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Jet correlations from unintegrated parton distributions.

F. Hautmann CERN Switzerland Hadronic Physics 08 — Triest, May 2008

Jet correlations from unintegrated parton distributions F. Hautmann (Oxford/CERN)

- I. Motivation: multiparticle production in high-energy hadron collisions
- **II**. General issues on unintegrated parton distributions
- **III**. Multi-jet correlations in small-x final states

$I. \ \mathsf{INTRODUCTION}$

Multi-scale hard processes at high-energy hadron colliders



phase space opening up for large \sqrt{s} \Downarrow

- large number of events with multiple hard scales: q_1^2, \cdots, q_n^2
 - potentially large corrections to all orders in α_s , $\sim \ln^k (q_i^2/q_j^2)$
- parton distributions probed near kinematic boundaries $x \rightarrow 0$, $1 x \rightarrow 0$

▷ Part of the effects are universal

 \hookrightarrow ex.: high-order corrections in renormalization group evolution

$$\mu \frac{d}{d\mu}f = \gamma \otimes f$$

 $\gamma\simeq\gamma^{(LO)}\left(1+c_1\alpha_s+\ldots+c_{n+m}\alpha_s^m(\alpha_s\ L)^n+\ldots\right)\ ,\ L=\ \text{``large log''}$

▷ Part of them are not universal (final-state correlations, exclusive variables, ...)

- \hookrightarrow yet can be summed by techniques that generalize RG factorization
 - pdf's unintegrated in both || and \perp components

Examples:

- Sudakov processes
 - \bullet small-x physics
- reconstruction of fully exclusive final states by Monte-Carlos

• perturbative calculations at fixed order (NLO, multi-leg)

Multi-jet final states:

• parton-shower event simulation (higher orders, hadronization)

- included partially, order-by-order, in perturbative calculations (higher loops)
 amounts to corrections to the angular ordering in standard parton showers (HERWIG, PYTHIA)
 - \diamond inclusive jet cross sections: NLO (+ standard shower) probably sufficient \diamond correlations, exclusive final-state structure?

 \diamond Multiple QCD radiation \rightarrow parton shower:

 \triangleright HERWIG: ordering in decay angles in space-like shower (\approx k_1-ordering for x \ll 1)



<u>Outline</u>

i) How to characterize u-pdf's with precision?

p gauge-invariant operator matrix elements

Ightcone divergences and regularization methods

ii) Applications to $x \ll 1$ parton showers and jets

effects of initial-state radiation on multi-jet angular correlations

II. General issues on u-pdf's

Example 1: Ordinary (integrated) pdf



correlation of quark fields at lightlike separation $y = (0, y^-, 0_\perp)$:

 $\widetilde{f}(y) = \langle P \mid \overline{\psi}(y) V_y^{\dagger}(n) \gamma^+ V_0(n) \psi(0) \mid P \rangle ,$

 $V_y(n) = \mathcal{P} \exp\left(ig_s \int_0^\infty d au \,\, n \cdot A(y+ au \,\, n)
ight)$ eikonal line in direction $n=(0,1,0_\perp)$

- μ -dependence from renormalization of operator product
 - gauge-invariant Wilson line matrix elements

Example 2: Unintegrated pdf from physical cross section (high energy limit). E.g.:



 \diamondsuit single gluon polarization dominates $s \gg M^2 \gg \Lambda_{\rm QCD}^2$

 \hookrightarrow gauge invariance rescued (despite gluon off-shell)

♦ but to define u-pdf gauge-invariantly over the whole phase space is more difficult

Example 3: Generalize matrix element to non-lightlike distances

 $\widetilde{f}(y) = \langle P \mid \overline{\psi}(y) V_y^{\dagger}(n) \gamma^+ V_0(n) \psi(0) \mid P \rangle \quad , \qquad y = (0, y^-, y_{\perp})$

• works at tree level [Mulders, 2002; Belitsky et al., 2003; Collins, 2004]

• subtler at level of radiative corrections \hookrightarrow

 \diamond Suppose a gluon is absorbed or emitted by eikonal line:

 \diamond Physical observables:

$$egin{array}{rcl} \mathcal{O} &=& \int dx \; dk_\perp \; f_{(1)}(x,k_\perp) \; arphi(x,k_\perp) \ &=& \int dx \; dk_\perp \; \left[arphi(x,k_\perp) - arphi(1,0_\perp)
ight] P_R(x,k_\perp) \end{array}$$

inclusive case: φ independent of $k_{\perp} \Rightarrow 1/(1-x)_{+}$ from real + virtual general case: endpoint divergences (incomplete KLN cancellation)

 \bullet Distributions at fixed k_\perp are no longer protected by KLN mechanism against uncancelled lightcone divergences

• Only after supplying matrix element with a regularization prescription is distribution well defined.

 \bullet Note: regularization of endpoint divergences also affects distributions integrated over k_\perp and UV subtractions

[H, hep-ph/0702196]

Ex.:
$$\int dk_{\perp} f(x, k_{\perp}, \mu) \Theta(\mu - k_{\perp}) \stackrel{?}{=} f^{\overline{\mathrm{MS}}}(x, \mu)$$

= holds only at tree level: full relation involves coefficient function R

$$\int^{\mu} dk_{\perp} f(x, k_{\perp}, \mu) = R(x) \otimes f^{\overline{\mathrm{MS}}}(x, \mu)$$

 $\Diamond R$ calculable as a power series in α_s , $R(x) = \delta(1-x) + \sum_k r_k \alpha_s^k$

• Applications: Cut-off regularization vs. Subtractive regularization

CUT-OFF REGULARIZATION

cut-off in Monte-Carlo generators using u-pdf's

CASCADE	www.quark.lu.se/~hannes/cascade
SMALLX	Marchesini & Webber, 90's
LDCMC	www.thep.lu.se/~leif/ariadne

 \triangleright cut-off from gauge link in non-lightlike direction n:



finite $\eta \Rightarrow$ singularity is cut off at $1-x \gtrsim \sqrt{k_\perp/4\eta}$

• Note: lightcone limits $y^2 \rightarrow 0$ and $n^2 \rightarrow 0$ do not commute \Rightarrow

$$\Rightarrow \int dk_{\perp} f(x, k_{\perp}, \mu, \eta) = F(x, \mu, \eta) \neq \text{ ordinary pdf}$$

UPDF's WITH SUBTRACTIVE REGULARIZATION

• Endpoint divergences $x \rightarrow 1$ from incomplete KLN cancellation

Subtractive method: more systematic than cut-off. Widely used in NLO calculations. Formulation suitable for eikonal-operator matrix elements: Collins & H, 2001.

 \bullet gauge link still evaluated at n lightlike, but multiplied by "subtraction factors"



H, arXiv:0708.1319

 $\diamond u$ serves to regularize the endpoint; drops out of distribution integrated over k_{\perp}

III. Jet correlations in small-x final states

 \diamond All MC's based on u-pdf's rely on factorization $in_{\underline{k}} k_{\perp}$ to

a) generate hard-scattering event (hard ME)

b) couple it to initial-state shower

 \diamondsuit differ by detailed model for initial state



• all implement correct $\alpha_s^n x^{-1} \ln^{n-1} x$ behavior for spacelike evolution at $x \ll 1$ to all orders in α_s

 $\exp \int (dk^2/k^2)\gamma(\alpha_s(k^2))$

• resum non-universal $\alpha_s^k \ln^k(s/p_{\perp}^2)$ (in certain cases)

subleading contributions possibly important for final states

Implementations:

Höche, Kra	uss and Teubner, arXiv:0705.4577 (BFKL)	
Golec, Jada	ach, Placzek, Stephens, Skrzypek, hep-ph/0703317 (CCFM)	
LDCMC	Lönnblad & Sjödahl, 2005; Gustafson, Lönnblad & Miu, 2002	(LDC)
CASCADE	Jung, 2004, 2002; Jung and Salam, 2001 (CCFM)	
SMALLX	Marchesini & Webber, 1992 (CCFM)	

Advantages over standard Monte-Carlo like PYTHIA or HERWIG:

- better treatment of high-energy logarithmic effects
- \bullet likely more suitable for simulating underlying event's k_\perp

Current limitations:

- \bullet radiative terms associated to $x\sim 1$ not automatically included
- procedure to correct for this not yet systematic

 $\hookrightarrow e.g.: \text{ LO-DGLAP in Höche et al}$

• quark contributions in initial state included partially

 \hookrightarrow see also: k_{\perp} kernel for sea-quark evolution [Catani & H]

• limited knowledge of u-pdf's [Jung et al., arXiv:0706.3793;

J. R. Andersen et al., 2006]

Basic ingredients in the CASCADE Monte-Carlo

• ME by perturbative computation

• branching eq. :
$$\mathcal{A}(x, k_T, \mu) = \mathcal{A}_0(x, k_T, \mu) + \int \frac{dz}{z} \int \frac{dq^2}{q^2} \Theta(\mu - zq)$$

 $\times \quad \Delta(\mu, zq) \ \mathcal{P}(z, q, k_T) \ \mathcal{A}(\frac{x}{z}, k_T + (1 - z)q, q)$



(left) Coherent radiation in the space-like parton shower for $x \ll 1$; (right) the unintegrated splitting function \mathcal{P} , including small-x virtual corrections.

 $\alpha/x > \alpha_1 > \alpha$ (small - x coherence region)

U-pdf fits \oplus evolution

 $[\hookrightarrow \mathsf{DIS}, \, \mathsf{jets}, \, \mathsf{heavy} \, \mathsf{flavors}]$

unintegrated gluon distribution as a function of x , k_1, μ [Hansson & Jung, 2007]



MULTI-JET DIS PRODUCTION AND NLO RESULTS



(left) Azimuth dependence and (right) Bjorken-x dependence of di-jet distributions
 measured by ZEUS [arXiv:0705.1931]

• compared with NLO results [Z. Nagy and Z. Trocsanyi, PRL 87 (2001)]

 \diamond large variation from order- α_s^2 to order- α_s^3 prediction as $\Delta \phi$ and x decrease \Rightarrow sizeable theory uncertainty at NLO (underestimated by " μ error band")

- Jet clustering and hadronization:
 - ▷ moderate hadronization corrections from jet algorithm used by Zeus and H1
 [arXiv:0705.1931 [hep-ex]; hep-ex/0310019]
 ▷ jet clustering free of non-global logarithms
 [Dasgupta et al., hep-ph/0610242]
 ▷ asymmetric jet cuts to avoid double logs in minimum p_T
 [Banfi and Dasgupta, hep-ph/0312108]
 ▷ nonperturbative corrections in inverse powers of Q moderate for Q² > 10GeV²
- Radiative effects at higher order:

fixed-order beyond NLO is outside present reach for multi-jets in ep and pp
 enhanced (soft/collinear) higher orders from near back-to-back region
 Y.Delenda et al., arXiv:0706.2172; arXiv:0804.3786; HERWIG

 \diamond largest effects seen at small $\Delta \phi$ (3 well-separated hard jets)



- besides angular correlations, sizeable NLO uncertainties in other associated distributions
 - NLO results much more stable for inclusive jet cross sections

AZIMUTHAL DISTRIBUTION OF THE THIRD JET



Cross section in the azimuthal angle between the hardest and the third jet for small (left) and large (right) azimuthal separations between the leading jets

Jung & H, arXiv:0712.0568 [hep-ph]

• small $\Delta \phi \Rightarrow$ non-negligible initial $k_{\perp} \Rightarrow$ larger corrections to collinear ordering • curves become closer at large $\Delta \phi$

Angular jet correlations from CASCADE and HERWIG compared with DIS data



(left) di-jet cross section; (right) three-jet cross section

Jung & H, arXiv:0712.0568 [hep-ph]

- different shapes from the two MC
 - largest differences at small $\Delta\phi$
- good description of measurement by CASCADE

Normalize to the back-to-back cross section:



▷ high-k_⊥ component in ME essential to describe correlation at small $\Delta \phi$ ▷ k_⊥-dependence in u-pdf alone not sufficient



JET MULTIPLICITIES

(left) $\Delta \phi < 2$; (right) $\Delta \phi > 2$

[Jung & H, arXiv:0805.1049]

• larger contribution from high multiplicity in the MC with u-pdf



between the leading jets

Summary on DIS 3-jet

 \triangleright U-pdfs \oplus k_{\perp}-dependent hard MEs describe multi-jet measurements including correlations.

Physical picture: • growth of k_⊥ along spacelike jet
 • finite-angle emission corrections

▷ Furthermore:

- Results similar to HERWIG if reduced to k_{\perp} -ordered phase space
 - Similar to fixed NLO where corrections are not large

 \triangleright Non-forward jets \Rightarrow results less dependent on details of u-pdf evolution models

IV. Further developments and conclusions

\diamond Forward-region observables

- More pronounced dependence on evolution model
- better understanding of u-pdf's needed in target fragmentation region [Trentadue et al, 2007]

\diamondsuit Gluon-gluon fusion processes:

 \bullet production of b, c

large NLO uncertainties at LHC energies

[Nason et al. 2004]

• final states with Higgs

 $10 \div 20 \%$ effects in p_t spectrum from $x \ll 1$ terms

[Kulesza, Sterman & Vogelsang, 2004]

ISSUES AT HIGHER ORDER

- u-pdf defined gauge-invariantly for small x by high-energy factorization
 - general definitions including x $\sim 1?$

Collins, Rogers and Stasto, arXiv:0708.2833 H, PLB 655 (2007) [hep-ph/0702196]

soft gluon exchange with spectator partons in pp collisions

 \longrightarrow possibly factorization-breaking? (back-to-back dihadron production) Mulders, Bomhof, Collins,

> Vogelsang, Qiu, Yuan, Pijlman, ... 2006-2008

 \diamond appears at N³LO (2 soft, 1 collinear partons)

 \diamond does it survive destructive interference from multiple emission?

 Note: Coulomb/radiative mixing terms also appear to break coherence in di-jet cross sections with gap in rapidity

Forshaw, Kyrieleis & Seymour, JHEP 08 (2006)

MORE ON U-PDF'S WITH SUBTRACTIVE REGULARIZATION

One loop expansion:

 $[\zeta = (p^{+2}/2)u^{-}/u^{+}]$

$$\begin{split} f_{(1)}^{(\mathrm{subtr})}(x,k_{\perp}) &= P_R(x,k_{\perp}) - \delta(1-x)\,\delta(k_{\perp}) \int dx' dk'_{\perp} P_R(x',k'_{\perp}) \quad (\leftarrow \mathrm{from\ numerator}) \\ &- W_R(x,k_{\perp},\zeta) + \delta(k_{\perp}) \int dk'_{\perp} W_R(x,k'_{\perp},\zeta) \quad (\leftarrow \mathrm{from\ vev's}) \end{split}$$

with $P_R = \alpha_s C_F / \pi^2 \left\{ 1 / [(1-x) \ (k_\perp^2 + m^2 (1-x)^2)] + \dots \right\} = \text{real emission prob.}$ $W_R = \alpha_s C_F / \pi^2 \left\{ 1 / [(1-x) \ (k_\perp^2 + 4\zeta (1-x)^2)] + \dots \right\} = \text{counterterm}$

• ζ -dependence cancels upon integration in k_{\perp}

$$\Rightarrow \mathcal{O} = \int dx \ dk_{\perp} \ f_{(1)}^{(\text{subtr})}(x,k_{\perp}) \ \varphi(x,k_{\perp})$$
$$= \int dx \ dk_{\perp} \ \{P_R \ [\varphi(x,0_{\perp}) - \varphi(1,0_{\perp})] + (P_R - W_R) \ [\varphi(x,k_{\perp}) - \varphi(x,0_{\perp})]\}$$

• first term: usual $1/(1-x)_+$ distribution

• second term: singularity in P_R cancelled by W_R

Note: it works because terms in $\delta(1-x)$ cancel between the two vev's,

$$-W_R(x,k_\perp,\zeta)+\delta(1-x)\,\delta(k_\perp)\int dx'dk'_\perp W_R$$

and

$$+\delta(k_{\perp})\int dk'_{\perp}W_R(x,k'_{\perp},\zeta) - \delta(1-x)\,\delta(k_{\perp})\int dx'dk'_{\perp}W_R \quad .$$

• virtual correction to gauge link does not depend on y_{\perp} G. Korchemsky

V. Braun et al

▷ subtractions have (relatively) simple form in coordinate space

operator representation valid to all orders

 \triangleright one-loop counterterm gives extension for ${\sf k}_\perp \neq 0$ of the plus-distribution regularization

Conclusions

• Branching methods based on k_{\perp} -dependent u-pdfs and MEs useful for simulation of high-energy parton showers

▷ k⊥ shower Monte-Carlo gives good description of small-x multi-jet final states

• Extension of u-pdf's over whole phase space important to turn these Monte-Carlo's into general-purpose tools

 \triangleright special issues at x ~ 1 (and matching with small x) relevant for showering algorithm