



*The Abdus Salam  
International Centre for Theoretical Physics*



**1942-38**

**Sixth International Conference on Perspectives in Hadronic Physics**

*12 - 16 May 2008*

**Parity violation and strangeness content of the nucleon.**

F.E. Maas  
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# Parity Violating Electron Scattering and Strangeness in the Nucleon

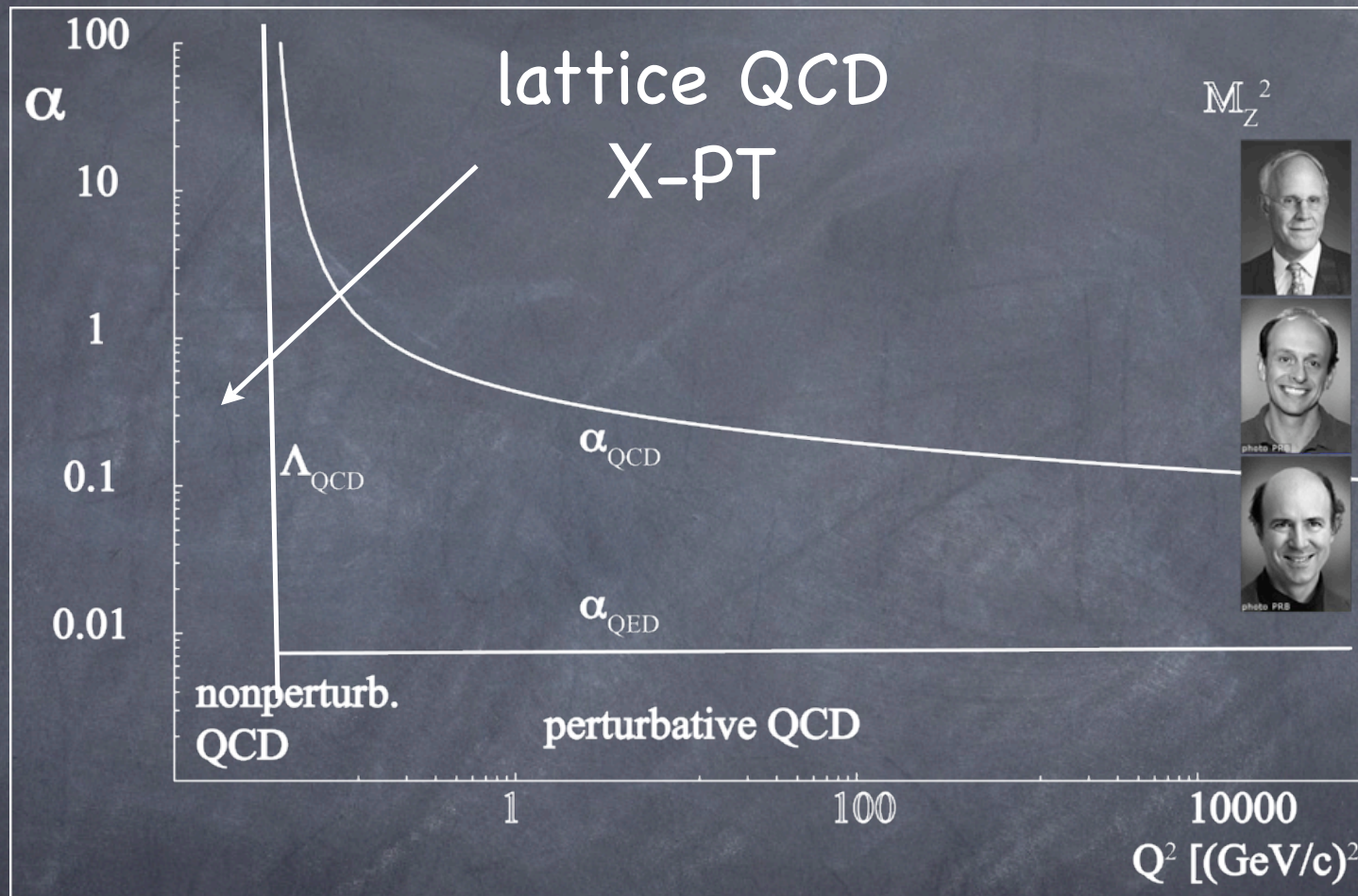
Frank E. Maas  
GSI/Mainz University

Sixth International Conference  
on  
Perspectives in Hadronic Physics  
Abdus Salam International Centre for Theoretical Physics  
Miramare-Trieste  
15.05.2008

# Outline

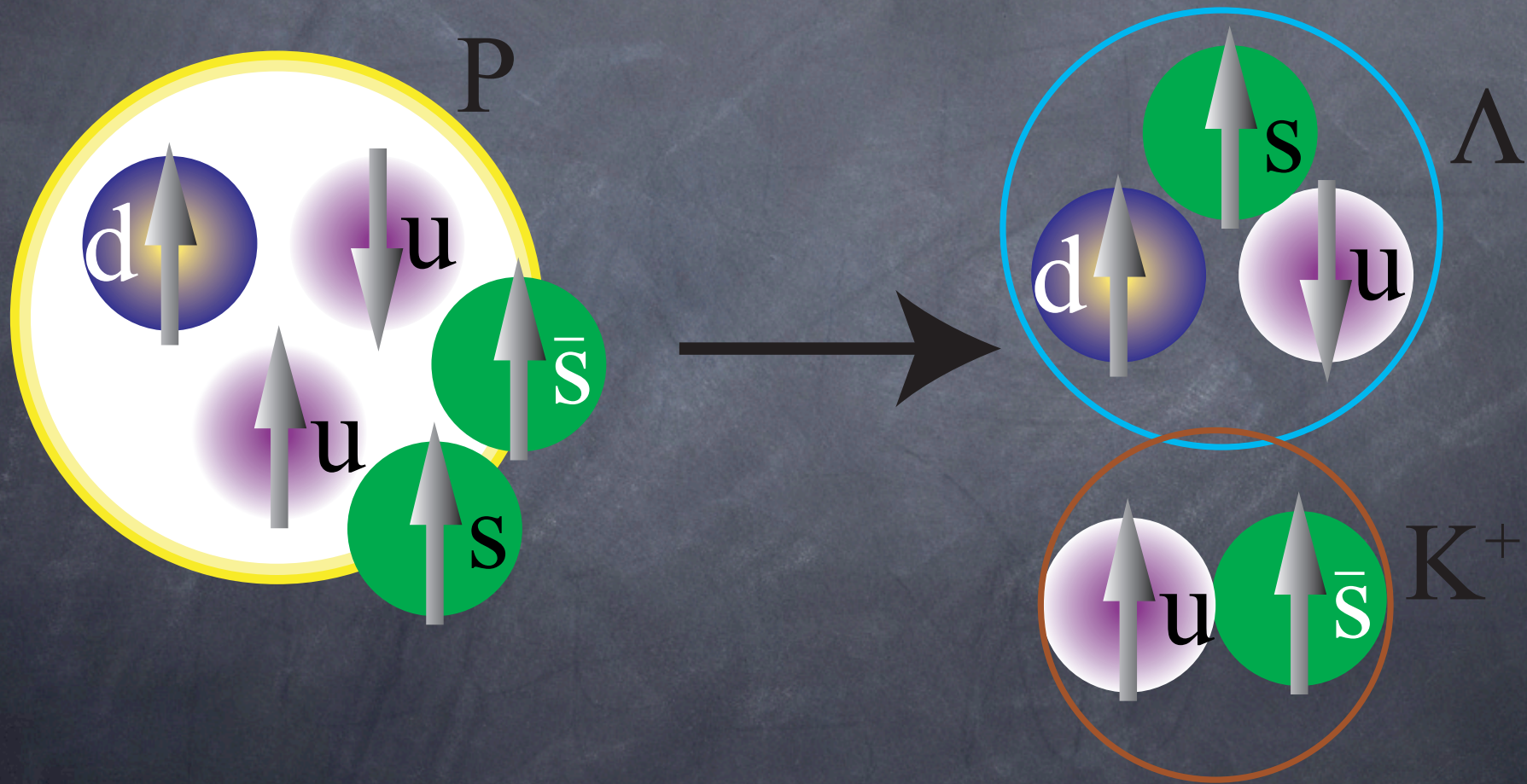
- Nonperturbative QCD: Strangeness
- weak form factors  $\rightarrow$  asymmetries in ep-scattering
- strangeness parity experiments: A4 in Mainz

# QCD-Renormalisation à la QED

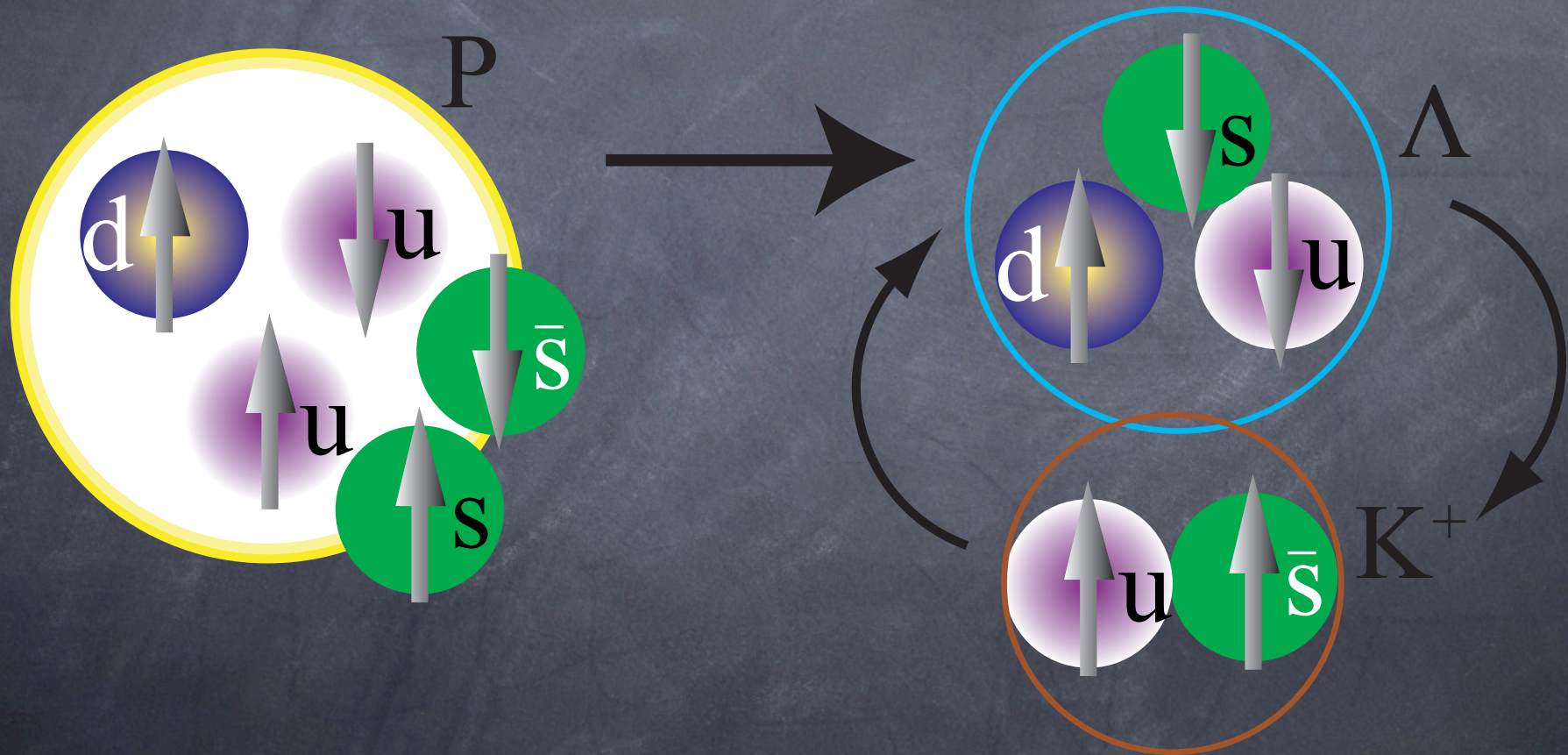


$$m_u, m_d \ll m_s \approx \Lambda_{\text{QCD}} \ll m_c, m_b, m_t$$

# Contribution to CHARGE distribution ( $G_E^S$ )



# Contribution to MAGNETISATION distribution ( $G_M^S$ )



# Strangeness in the Nucleon

Vacuum	$\langle 0   \bar{s}s   0 \rangle$	$(0.8 \pm 0.1)$ $\langle 0   \bar{q}q   0 \rangle$	QCD sum rules
Momentum	$\int x(\bar{s}s) dx$	2-4%	DIS U, $\mu$ , e
Mass	$m_s \langle N   \bar{s}s   N \rangle$	220 MeV	$\pi N$ -scatt. $\Sigma_{\pi N}$ -Term
Spin	$\langle N   \bar{s} \gamma_\mu \gamma^5 s   N \rangle$	- 10 %	pol. DIS
EM FF $G_E^s, G_M^s$	$\langle N   \bar{s} \gamma_\mu s   N \rangle$	???	PV electron scattering

# Theoretical Estimates of Strangeness

- Dispersion Theory: Vector Meson Dominance

Jaffe, Drechsel, Musolf, Hammer

- Quark Models

Jido and Weise  $\mu_s = +0.16\mu_N$

Zou and Riska:  $\mu_s > 0$ , s in ground state, uud: L = 1

$p \rightarrow K^+ + \Lambda$ ,  $p \rightarrow \pi^+ + n$  ( $G_E^s, G_M^s < 0$ )

Skyrme-Models (Baryon as Soliton of Mesons)

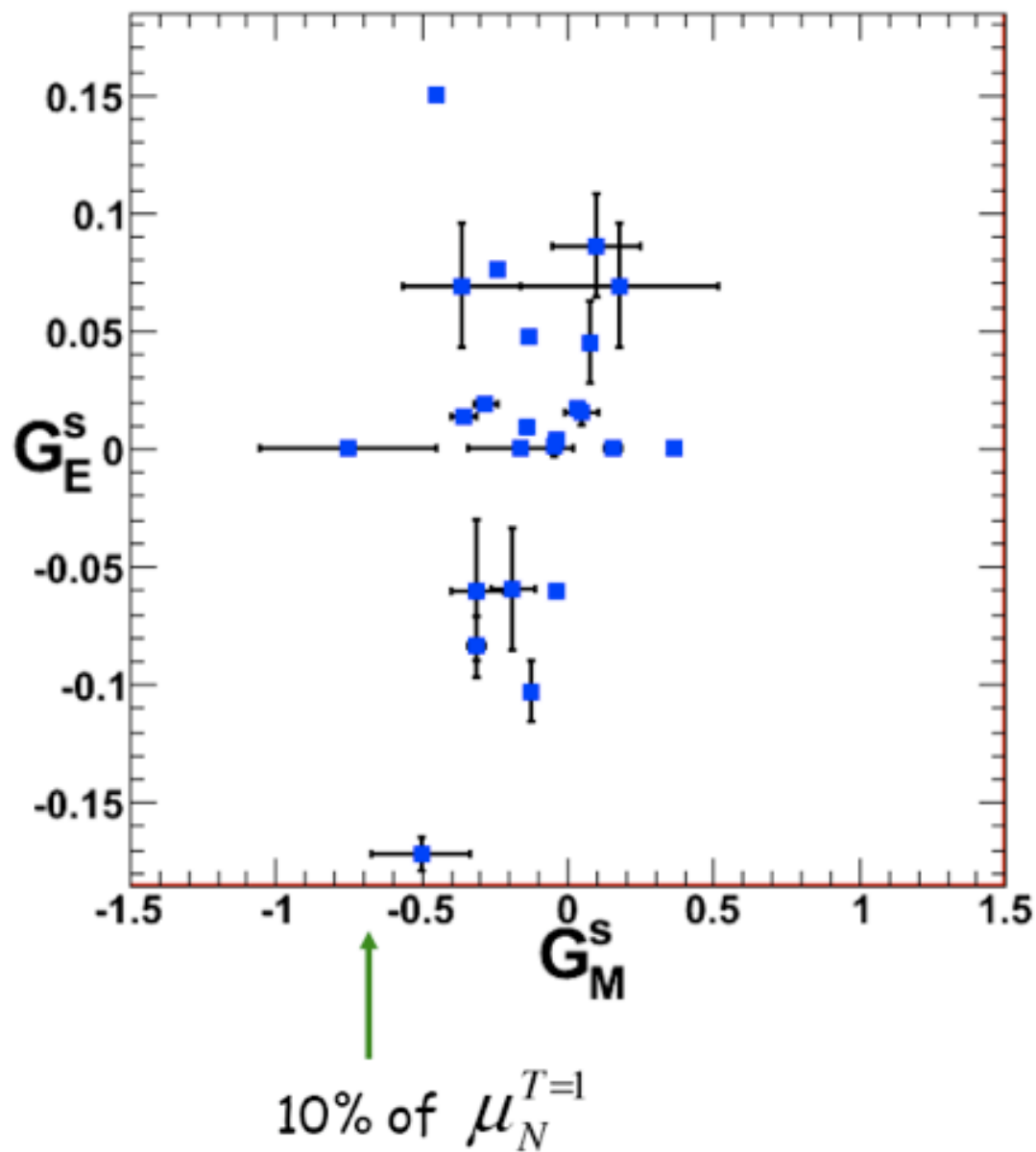
Chiral Perturbation Theory

Lattice Gauge Theory:

$$G_M^s(0) = \mu_s = -0.051 \pm 0.021 \mu_N$$



# Strangeness Models



Define leading moments of form factors:

$$\mu_s = G_M^s(Q^2 = 0)$$

(strange magnetic moment)

$$\rho_s = \left. \frac{\partial G_E^s}{\partial \tau} \right|_{\tau=0}$$

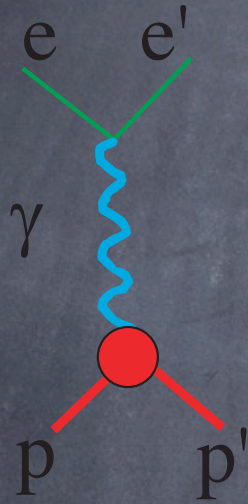
(strange radius)

$$\tau = \frac{Q^2}{4M^2}$$

*note: caveats...*

# Born Approximation

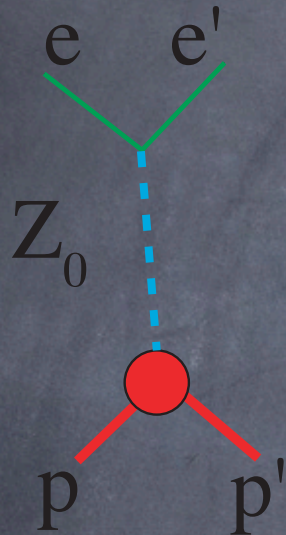
## Elastic Scattering



$$\begin{aligned}\sigma &\sim \mathcal{M} \mathcal{M}^* \\ &\sim \left( \dot{j}_\mu \frac{1}{Q^2} J^\mu \right) \left( \dot{j}_\mu \frac{1}{Q^2} J^\mu \right)^* \\ \dot{j}_\mu &\sim \bar{e} \gamma_\mu e \text{ Vector Current}\end{aligned}$$

$$\begin{aligned}J_\gamma^\mu &\sim \left\langle N \left| q^u \bar{u} \gamma_\mu u + q^d \bar{d} \gamma_\mu d + q^s \bar{s} \gamma_\mu s \right| N' \right\rangle \\ &= \bar{\mathcal{P}} \left[ \gamma^\mu F_1 - i \sigma^{\mu\nu} q_\nu \frac{\kappa_p}{2M_N} F_2 \right] \mathcal{P}\end{aligned}$$

# Born Approximation Elastic Scattering



$$\tilde{q}_V^d = \tau_3 - 2q^d \sin^2(\theta_W)$$

weak vector charge

$$\begin{aligned} \tilde{J}_Z^\mu &\sim \left\langle N \left| \tilde{q}^u \bar{u} \gamma_\mu u + \tilde{q}^d \bar{d} \gamma_\mu d + \tilde{q}^s \bar{s} \gamma_\mu s \right| N' \right\rangle \\ &= \bar{\mathcal{P}} \left[ \gamma^\mu \tilde{F}_1 - i \sigma^{\mu\nu} q_\nu \frac{\kappa_p}{2M_N} \tilde{F}_2 \right] \mathcal{P} \end{aligned}$$

# Strangeness Contribution to electromagnetic Form Factors

Isospin

Universality

EW mixing

$$F_1^p = \frac{2}{3}F^u_1 - \frac{1}{3}F^d_1 - \frac{1}{3}F^s_1$$

$$F_1^n = \frac{2}{3}F^d_1 - \frac{1}{3}F^u_1 - \frac{1}{3}F^s_1$$

$$\tilde{F}_1^p = \left(\frac{1}{4} - \frac{2}{3}\sin^2\theta_W\right)F^u_1 - \left(\frac{1}{4} - \frac{1}{3}\sin^2\theta_W\right)F^d_1 - \left(\frac{1}{4} - \frac{1}{3}\sin^2\theta_W\right)F^s_1$$

$$\tilde{F}_1^n = \frac{1}{4}(F^u_1 - F^d_1) - \frac{1}{4}F^s_1 - \sin^2\theta_W\left(\frac{2}{3}F^u_1 - \frac{1}{3}F^d_1 - \frac{1}{3}F^s_1\right)$$

$$\tilde{F}_1^p = \frac{1}{4}(F_1^p - F_1^n) - \sin^2\theta_W F_1^p - \frac{1}{4}F^s_1$$

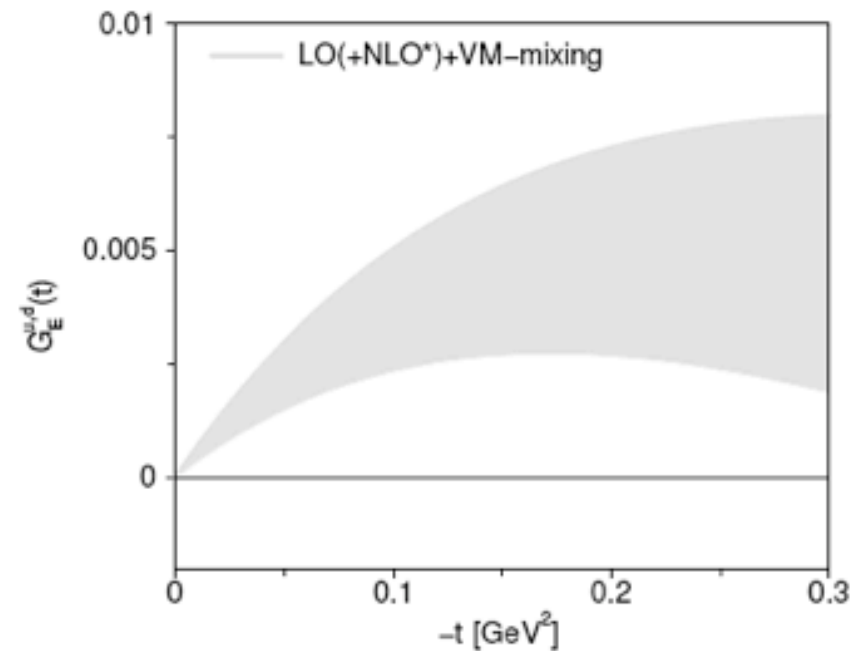
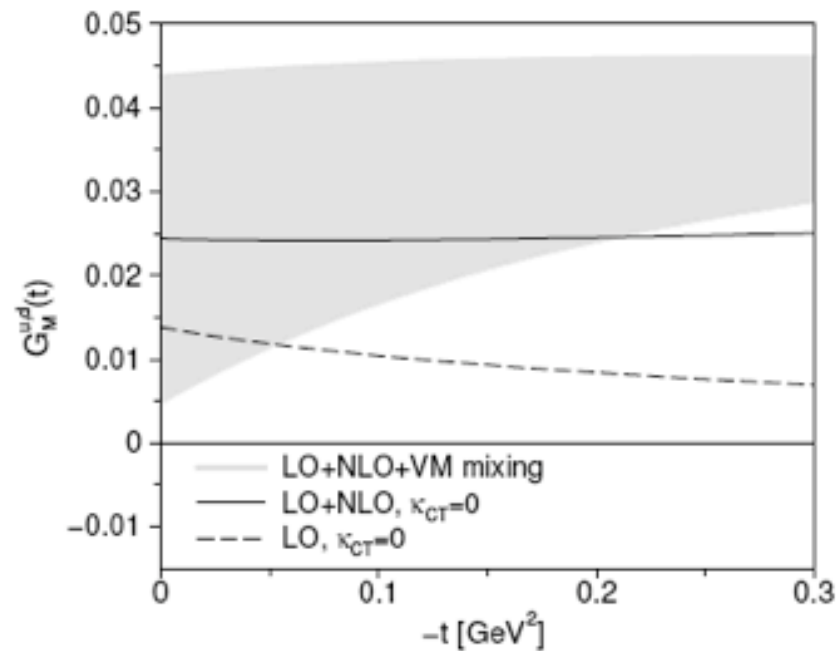
electric ( $G_E$ ) and magnetic ( $G_M$ )  
form factor

$$G_E = F_1 - \tau F_2$$

$$G_M = F_1 + F_2$$

# Isospin breaking in the vector current of the nucleon

0. motivation
1. constituent quark model
  - ▷ *Dmitrašinović and Pollock, Phys. Rev. C52, 1061 (1995).*
  - ▷ *Miller, Phys. Rev. C57, 1492 (1998).*
2. light-cone meson-baryon model
  - ▷ *Ma, Phys. Lett. B408, 387 (1997).*
3. chiral perturbation theory
  - ▷ *Lewis and Moberg, Phys. Rev. D59, 073002 (1999).*
4. chiral perturbation theory with resonance saturation
  - ▷ *Kubis and Lewis, nucl-th/0605006 (2006).*



SAMPLE:  $G_M^s(-0.1 \text{ GeV}^2) = 0.37 \pm 0.20 \pm 0.26 \pm 0.07$   
 $G_M^{u,d}(-0.1 \text{ GeV}^2) = 0.02 \dots 0.05$

A4:  $\left[ G_E^s + 0.106 G_M^s \right](-0.108 \text{ GeV}^2) = 0.071 \pm 0.036$   
 $\left[ G_E^{u,d} + 0.106 G_M^{u,d} \right](-0.108 \text{ GeV}^2) = 0.004 \dots 0.010$

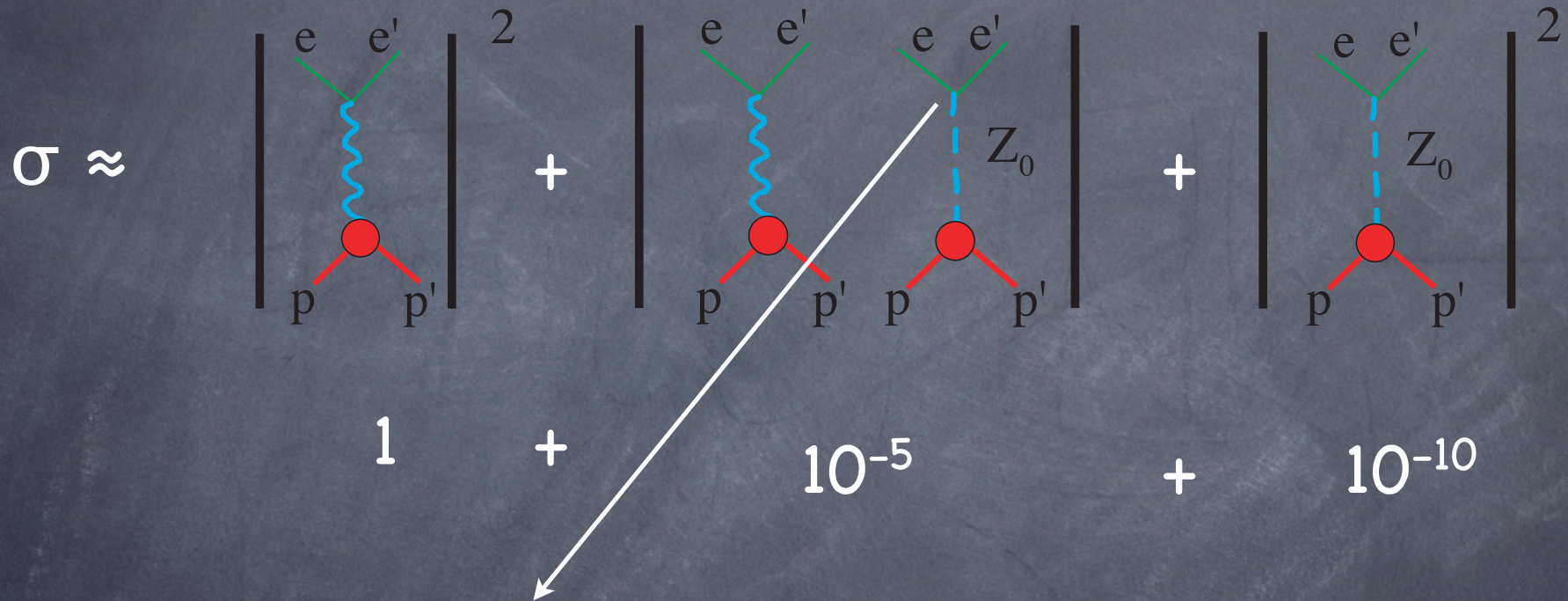
HAPPEX:  $\left[ G_E^s + 0.080 G_M^s \right](-0.099 \text{ GeV}^2) = 0.030 \pm 0.025 \pm 0.006 \pm 0.012$   
 $\left[ G_E^{u,d} + 0.080 G_M^{u,d} \right](-0.099 \text{ GeV}^2) = 0.004 \dots 0.009$

# Parity Violation in Electroweak Interaction

$$\sigma \approx \left| \begin{array}{c} e \quad e' \\ \diagdown \quad / \\ \text{---} \\ / \quad \diagdown \\ p \quad p' \end{array} \right|^2 + \left| \begin{array}{c} e \quad e' \quad e \quad e' \\ \diagdown \quad / \quad \diagdown \quad / \\ \text{---} \quad \text{---} \\ / \quad \diagdown \quad / \quad \diagdown \\ p \quad p' \quad p \quad p' \end{array} \right|^2 + \left| \begin{array}{c} e \quad e' \\ \diagdown \quad / \\ \text{---} \\ / \quad \diagdown \\ p \quad p' \end{array} \right|^2$$

1                    +                     $10^{-5}$                     +                     $10^{-10}$

# Parity Violation in Electroweak Interaction



V-A Coupling

$$A = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L}$$

long. polarised electrons  
unpolarised protons



# Parity Violation in Electroweak Interaction



**Vector**-Form Factor      **Axial**-Form Factor

$G^S_E, G^S_M$ : "Rosenbluth Separation",  $G_A$ : different Targets:  $p, d$

# Separation of Strangeness

$$A^{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = -\frac{G_F Q^2}{\pi\alpha\sqrt{2}} \times \frac{\varepsilon G_E^p \tilde{G}_E^p + \tau G_M^p \tilde{G}_M^p + \delta G_M^p \tilde{G}_A^p}{\varepsilon (G_E^p)^2 + \tau (G_M^p)^2}$$

$$\tilde{G}_E^p = \frac{1}{4} (G_E^p - G_E^n) - \sin^2 \theta_W G_E^p - \frac{1}{4} G^s_E$$

$$\tilde{G}_M^p = \frac{1}{4} (G_M^p - G_M^n) - \sin^2 \theta_W G_M^p - \frac{1}{4} G^s_M$$

$$A^{PV} = -\frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \times \left[ (1 - 4\sin^2 \theta_W) - \frac{\varepsilon G_E^p G_E^n + \tau G_M^p G_M^n}{\varepsilon (G_E^p)^2 + \tau (G_M^p)^2} \right.$$

$$\left. - \frac{\varepsilon G_E^p (G^s_E) + \tau G_M^p (G^s_M)}{\varepsilon (G_E^p)^2 + \tau (G_M^p)^2} \right]$$

$$- \left\{ \frac{(1 - 4\sin^2 \theta_W) \sqrt{1 - \varepsilon^2} \sqrt{\tau(1 + \tau)} G_M^p \tilde{G}_A^p}{\varepsilon (G_E^p)^2 + \tau (G_M^p)^2} \right\}$$

$$A^{PV} = (A_{ns} + A_s)_V + A_A = (A_0) + (A_s)$$

# Error in Asymmetry from Input Parameters

at  $E_e = 315\text{MeV}$ ,  $\theta_e = 145^\circ$ :

$Q^2 = (0.223 \text{ GeV}^2/c^2)$

$A_0 = (-16.17 \pm 1.02) \text{ ppm}$

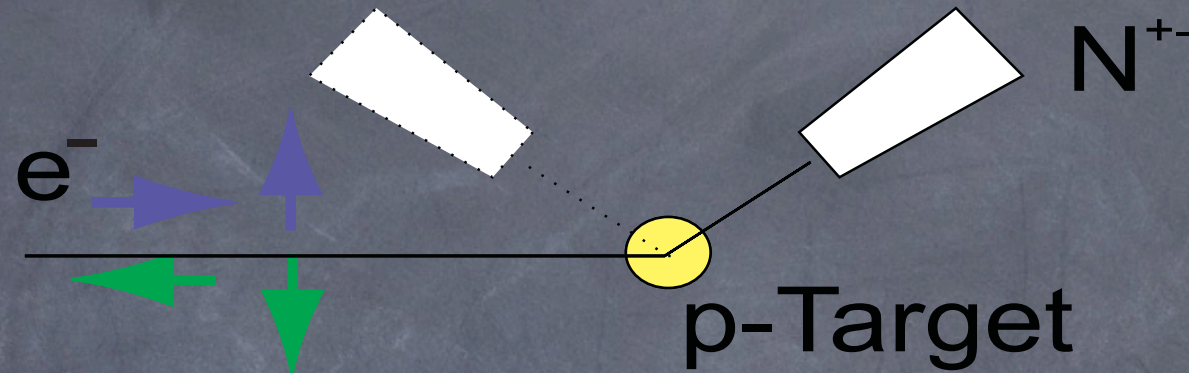
\* Error contribution to  $A_0$  at 145 degree:

- |               |               |
|---------------|---------------|
| * $G_{Ap}$    | err: 0.96 ppm |
| * $G_{Mn}$    | err: 0.27 ppm |
| * $G_{Mp}$    | err: 0.23 ppm |
| * $G_{Ep}$    | err: 0.04 ppm |
| * Weinberg    | err: 0.03 ppm |
| * $G_{En}$    | err: 0.02 ppm |
| * $G_{\mu e}$ | err: 0.00 ppm |

=====

\* quadr. sum      1.02 ppm

# Parity Violating Electron Scattering



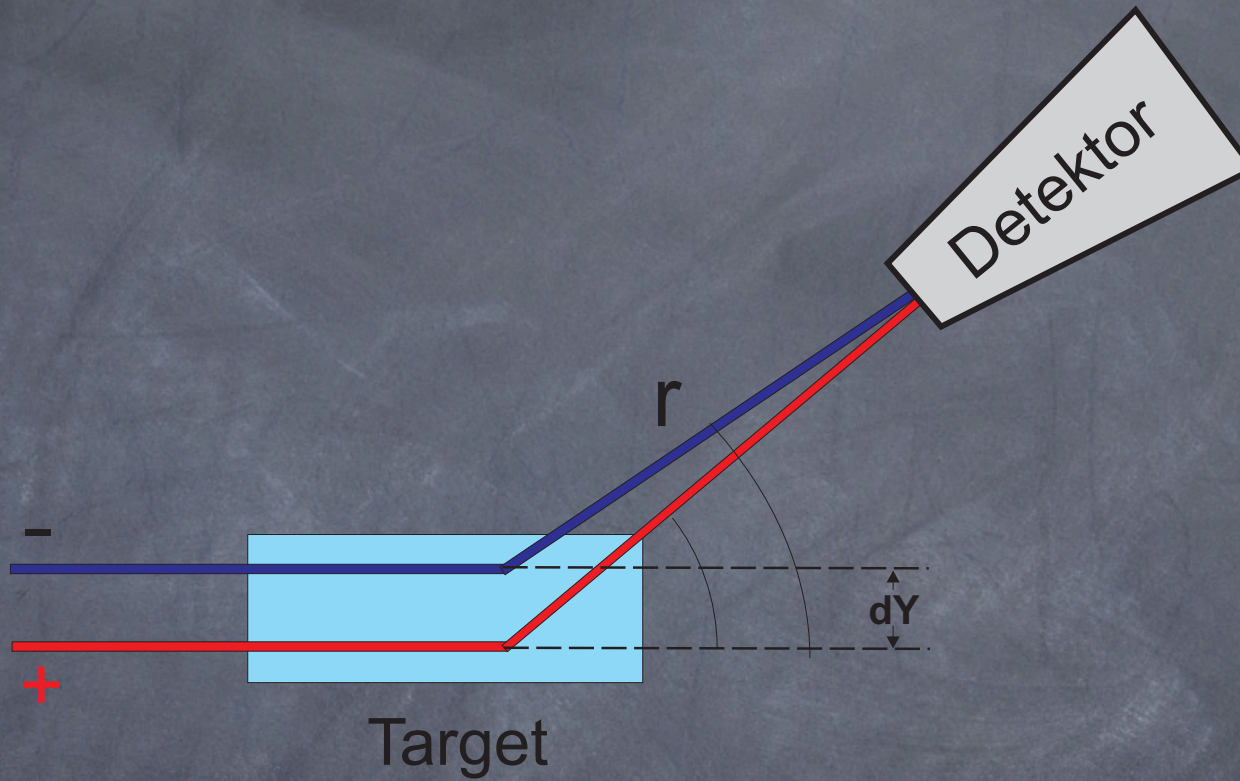
$$A = \frac{N^+ - N^-}{N^+ + N^-}$$

$$A_{\text{exp}} - A_0 \rightarrow A_s$$

$$G_E^s + a G_M^s$$

Rosenbluth Separation, different Targets (p, d, He)

# False Asymmetries



$$A_{\text{exp}} = A_{\text{pv}} + A_{\text{f}}^{\theta}$$

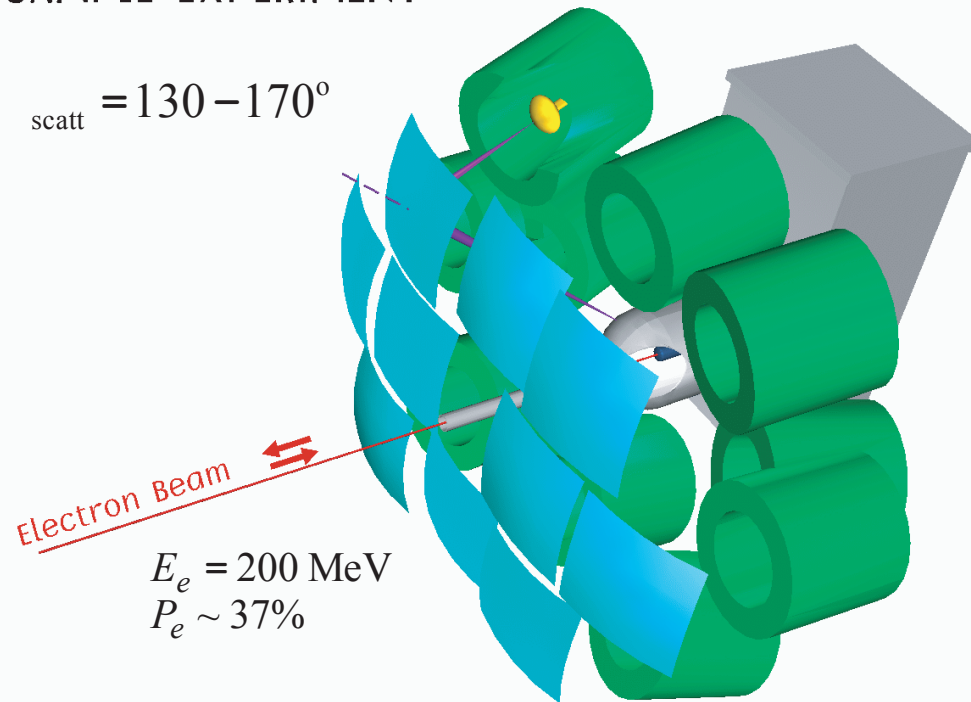
# Experiments

Asymmetries:  $10^{-6} \rightarrow 10^{14}$  events  
high luminosity, high count rates  
inelastic scattering

SAMPLE  
MIT/Bates  
Air Cherenkov  
Integrating  
No Magnet  
Backward

## SAMPLE EXPERIMENT

scatt =  $130 - 170^\circ$

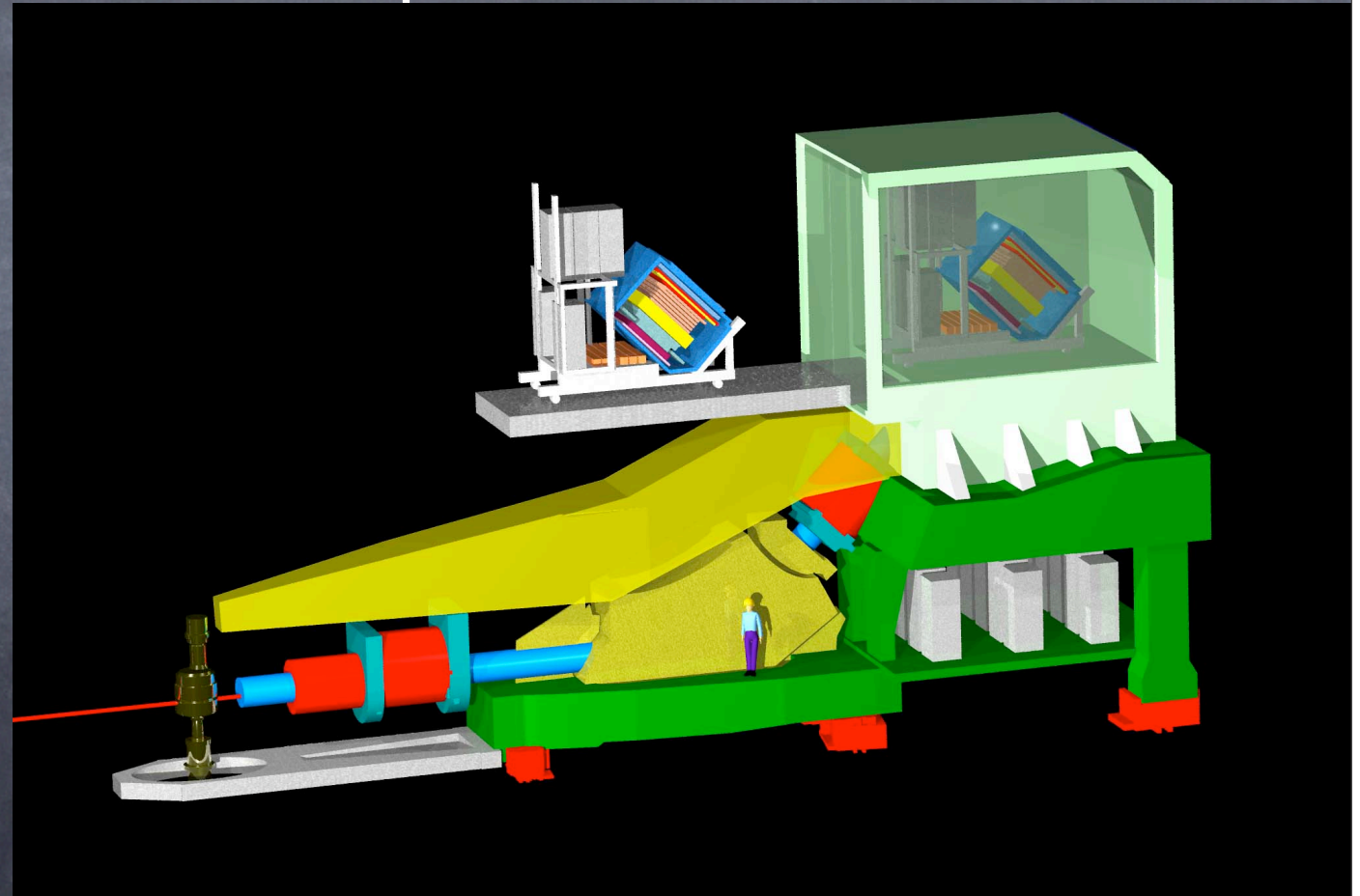


$E_e = 200 \text{ MeV}$   
 $P_e \sim 37\%$

# Experiments

Asymmetries:  $10^{-6}$   $\rightarrow$   $10^{14}$  events  
high luminosity, high count rates  
inelastic scattering

HAPPEX  
Hall A,  
Jefferson Lab  
Magnetic  
Spectrometer  
Integrating  
Forward



# Experiments

Asymmetries:  $10^{-6} \rightarrow 10^{14}$  events  
high luminosity, high count rates  
inelastic scattering

GO

HALL C

Jefferson Lab

Toroidal magnetic  
Spectrometer

Forward

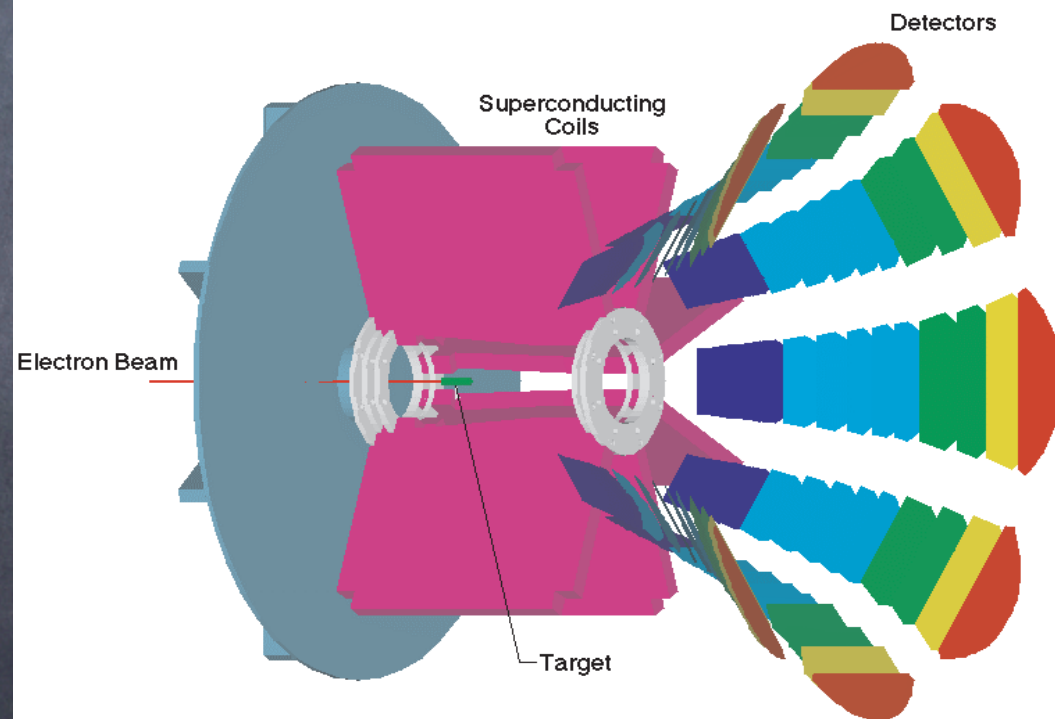
Backward

Counting

ToF

$G_E^s$ ,  $G_M^s$  and  $G_A^e$  separated

over range  $Q^2 \sim 0.1 \text{ -- } 1.0 \text{ (GeV/c)}^2$





# Experiments

Asymmetries:  $10^{-6}$   $\rightarrow$   $10^{14}$  events  
high luminosity,  
inelastic scatter

A4

MAMI (Mainz)

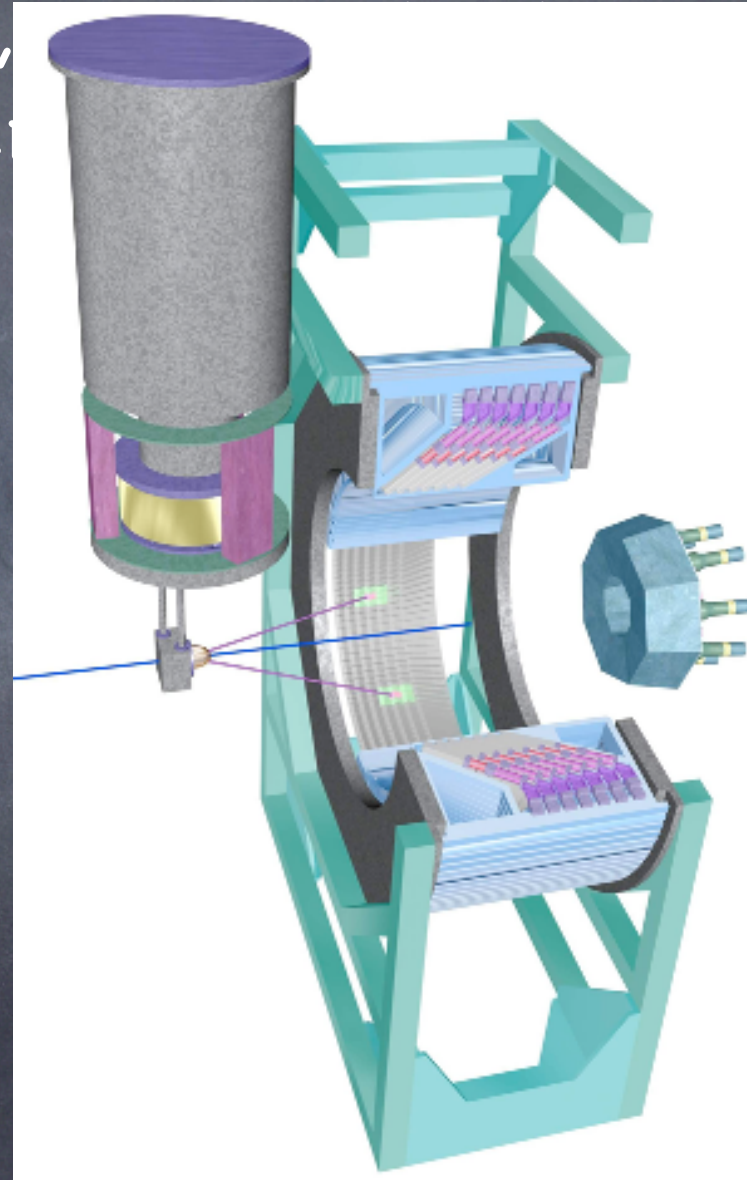
Electromagnetic

Calorimeter

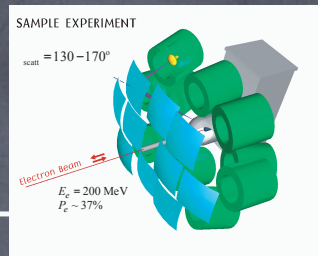
Counting

Forward

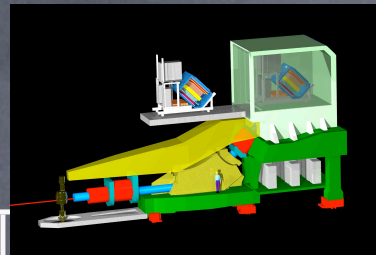
Backward



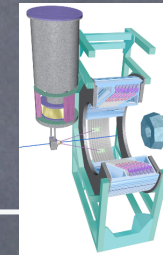
# PV Experiments



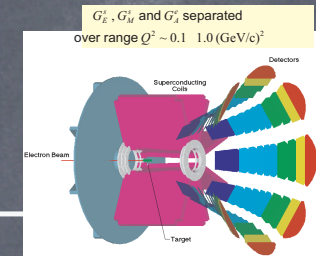
SAMPLE  
(MIT Bates)



HAPPEX  
(CEBAF, JLab)



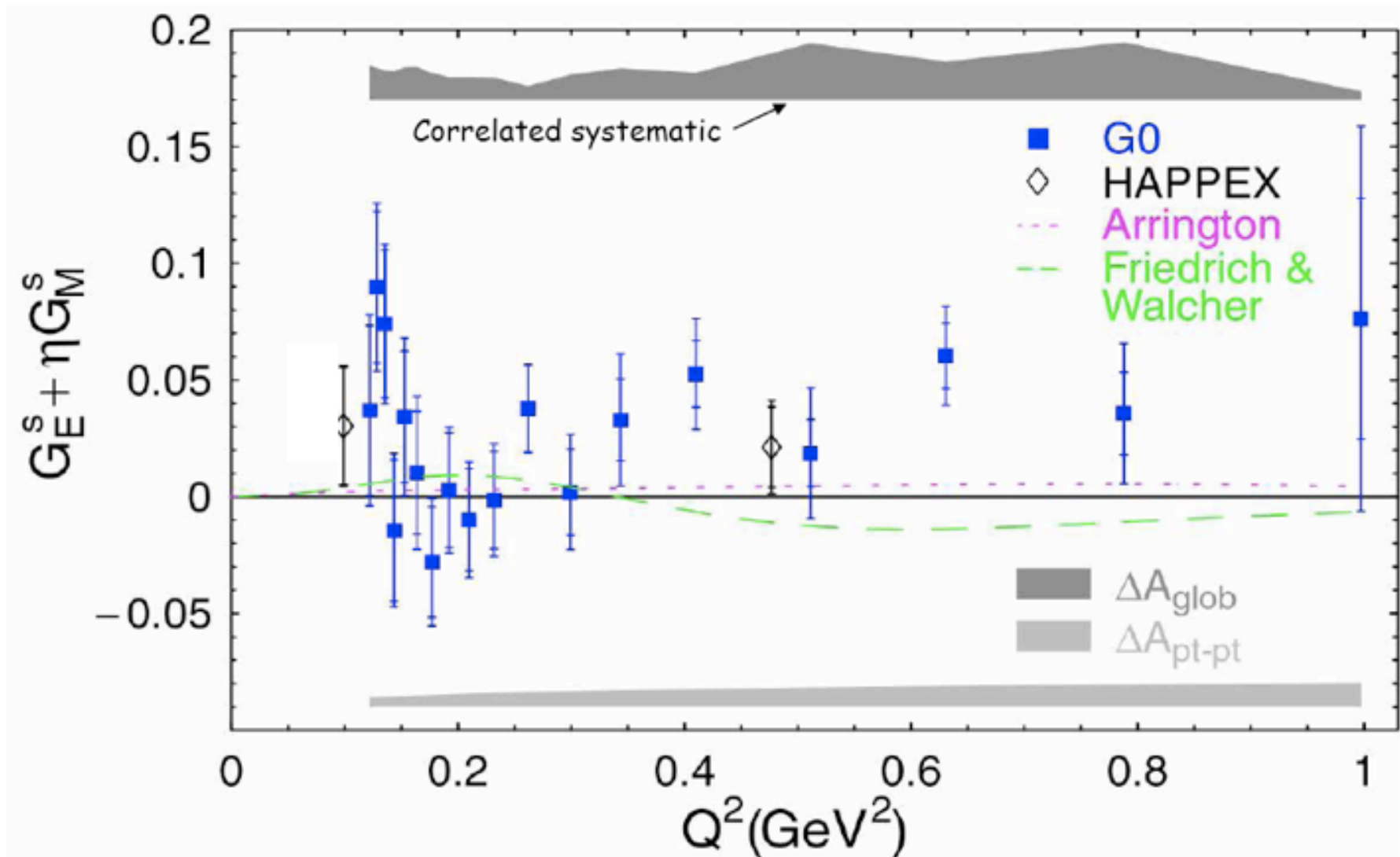
A4  
(MAMI)



G<sup>0</sup>  
(CEBAF, JLab)

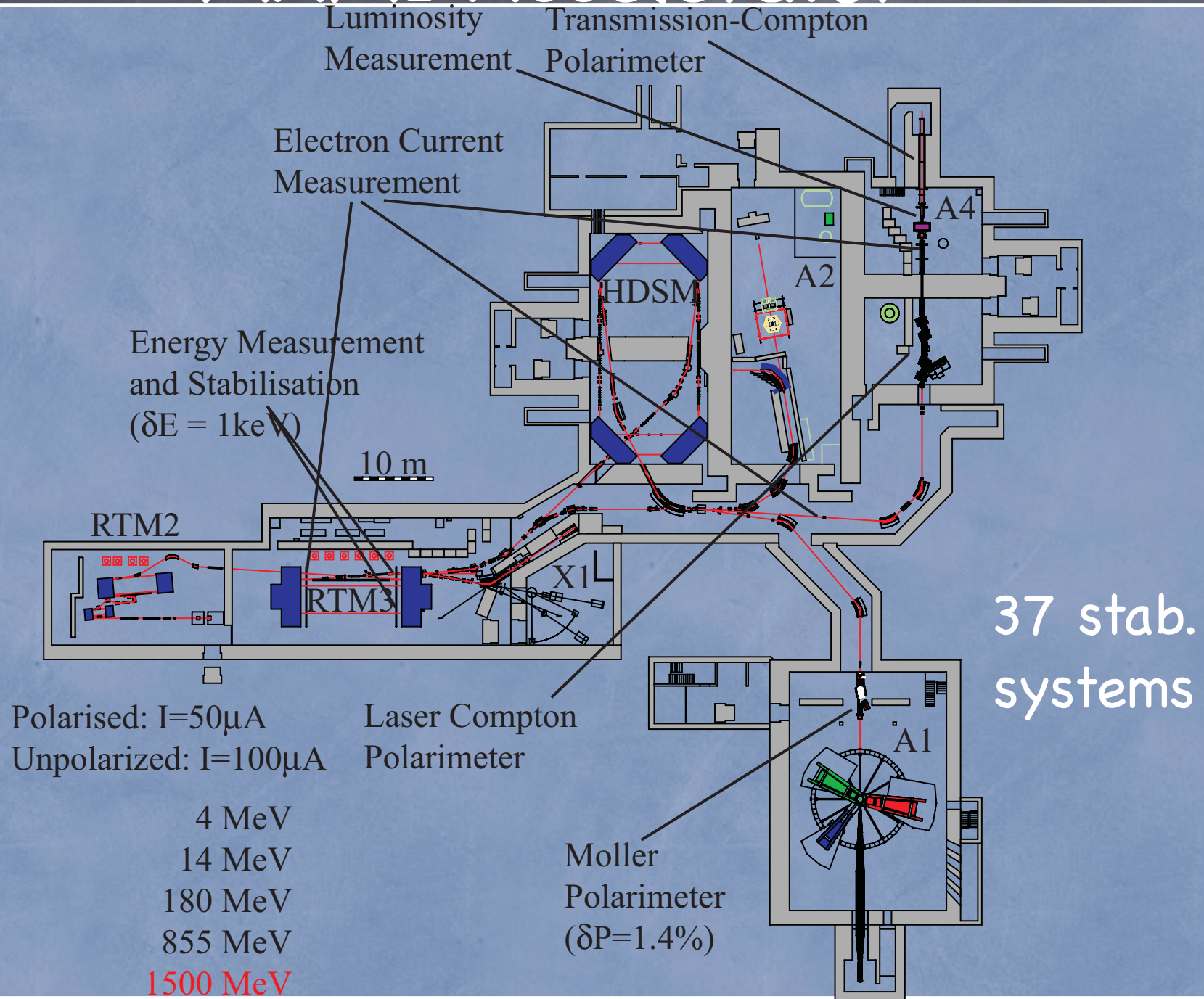
	SAMPLE (MIT Bates)	HAPPEX (CEBAF, JLab)	A4 (MAMI)	G <sup>0</sup> (CEBAF, JLab)
$Q^2$ [GeV <sup>2</sup> /c <sup>2</sup> ]	0.04, 0.1	0.1, 0.48, (0.63)	0.1, 0.23, (0.48) (0.23 fw)	0.1, ... 1,0 0.23, 0.63
Angle	B	F	F, B	F, B
Target	H, D	H, He	H, D	H, D
Separation	$G_M^S, G_A$	$G_E^S, G_M^S$	$G_E^S, G_M^S,$ $G_A$	$G_E^S, G_M^S,$ $G_A$

## G0: Forward-angle results

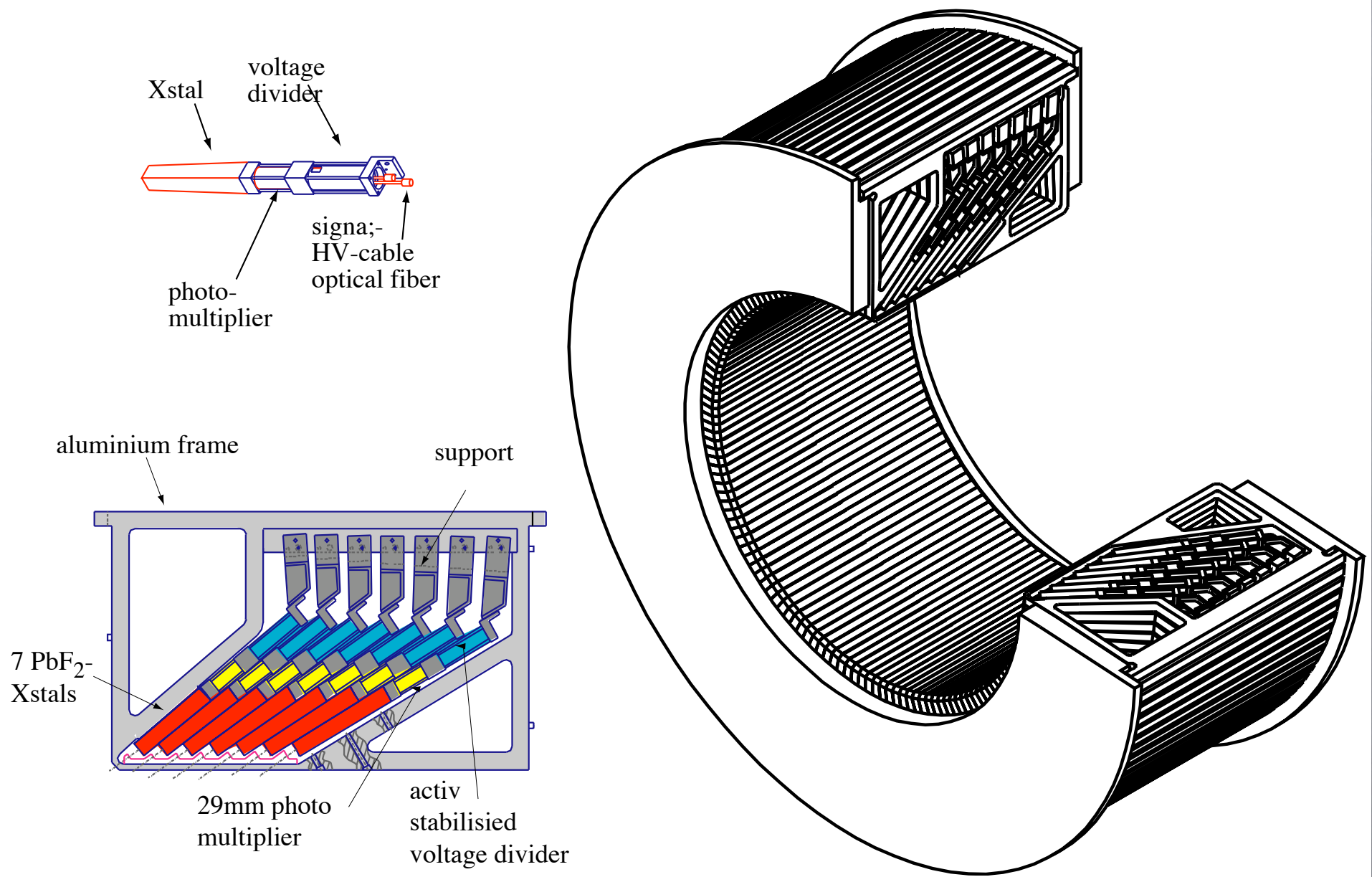


$G_E^s = G_M^s = 0$  Hypothesis excluded at 89% C.L.

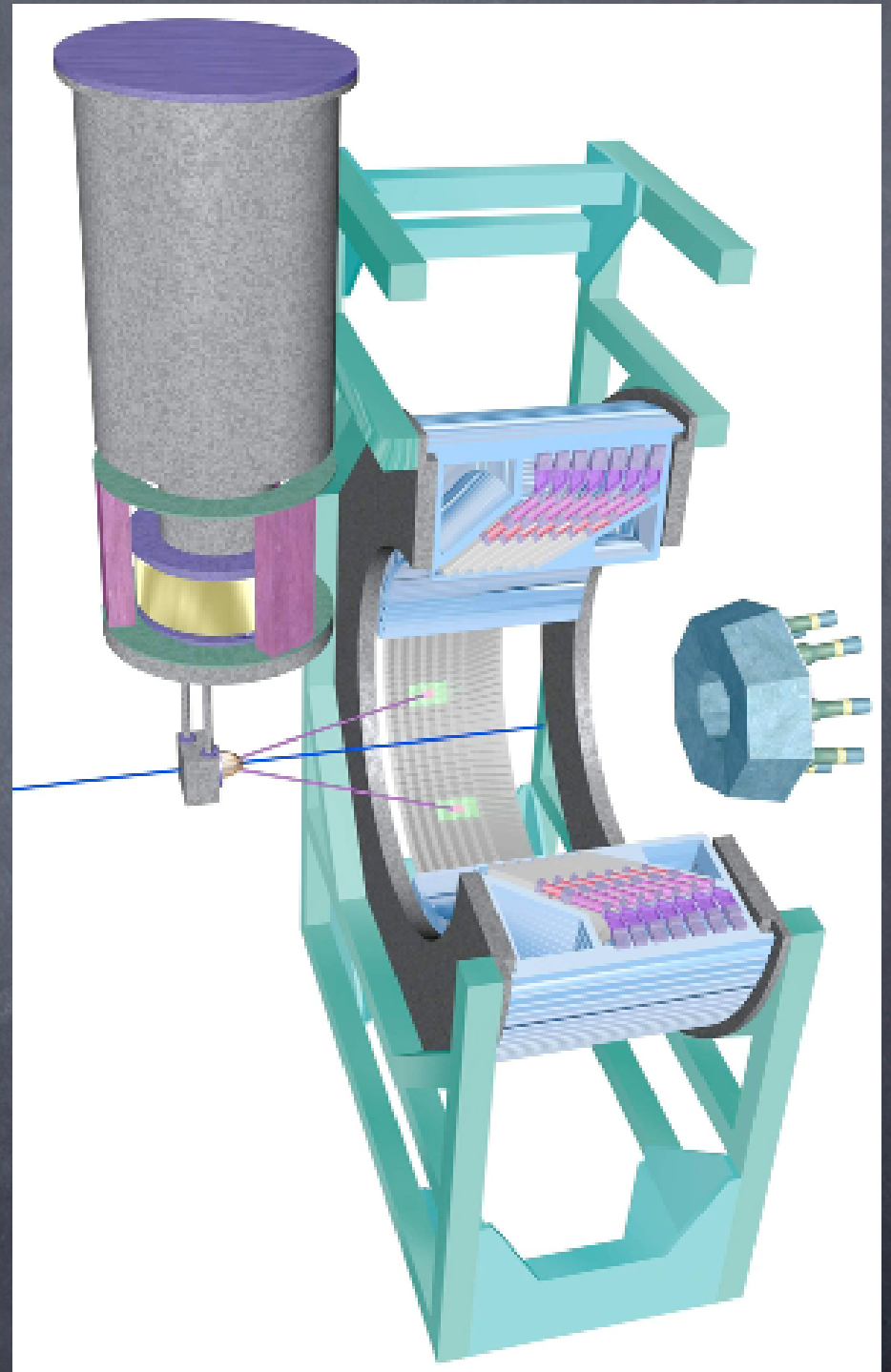
# MAMI Accelerator

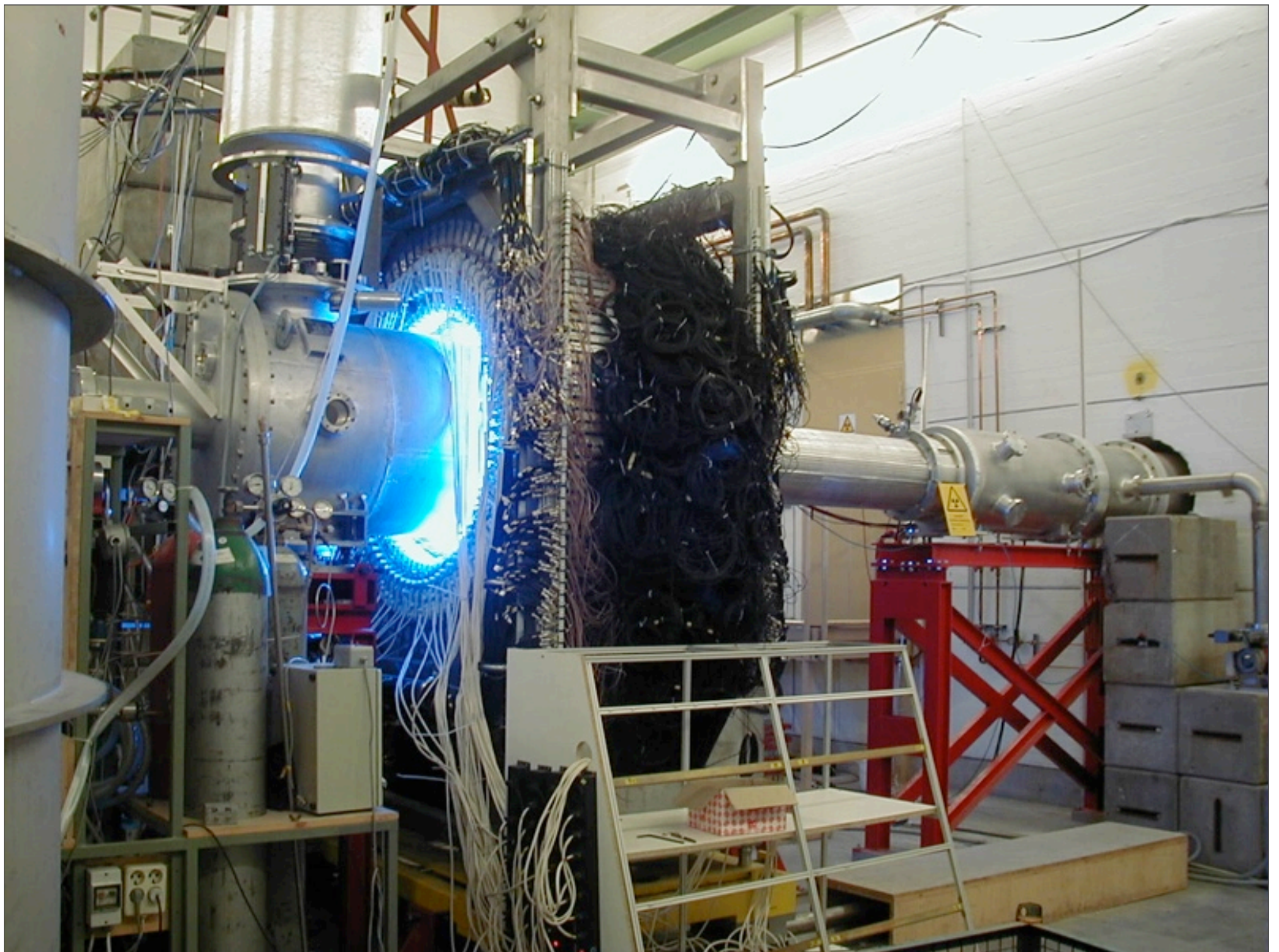


# Fast PbF<sub>2</sub> Calorimeter

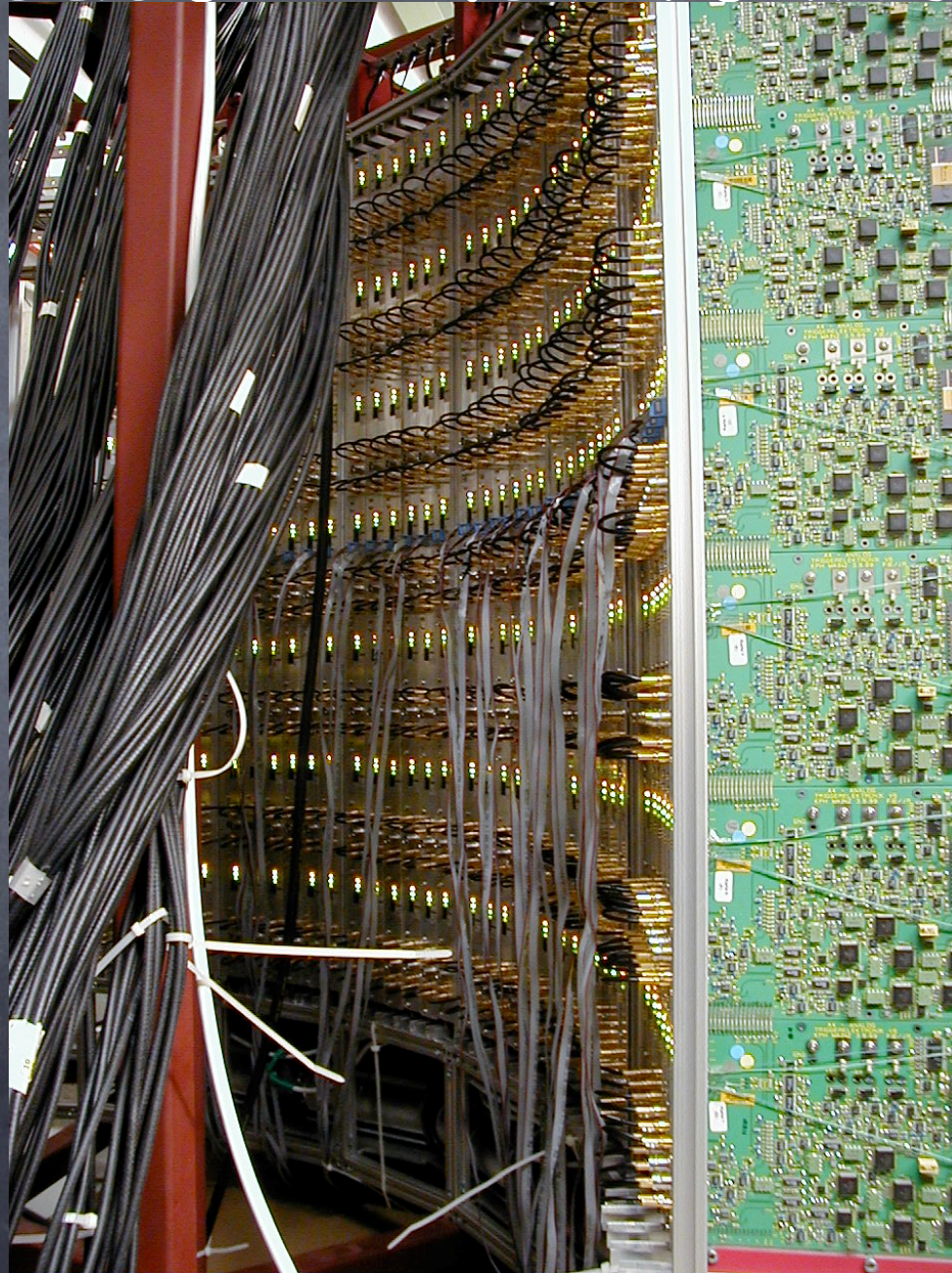


# A4: Fast $\text{PbF}_2$ Calorimeter





# Readout Electronics

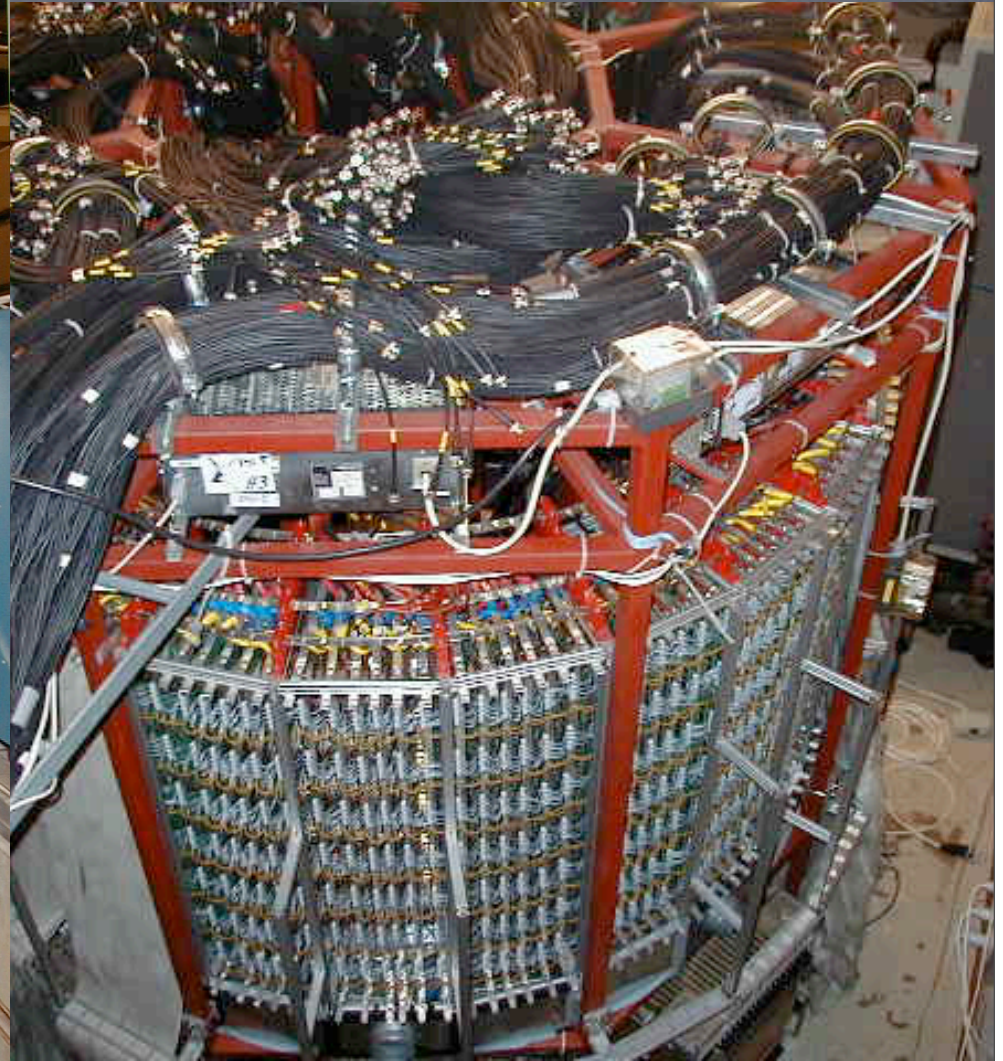




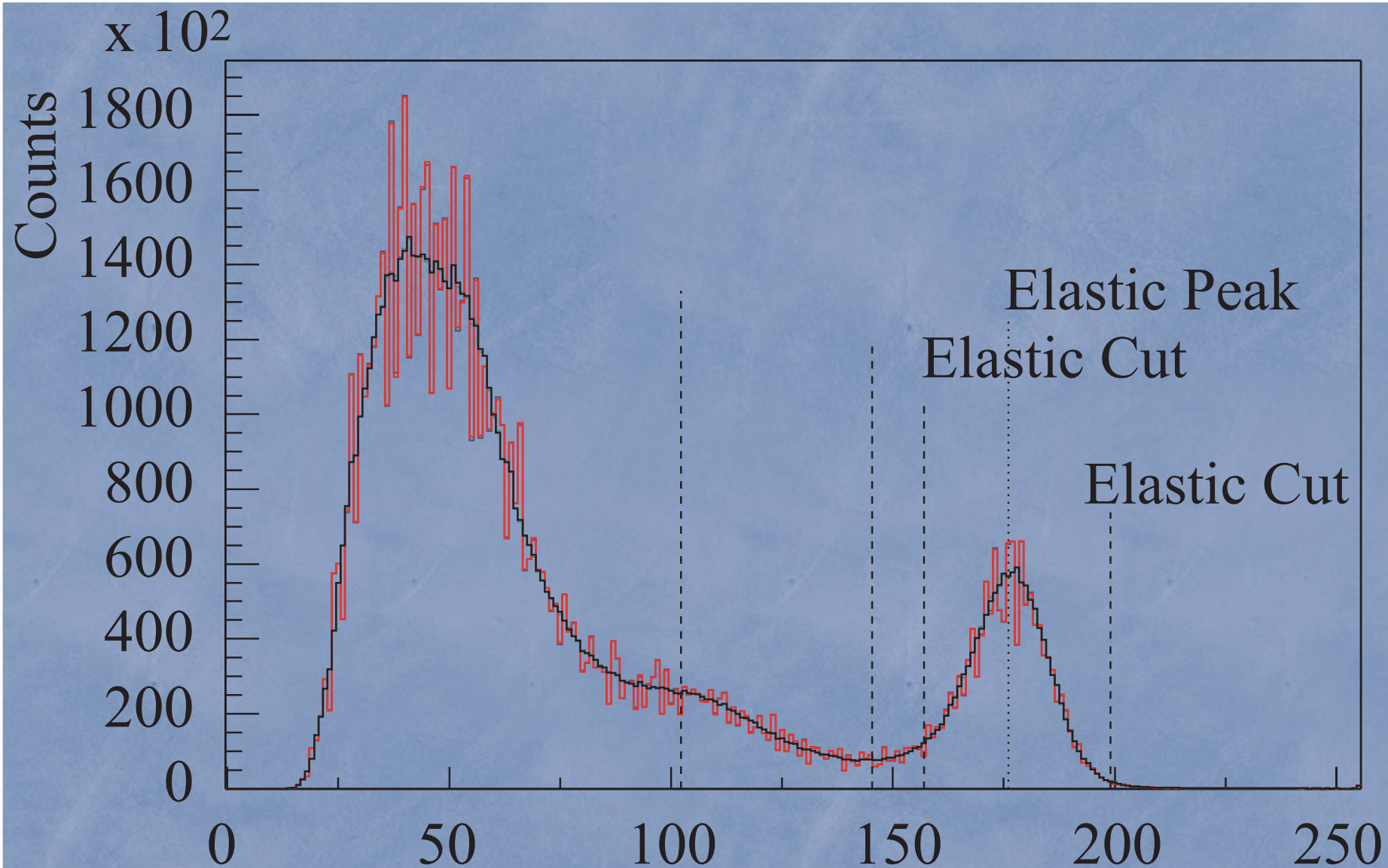
# Readout Electronics



# Readout Electronics

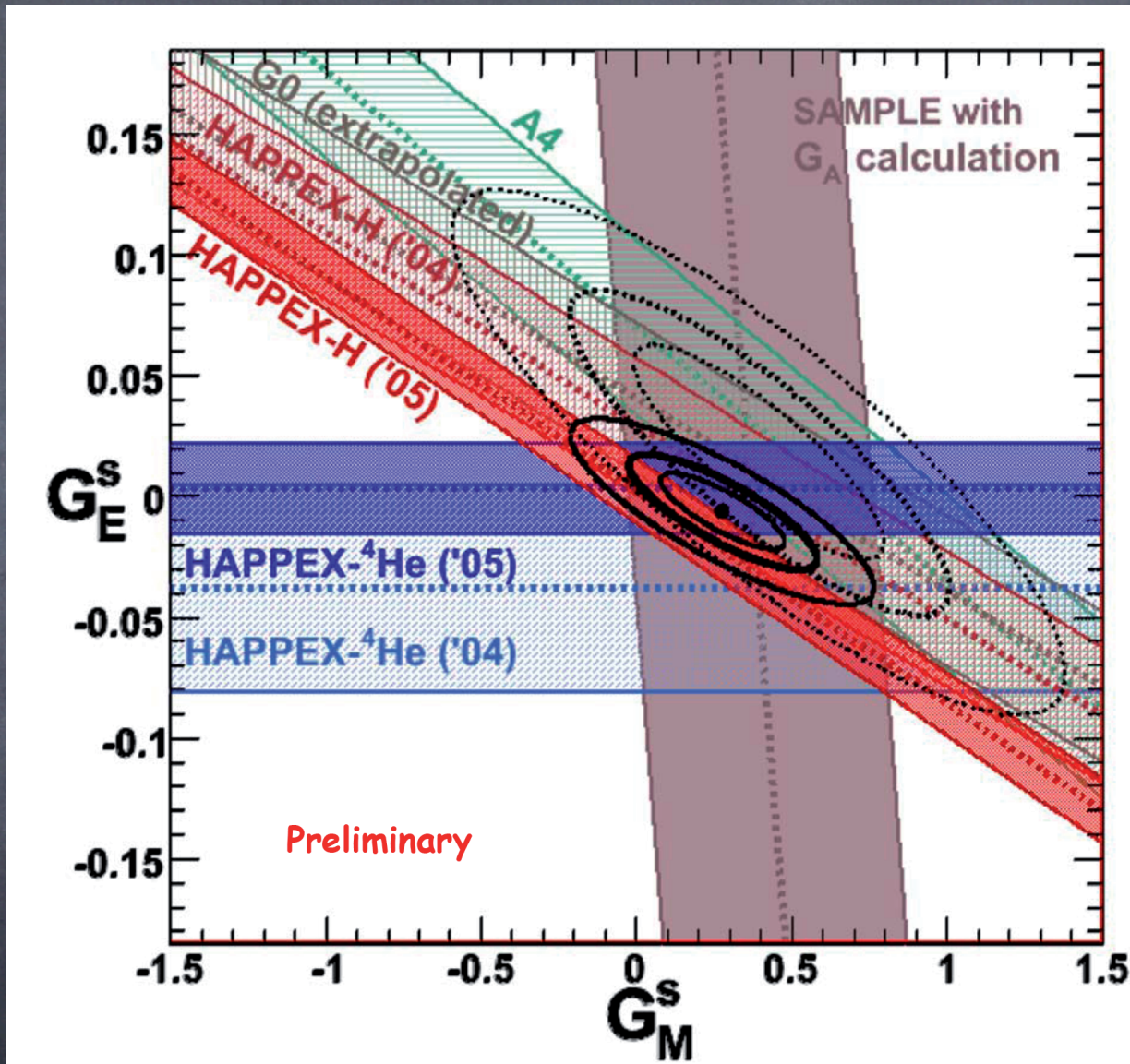


# Detector Data



16  $10^6$  Histogramms  $\rightarrow 10^{13}$  events  
Filtering

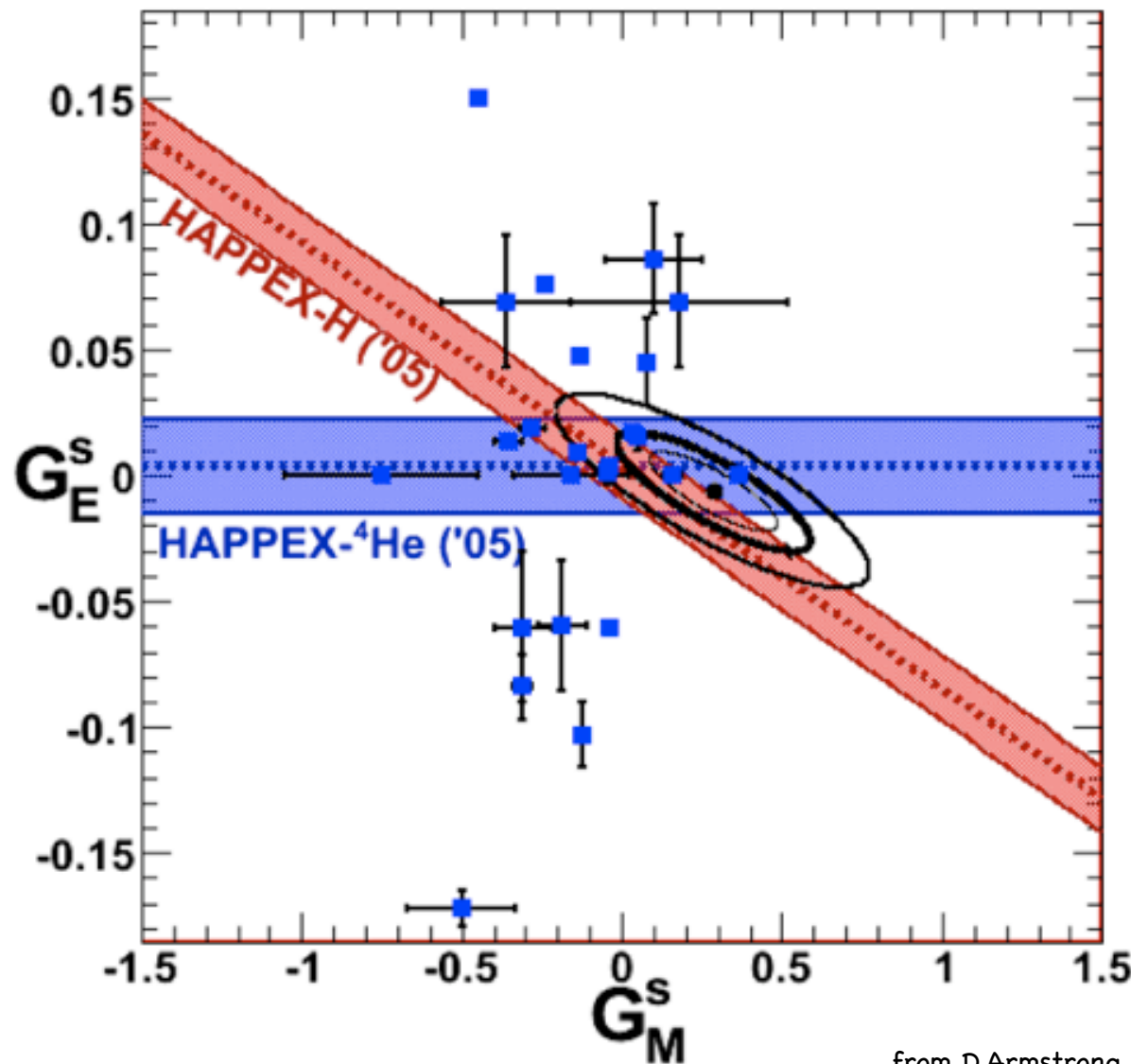
# World Data at $0.1 \text{ (GeV/c)}^2$



$$G_M^s = 0.28 \pm 0.20$$

$$G_E^s = -0.006 \pm 0.016$$

# World Data near $Q^2 \sim 0.1 \text{ GeV}^2$



$$G_M^s = 0.28 \pm 0.20$$

↓  
21% of  $\mu_N^{T=0}$

$$\langle r^2 \rangle_E^p = 0.766 \pm 0.012 \text{ fm}^2$$

$$\langle r^2 \rangle_E^s = 0.002 \pm 0.015 \text{ fm}^2$$

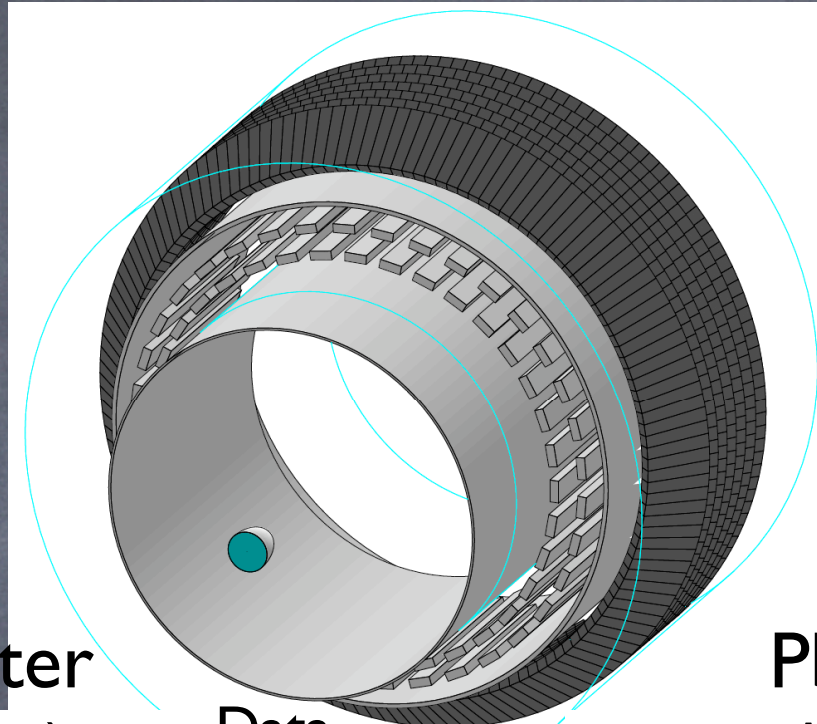
Lattice: Leinweber et al.

$$G_M^s = -0.046 \pm 0.022$$

$$G_E^s = +0.001 \pm 0.006$$

# A4-Backward Angle

$Q^2=0.23 \text{ (GeV/c)}^2$  Data and Simulations  
backward



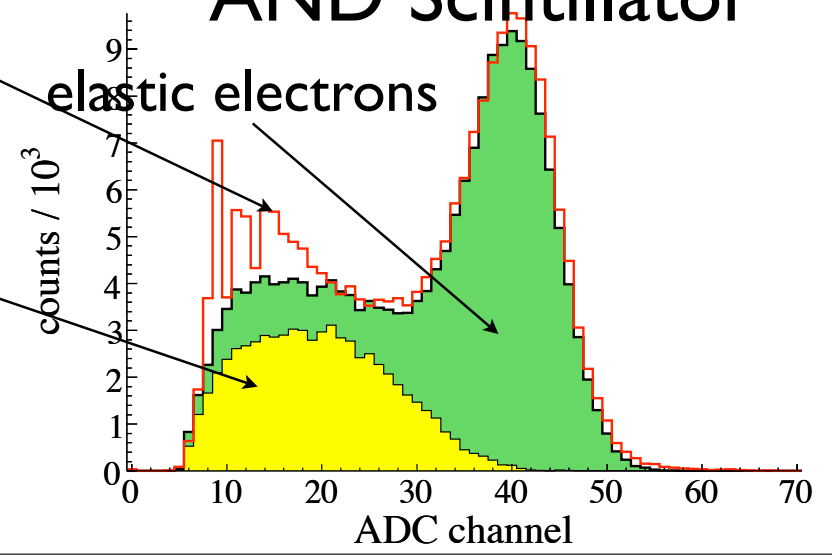
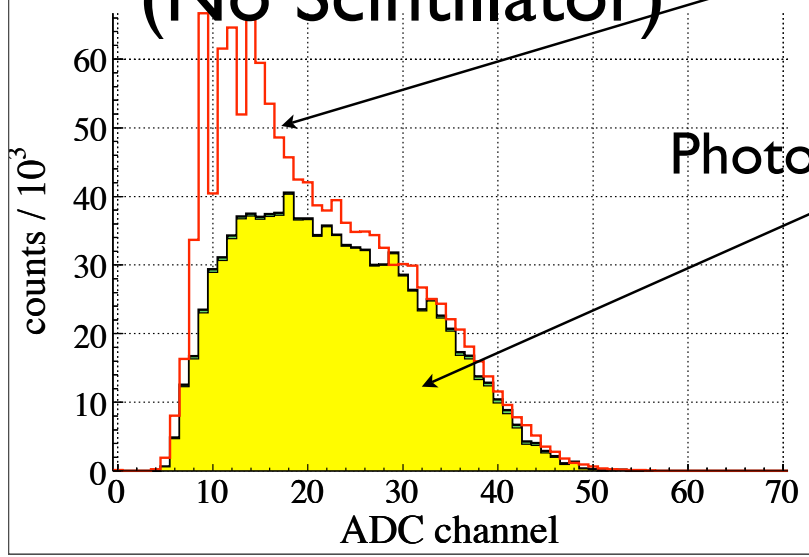
PbF<sub>2</sub>-Calorimeter  
(No Scintillator)

PbF<sub>2</sub>-Calorimeter  
AND Scintillator

Data

Photons

elastic electrons

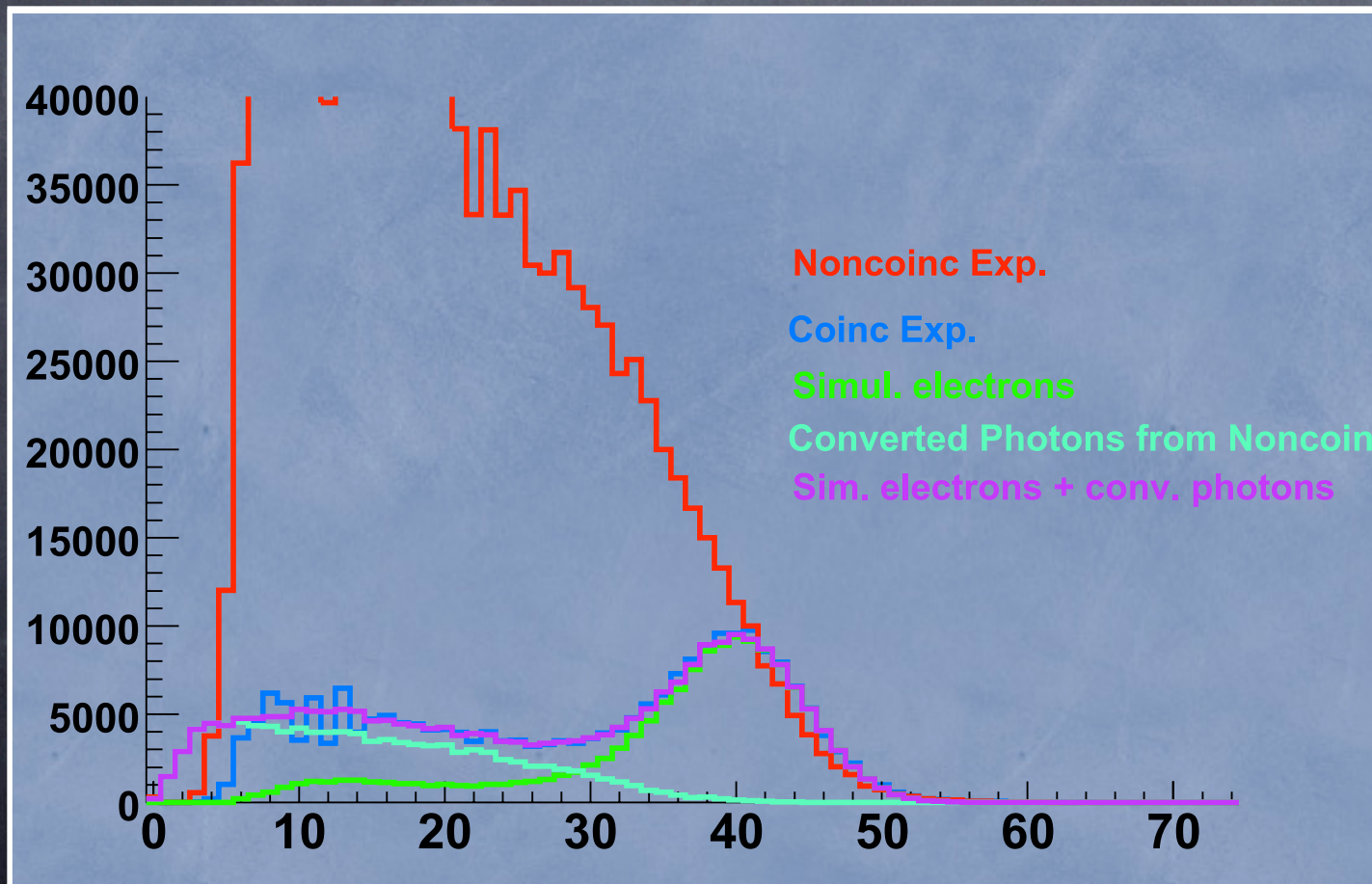


# $Q^2=0.23 \text{ (GeV/c)}^2$ backward

About 1050h of data

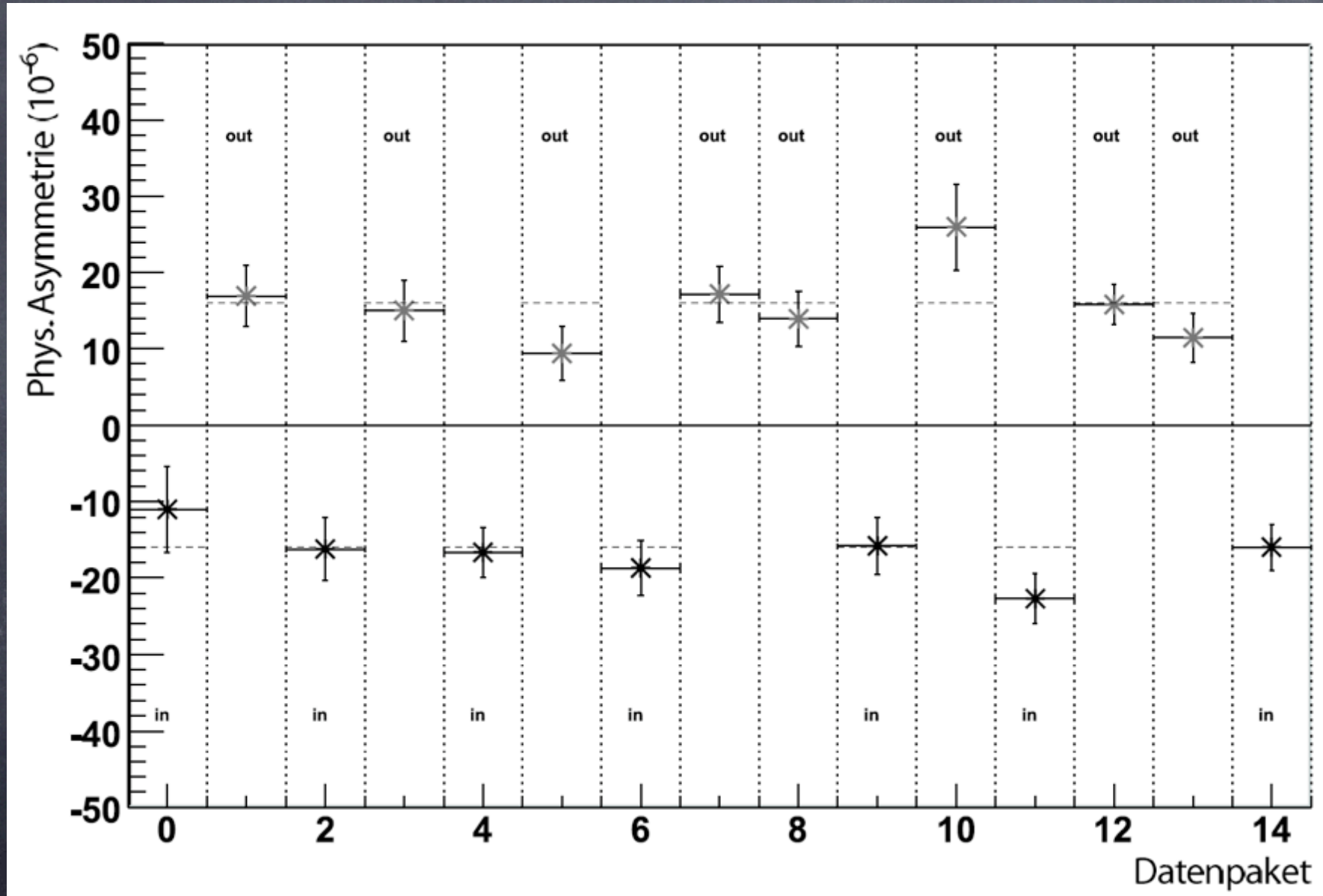
$N_{\text{elastic}}=2.1 \times 10^{12}$

$A_{\text{coinc}} = (-16.22 \pm 1.15) \text{ ppm}$   
( $\pm 0.93 \text{ stat} \pm 0.67 \text{ sys}$ )



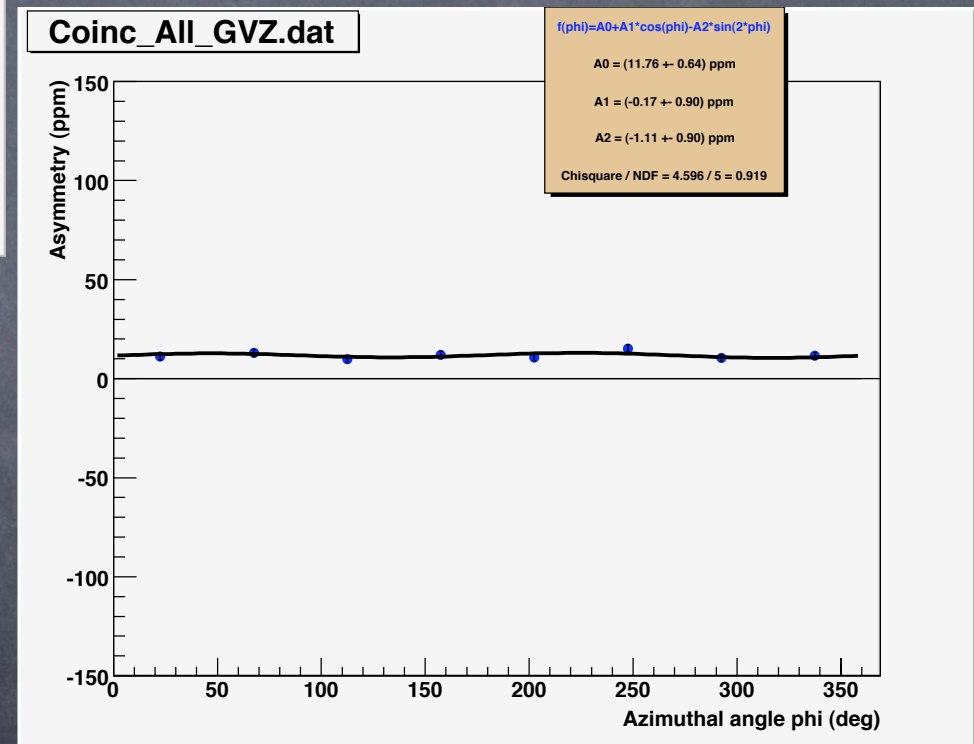
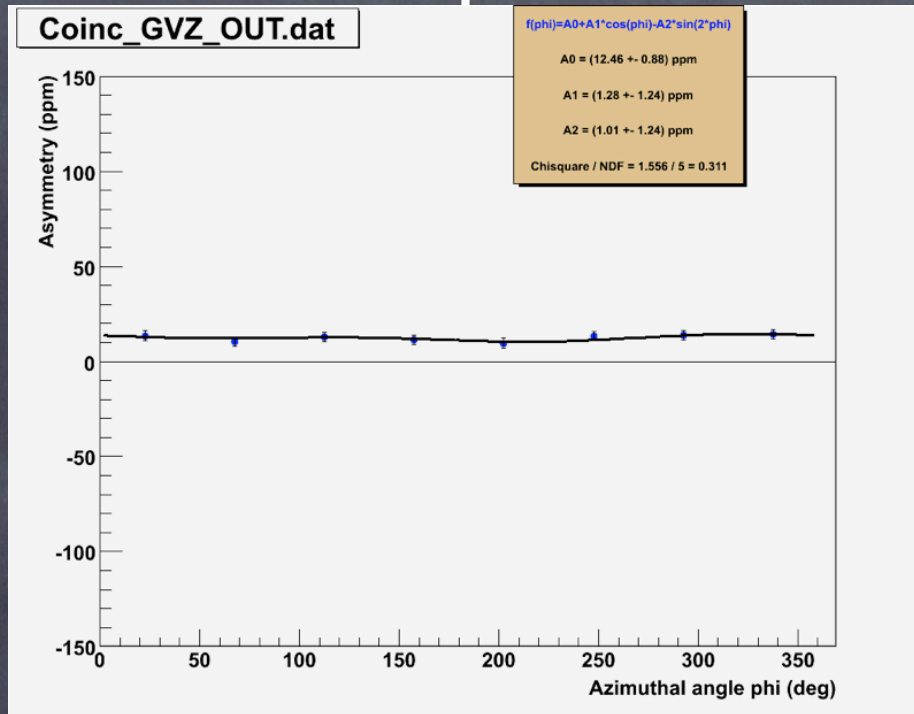


$Q^2=0.23 \text{ (GeV/c)}^2$  backward



About 1100h of stored data (2000h real time)

# A4-Data, proton, backward angle, signal

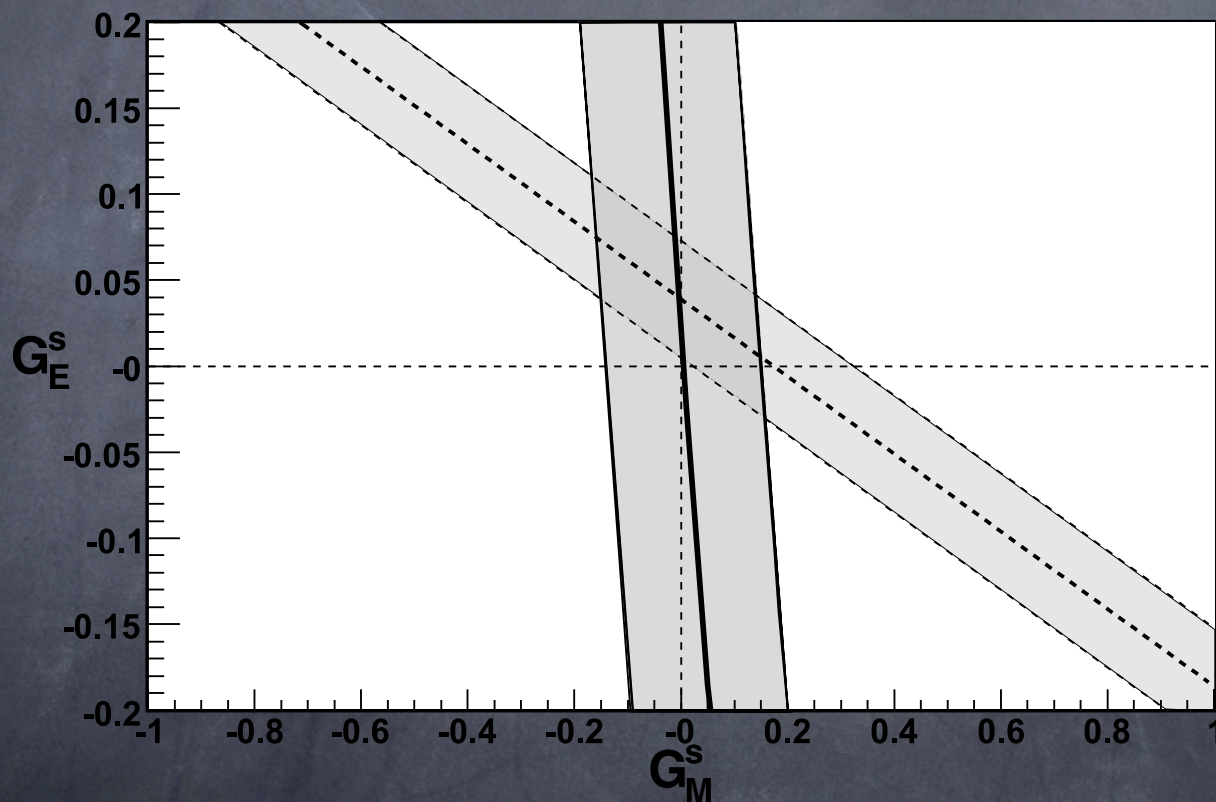


signal, preliminary

$Q^2=0.23 \text{ (GeV/c)}^2$  backward

$$APV = (-16.23 \pm 0.96_{\text{stat}} \pm 0.75_{\text{syst}}) 10^{-6}$$

$$G_{SM} + 0.25 G_{SE} = 0.004 \pm 0.146$$

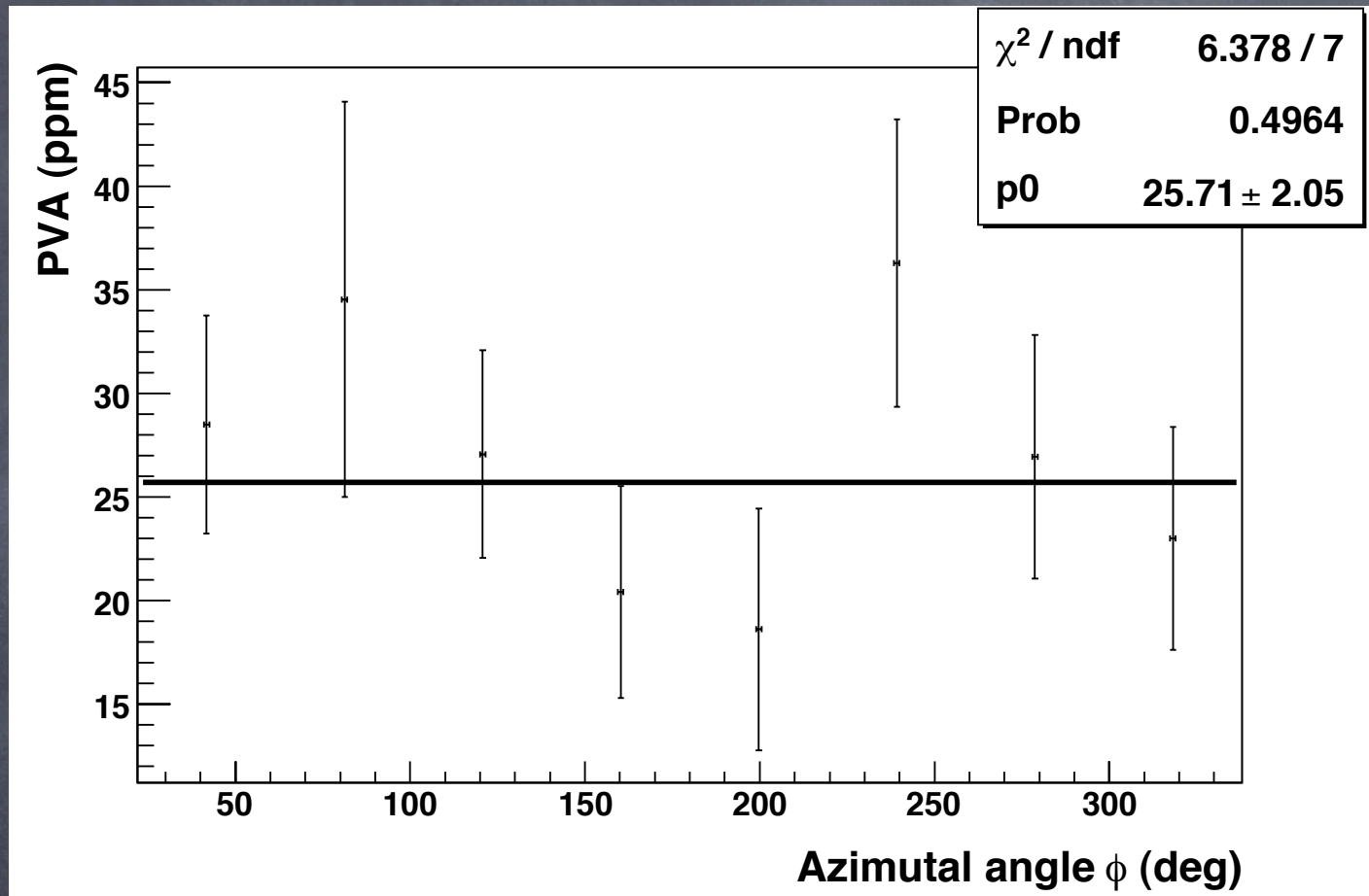


$$G_{SM} = -0.01 \pm 0.15$$

$$G_{SE} = 0.034 \pm 0.050$$

preliminary

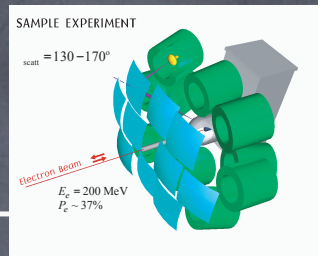
# A4-Data, deuterium, backward angle



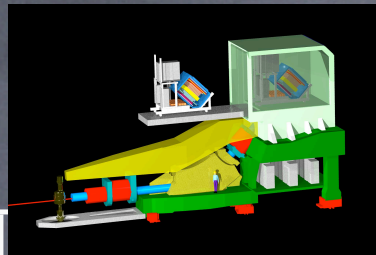
signal

preliminary

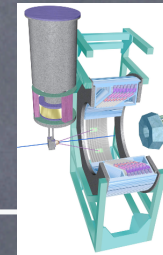
# PV Experiments



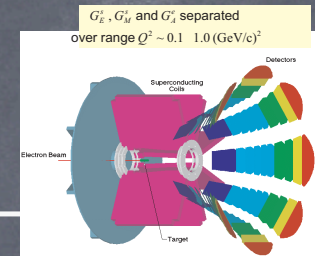
SAMPLE  
(MIT Bates)



HAPPEX  
(CEBAF, JLab)



A4  
(MAMI)



G<sup>0</sup>  
(CEBAF, JLab)

	SAMPLE (MIT Bates)	HAPPEX (CEBAF, JLab)	A4 (MAMI)	G <sup>0</sup> (CEBAF, JLab)
$Q^2$ [GeV <sup>2</sup> /c <sup>2</sup> ]	0.04, 0.1	0.1, 0.48, (0.63)	0.1, 0.23 (0.23 fw)	0.1, ... 1,0 0.23, 0.63
Angle	B	F	F, B	F, B
Target	H, D	H, He	H, D	H, D
Separation	$G_M^S, G_A$	$G_E^S, G_M^S$	$G_E^S, G_M^S,$ $G_A$	$G_E^S, G_M^S,$ $G_A$

# Summary

- Perturbative QCD
- PV  $e(p, p')e'$ : Strangeness Vector Form Factors

A4: Fast (100 Mhz) EM Calorimeter

Situation on Strangeness,

world data:

$$Q^2 = 0.10 \text{ (GeV/c)}^2: G_M^s = 0.28 \pm 0.20 \quad G_E^s = -0.006 \pm 0.016$$

A4:

$$Q^2 = 0.23 \text{ (GeV/c)}^2: G_M^s = -0.01 \pm 0.15 \quad G_E^s = 0.034 \pm 0.050$$

preliminary!!

Effect of Sea in nonpert. QCD

Effect is small: Constituent s-quark suppressed

Analysis of Backward Angles (0.23  $\text{GeV}^2$ , deuterium)