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International Centre for Theoretical Physics**



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Sixth International Conference on Perspectives in Hadronic Physics

12 - 16 May 2008

Short-Range Correlations from Hadron-Induced Reactions.

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*Kent State University
USA*

**Study of Short-Range Correlations
with 6-9 GeV/c Protons**

**Adventures Beyond
the
Shell Model**

**John Watson
Kent State University**



Study of SRCs with High-Energy Protons
Trieste, May 2008

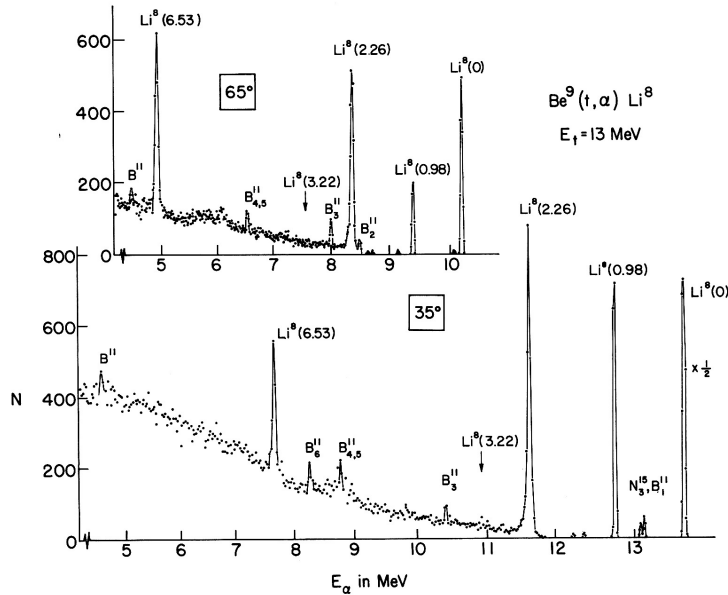


Fig. 1. Spectra of α particles from ${}^9\text{Be}(t, \alpha){}^8\text{Li}$, ${}^{12}\text{C}(t, \alpha){}^{11}\text{B}$, and ${}^{16}\text{O}(t, \alpha){}^{15}\text{N}$ at $E_t = 12.87$ MeV ($\theta = 35^\circ$ and 65°). The ordinate gives the number of α tracks recorded in a 212μ wide "bin" of the photographic plate detector. ${}^8\text{Li}(0)$, ${}^8\text{Li}(0.98)$ and ${}^8\text{Li}(2.26)$ are alpha groups corresponding to the ground and first two excited states of ${}^8\text{Li}$. ${}^8\text{Li}(6.53)$ is the new state discussed in the text. The position of α -particles from ${}^8\text{Li}(3.22)$ is indicated. The groups labelled ${}^{11}\text{B}_x$ ($x = 1$ to 6) and ${}^{15}\text{N}_3$ correspond to excited states in ${}^{11}\text{B}$ and ${}^{15}\text{N}$.

A NEW EXCITED STATE OF ${}^8\text{Li}^*$

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and

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Received 2 August 1965

${}^8\text{Li}$ can be conveniently investigated by means of three reactions: ${}^7\text{Li}(d, p){}^8\text{Li}$, ${}^6\text{Li}(t, p){}^8\text{Li}$, ${}^9\text{Be}(t, \alpha){}^8\text{Li}$ with Q -values of -0.192 , 0.803 and 0.803 MeV, respectively. The ${}^8\text{Li}(6.53)$ state

carbon and oxygen contamination, was observed at 9 angles between 12.5° and 72.5° to the incident beam. Fig. 1 shows the spectra at 35° and 65° . The new state is labeled ${}^8\text{Li}(6.53)$ in both



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Things I learned from Fay Selove

1. Nuclear Structure can be fascinating.

2. Stay from neutron detection!



$^{40}\text{Ca}(p,pn)^{39}\text{Ca}$ and $^{48}\text{Ca}(p,pn)^{47}\text{Ca}$ neutron knockout reactions at 149.5 MeV

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The reactions $^{40}\text{Ca}(p,pn)^{39}\text{Ca}$ and $^{48}\text{Ca}(p,pn)^{47}\text{Ca}$ were studied at 149.5 MeV in coplanar geometries. An overall separation energy resolution of about 1 MeV was achieved. Probable neutron-hole strength is seen for $1d_{5/2}$ and $1p$ shell knockout from both targets. The data are compared with distorted-wave-impulse-approximation calculations and spectroscopic factors are extracted for neutron-hole states.

We identified valance
neutron hole states and
extracted spectroscopic
factors

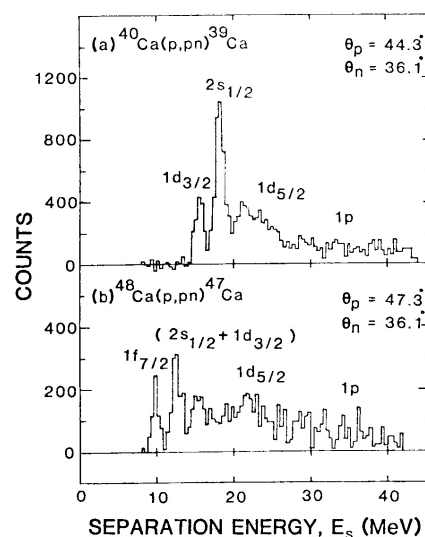


FIG. 1. Neutron separation energy spectra (a) for the $^{40}\text{Ca}(p,pn)^{39}\text{Ca}$ reaction at 149.5 MeV with $(\theta_p, \theta_n) = (44.3^\circ, 36.1^\circ)$, and (b) for the $^{48}\text{Ca}(p,pn)^{47}\text{Ca}$ reaction at 149.5 MeV with $(\theta_p, \theta_n) = (47.3^\circ, 36.1^\circ)$.



**Relationship between Gamow-Teller Transition Probabilities and (p,n)
Cross Sections at Small Momentum Transfers**

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Gamow-Teller transition probabilities are extracted for eight nuclei with masses between $A = 13$ and 39 from medium-energy (p,n) reactions via the distorted-wave impulse approximation, and compared with experimental β -decay and with free-nucleon transition probabilities. These comparisons indicate strongly that the renormalization of the Gamow-Teller operator needed for (p,n) reactions on finite nuclei is different from that needed for β decay.

**Here we were converting
single proton holes into
single neutron holes**



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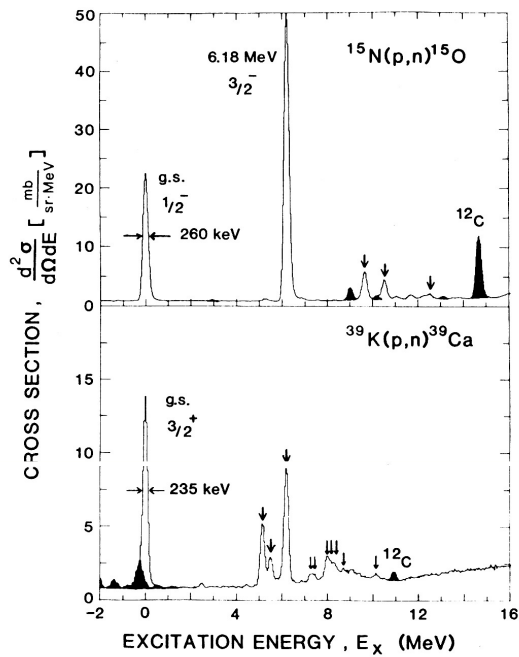
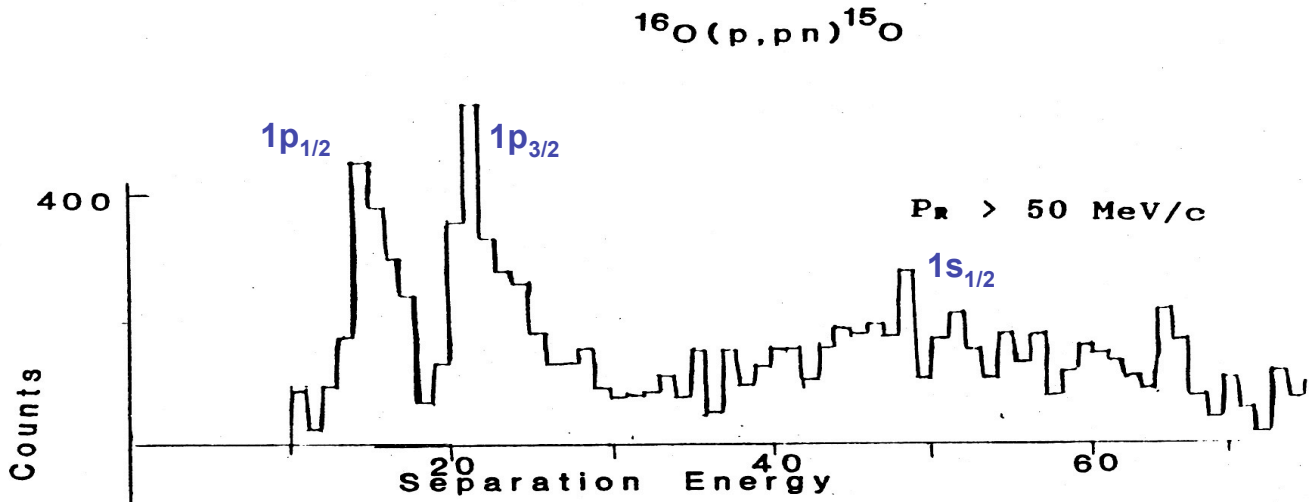


FIG. 1. Excitation-energy spectra for the reactions $^{15}\text{N}(p,n)^{15}\text{O}$ and $^{39}\text{K}(p,n)^{39}\text{Ca}$ at 135 MeV and 0° . The arrows indicate the locations of transitions with $\Delta L = 0$ angular distribution which are known or presumed to be $1p_{3/2}$ ($1d_{5/2}$) hole states for ^{15}O (^{39}Ca). Shaded peaks are from contaminants.

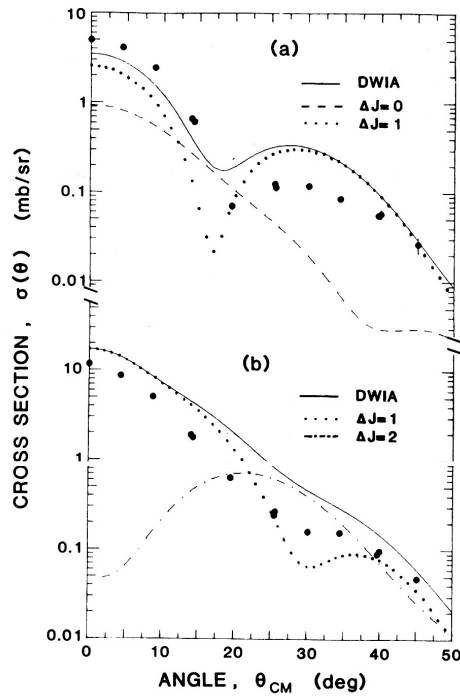


FIG. 2. Cross-section angular distributions for the reaction $^{15}\text{N}(p,n)^{15}\text{O}$ at 135 MeV, (a) for the ^{15}O g.s. and (b) for the ^{15}O 6.18-MeV state. The curves are DWIA calculations described in the text.

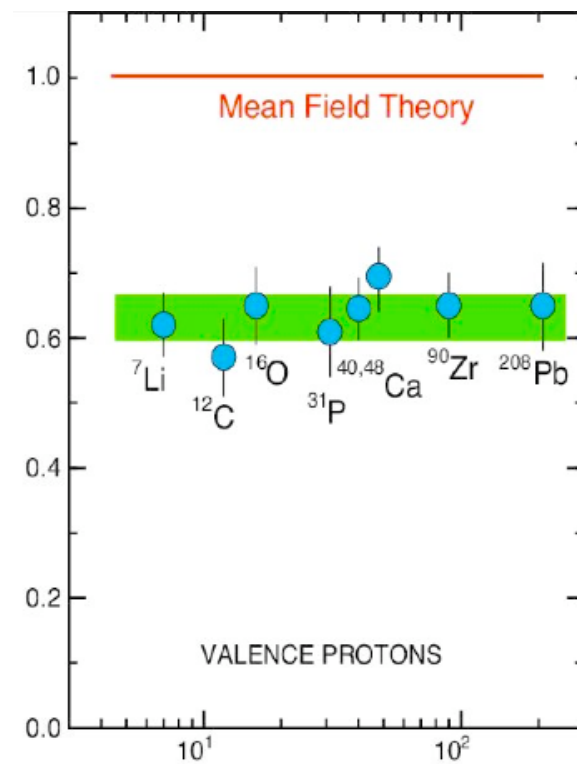


Study of SRCs with High-Energy Protons

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But I knew something was
MISSING!

Spectroscopic
factors
for (e,e'p)
reactions
show only
60-70%
of the
expected
single-particle
strength.



There must be more!



Study of SRCs with High-Energy Protons
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Experiment E850

The EVA Collaboration

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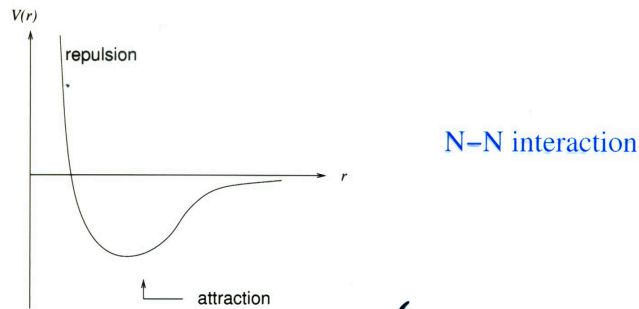
Kyoto Univ.



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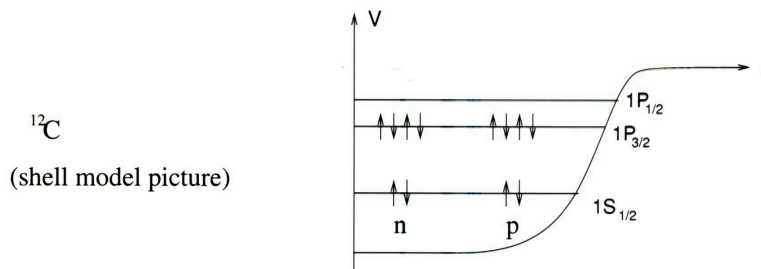
The N-N Interaction, the Shell Model and SRC



Nuclear Shell Model (~ 1950)

}	Maria Mayer
	J.H.D. Jensen
	Nobel Prize in 1963

The attractive part of the N-N interaction in combination with Pauli principle produces an average attractive potential with well defined quantum states.



Short-range repulsion \rightarrow saturation of nuclear densities, etc.

However, the short-range repulsive part must also manifest itself in the wavefunctions of nucleons in the nucleus. Because it is short range, high-momentum components will be affected. Typically we might expect N-N interactions of short range to produce pairs of nucleons with large, \sim equal, and opposite momenta.

Study of SRCs with High-Energy Protons

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Nuclear Fermi Momenta from Quasielastic Electron Scattering

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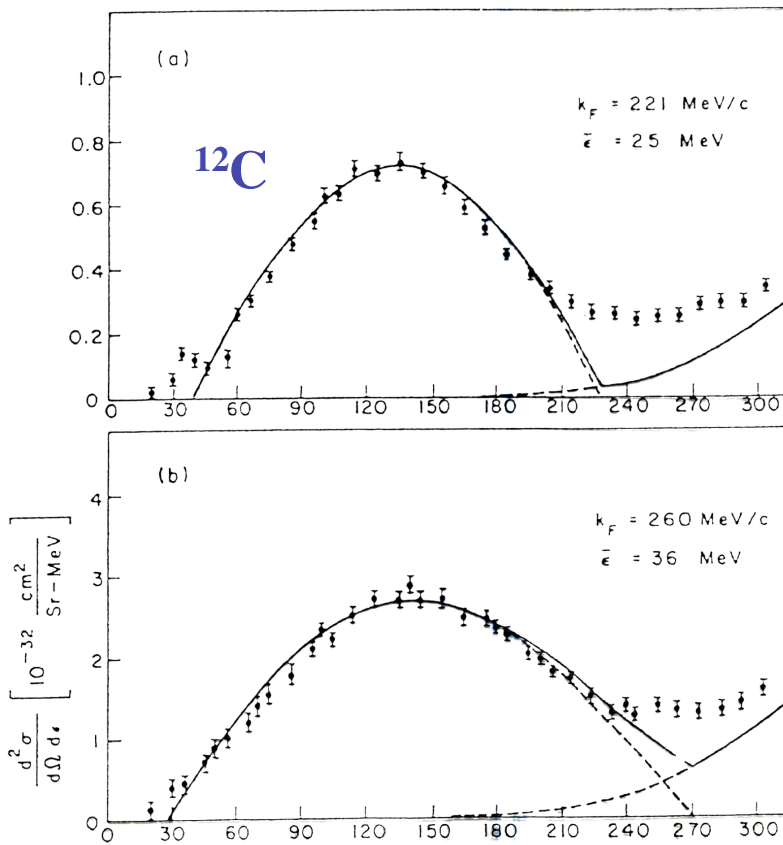
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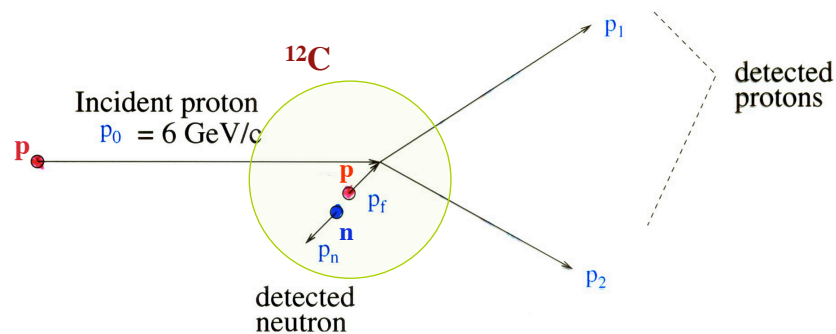


Study of SRCs with High-Energy Protons

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For quasi-elastic scattering, we can apply the impulse approximation (IA) to the interaction of the projectile with a proton in a correlated pair.



We reconstruct the momentum \vec{p}_f of the struck proton:

$$\vec{p}_f = \vec{p}_1 + \vec{p}_2 - \vec{p}_0$$

We then ask is there a neutron in coincidence, and are \vec{p}_n and \vec{p}_f "Correlated"

i.e. roughly *equal* and *opposite*?



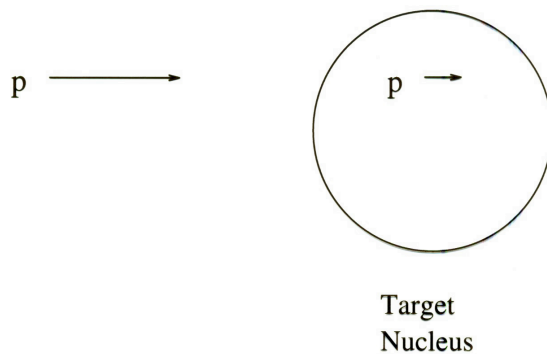
For energies of several GeV and up,
 For p-p elastic scattering near 90° c.m.,

$$\frac{d\sigma}{dt} \sim s^{-(n_1+n_2+n_3+n_4-2)}$$

$$\sim s^{-10}$$

where the Mandelstam variable $s = (P_0 + P_F)^2$ is the square of the total c.m. energy.

So for quasi-elastic p-p scattering near 90° c.m., we have a very strong preference for reacting with nuclear protons with their Fermi motion in the beam direction.



Forward going, high-momentum nuclear protons are preferentially selected, because *this minimizes s.*



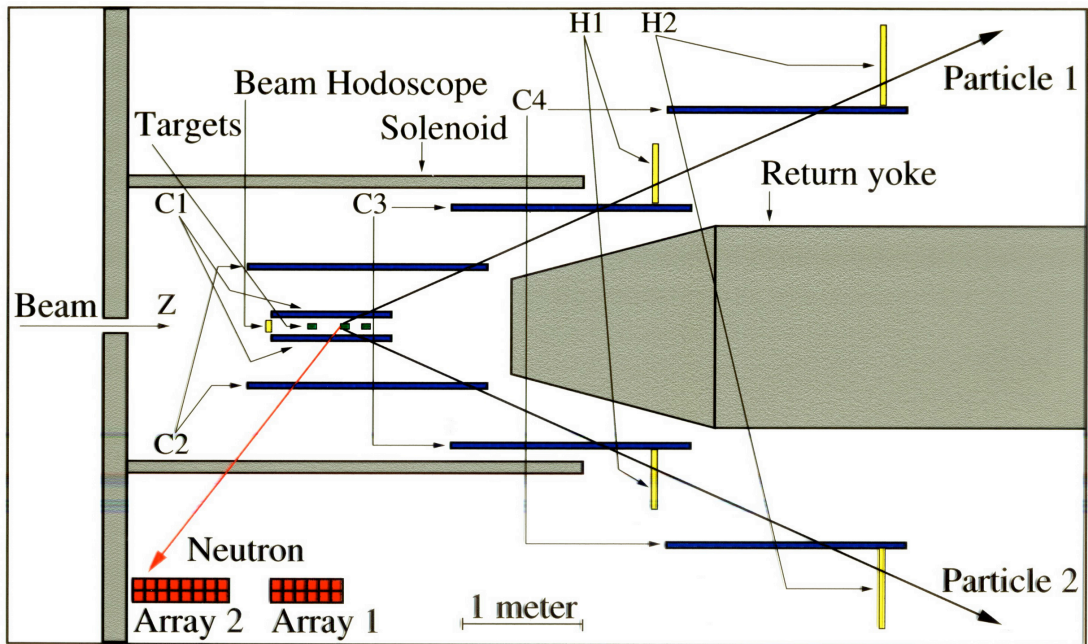
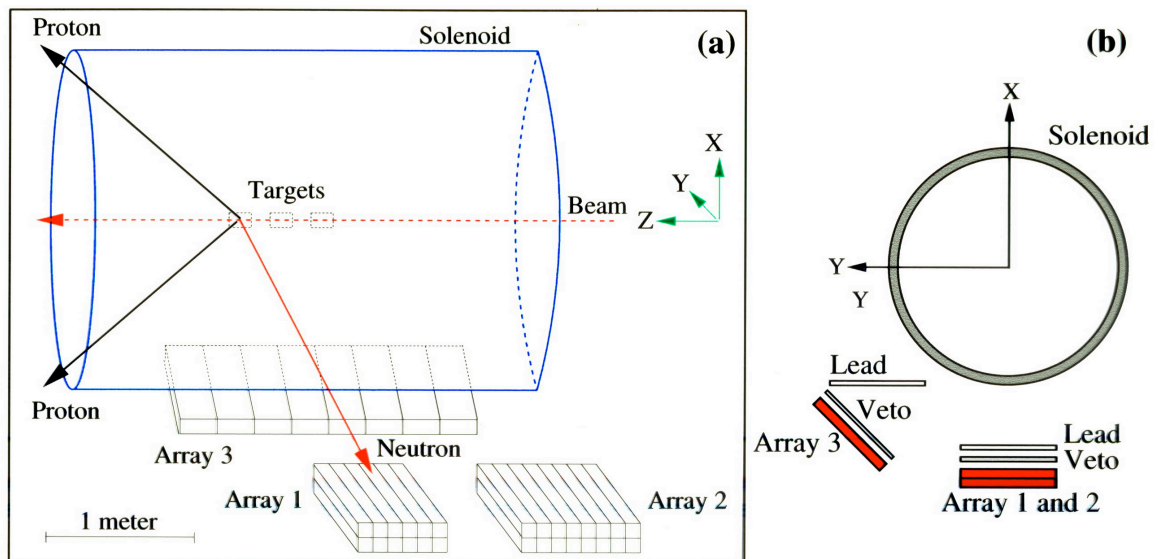


Figure 1: A schematic side view of the EVA spectrometer.





Array 1: total area $0.6 \times 1.0 \text{ m}^2$, 12 counters, 2 layers 0.125 m each.
 Array 2: total area $0.8 \times 1.0 \text{ m}^2$, 16 counters, 2 layers 0.125 m each.
 Array 3: total area $2 \times 1.0 \text{ m}^2$, 8 counters, 1 layers 0.1 m each.

Figure 5: A schematic side view (a) and a head-on view (b) of the EVA spectrometer and the neutron counter arrays.



Quasi-elastic analysis:

→ Track Reconstruction:

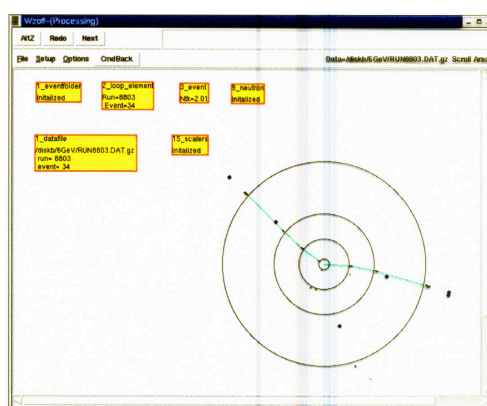


Figure 9: *woff* event display in transverse plane.

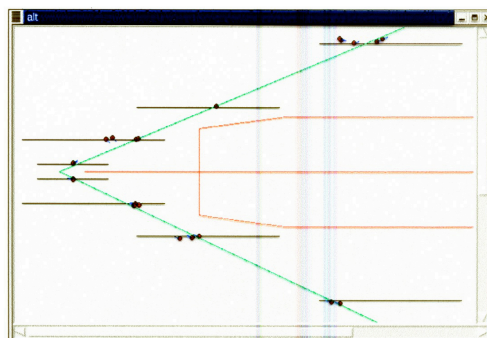


Figure 10: *woff* event display in RZ plane.



➔ Calculation of Kinematic Variables:

z-coordinate of The Vertex:

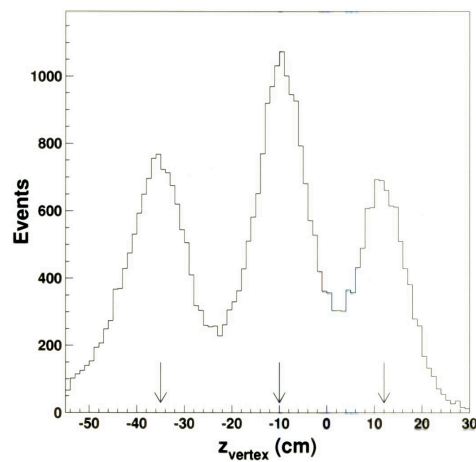


Figure 12: Distribution of z_{vertex} for reconstructed events at 5.9 GeV/c beam momentum. The length of each target is 6 cm and the arrows show the three target central positions.

Cuts to identifying the targets:

$$dz < 15 \text{ cm}$$

$$-45 < z_{vertex} < -25 \longrightarrow \text{target at } -35 \text{ cm}$$

$$-20 < z_{vertex} < 0 \longrightarrow \text{target at } -10 \text{ cm}$$

$$0 < z_{vertex} < 25 \longrightarrow \text{target at } 12 \text{ cm}$$



➔ Calculation of Physical Quantities:

Missing Energy:

$$E_{miss} = E_0 + m - E_1 - E_2$$

where E_0 is the beam energy, m is the mass of proton, E_1 and E_2 are the energies of the two outgoing protons.

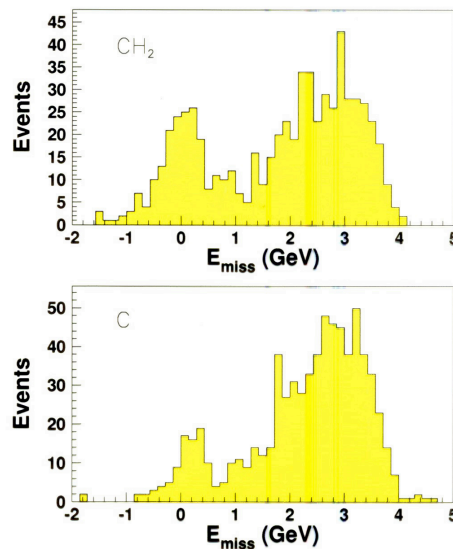


Figure 14: Missing energy spectra for (p,2p) events at 5.9 GeV/c beam momentum on CH₂ targets (top panel) and on C targets (bottom panel).



Measurement of quasi-elastic $^{12}\text{C}(p,2p)$ scattering at high momentum transfer

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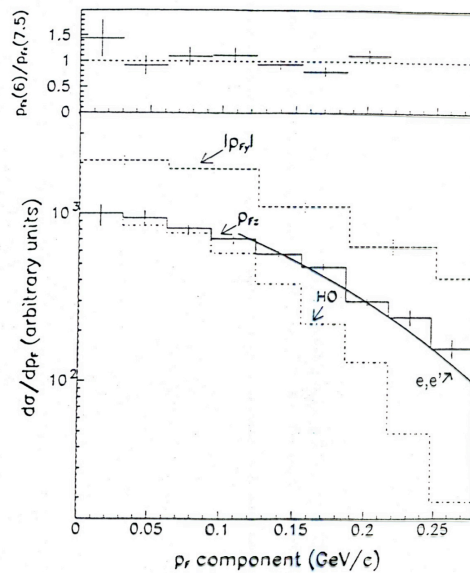
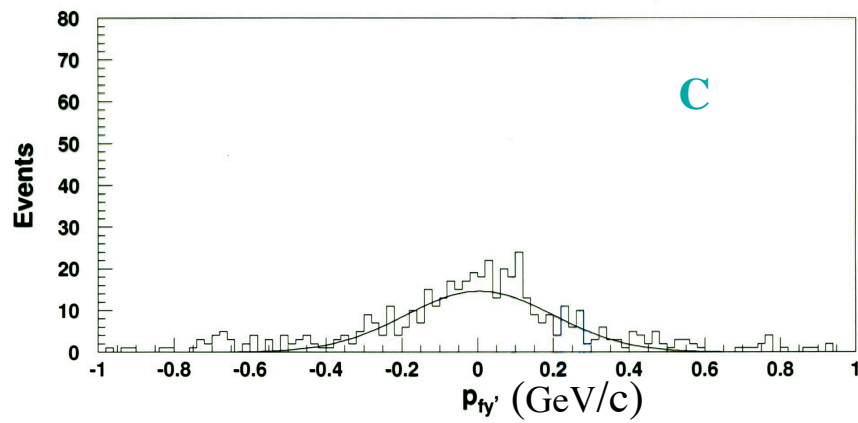
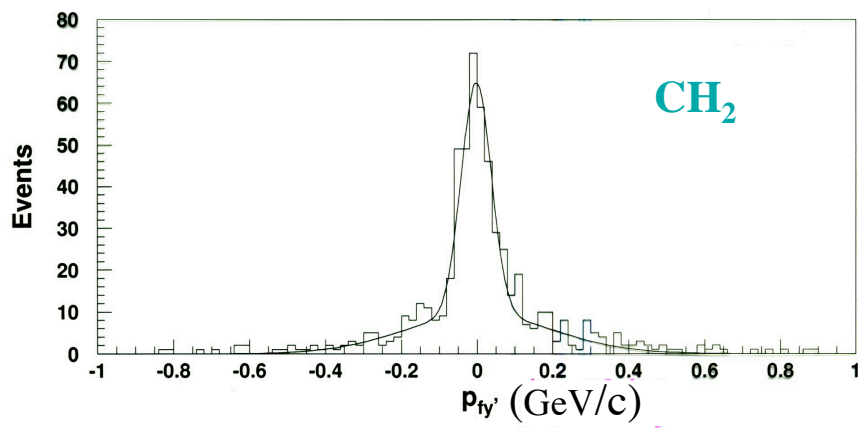


Fig. 3. The upper part of the figure shows the ratio of the two distributions measured at 6 and 7.5 GeV/c (the last two highest momentum points were measured at 6 GeV/c only). p_{Fz} is the longitudinal ground state momentum distribution, obtained from the α distributions for 6 and 7.5 GeV/c combined, after correction for the s dependence induced by the elementary free cross section. The $|p_{Fy}|$ is the transverse distribution extracted from several α regions (see text). HO is a harmonic oscillator indepen-



Transverse component of p_f



Light Cone Description of the (p,2p+n) Reaction:

The momentum of a nucleon is described in light-cone space by (\mathbf{p}_t, α) , where \mathbf{p}_t is the transverse momentum and α defined as:

$$\alpha = \frac{E - p_z}{m}$$

represents the fraction of the nuclear momentum carried by the target nucleon in the light-cone reference frame.

➔ Mandelstam variable s :

$$\begin{aligned} s &= (P_0 + P_F)^2 \\ &= m^2 + m_1^2 + 2P_0P_F \\ &= m^2 + m_1^2 + (E_0 - P_0)(E_F + p_F^z) + \alpha m(E_0 + P_0) \\ &\sim m^2 + m_1^2 + 2\alpha m p_0 \end{aligned}$$

where $\alpha = \frac{E_F - p_F^z}{m}$ is the light cone variable for target nucleon and for large incident momenta, the approximation: $E_0 - p_0 \approx 0$ and $E_0 + p_0 \approx 2p_0$ was used.



Longitudinal component of p_f

From the momentum conservation:

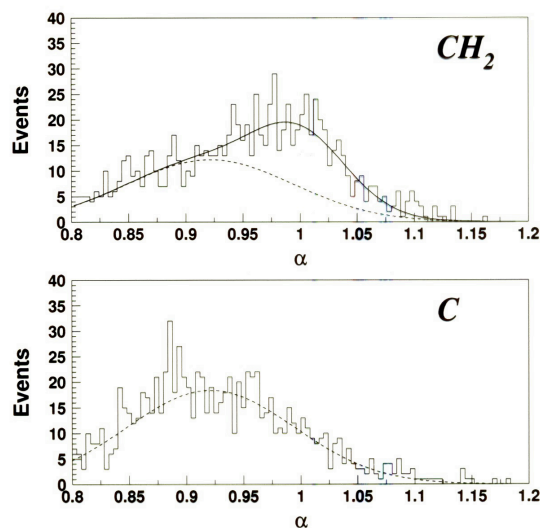
$$p_{fz} = \frac{p_{t1}}{\tan\theta_1} + \frac{p_{t2}}{\tan\theta_2} - p_0$$

Subtraction
of large numbers

From light cone variable α :

$$\alpha = \frac{E_f - p_{fz}}{m} \sim 1 - \frac{p_{fz}}{m}$$

$$p_{fz} = m \cdot (1 - \alpha).$$



*Light-cone
Magic!*

Figure 16: Light-cone variable α distribution for CH_2 and C targets at 5.9 GeV/c beam momentum.



Neutron Analysis:

➔ Inverse Velocity:

$$v^{-1} = \frac{TOF}{l} = \frac{TOF}{\sqrt{x_{hit}^2 + y_{hit}^2 + (z_{hit} - z_{target})^2}}$$

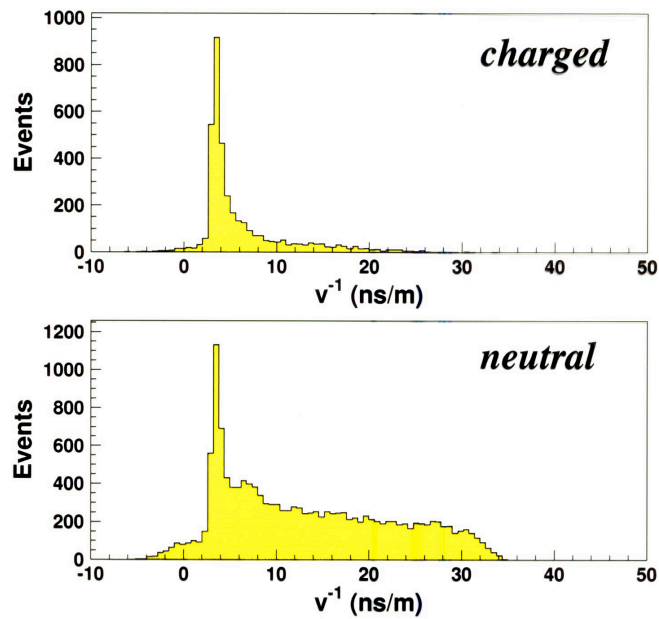


Figure 17: Inverse velocity spectra for charged and neutral particles detected in neutron counter array 3 at 5.9 GeV/c beam momentum.



Software cuts for data replay.

Cuts on protons:

Čerenkov cut: select protons

Number of tracks: 2 tracks

Target Positions: $|z_{target} + 10| < 10$

$|z_{target} + 35| < 10$

$|z_1 - z_2| < 12$

Missing Energy: $|E_{miss} - 0.32| < 0.5$ GeV

ϕ (for arrays 1 and 2): $45^\circ < \phi_1 < 135^\circ$, or

$225^\circ < \phi_1 < 315^\circ$

ϕ (for array 3): $0^\circ < \phi_1 < 90^\circ$, or

$180^\circ < \phi_1 < 270^\circ$

Cuts on neutrons:

Neutron Momentum: $0.05 < p_n < 0.55$ GeV/c



Identification of Correlated Events

One-Dimensional Correlations:

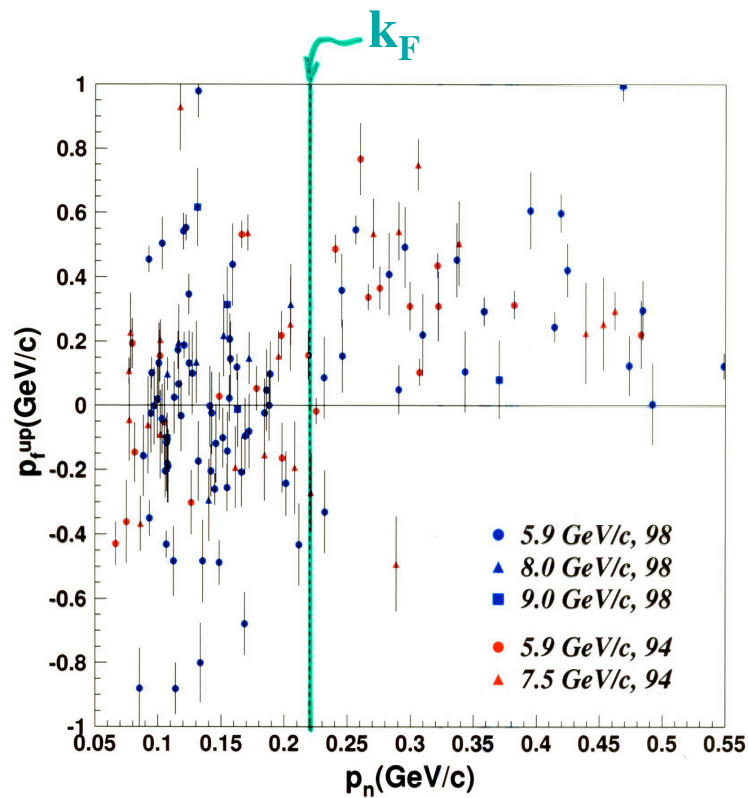


Figure 19: p_f^{up} vs. p_n for $^{12}\text{C}(p,2p+n)$ events. Data labelled “98” (solid symbols) are for 98 runs (this experiment). Data labelled “94” are from Aclander, et al. The vertical line at 0.22 GeV/c corresponds to k_F , the Fermi momentum for ^{12}C .



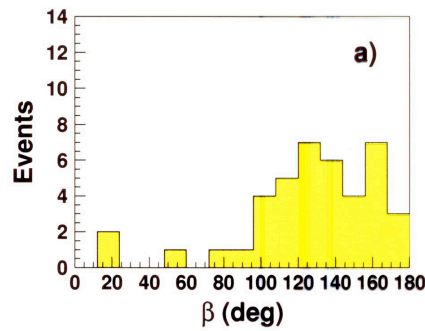
Study of SRCs with High-Energy Protons

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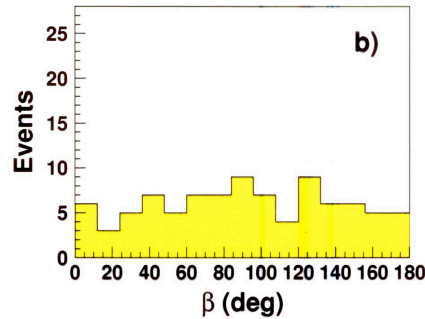
Transverse Correlations:

The angle between the transverse momenta of proton and neutron is defined as:

$$\beta = \cos^{-1} \left(\frac{\vec{p}_{nt} \cdot \vec{p}_{ft}}{|\vec{p}_{nt}| |\vec{p}_{ft}|} \right).$$



$p_n > k_F$



$p_n < k_F$

Figure 20: Plots of β , the angle in the transverse plane between \vec{p}_f and \vec{p}_n . Panel (a) is for events with $p_n > 0.22$ GeV/c, and panel (b) is for events with $p_n < 0.22$ GeV/c, where 0.22 GeV/c = k_F , the Fermi momentum for ^{12}C .



Full Correlations:

We then construct the directional correlation between \vec{p}_f and \vec{p}_n as

$$\cos\gamma = \frac{\vec{p}_f \cdot \vec{p}_n}{|\vec{p}_f| |\vec{p}_n|}$$

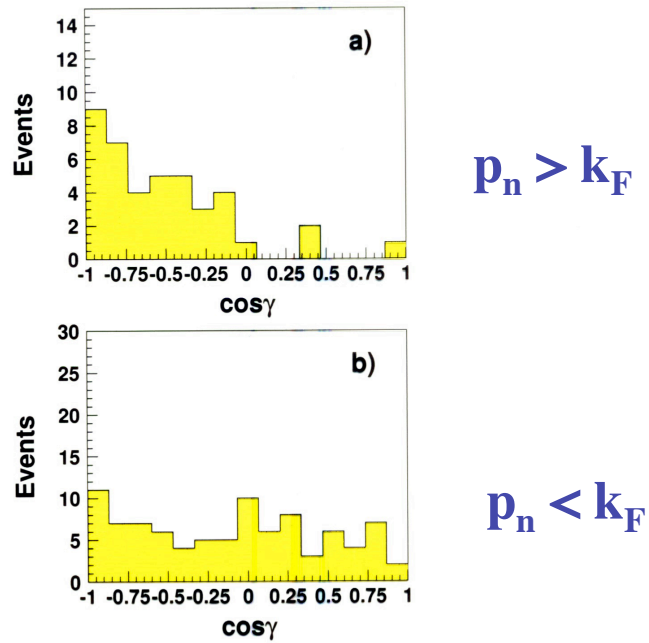


Figure 21: Plots of $\cos\gamma$, where γ is the angle between \vec{p}_n and \vec{p}_f . Panel (a) is for events with $p_n > 0.22$ GeV/c, and panel (b) is for events with $p_n < 0.22$ GeV/c; 0.22 GeV/c = k_F , the Fermi momentum for ^{12}C .



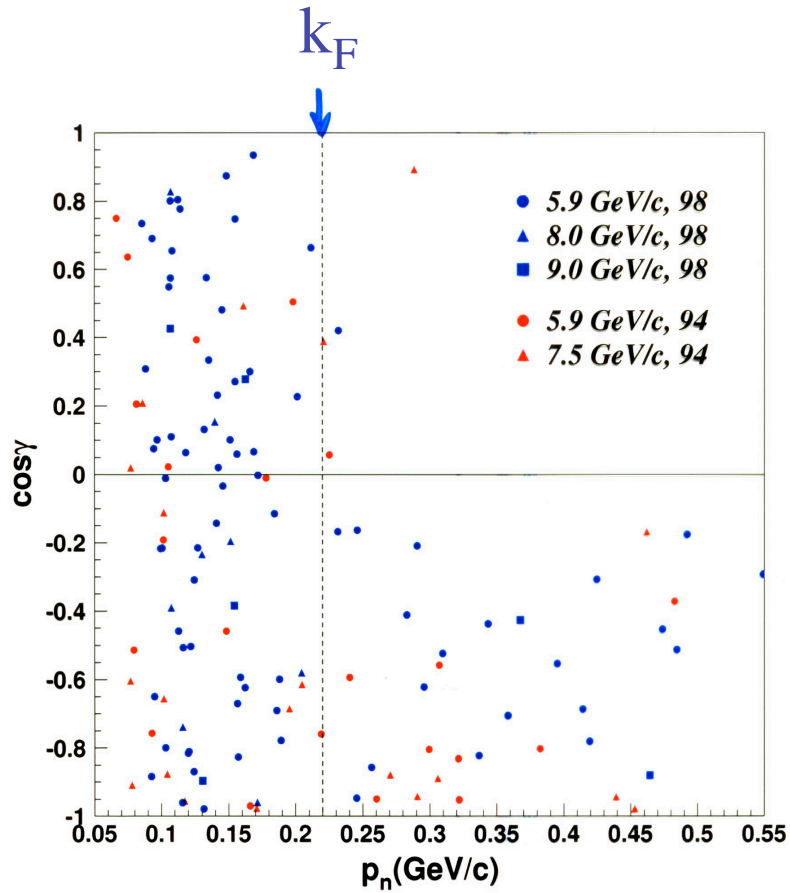
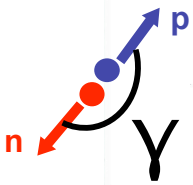


Figure 22: $\cos\gamma$ vs. p_n for $^{12}\text{C}(p,2p+n)$ events. The vertical line at 0.22 GeV/c corresponds to k_F , the Fermi momentum for ^{12}C .



Study of SRCs with High-Energy Protons

Trieste, May 2008

**So why did this work so well
when our count rate was only
* * 1 per week ?**

1. The s^{-10} dependence of p-p elastic scattering, which preferentially selects high momentum nuclear protons. (Hadrons *are* different from leptons!)
2. The improved resolution from using light cone variables.
3. The small deBroglie wavelength of the incident protons:

$$\lambda = h/p = hc/pc = 2\pi \cdot 0.197 \text{ GeV-fm}/(6 \text{ GeV})$$

$$\approx 0.2 \text{ fm.}$$

This meant that our probe could interact with a single member of a correlated pair!



The Correlated Fraction of (p,2p) Events:

For the 6 GeV 1998 data set we estimated the fraction of (p,2p) events with $p_f > 0.22$ GeV/c, which have a correlated backwards neutrons with $p_n > 0.22$ GeV/c.

$$F = \frac{\text{corrected \# of } (p,2p+n) \text{ events}}{\text{\# of } (p,2p) \text{ events}} = \frac{A}{B}$$

The quantity A was obtained from the sample of all 18 (p,2p+n) events with $p_n \geq k_F = 0.22$ GeV/c, where a correction for flux attenuation and detection efficiency was applied event-by-event, and then corrected for the solid-angle coverage:

$$A = \frac{2\pi}{\Delta\Omega} \sum_{i=1}^{18} \frac{1}{\epsilon_i} \cdot \frac{1}{t_i} = 1090.$$

The average value of $(1/\epsilon_i t_i)$ was 8.2 ± 0.82 and $2\pi/\Delta\Omega = 7.42$. We can then calculate

$$F = \frac{A}{B} = \frac{1090}{2205} = 0.49 \pm 0.13.$$



- The Center of Mass Motion of the $n - p$ Pair:

$$p_z^{cm} = p_{nz} + p_{fz}$$

We can express this in terms of α as

$$\begin{aligned} \alpha_p + \alpha_n &= \frac{E_f - p_p^z}{m} + \frac{E_f - p_n^z}{m} \\ &= \left(1 - \frac{p_{fz}}{m}\right) + \left(1 - \frac{p_{nz}}{m}\right) \end{aligned}$$

⇒

$$p_z^{cm} = 2m\left(1 - \frac{\alpha_p + \alpha_n}{2}\right)$$

- The Relative Motion of the Correlated Nucleons:

$$\begin{aligned} \alpha_p - \alpha_n &= \left(1 - \frac{p_{fz}}{m}\right) - \left(1 - \frac{p_{nz}}{m}\right) \\ &= \left(\frac{p_{nz} - p_{fz}}{m}\right) \end{aligned}$$

⇒

$$\begin{aligned} p_z^{rel} &= |p_{fz} - p_{nz}| \\ &= m|\alpha_p - \alpha_n| \end{aligned}$$



The Relative and c.m. Motion of Correlated n-p Pairs:

$$p_z^{cm} = 2m\left(1 - \frac{\alpha_p + \alpha_n}{2}\right),$$

$$p_z^{rel} = m|\alpha_p - \alpha_n|.$$

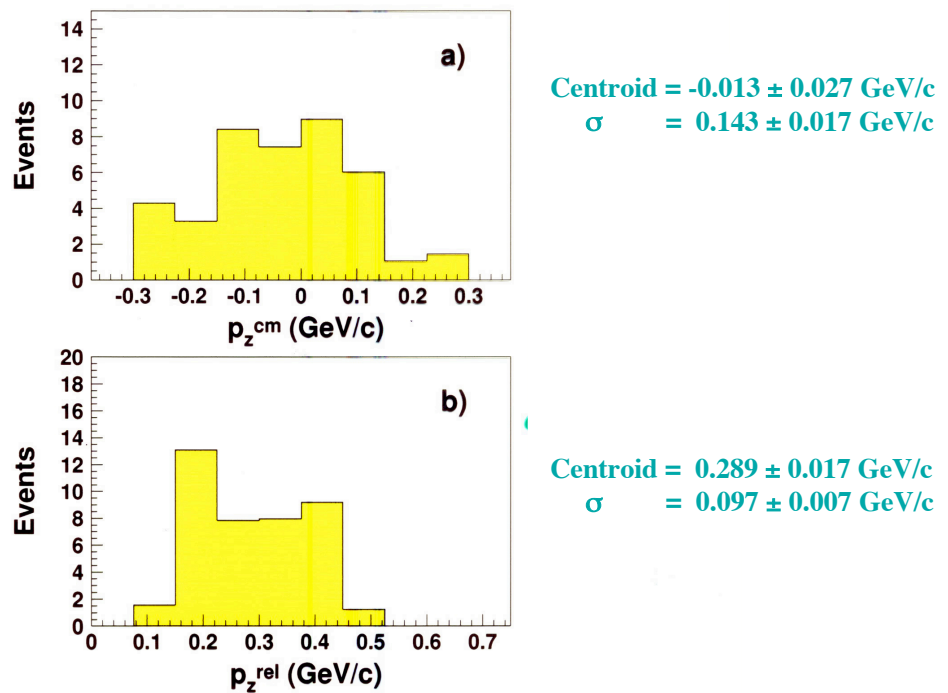


Figure 23: Plots of (a) p_z^{cm} and (b) p_z^{rel} for correlated n-p pairs in ^{12}C , for $^{12}\text{C}(p,2p+n)$ events. Each event has been “s-weighted”.



Summary

1. For quasielastic (p,2p) events we reconstructed \vec{p}_f the momentum of the knocked-out proton before the reaction; \vec{p}_f was then compared with \vec{p}_n , the measured, coincident neutron momentum. For $|\vec{p}_n| > k_F = 0.220 \text{ GeV}/c$ (the Fermi momentum) a strong back-to-back directional correlation between \vec{p}_f and \vec{p}_n was observed, indicative of short-range n-p correlations.
2. We determined that $49 \pm 13 \%$ of events with $|\vec{p}_f| > k_F$ had directionally correlated neutrons with $|\vec{p}_n| > k_F$. Thus 2N SRCs are a major source of high-momentum nucleons in nuclei.
3. We also measured the c.m. and relative momenta of correlated n-p pairs in the longitudinal direction.

4. And . . .



**A. A. Tang et al.,
Phys. Rev. Lett. 90, 042301 (2003)**



Study of SRCs with High-Energy Protons
Trieste, May 2008

Recent Development

“Evidence for the Strong Dominance of Proton-Neutron Correlations in Nuclei”

by

E. Piassetzky, M Sargsian, L. Frankfurt, M Strikman
and J. W. Watson

Phys. Rev. Lett., 20 October 2006

- ⊗ Analysis of the EVA Data
- ⊗ Assumes 100% NN-SRCs above 275 MeV/c
- ⊗ Includes the motion of the pair
- ⊗ Includes absorption of entering and
exiting nucleons in the nuclear medium

**Conclusion: $92 \pm 18\%$ of high-momentum
protons have correlated neutrons.**



B. JLab Experiment E01-015
Completed in Spring 2005

Spokesmen: Bill Bertozzi, MIT
Eli Piassetzky, Tel Aviv
John Watson, Kent State
Steve Wood, Jlab

And: Shalev Gilad
Doug Higinbotham

Ph.D. Students: Ramesh Subedi, Kent State
Ran Shneor, Tel Aviv
Peter Monaghan, MIT



The Results from E01-015 can be found in:

- 1) R. Shneor, et al., Phys. Rev. Lett. **99**, 072501 (2007).
- 2) R. Subedi, et al., **SCIENCE**, in press.

The results of the BNL (p,2p+n) experiment are fully consistent with the results of the JLab (e,e'p+N) experiment:

- * Different Laboratories
- * Different probes
- * Different Graduate Students
- * Different millenia
- * **Same Results!**
- * **We are observing nuclear structure**





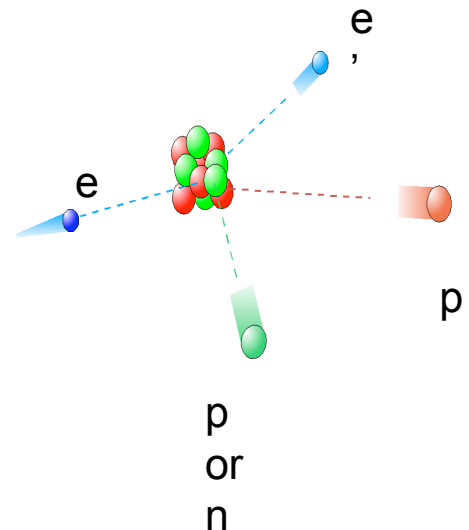
Studying Short range Correlations in Nuclei at the Repulsive Core Limit via the triple Coincidence (e, e' p N) Reaction

Hall A / TJNAF

Proposal 07-006

(Next Generation of E01-015)

PAC 31/TJNAF Jan. 2007



Study of SRCs with High-Energy Protons

Trieste, May 2008

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