



**The Abdus Salam  
International Centre for Theoretical Physics**



**1942-18**

**Sixth International Conference on Perspectives in Hadronic Physics**

*12 - 16 May 2008*

**Diffractive Hadroproduction of  $W^+$ ,  $W^-$  and  $Z^0$  bosons at high energies.**

M.B. Gay Ducati  
*High Energy Phenomenology Group  
GFPAE - IF - UFRGS  
Brazil*



# Diffraction Hadroproduction of $W^+$ , $W^-$ and $Z^0$ bosons at high energies (\*)

Maria Beatriz Gay Ducati

High Energy Phenomenology Group  
GFP AE - IF – UFRGS, Porto Alegre  
beatriz.gay@ufrgs.br  
www.if.ufrgs.br/gfpae

(\*) M. B. Gay Ducati, M. M. Machado, M. V. T. Machado, PRD 75, 114013 (2007)



# Outline

---



- Diffractive Scattering
- Ingelman-Schlein Model
- Inclusive Cross Section
- Diffractive Cross Section
- Multiple Pomeron Corrections – Gap Survival Probability (GSP)
  - Khoze – Martin – Ryskin (KMR)
  - Gotsman – Levin – Maor (GLM)
- Tevatron Results
- LHC Prediction



# This work



- Results from a phenomenological analysis of W and Z hard diffractive hadroproduction at high energies
- Use of Regge factorization approach
- Consider recent diffractive parton density functions extracted by the H1 Collaboration at DESY-HERA
- Multiple Pomeron exchange corrections considering gap survival probability factor
- Ratio of diffractive to non-diffractive boson production is in good agreement with the CDF and D0 data on central region
- Prediction for the future measurements at the LHC



# Motivations




- Study of inclusive and diffractive cross section:
  - charged gauge boson  $W^+$  and  $W^-$   $\longrightarrow p + \bar{p} \rightarrow p + W(\rightarrow e\nu)X$
  - neutral gauge boson  $Z^0$   $\longrightarrow p + \bar{p} \rightarrow p + Z^0(\rightarrow e^+e^-)X$
- Study of Pomeron trajectory  $\longrightarrow$  phenomenology describes the diffractive scattering
- Study of hard diffractive process  $\longrightarrow$  Ingelman-Schlein model
- Investigation of the effects from multiple Pomeron scattering in the central region  $\longrightarrow$  gap survival probability factor (GSP)
- Analysis using recent parametrization for Pomeron structure function

$$F_2^{D(3)}(x_{IP}, \beta, Q^2) \longrightarrow \text{H1 Collaboration}$$



# Introduction



- Diffractive processes are a way of amplifying the physics program at proton colliders
- Inclusion of new channels searching for New Physics
- Investigation of these reactions gives important information on the structure of hadrons and their interaction mechanisms
- Diffractive production of massive electroweak bosons allows the study of the interplay of the small- and large-distance dynamics within QCD
- In boson hadroproduction, single diffractive dissociation can occur characterized by the existence of large rapidity gap  IP exchange



# General Aspects

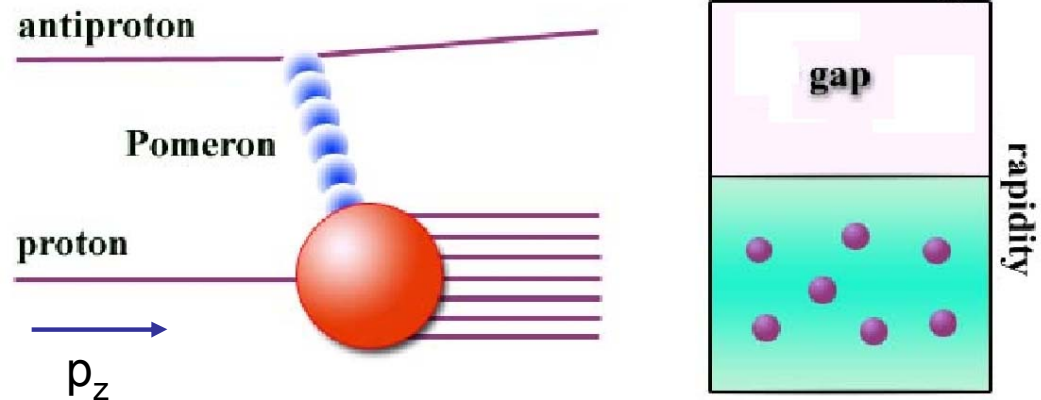


- Expected that unitarity effects at high energies affect the results of diffractive cross sections
- Multiple-Pomeron contributions reduce the diffractive cross section
- Dependence on the particular hard process
- Tevatron energies ( $\sqrt{s}=1.8\text{TeV}$ )  $\longrightarrow$  suppression is in the range 0.05-0.2
- For LHC energy ( $\sqrt{s}=14\text{TeV}$ )  $\longrightarrow$  suppression is in the range 0.08-0.1
- Adequate treatment of the multiple scattering effect is crucial for the reliability of theoretical predictions of the cross sections for diffractive processes

- Discovered at DESY (HERA) collider (H1 and Zeus Collaboration)
- Rapidity ( $y$ ) gaps  $\longrightarrow$  no particle production

$$y = \frac{1}{2} \ln \left| \frac{E + p_z}{E - p_z} \right|$$

$p_z$  proton momentum

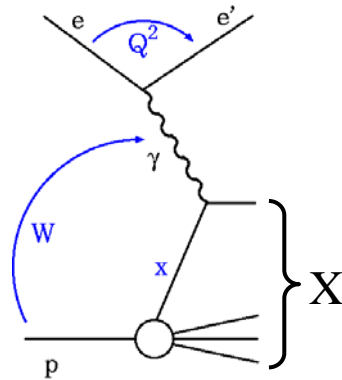


- Final state with same quantum numbers of initial state
- **Pomeron**  $\longrightarrow$  exchange of vacuum quantum numbers
- $M_W = 80 \text{ GeV}$ ,  $M_Z = 90.1 \text{ GeV}$

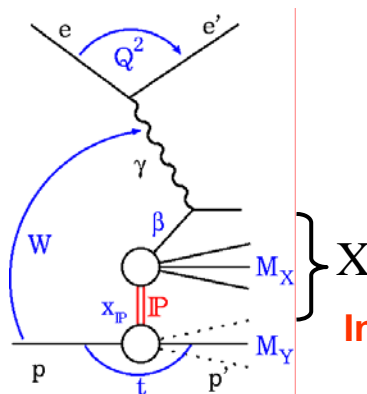


- Diffractive Deep Inelastic Scattering (DDIS) contributes substantially to the cross section

- (~ 10% of visible low-x events)



Inclusive DIS:  
Probes partonic structure of the proton



Diffractive DIS:  
Probes structure of the exchanged color singlet

**Ingelman-Schlein model**

- $Q^2$ : 4-momentum exchange
- $W$ :  $\gamma$  p centre of mass energy
- $x$ : fraction of p momentum carried by the struck quark
- $x_{IP}$ : fraction of p momentum carried by the Pomeron (IP)

$$x_{IP} = \frac{q \cdot (p - p')}{q \cdot p} \approx \frac{Q^2 + M_X^2}{Q^2 + W^2}$$

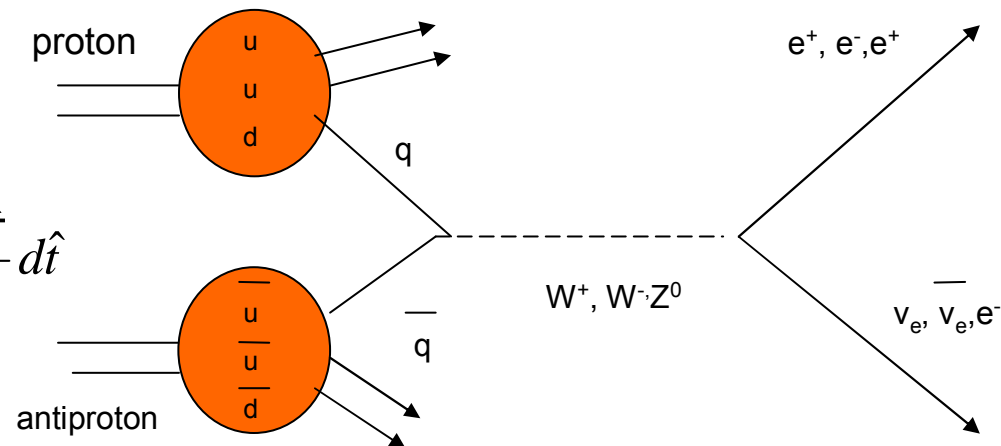
- $\beta$ : fraction of IP momentum carried by the struck quark

$$\beta = \frac{Q^2}{2q \cdot (p - p')} \approx \frac{Q^2}{Q^2 + M_X^2} = \frac{x}{x_{IP}}$$

- Hard diffractive process, considering the Ingelman-Schlein model
- Pomeron structure (quark and gluon content) is probed
- Cross section for a process in which partons of two hadrons (A and B) interact to produce a massive electroweak boson

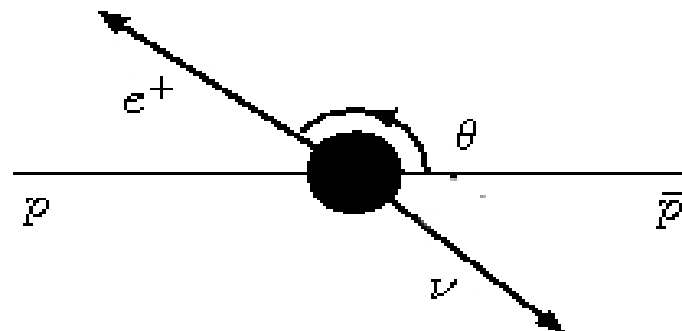
$$A + B \rightarrow (W^\pm / Z^0) + X$$

$$d\sigma = \sum_{a,b} \int dx_a \int dx_b f_{a/p}(x_a) f_{b/\bar{p}}(x_b) \frac{d\hat{\sigma}}{d\hat{t}} d\hat{t}$$



- $x_a$  and  $x_b$  are the **momentum fraction of nucleons** carried by the partons
- $f_{i/h}$  is the parton distribution function (PDF) of a parton of flavor  $i = a, b$  in the hadron  $h = A, B$

- $d\hat{\sigma}/d\hat{t}$  gives the elementary cross section of the corresponding subprocess
- The cross section is the usual leading-order QCD procedure to obtain the non-diffractive cross section
- Next-to-leading-order contributions are not essential, since corrections to W and Z production are small
- High energies ( $m_p \ll E$ ) pseudo-rapidity  $\rightarrow \eta = -\ln \operatorname{tg} \frac{\theta}{2}$
- $\theta$  is the electron scattering angle related to the proton beam direction



- Total Energy  $\rightarrow E_e = \frac{\sqrt{s}}{4} [x_a(1 + \cos \theta) + x_b(1 - \cos \theta)]$
- Longitudinal Energy  $\rightarrow E_L = \frac{\sqrt{s}}{4} [x_a(1 + \cos \theta) - x_b(1 - \cos \theta)]$
- Transversal Energy  $\rightarrow E_T = \frac{M_W}{2} \sin \theta$
- Mandelstan variables of the process

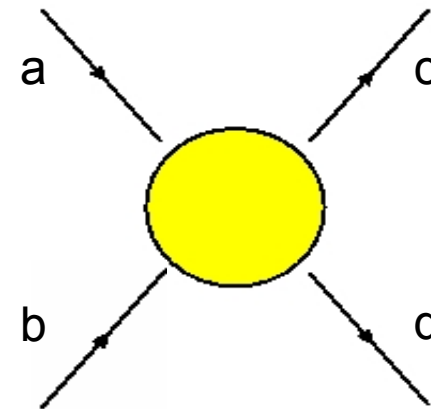
$$\hat{t} = (p_c - p_a)^2 = -\frac{\hat{s}}{2} (1 - \cos \theta)$$

$$\hat{u} = (p_c - p_b)^2 = -\frac{\hat{s}}{2} (1 + \cos \theta)$$

$$\hat{s} = (p_a + p_b)^2 = M_W^2$$

$$\cos \theta = \pm \frac{\sqrt{A^2 - 1}}{A}$$

$$A = M_W / 2E_T$$





# W- inclusive cross section




- General cross section for W and Z

$$\frac{d\sigma}{dx_a dx_b} = \sum_{a,b} \int dx_a f_{a/p}(x_a, \mu^2) f_{b/\bar{p}}(x_b, \mu^2) \frac{d\hat{\sigma}(p\bar{p} \rightarrow [W/Z]X)}{d\hat{t}}$$

- W - inclusive cross section

$$\frac{d\sigma}{d\eta_{e^-}} = \sum_{a,b} \int dE_T f_{a/p}(x_a) f_{b/\bar{p}}(x_b) \left[ \frac{V_{ab}^2 G_F^2}{6s\Gamma_W M_W} \right] \frac{\hat{u}^2}{\sqrt{A^2 - 1}}$$

- $\mu^2 = M_W^2$  hard scale in which the PDFs are evolved
- Total decay width   $\Gamma_W = 2.06 \text{ GeV}$
- Fermi Constant  $G_F = 1.166 \times 10^{-5} \text{ GeV}^{-2}$
- $V_{ab}$  is the Matrix CKM element



# $W^+$ inclusive cross section



- $W^+$  inclusive cross section

$$\frac{d\sigma}{d\eta_{e^+}} = \sum_{a,b} \int dE_T f_{a/p}(x_a) f_{b/\bar{p}}(x_b) \left[ \frac{V_{ab}^2 G_F^2}{6s\Gamma_W M_W} \right] \frac{\hat{t}^2}{\sqrt{A^2 - 1}}$$

- $\mu^2 = M_W^2$        $\hat{t} = -E_T M_W \left[ A + \sqrt{(A^2 - 1)} \right]$
- Total decay width  $\longrightarrow \Gamma_W = 2.06 \text{ GeV}$
- $G_F = 1.166 \times 10^{-5} \text{ GeV}^{-2}$ ,  $V_{ab}$  is the CKM Matrix element
- $W^+$   $\longrightarrow$  dependence in t channel
- $W^-$   $\longrightarrow$  dependence in u channel



# W Diffractive cross sections



- W<sup>-</sup> diffractive cross section

$$\frac{d\sigma}{d\eta_{e^-}} = \sum_{a,b} \int dx_{IP} g(x_{IP}) \int dE_T f_{a/IP}(x_a) f_{b/\bar{p}}(x_b) \left[ \frac{V_{ab}^2 G_F^2}{6s\Gamma_W M_W} \right] \frac{\hat{u}^2}{\sqrt{A^2 - 1}}$$

- W<sup>+</sup> diffractive cross section

$$\frac{d\sigma}{d\eta_{e^+}} = \sum_{a,b} \int dx_{IP} g(x_{IP}) \int dE_T f_{a/IP}(x_a) f_{b/\bar{p}}(x_b) \left[ \frac{V_{ab}^2 G_F^2}{6s\Gamma_W M_W} \right] \frac{\hat{t}^2}{\sqrt{A^2 - 1}}$$

- $f_{a/IP}$  is the quark distribution in the IP  $\rightarrow$  parametrization of the IP structure function (H1)
- $g(x_{IP})$  is the IP flux integrated over  $t$



# Z<sup>0</sup> Diffractive cross sections



- Z<sup>0</sup> diffractive cross section

$$\sigma = \sum_{a,b} \int \frac{dx_{IP}}{x_{IP}} \int \frac{dx_b}{x_b} \int \frac{dx_a}{x_a} \bar{f}(x_{IP}) f_{a/IP}(x_a, \mu^2) f_{b/\bar{p}}(x_b, \mu^2) \left[ \frac{2\pi C_{ab}^Z G_F M_Z^2}{3\sqrt{2}s} \right] \frac{d\hat{\sigma}(ab \rightarrow ZX)}{d\hat{t}}$$

- $f_{a/IP}$  is the quark distribution in the IP  $\bar{f}(x_{IP}) = \int_{-\infty}^0 f_{IP/p}(x_{IP}, t) dt$
- $g(x_{IP})$  is the Pomeron flux integrated over t
- $C_{qq}^Z, 1/2 - 2|e_q| \sin^2 \theta_W + 4|e_q|^2 \sin^4 \theta_W$
- $\theta_W$  is the Weinberg or weak-mixing angle
- Same result of H1 with LO Pomeron structure function (STIRLING 96)





# Pomeron flux factor



- $x_{IP}$  dependence is parametrized using a flux factor

$$f_{IP/p}(x_{IP}, t) = A_{IP} \frac{e^{B_{IP}t}}{x_{IP}^{2\alpha_{IP}(t)-1}}$$

- IP trajectory is assumed to be linear  $\longrightarrow \alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t$

- $B_{IP}$ ,  $\alpha'_{IP}$   
their uncertainties

obtained from the fits to H1 forward proton spectrometer (FPS) data

Normalization parameter  $x_{IP}$  is chosen such that  $x_{IP} \cdot \int_{t_{cut}}^{t_{min}} f_{IP/p} dt = 1$  at  $x_{IP} = 0.003$

- $|t_{min}| \approx m_p^2 x_{IP} / (1 - x_{IP})$  is the proton mass
- $|t_{cut}| = 1.0 \text{ GeV}^2$  is the limit of the measurement



# Pomeron structure function



- Pomeron structure function has been modeled in terms of a light flavor singlet distribution  $\Sigma(z)$
- Consists of u, d and s quarks and antiquarks and a gluon distribution  $g(z)$
- $z$  is the longitudinal momentum fraction of the parton entering the hard subprocess with respect of the diffractive exchange
- ( $z = \beta$ ) for the lowest order quark-parton model process and  $0 < \beta < z$  for higher order processes
- Quark singlet and gluon distributions are parametrized at  $Q_0^2$

$$zf_{i/IP}(z, Q_0^2) = A_i z^{B_i} (1-z)^{C_i} \exp\left[-\frac{0.01}{(1-z)}\right]$$



# Pomeron structure function



- Experimental determination of the diffractive PDFs involves the following cuts

$$\beta < 0.8, M_x > 2\text{GeV}; Q^2 < 8.5\text{GeV}^2$$

- Quark singlet distribution, data requires inclusion of parameters  $A_q$ ,  $B_q$  and  $C_q$
- Gluon density is weakly constrained by data which are found to be insensitive to the  $B_g$  parameter
- **FIT A** - Gluon density is parametrized using only  $A_g$  and  $C_g$  parameters ( $Q_0^2 = 1.75 \text{ GeV}^2$ )
- This procedure is not sensitive to the gluon PDF and a new adjustment was done with  $C_g = 0$
- **FIT B** - Gluon density is a simple constant at the starting scale for evolution ( $Q_0^2 = 2.5 \text{ GeV}^2$ )



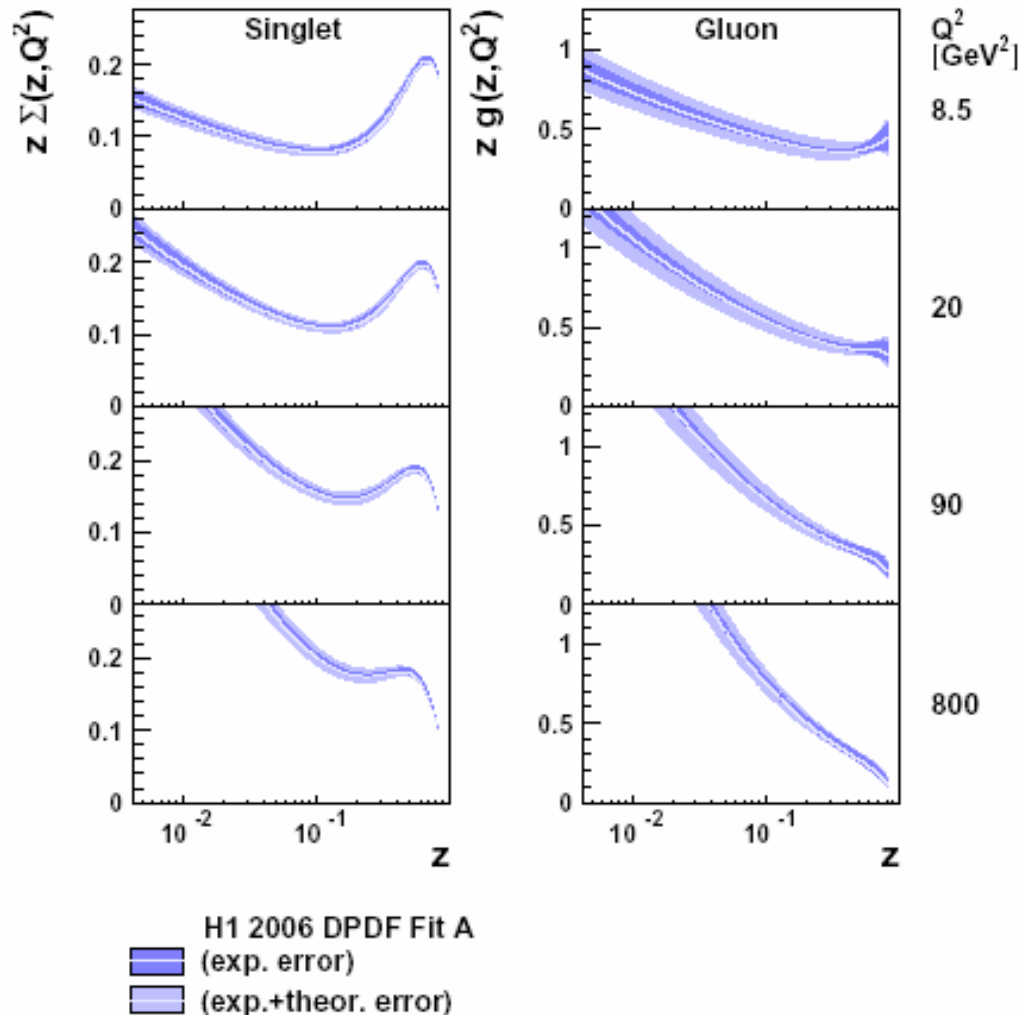
# Pomeron structure function



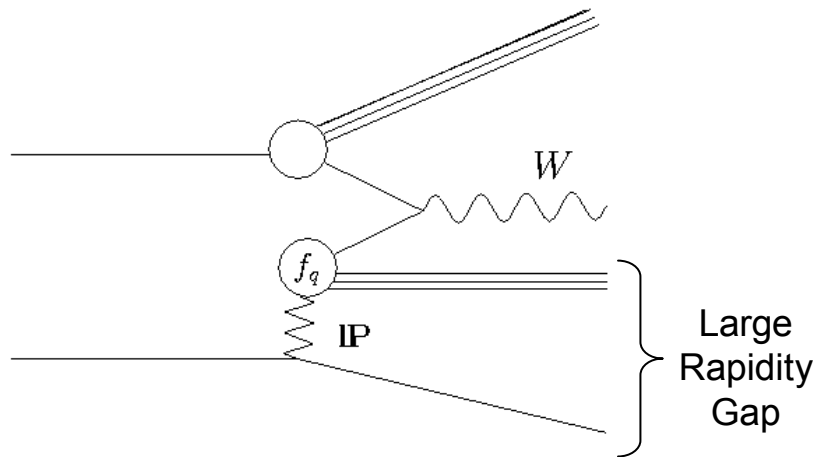
<i>Parameter</i>	<i>Value</i>
$\alpha'_{IP}$	$0.06^{+0.19}_{-0.06} GeV^{-2}$
$B_{IP}$	$5.5^{+2.0}_{-0.7} GeV^{-2}$
$\alpha_{IR}(0)$	$0.50 \pm 0.10$
$\alpha'_{IR}$	$0.3^{+0.6}_{-0.3} GeV^{-2}$
$B_{IR}$	$1.6^{+1.6}_{-0.4} GeV^{-2}$
$m_c$	$1.4 \pm 0.2 GeV$
$m_b$	$4.5 \pm 0.5 GeV$
$\alpha_8^{(5)}(M_Z^2)$	$0.118 \pm 0.002$

- Values of fixed parameters (masses) and their uncertainties, as used in the QCD fits.
- $\alpha'_{IP}$  and  $B_{IP}$  (strongly anti-correlated) are varied simultaneously to obtain the theoretical errors on the fits (as well as  $\alpha'_{IR}$  and  $B_{IR}$ ).
- Remaining parameters are varied independently.
- Theoretical uncertainties on the free parameters of the fit are sensitive to the variation of the parametrization scale  $Q_0^2$

DESY – 06-049 May 2006



- Total quark singlet and gluon distributions obtained from NLO QCD H1. DPDF Fit A,
- Range  $0.0043 < z < 0,8$ , corresponding approximately to that of measurement.
- Central lines are surrounded by inner errors bands corresponding to the experimental uncertainties and outer error bands corresponding to the experimental and theoretical uncertainties
- In this work, we use FIT A.
- Similar results are obtained with FIT B



- Currently a subject of intense theoretical and experimental interest
- GAP – region of angular phase space devoid of particles
- Survival probability – fulfilling of the gap by hadrons produced in interactions of remanescant particles

$$\langle |S| \rangle^2 = \frac{\int d^2b |A(s,b)|^2 P^s(s,b)}{\int d^2b |A(s,b)|^2}$$

- $A(s,b)$  is the amplitude (in the parameter space) of the particular process of interest at center-of-mass energy  $\sqrt{s}$
- $P^s(s,b)$  is the probability that no inelastic interaction occurs between scattered hadrons



# KMR - GSP



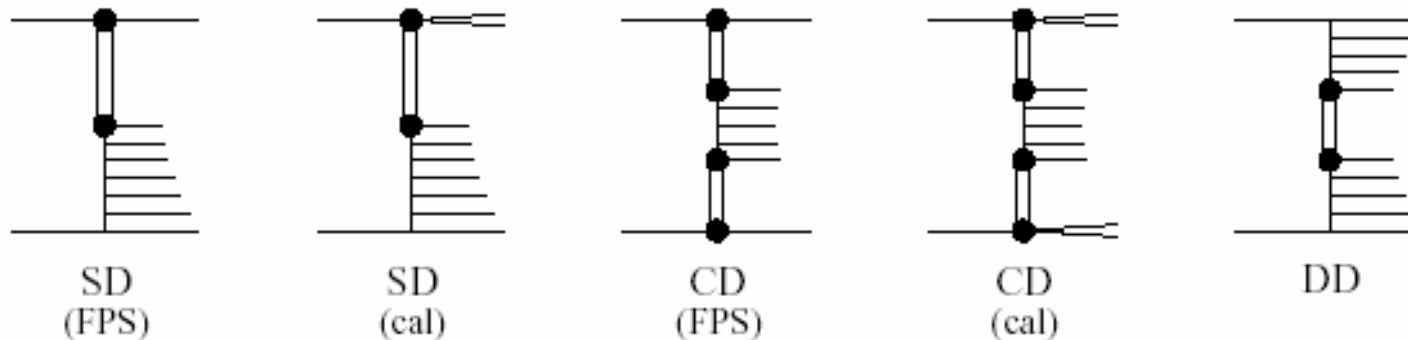
(\*) Khoze-Martin-Ryskin Eur. Phys. J. C. 26 229 (2002)

- The survival probability of the rapidity gaps (associated with the Pomeron, represented by the double vertical line)

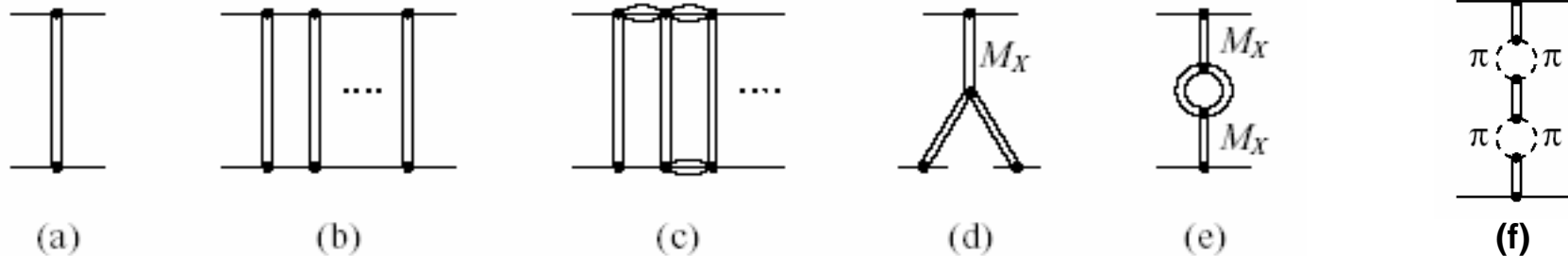
- Calculated

- \* single diffraction (SD)
- \* central diffraction (CD)
- \* double diffraction (DD)

- FPS or cal denotes “forward photon spectrometer” or “calorimeter”, and corresponds to the detection of isolated protons, or to events where the leading baryon is either a proton or a  $N^*$  (symbolically, two lines emerging from the vertex)



- $t$  dependence of elastic pp differential cross section in the form  $\exp(Bt)$
- pion-loop insertions in the Pomeron trajectory
- non-exponential form of the proton-Pomeron vertex  $\beta(t)$
- absorptive corrections, associated with eikonalization, which lead to a dip in  $d\sigma/dt$  at  $|t| \sim 1 \text{ GeV}^2$ , whose position moves to smaller  $|t|$  as the collider energy increases



- (a) Pomeron exchange contribution;
- (b-e) are unitarity corrections to the pp elastic amplitude.
- (f) is a two pion-loop insertion in the Pomeron trajectory





# KMR model

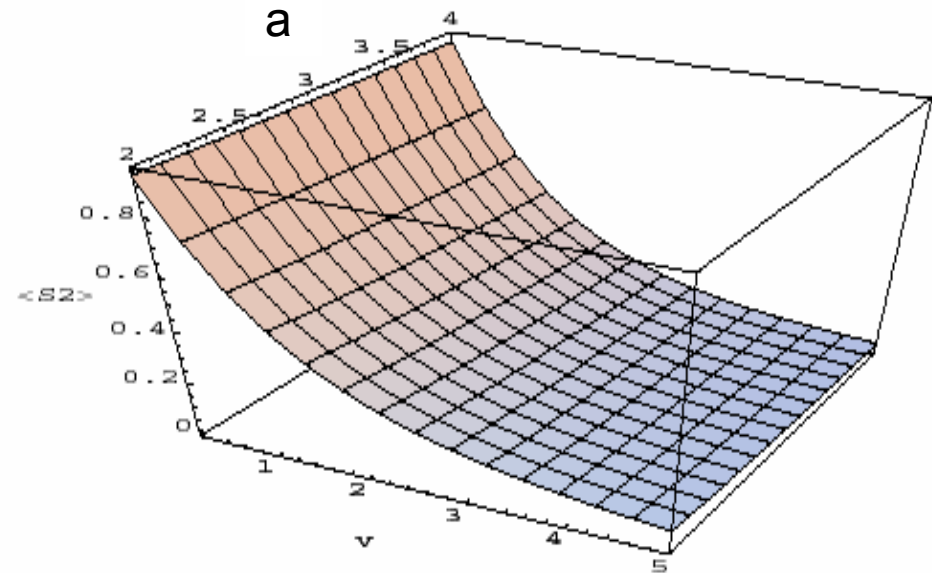
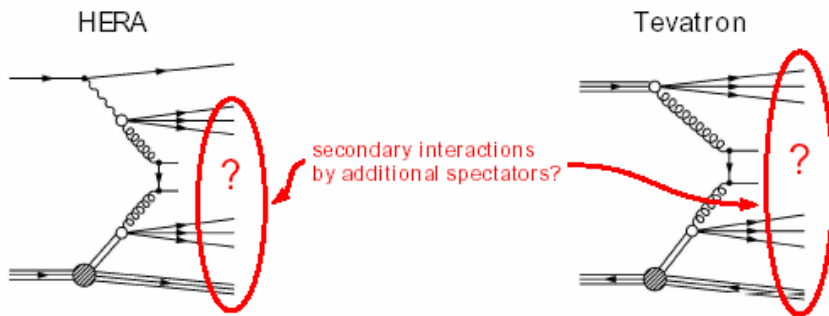


- GSP KMR values

$\sqrt{s}$ (TeV)	$2b$ (GeV <sup>-2</sup> )	Survival probability $S^2$ for:				
		SD (FPS)	SD (cal)	CD (FPS)	CD (cal)	DD
0.54	4.0	0.14	0.13	0.07	0.06	0.20
	5.5	0.20	0.18	0.11	0.09	0.26
	7.58	0.27	0.25	0.16	0.14	0.34
1.8	4.0	0.10	0.09	0.05	0.04	0.15
	5.5	0.15	0.14	0.08	0.06	0.21
	8.47	0.24	0.23	0.14	0.12	0.32
14	4.0	0.06	0.05	0.02	0.02	0.10
	5.5	0.09	0.09	0.04	0.03	0.15
	10.07	0.21	0.20	0.11	0.09	0.29

- GSP considering multiple channels

(\*) Gotsman-Levin-Maor PLB 438 229 (1998)



- Suppression due to secondary interactions by additional spectators hadrons

$$\langle |S|^2 \rangle = \frac{\int |A(s,b)|^2 e^{-\Omega(s,b)} d^2b}{\int |A(s,b)|^2 d^2b}$$

- Survival probability as a function of  $\nu(s) = \Omega(s, b=0)$  ( $\Omega$  is the opacity or optic density of interaction of incident hadrons and  $a$ , where  $a$  is the ratio of the radius in soft and hard interactions)

$$a = R_s / R_h$$



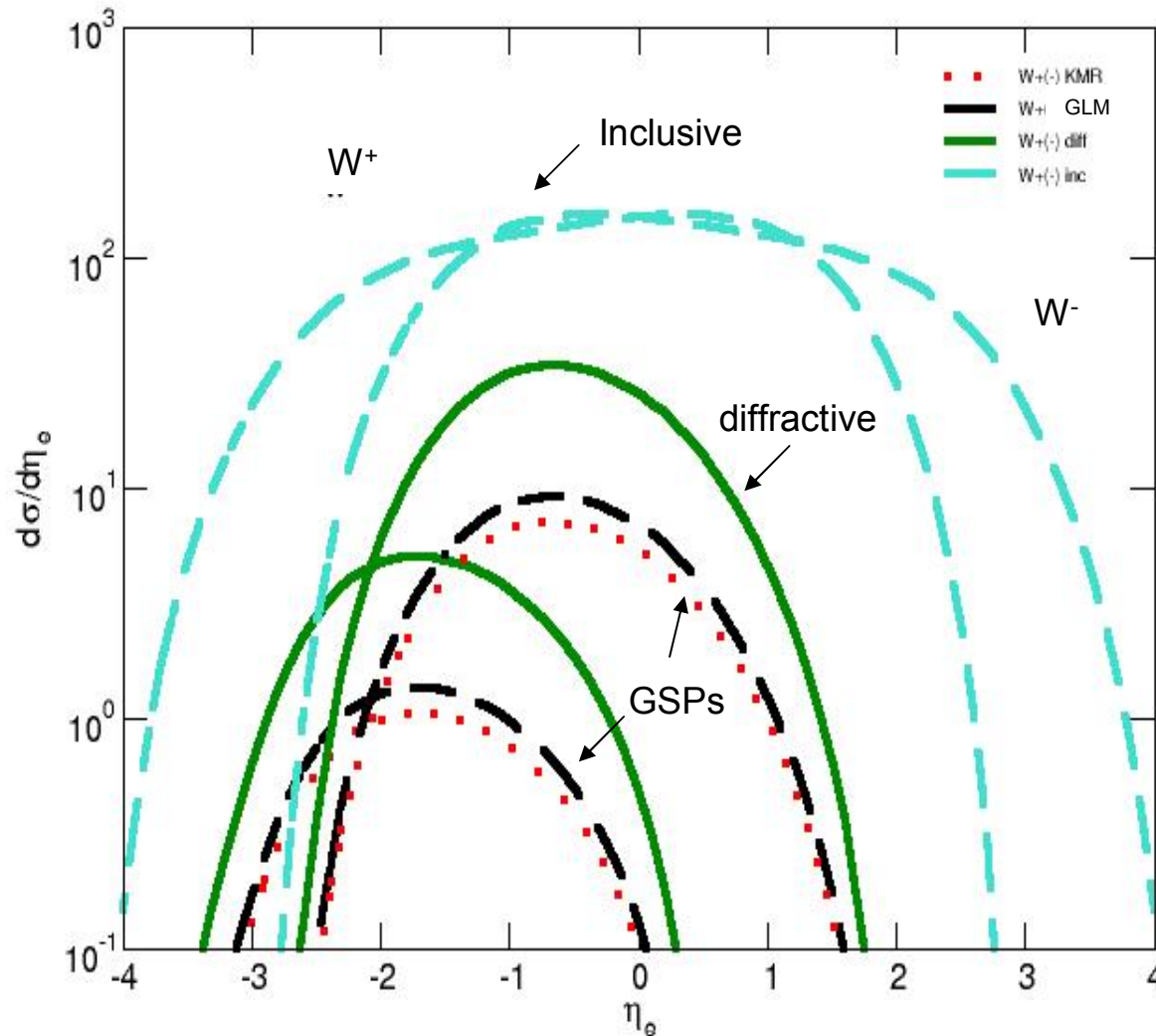
# GLM model



- Eikonal model originally conceived so as to explain the exceptionally mild energy dependence of soft diffractive cross sections.
- Considers that the s-channel unitarization enforced by the eikonal model operates on a diffractive amplitude in a different way than it does on the elastic amplitude
- We consider the single-channel eikonal approach
- Case where the soft input is obtained directly from the measured values of  $\sigma_{\text{tot}}$ ,  $\sigma_{\text{el}}$  and hard radius  $R_H$

$\langle  S  \rangle^2$	GLM
Tevatron	0.126
LHC	0.081

## Tevatron



$$R = \frac{\int_{-\eta}^{\eta} \sigma_{diff}^{W^+} + \sigma_{diff}^{W^-}}{\int_{-\eta}^{\eta} \sigma_{inc}^{W^+} + \sigma_{inc}^{W^-}}$$

• Ranges

$$\left\{ \begin{array}{l} |\eta_e| < 1.1 \\ 1.5 < |\eta_e| < 2.5 \end{array} \right.$$



# W<sup>+</sup>, W<sup>-</sup> and Z<sup>0</sup> Ratios



	Pseudo-rapidity	Data (%)	R(%)	
1.8 TeV	$ \eta_e  < 1.1$	$1.15 \pm 0.55$	$0.715 \pm 0.045$	CDF
		$1.08 \pm 0.25$	$0.715 \pm 0.045$	
	$1.5 <  \eta_e  < 2.5$	$0.64 \pm 0.24$	$1.7 \pm 0.875$	D0
	Total $W \rightarrow e\nu$	$0.89 \pm 0.25$	$0.735 \pm 0.055$	
	Total $Z \rightarrow e^+e^- (*)$	$1.44 \pm 0.80$	$0.71 \pm 0.05$	
14 TeV	$ \eta_e  < 1.1$	...	$31.1 \pm 1.6$	LHC
	Total $Z \rightarrow e^+e^- (*)$	...	$30.26 \pm 1.41$	

\*  $|\eta| < 1.1$

Average of KMR and GLM predictions

- Tevatron, without GSP – 7.2 %



# Other GSPs results



- Diffractive W production

	Pseudo-rapidity	Model	R (%)	
1.8 TeV	$ \eta_e  < 1.1$	DGM 1 – 27.6	$2.10 \pm 0.065$	} 3 ch
	$ \eta_e  < 1.1$	DGM 2 – 32.6	$2.48 \pm 0.129$	
	$ \eta_e  < 1.1$	BH – 20.8	$1.12 \pm 0.075$	
	$ \eta_e  < 1.1$	KMR – 15.0	$0.67 \pm 0.065$	} 1 ch
	$ \eta_e  < 1.1$	GLM – 12.6	$0.76 \pm 0.055$	

DGM – Dynamical Mass Gluon  $\rightarrow$  Luna (2006)

BH – Block Halzen model  $\rightarrow$  (2002)

GLM – Gotsman Levin Maor  $\rightarrow$  (2001)



# Conclusions

---



- Analysis of W and Z diffractive hadroproduction process and central rapidity distributions of produced leptons
- Using new Pomeron diffractive parton distributions (H1 Collaboration – DESY – HERA) and theoretical estimates for gap survival factor
- Very good agreement with experiment (D0 and CDF, Tevatron)
- Improvement of data description using gap survival probability
- Important subject to verify future IP PDF's
- Estimates to be compared at LHC