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**Data Analyses  
(Evaluation of  $^{56}\text{Co}$  Decay Data)**

Desmond MacMahon  
*National Physical Laboratory  
London  
U.K.*



# Evaluation of $^{56}\text{Co}$ Decay Data

*Desmond MacMahon*

*Coral Baglin*

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# $^{56}\text{Co}$ Decay Data

- ◆  $^{56}\text{Co}$  decays by positron emission (19.58%) and by electron capture (80.42%) to excited states of  $^{56}\text{Fe}$ .
- ◆ 46 gamma rays with energies up to 3.6 MeV de-exciting 15 excited states in  $^{56}\text{Fe}$  have been reported.
- ◆ This energy range makes  $^{56}\text{Co}$  useful as a calibration source in gamma ray spectrometry.

# $^{56}\text{Co}$ Decay Data

- ♦ The Q value for the decay is given by Audi *et al.* as **4566 (20) keV**.
- ♦ The half-life of  $^{56}\text{Co}$  has been evaluated by Woods *et al.* as **77.236 (26) days**.
- ♦ The main gamma ray energies are taken from the Helmer & van der Leun evaluation (2000).

# $^{56}\text{Co}$ Gamma Ray Emission Probabilities

- ◆ Relative gamma ray emission probabilities for the 46 gamma rays reported by 31 authors between 1965 and 2002 were tabulated.
- ◆ A problem arose when considering the high energy data.
- ◆ In many cases detector efficiency curves used measured data up to about 2.5 MeV and were then extrapolated to 3.6 MeV.

# $^{56}\text{Co}$ Gamma Ray Emission Probabilities

- ◆ It was clear from experimentally determined efficiency curves above 3 MeV that the extrapolated curves introduced errors of up to 6%.
- ◆ Therefore, of the 31 papers cited, only 8 which had used experimentally determined efficiency curves up to 3.6 MeV were included in the evaluation of data above 3 MeV.



# $^{56}\text{Co}$ Gamma Ray Emission Probabilities



- ◆ The second problem was the significant number of discrepant data.
- ◆ Of the 46 gamma rays considered, 18 had data sets with a reduced chi-squared ranging from 2.0 to 7.8, indicating significant discrepancies.



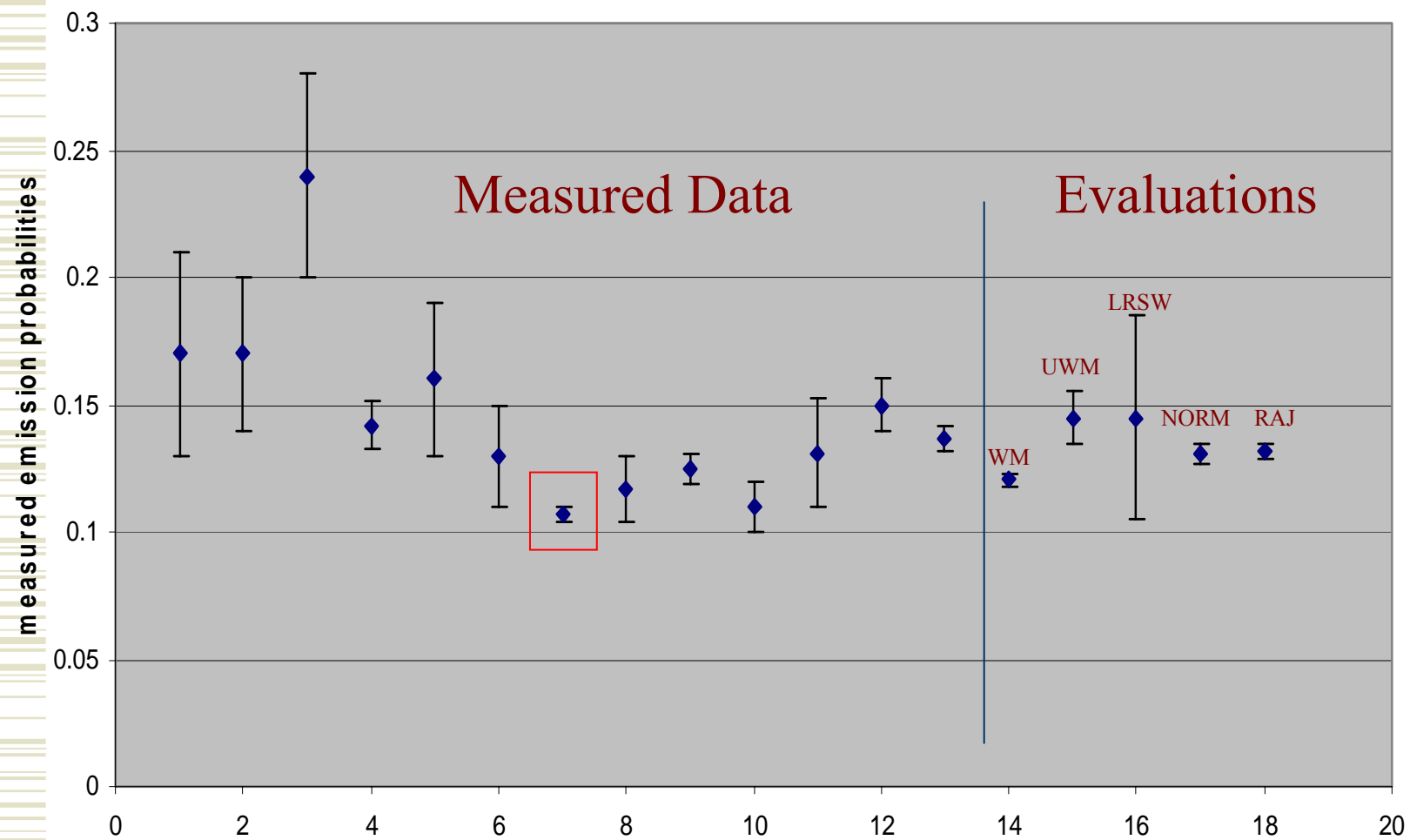
# $^{56}\text{Co}$ Gamma Ray Emission Probabilities



- ◆ The following graph shows the data for the 1140.5 keV gamma ray, for which the reduced chi-squared is 5.2.
- ◆ The discrepancies are clear from the graph.



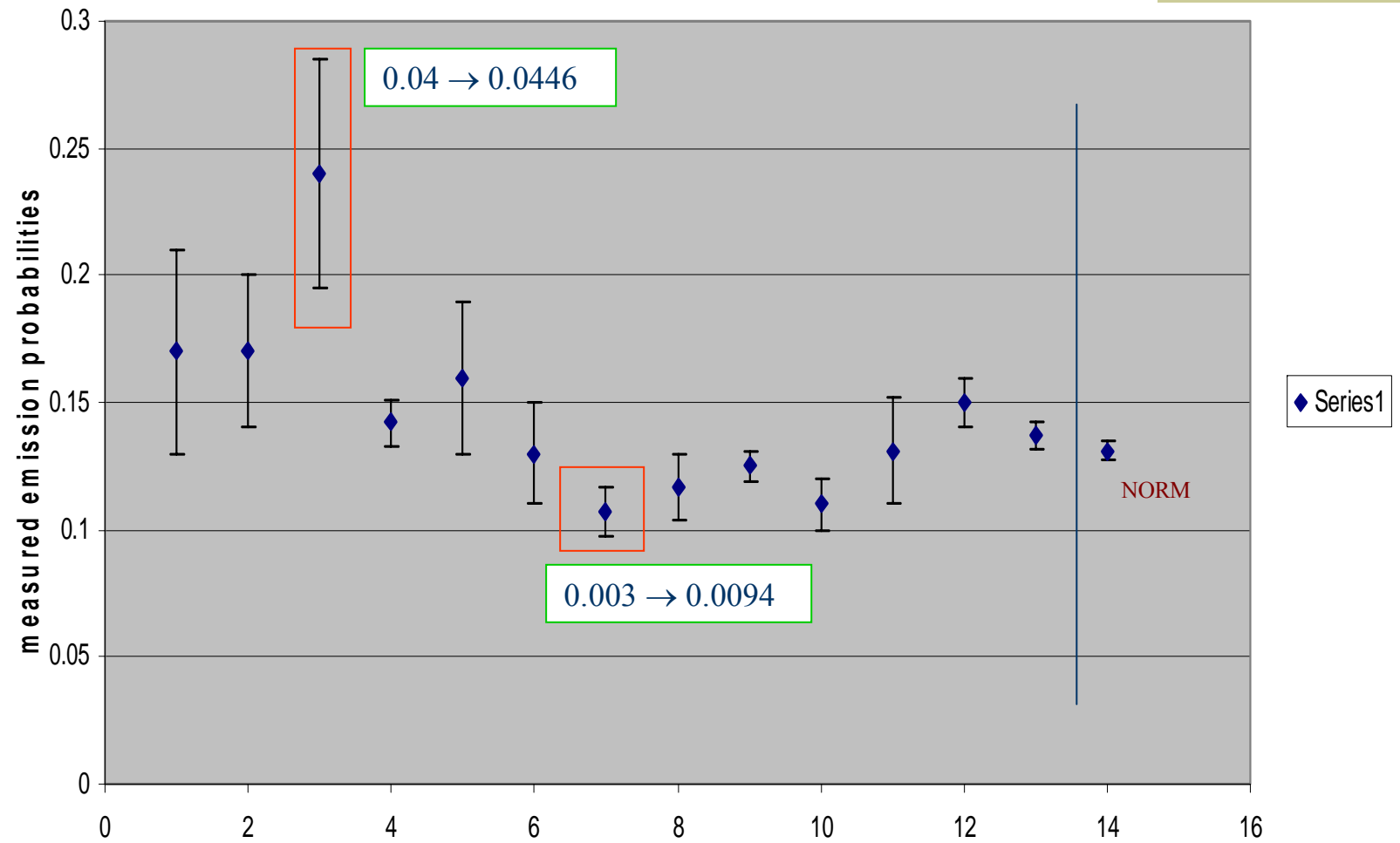
1140.5 keV gamma ray



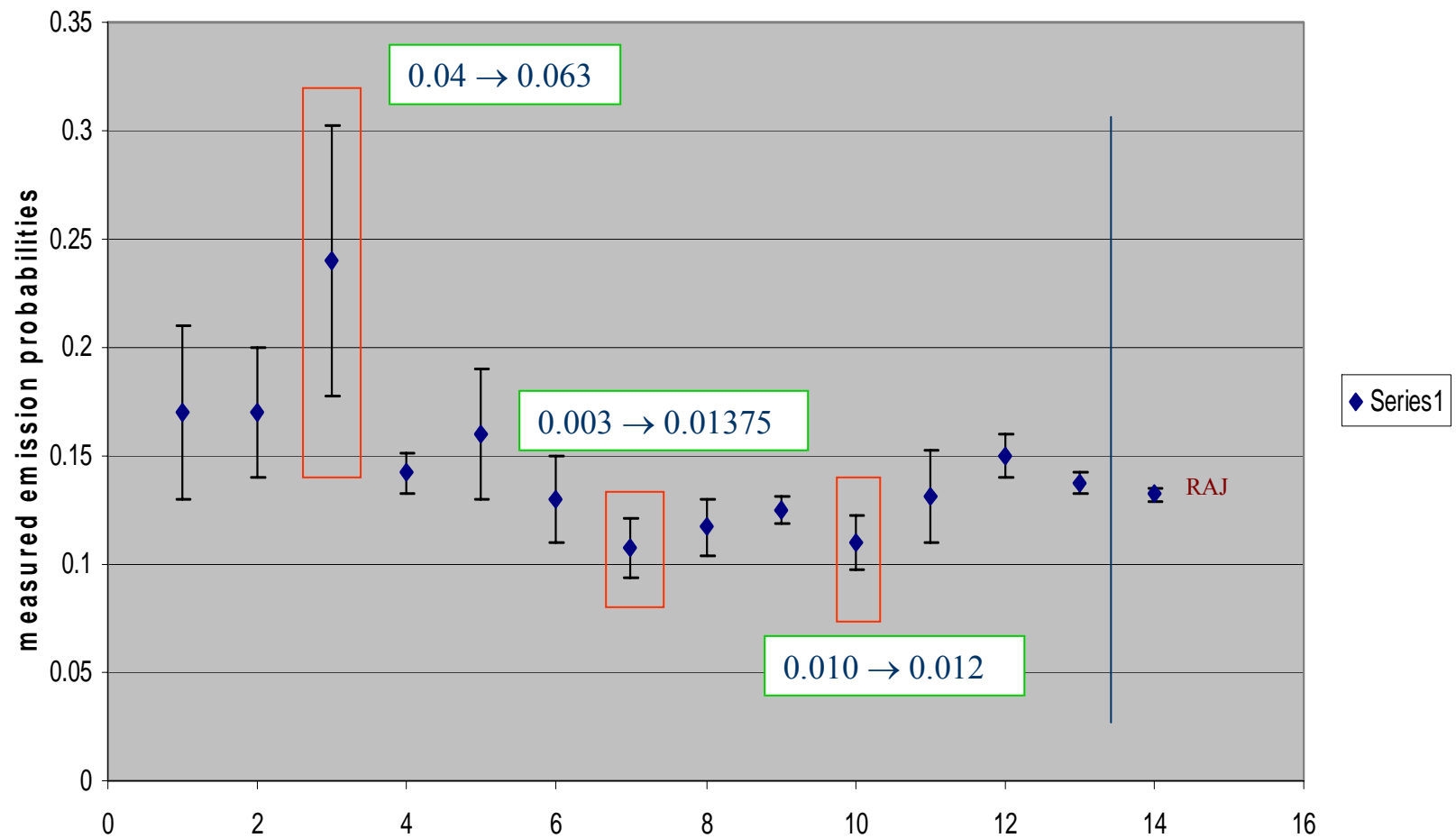
# $^{56}\text{Co}$ Gamma Ray Emission Probabilities

- ◆ On the previous graph points 1 to 13 are the experimental data.
- ◆ Point 14 is the weighted mean 0.1204(21)
- ◆ Point 15 is the unweighted mean 0.145(10)
- ◆ Point 16 is the LRSW 0.145 (38)
- ◆ Point 17 is the norm. resid. 0.131(4)
- ◆ Point 18 is the Rajeval value 0.132(4)

1140.5 keV gamma ray  
Normalised Residuals adjustment (point 14)



1140.5 keV gamma ray  
Rajeval adjustment (point 14)





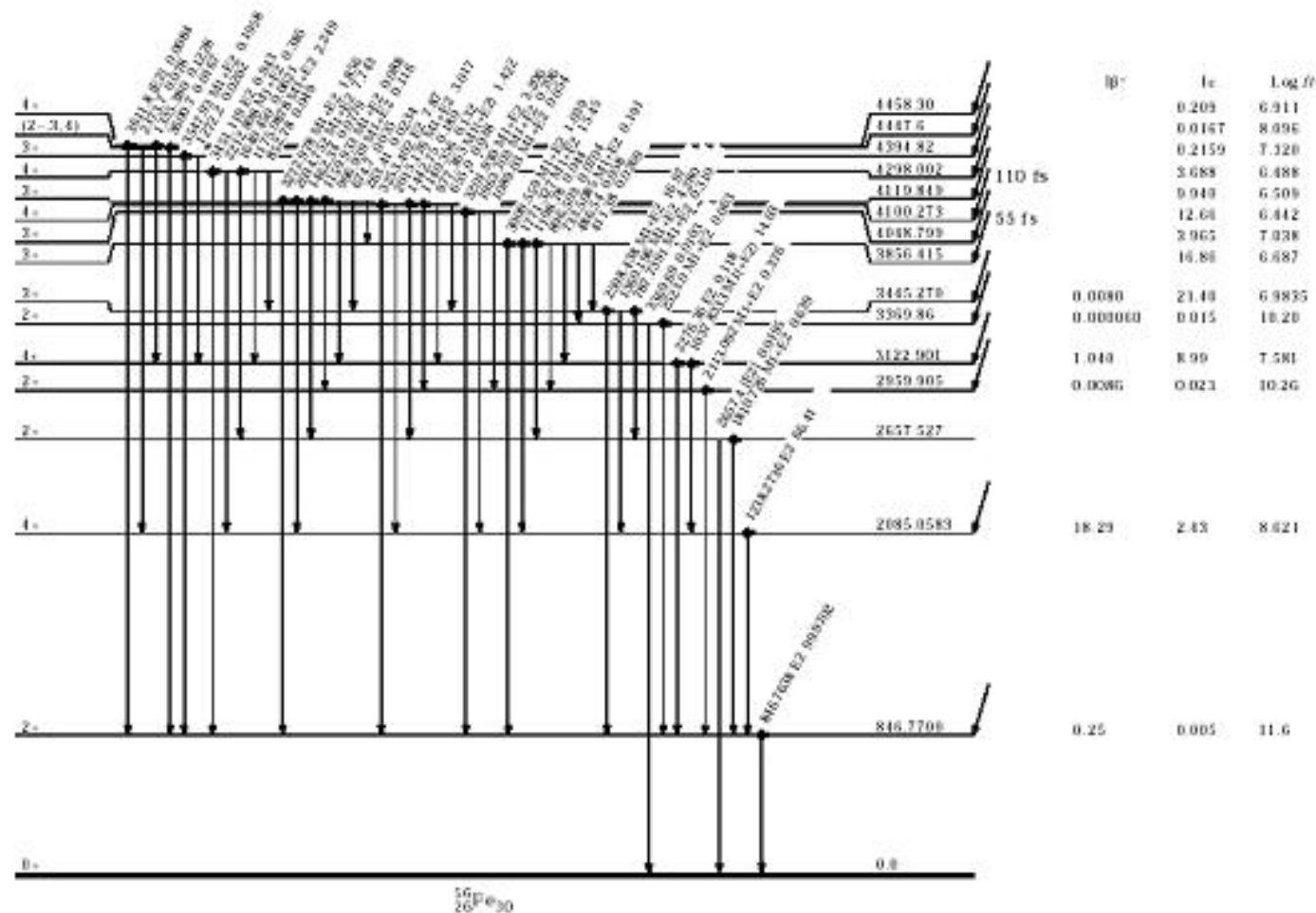
# Normalisation



- ◆ Evaluated intensities are relative to the strongest 847 keV transition to the ground state.
- ◆ Normalisation is accomplished by requiring that all transitions to the ground state add up to 100.

# Decay Scheme

Intensities: I(γ,α) per 100 parent decays



# Normalisation

- ◆ Assuming zero electron capture/positron feeding from the  $4+ {}^{56}\text{Co}$  parent to the  $0+ {}^{56}\text{Fe}$  ground state:

$$\Sigma(I(\gamma + ce) \text{ to the ground state}) = 100$$

# Normalisation

$$\begin{aligned} N &= \frac{100}{[I(847\gamma)(1 + \alpha(847\gamma)) + I(2657\gamma) + I(3370\gamma)]} \\ &= \frac{100}{100.0303(9) + 0.0195(20) + 0.0103(8)} \\ &= 0.999399(23) \end{aligned}$$



# Evaluated Data

Gamma Energy keV	Relative I <sub>γ</sub>	Absolute P <sub>γ</sub>
846.772	100	0.999399(23)
1037.840	14.04(5)	0.1403(5)
1238.282	66.45(16)	0.6641(16)
1360.215	4.283(13)	0.04280(13)
1771.351	15.46(4)	0.1545(4)
2034.755	7.746(13)	0.07741(13)
2598.458	16.97(4)	0.1696(4)
3201.962	3.205(13)	0.03203(13)
3253.416	7.87(3)	0.0787(3)

# Positron Emission Probabilities

	Energy (keV)	Probability × 100	Nature	log <i>ft</i>
$\beta^+_{0,7}$	98.7 (20)	0.0080 (7)	allowed	6.984
$\beta^+_{0,6}$	174.3 (20)	6.0 E-5 (20)	2 <sup>nd</sup> forbidden	10.20
$\beta^+_{0,5}$	421.1 (20)	1.040 (20)	allowed	7.581
$\beta^+_{0,4}$	584.1 (20)	0.0086 (22)	2 <sup>nd</sup> forbidden	10.26
$\beta^+_{0,2}$	1458.9 (20)	18.29 (16)	allowed	8.621
$\beta^+_{0,1}$	2697.2 (20)	0.25 (17)	2 <sup>nd</sup> forbidden	11.6

# Electron Capture Probabilities

	Energy (keV)	Probability × 100	Nature	log <i>ft</i>
$\epsilon_{0,8}$	709.5(20)	16.86(5)	allowed	6.687(3)
$\epsilon_{0,7}$	1120.7(20)	21.40(5)	allowed	6.984(2)
$\epsilon_{0,6}$	1195.9(20)	0.015(5)	2 <sup>nd</sup> forbidden	10.20(15)
$\epsilon_{0,5}$	1443.1(20)	8.99(6)	allowed	7.581(4)
$\epsilon_{0,4}$	1606.1(20)	0.023(6)	2 <sup>nd</sup> forbidden	10.26(11)
$\epsilon_{0,2}$	2480.9(20)	2.43(3)	allowed	8.621(5)
$\epsilon_{0,1}$	3719.2(20)	0.005(3)	2 <sup>nd</sup> forbidden	11.6(3)

# Electron Capture Probabilities

	Energy (keV)	Probability × 100	Nature	log <i>ft</i>
$\epsilon_{0,15}$	107.7(20)	0.209(7)	allowed	6.911(23)
$\epsilon_{0,14}$	118.4(20)	0.0167(5)	unknown	8.096(21)
$\epsilon_{0,13}$	171.2(20)	0.2159(18)	allowed	7.320(12)
$\epsilon_{0,12}$	268.0(20)	3.688(13)	allowed	6.489(7)
$\epsilon_{0,11}$	446.1(20)	9.940(18)	allowed	6.509(4)
$\epsilon_{0,10}$	465.7(20)	12.66(4)	allowed	6.442(4)
$\epsilon_{0,9}$	517.2(20)	3.965(15)	allowed	7.038(4)

# X Ray Emissions

	Energy (keV)	Photons per 100 disintegrations
XL	0.615-0.792	0.581 (17)
XK $\alpha_2$	6.39091(5)	7.53 (10)
XK $\alpha_1$	6.40391(3)	14.75 (17)
XK $\beta_3$	} 7.05804(7)	} 3.05 (5)
XK $\beta_1$	}	}
XK $\beta''_5$	7.1083(4)	

# Auger Electron Emissions

	Energy (keV)	Electrons per 100 disintegrations
$e_{AL}$	0.510 – 0.594	111.8 (8)
$e_{AK}$		46.04 (30)
KLL	5.370-5.645	35.61 (25)
KLX	6.158-6.400	9.76 (13)
KXY	6.926-7.105	0.666 (15)