

Outline

Surface, interface, and nanoscience—short introduction

Some surface/interface concepts and techniques

**Experimental aspects:
intro. to laboratory-based and SR-based**

 **Electronic structure—a brief review**

**The basic synchrotron radiation techniques:
more experimental and theoretical details**

Core-level photoemission

Valence-level photoemission

What properties do wave functions of overlapping (thus indistinguishable) particles have?—electrons as example:



$\psi = \psi(\vec{r}_1, \vec{s}_1; \vec{r}_2, \vec{s}_2)$, including spin of both electrons

But labels can't affect any measurable quantity.

E.g. – probability density :

$$|\psi(\vec{r}_1, \vec{s}_1; \vec{r}_2, \vec{s}_2)|^2 = |\psi(\vec{r}_2, \vec{s}_2; \vec{r}_1, \vec{s}_1)|^2$$

Therefore

$$\begin{aligned} \psi(\vec{r}_1, \vec{s}_1; \vec{r}_2, \vec{s}_2) &= \pm 1 \psi(\vec{r}_2, \vec{s}_2; \vec{r}_1, \vec{s}_1) \\ &\equiv \hat{P}_{12} \psi(\vec{r}_1, \vec{s}_1; \vec{r}_2, \vec{s}_2) \end{aligned}$$

with \hat{P}_{12} = permutation operator $\rightarrow \vec{r}_1, \vec{s}_1; \vec{r}_2, \vec{s}_2$
and eigenvalues of ± 1

Finally, all particles in two classes :

FERMIONS : (incl. e^- 's) : ψ antisymmetric

$$s = \frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \dots$$

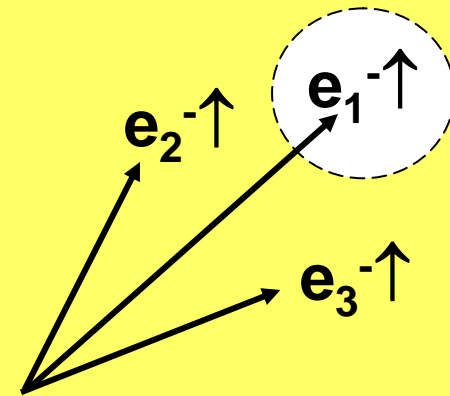
$$\hat{P}_{12} \psi = -1 \psi$$

BOSONS : (incl. photons) : ψ symmetric

$$s = 0, 1, 2, \dots$$

$$\hat{P}_{12} \psi = +1 \psi$$

Probability of finding two electrons at the same point in space with the same spin is zero: “the Fermi Hole”



→the Exchange Interaction

→Hund's 1st rule & magnetism

A first try at many-electron wave functions:
The Hartree-Fock Method

Assume N-electron, P nucleus wave function to be:

$\Psi \approx \Phi = \text{Slater determinant}$

$$= \frac{1}{\sqrt{N!}} \begin{pmatrix} \phi_1(\vec{r}_1)\chi_1(\sigma_1) & \dots & \phi_N(\vec{r}_1)\chi_N(\sigma_1) \\ \vdots & \ddots & \vdots \\ \phi_1(\vec{r}_N)\chi_1(\sigma_N) & \dots & \phi_N(\vec{r}_N)\chi_N(\sigma_N) \end{pmatrix} \quad (35a)$$

↗ space: like 1s, 2s, ...
↘ spin: $\alpha(\uparrow)$ or $\beta(\downarrow)$

and also require orthonormality of one-electron orbitals

$$\int \phi_i^*(\vec{r})\phi_j(\vec{r})dV = \delta_{ij}$$

Minimize total energy → Hartree-Fock equations:

$$\hat{H}(\vec{r}_1)\phi_i(\vec{r}_1) = \varepsilon_i\phi_i(\vec{r}_1); i = 1, 2, \dots, N \quad (42)$$

with:

$$\varepsilon_i = \varepsilon_i^0 + \sum_{j=1}^N J_{ij} - \delta_{m_{s_i}, m_{s_j}} K_{ij} \quad (47)$$

↑↑ or ↓↓

→ One-electron energies or eigenvalues
 ≈ binding energy → Koopmans' Theorem

One-electron integral:

$$\varepsilon_i^0 = \left\langle \phi_i(\vec{r}_1) \left| -\frac{1}{2}\nabla_1^2 - \sum_{\ell=1}^P \frac{Z_\ell}{r_{1\ell}} \right| \phi_i(\vec{r}_1) \right\rangle \quad (48)$$

Two-electron coulomb integral:

$$J_{ij} \equiv \left\langle \phi_i(\vec{r}_1) \left| \hat{J}_j \right| \phi_i(\vec{r}_1) \right\rangle = \iint \phi_i^*(\vec{r}_1)\phi_j^*(\vec{r}_2) \frac{1}{r_{12}} \phi_i(\vec{r}_1)\phi_j(\vec{r}_2)dV_1dV_2 \quad (45)$$

Two-electron exchange integral:

$$K_{ij} \equiv \left\langle \phi_i(\vec{r}_1) \left| \hat{K}_j \right| \phi_i(\vec{r}_1) \right\rangle = \iint \phi_i^*(\vec{r}_1)\phi_j^*(\vec{r}_2) \frac{1}{r_{12}} \phi_j(\vec{r}_1)\phi_i(\vec{r}_2)dV_1dV_2 \quad (46)$$

Lowers energy — "attractive"

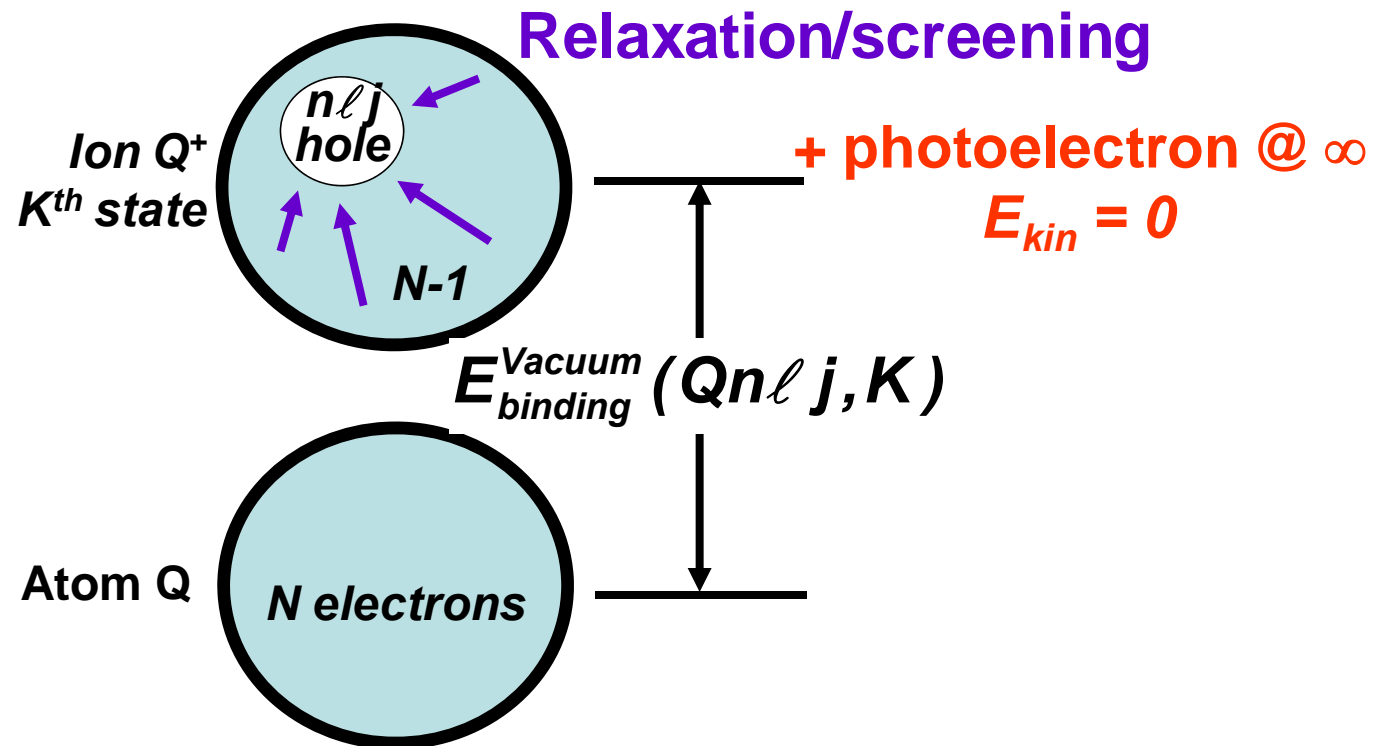
Paper [1]--Basic Concepts of XPS

Note-- K_{ij} often J_{ij} in solid-state

Basic energetics—Many e⁻ picture

$$h\nu = E_{\text{binding}}^{\text{Vacuum}} + E_{\text{kinetic}} = E_{\text{binding}}^{\text{Fermi}} + \varphi_{\text{spectrometer}} + E_{\text{kinetic}}$$

$$E_{\text{binding}}^{\text{Vacuum}}(Qn\ell j, K) = E_{\text{final}}(N-1, Qn\ell j \text{ hole}, K) - E_{\text{initial}}(N)$$



What does the hole do?

BINDING ENERGIES + KOOPMANS' THEOREM:

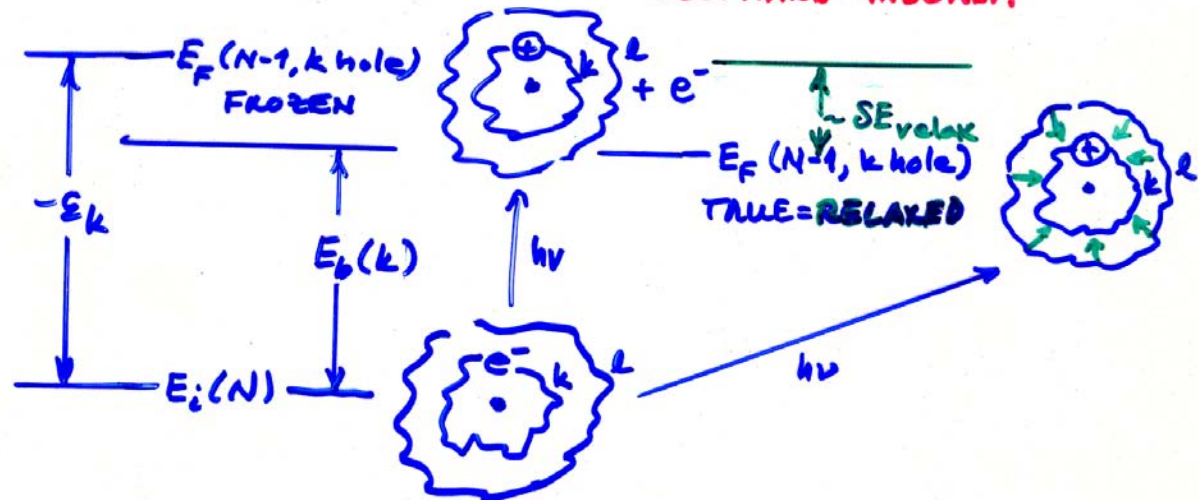
$N-e^-$ SCH. EQN. — $\hat{H}(N)\Psi_j(N) = E_j(N)\Psi_j(N), j=1,2,\dots$
 MINIMIZE $E_j(N) \left\{ \begin{array}{l} \Psi_j \approx \Phi_j = \text{SLATER DET.} \end{array} \right.$

N $1-e^-$ HARTREE-FOCK EQNS. — $\hat{H}(1)\varphi_k(1) = \epsilon_k(1)\varphi_k(1)$

- COUPLED INTEGRO-DIFF.
- COULOMB + EXCHANGE

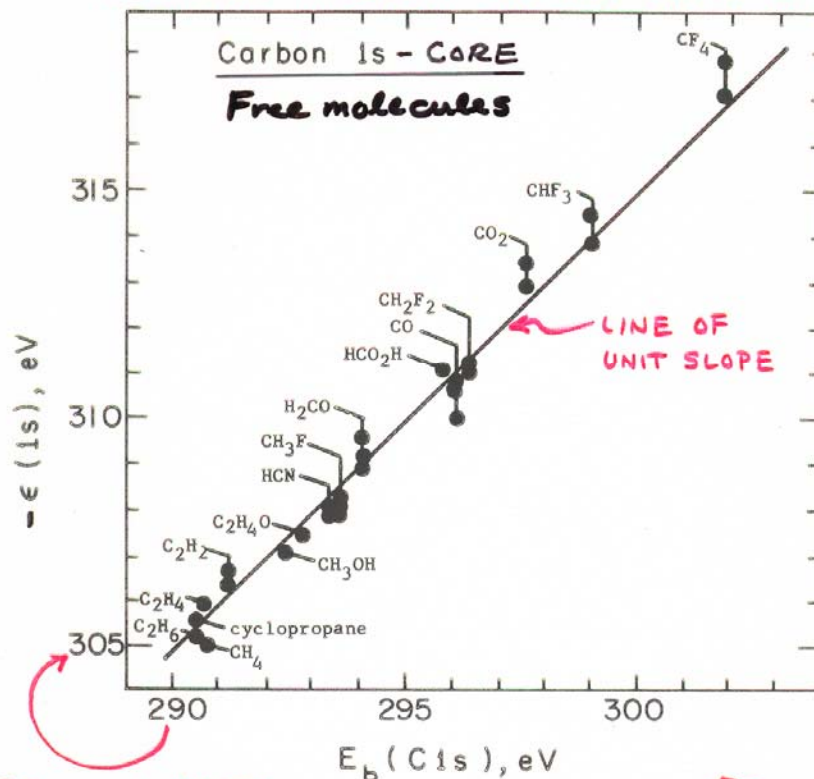
$E_b(k) = k^{\text{th}}$ BINDING ENERGY = $E_f(N-1, k \text{ hole}) - E_i(N)$
 (+) EXACT
 OR $E_b(k) = -\epsilon_k$ IF $\varphi_{ki} = \varphi_{kf}$ (FROZEN ORBITAL)

KOOPMANS' THEOREM



\Rightarrow RELAXATION, SCREENING, CONFIGURATION INTERACTION, SELF-ENERGY EFFECTS ALWAYS PRESENT; ANDERSON IMPURITY MODEL ETC.

KOOPMANS' THEOREM CALCULATION OF SHIFTS



DIFF. = $\Delta E_{relax} \approx 15 \text{ eV} \approx \text{CONSTANT} \approx 5\% \text{ OF } E_b^V$

$\Delta E_b(\text{C } 1s, "1" - \text{CH}_4) = -\Delta E_{\text{C } 1s, "1" - \text{CH}_4}$

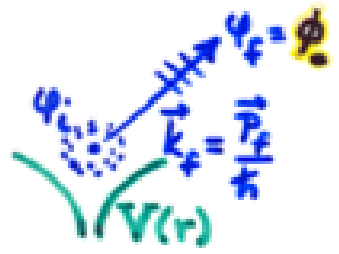
Figure 18 -- Plot of carbon 1s binding energies calculated via Koopmans' Theorem against experimental binding energies for several carbon-containing gaseous molecules. For some molecules, more than one calculated value is presented. The slope of the straight line is unity. The two scales are shifted with respect to one another by 15 eV, largely due to relaxation effects. All of the theoretical calculations were of roughly double-zeta accuracy or better. (From Shirley, reference 7.)

PHOTOELECTRON EMISSION-
BASIC MATRIX ELEMENTS + SELECTION RULES:

• ATOMIC-LIKE (LOCALIZED) STATES ⇒ CORE:

PLUS SPIN:

$$\psi_i(\vec{r}) = \psi_{n_i, l_i, m_i}(r, \theta, \phi) = R_{n_i, l_i}(r) Y_{l_i, m_i}(\theta, \phi) \begin{cases} \alpha(\sigma) = m_{s_i} = +1/2 = \uparrow \\ \beta(\sigma) = m_{s_i} = -1/2 = \downarrow \end{cases}$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}^k} Y_{l_f, m_f}^*(\theta_f, \phi_f) Y_{l_f, m_f}(\theta, \phi) R_{E_f, l_f}(r) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

PHASE SHIFT OF l_f WAVE IN $V(r)$

DIPOLE APPROX.

INT. $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2 \Rightarrow$

EQUIVALENT WITHIN CONSTANT FACTOR



- < $\Delta l = l_f - l_i = \pm 1$ TWO CHANNELS
- < $\Delta m = m_f - m_i = 0, \pm 1$ LINEAR POLARIZ.
- < $\Delta m = \pm 1$, CIRCULAR POLARIZATION

$\Delta m_s = m_{s_f} - m_{s_i} = 0!$

● RADIATION POLARIZATION: $\hat{\mathbf{e}} \cdot \vec{r} = \hat{\mathbf{e}} \cdot (x\hat{\mathbf{x}} + y\hat{\mathbf{y}} + z\hat{\mathbf{z}})$



LINEARLY POLARIZED -



x: $\hat{\mathbf{e}} \cdot \vec{r} \Rightarrow x \Rightarrow \text{INT.}_x$
 $\propto Y_{\ell=1, m_\ell=+1}(\theta, \phi) + Y_{\ell=1, m_\ell=-1}(\theta, \phi)$



y: $\hat{\mathbf{e}} \cdot \vec{r} \Rightarrow y \Rightarrow \text{INT.}_y$

CIRCULARLY POLARIZED



LEFT \equiv LCP: $\hat{\mathbf{e}} \cdot \vec{r} \Rightarrow x - iy \Rightarrow \text{INT.}_{LCP}$
 $\propto Y_{\ell=1, m_\ell=+1}(\theta, \phi) - Y_{\ell=1, m_\ell=-1}(\theta, \phi)$



RIGHT \equiv RCP: $\hat{\mathbf{e}} \cdot \vec{r} \Rightarrow x + iy \Rightarrow \text{INT.}_{RCP}$

UNPOLARIZED -



$\text{INT.}_{UNP} = \text{INT.}_x + \text{INT.}_y$
 $= \text{INT.}_{LCP} + \text{INT.}_{RCP}$

Atomic orbitals:

COMPLEX, IF $m \neq 0$

TABLE 6.1

NORMALIZED WAVE FUNCTIONS OF THE HYDROGEN ATOM FOR $n = 1, 2,$ AND 3^* ($Z=1 = \text{HYDROGEN}$)

n	l	m_l	$\Phi_{m_l}(\phi)$	$\Theta_{lm}(\theta)$	$R_{nl}(r)$	$\Psi_{nlm}(r, \theta, \phi) = \Phi_{m_l} \Theta_{lm} R_{nl}$
1	0	0	$\frac{1}{\sqrt{2\pi}}$	$\frac{1}{\sqrt{2}}$	$\frac{2}{a_0^{3/2}} e^{-r/a_0}$	$\frac{1}{\sqrt{\pi} a_0^{3/2}} e^{-r/a_0}$
2	0	0	$\frac{1}{\sqrt{2\pi}}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2\sqrt{2} a_0^{3/2}} \left(2 - \frac{r}{a_0}\right) e^{-r/2a_0}$	$\frac{1}{4\sqrt{2\pi} a_0^{3/2}} \left(2 - \frac{r}{a_0}\right) e^{-r/2a_0}$
2	1	0	$\frac{1}{\sqrt{2\pi}}$	$\frac{\sqrt{6}}{2} \cos \theta$	$\frac{1}{2\sqrt{6} a_0^{3/2}} \frac{r}{a_0} e^{-r/2a_0}$	$\frac{1}{4\sqrt{2\pi} a_0^{3/2}} \frac{r}{a_0} e^{-r/2a_0} \cos \theta$
2	1	± 1	$\frac{1}{\sqrt{2\pi}} e^{\pm i\phi}$	$\frac{\sqrt{3}}{2} \sin \theta$	$\frac{1}{2\sqrt{6} a_0^{3/2}} \frac{r}{a_0} e^{-r/2a_0}$	$\frac{1}{8\sqrt{\pi} a_0^{3/2}} \frac{r}{a_0} e^{-r/2a_0} \sin \theta e^{\pm i\phi}$
3	0	0	$\frac{1}{\sqrt{2\pi}}$	$\frac{1}{\sqrt{2}}$	$\frac{2}{81\sqrt{3} a_0^{3/2}} \left(27 - 18 \frac{r}{a_0} + 2 \frac{r^2}{a_0^2}\right) e^{-r/3a_0}$	$\frac{1}{81\sqrt{3\pi} a_0^{3/2}} \left(27 - 18 \frac{r}{a_0} + 2 \frac{r^2}{a_0^2}\right) e^{-r/3a_0}$
3	1	0	$\frac{1}{\sqrt{2\pi}}$	$\frac{\sqrt{6}}{2} \cos \theta$	$\frac{4}{81\sqrt{6} a_0^{3/2}} \left(6 - \frac{r}{a_0}\right) \frac{r}{a_0} e^{-r/3a_0}$	$\frac{\sqrt{2}}{81\sqrt{\pi} a_0^{3/2}} \left(6 - \frac{r}{a_0}\right) \frac{r}{a_0} e^{-r/3a_0} \cos \theta$
3	1	± 1	$\frac{1}{\sqrt{2\pi}} e^{\pm i\phi}$	$\frac{\sqrt{3}}{2} \sin \theta$	$\frac{4}{81\sqrt{6} a_0^{3/2}} \left(6 - \frac{r}{a_0}\right) \frac{r}{a_0} e^{-r/3a_0}$	$\frac{1}{81\sqrt{\pi} a_0^{3/2}} \left(6 - \frac{r}{a_0}\right) \frac{r}{a_0} e^{-r/3a_0} \sin \theta e^{\pm i\phi}$
3	2	0	$\frac{1}{\sqrt{2\pi}}$	$\frac{\sqrt{10}}{4} (3 \cos^2 \theta - 1)$	$\frac{4}{81\sqrt{30} a_0^{3/2}} \frac{r^2}{a_0^2} e^{-r/3a_0}$	$\frac{1}{81\sqrt{6\pi} a_0^{3/2}} \frac{r^2}{a_0^2} e^{-r/3a_0} (3 \cos^2 \theta - 1)$
3	2	± 1	$\frac{1}{\sqrt{2\pi}} e^{\pm i\phi}$	$\frac{\sqrt{15}}{2} \sin \theta \cos \theta$	$\frac{4}{81\sqrt{30} a_0^{3/2}} \frac{r^2}{a_0^2} e^{-r/3a_0}$	$\frac{1}{81\sqrt{\pi} a_0^{3/2}} \frac{r^2}{a_0^2} e^{-r/3a_0} \sin \theta \cos \theta e^{\pm i\phi}$
3	2	± 2	$\frac{1}{\sqrt{2\pi}} e^{\pm 2i\phi}$	$\frac{\sqrt{15}}{4} \sin^2 \theta$	$\frac{4}{81\sqrt{30} a_0^{3/2}} \frac{r^2}{a_0^2} e^{-r/3a_0}$	$\frac{1}{162\sqrt{\pi} a_0^{3/2}} \frac{r^2}{a_0^2} e^{-r/3a_0} \sin^2 \theta e^{\pm 2i\phi}$

*The quantity $a_0 = 4\pi\epsilon_0\hbar^2/me^2 = 5.3 \times 10^{-11} \text{ m}$ is equal to the radius of the innermost Bohr orbit.

IS SAME FOR
MANY e^- ATOMS

CHANGES FOR
MANY e^- ATOMS

MAKING THE ATOMIC ORBITALS REAL (E.G., FOR CHEMICAL BONDING):

$$\Psi_{nlm_l}(r, \theta, \phi) = R_{nl}(r) \Theta_{lm_l}(\theta) \frac{1}{\sqrt{2\pi}} e^{im_l \phi}$$

COMPLEX
REAL
REAL
COMPLEX IF $m_l \neq 0$

SO JUST TAKE COMB. OF $\pm m_l$ AS:

$$\Psi_{nl(-)}(r, \theta, \phi) = \begin{cases} \frac{1}{2} [\Psi_{nlm_l} + \Psi_{nl-m_l}] \propto R_{nl} \Theta_{lm_l} \cos m_l \phi \\ \frac{1}{2i} [\Psi_{nlm_l} - \Psi_{nl-m_l}] \propto R_{nl} \Theta_{lm_l} \sin m_l \phi \end{cases}$$

REAL

EXAMPLE: 2p ORBITALS

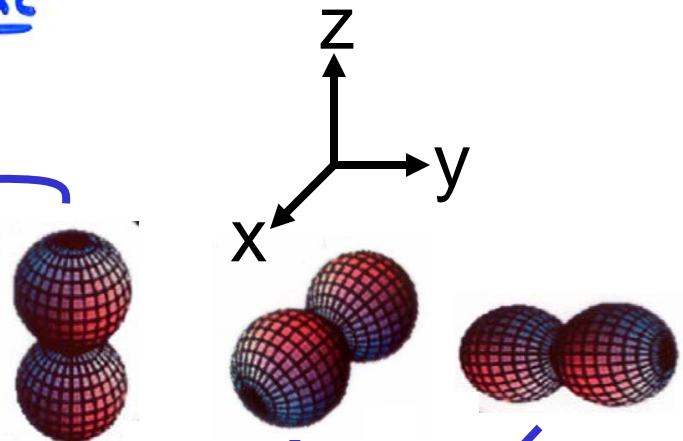
$$\Psi_{210} = \Psi_{2p_0} = \underline{\Psi_{2p_z}} \propto r \cos \theta = z \text{ (ALREADY REAL)}$$

$$\Psi_{211} = \Psi_{2p_{+1}} \propto r \sin \theta e^{i\phi} = r \sin \theta [\cos \phi + i \sin \phi]$$

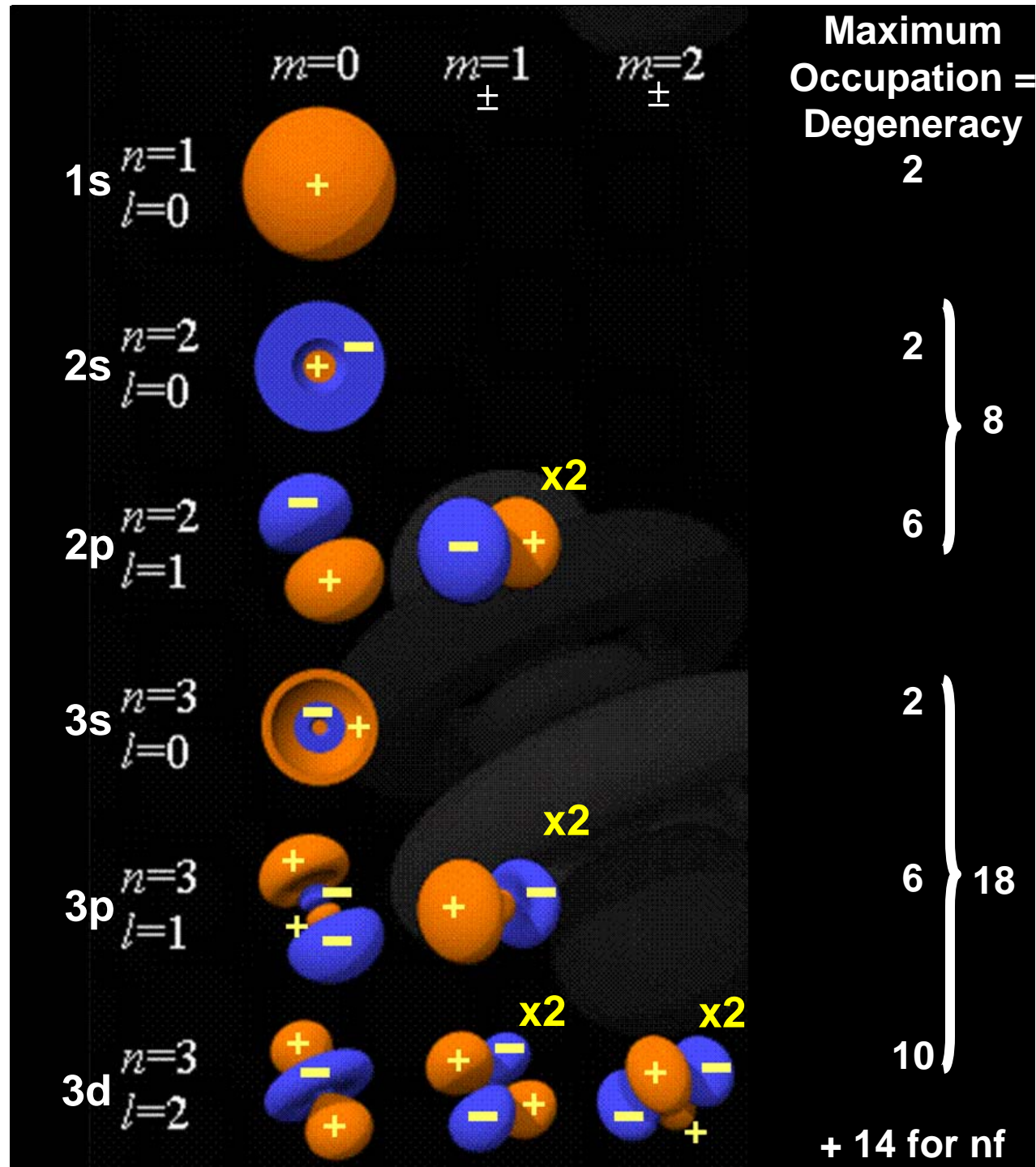
$$\Psi_{21-1} = \Psi_{2p_{-1}} \propto r \sin \theta e^{-i\phi} = r \sin \theta [\cos \phi - i \sin \phi]$$

$$\frac{1}{2} [\Psi_{2p_{+1}} + \Psi_{2p_{-1}}] = \underline{\Psi_{2p_x}} \propto r \sin \theta \cos \phi = x$$

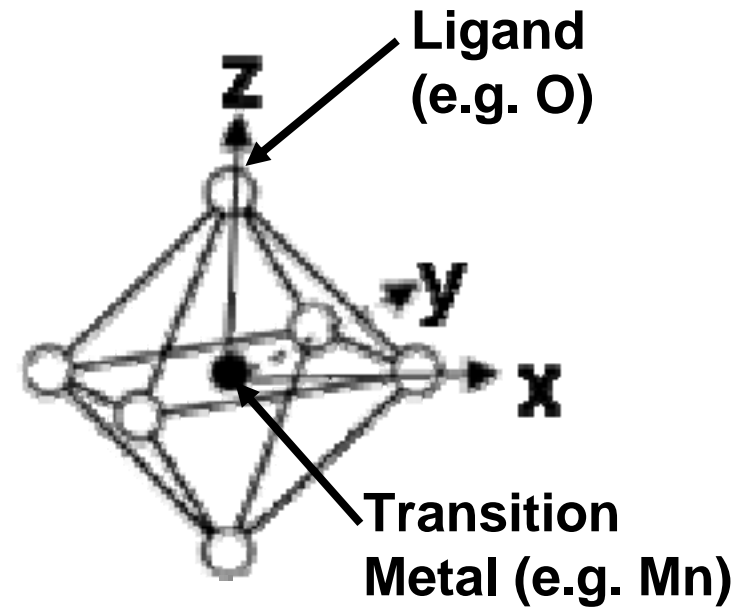
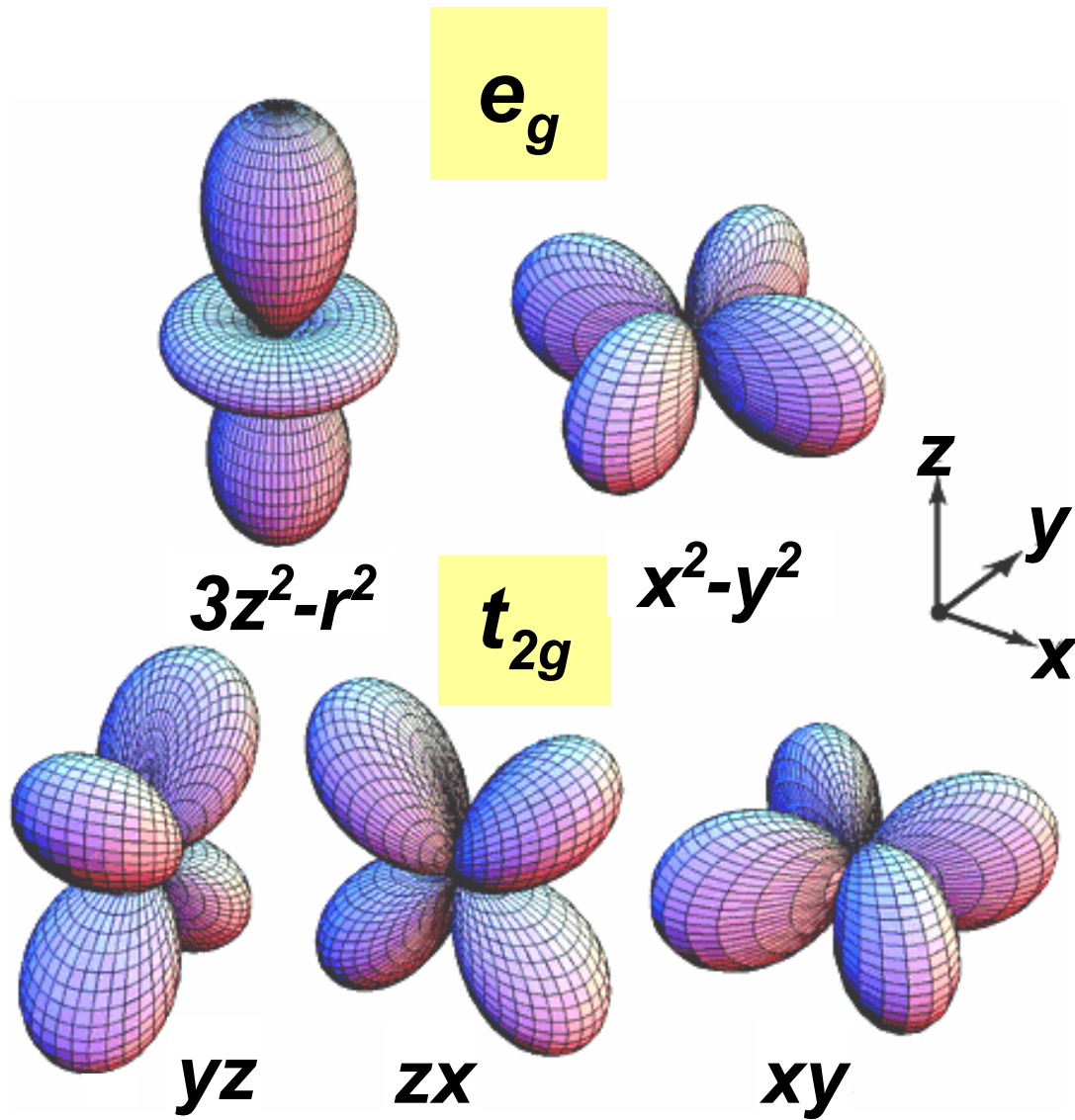
$$\frac{1}{2i} [\Psi_{2p_{+1}} - \Psi_{2p_{-1}}] = \underline{\Psi_{2p_y}} \propto r \sin \theta \sin \phi = y$$



Filling the Atomic Orbitals:



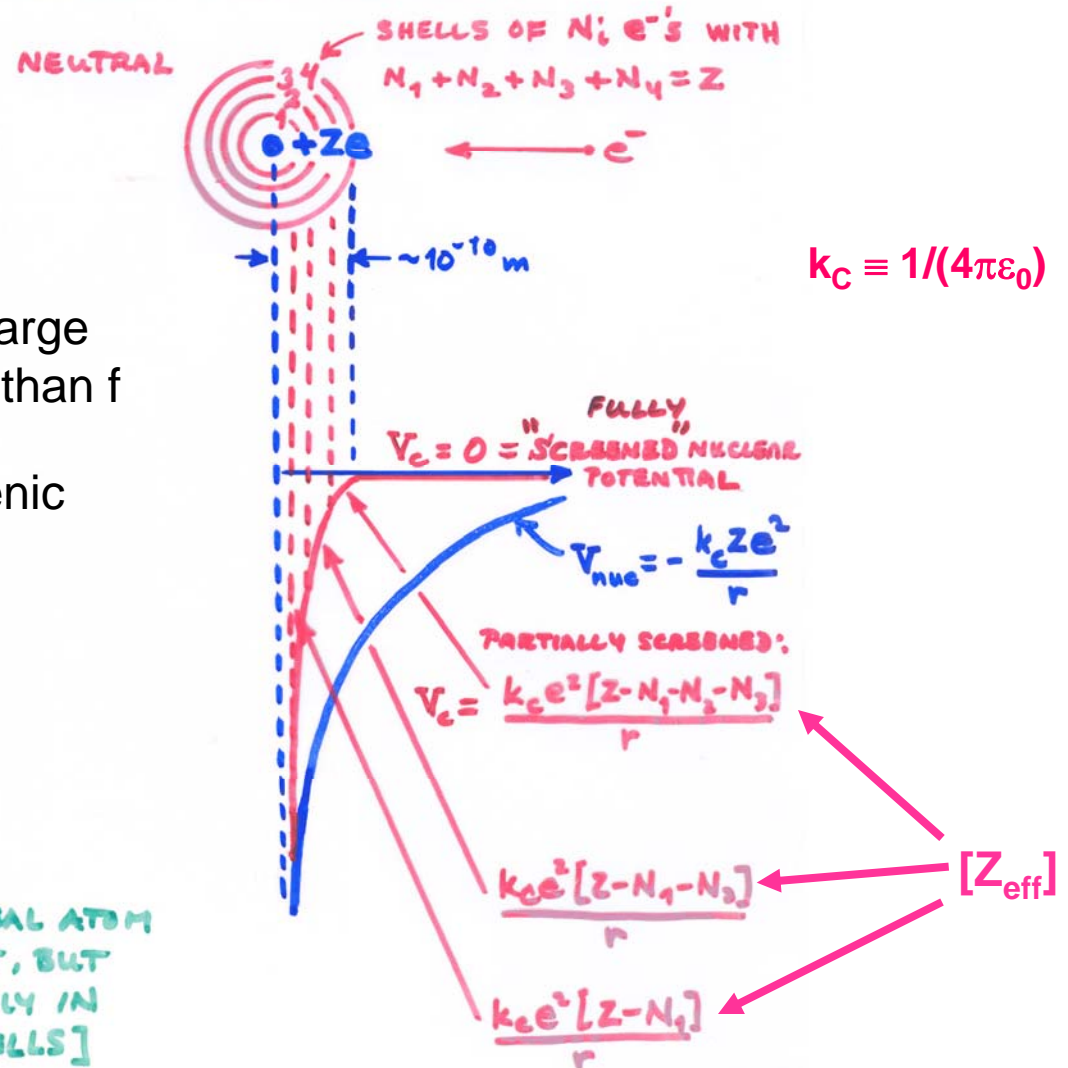
And the same thing for the d orbitals:



e_g and t_{2g} not equivalent in octahedral (cubic) environment

Intraatomic electron screening in many-electron atoms--a simple model

POINT CHARGE ($\sim e^-$) + SPHERICAL SHELLS
OF e^- CHARGE (\sim ORBITS) AROUND POINT-
CHARGE NUCLEUS $\Rightarrow \sim$ ATOM :



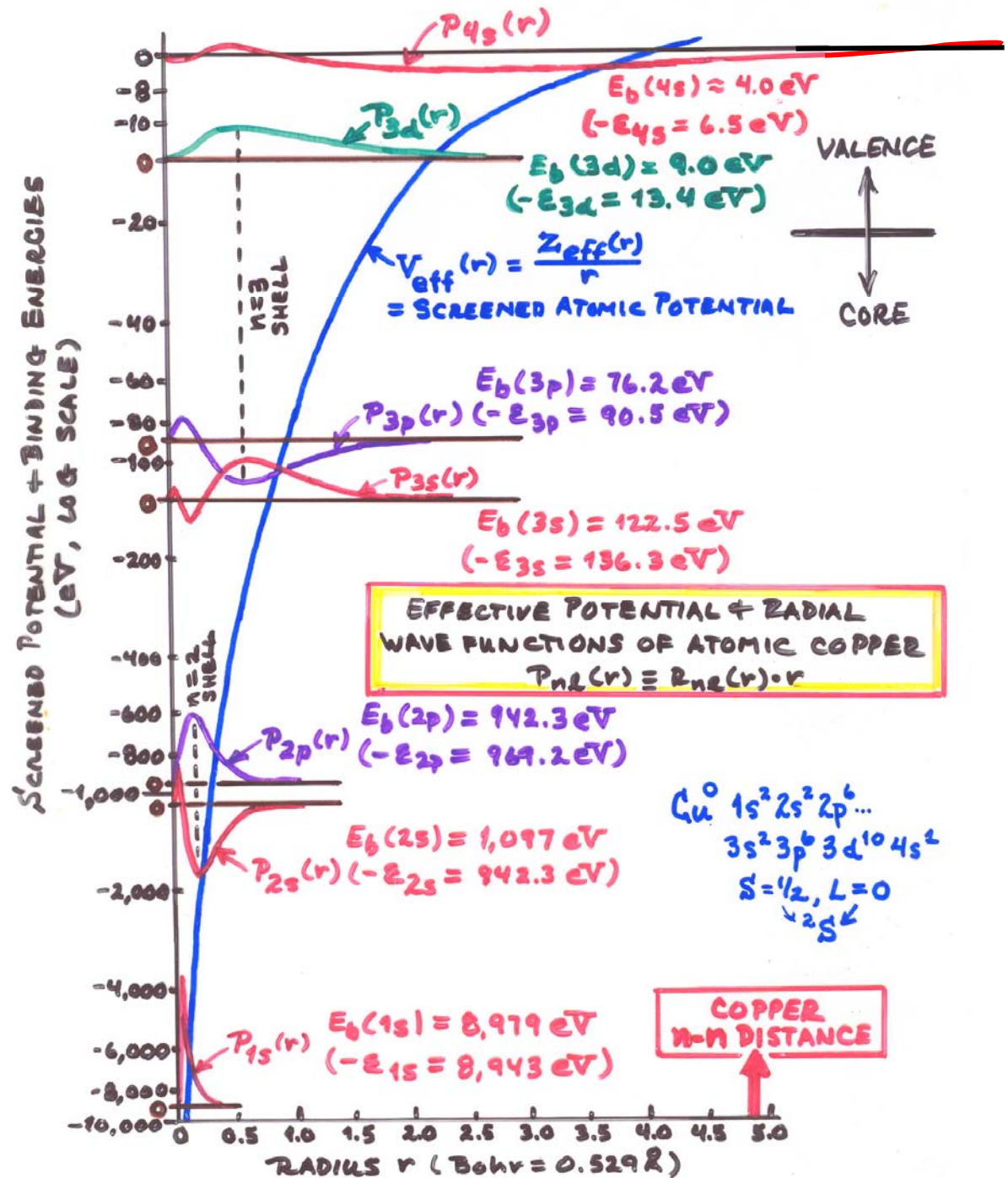
In many-electron atoms:
For a given n , s feels nuclear charge
more than p , more than d , more than f

Lifts degeneracy on ℓ in hydrogenic
atom

[CHARGE IN REAL ATOM
SMEARED OUT, BUT
STILL ROUGHLY IN
RADIAL SHELLS]

Intraatomic electron screening in many-electron atoms--a self-consistent Q.M. calculation

Plus radial one-electron functions:
 $P_{nl}(r) \equiv rR_{nl}(r)$



OBSERVED (+ CALCULATED) ORDER OF FILLING ATOMIC LEVELS:

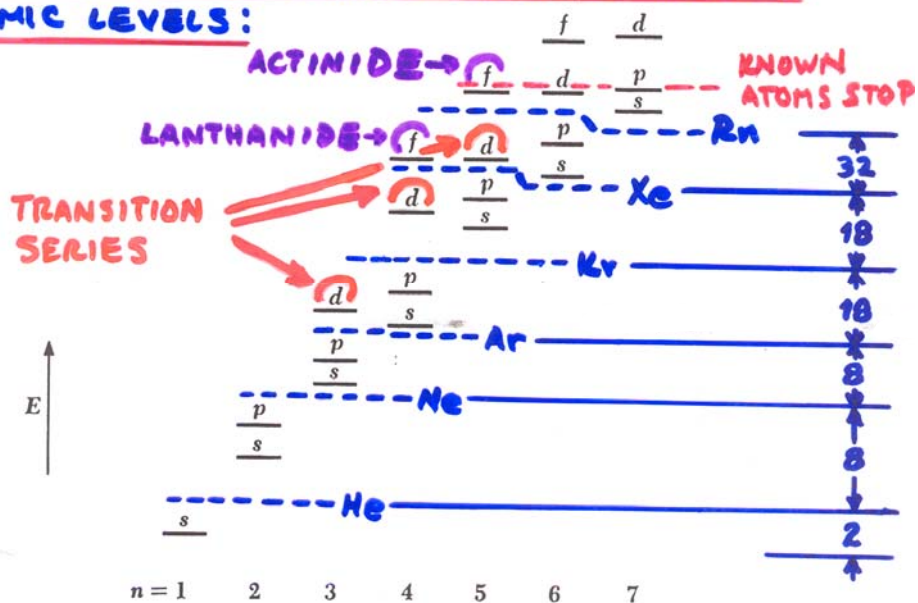


FIGURE 7.13 The sequence of quantum states in an atom. Not to scale.

EXAMPLE CONFIGURATIONS:

Z ATOM CONFIG.

8 O $1s^2 2s^2 2p^4$

GROUND-STATE OPEN SHELL COUPLING?

$\uparrow\downarrow$ \uparrow \uparrow
 $2p_{-1}$ $2p_0$ $2p_{+1}$

26 Fe $1s^2 2s^2 2p^6 3s^2 3p^6$
 $3d^6 4s^2$

$\uparrow\downarrow$ \uparrow \uparrow \uparrow \uparrow
 $3d_{-2}$ $3d_{-1}$ $3d_0$ $3d_{+1}$ $3d_{+2}$

\Rightarrow LARGE μ_{3d} + MAGNETISM

63 Eu $1s^2 2s^2 2p^6 3s^2 3p^6$
 $3d^{10} 4s^2 4p^6 4d^{10}$
 $4f^7 6s^2$

ALSO MAGNETIC! \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow
 $4f_{-3}$ $4f_{-2}$ $4f_{-1}$ $4f_0$ $4f_{+1}$ $4f_{+2}$ $4f_{+3}$

s²

TRANSITION METALS

Periodic Table, with the Outer Electron Configurations of Neutral Atoms in Their Ground States

The notation used to describe the electronic configuration of atoms and ions is discussed in all textbooks of introductory atomic physics. The letters *s*, *p*, *d*, ... signify electrons having orbital angular momentum 0, 1, 2, ... in units \hbar ; the number to the left of the letter denotes the principal quantum number of one orbit, and the superscript to the right denotes the number of electrons in the orbit.

H ¹																	He ²																																																																																																		
1s																	1s ²																																																																																																		
Li ³	Be ⁴															B ⁵	C ⁶	N ⁷	O ⁸	F ⁹	Ne ¹⁰																																																																																														
2s	2s ²															2s ² 2p	2s ² 2p ²	2s ² 2p ³	2s ² 2p ⁴	2s ² 2p ⁵	2s ² 2p ⁶																																																																																														
Na ¹¹	Mg ¹²															Al ¹³	Si ¹⁴	P ¹⁵	S ¹⁶	Cl ¹⁷	Ar ¹⁸																																																																																														
3s	3s ²															3s ² 3p	3s ² 3p ²	3s ² 3p ³	3s ² 3p ⁴	3s ² 3p ⁵	3s ² 3p ⁶																																																																																														
K ¹⁹	Ca ²⁰	Sc ²¹	Ti ²²	V ²³	Cr ²⁴	Mn ²⁵	Fe ²⁶	Co ²⁷	Ni ²⁸	Cu ²⁹	Zn ³⁰	Ga ³¹	Ge ³²	As ³³	Se ³⁴	Br ³⁵	Kr ³⁶																																																																																																		
4s	4s ²	3d	3d ²	3d ³	3d ⁵	3d ⁵	3d ⁶	3d ⁷	3d ⁸	3d ¹⁰	3d ¹⁰	4s ² 4p	4s ² 4p ²	4s ² 4p ³	4s ² 4p ⁴	4s ² 4p ⁵	4s ² 4p ⁶																																																																																																		
Rb ³⁷	Sr ³⁸	Y ³⁹	Zr ⁴⁰	Nb ⁴¹	Mo ⁴²	Tc ⁴³	Ru ⁴⁴	Rh ⁴⁵	Pd ⁴⁶	Ag ⁴⁷	Cd ⁴⁸	In ⁴⁹	Sn ⁵⁰	Sb ⁵¹	Te ⁵²	I ⁵³	Xe ⁵⁴																																																																																																		
5s	5s ²	4d	4d ²	4d ⁴	4d ⁵	4d ⁶	4d ⁷	4d ⁸	4d ¹⁰	4d ¹⁰	4d ¹⁰	5s ² 5p	5s ² 5p ²	5s ² 5p ³	5s ² 5p ⁴	5s ² 5p ⁵	5s ² 5p ⁶																																																																																																		
Cs ⁵⁵	Ba ⁵⁶	La ⁵⁷	Hf ⁷²	Ta ⁷³	W ⁷⁴	Re ⁷⁵	Os ⁷⁶	Ir ⁷⁷	Pt ⁷⁸	Au ⁷⁹	Hg ⁸⁰	Tl ⁸¹	Pb ⁸²	Bi ⁸³	Po ⁸⁴	At ⁸⁵	Rn ⁸⁶																																																																																																		
6s	6s ²	5d	4f ¹⁴	5d ²	5d ³	5d ⁴	5d ⁵	5d ⁶	5d ⁹	5d ⁹	5d ¹⁰	5d ¹⁰	6s ² 6p	6s ² 6p ²	6s ² 6p ³	6s ² 6p ⁴	6s ² 6p ⁵	6s ² 6p ⁶																																																																																																	
Fr ⁸⁷	Ra ⁸⁸	Ac ⁸⁹	<p>4f¹⁴ ... 4f(5d) FILLING ... 4f¹⁴</p> <table border="1"> <tr> <td>Ce⁵⁸</td> <td>Pr⁵⁹</td> <td>Nd⁶⁰</td> <td>Pm⁶¹</td> <td>Sm⁶²</td> <td>Eu⁶³</td> <td>Gd⁶⁴</td> <td>Tb⁶⁵</td> <td>Dy⁶⁶</td> <td>Ho⁶⁷</td> <td>Er⁶⁸</td> <td>Tm⁶⁹</td> <td>Yb⁷⁰</td> <td>Lu⁷¹</td> </tr> <tr> <td>4f²</td> <td>4f³</td> <td>4f⁴</td> <td>4f⁵</td> <td>4f⁶</td> <td>4f⁷</td> <td>4f⁷</td> <td>4f⁸</td> <td>4f¹⁰</td> <td>4f¹¹</td> <td>4f¹²</td> <td>4f¹³</td> <td>4f¹⁴</td> <td>4f¹⁴</td> </tr> <tr> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> <td>6s²</td> </tr> <tr> <td>Th⁹⁰</td> <td>Pa⁹¹</td> <td>U⁹²</td> <td>Np⁹³</td> <td>Pu⁹⁴</td> <td>Am⁹⁵</td> <td>Cm⁹⁶</td> <td>Bk⁹⁷</td> <td>Cf⁹⁸</td> <td>Es⁹⁹</td> <td>Fm¹⁰⁰</td> <td>Md¹⁰¹</td> <td>No¹⁰²</td> <td>Lr¹⁰³</td> </tr> <tr> <td>-</td> <td>5f²</td> <td>5f³</td> <td>5f⁵</td> <td>5f⁶</td> <td>5f⁷</td> <td>5f⁷</td> <td>5f⁷</td> <td>5f⁸</td> <td>5f⁹</td> <td>5f⁹</td> <td>5f⁹</td> <td>5f⁹</td> <td>5f⁹</td> </tr> <tr> <td>6d²</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> <td>6d</td> </tr> <tr> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> <td>7s²</td> </tr> </table>															Ce ⁵⁸	Pr ⁵⁹	Nd ⁶⁰	Pm ⁶¹	Sm ⁶²	Eu ⁶³	Gd ⁶⁴	Tb ⁶⁵	Dy ⁶⁶	Ho ⁶⁷	Er ⁶⁸	Tm ⁶⁹	Yb ⁷⁰	Lu ⁷¹	4f ²	4f ³	4f ⁴	4f ⁵	4f ⁶	4f ⁷	4f ⁷	4f ⁸	4f ¹⁰	4f ¹¹	4f ¹²	4f ¹³	4f ¹⁴	4f ¹⁴	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	Th ⁹⁰	Pa ⁹¹	U ⁹²	Np ⁹³	Pu ⁹⁴	Am ⁹⁵	Cm ⁹⁶	Bk ⁹⁷	Cf ⁹⁸	Es ⁹⁹	Fm ¹⁰⁰	Md ¹⁰¹	No ¹⁰²	Lr ¹⁰³	-	5f ²	5f ³	5f ⁵	5f ⁶	5f ⁷	5f ⁷	5f ⁷	5f ⁸	5f ⁹	5f ⁹	5f ⁹	5f ⁹	5f ⁹	6d ²	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²
Ce ⁵⁸	Pr ⁵⁹	Nd ⁶⁰	Pm ⁶¹	Sm ⁶²	Eu ⁶³	Gd ⁶⁴	Tb ⁶⁵	Dy ⁶⁶	Ho ⁶⁷	Er ⁶⁸	Tm ⁶⁹	Yb ⁷⁰	Lu ⁷¹																																																																																																						
4f ²	4f ³	4f ⁴	4f ⁵	4f ⁶	4f ⁷	4f ⁷	4f ⁸	4f ¹⁰	4f ¹¹	4f ¹²	4f ¹³	4f ¹⁴	4f ¹⁴																																																																																																						
6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²	6s ²																																																																																																						
Th ⁹⁰	Pa ⁹¹	U ⁹²	Np ⁹³	Pu ⁹⁴	Am ⁹⁵	Cm ⁹⁶	Bk ⁹⁷	Cf ⁹⁸	Es ⁹⁹	Fm ¹⁰⁰	Md ¹⁰¹	No ¹⁰²	Lr ¹⁰³																																																																																																						
-	5f ²	5f ³	5f ⁵	5f ⁶	5f ⁷	5f ⁷	5f ⁷	5f ⁸	5f ⁹	5f ⁹	5f ⁹	5f ⁹	5f ⁹																																																																																																						
6d ²	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d	6d																																																																																																						
7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²	7s ²																																																																																																						

s²

p¹ p² p³ p⁴ p⁵

p⁶

d¹ d² d³ d⁴ d⁵ d⁶ d⁷ d⁸ d⁹ d¹⁰

4f¹⁴ ... 4f(5d) FILLING ... 4f¹⁴

5f(6d) FILLING ...

RARE EARTHS

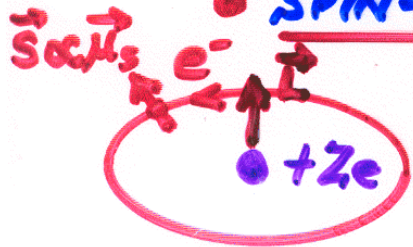
ACTINIDES

□ = EXCEPTIONS

◻ = EXCEPTIONS

→ d⁵ + d¹⁰ : 1/2 FILLED / FILLED MORE STABLE

• SPIN-ORBIT SPLITTING OF LEVELS:



⇒ EFFECTIVE \vec{B} (NUCLEUS AROUND e^-) $\propto \vec{L}$

$$\hat{H}_{s.o} = \xi(r) \vec{L} \cdot \vec{S}$$

• SPLITS ALL nl LEVELS $2(2l+1)$

- $nl_j = l + 1/2 \rightarrow 2l+2$
- $nl_j = l - 1/2 \rightarrow 2l$

• MIXES SPIN + ORBITAL ANGULAR MOM.:

$$\psi_{nljm_j} = C_1 \psi_{nl, m_j - 1/2} \begin{pmatrix} 1 \\ 0 \end{pmatrix} + C_2 \psi_{nl, m_j + 1/2} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

\parallel
 $m_s = +1/2$
 \parallel
 \uparrow

\parallel
 $m_s = -1/2$
 \parallel
 \downarrow

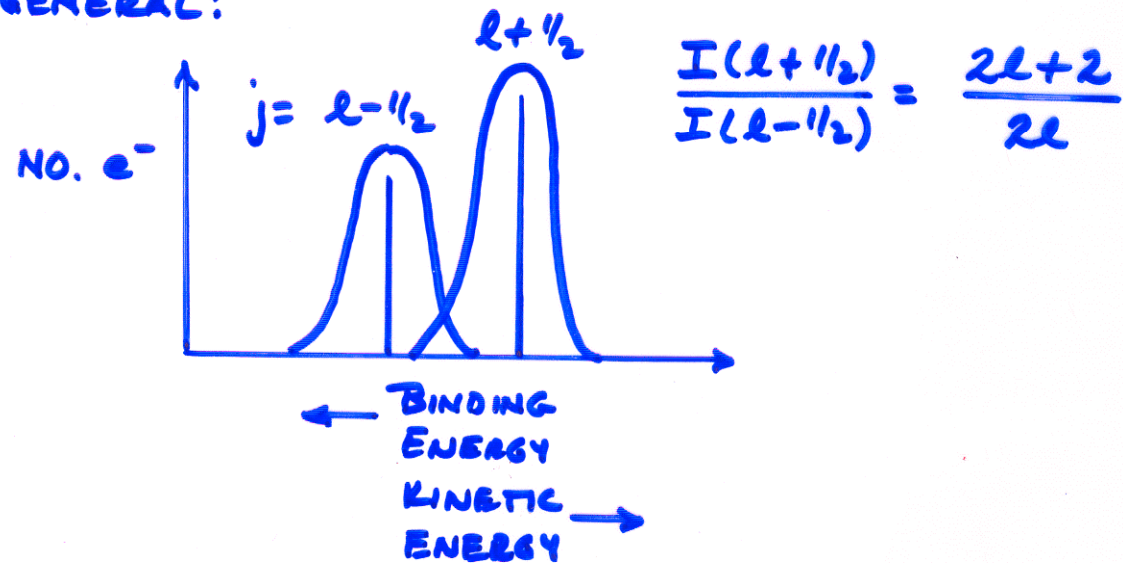
WITH C1 AND C2 TABULATED CLEBSCH-GORDAN OR WIGNER 3j SYMBOLS

SOME SPIN-ORBIT SPLITTINGS: (IN eV)

$2p^6$ $\swarrow \searrow$ $2p_{1/2}^2 \quad 2p_{3/2}^4$	$Z = 13$ (Al) $Z = 30$ (Zn) $Z = 74$ (W)	28 (Ni) 48 (Cd) 84 (Pb)	46 (Pd) 64 (Gd) 92 (U)
	0.4 0.1 2.2	17.8 6.7 7.0	157.0 32.3 64

INCREASE WITH Z FOR A GIVEN LEVEL.

IN GENERAL:



X-Ray Data Booklet--Section 1.1 ELECTRON BINDING ENERGIES

The energies are given in eV relative to the vacuum level for the rare gases and for H₂, N₂, O₂, F₂, and Cl₂; relative to the Fermi level for the metals; and relative to the top of the valence bands for semiconductors (and insulators).

Electronic configuration	Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}
1s	1 H	13.6						
1s ²	2 He	24.6*						
1s ² 2s	3 Li	54.7*						
1s ² 2s ²	4 Be	111.5*						
1s ² 2s ² 2p	5 B	188*						
1s ² 2s ² 2p ²	6 C	284.2*						
1s ² 2s ² 2p ³	7 N	409.9*	37.3*	~ 9	~ 9			
1s ² 2s ² 2p ⁴	8 O	543.1*	41.6*	~ 13	~ 13			
1s ² 2s ² 2p ⁵	9 F	696.7*	~ 45	~ 17	~ 17			
1s ² 2s ² 2p ⁶	10 Ne	870.2*	48.5*	21.7*	21.6*			
[Ne] 3s	11 Na	1070.8†	63.5†	30.65	30.81			
[Ne] 3s ²	12 Mg	1303.0†	88.7	49.78	49.50			
[Ne] 3s ² 3p	13 Al	1559.6	117.8	72.95	72.55			
[Ne] 3s ² 3p ²	14 Si	1839	149.7*b	99.82	99.42			
[Ne] 3s ² 3p ³	15 P	2145.5	189*	136*	135*			
[Ne] 3s ² 3p ⁴	16 S	2472	230.9	163.6*	162.5*			
[Ne] 3s ² 3p ⁵	17 Cl	2822.4	270*	202*	200*			
[Ne] 3s ² 3p ⁶	18 Ar	3205.9*	326.3*	250.6†	248.4*	29.3*	15.9*	15.7*
[Ar] 4s	19 K	3608.4*	378.6*	297.3*	294.6*	34.8*	18.3*	18.3*
[Ar] 4s ²	20 Ca	4038.5*	438.4†	349.7†	346.2†	44.3 †	25.4†	25.4†
	21 Sc	4492	498.0*	403.6*	398.7*	51.1*	28.3*	28.3*
	22 Ti	4966	560.9†	460.2†	453.8†	58.7†	32.6†	32.6†

Valence levels

~ 9 ~ 9
~ 13 ~ 13

~ 45 ~ 17 ~ 17

Interpolated, extrapolated

Missing valence B.E.s

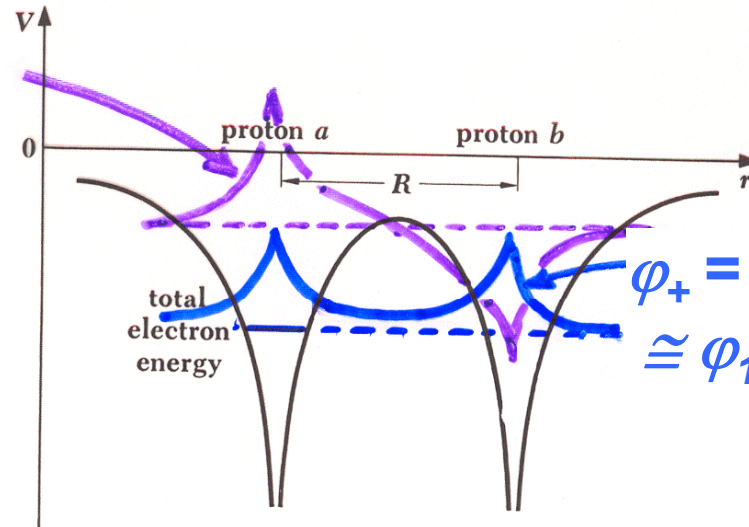
Valence levels

X-Ray Data Booklet--Section 1.1 ELECTRON BINDING ENERGIES

Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}	M ₄ 3d _{3/2}	M ₅ 3d _{5/2}	N ₁ 4s	N ₂ 4p _{1/2}	N ₃ 4p _{3/2}
23 V	5465	626.7†	519.8†	512.1†	66.3†	37.2†	37.2†	Valence levels				
24 Cr	5989	696.0†	583.8†	574.1†	74.1†	42.2†	42.2†					
25 Mn	6539	769.1†	649.9†	638.7†	82.3†	47.2†	47.2†					
26 Fe	7112	844.6†	719.9†	706.8†	91.3†	52.7†	52.7†					
27 Co	7709	925.1†	793.2†	778.1†	101.0†	58.9†	59.9†					
28 Ni	8333	1008.6†	870.0†	852.7†	110.8†	68.0†	66.2†					
29 Cu	8979	1096.7†	952.3†	932.7	122.5†	77.3†	75.1†					
30 Zn	9659	1196.2*	1044.9*	1021.8*	139.8*	91.4*	88.6*	10.2*	10.1*	Valence levels		
31 Ga	10367	1299.0*b	1143.2†	1116.4†	159.5†	103.5†	100.0†	18.7†	18.7†			
32 Ge	11103	1414.6*b	1248.1*b	1217.0*b	180.1*	124.9*	120.8*	29.8	29.2			
33 As	11867	1527.0*b	1359.1*b	1323.6*b	204.7*	146.2*	141.2*	41.7*	41.7*			
34 Se	12658	1652.0*b	1474.3*b	1433.9*b	229.6*	166.5*	160.7*	55.5*	54.6*			
35 Br	13474	1782*	1596*	1550*	257*	189*	182*	70*	69*			
36 Kr	14326	1921	1730.9*	1678.4*	292.8*	222.2*	214.4	95.0*	93.8*			
37 Rb	15200	2065	1864	1804	326.7*	248.7*	239.1*	113.0*	112*	30.5*	16.3*	15.3*
38 Sr	16105	2216	2007	1940	358.7†	280.3†	270.0†	136.0†	134.2†	38.9†	21.3	20.1†
39 Y	17038	2373	2156	2080	392.0*b	310.6*	298.8*	157.7†	155.8†	43.8*	24.4*	23.1*
40 Zr	17998	2532	2307	2223	430.3†	343.5†	329.8†	181.1†	178.8†	50.6†	28.5†	27.1†
41 Nb	18986	2698	2465	2371	466.6†	376.1†	360.6†	205.0†	202.3†	56.4†	32.6†	30.8†
42 Mo	20000	2866	2625	2520	506.3†	411.6†	394.0†	231.1†	227.9†	63.2†	37.6†	35.5†
43 Tc	21044	3043	2793	2677	544*	447.6	417.7	257.6	253.9*	69.5*	42.3*	39.9*
44 Ru	22117	3224	2967	2838	586.1*	483.5†	461.4†	284.2†	280.0†	75.0†	46.3†	43.2†
45 Rh	23220	3412	3146	3004	628.1†	521.3†	496.5†	311.9†	307.2†	81.4*b	50.5†	47.3†
46 Pd	24350	3604	3330	3173	671.6†	559.9†	532.3†	340.5†	335.2†	87.1*b	55.7†a	50.9†
47 Ag	25514	3806	3524	3351	719.0†	603.8†	573.0†	374.0†	368.3	97.0†	63.7†	58.3†

The quantum mechanics of covalent bonding in molecules: H₂⁺ with one electron

$$\varphi_- = \varphi_{\text{antibonding}} \cong \varphi_{1sa} - \varphi_{1sb}$$



$$\varphi_+ = \varphi_{\text{bonding}} \cong \varphi_{1sa} + \varphi_{1sb}$$

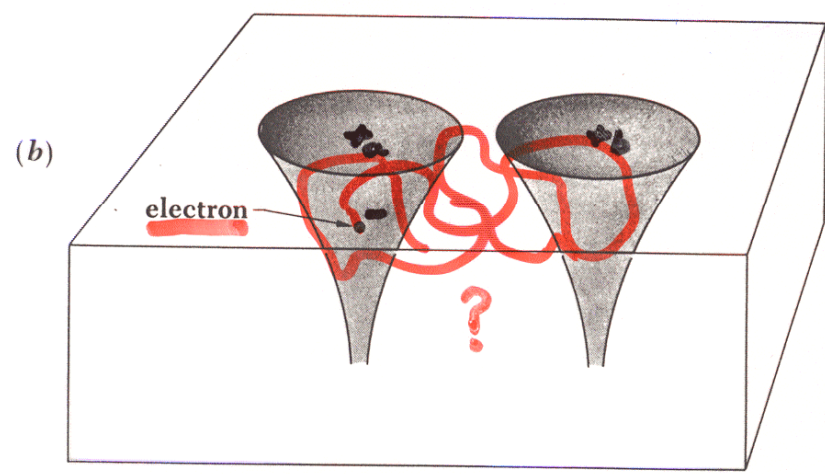
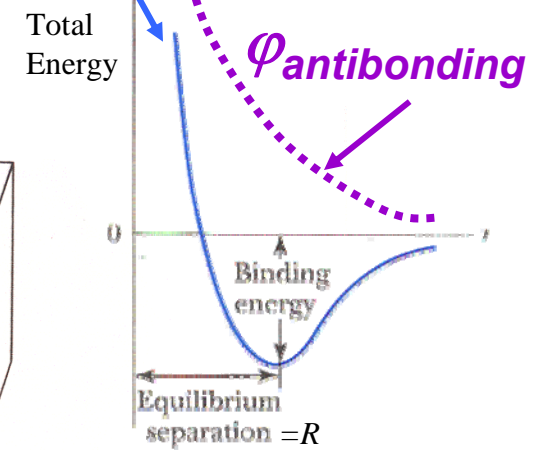
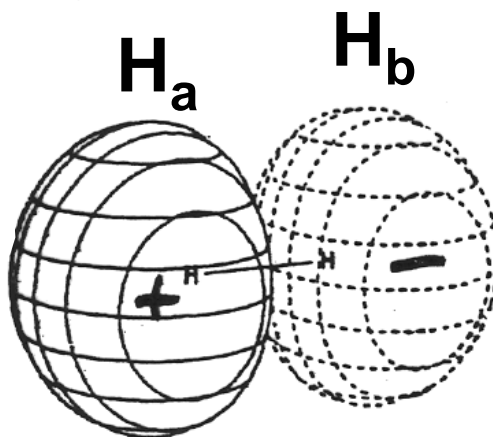


FIGURE 8.4 (a) Potential energy of an electron in the electric field of two nearby protons. The total energy of a ground-state electron in the hydrogen atom is indicated. (b) Two nearby protons correspond quantum-mechanically to a pair of boxes separated by a barrier.

FIGURE 10.2 The net potential energy curve, showing the equilibrium separation and binding energy.

1. Hydrogen

Symmetry: $D_{\infty h}$

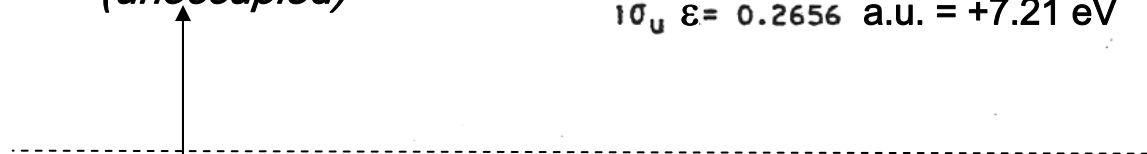


Anti-Bonding

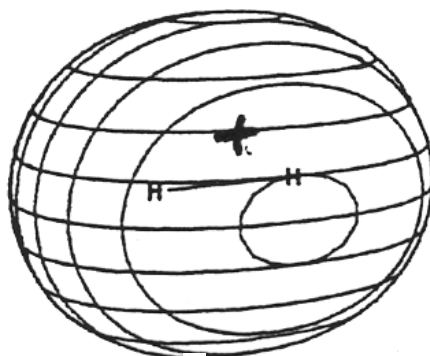
$$\varphi_{\text{anti}}^{MO} \cong \varphi_{1s_a} - \varphi_{1s_b}$$

$$1\sigma_u \quad \epsilon = 0.2656 \text{ a.u.} = +7.21 \text{ eV}$$

ϵ positive
(unoccupied)



ϵ negative
(occupied)



Bonding

$$\varphi_{\text{bonding}}^{MO} \cong \varphi_{1s_a} + \varphi_{1s_b}$$

$$1\sigma_g \quad \epsilon = -0.5944 \text{ a.u.} = -16.16 \text{ eV}$$

(Compare - 13.61 for H atom 1s)

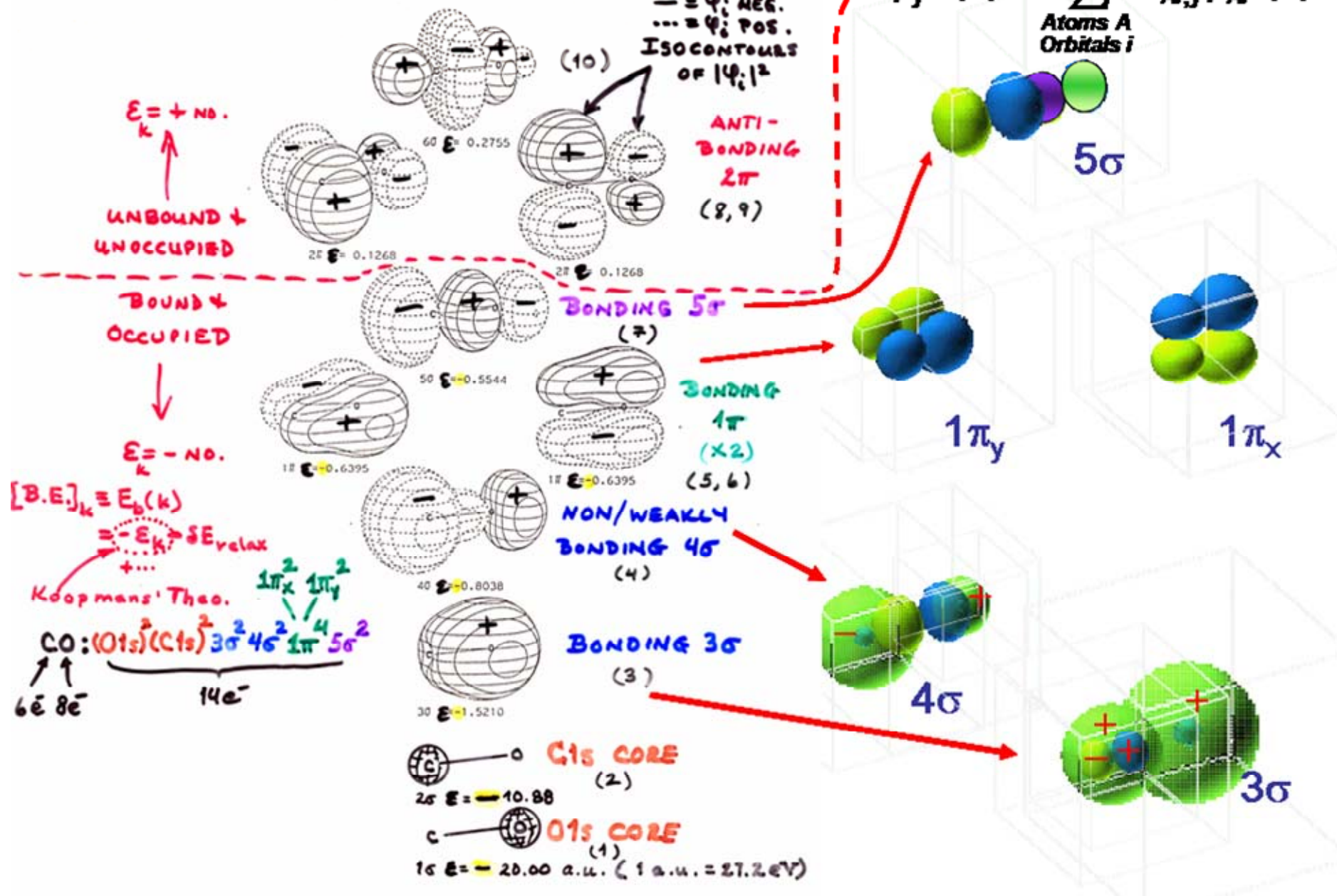
THE ELECTRONS IN CARBON MONOXIDE:

15. Carbon Monoxide

Symmetry: $C_{\infty v}$

Atomic orbital makeup

$$\varphi_j^{MO}(\vec{r}) = \sum_{\text{Atoms } A} \sum_{\text{Orbitals } i} c_{Ai,j} \varphi_{Ai}^{AO}(\vec{r})$$



Theoretical Calculations of charge density for CO bound to Ni(001)- "on-top":

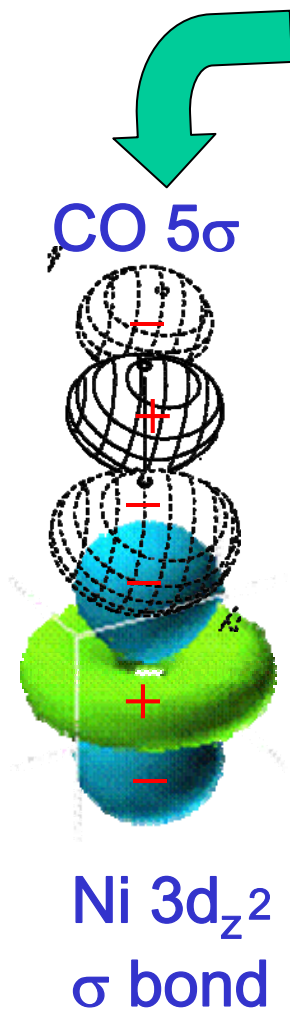
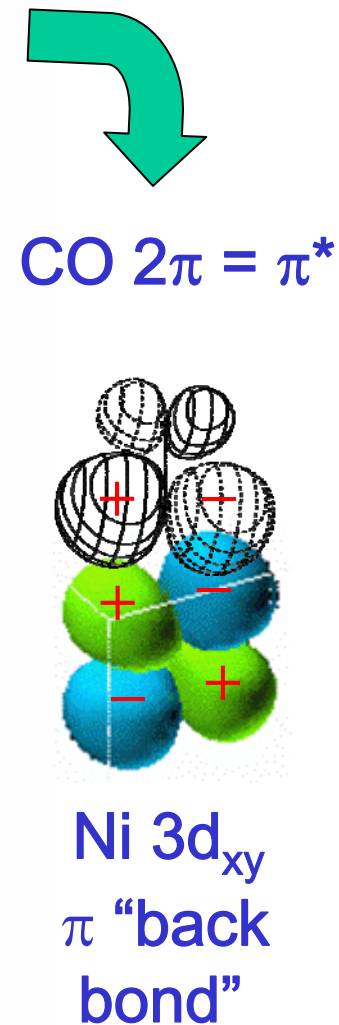
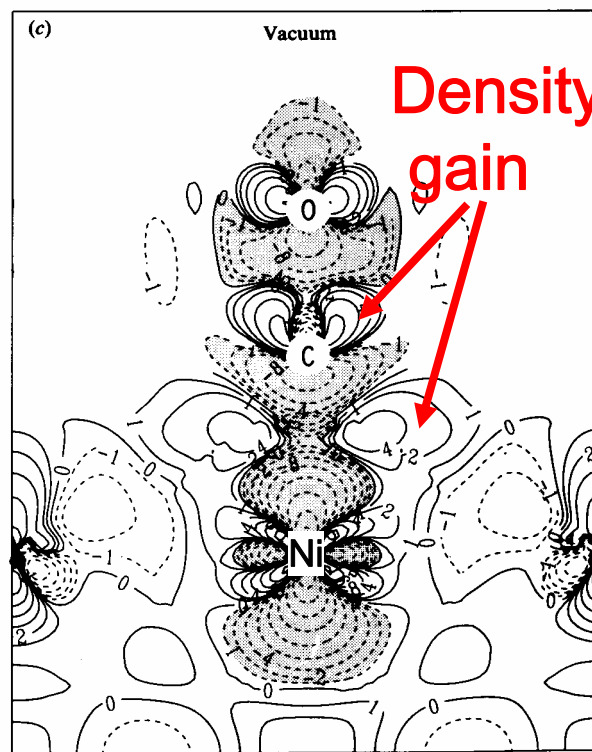
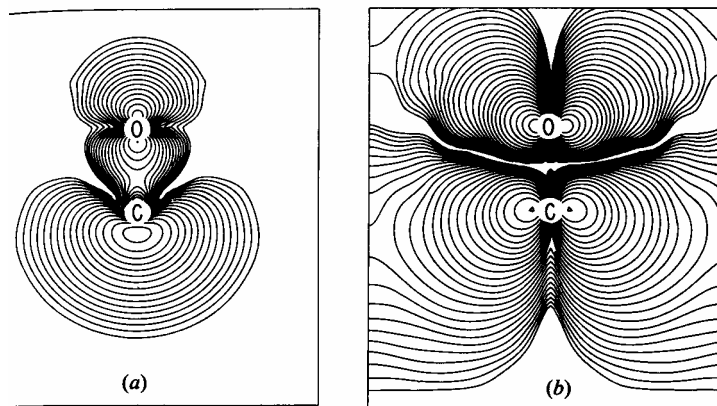


Fig. 12.14. Charge density contour plots appropriate to Ni(100) c(2 × 2)-CO: (a) free molecule 5 σ orbital; (b) free molecule 2 π orbital; (c) difference between CO/Ni(100) and the superposition of clean Ni(100) and an unsupported CO monolayer. Solid (dashed) lines indicate a gain (loss) of electronic charge (Wimmer, Fu & Freeman, 1985).

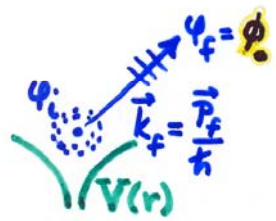


Zangwill,
p. 307, plus
PRL 55, 2618 ('85)

PHOTOELECTRON EMISSION-
BASIC MATRIX ELEMENTS + SELECTION RULES:

• ATOMIC-LIKE (LOCALIZED) STATES ⇒ CORE:

$$\psi_i(\vec{r}) = \psi_{n_i, l_i, m_i}(r, \theta, \phi) = R_{n_i, l_i}(r) Y_{l_i, m_i}(\theta, \phi)$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f)$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f, m_f}^*(\theta, \phi) Y_{l_f, m_f}(\theta, \phi) R_{E_f, l_f}(r)$$

PHASE SHIFT OF l_f WAVE IN $V(r)$

DIPOLE APPROX. : INT. $\propto \langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2$

EQUIVALENT WITHIN CONSTANT FACTOR



- < $\Delta l = l_f - l_i = \pm 1$
TWO CHANNELS
- < $\Delta m = m_f - m_i = 0, \pm 1$
LINEAR POLARIZ.
- < $\Delta m = \pm 1$, CIRCULAR POLARIZATION

• BLOCH-FUNCTION (DELOCALIZED) STATES ⇒ VALENCE:



$$\psi_i(\vec{r}) = u_{\vec{k}_i}(\vec{r}) e^{i\vec{k}_i \cdot \vec{r}}$$

$$\psi_f(\vec{r}) = u_{\vec{k}_f}(\vec{r}) e^{i\vec{k}_f \cdot \vec{r}} ; E_f = \frac{p_f^2}{2m} = \frac{\hbar^2 k_f^2}{2m} \text{ USUALLY NEGLIG.}$$

$$|\langle \psi_f | \hat{E} \cdot \vec{p} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{p} | \psi_i \rangle|^2 \Rightarrow \Delta \vec{k} = \vec{k}_f - \vec{k}_i - \vec{k}_{PHONON} = \vec{g}_{BULK} \text{ (OR } \vec{g}_{SURF})$$

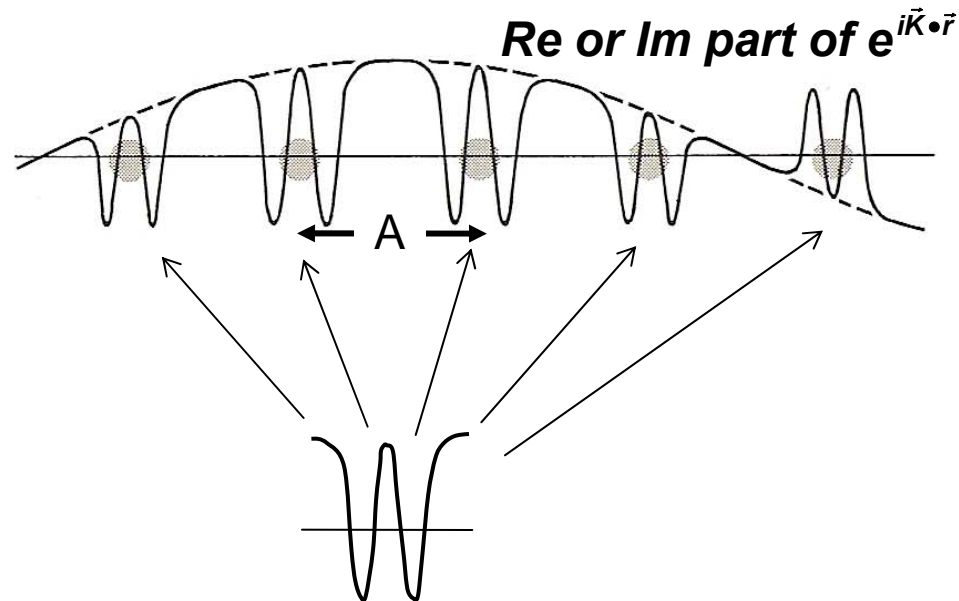
DIRECT TRANSITIONS

BUT LATTICE VIBRATIONS ⇒ SUM OVER \vec{k}_{PHONON}
 ⇒ FRACTION DIRECT = DEBYE-WALLER FACTOR
 $= \exp[-g^2 \bar{u}^2]$

For all states in crystalline (ordered) solids:

$$\Psi_{\vec{k}}(\vec{r}) = u_{\vec{k}}(\vec{r})e^{i\vec{k}\cdot\vec{r}}, \text{ where } u_{\vec{k}}(\vec{r}) = u(\vec{r} + \vec{A}) \text{ -- a Bloch function}$$

A typical Bloch function

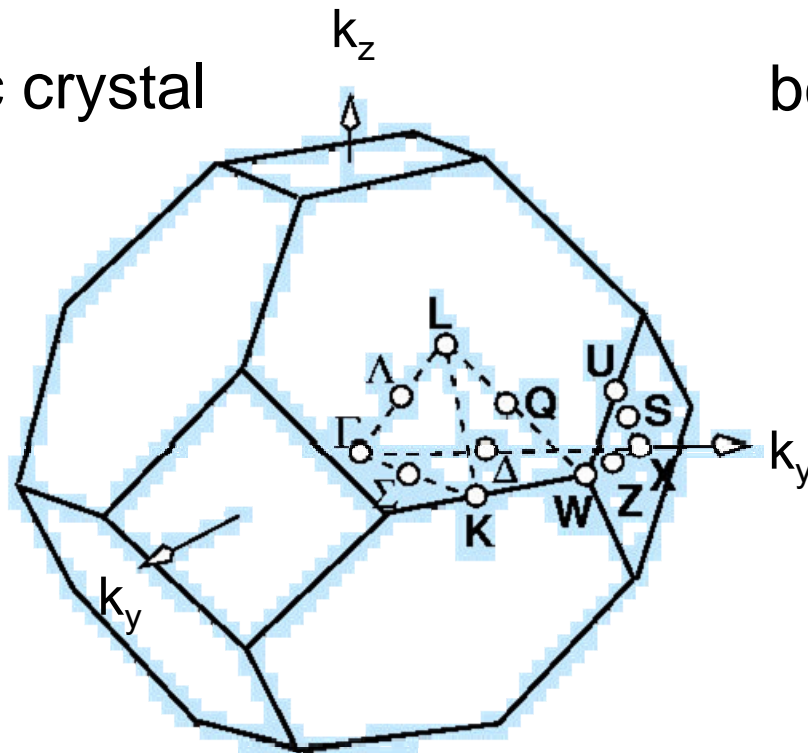


$u_{\vec{k}}(\vec{r})$ has periodicity of lattice, same in each unit cell

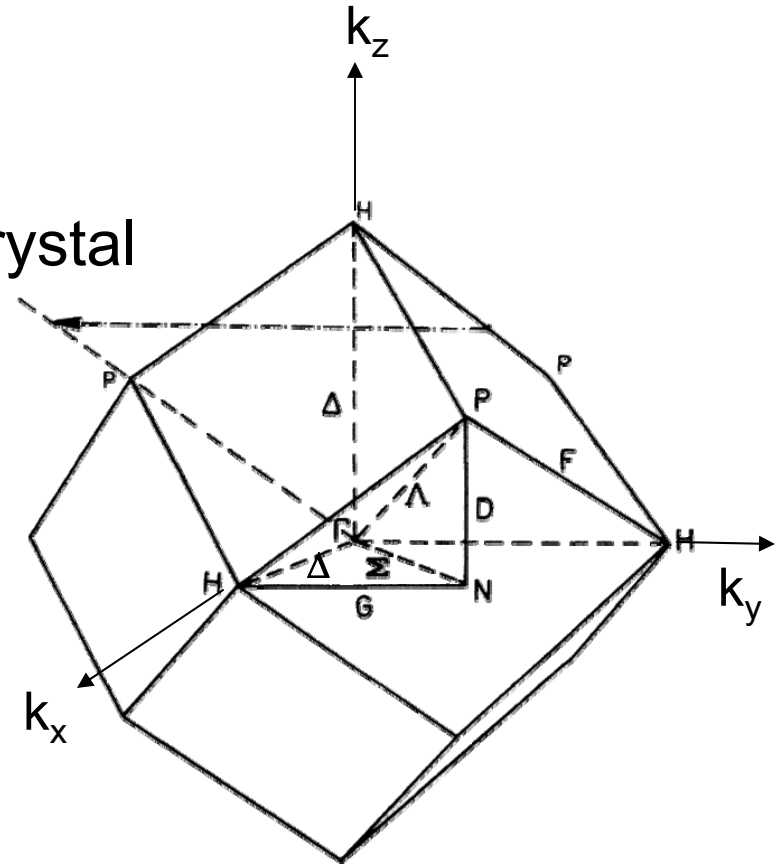
Different directions in k-space:

**The first (reduced)
Brillouin zone:**

fcc crystal



bcc crystal



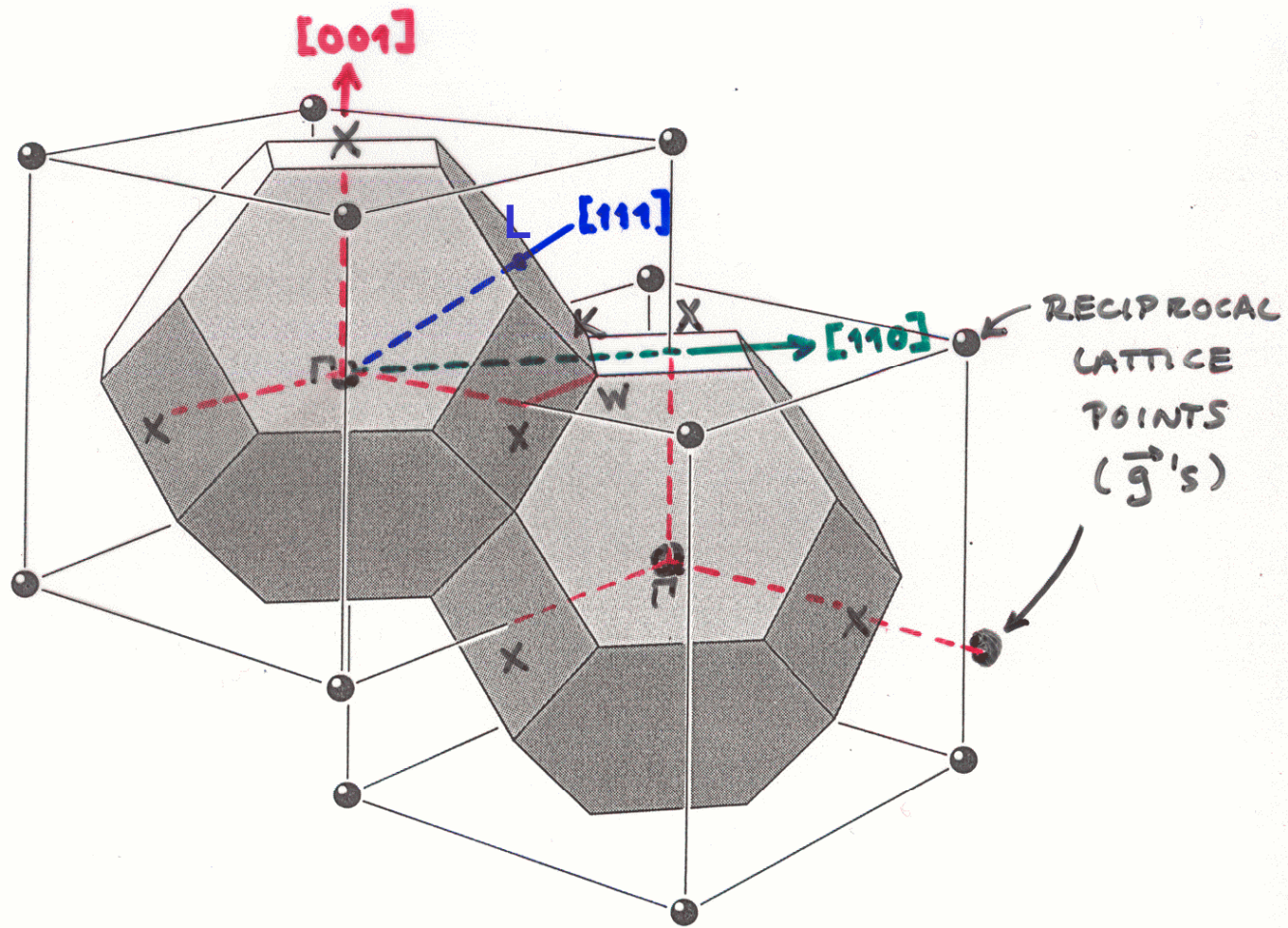


Figure 28 Brillouin zones of the face-centered cubic lattice. The cells are in reciprocal space, and the reciprocal lattice is body-centered, as drawn.

— STACKING OF FCC BRILLOUIN ZONES —

DIRECT TRANSITIONS
FOR NEARLY-FREE
ELECTRONS IN A WEAK
PERIODIC POTENTIAL
—1 DIMENSION

EXTENDED ZONE:

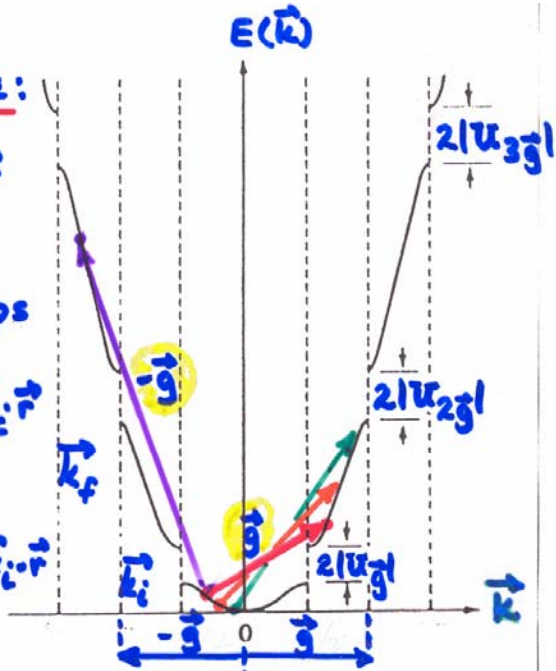
$$V(\vec{r}) = \sum_{\vec{g}} U_{\vec{g}} e^{i\vec{g}\cdot\vec{r}}$$

$$E(\vec{k}) \approx \frac{\hbar^2 k^2}{2m} + \text{gaps}$$

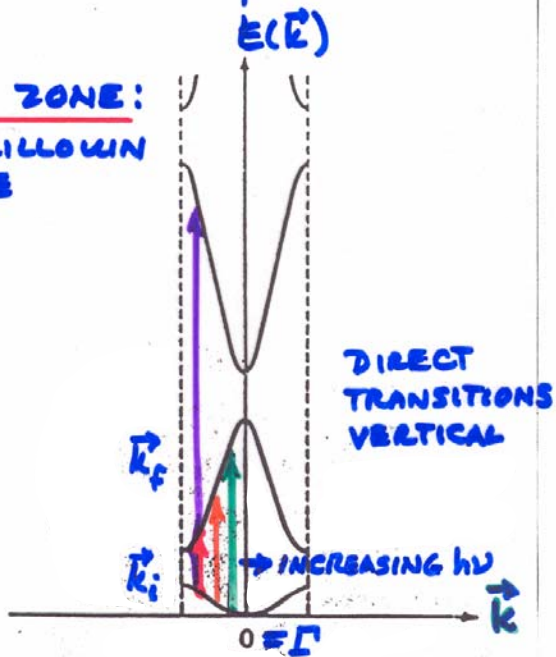
$$\vec{k}_f = \vec{k}_i + \vec{g}$$

$$\psi_f(\vec{r}) = u_{\vec{k}_f}(\vec{r}) e^{i\vec{k}_f\cdot\vec{r}}$$

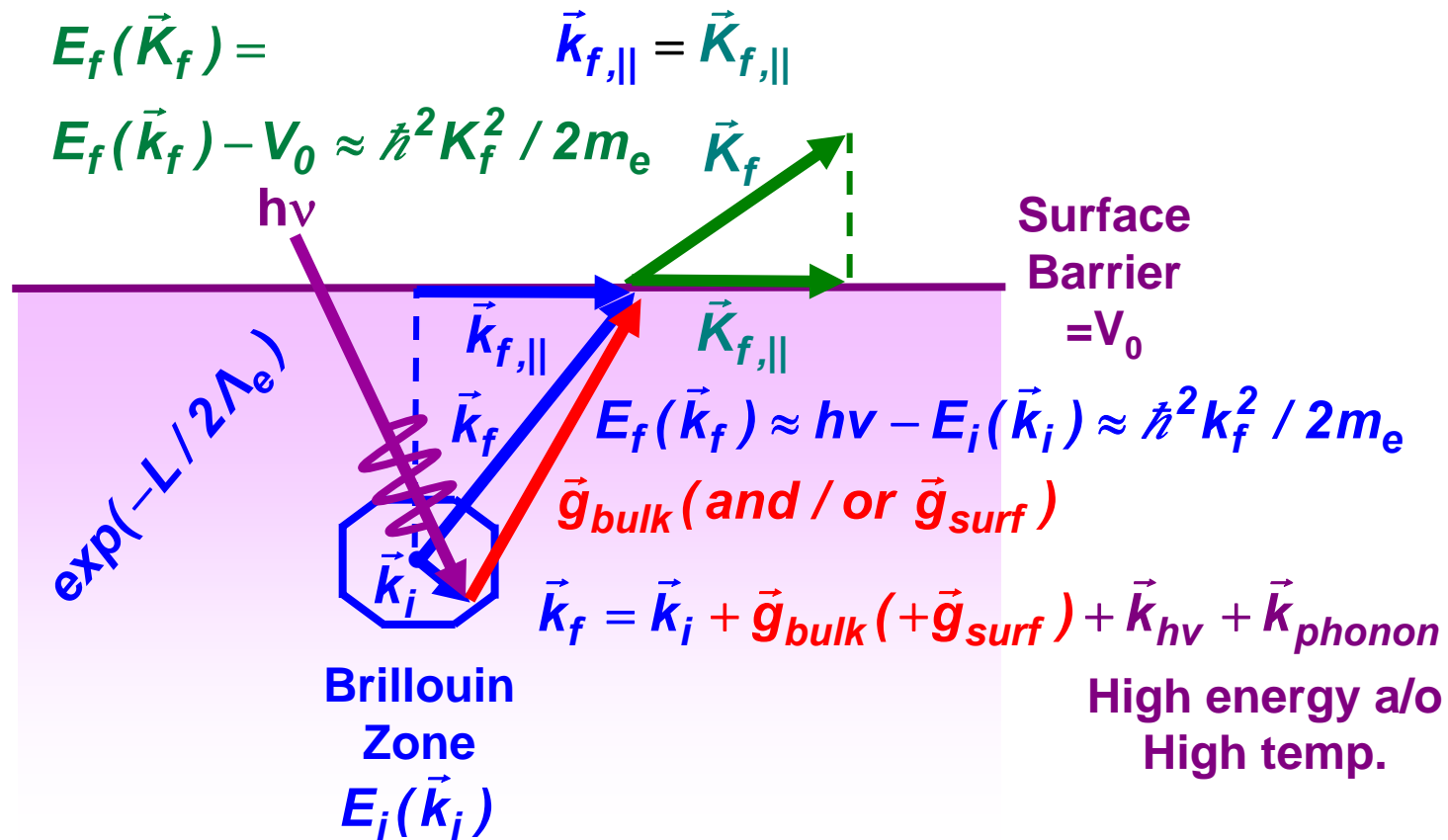
$$\psi_i(\vec{r}) = u_{\vec{k}_i}(\vec{r}) e^{i\vec{k}_i\cdot\vec{r}}$$



REDUCED ZONE:
= FIRST BRILLOUIN
ZONE



Valence-band photoemission: Angle-Resolved Photoemission (ARPES)



$$I(E_f, \vec{k}_f) \propto \left| \hat{\epsilon} \cdot \left\langle \varphi_{photoe}(E_f = h\nu + E_i, \vec{k}_f = \vec{k}_i + \vec{g}) \middle| \vec{r} \middle| \varphi(E_i, \vec{k}_i) \right\rangle \right|^2$$

“Direct” or k-conserving transitions

Fig. 13

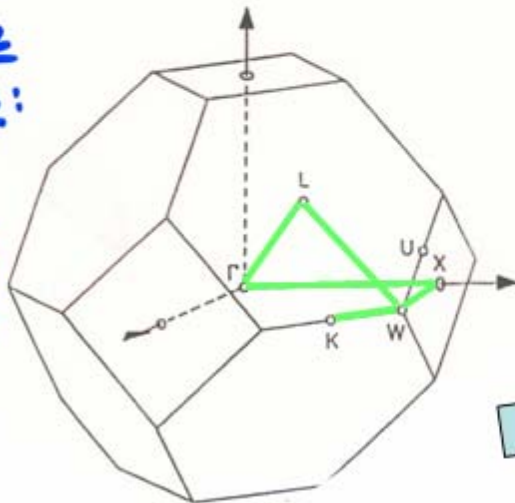
The electronic structure of a nearly free-electron metal—fcc Al

$$\phi(\vec{r}) = u_{\vec{k}}(\vec{r}) e^{i\vec{k}\cdot\vec{r}}; E(\vec{k}) \approx \frac{\hbar^2 k^2}{2m}$$

(Bloch)

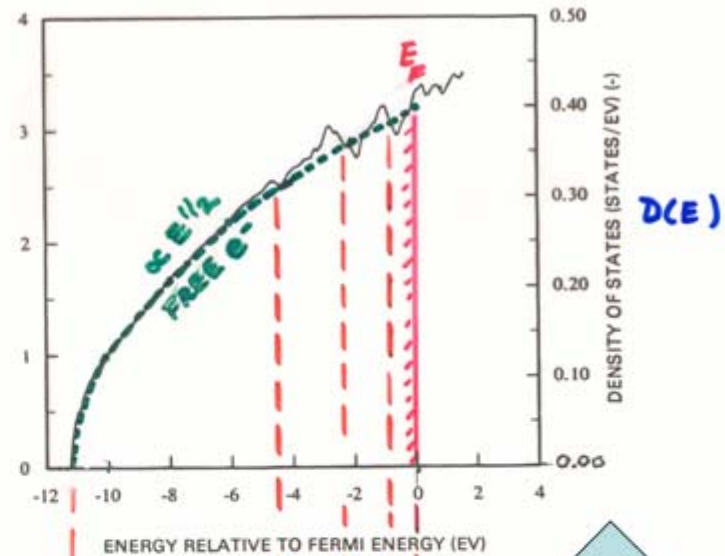
3D Brillouin zone

REAL
fcc:
↓
RECIP.
bcc

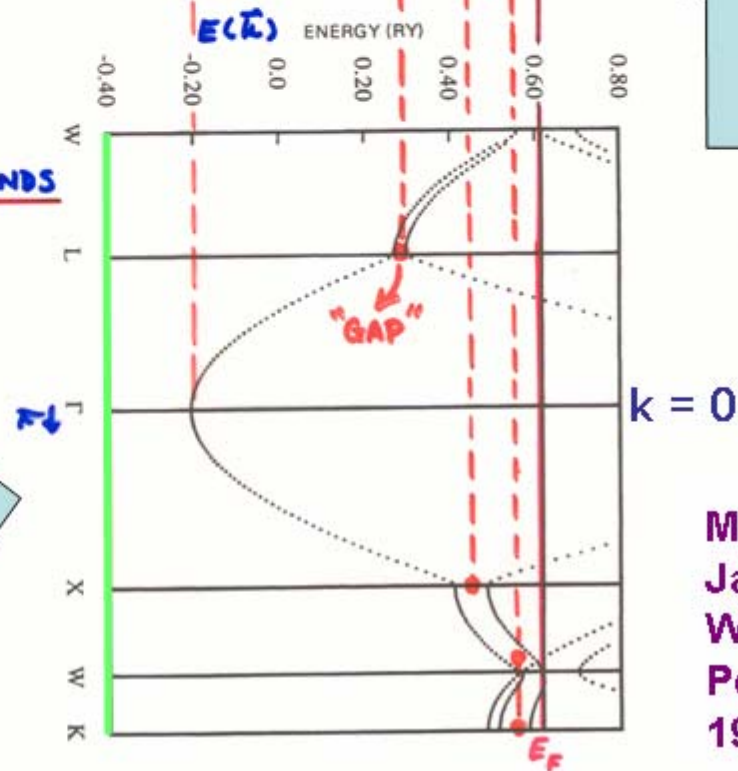


ALUMINUM - ELECTRONIC BANDS & D.O.S.

D.O.S.



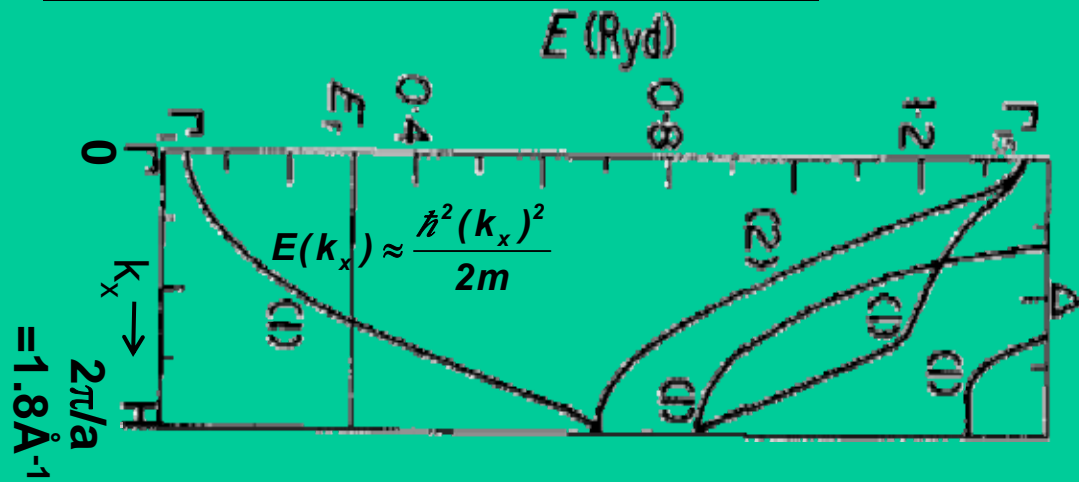
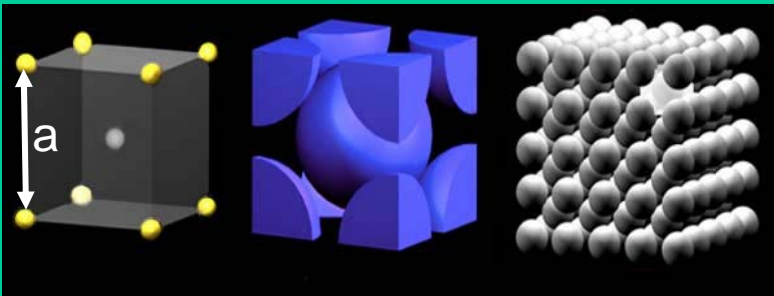
BANDS



Moruzzi,
Janak,
Williams,
Pergamon,
1978

Electronic bands and density of states for “free-electron” metals-
 Rydberg = 13.605 eV

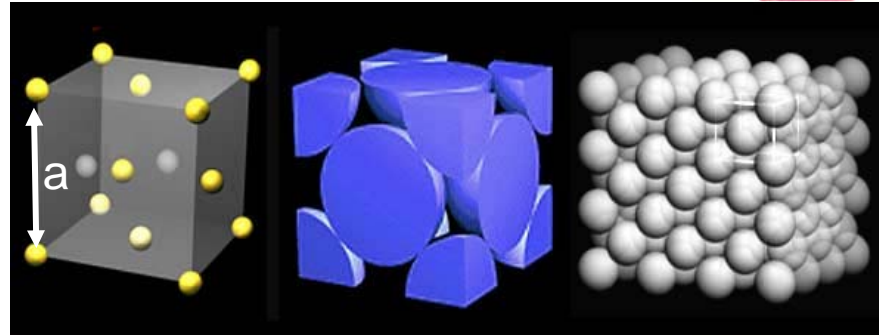
Lithium—bcc, $a = 3.49 \text{ \AA}$
 $1s^2 2s^1$



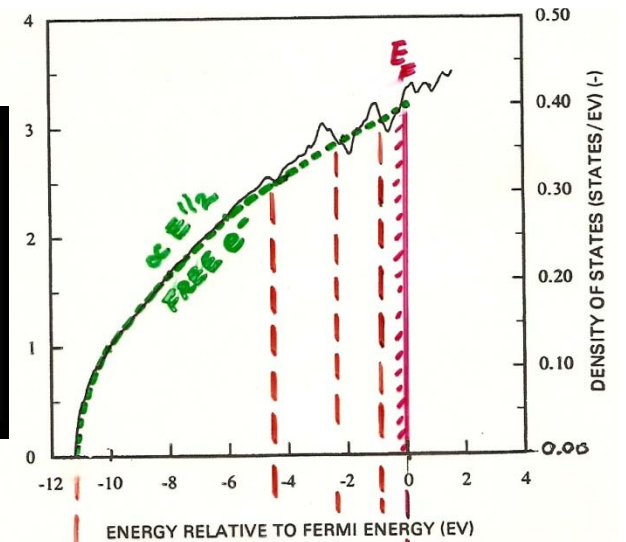
Electronic bands and density of states for “free-electron” metals-

Rydberg = 13.605 eV

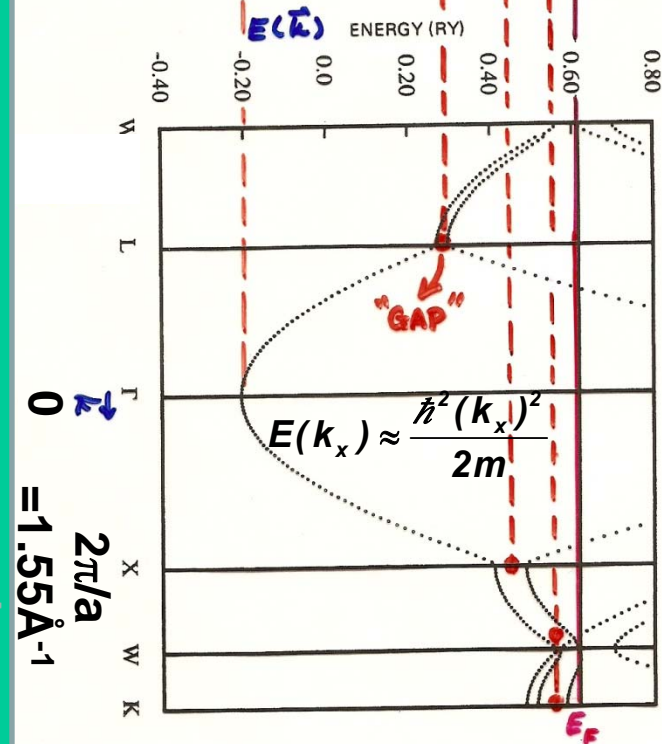
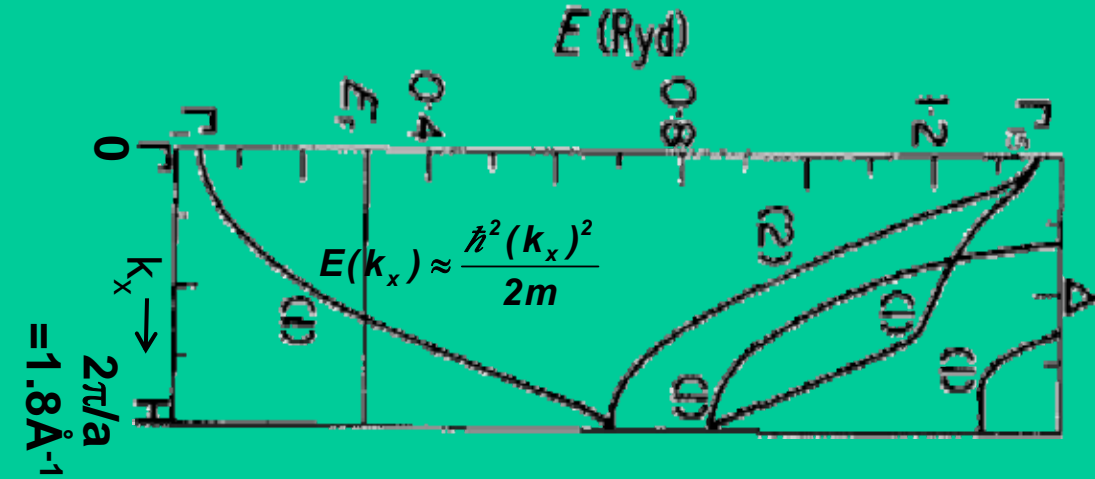
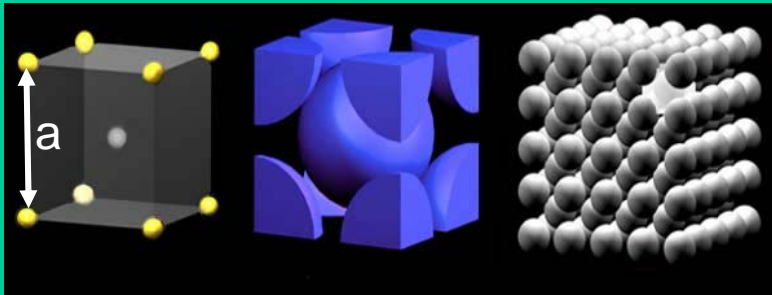
Aluminum—fcc,
 $a = 4.05 \text{ \AA}$
 $1s^2 2s^2 2p^6 3s^2 3p^1$



D.O.S.



Lithium—bcc, $a = 3.49 \text{ \AA}$
 $1s^2 2s^1$

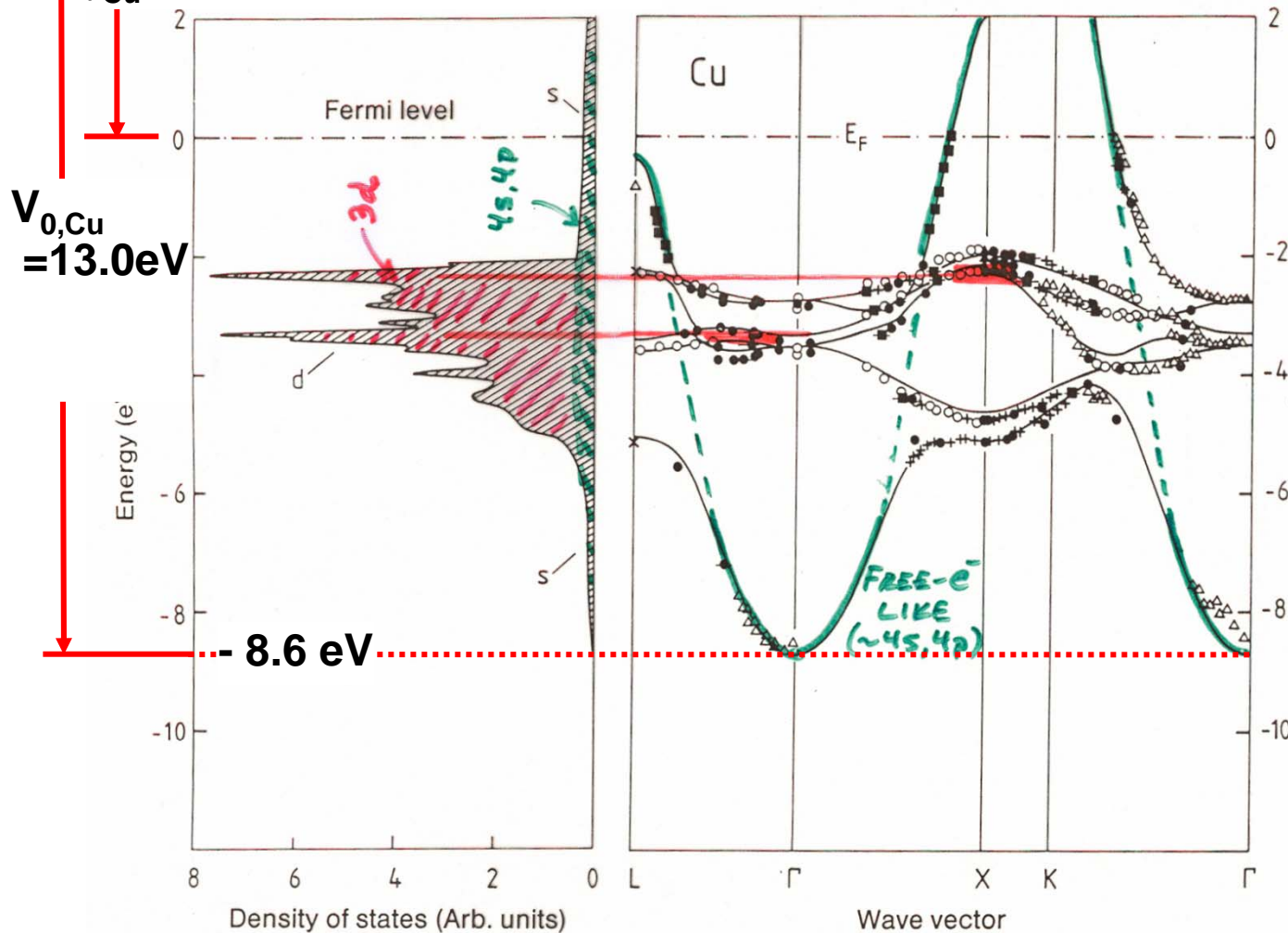


Vacuum level

The electronic structure of a transition metal—fcc Cu

$\phi_{\text{Cu}} = 4.4 \text{ eV} = \text{work function}$

$V_{0,\text{Cu}} = 13.0 \text{ eV}$



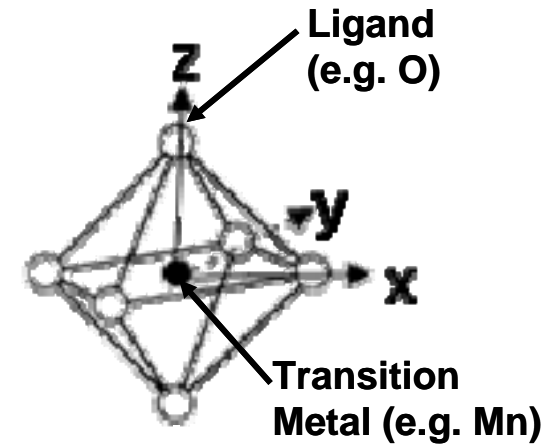
Cu $1s^2 \dots 3d^{10} 4s^1$
ELECTRONIC BANDS
+ DENSITY OF STATES

} MIXING
} 3d LIKE
} MIXING

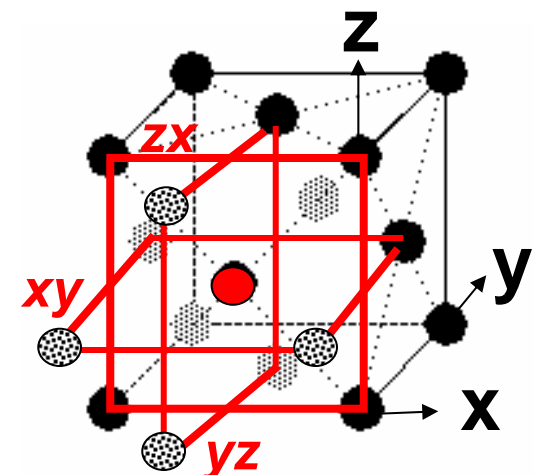
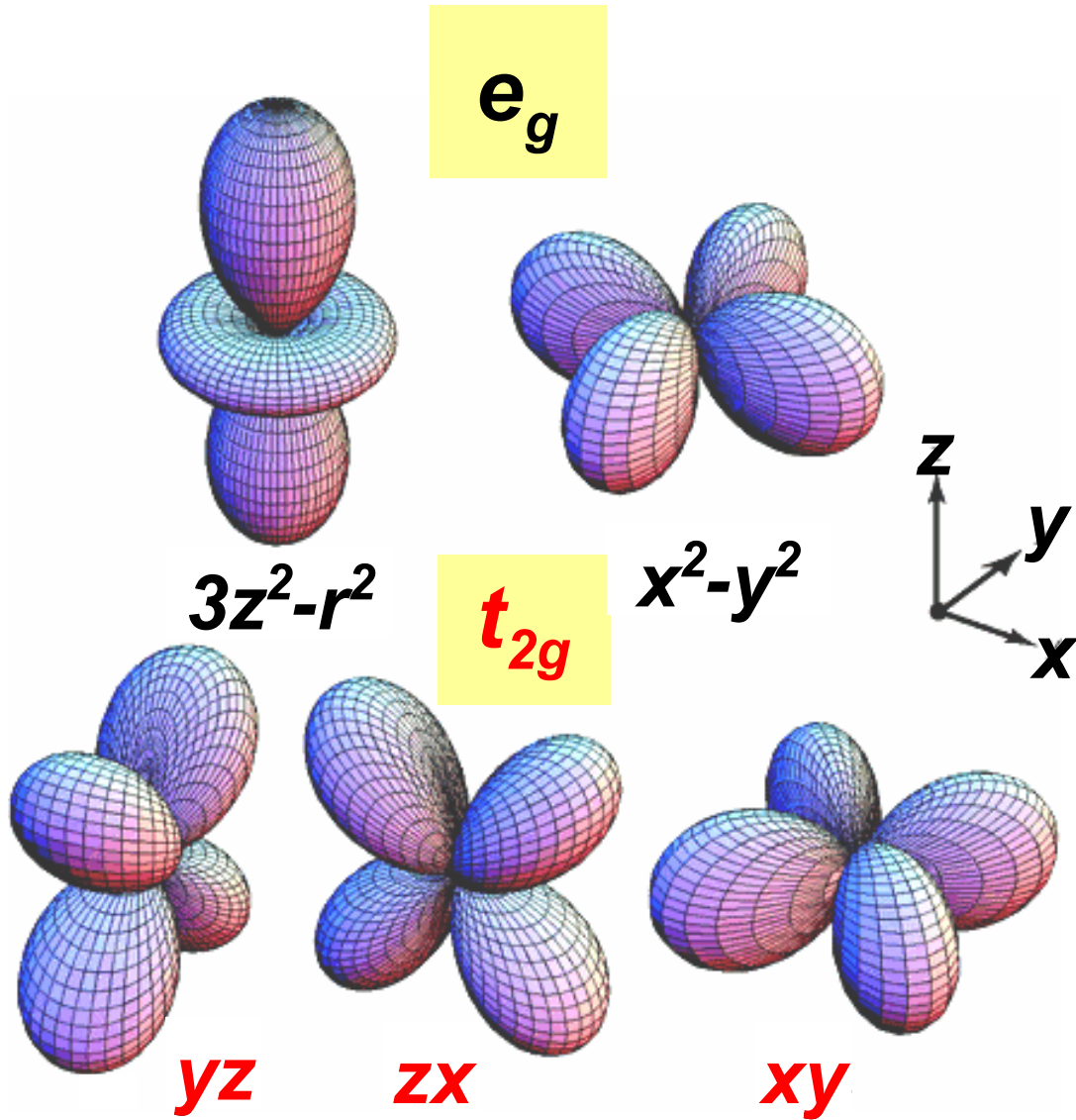
Experimental points from angle-resolved photoelectron spectroscopy (more later)

Fig. 7.12. Bandstructure $E(k)$ for copper along directions of high crystal symmetry (right). The experimental data were measured by various authors and were presented collectively by Courths and Hüfner [7.4]. The full lines showing the calculated energy bands and the density of states (left) are from [7.5]. The experimental data agree very well, not only among themselves, but also with the calculation

And the d orbitals are not equivalent in different bonding environments:

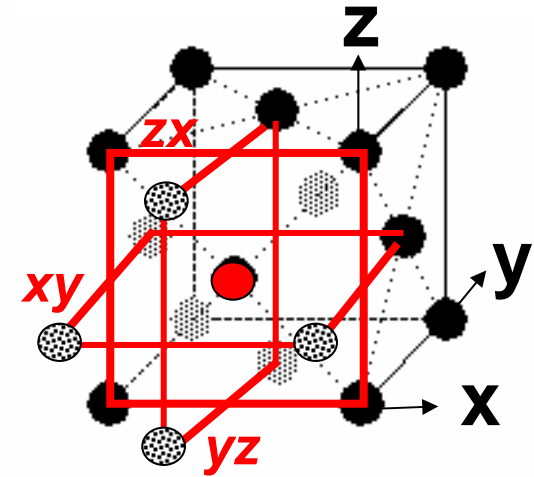
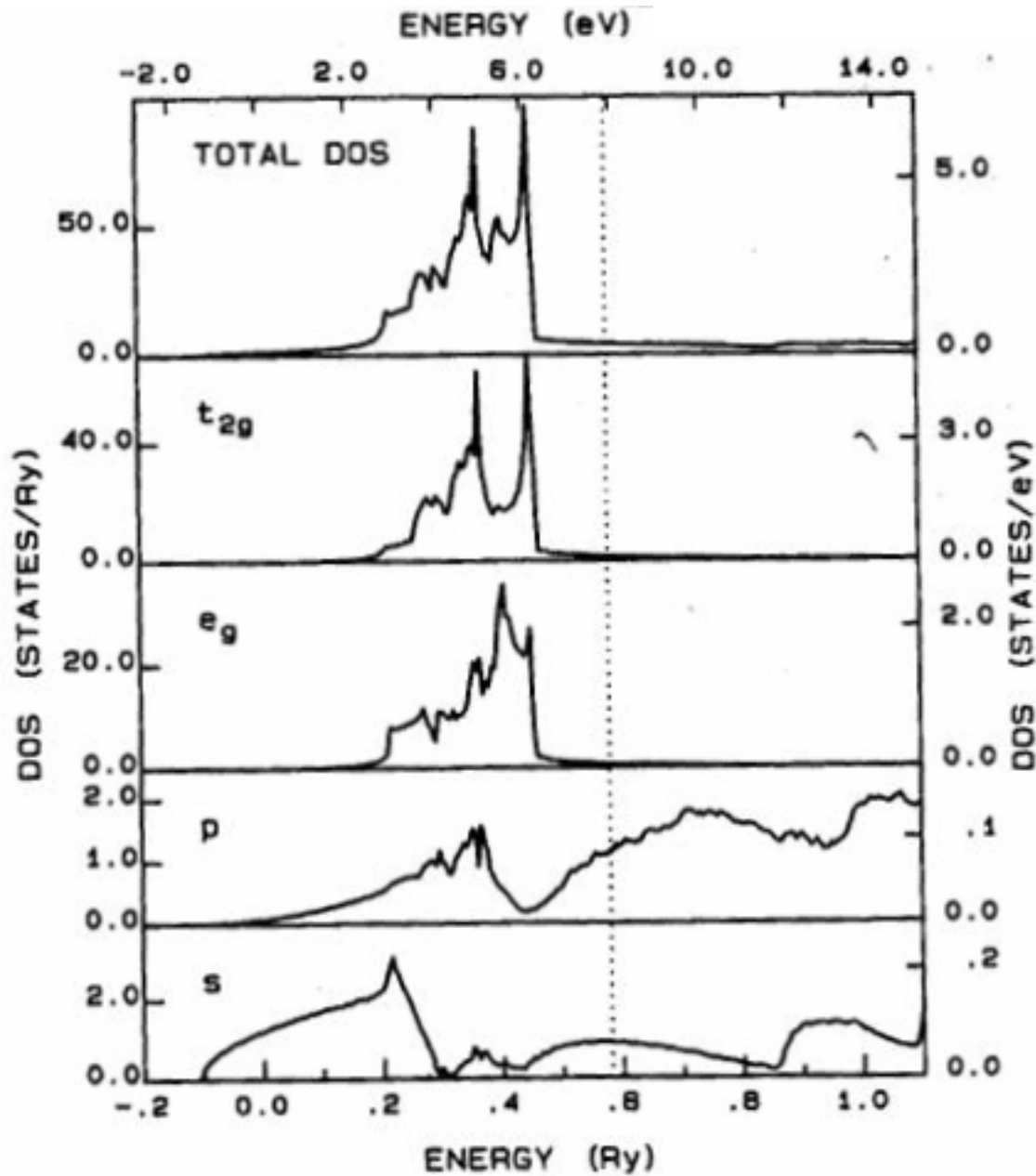


e_g and t_{2g} not equivalent in octahedral (cubic) environment



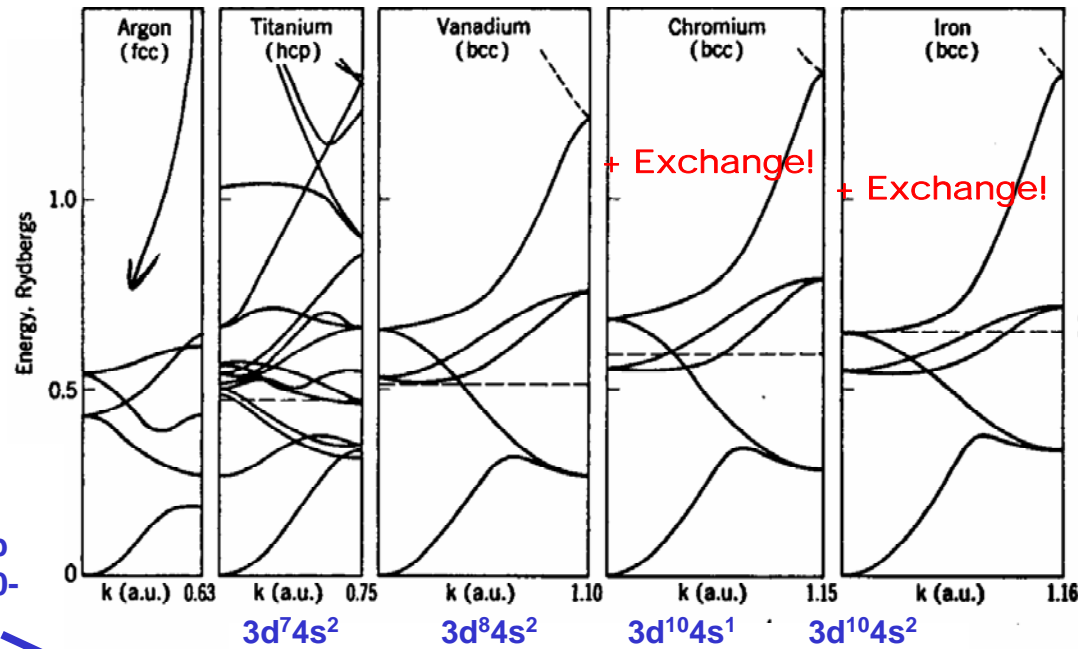
Face-centered cubic—
12 nearest neighbors

Copper densities of states-total and by orbital type:



The electronic structures of the 3d transition metals—
 ≈ “rigid-band model”

3s²3p⁶ filled + 3d,4s CB 3d²4s² 3d³4s² 3d⁵4s¹ 3d⁶4s²



+ Flat “core-like” Ar 3s, 3p bands at ~-1.0-1.5 Rydbergs

Ti ²²	V ²³	Cr ²⁴	Mn ²⁵	Fe ²⁶	Co ²⁷	Ni ²⁸	Cu ²⁹	Zn ³⁰
3d ²	3d ³	3d ⁵	3d ⁵	3d ⁶	3d ⁷	3d ⁸	3d ¹⁰	3d ¹⁰
4s ²	4s ²	4s	4s ²	4s ²	4s ²	4s ²	4s	4s ²

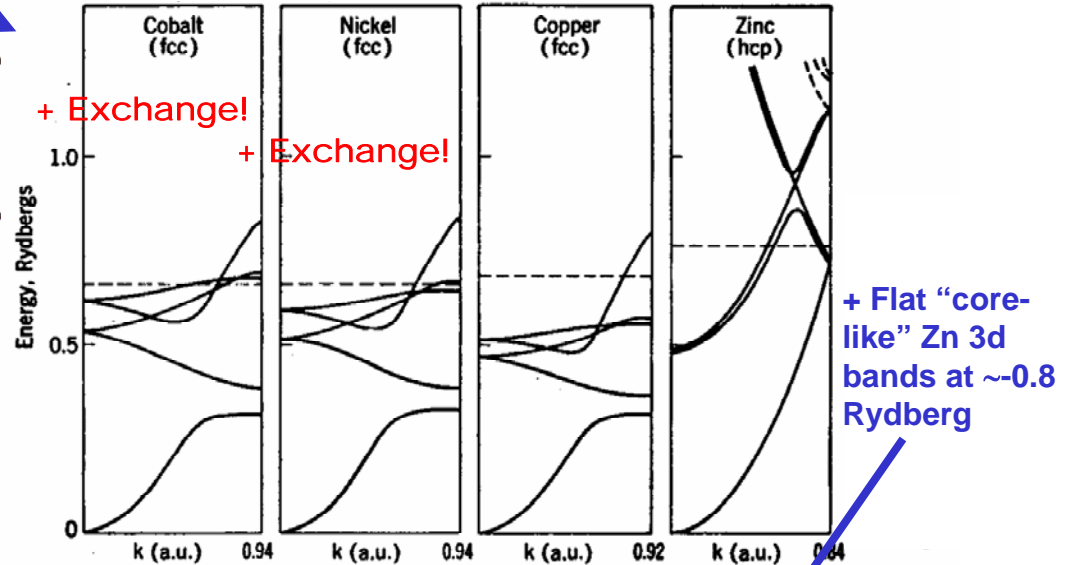
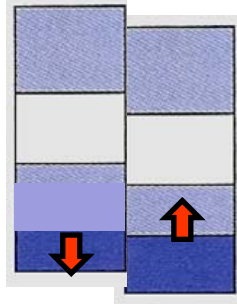
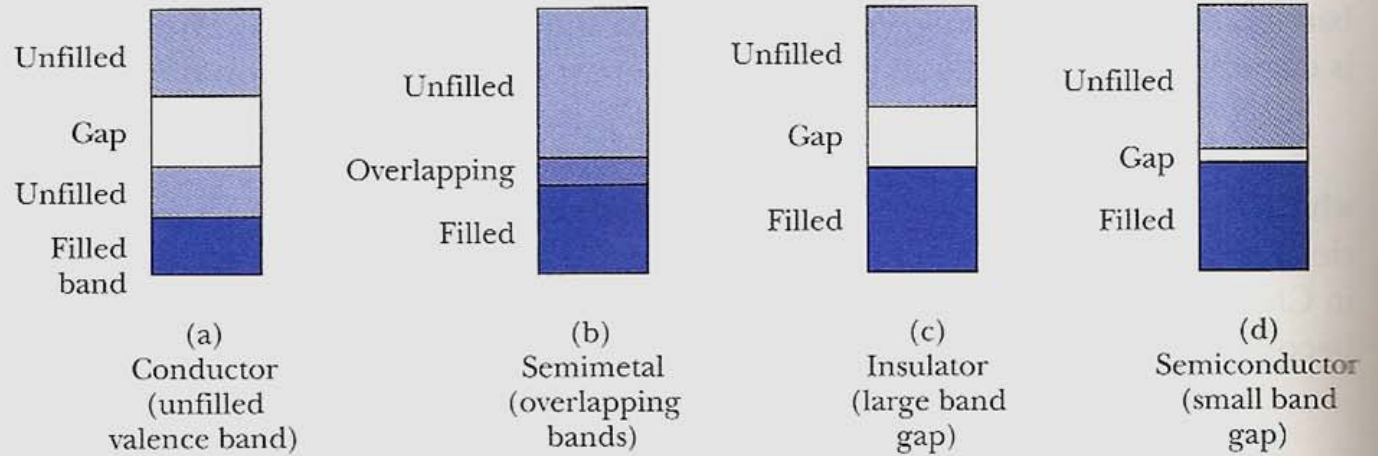


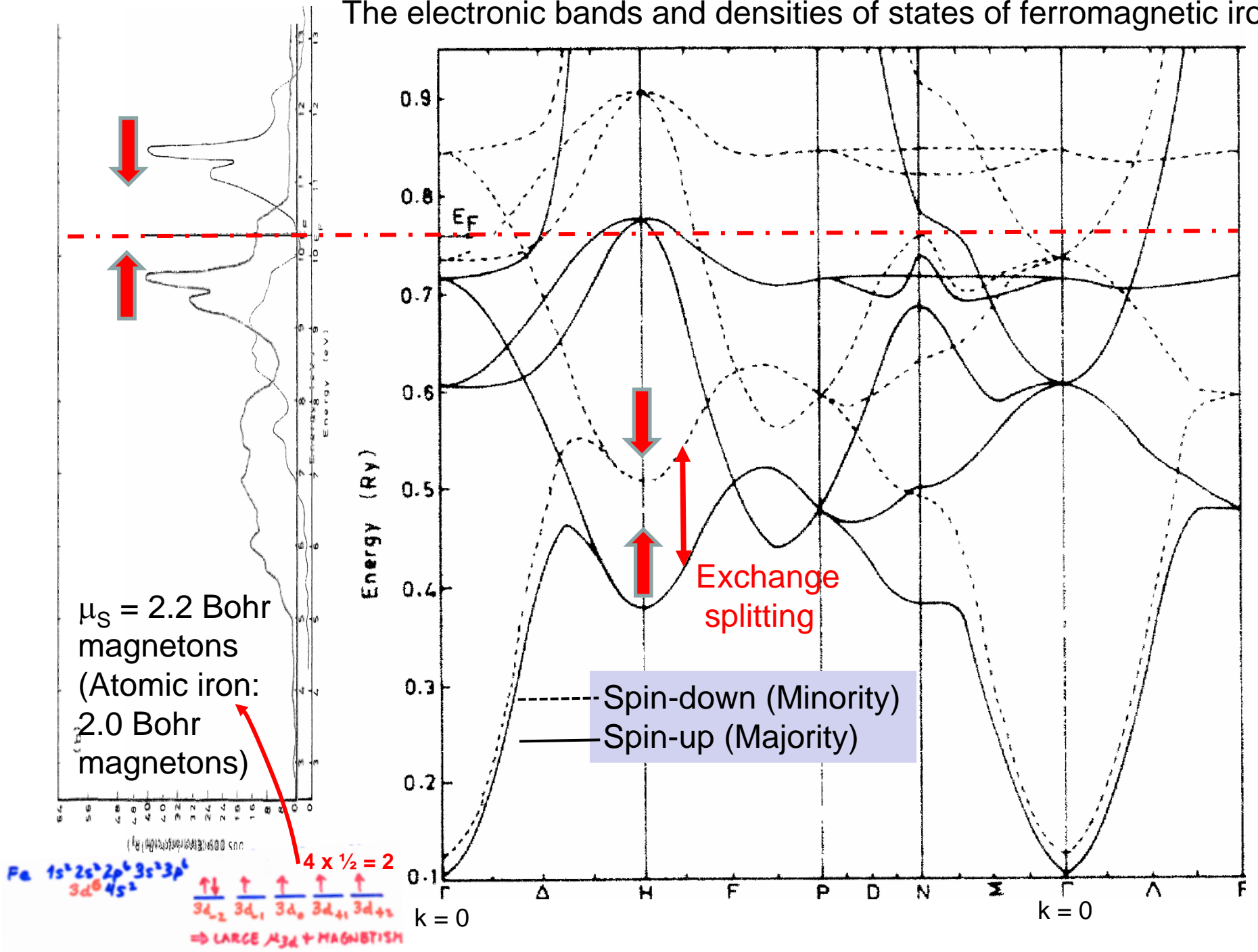
FIG. 10-20. Energy bands of 3d transition elements, along a single direction, from Mattheiss.

Figure 11.6 Possible band structures: (a) a conductor with an unfilled valence band, (b) a conductor with overlapping valence and conduction bands (a semimetal), (c) an insulator due to its large band gap, and (d) a semiconductor (due to its small band gap).



(e)
Spin-down Spin-up
Ferromagnetic
Conductor
(The exchange interaction)

The electronic bands and densities of states of ferromagnetic iron



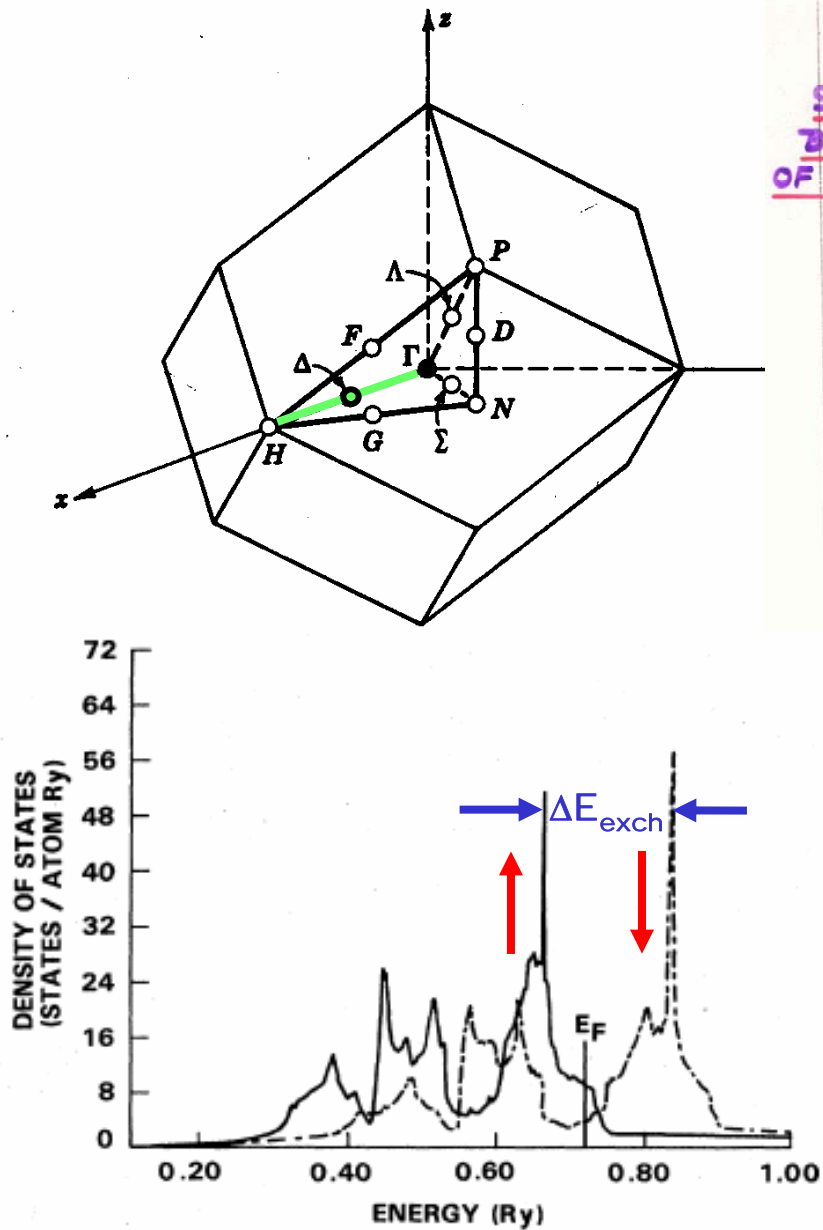
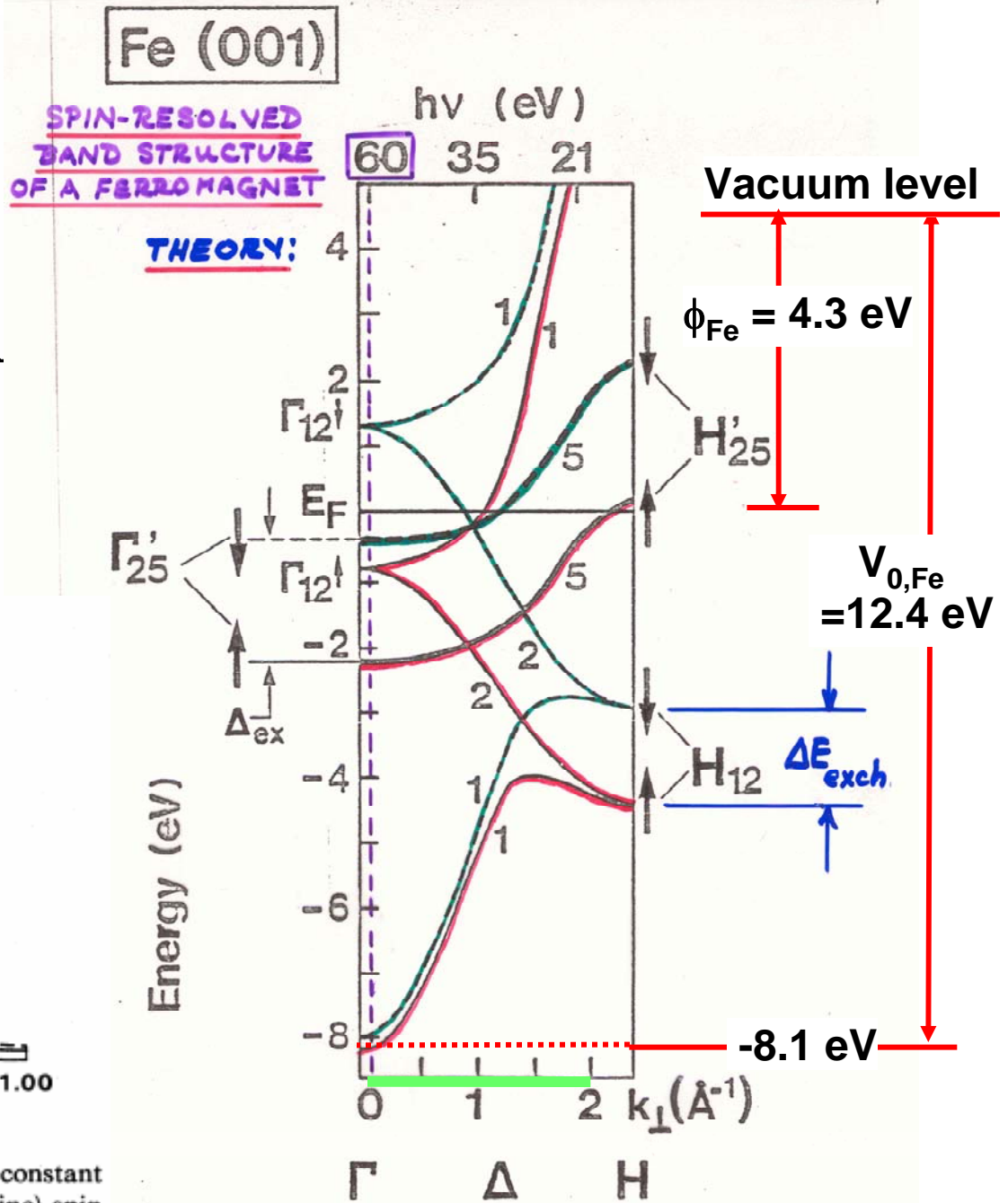


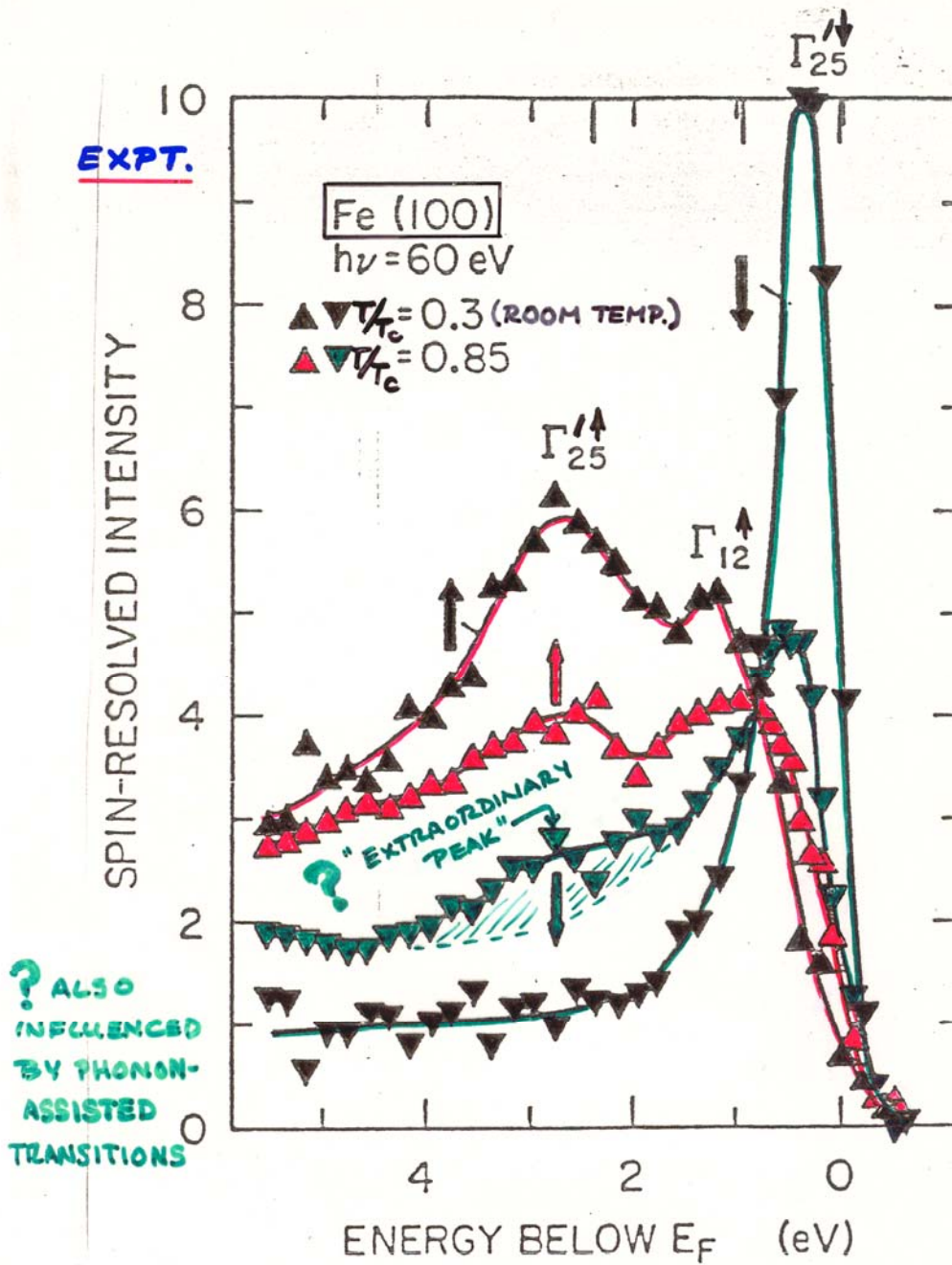
FIG. 4. Density of states at the equilibrium lattice constant of Fe for majority- (solid line) and minority- (broken line) spin states.

Hathaway et al., Phys. Rev. B 31, 7603 ('85)



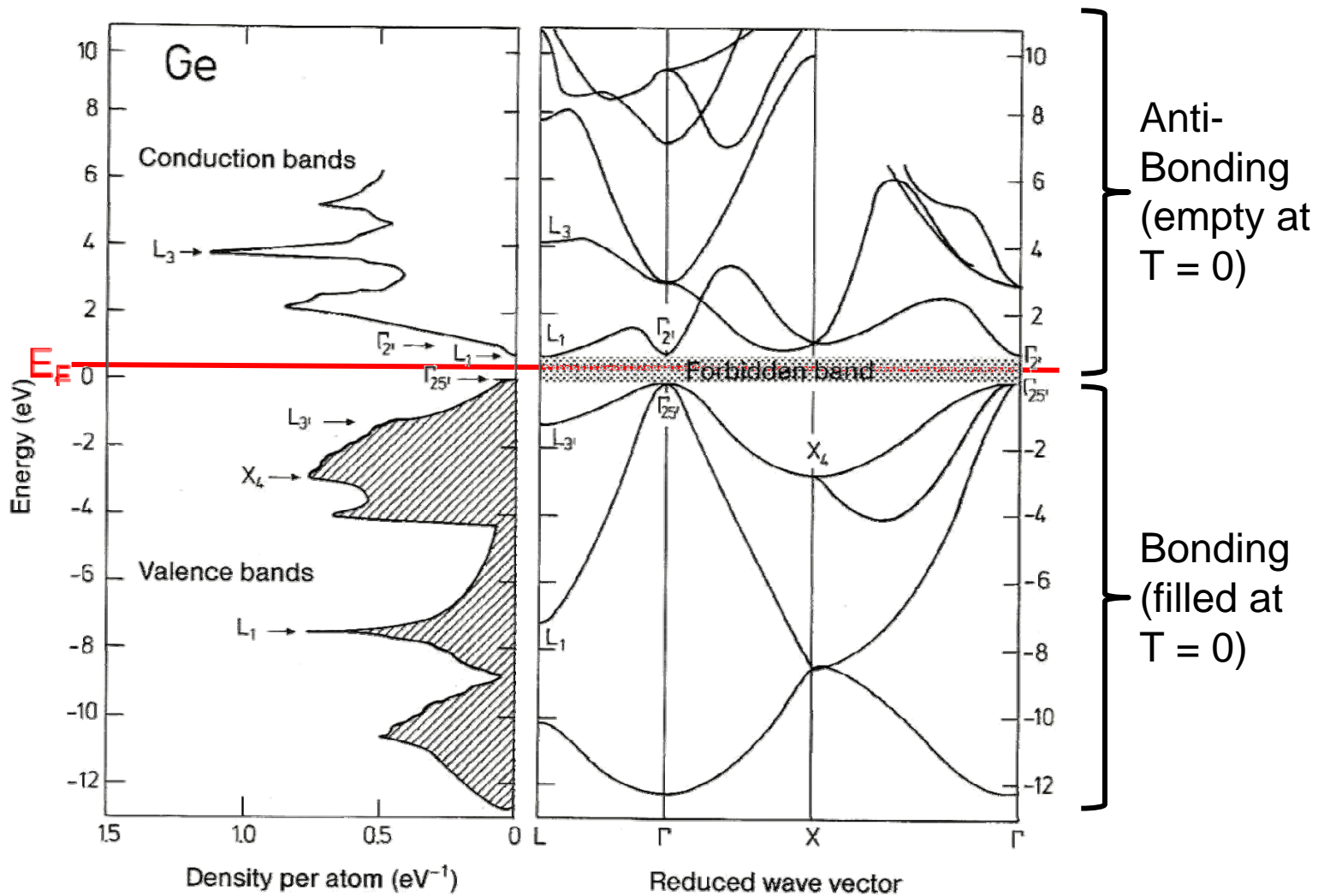
E. KISKER ET AL., PHYS. REV. B
31, 329 (1985)

Fe: ANGLE AND SPIN-RESOLVED SPECTRA AT Γ POINT

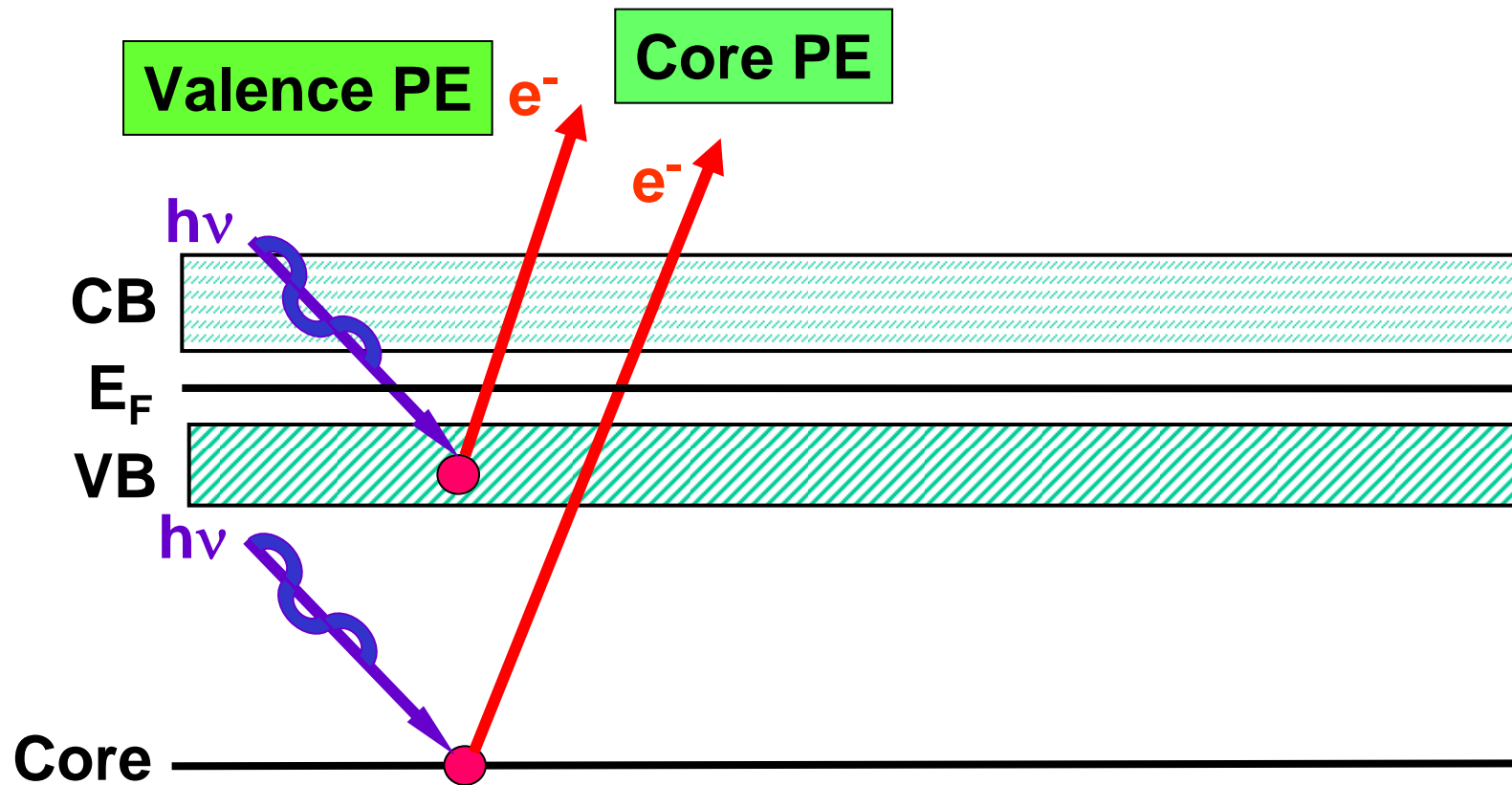


E. KISKER ET AL., PHYS.REV.B
 31, 329 (1985)

Electronic bands and density of states for a semiconductor-Germanium—
 $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^2 4p^2$



The Soft X-Ray Spectroscopies



PE = photoemission = photoelectron spectroscopy

XAS = x-ray absorption spectroscopy

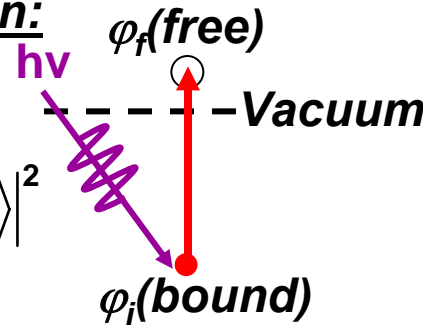
AES = Auger electron spectroscopy

XES = x-ray emission spectroscopy

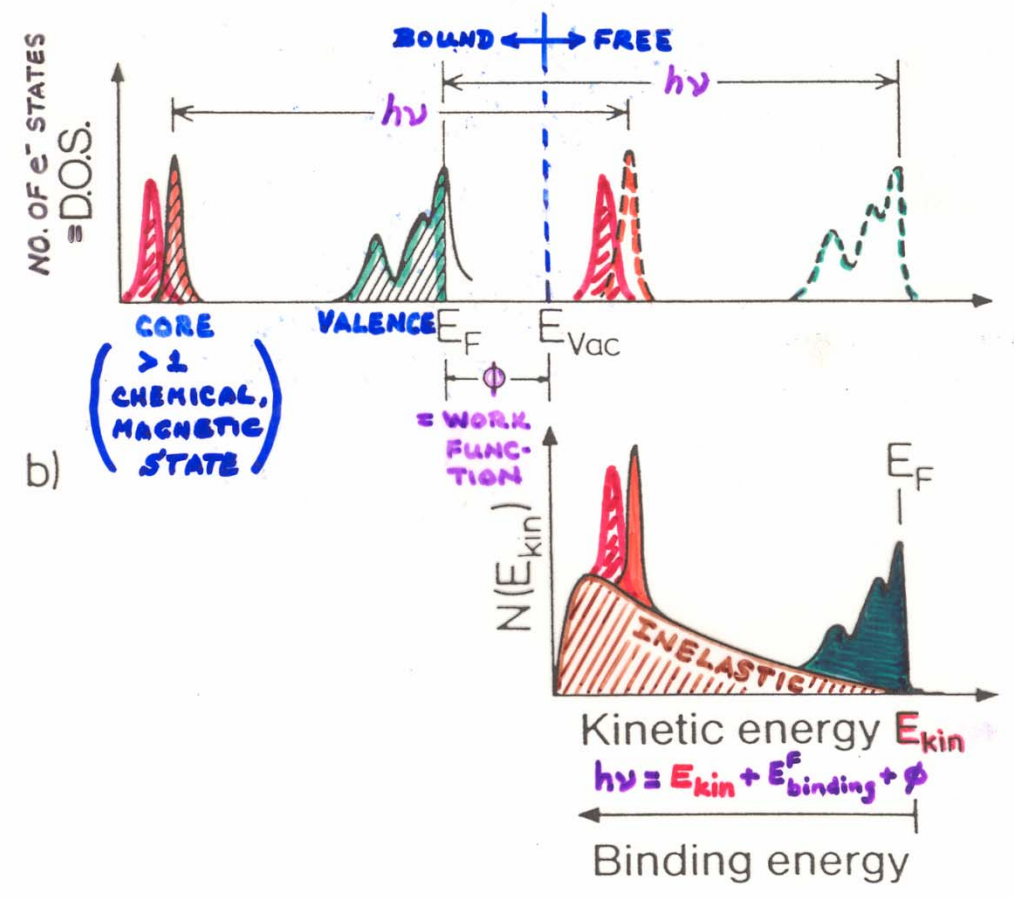
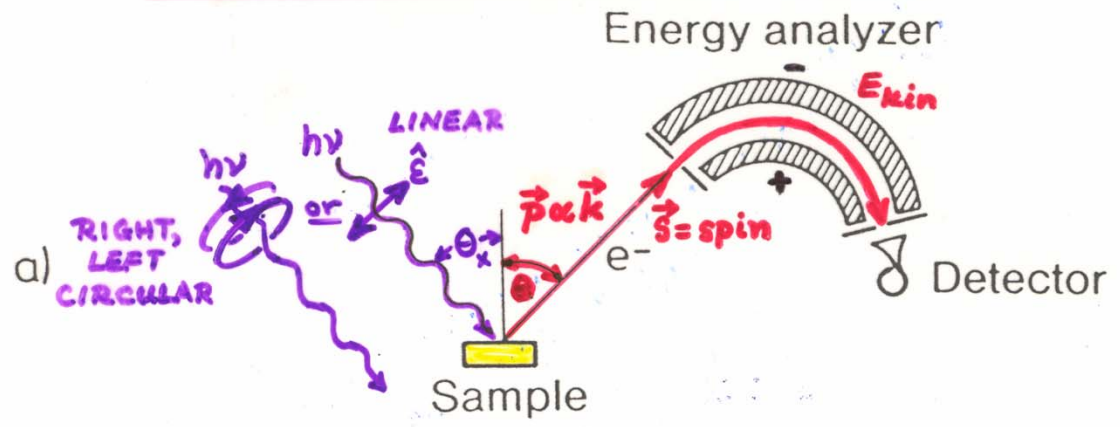
RIXS = resonant inelastic x-ray scattering / x-ray Raman scatt.

MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: DIPOLE LIMIT

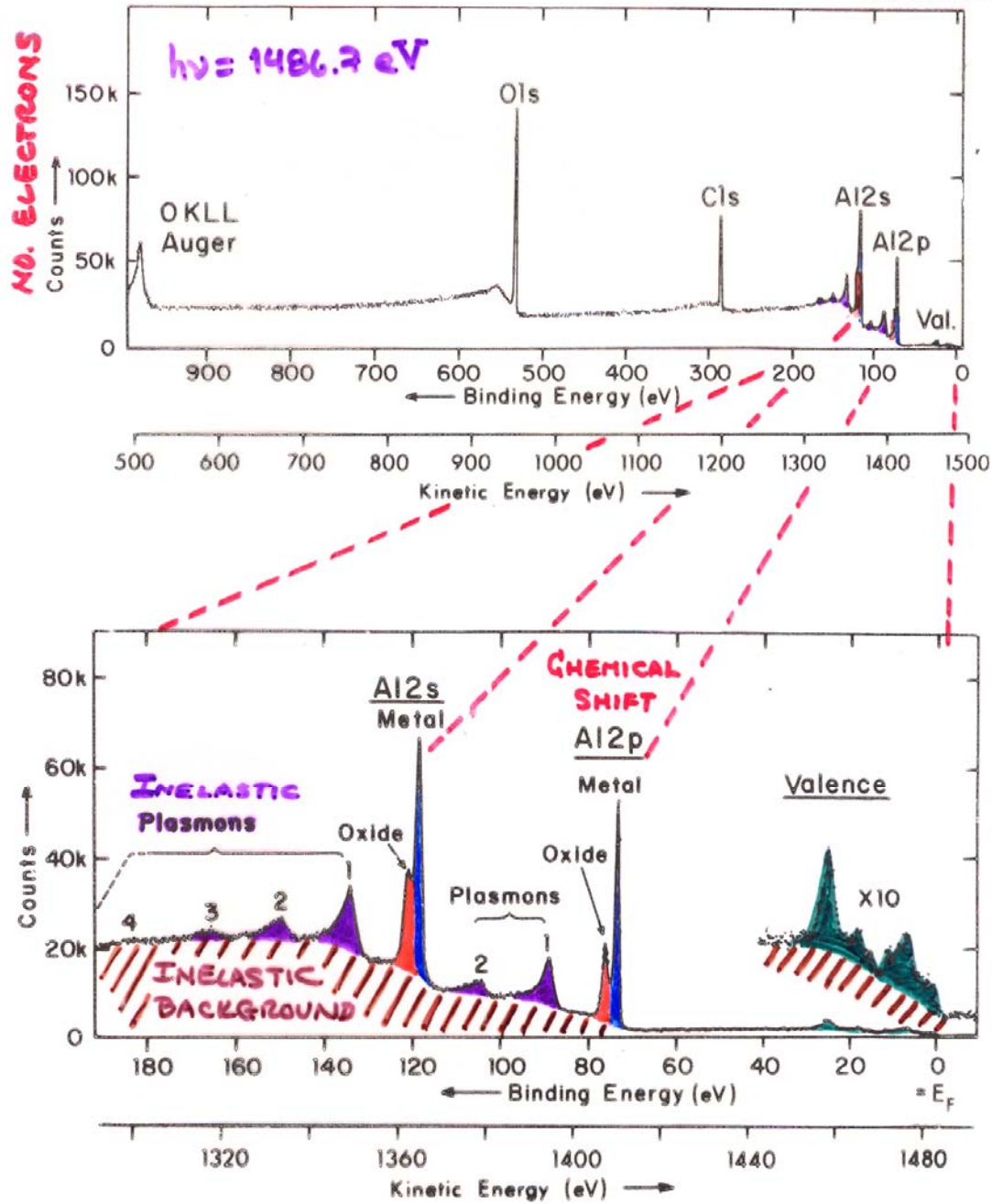
- Photoelectron spectroscopy/photoemission:

$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$


PHOTOELECTRON SPECTROSCOPY



TYPICAL PHOTOELECTRON SPECTRA: OXIDIZED ALUMINUM



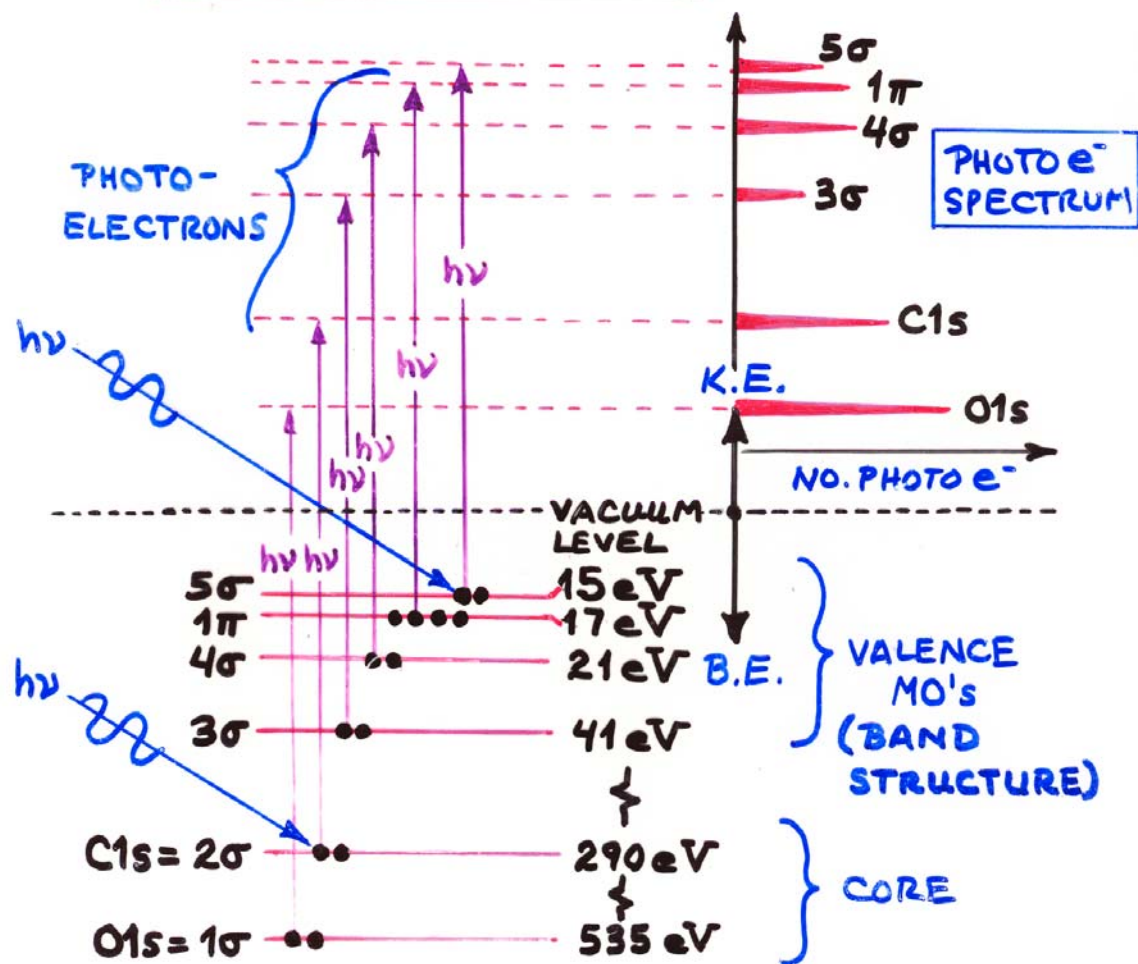
“Basic Concepts of XPS”
Figure 1

PHOTOELECTRON SPECTROSCOPY

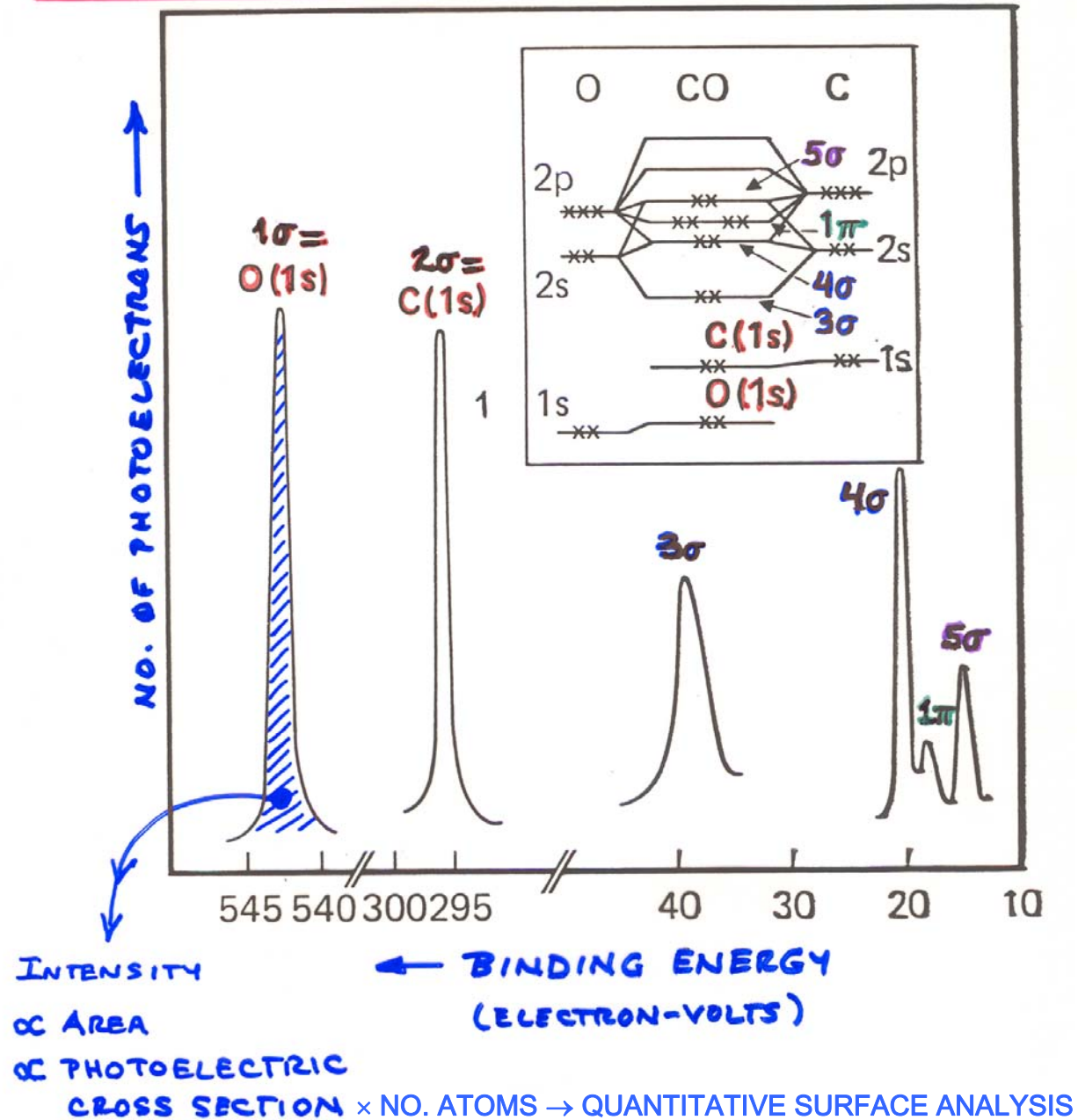
THE PHOTOELECTRIC EFFECT (EINSTEIN, 1905):

$$\begin{aligned}
 & \text{(PHOTON ENERGY)} = \text{(e}^{-}\text{ BINDING ENERGY IN SYSTEM)} + \text{(PHOTOELECTRON KINETIC ENERGY)} \\
 & \text{(ABSORBED)} = \text{B.E.} + \text{K.E.}
 \end{aligned}$$

EXAMPLE - CO MOLECULE:



X-RAY PHOTOELECTRON SPECTRUM OF CO



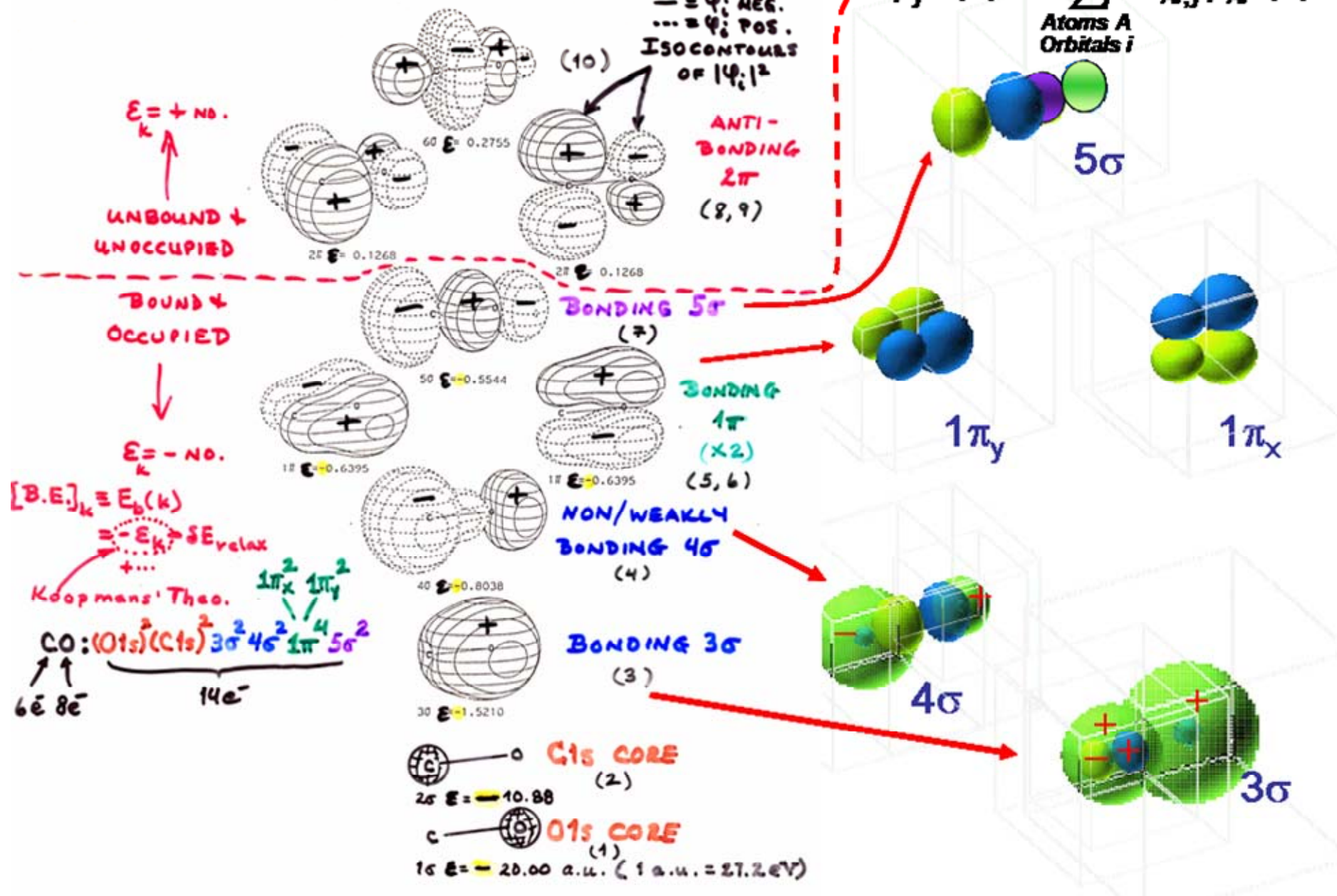
THE ELECTRONS IN CARBON MONOXIDE:

15. Carbon Monoxide

Symmetry: $C_{\infty v}$

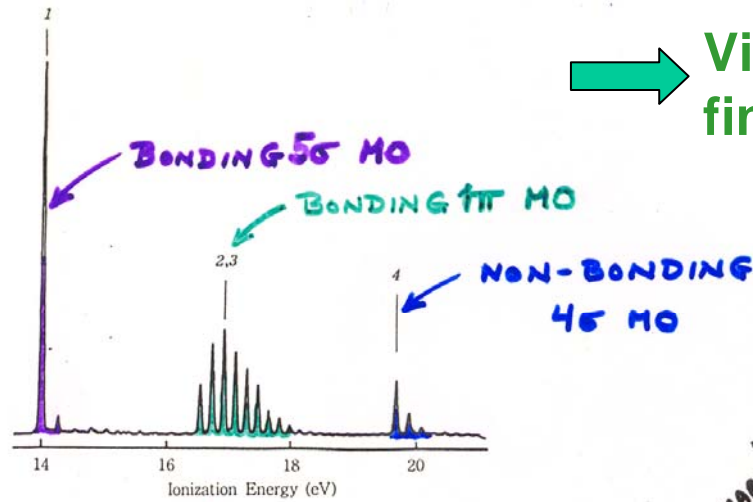
Atomic orbital makeup

$$\varphi_j^{MO}(\vec{r}) = \sum_{\text{Atoms } A} c_{Ai,j} \varphi_{Ai}^{AO}(\vec{r})$$



(9) CO Carbon Monoxide

UV PHOTOELECTRON SPECTRUM OF CO

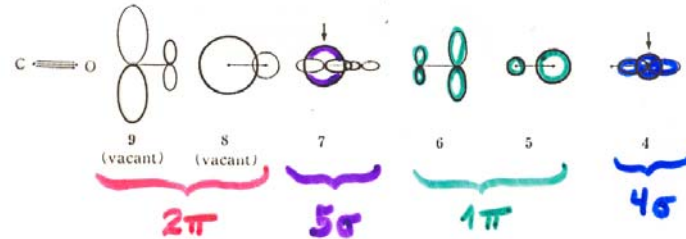


➔ Vibrational fine structure

Exptl. ^{a)} I_v (eV)	Koopmans'		CI FINAL STATE		
	$-\epsilon$ (eV)	SCF MO [6-31 G] ^{b)}	CI (Ionic State) [6-31 G] ^{c)}	State	Configuration
1	14.01	14.99	5σ (7) σ_{CO}	13.11	1 ² Σ ⁺ 0.93(7 ⁻¹); -0.15(6 ⁻¹ , 7 ⁻¹ , 9 ¹) _a ; -0.15(5 ⁻¹ , 7 ⁻¹ , 8 ¹) _a
2	16.91	17.48	1π (6, 5) π_{bond}	16.69	1 ² Π 0.95(6 ⁻¹); 0.95(5 ⁻¹)
3	16.91	17.48			
4	19.72	21.69	4σ (4) n_O	19.29	2 ² Σ ⁺ 0.92(4 ⁻¹); +0.16(6 ⁻¹ , 7 ⁻¹ , 9 ¹) _a ; +0.16(5 ⁻¹ , 7 ⁻¹ , 8 ¹) _a

PRIMARY HOLES
RELAX. + CORREL.

a) The spectrum: this work. The I_v 's: Turner *et al.* (215). See also other works: Turner and May (215 a); Carlson and Jonas (54); Gardner and Samson (104); Edqvist *et al.* (90); Potts and Williams (182 a); and Natalis *et al.* (165).
 b) We used the bond length reported (A 3); symmetry $C_{\infty h}$. $E_{SCF} = -112.6672$ hartree. In 4-31 G calculations, $E_{SCF} = -112.5524$ hartree and $-\epsilon$ (eV) = 14.93, 17.41, 17.41, and 21.60.
 c) CI-IL (9, 8) = 1π. |N⟩ = 0.98 (SCF). The results obtained in other CI levels are given in Appendix B.



Kimura et al.,
 "Handbook of Hel
 Photoelectron Spectra"

INTENSITIES IN PHOTOELECTRON SPECTRA:

- GENERAL: FINAL STATE K (k -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_c^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPPENHEIMER: e^- 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_c^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION: $\Psi_c \rightarrow \Psi_f \approx \text{PHOTO}$ (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 |\langle \Psi_c^f(N-1, K) | \Psi_R^{\pm}(N-1, K) \rangle|^2$$

$$|\hat{e} \cdot \langle \varphi_f | \vec{r} | \varphi_k \rangle|^2$$

SAME SUBSHELL COUPLING +
TOTAL L, S \rightarrow "MONOPOLE"

$$\rightarrow \text{NORMAL } \frac{d\sigma_K}{d\Omega}$$

- SLATER DETS. FOR $\Psi_c^f = \det(\varphi_1', \varphi_2', \dots, \varphi_{k-1}', \varphi_{k+1}', \dots, \varphi_N')$

$$\Psi_R = \det(\varphi_1, \varphi_2, \dots, \varphi_{k-1}, \varphi_{k+1}, \dots, \varphi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 |\langle \varphi_1' | \varphi_1 \rangle|^2 |\langle \varphi_2' | \varphi_2 \rangle|^2 \dots$$

$$|\langle \varphi_{k-1}' | \varphi_{k-1} \rangle|^2 |\langle \varphi_{k+1}' | \varphi_{k+1} \rangle|^2 \dots |\langle \varphi_N' | \varphi_N \rangle|^2$$

$$|\hat{e} \cdot \langle \varphi_f | \vec{r} | \varphi_k \rangle|^2$$

1e- DIPOLE $\rightarrow d\sigma/d\Omega$

(N-1)e- SHAKE-UP/
SHAKE-OFF \rightarrow
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN φ_f ESCAPE

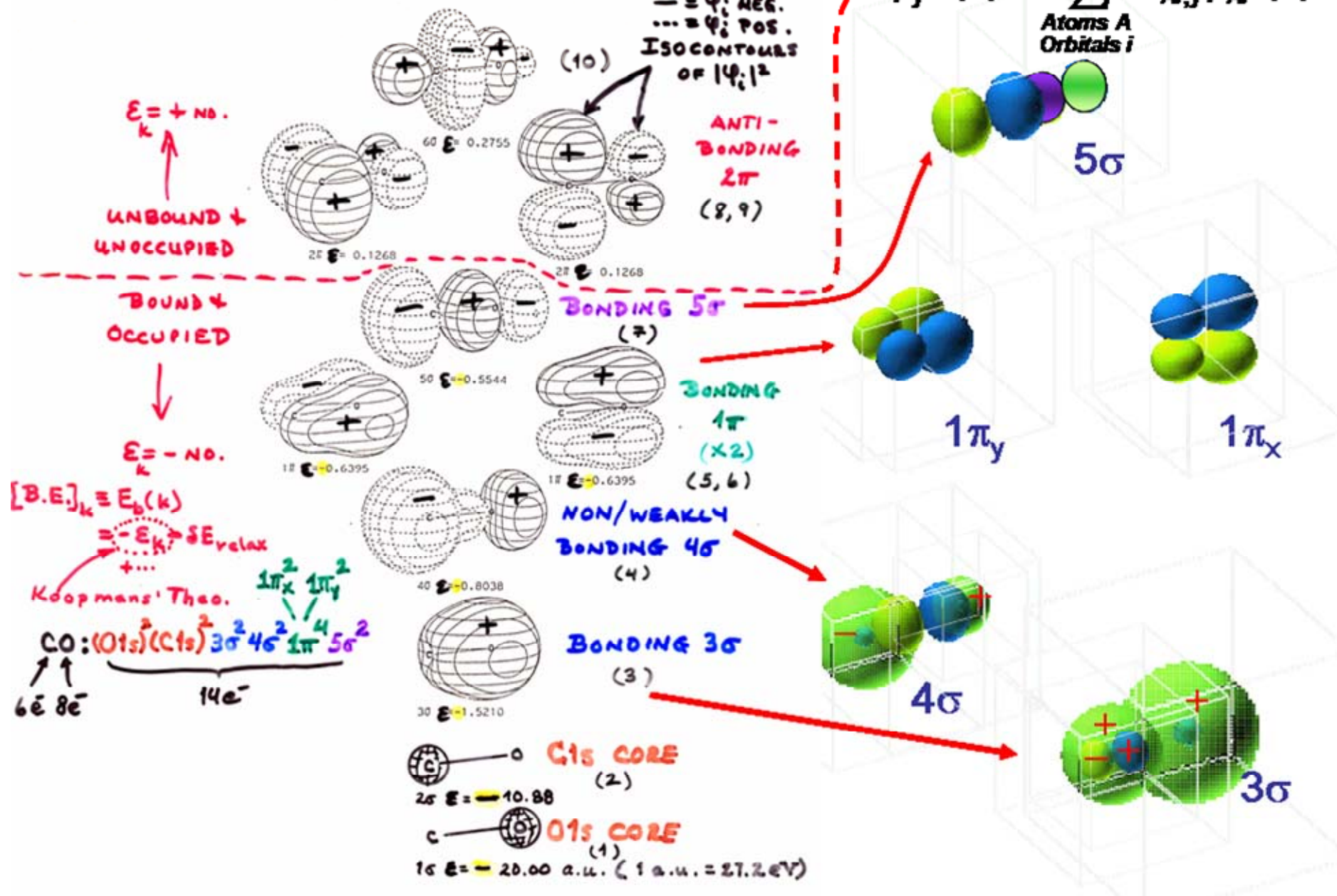
THE ELECTRONS IN CARBON MONOXIDE:

15. Carbon Monoxide

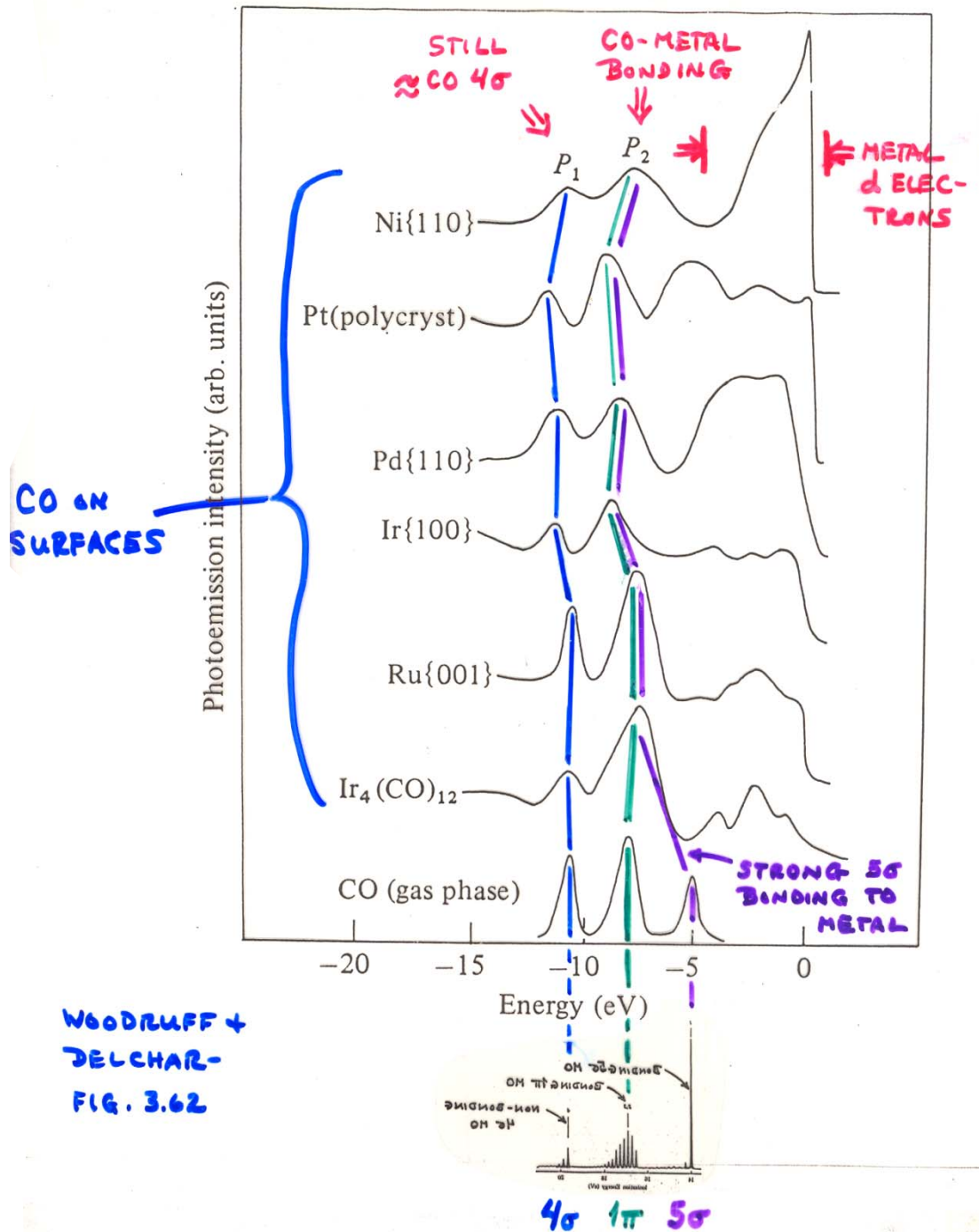
Symmetry: $C_{\infty v}$

Atomic orbital makeup

$$\varphi_j^{MO}(\vec{r}) = \sum_{\text{Atoms } A} c_{Ai,j} \varphi_{Ai}^{AO}(\vec{r})$$



Valence-level Photoelectron spectra of CO adsorbed on various transition metal surfaces



Theoretical Calculations of charge density for CO bound to Ni(001)- “on-top”:

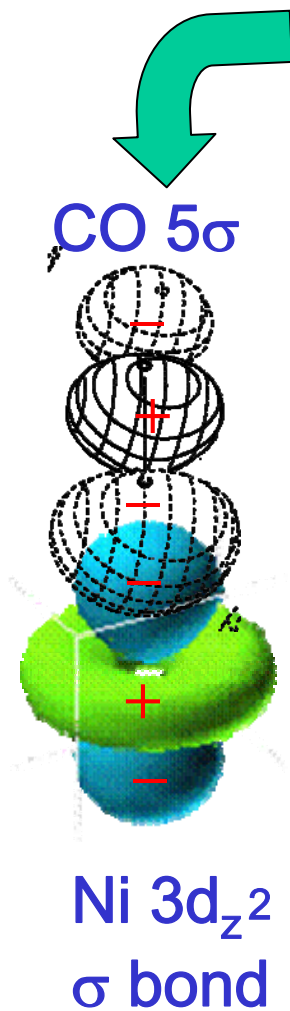
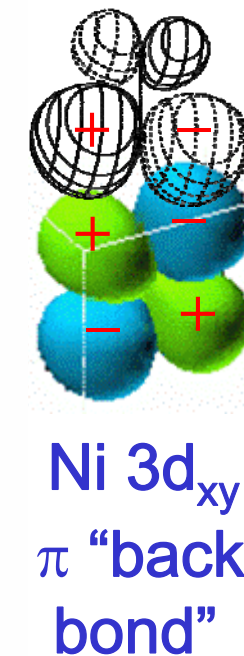
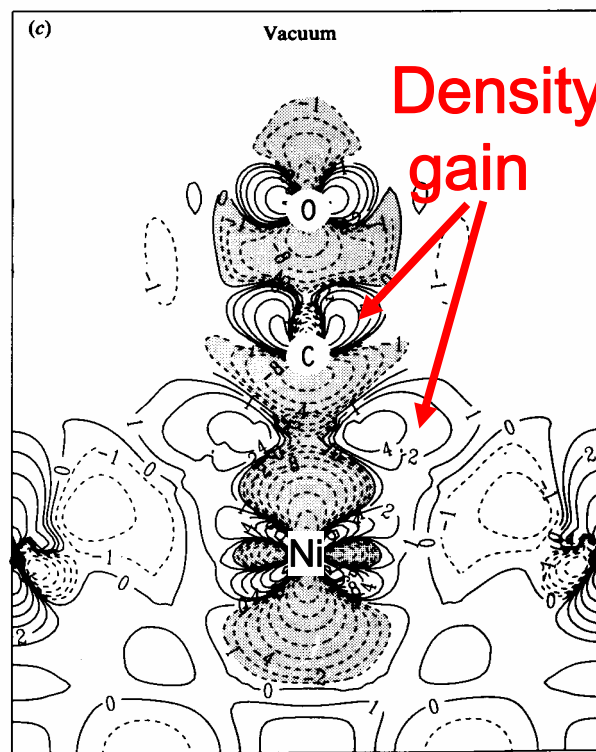
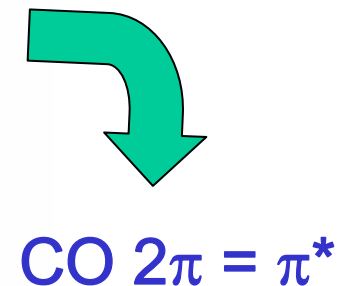
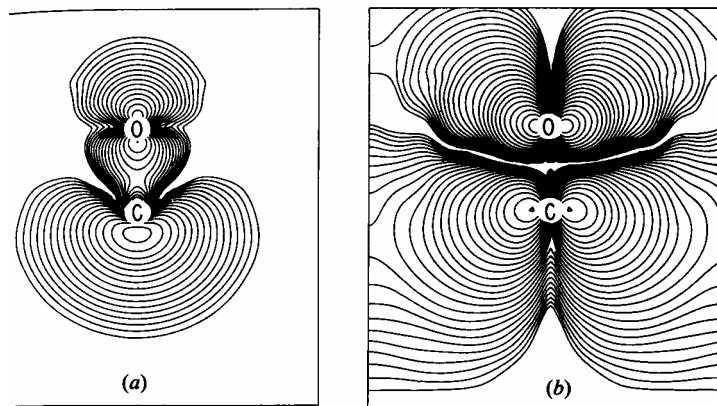
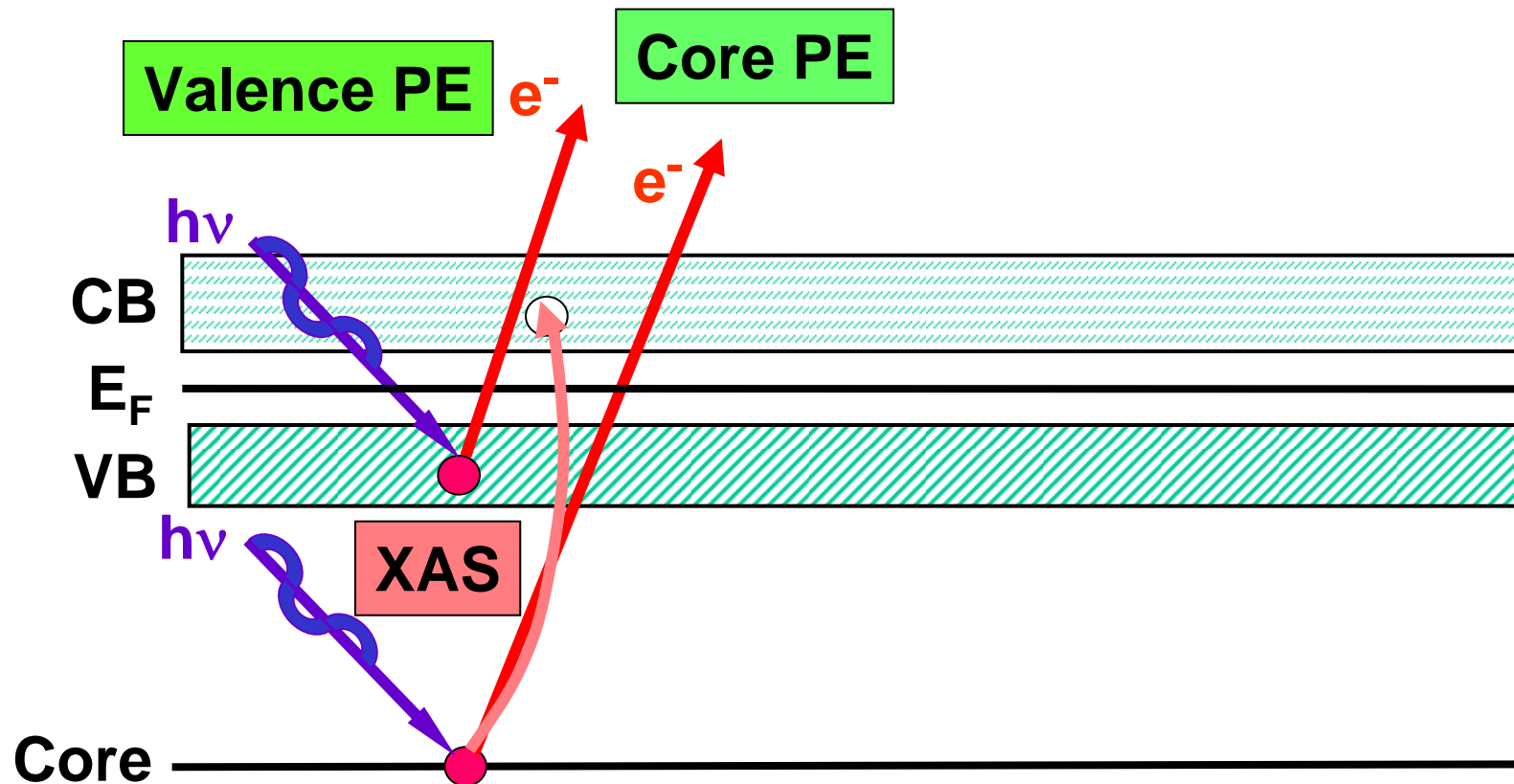


Fig. 12.14. Charge density contour plots appropriate to Ni(100) c(2 × 2)-CO: (a) free molecule 5 σ orbital; (b) free molecule 2 π orbital; (c) difference between CO/Ni(100) and the superposition of clean Ni(100) and an unsupported CO monolayer. Solid (dashed) lines indicate a gain (loss) of electronic charge (Wimmer, Fu & Freeman, 1985).



Zangwill,
p. 307, plus
PRL 55, 2618 ('85)

The Soft X-Ray Spectroscopies



PE = photoemission = photoelectron spectroscopy

XAS = x-ray absorption spectroscopy

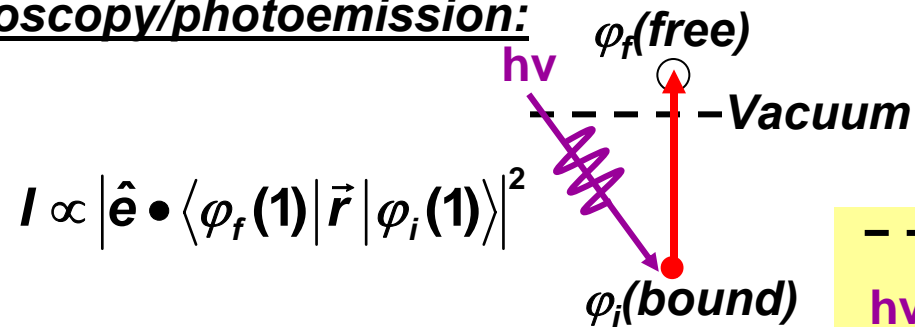
AES = Auger electron spectroscopy

XES = x-ray emission spectroscopy

RIXS = resonant inelastic x-ray scattering / x-ray Raman scatt.

MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: DIPOLE LIMIT

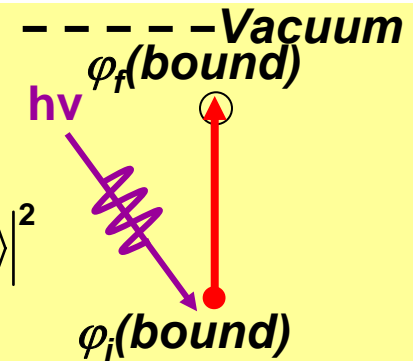
- Photoelectron spectroscopy/photoemission:



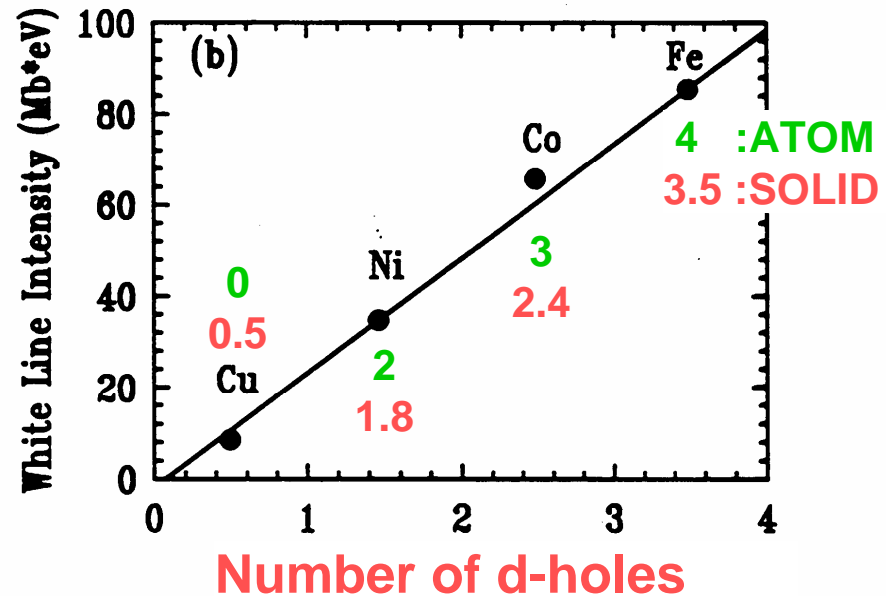
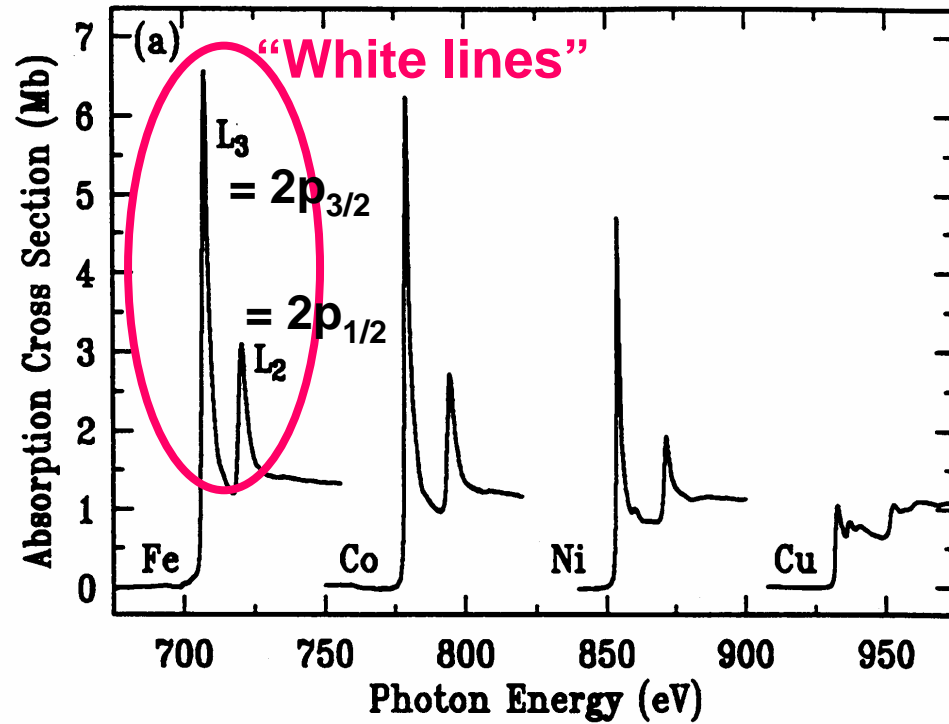
$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$

- Near-edge x-ray absorption:

$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$



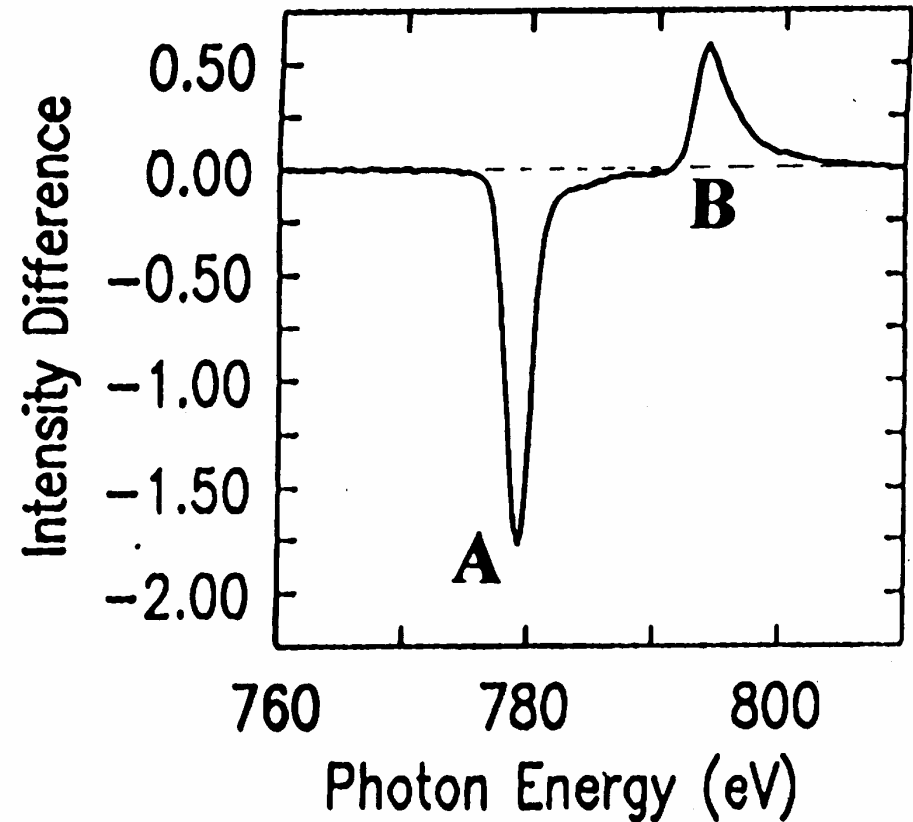
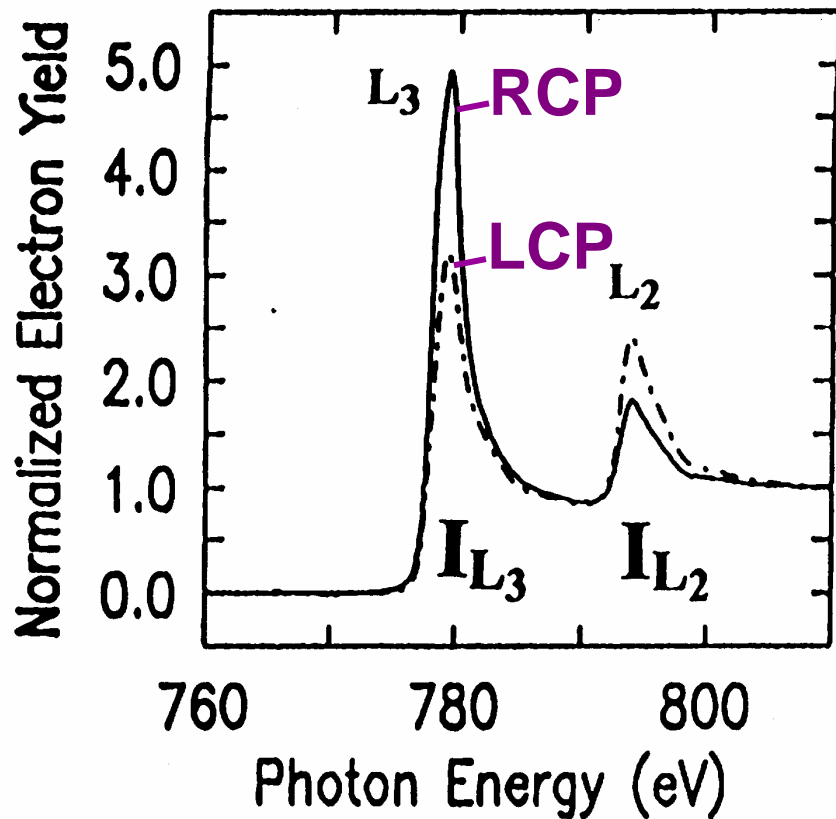
Variation of
Near-Edge X-Ray
Absorption Fine
Structure
(NEXAFS) with Atomic
No. for Some 3d
Transition Metals



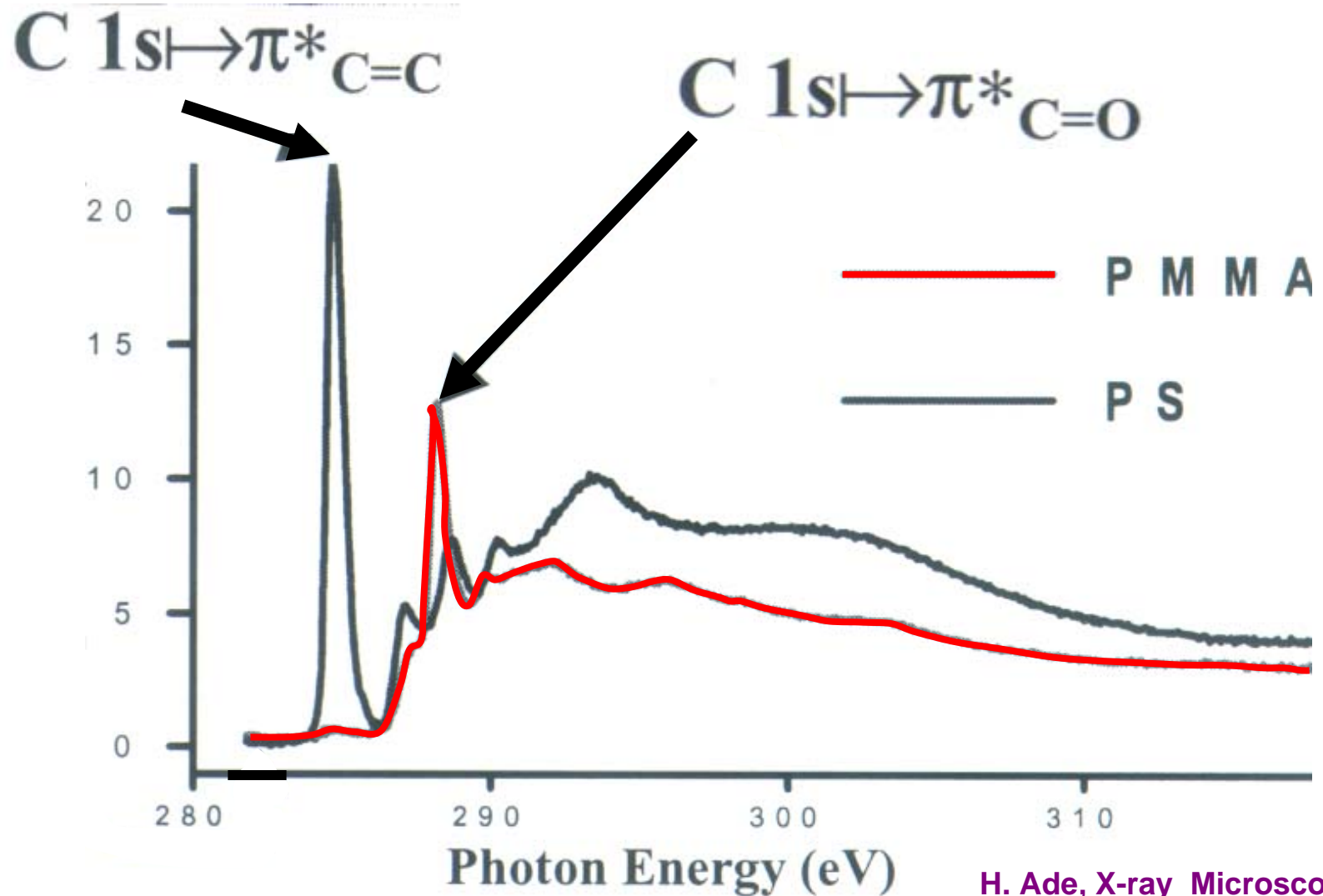
J. Stohr, "NEXAFS
Spectroscopy"

Magnetic Circular Dichroism in X-Ray Absorption (XMCD)

Ferromagnetic cobalt with magnetization along incident light direction

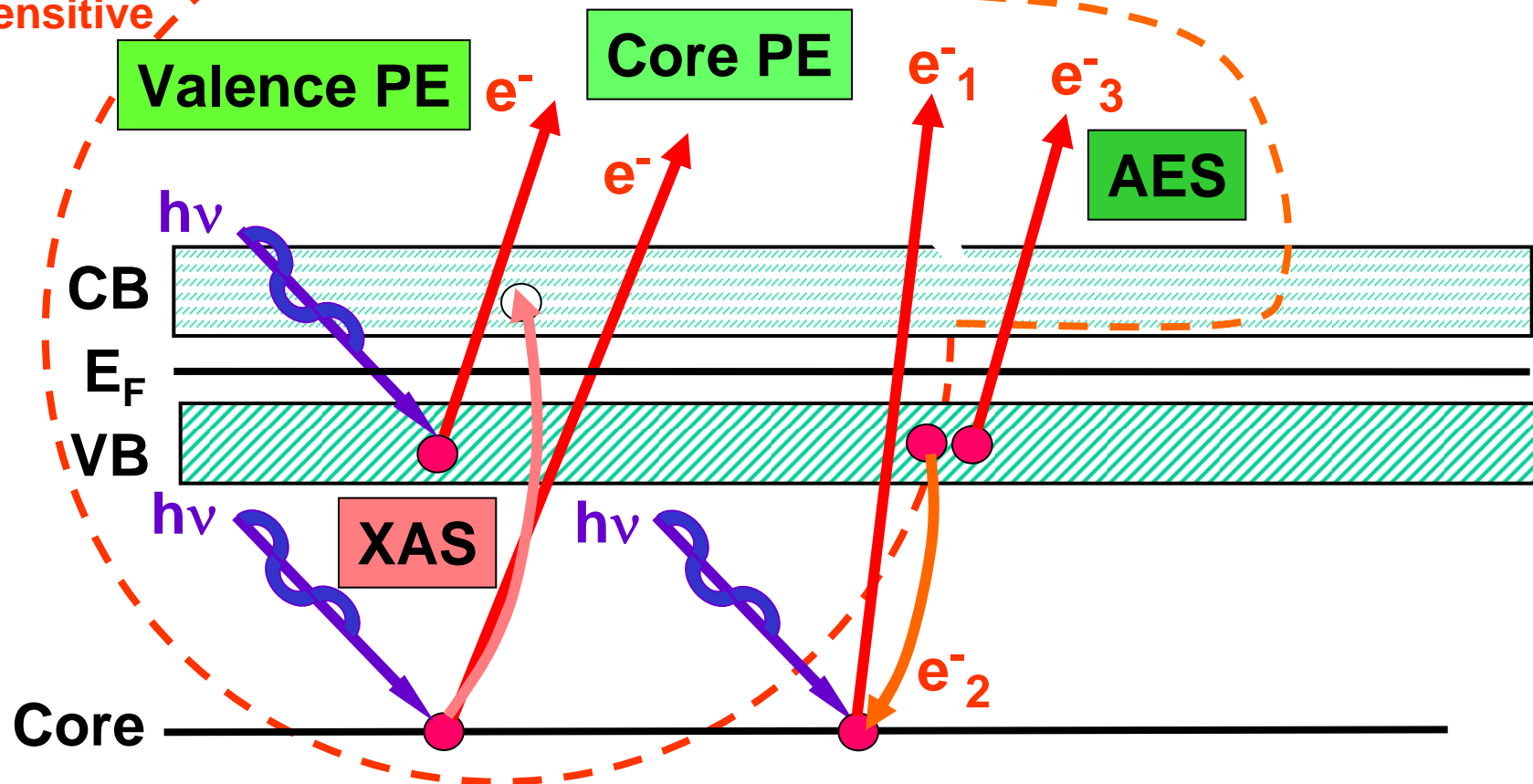


Variation of Near-Edge X-Ray Absorption Fine Structure (NEXAFS) for Different Polymers



Electron-out:
surface
sensitive

The Soft X-Ray Spectroscopies



PE = photoemission = photoelectron spectroscopy

XAS = x-ray absorption spectroscopy

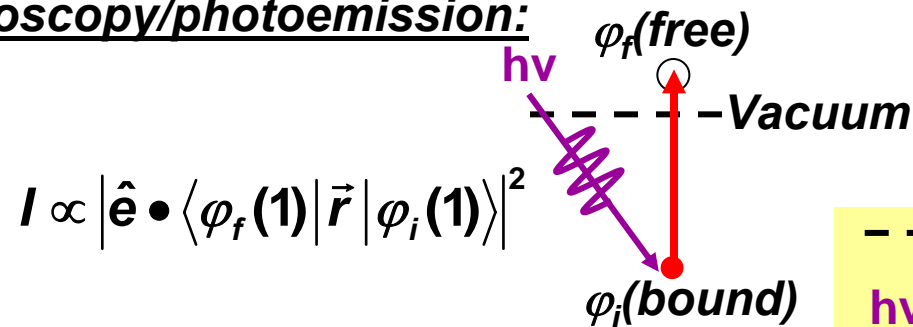
AES = Auger electron spectroscopy

XES = x-ray emission spectroscopy

REXS/RIXS = resonant elastic/inelastic x-ray scattering

MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: DIPOLE LIMIT

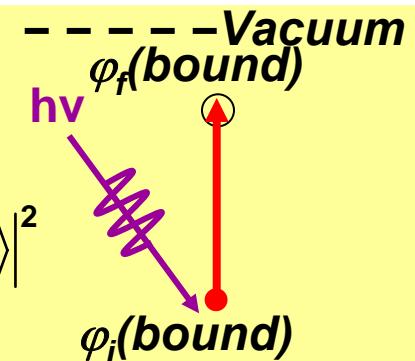
- Photoelectron spectroscopy/photoemission:



$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$

- Near-edge x-ray absorption:

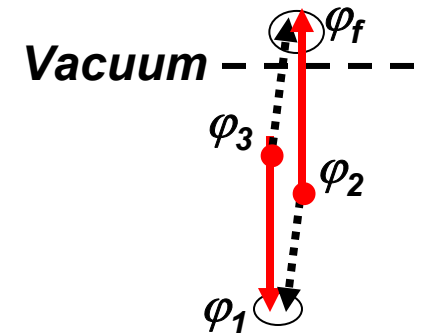
$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$



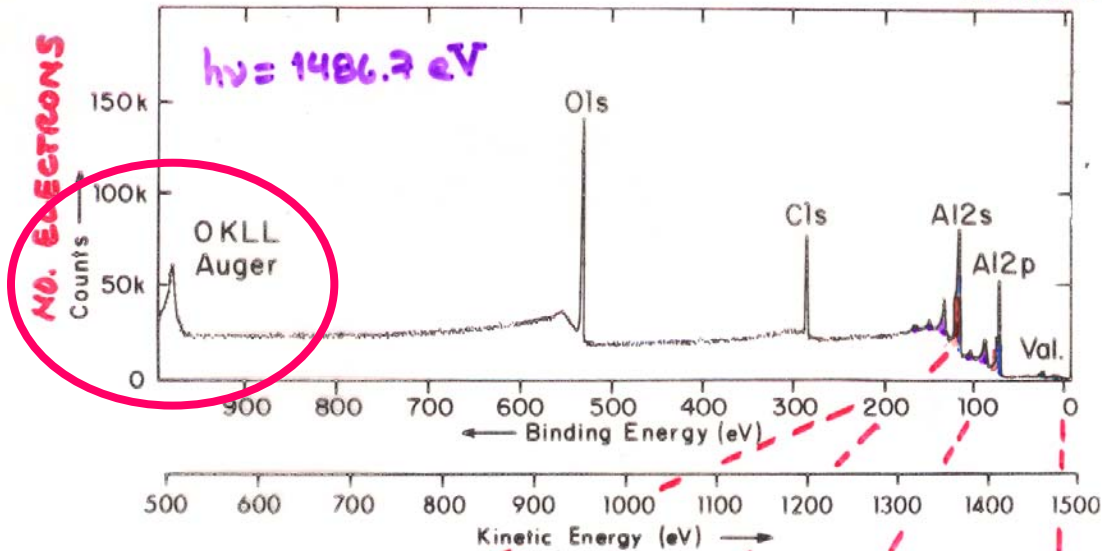
- Auger electron emission:

$$I \propto \left| \langle \varphi_f(\mathbf{1})\varphi_1(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_3(\mathbf{1})\varphi_2(\mathbf{2}) \rangle - \langle \varphi_1(\mathbf{1})\varphi_f(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_3(\mathbf{1})\varphi_2(\mathbf{2}) \rangle \right|^2$$

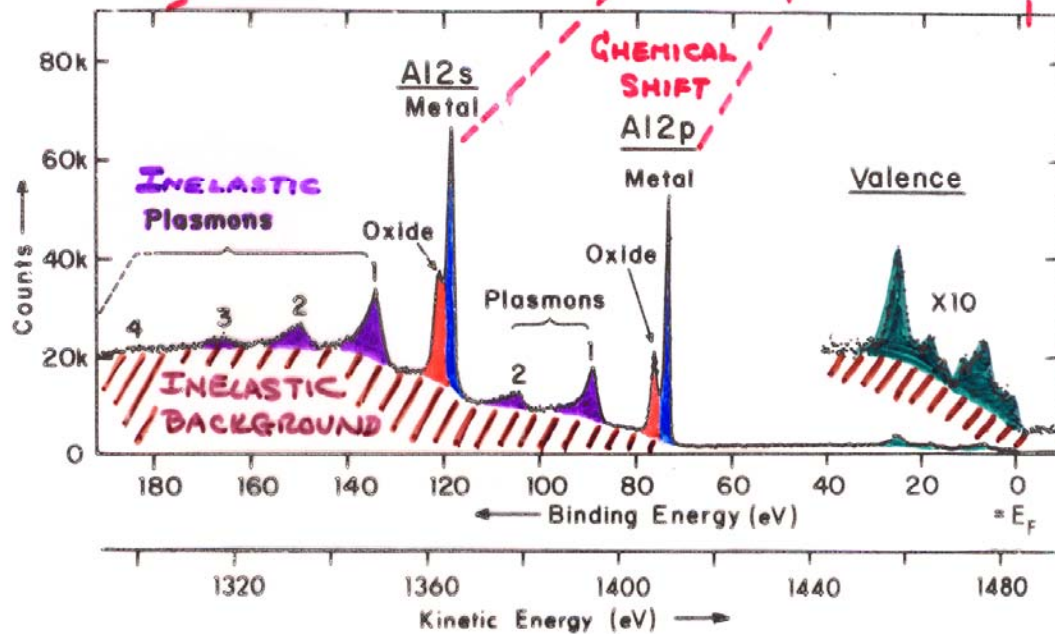
Direct
Exchange



TYPICAL PHOTOELECTRON SPECTRA: OXIDIZED ALUMINUM



Auger kinetic energies do not change with photon energy
 Photoelectron kinetic energies shift linearly with photon energy



“Basic Concepts of XPS”
 Figure 1

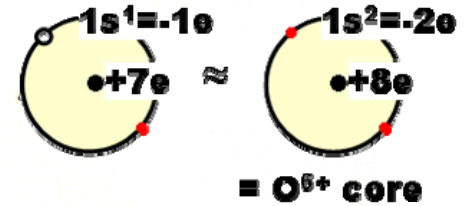
THE AUGER PROCESS

TWO-STEP PROCESS.
TWO-HOLE FINAL STATE.
NO STRONG SELEC. RULES.
COMPLEX SPECTRA.

$$N \text{ core} = N 1s^2 = N^{6+}$$



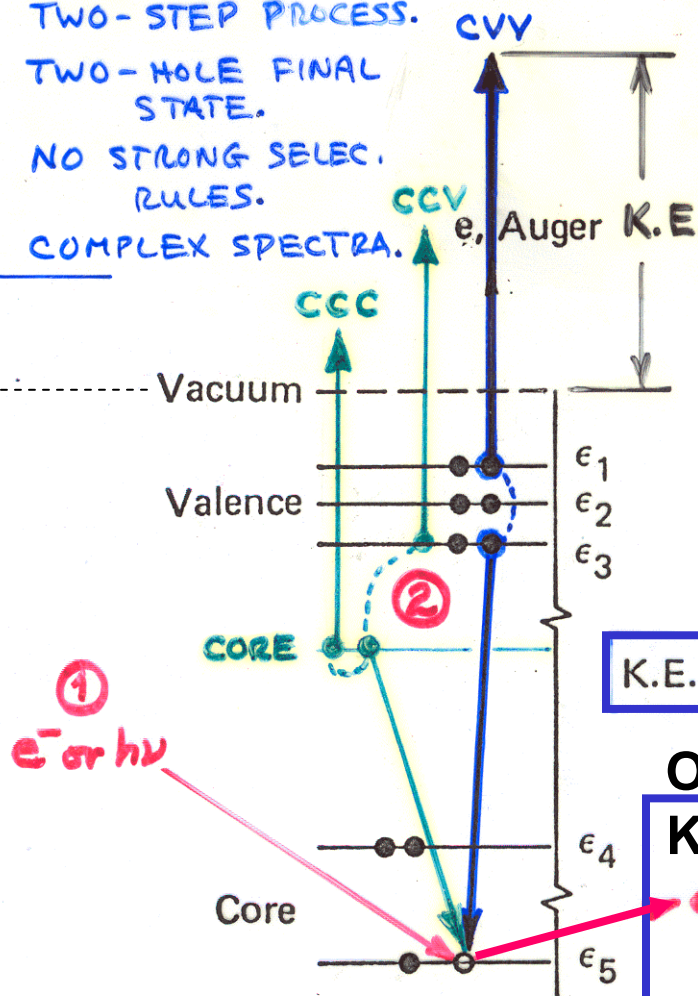
Assume:
 N^{6+} core with
 $1s$ hole = N^{6+}



The equivalent core or $Z+1$ approximation

ϵ positive

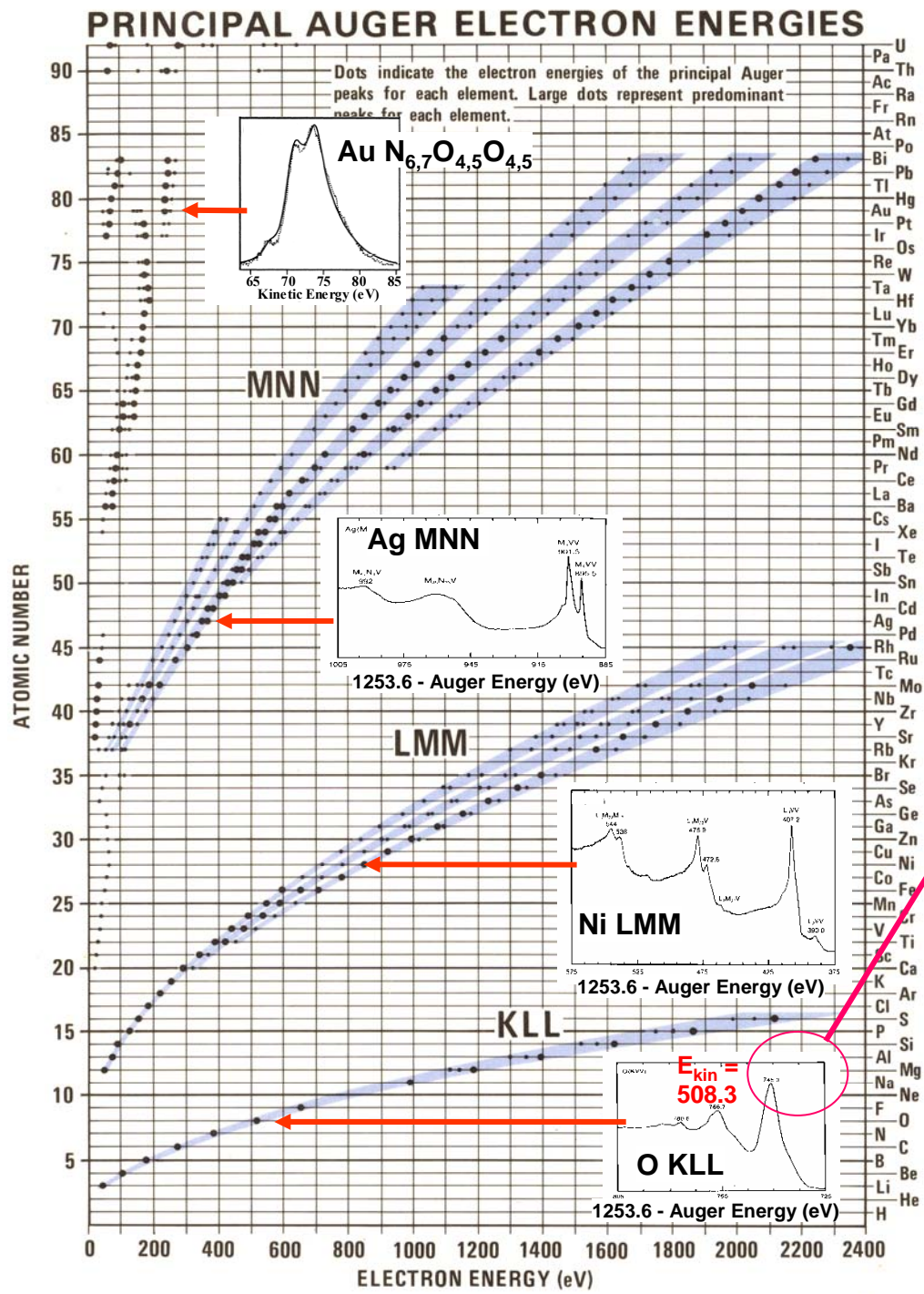
ϵ negative



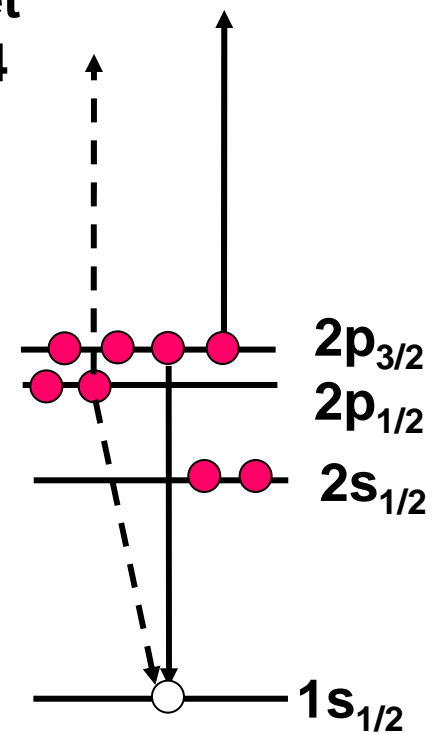
$K.E. \approx -\epsilon_5 + \epsilon_3 + \epsilon_1$ DOES NOT DEPEND ON $h\nu$!

Or more accurately:
 $K.E. \approx B.E._5^Z - B.E._3^{Z+1} - B.E._1^Z$
 $e^- \approx B.E._5^Z - B.E._3^Z - B.E._1^{Z+1}$
 \approx (average of two above)

Figure 2. Scheme of the Auger process. A valence-level involved Auger emission is illustrated here, but the two electrons involved also could have come from core level, ϵ_4 , provided $\epsilon_5 - 2\epsilon_4 > 0$.



X-Ray Data Booklet Fig. 1.4



$$\begin{aligned}
 \text{K.E.} &\approx \text{B.E.}_{1s}^{Z=8} - \text{B.E.}_{2p}^9 - \text{B.E.}_{2p}^8 \\
 &\approx \text{B.E.}_{1s}^8 + \text{B.E.}_{2p}^8 - \text{B.E.}_{2p}^9 \\
 &\approx 543.1 - 17 - 13 \approx \mathbf{513 \text{ eV}}
 \end{aligned}$$

X-Ray Data Booklet--Section 1.1 ELECTRON BINDING ENERGIES

The energies are given in eV relative to the vacuum level for the rare gases and for H₂, N₂, O₂, F₂, and Cl₂; relative to the Fermi level for the metals; and relative to the top of the valence bands for semiconductors (and insulators).

Electronic configuration	Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}
1s	1 H	13.6						
1s ²	2 He	24.6*						
1s ² 2s	3 Li	54.7*						
1s ² 2s ²	4 Be	111.5*						
1s ² 2s ² 2p	5 B	188*						
1s ² 2s ² 2p ²	6 C	284.2*						
1s ² 2s ² 2p ³	7 N	409.9*	37.3*	~ 9	~ 9			
1s ² 2s ² 2p ⁴	8 O	543.1*	41.6*	~ 13	~ 13			
1s ² 2s ² 2p ⁵	9 F	696.7*	~ 45	~ 17	~ 17			
1s ² 2s ² 2p ⁶	10 Ne	870.2*	48.5*	21.7*	21.6*			
[Ne] 3s	11 Na	1070.8†	63.5†	30.65	30.81			
[Ne] 3s ²	12 Mg	1303.0†	88.7	49.78	49.50			
[Ne] 3s ² 3p	13 Al	1559.6	117.8	72.95	72.55			
[Ne] 3s ² 3p ²	14 Si	1839	149.7*b	99.82	99.42			
[Ne] 3s ² 3p ³	15 P	2145.5	189*	136*	135*			
[Ne] 3s ² 3p ⁴	16 S	2472	230.9	163.6*	162.5*			
[Ne] 3s ² 3p ⁵	17 Cl	2822.4	270*	202*	200*			
[Ne] 3s ² 3p ⁶	18 Ar	3205.9*	326.3*	250.6†	248.4*	29.3*	15.9*	15.7*
[Ar] 4s	19 K	3608.4*	378.6*	297.3*	294.6*	34.8*	18.3*	18.3*
[Ar] 4s ²	20 Ca	4038.5*	438.4†	349.7†	346.2†	44.3 †	25.4†	25.4†
	21 Sc	4492	498.0*	403.6*	398.7*	51.1*	28.3*	28.3*
	22 Ti	4966	560.9†	460.2†	453.8†	58.7†	32.6†	32.6†

Valence levels

~ 9 ~ 9
~ 13 ~ 13

~ 45 ~ 17 ~ 17

Interpolated, extrapolated

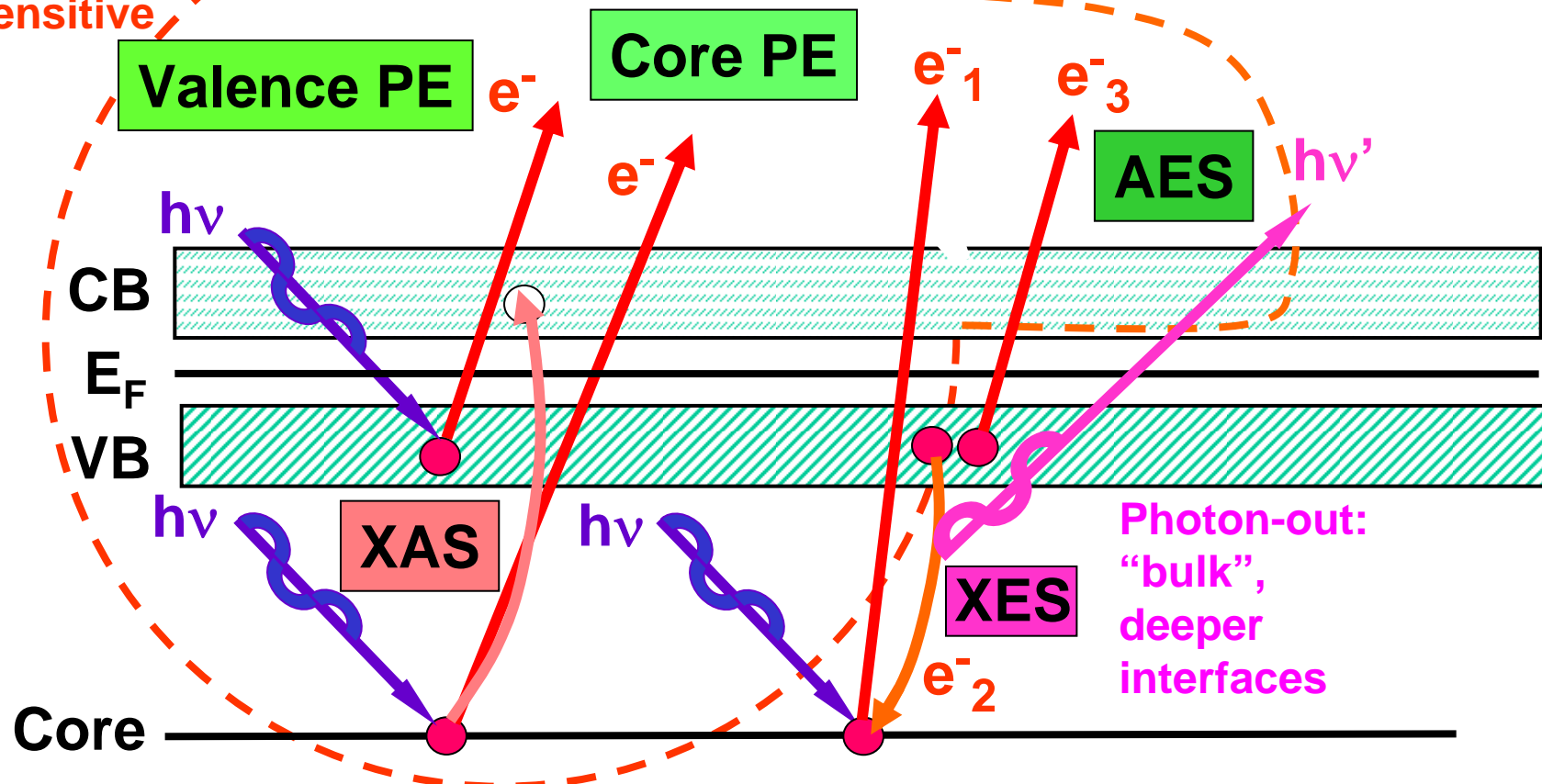
Valence levels

Valence levels

Missing valence B.E.s

Electron-out:
surface
sensitive

The Soft X-Ray Spectroscopies



PE = photoemission = photoelectron spectroscopy

XAS = x-ray absorption spectroscopy

AES = Auger electron spectroscopy

XES = x-ray emission spectroscopy

REXS/RIXS = resonant elastic/inelastic x-ray scattering

THE AUGER PROCESS

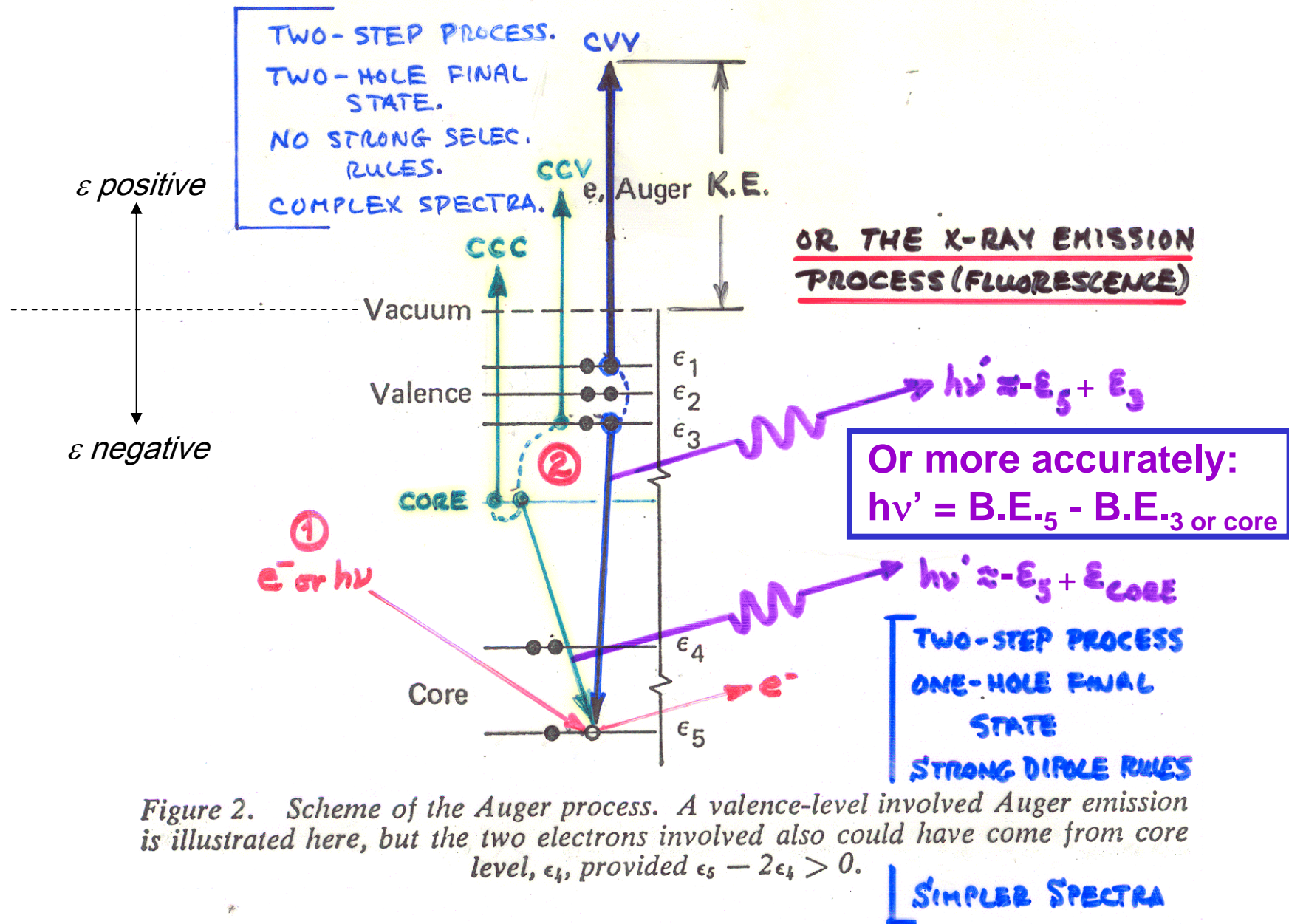


Figure 2. Scheme of the Auger process. A valence-level involved Auger emission is illustrated here, but the two electrons involved also could have come from core level, ϵ_4 , provided $\epsilon_5 - 2\epsilon_4 > 0$.

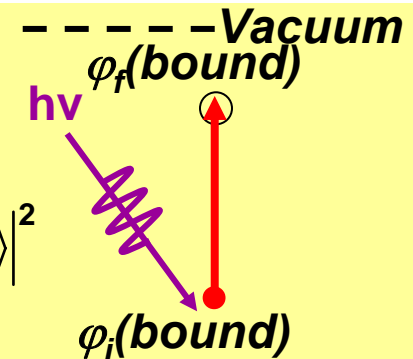
MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: DIPOLE LIMIT

- Photoelectron spectroscopy/photoemission:

$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$

- Near-edge x-ray absorption:

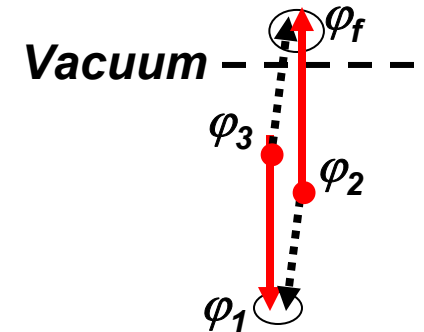
$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$



- Auger electron emission:

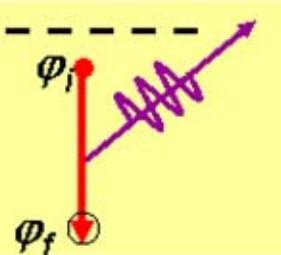
$$I \propto \left| \langle \varphi_f(\mathbf{1})\varphi_1(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_3(\mathbf{1})\varphi_2(\mathbf{2}) \rangle - \langle \varphi_1(\mathbf{1})\varphi_f(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_3(\mathbf{1})\varphi_2(\mathbf{2}) \rangle \right|^2$$

Direct Exchange



- X-ray emission:

$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$



1.3 FLUORESCENCE YIELDS FOR K AND L SHELLS

Jeffrey B. Kortright

Fluorescence yields for the *K* and *L* shells for the elements $5 \leq Z \leq 110$ are plotted in Fig. 1-2; the data are based on Ref. 1. These yields represent the probability of a core hole in the *K* or *L* shells being filled by a radiative process, in competition with nonradiative processes. Auger processes are the only nonradiative processes competing with fluorescence for the *K* shell and

If fluorescence yield \equiv FY

FY = probability of radiative decay \rightarrow x-ray emission)

$1 - \text{FY} =$ probability of non-radiative decay \rightarrow Auger electron emission

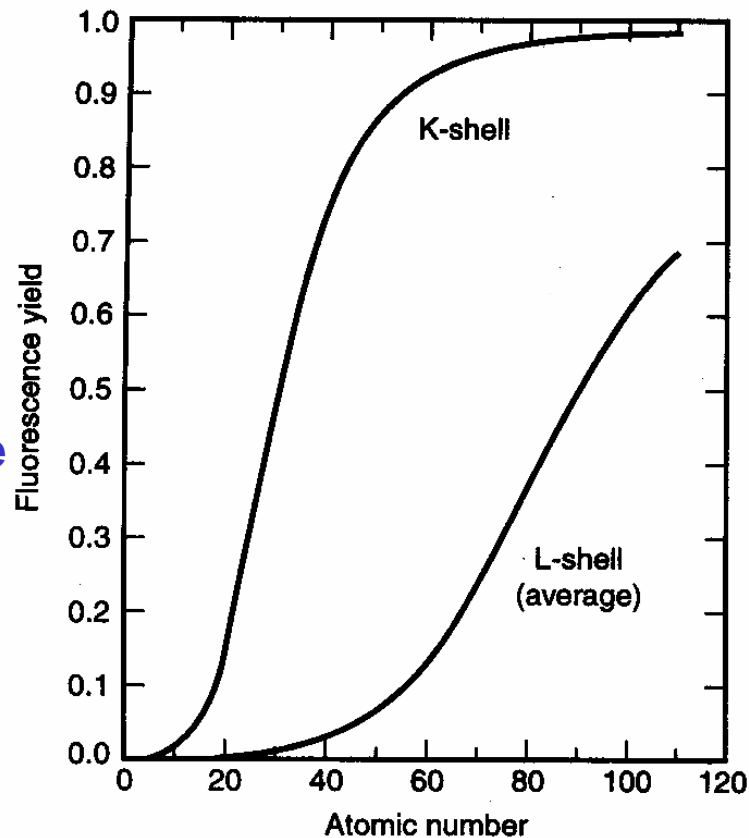
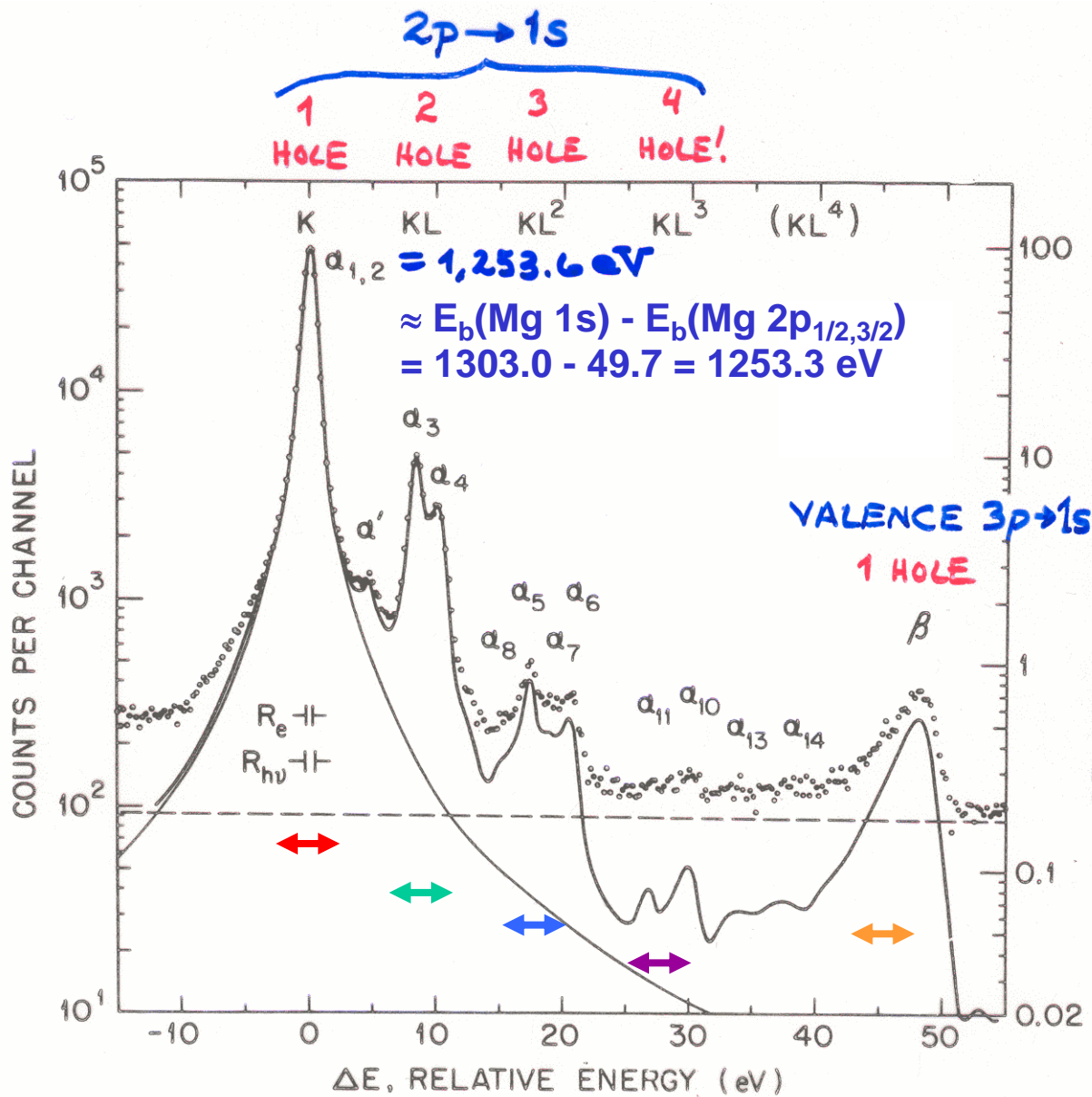
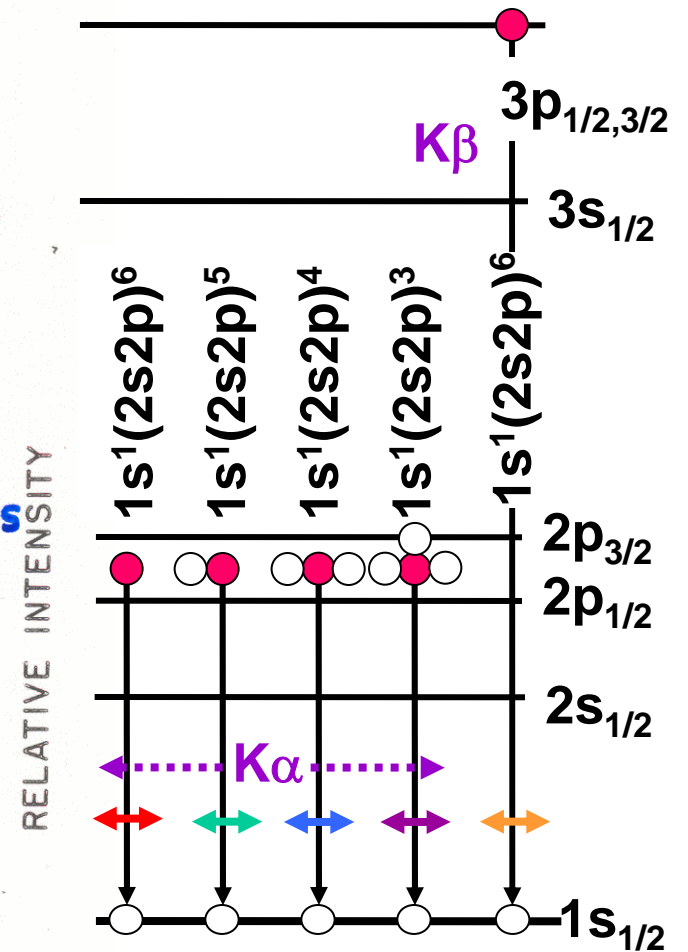


Fig. 1-2. Fluorescence yields for K and L shells for elements 5 to 110. The plotted curve for the L shell represents the average of L_1 , L_2 , and L_3 effective yields.

“X-Ray Data Booklet”
Section 1.3



A STANDARD LABORATORY X-RAY SOURCE



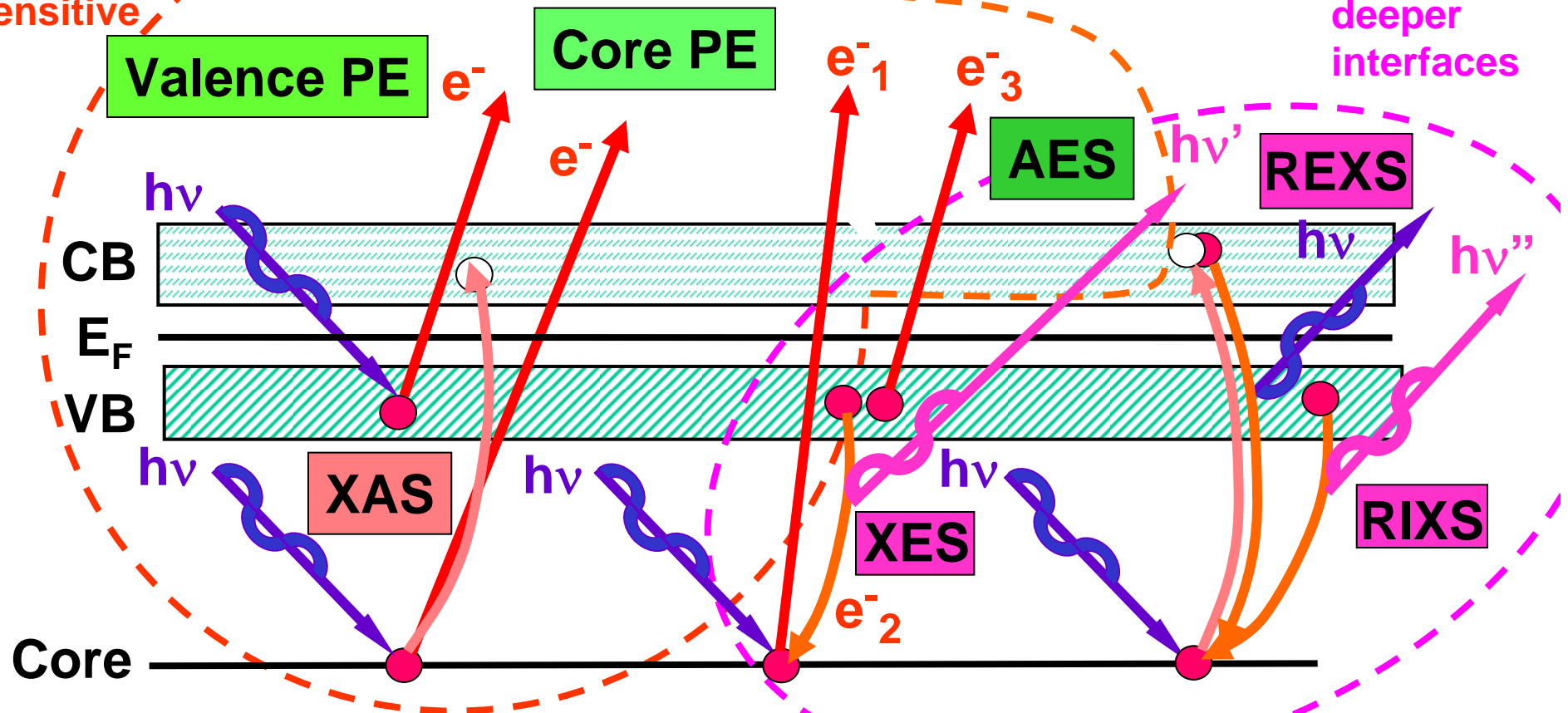
Mg K series of x-rays:
 atomic no. = 12
 Fluorescence Yield ≈ 0.03

“Basic Concepts of XPS”
 Figure 2

The Soft X-Ray Spectroscopies

Electron-out:
surface
sensitive

Photon-out:
"bulk",
deeper
interfaces



PE = photoemission = photoelectron spectroscopy

XAS = x-ray absorption spectroscopy

AES = Auger electron spectroscopy

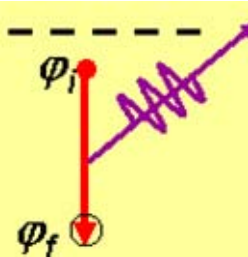
XES = x-ray emission spectroscopy

REXS/RIXS = resonant elastic/inelastic x-ray scattering

MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: RESONANT EFFECTS

- X-ray emission:

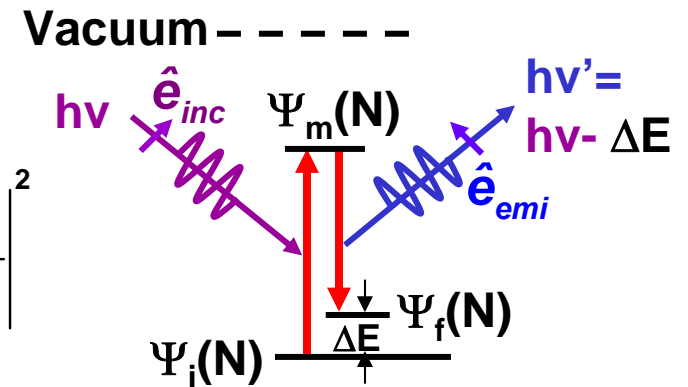
$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$



- Resonant inelastic x-ray scattering:

$$I \propto \sum_f \left| \sum_m \frac{\langle \Psi_f(N) | \hat{\mathbf{e}}_{emi} \cdot \vec{r} | \Psi_m(N) \rangle \langle \Psi_m(N) | \hat{\mathbf{e}}_{inc} \cdot \vec{r} | \Psi_i(N) \rangle}{h\nu + E_i(N) - E_m(N) - i\Gamma_m} \right|^2$$

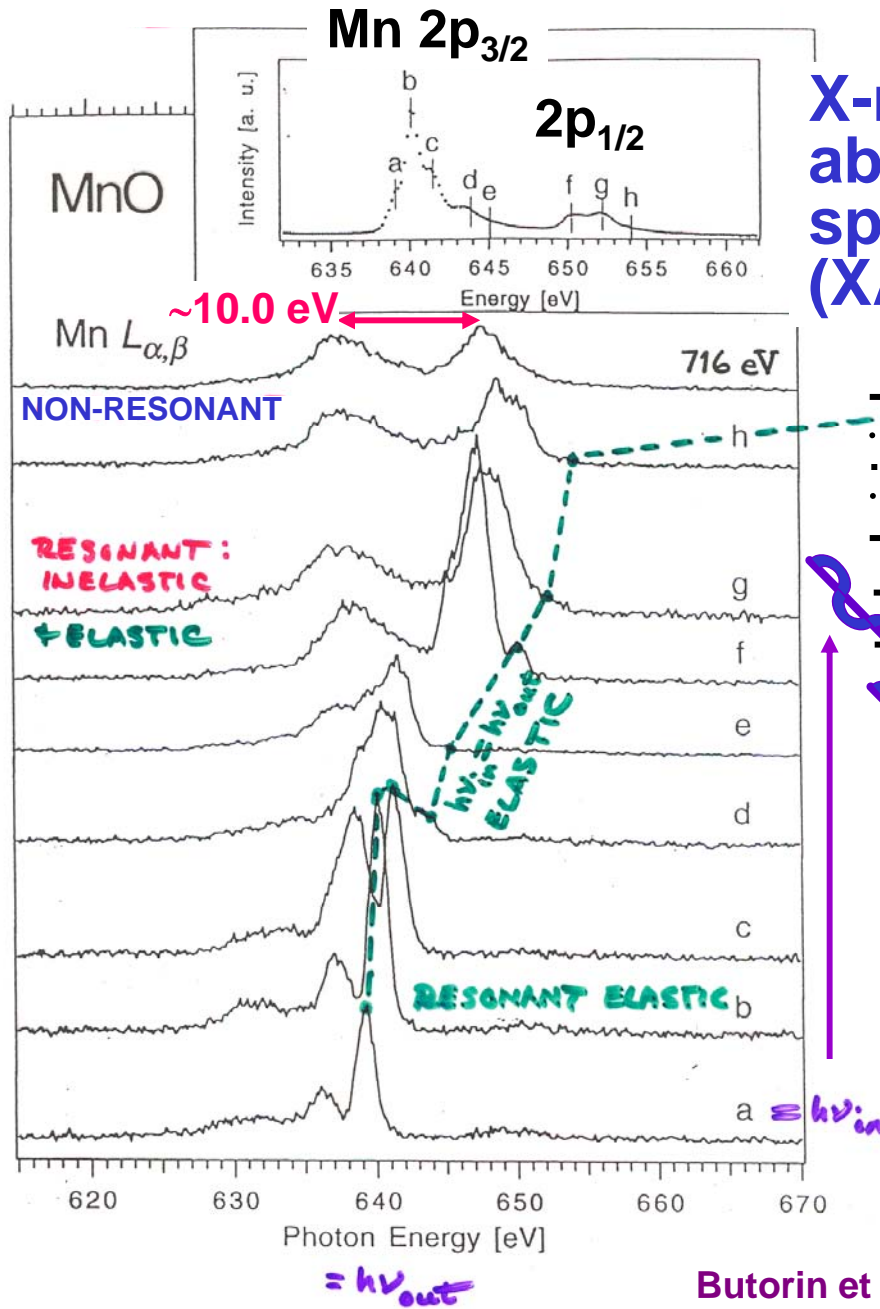
$$\times \delta(h\nu - (E_m(N) - E_i(N)))$$



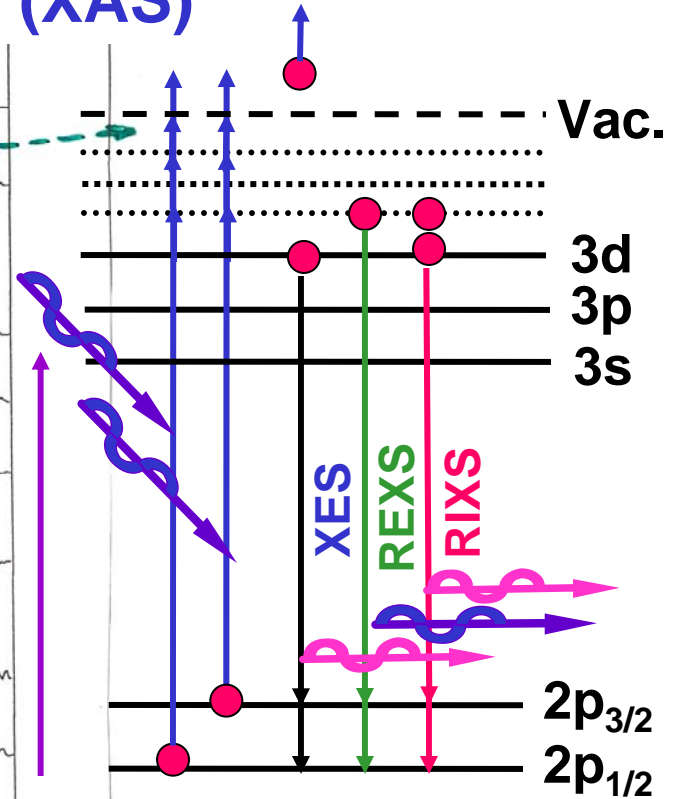
$$N_m(t) = N_m(0) e^{-\frac{2\Gamma_m t}{\hbar}} = N_m(0) e^{-\frac{t}{T_{lifetime}}}$$

X-ray
fluorescence
spectroscopy
=X-ray
emission
spectroscopy
(XES)

Resonant
inelastic
x-ray
scattering
(RIXS)
and
Resonant
elastic
x-ray
scattering
(REXS)



X-ray
absorption
spectroscopy
(XAS)

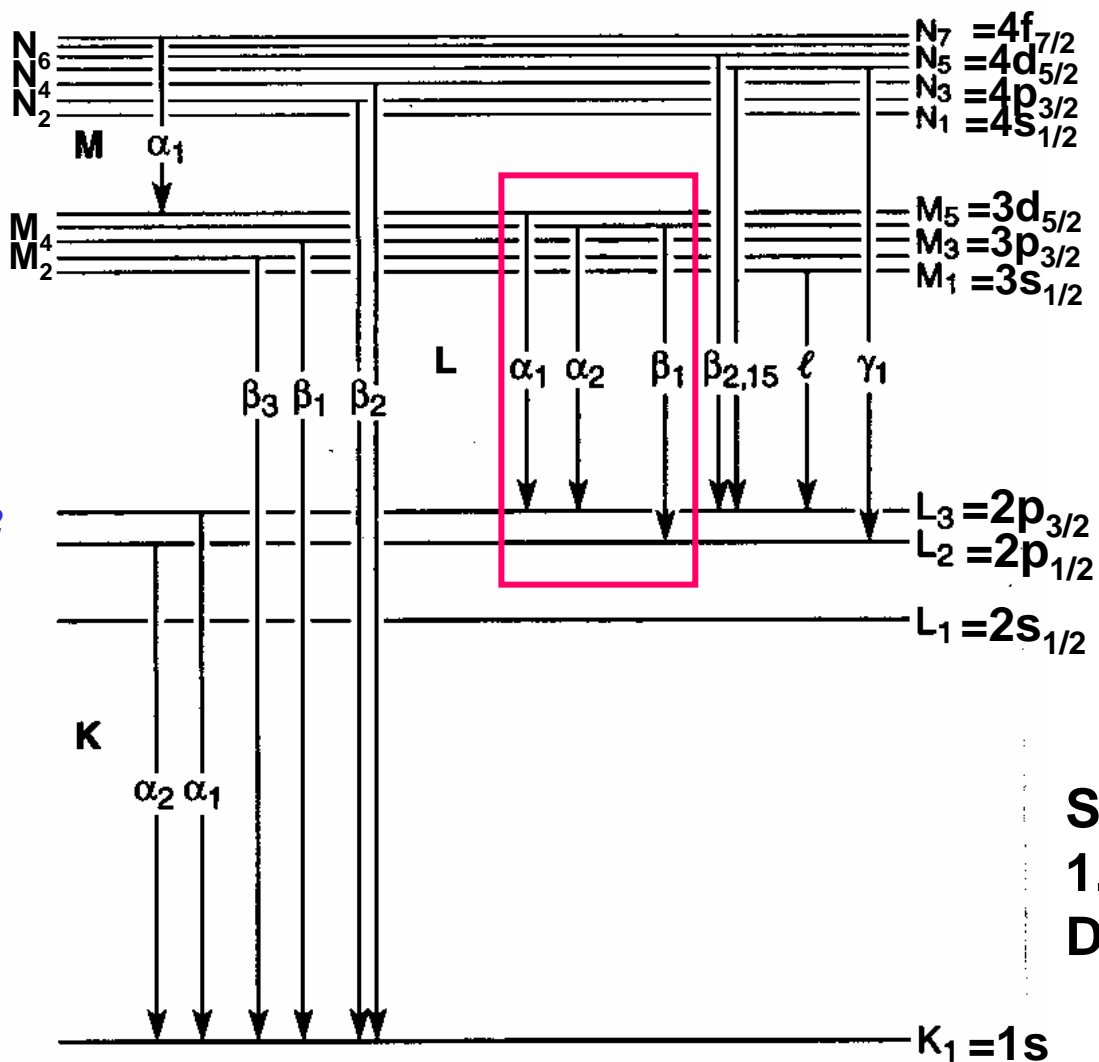


Butorin et al., Phys. Rev.
B 54, 4405 ('96)

**X-Ray
Nomenclature
(from "X-Ray
Data Booklet")**

In general:

$$nl \rightarrow \begin{cases} \text{Spin-} & nl_{j=l+1/2} \\ \text{orbit} & nl_{j=l-1/2} \end{cases}$$



$\Delta j = 0, \pm 1$

**See Section
1.2 in "X-Ray
Data Booklet"**

Fig. 1-1. Transitions that give rise to the emission lines in Table 1-3.

Electron binding energies

Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}	M ₄ 3d _{3/2}	M ₅ 3d _{5/2}
23 V	5465	626.7†	519.8†	512.1†	66.3†	37.2†	37.2†		
24 Cr	5989	696.0†	583.8†	574.1†	74.1†	42.2†	42.2†		
25 Mn	6539	769.1†	649.9†	638.7†	82.3†	47.2†	47.2†		
26 Fe	7112	844.6†	719.9†	706.8†	91.3†	52.7†	52.7†		
27 Co	7709	925.1†	793.2†	778.1†	101.0†	58.9†	59.9†		
28 Ni	8333	1008.6†	870.0†	852.7†	110.8†	68.0†	66.2†		
29 Cu	8979	1096.7†	952.3†	932.7	122.5†	77.3†	75.1†		
30 Zn	9659	1196.2*	1044.9*	1021.8*	139.8*	91.4*	88.6*	10.2*	10.1*

Diff. = 11.2

Table 1-2. Energies of x-ray emission lines (continued).

Element	Kα ₁	Kα ₂	Kβ ₁	Lα ₁	Lα ₂	Lβ ₁	Lβ ₂	Lγ ₁	Mα ₁
22 Ti	4,510.84	4,504.86	4,931.81	452.2	452.2	458.4			
23 V	4,952.20	4,944.64	5,427.29	511.3	511.3	519.2			
24 Cr	5,414.72	5,405.509	5,946.71	572.8	572.8	582.8			
25 Mn	5,898.75	5,887.65	6,490.45	637.4	637.4	648.8			
26 Fe	6,403.84	6,390.84	7,057.98	705.0	705.0	718.5			
27 Co	6,930.32	6,915.30	7,649.43	776.2	776.2	791.4			
28 Ni	7,478.15	7,460.89	8,264.66	851.5	851.5	868.8			
29 Cu	8,047.78	8,027.83	8,905.29	929.7	929.7	949.8			
30 Zn	8,638.86	8,615.78	9,572.0	1,011.7	1,011.7	1,034.7			

Diff. = 11.4

The five ways in which x-rays interact with Matter:

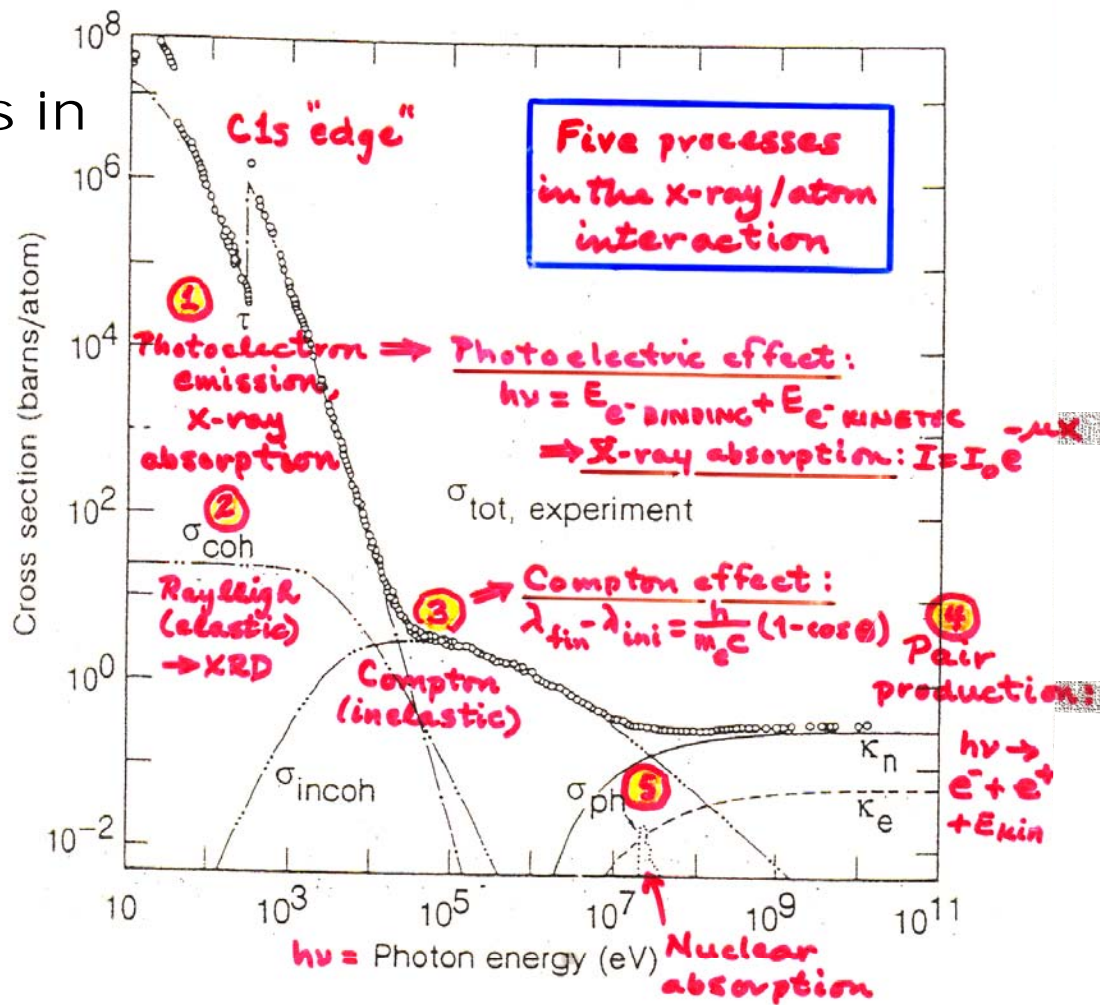


Fig. 3-1. Total photon cross section σ_{tot} in carbon, as a function of energy, showing the contributions of different processes: τ , atomic photo-effect (electron ejection, photon absorption); σ_{coh} , coherent scattering (Rayleigh scattering—atom neither ionized nor excited); σ_{incoh} , incoherent scattering (Compton scattering off an electron) κ_n , pair production, nuclear field; κ_e , pair production, electron field; σ_{ph} , photonuclear absorption (nuclear absorption usually followed by emission of a neutron or other particle). (From Ref. 3; figure courtesy of J. H. Hubbell.)

“X-Ray Data Booklet”
Section 3.1