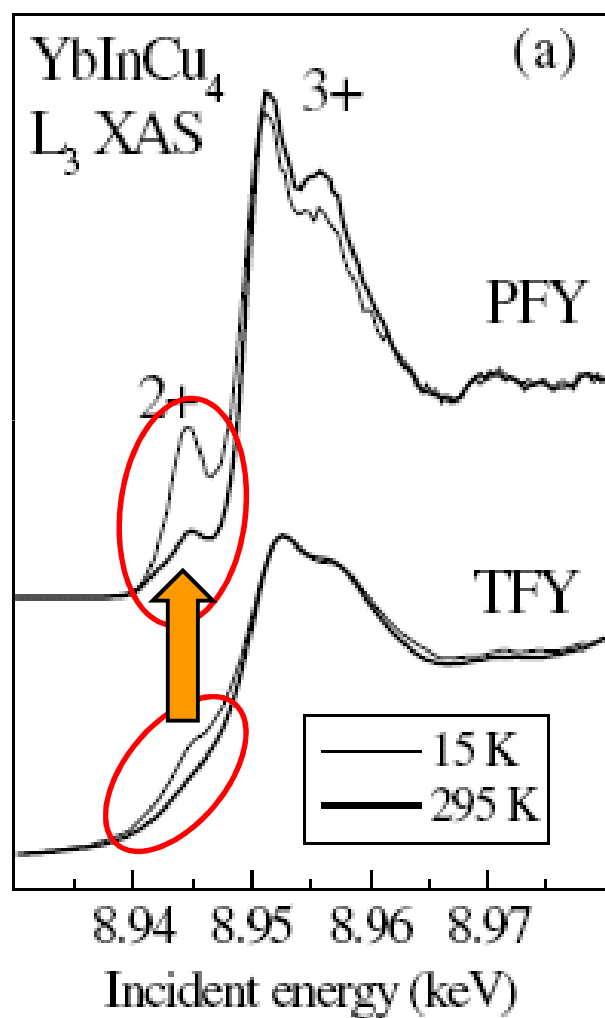
RIXS in Rare-Earths (Nd & Sm)



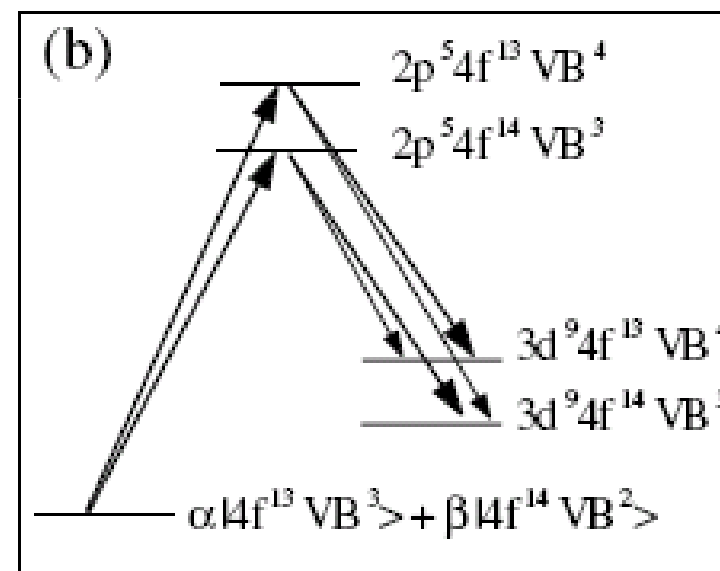
A2 and A2: 2p → 4f transitions
Different intermediate states due to partially filled f sub-shells.
Compatible with calculations and with XMCD results

Experimental highlights (RIXS)

RIXS in Rare-Earths (valence transition)



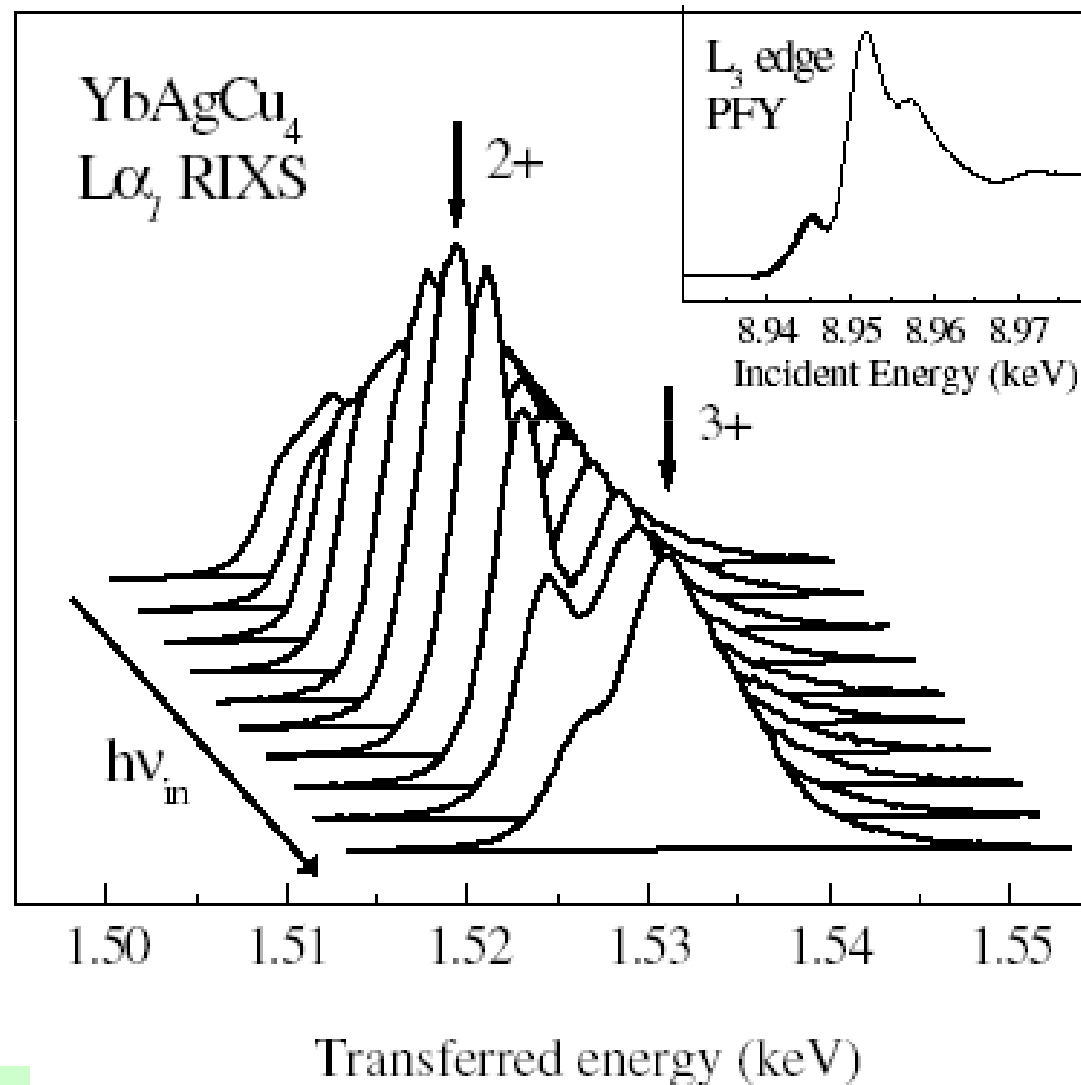
- Mixed ground state (Yb^{2+} ; Yb^{3+})
- Pre-edge $\rightarrow$ larger Yb^{2+} at low-T
- XAS final = RIXS intermediate



Weak Yb^{2+} feature can be resonantly enhanced: possible to study T-dependence

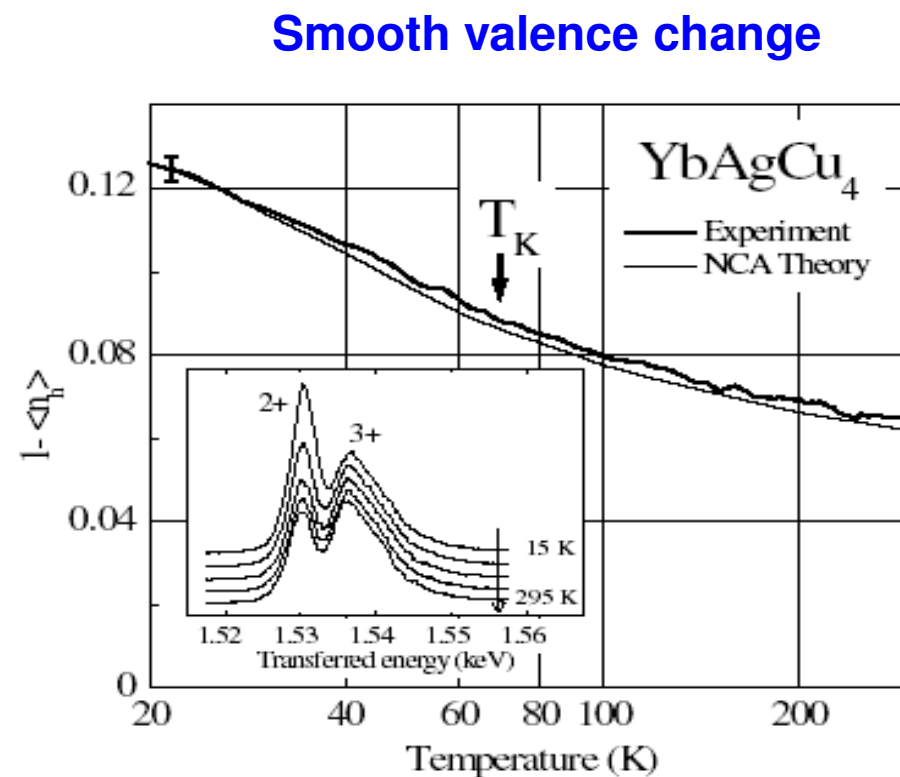
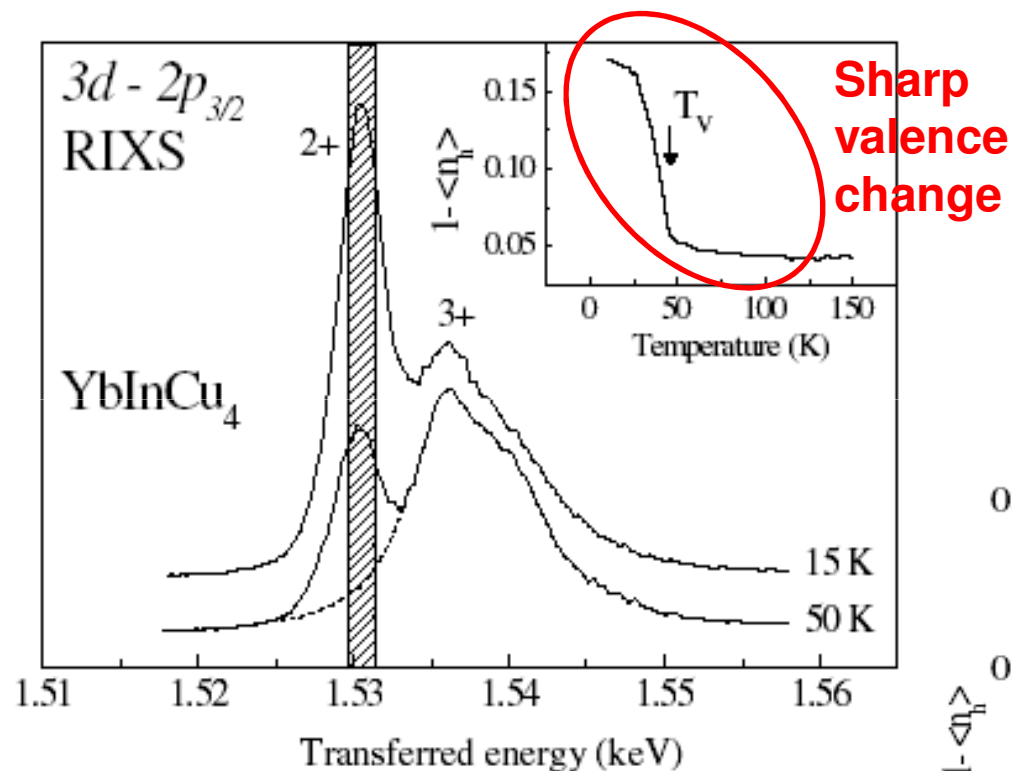
Experimental highlights (RIXS)

RIXS in Rare-Earths (valence transition)



Experimental highlights (RIXS)

RIXS in Rare-Earths (valence transition)



Experimental highlights (RIXS)

RiXS in summary:

Final state core-hole lifetime $<$ energy separation of the multiplet families



RIXS allows the separation of different excitation channels which are obscured in a standard absorption measurement

Keeping E fixed and tuning E_{in} through edge (CFS scan)



Resonant enhancement of “subtle” intermediate states