



*The Abdus Salam
International Centre for Theoretical Physics*



1942-49

Sixth International Conference on Perspectives in Hadronic Physics

12 - 16 May 2008

High-energy hadron physics at J-PARC.

S. Kumano
*KEK
Japan*

High-Energy Hadron Physics at J-PARC

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Sixth International Conference on Perspectives in Hadronic Physics

ITCP, Trieste, Italy

May 12 – 16, 2008

(Talk on May 16)

Contents

1. Introduction to high-energy hadron physics at J-PARC

- Introduction to the J-PARC facility
- Possible projects with 30 – 50 GeV proton beam

2. Structure functions

Possible roles of J-PARC projects in

- Unpolarized and Polarized parton distribution functions (PDFs), Nuclear PDFs
- Fragmentation functions
- Tensor structure functions

Topics related to my studies

Part I

Introduction to High-Energy Hadron Physics at J-PARC

J-PARC Facility

J-PARC Location

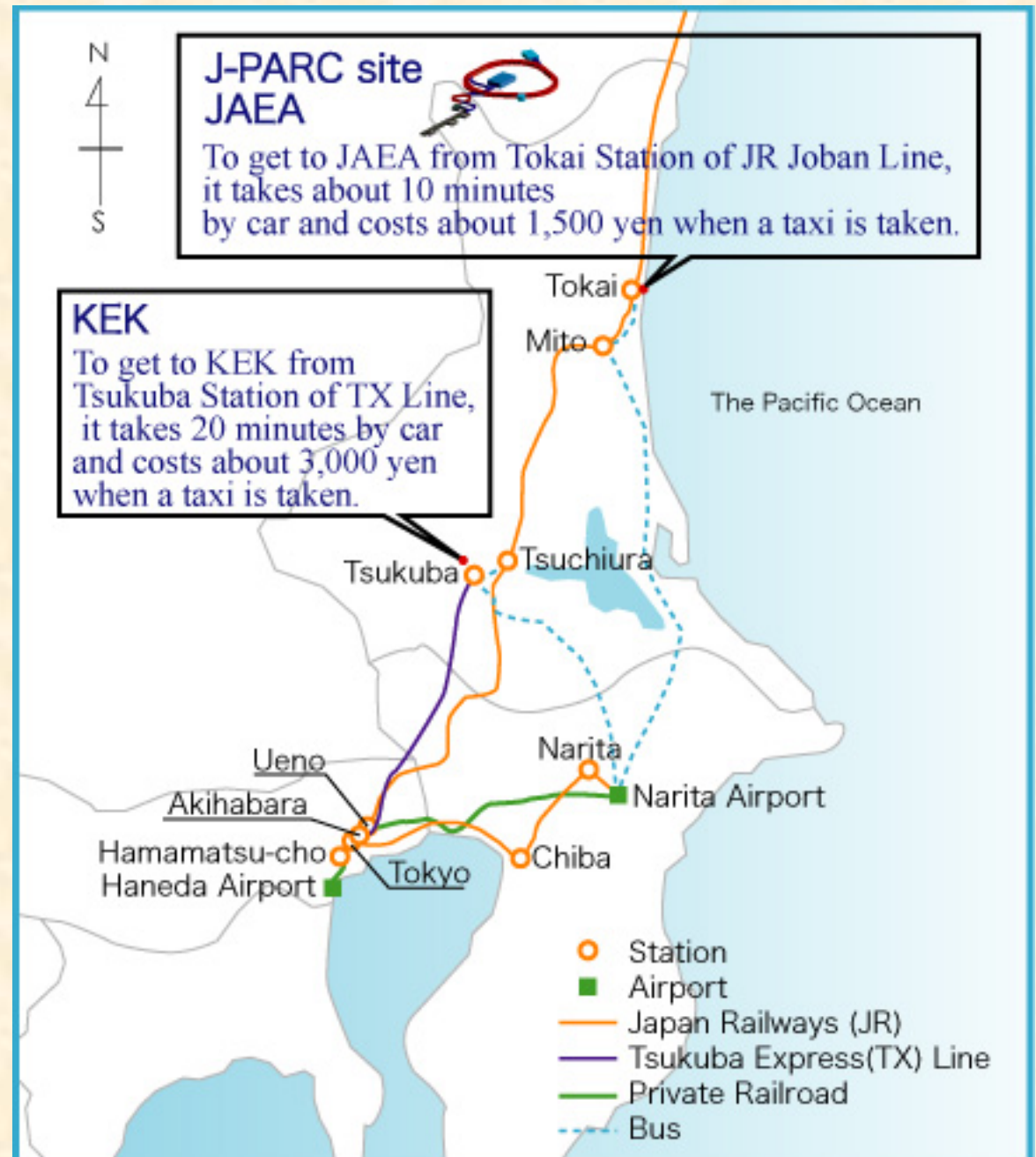
J-PARC (Japan Proton Accelerator Research Complex)

<http://j-parc.jp/index-e.html>

Joint facility of JAEA and KEK.

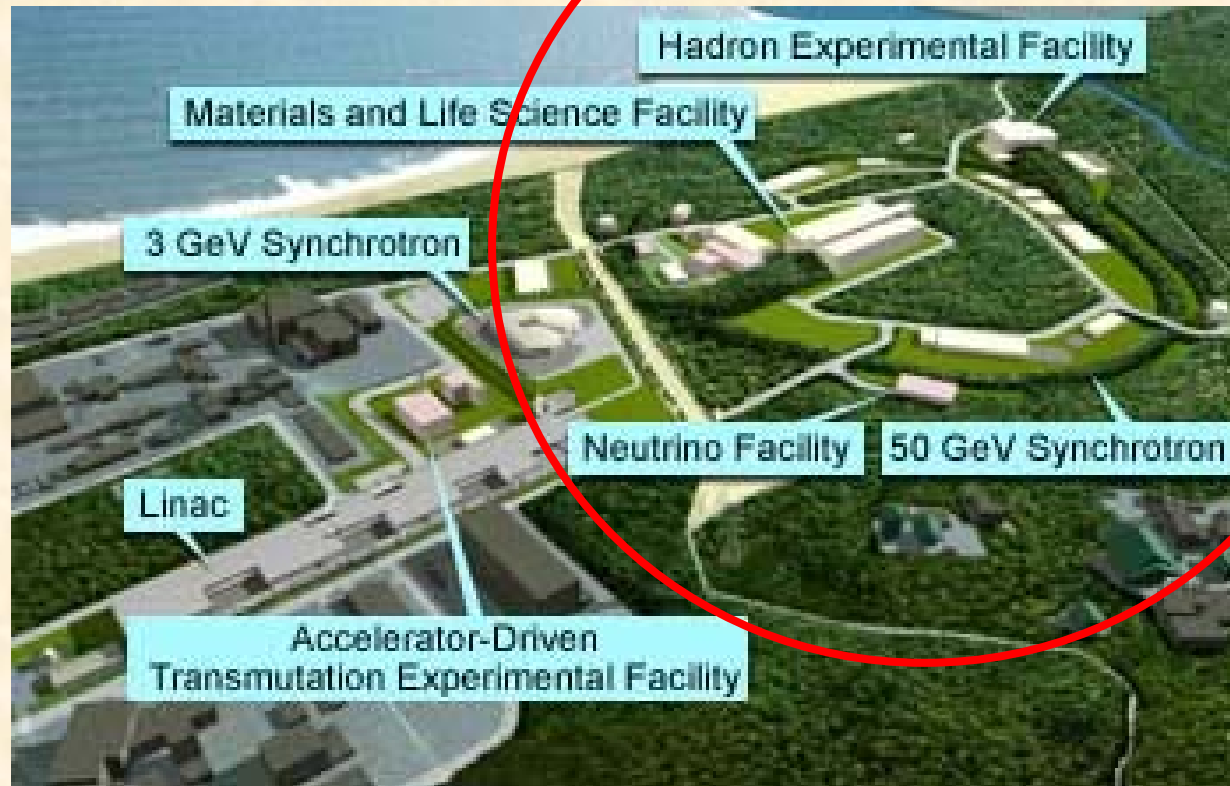
JAEA (Japan Atomic Energy Agency)

**KEK (High Energy Accelerator
Research Organization)**



Bird's-eye view

Particle and Nuclear Physics

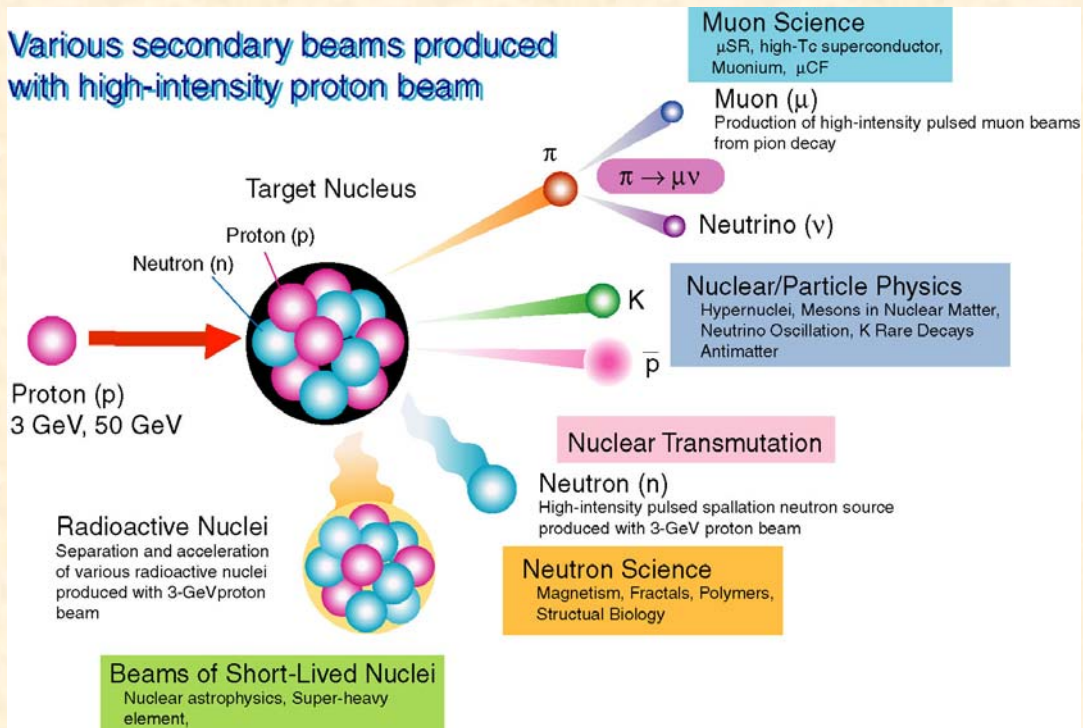


High-Intensity Frontier of Proton Accelerator

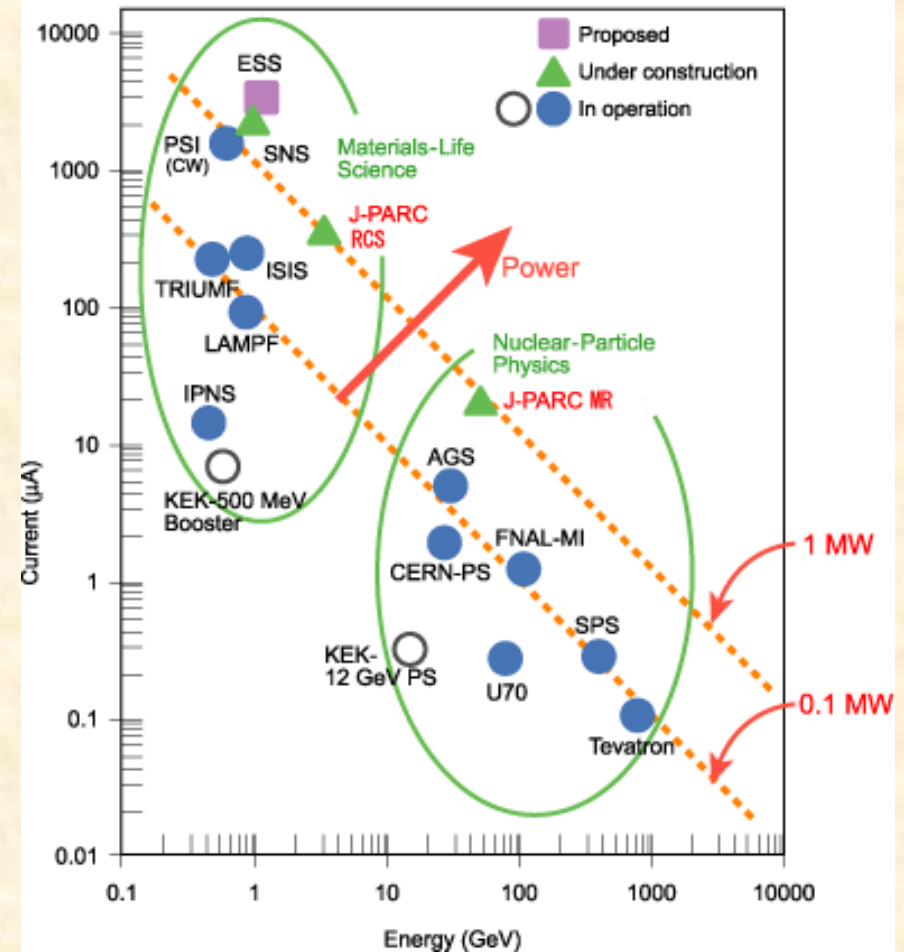
High-intensity proton beam

→ High-intensity secondary beams
(Neutrino, Kaon, Pion, Neutron ...)

Various secondary beams produced with high-intensity proton beam



Power map of worldwide proton accelerators



- **Strangeness nuclear physics (1st experiment)**

- **Exotic hadrons**

- **Hadrons in nuclear medium**

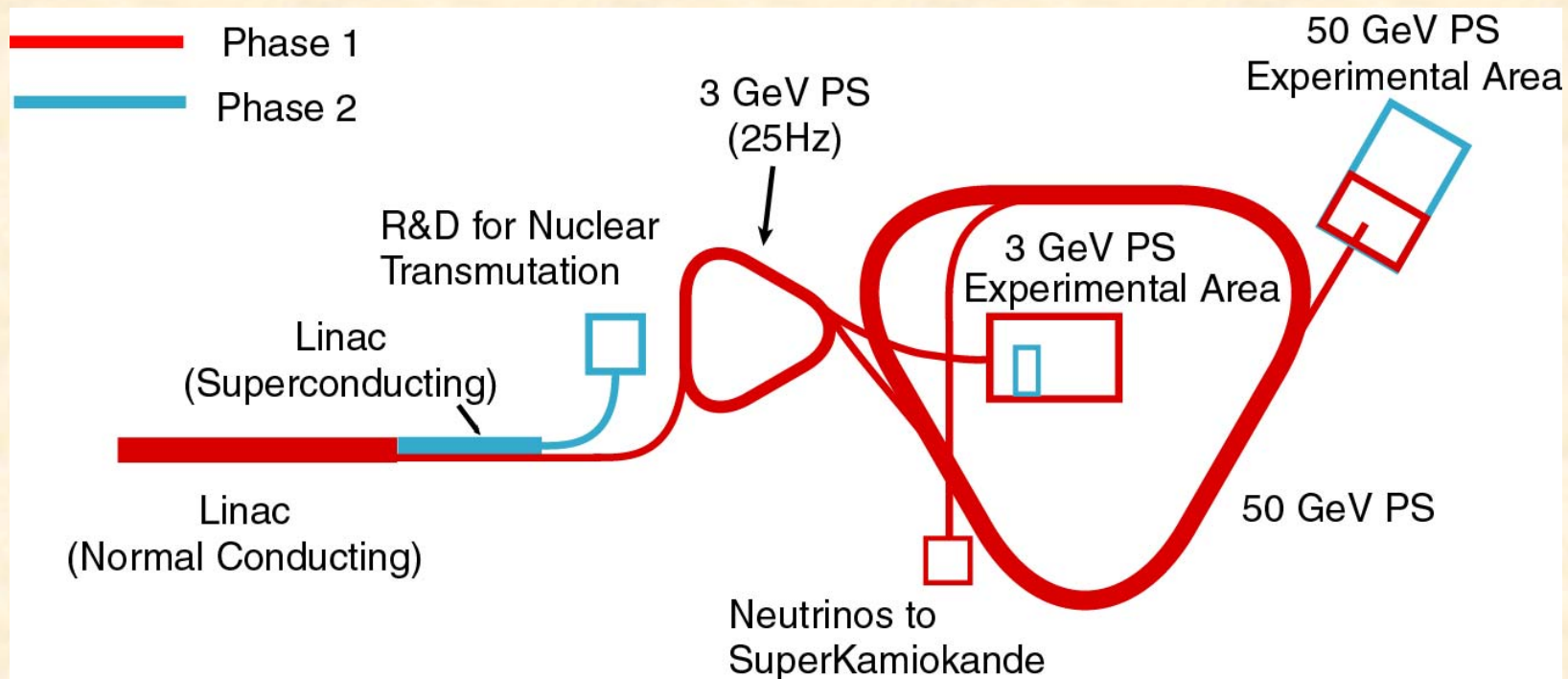
- **Hard processes (50 GeV recovery)**

- **Nucleon spin (proton polarization)**

- **Quark-hadron matter (heavy ion)**

Efforts are needed to get approval for projects after strangeness physics.

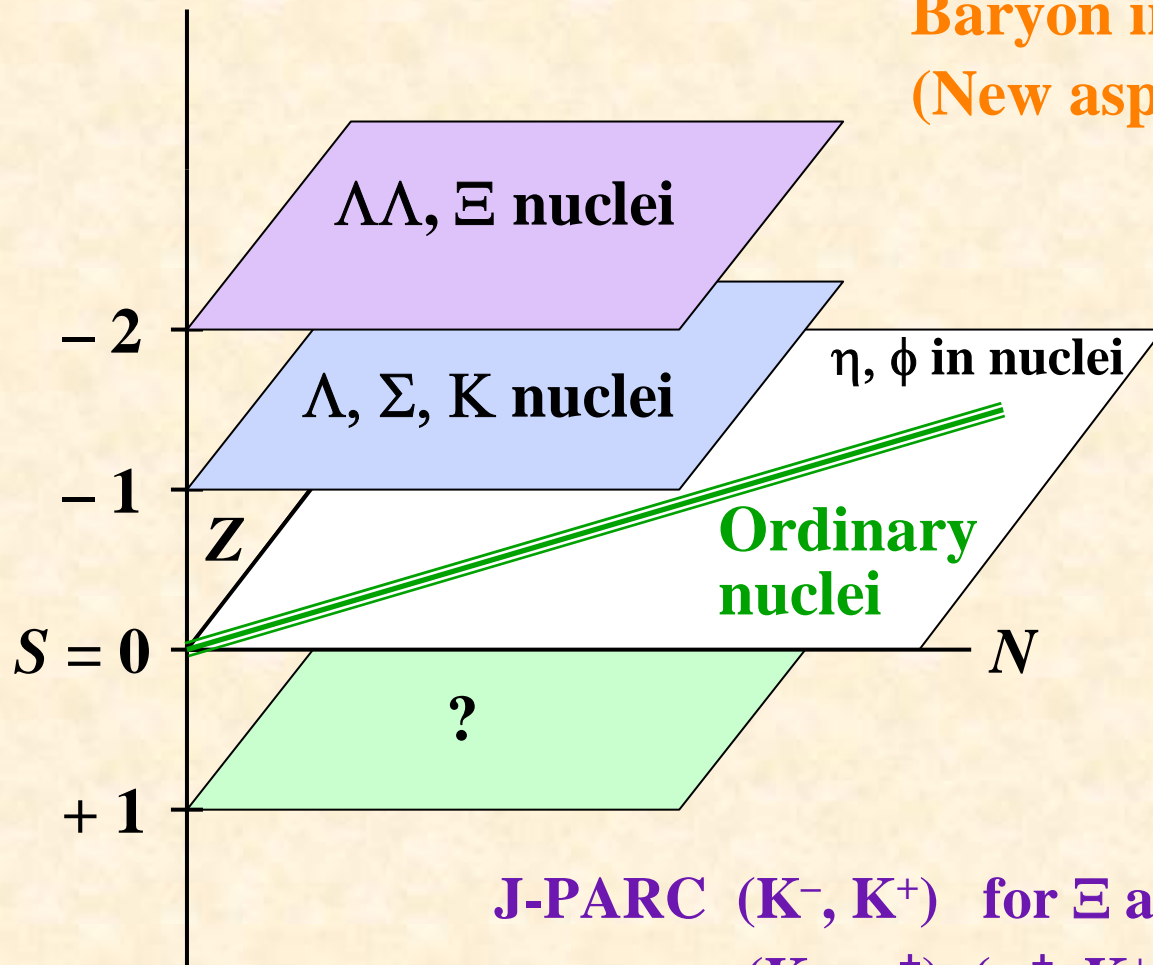
Theorist's contributions are crucial for the 2nd projects.



New nuclei with strangeness

New hadronic many-body system
by extending the flavor degrees of freedom.

**Baryon interactions with strangeness
(New aspect of low-energy QCD)**



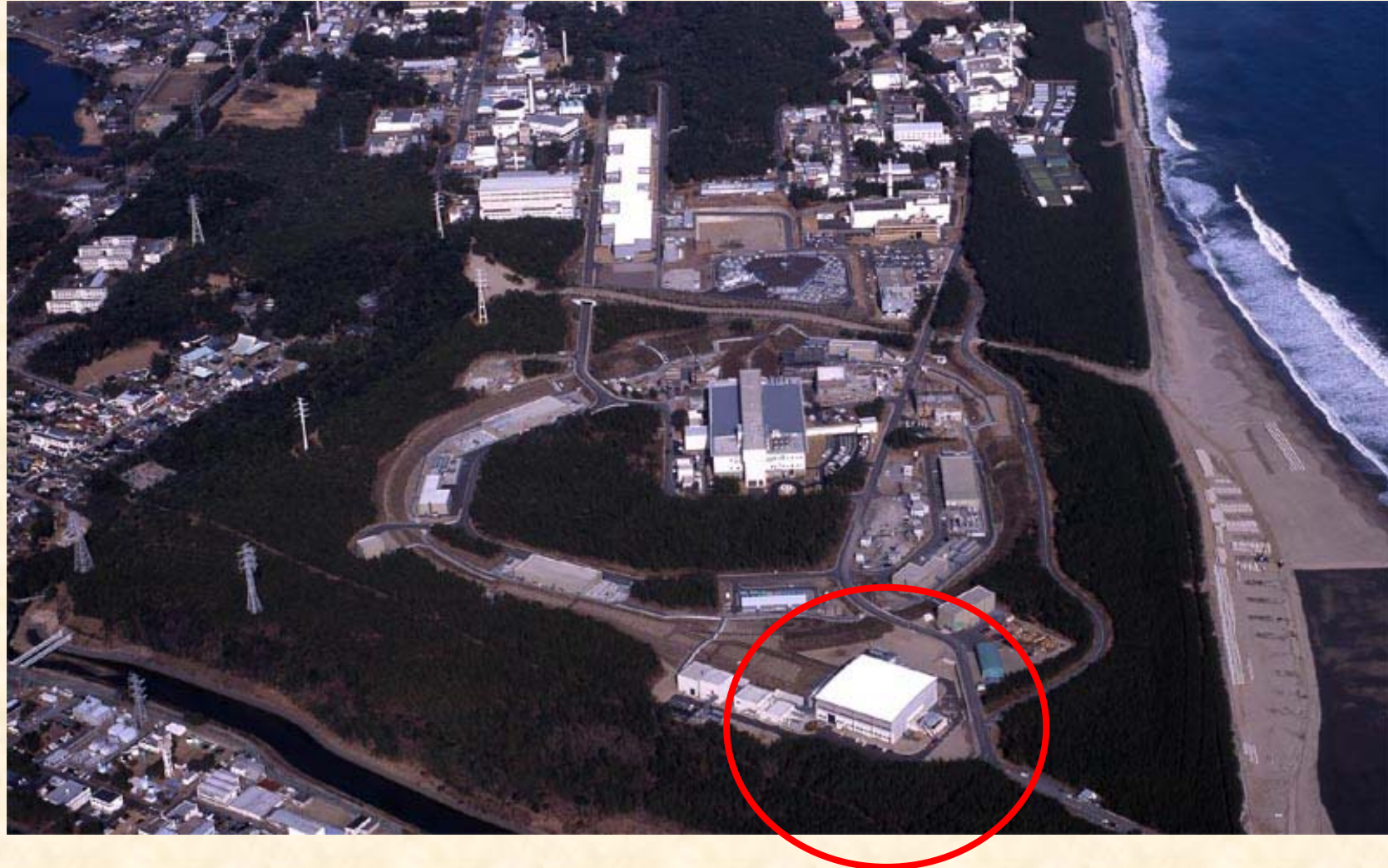
• No data for YY interactions

• Some data
for YN interactions (~ 40)

• Plenty of data
for NN interactions (~ 4,000)

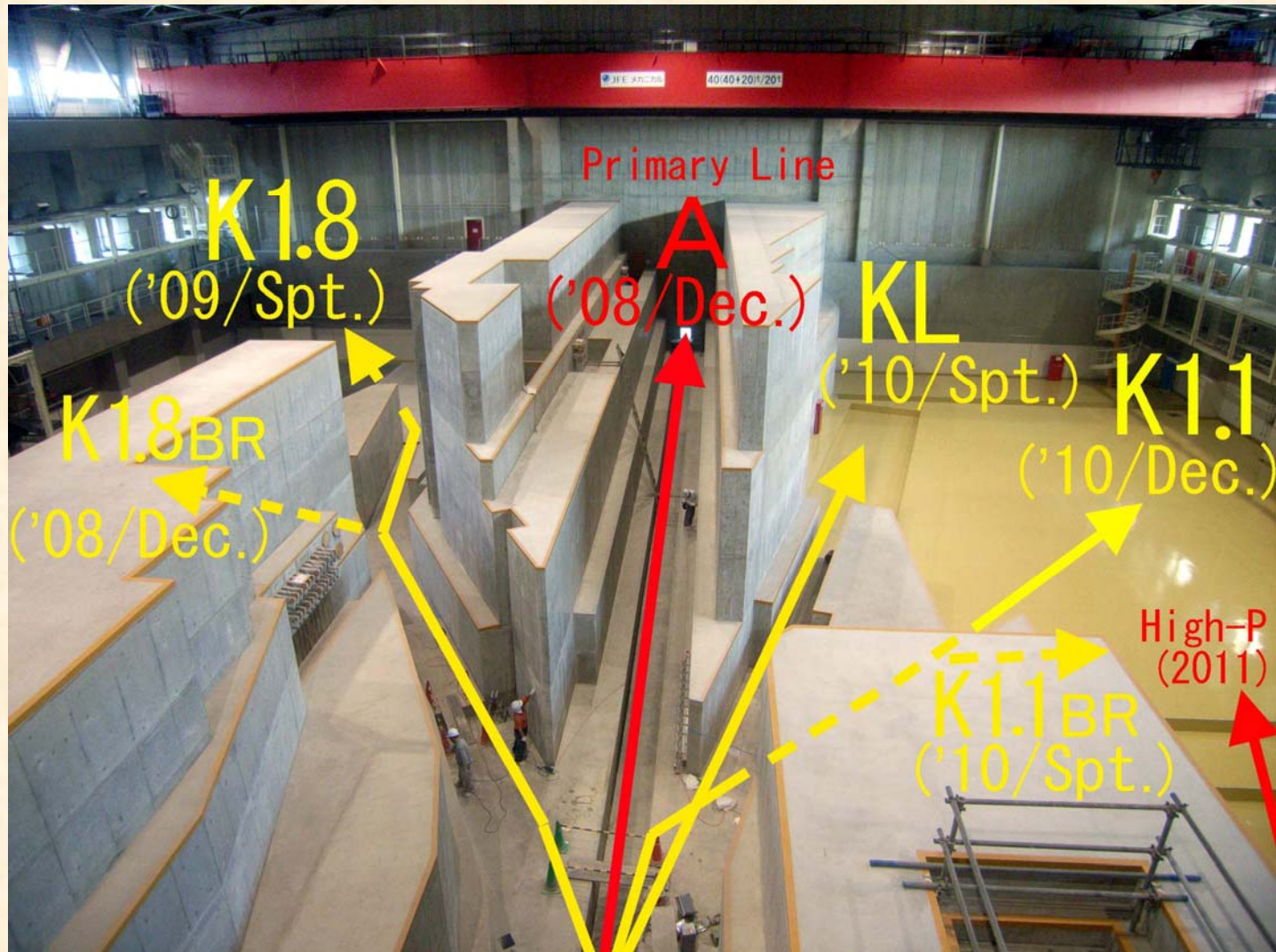
**J-PARC (K^- , K^+) for Ξ and $\Lambda\Lambda$ nuclei, YN scattering
(K^- , π^\pm), (π^\pm , K^+) for Λ nuclei, YN scattering**

Aerial photograph on January 28, 2008



Hadron facility

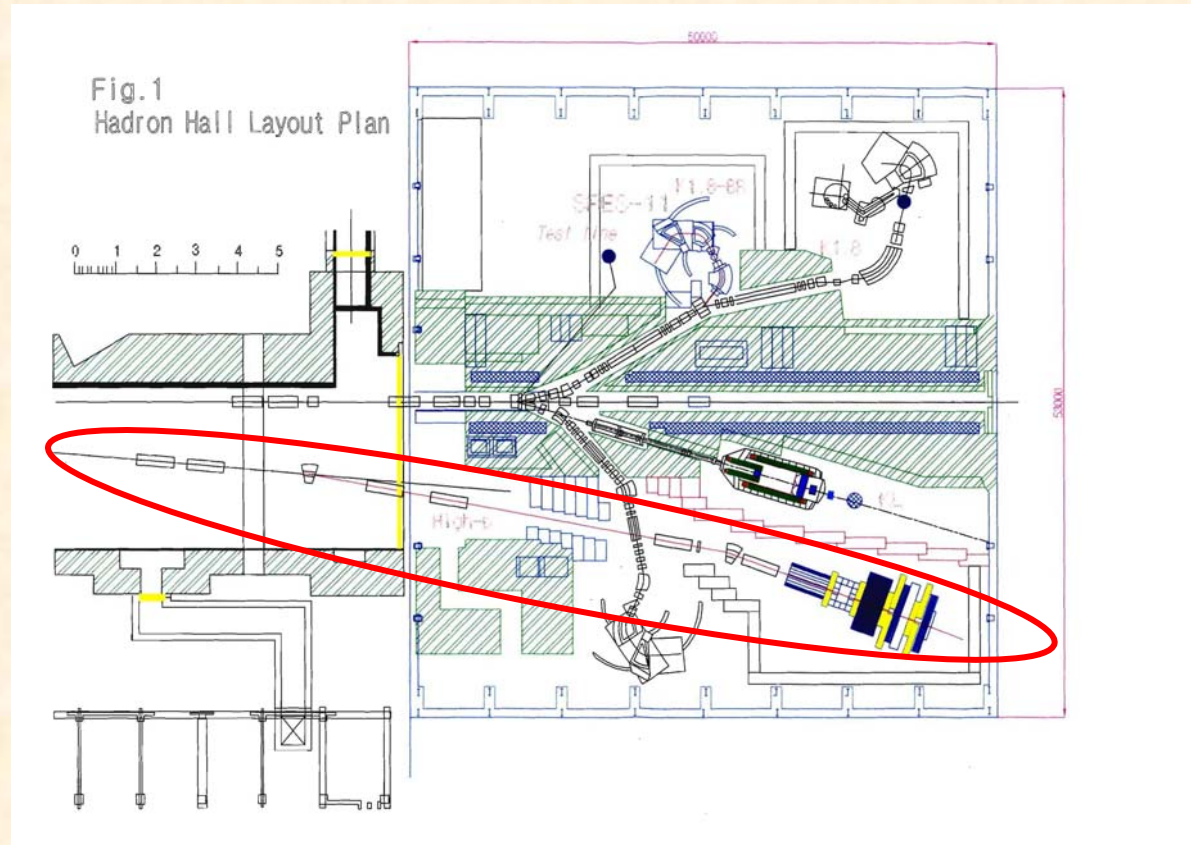
Hadron Facility in May 2007 and a possible schedule for beam lines



Hadron Facility on April 11, 2008



High-Momentum Beam Line (30, 50 GeV Proton)



This beam line should be interesting for the audience of this workshop.

General comments on J-PARC projects with 30 – 50 GeV proton beam

J-PARC workshops on hadron physics

- J-PARC-HS05,
<http://www-conf.kek.jp/J-PARC-HS05/program.html>
- J-PARC-NP07,
http://www-conf.kek.jp/NP_JPARC/program.html
- J-PARC-NP08, <http://j-parc.jp/NP08/>

Refs. My talks on “Possible Hadron Physics at J-PARC”

in Trieste (2006) <http://www.pg.infn.it/hadronic06/>

in Ghent (2007) <http://inwpent5.ugent.be/workshop07/>

in Mito (2008) <http://j-parc.jp/NP08/>

Hadron Physics at J-PARC

*1st project
(also ν)*

- **Strangeness nuclear physics (1st experiment)**
Kaon and pion beams

- **Exotic hadrons**

- **Hadrons in nuclear medium** Proton beam

Next projects

- **Hard processes** (50 GeV recovery)

- **Nucleon spin** (proton polarization)

*Need major
upgrades*

- **Quark-hadron matter** (heavy ion) ↑
My talk is related to

Hadron physics with 30 – 50 GeV proton beam

30 GeV • J/ψ production

- Transition: Hadron → Quark degrees of freedom
- Hadron interactions in nuclear medium
- Short-range *NN* interactions
- GPDs
- ...

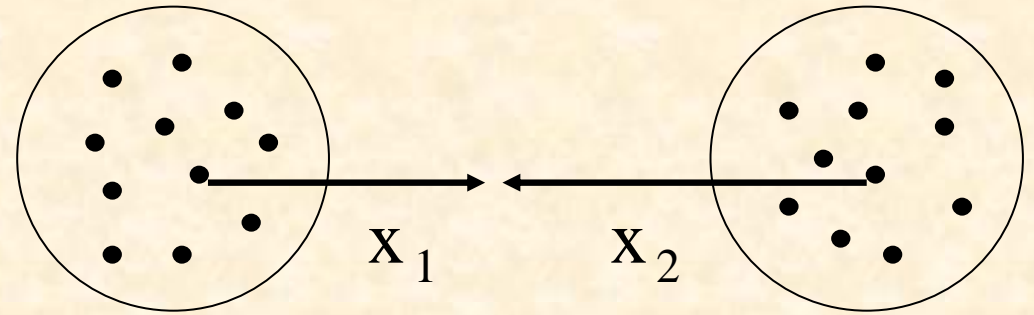
50 GeV • Drell-Yan (unpolarized PDFs)

- Single spin asymmetries
- Tensor structure at 50 GeV (Spin-1 hadrons)
- Fragmentation functions (Hadron productions)
- ...

Proton-beam polarization

- Drell-Yan: Double asymmetries (Polarized PDFs)
- Complimentary to RHIC-Spin (large-*x* physics)
- ...

Hadron facilities



e.g. Drell-Yan: $x_1 x_2 = \frac{m_{\mu\mu}^2}{s}$

$x : \frac{\sqrt{m_{\mu\mu}^2}}{\sqrt{s}}$

$p + p(A) \rightarrow \mu^+ \mu^- + X \quad (q\bar{q} \rightarrow \mu^+ \mu^-)$

- $s = (p_1 + p_2)^2$

J-PARC: $\sqrt{s} = 10 \text{ GeV}$

RHIC: $\sqrt{s} = 200 \text{ GeV}$

- $m_{\mu\mu} \geq 3 \text{ GeV}$

LHC: $\sqrt{s} = 14 \text{ TeV}$

$x : \frac{\sqrt{m_{\mu\mu}^2}}{\sqrt{s}} \geq \frac{3}{10} = 0.3$

J-PARC

**Large-x facility
(Medium-x)**

$\geq \frac{3}{200} = 0.02$

RHIC

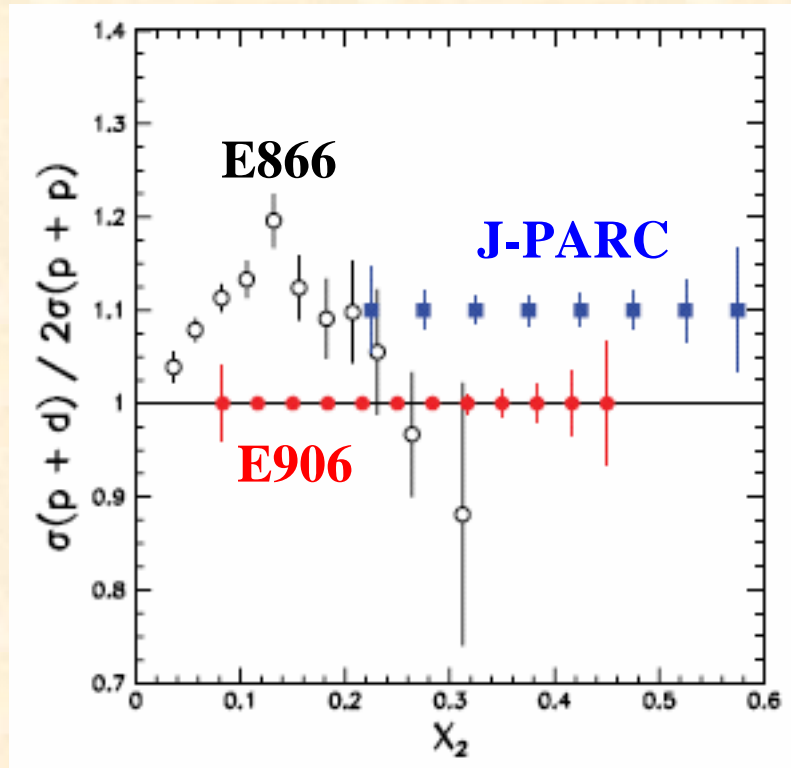
$\geq \frac{3}{14000} = 0.0002$

LHC

Small-x facility

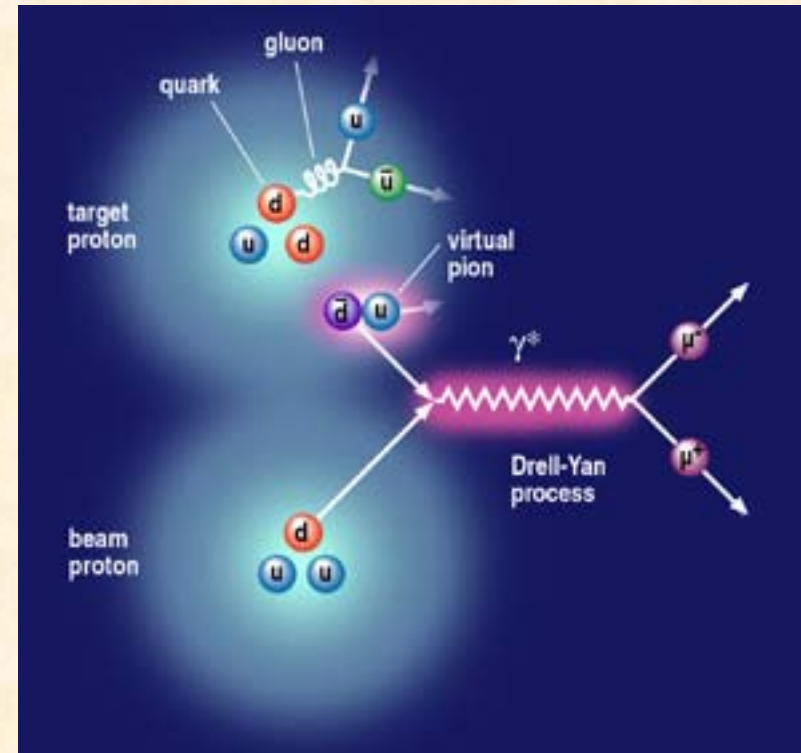
Flavor asymmetric antiquark distributions: \bar{u} / \bar{d}

J.-C. Peng's talk



J-PARC proposal, M. Bai *et al.* (2007)

This project is suitable for probing
“peripheral structure” of the nucleon.



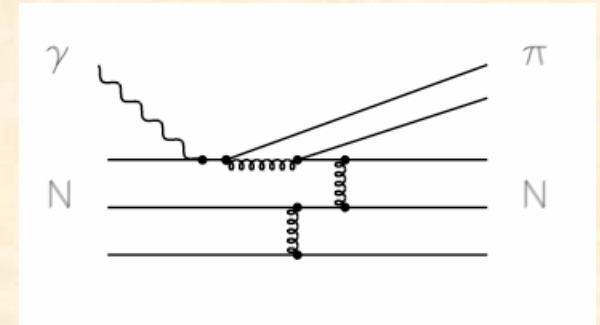
<http://www.acuonline.edu/academics/cas/physics/research/e906.html>

SK, Phys. Rep. 303 (1998) 183;
G. T. Garvey and J.-C. Peng,
Prog. Part. Nucl. Phys. 47 (2001) 203.

Elastic Scattering: $A+B \rightarrow C+D$ at large p_T

Brodsky@J-PARC-HS05

Transition from hadron degrees of freedom to quark-gluon d.o.f.



$\gamma p \rightarrow \pi^+ n$ H. Gao

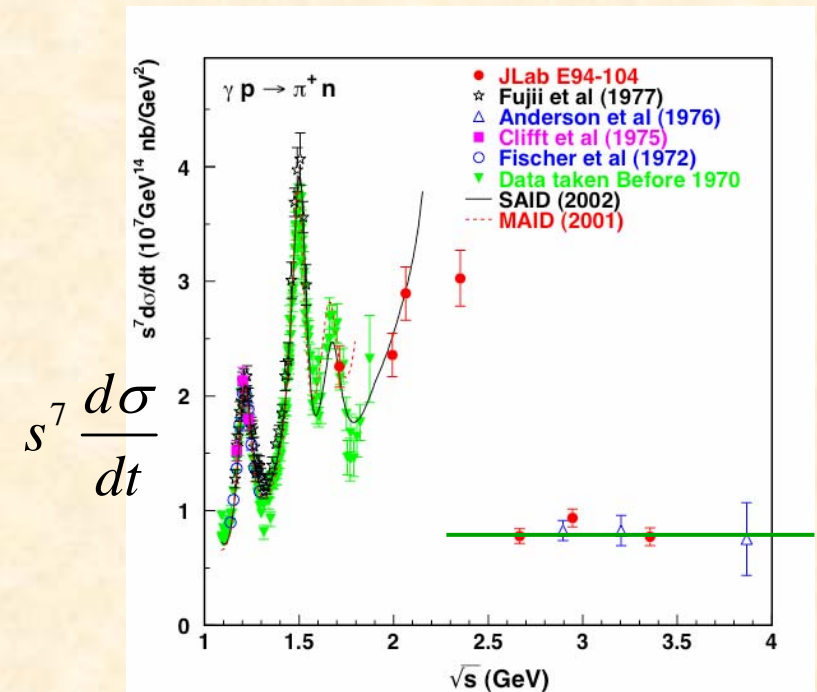
Constituent counting rule

$$\frac{d\sigma}{dt}(AB \rightarrow CD) : s^{2-n} f(\theta_{c.m.})$$

$$n = n_A + n_B + n_C + n_D$$

(total number of interacting elementary particles)

J-PARC: $p + p \rightarrow p + p$



L.Y. Zhu et al.,
PRL 91 (2003) 022003

Color Transparency

“Probe of dynamics of elementary reactions”

At large momentum transfer, a small-size component of the hadron wave function should dominate. This small-size hadron could freely pass through nuclear medium. (Transparent)

Brodsky, Strikman@J-PARC-HS05

Possibility at J-PARC

Investigate $p A \rightarrow p p (A-1)$

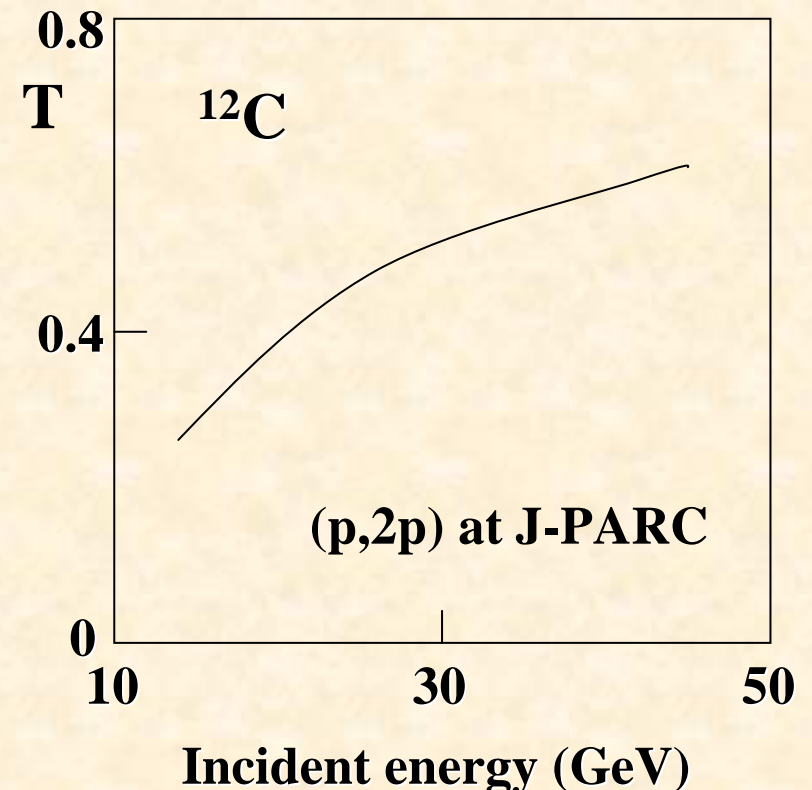
$$\text{Nuclear transparency: } T = \frac{\sigma_A}{A\sigma_N}$$

Hadron size $\sim 1 / \text{hard scale}$

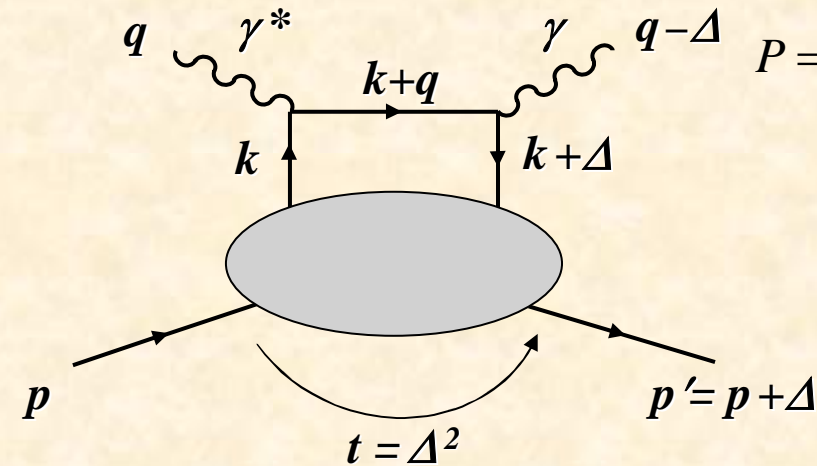
Color transparency:

$T \rightarrow \text{larger, as the hard scale} \rightarrow \text{larger}$

(BNL-EVA) J. Aclander et al.,
PRC 70 (2004) 015208



Generalized Parton Distributions (GPDs)



$$P = \frac{p^+ + p'^+}{2}, \quad \Delta = p' - p$$

GPDs are defined as correlation of off-forward matrix.

Bjorken variable $x = \frac{Q^2}{2p \cdot q}$

Momentum transfer squared $t = \Delta^2$

Skewness parameter $\xi = \frac{p'^+ - p^+}{p^+ + p'^+} = -\frac{\Delta^+}{2P^+}$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{\psi}(-z/2) \gamma^+ \psi(z/2) | p \rangle \Big|_{z^+=0, z_\perp=0} = \frac{1}{2P^+} \left[H(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u(p) \right]$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{\psi}(-z/2) \gamma^+ \gamma_5 \psi(z/2) | p \rangle \Big|_{z^+=0, z_\perp=0} = \frac{1}{2P^+} \left[\mathring{H}(x, \xi, t) \bar{u}(p') \gamma^+ \gamma_5 u(p) + \mathring{E}(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^+}{2M} u(p) \right]$$

Forward limit: PDFs

$$H(x, \xi, t) \Big|_{\xi=t=0} = f(x), \quad \mathring{H}(x, \xi, t) \Big|_{\xi=t=0} = \Delta f(x)$$

First moments: Form factors

There is no analog in E and \mathring{E}

Dirac and Pauli form factors F_1, F_2

$$\int dx H(x, \xi, t) = F_1(t), \quad \int dx E(x, \xi, t) = F_2(t)$$

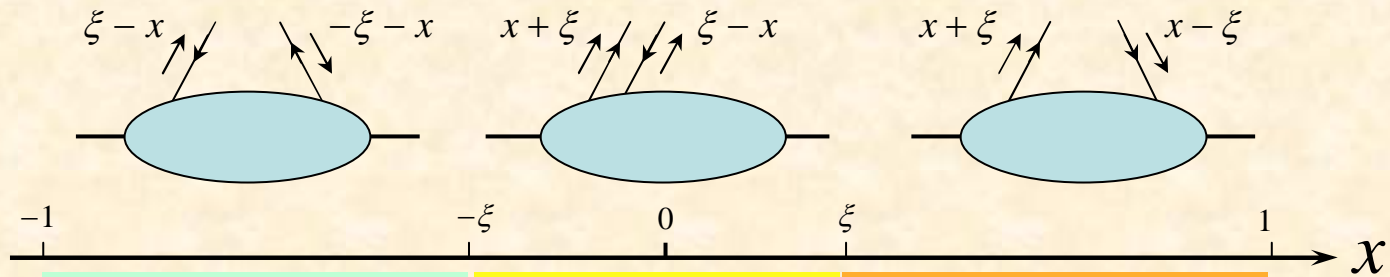
Axial and Pseudoscalar form factors G_A, G_P

$$\int dx \mathring{H}(x, \xi, t) = G_A(t), \quad \int dx \mathring{E}(x, \xi, t) = G_P(t)$$

Second moments: Angular momenta

Sum rule: $J_q = \frac{1}{2} \int dx x \left[H_q(x, \xi, t=0) + E_q(x, \xi, t=0) \right], \quad J_q = \frac{1}{2} \Delta q + L_q$

GPDs in different x regions and GPDs at J-PARC



$$-1 < x < \xi \quad (x + \xi < 0, x - \xi < 0)$$

$$\xi < x < 1 \quad (x + \xi > 0, x - \xi > 0)$$

$$-\xi < x < \xi \quad (x + \xi > 0, x - \xi < 0)$$

Quark distribution

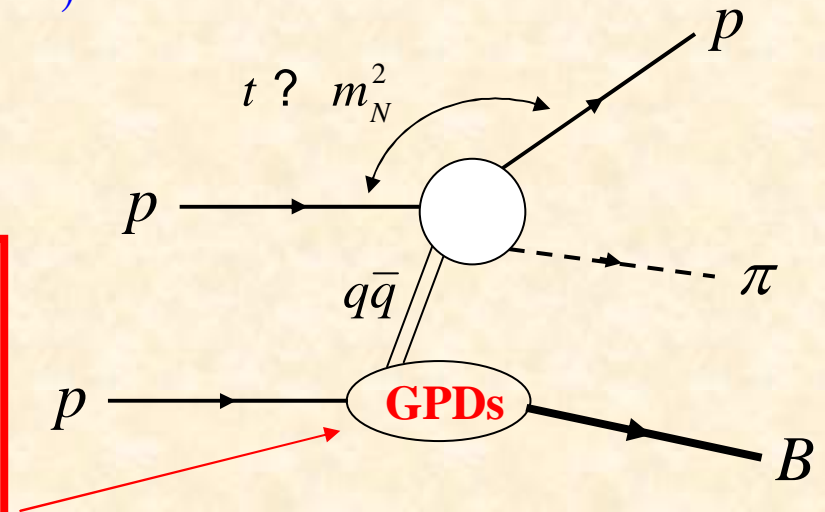
Emission of quark with momentum fraction $x + \xi$
 Absorption of quark with momentum fraction $x - \xi$

Meson distribution amplitude

Emission of quark with momentum fraction $x + \xi$
 Emission of antiquark with momentum fraction $\xi - x$

Antiquark distribution

Emission of antiquark with momentum fraction $\xi - x$
 Absorption of antiquark with momentum fraction $-x - \xi$



GPDs at J-PARC:
 SK, M. Strikman, K. Sudoh,
 in progress.

Short-range NN interaction

Ciofi degli Atti@J-PARC-NP07

Strikman@INPC07

E. Piasezky et al.,
PRL97 (2006) 162504

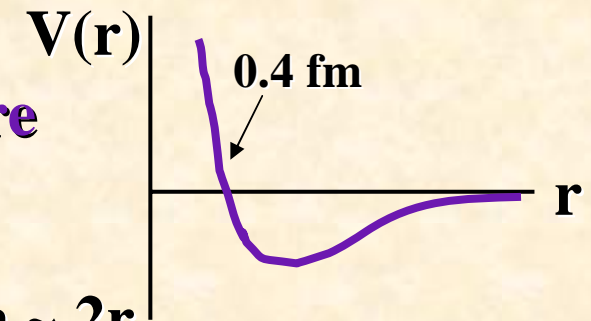
- Short-range repulsive core, Tensor force
- Quark degrees of freedom
- Cold dense nuclear matter, Neutron star

Nuclei do not collapse → Short-range repulsive core

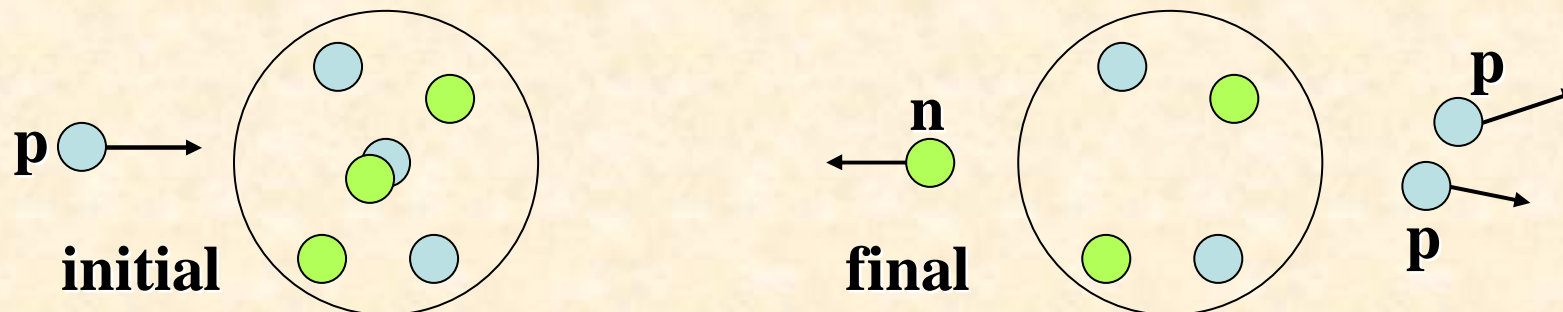
Nucleon size $r \approx 0.8$ fm

Average nucleon separation in a nucleus: $R \approx 2$ fm $\sim 2r$

→ The short-range part is important as the density becomes larger (neutron star).



$A(p, 2pN)X$ experiment for short range correlation



Single spin asymmetry (No polarized proton beam is needed!)

$$A_N = \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow}$$

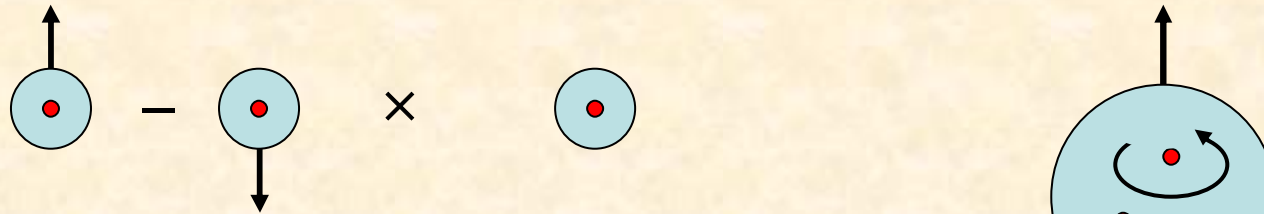
- Sivers effect



Nucleon

- Quark

$$A_N : f_{1T}^\perp \cdot D_1 \quad (\text{Sivers function} \times \text{Unpolarized fragmentation})$$



The Sivers function describes unpolarized quark in the transversely polarized nucleon.

Burkardt
@J-PARC-HS05

Probe of angular momentum

- Collins effect



$$A_N : \delta_T q \cdot H_1^\perp \quad (\text{Transversity} \times \text{Collins fragmentation function})$$

The transversity distribution describes transverse quark polarization in the transversely polarized nucleon.

The Collins fragmentation function describes a fragmentation of polarized quark into unpolarized hadron.

- Higher-twist

Qiu, Sterman; Koike@J-PARC-HS05

Part II

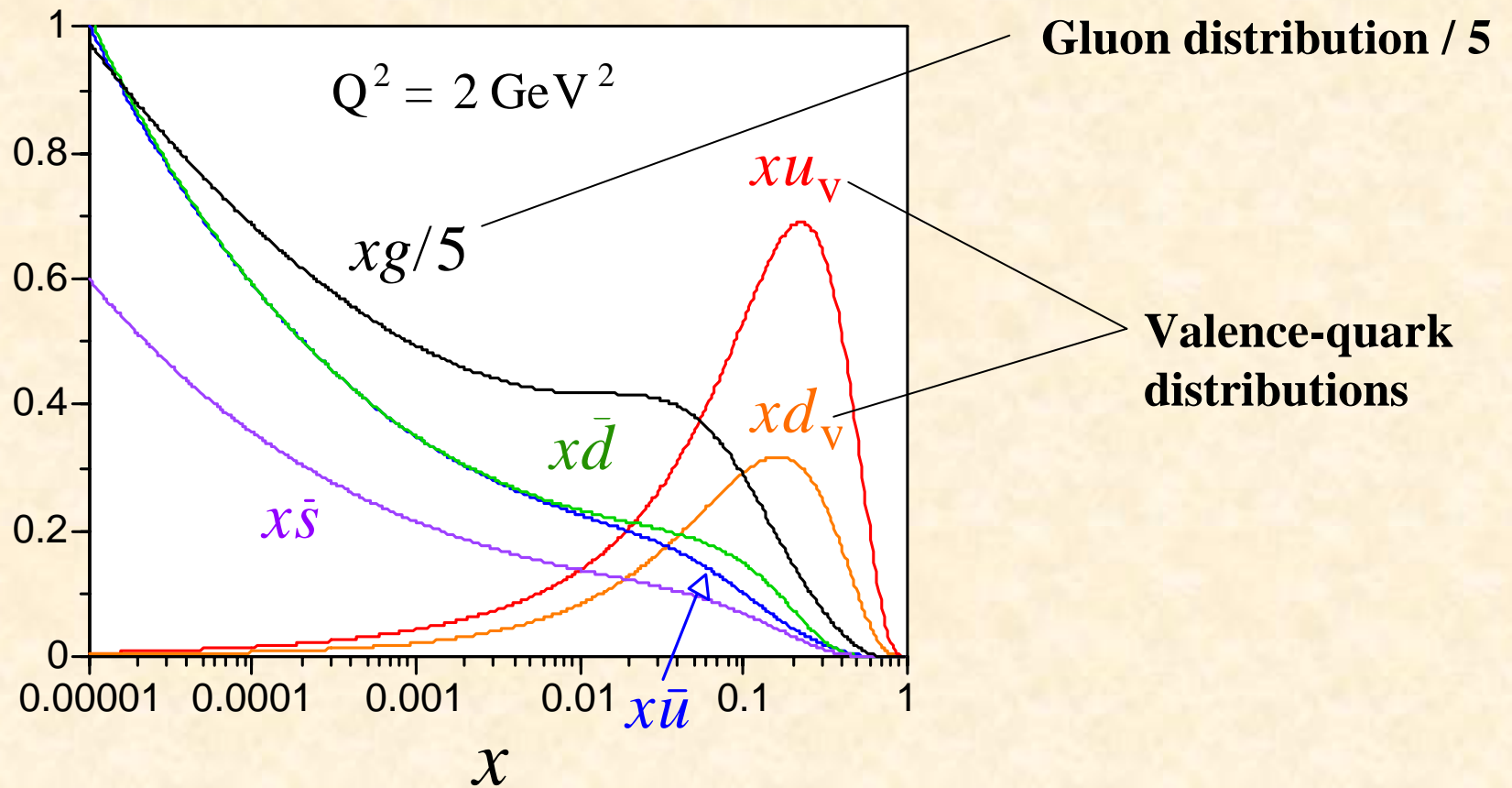
Parton Distribution Functions and Fragmentation Functions

in connection with J-PARC

Unpolarized Parton Distribution Functions (PDFs) in the nucleon

The PDFs could be obtained from

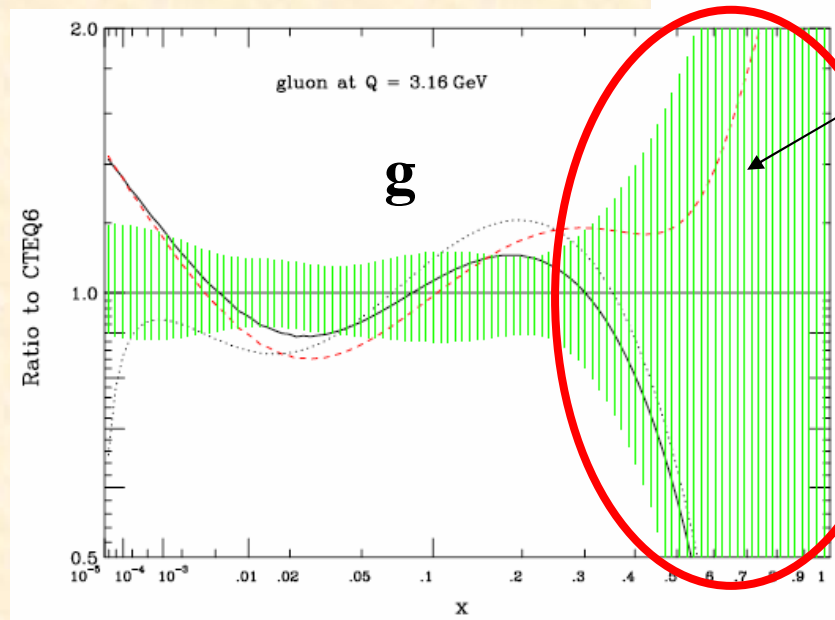
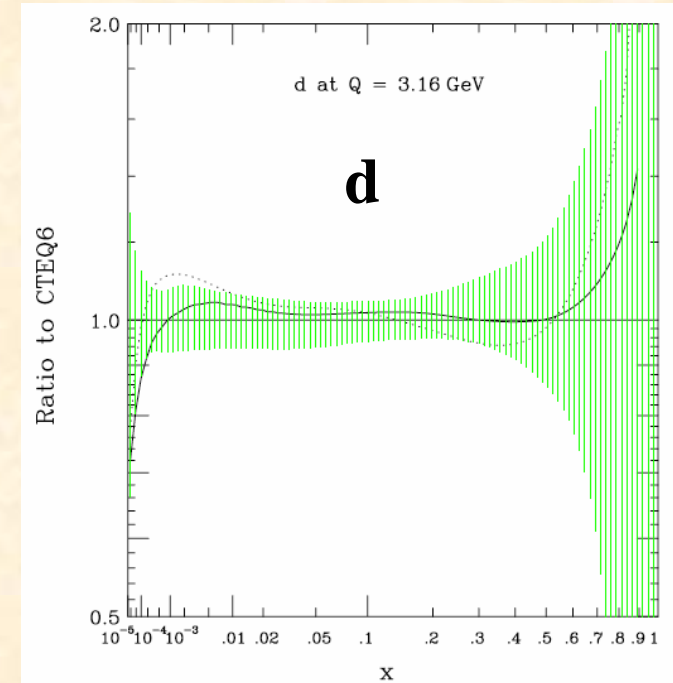
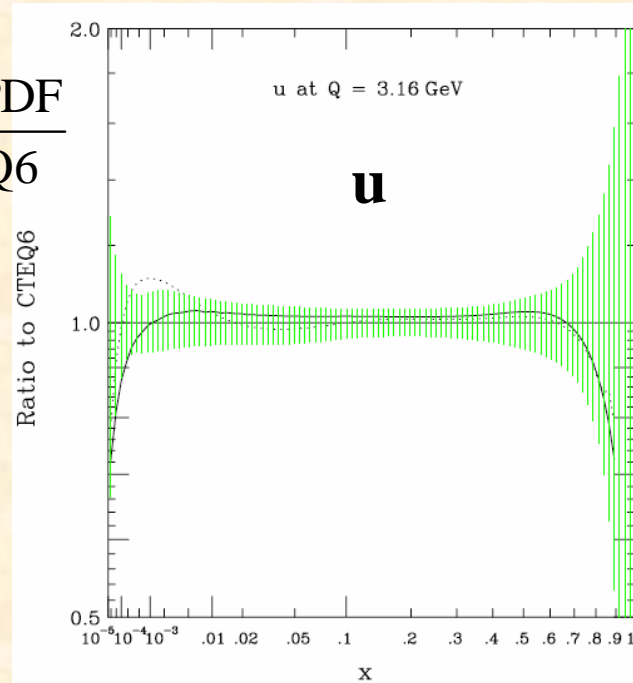
<http://durpdg.dur.ac.uk/hepdata/pdf.html>



PDF uncertainty

other PDF
CTEQ6
CTEQ6 (J. Pumplin *et al.*),
JHEP 0207 (2002) 012

———— CTEQ5M1
..... MRS2001
- - - - CTEQ5HJ



Important x region for finding an “exotic event” in a high- p_T region at LHC

J-PARC x region

If processes are well understood theoretically including pQCD terms, J-PARC measurements are important for finding new physics at LHC or possibly in cosmic rays.

Nuclear Parton Distribution Functions

<http://research.kek.jp/people/kumanos/nuclp.html>

Experimental data: total number = 1241

(1) F_2^A / F_2^D 896 data

NMC: p, He, Li, C, Ca

SLAC: He, Be, C, Al,
Ca, Fe, Ag, Au

EMC: C, Ca, Cu, Sn

E665: C, Ca, Xe, Pb

BCDMS: N, Fe

HERMES: N, Kr

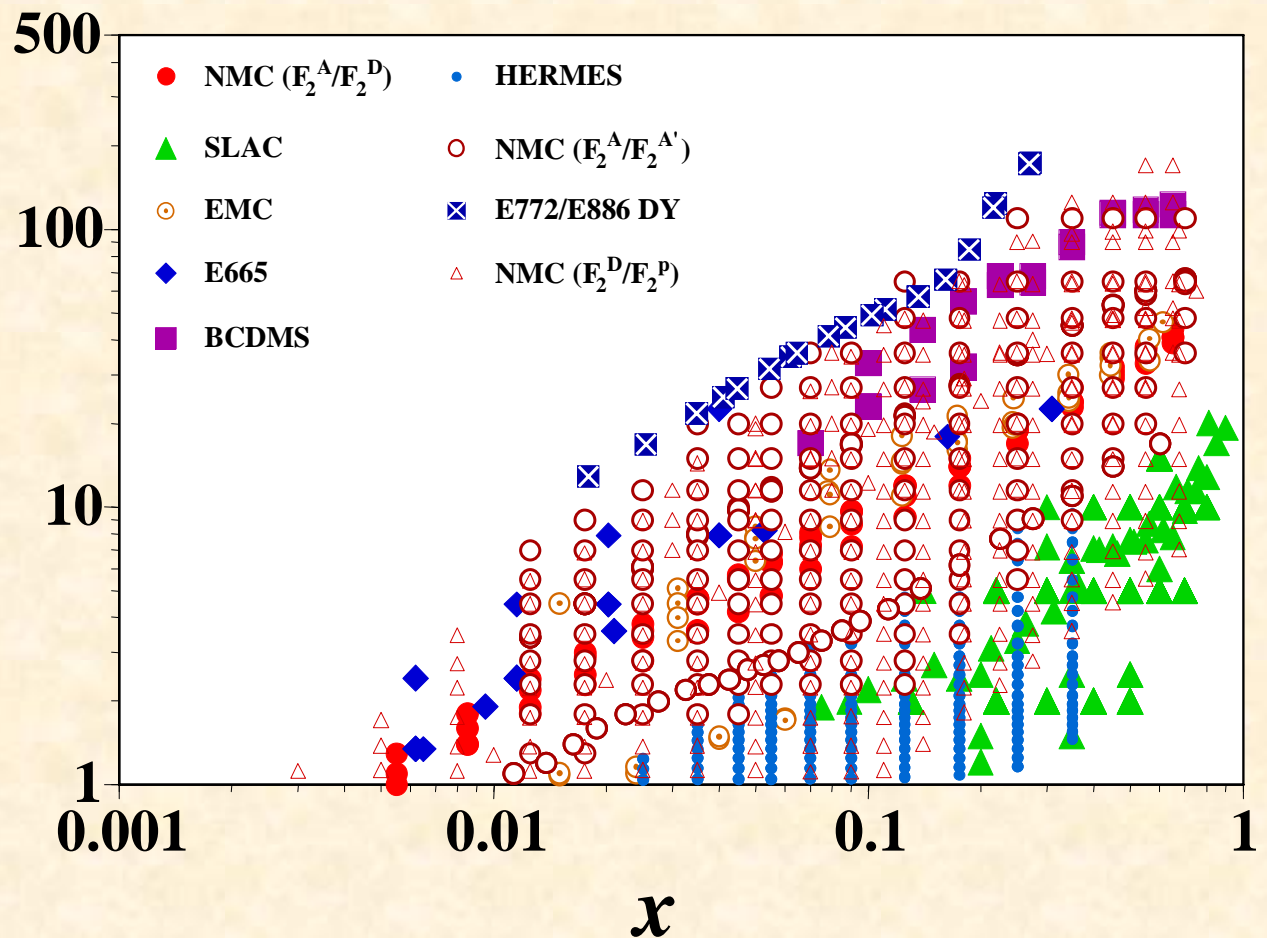
(2) $F_2^A / F_2^{A'}$ 293 data

NMC: Be / C, Al / C,
Ca / C, Fe / C,
Sn / C, Pb / C,
C / Li, Ca / Li

(3) $\sigma_{DY}^A / \sigma_{DY}^{A'}$ 52 data

E772: C / D, Ca / D,
Fe / D, W / D

E866: Fe / Be, W / Be



Functional form Nuclear PDFs “per nucleon”

If there were no nuclear modification

$$Au^A(x) = Zu^p(x) + Nu^n(x), \quad Ad^A(x) = Zd^p(x) + Nd^n(x) \quad p = \text{proton}, \quad n = \text{neutron}$$

Isospin symmetry :

$$u^n = d^p \equiv d, \quad d^n = u^p \equiv u$$

$$\rightarrow u^A(x) = \frac{Zu(x) + Nd(x)}{A}, \quad d^A(x) = \frac{Zd(x) + Nu(x)}{A}$$

Take account of nuclear effects by $w_i(x, A)$

$$u_v^A(x) = w_{u_v}(x, A) \frac{Zu_v(x) + Nd_v(x)}{A}, \quad d_v^A(x) = w_{d_v}(x, A) \frac{Zd_v(x) + Nu_v(x)}{A}$$

$$\bar{u}^A(x) = w_{\bar{q}}(x, A) \frac{Z\bar{u}(x) + N\bar{d}(x)}{A}, \quad \bar{d}^A(x) = w_{\bar{q}}(x, A) \frac{Z\bar{d}(x) + N\bar{u}(x)}{A}$$

$$\bar{s}^A(x) = w_{\bar{q}}(x, A) \bar{s}(x)$$

$$g^A(x) = w_g(x, A) g(x)$$

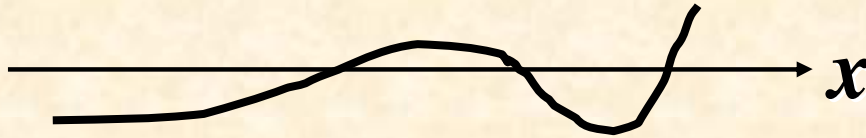
at $Q^2 = 1 \text{ GeV}^2 (\equiv Q_0^2)$

Functional form of $w_i(x, A)$

$$f_i^A(x, Q_0^2) = w_i(x, A) f_i(x, Q_0^2) \quad i = u_v, d_v, \bar{u}, \bar{d}, \bar{s}, g$$

$$w_i(x, A) = 1 + \left(1 - \frac{1}{A^\alpha}\right) \frac{a_i + b_i x + c_i x^2 + d_i x^3}{(1-x)^\beta}$$

Note: The region $x > 1$ cannot be described by this parametrization.



A simple function = cubic polynomial

Three constraints

Nuclear charge: $Z = A \int dx \left[\frac{2}{3} (u^A - \bar{u}^A) - \frac{1}{3} (d^A - \bar{d}^A) - \frac{1}{3} (s^A - \bar{s}^A) \right] = A \int dx \left[\frac{2}{3} u_v^A - \frac{1}{3} d_v^A \right]$

Baryon number: $A = A \int dx \left[\frac{1}{3} (u^A - \bar{u}^A) + \frac{1}{3} (d^A - \bar{d}^A) + \frac{1}{3} (s^A - \bar{s}^A) \right] = A \int dx \left[\frac{1}{3} u_v^A + \frac{1}{3} d_v^A \right]$

Momentum: $A = A \int dx \left[u^A + \bar{u}^A + d^A + \bar{d}^A + s^A + \bar{s}^A + g \right]$
 $= A \int dx \left[u_v^A + d_v^A + 2(\bar{u}^A + \bar{d}^A + \bar{s}^A) + g \right]$

Analysis conditions

- Nucleonic PDFs: **MRST98** [$\Lambda_{\text{QCD}} = 174 \text{ MeV (LO)}, 300 \text{ MeV (NLO)}$]
- Total number of parameter : **12**
- Total number of data : **1241 ($Q^2 \geq 1 \text{ GeV}^2$)**

$$896 (F_2^A/F_2^D) + 293 (F_2^A/F_2^{A'}) + 52 (\text{Drell-Yan})$$

- Subroutine for χ^2 analysis : **CERN-Minuit**

$$\chi^2 = \sum_i \frac{(R_i^{\text{data}} - R_i^{\text{theo}})^2}{(\sigma_i^{\text{data}})^2}$$

$$R = \frac{F_2^A}{F_2^D}, \quad \frac{F_2^A}{F_2^{A'}}, \quad \frac{\sigma^{pA}}{\sigma^{pA'}}$$

$$\sigma_i^{\text{data}} = \sqrt{(\sigma_i^{\text{sys}})^2 + (\sigma_i^{\text{stat}})^2}$$

$$\chi^2_{\text{min}} (\text{/d.o.f.}) = 1653.3 (1.35) \dots \text{LO}$$

$$= 1485.9 (1.21) \dots \text{NLO}$$

- Error estimate : **Hessian method**

$$[\delta F(x)]^2 = \Delta \chi^2 \sum_{i,j} \frac{\partial F(x)}{\partial \xi_i} H_{ij}^{-1} \frac{\partial F(x)}{\partial \xi_j}$$

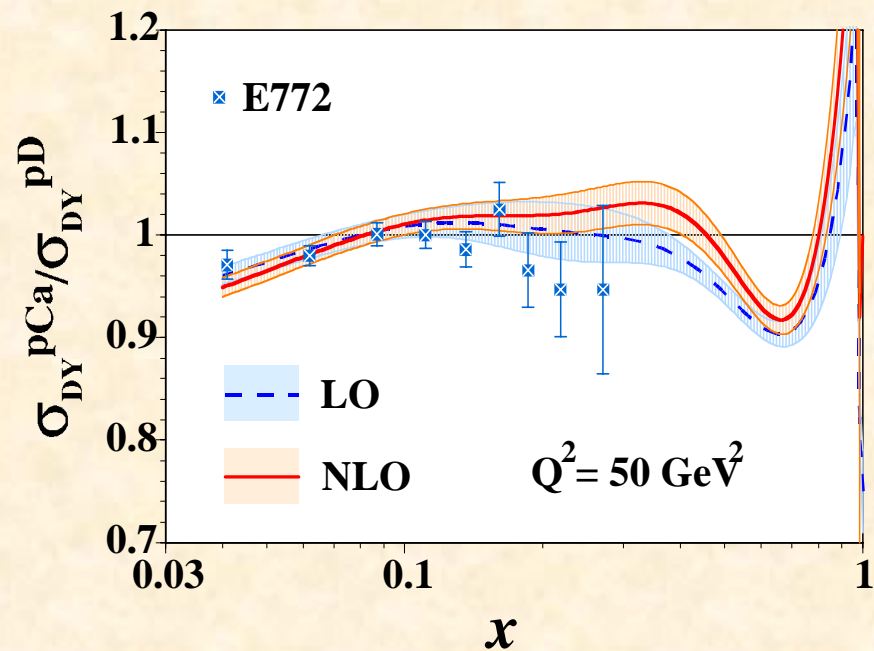
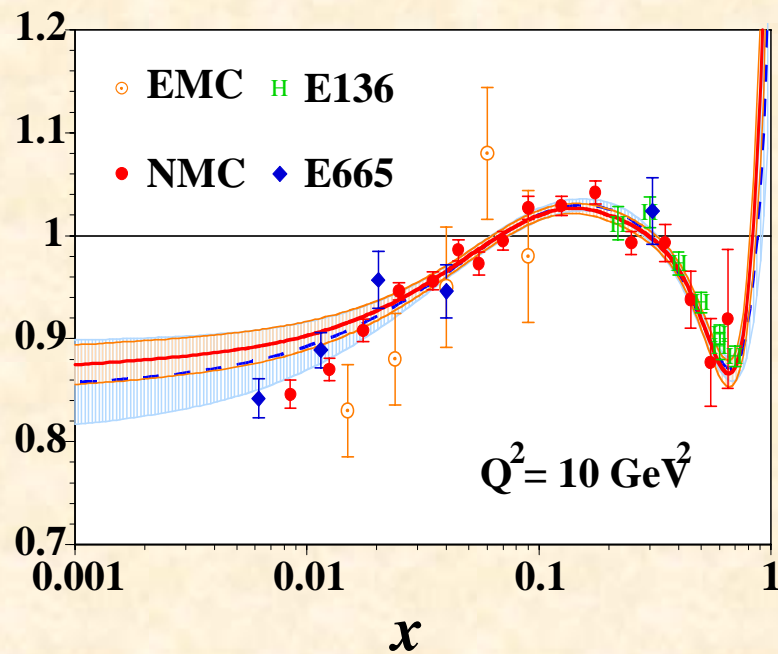
H_{ij} = Hessian

ξ_i = parameter

Comparison with $F_2^{\text{Ca}}/F_2^{\text{D}}$ & $\sigma_{\text{DY}}^{\text{pCa}}/\sigma_{\text{DY}}^{\text{pD}}$ data

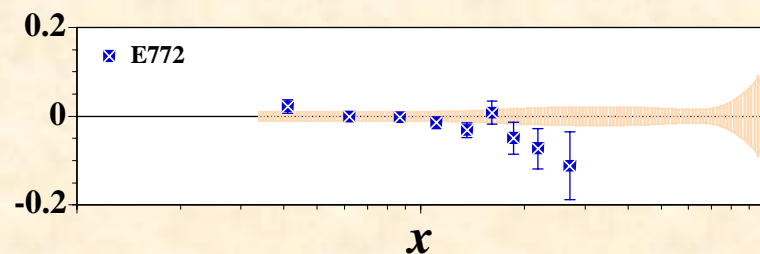
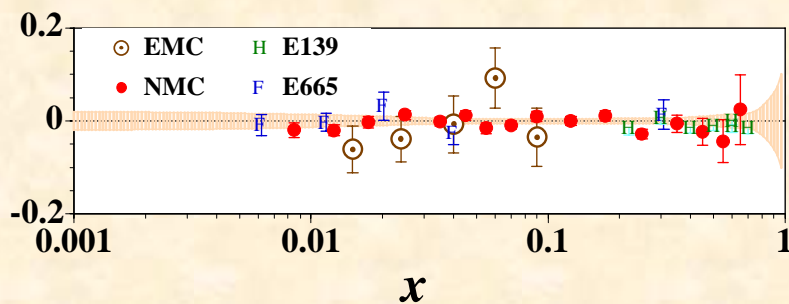
LO analysis

NLO analysis

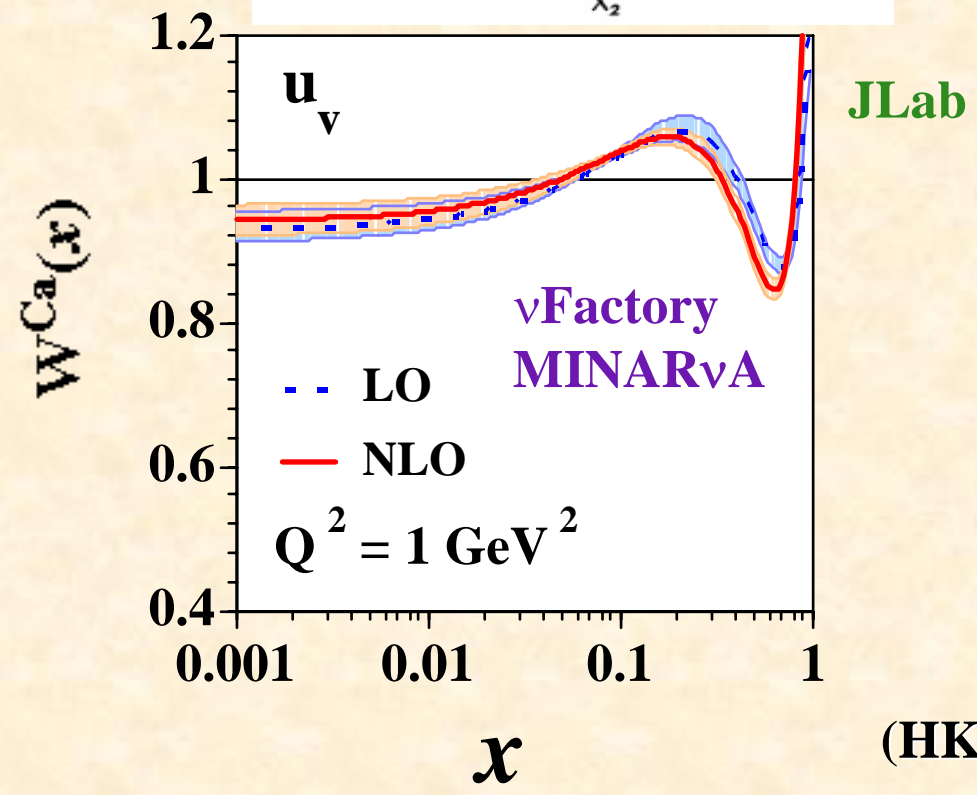
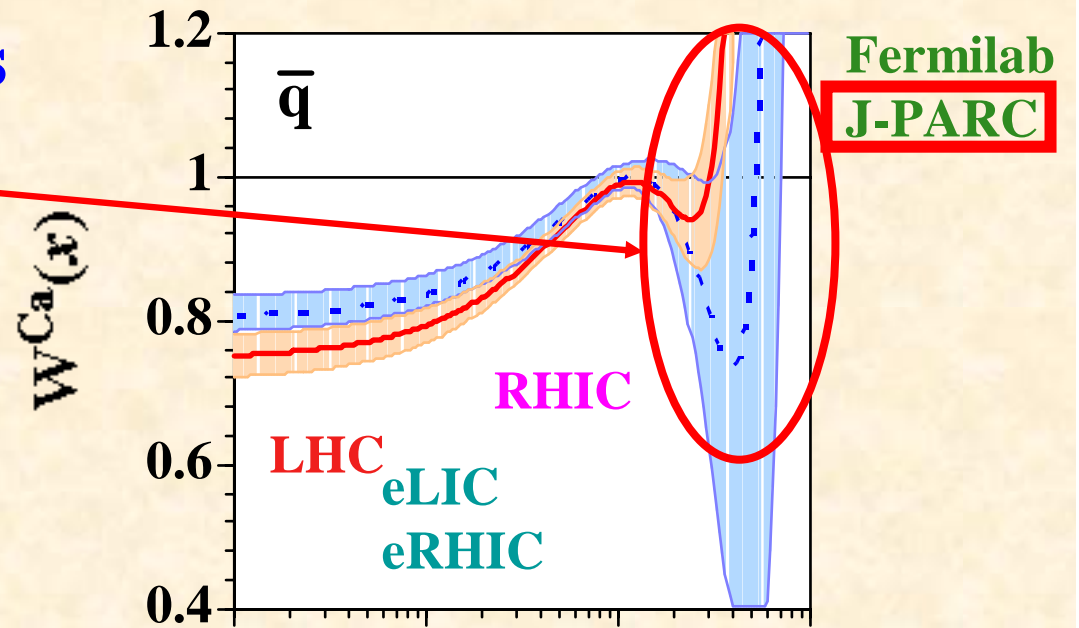
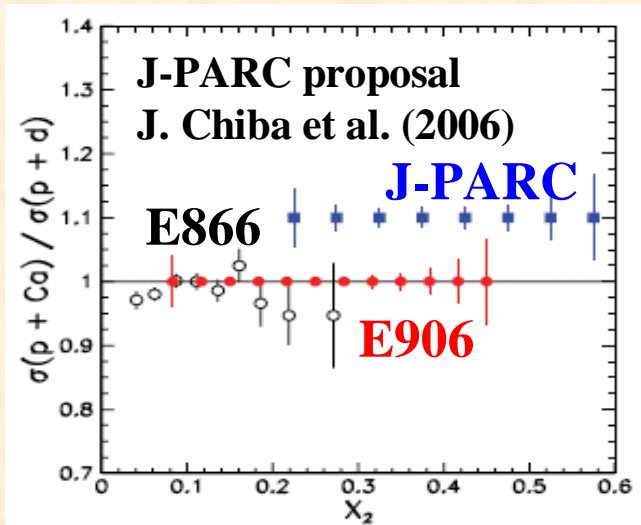


$(R^{\text{exp}} - R^{\text{theo}})/R^{\text{theo}}$ at the same Q^2 points

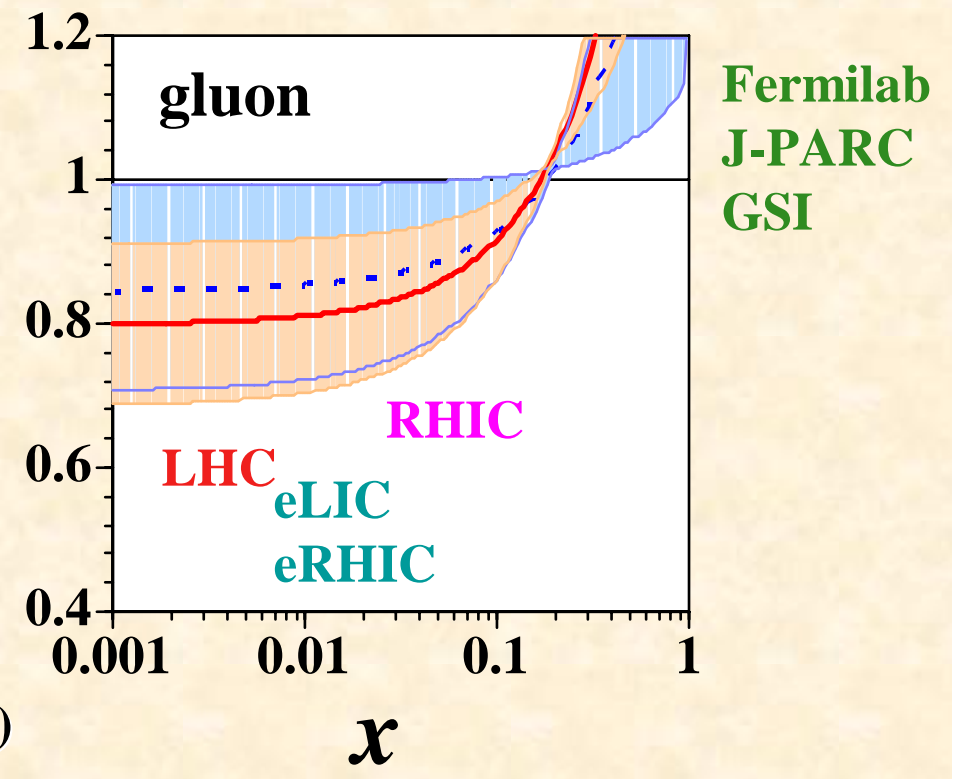
$R = F_2^{\text{Ca}}/F_2^{\text{D}}, \sigma_{\text{DY}}^{\text{pCa}}/\sigma_{\text{DY}}^{\text{pD}}$



Results & Future experiments



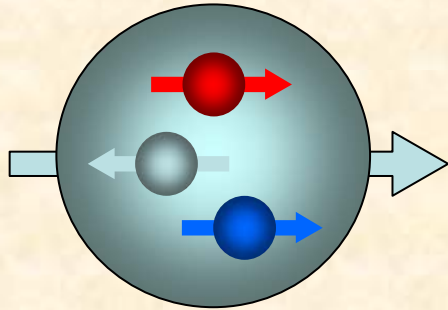
(HKN07)



Polarized Parton Distribution Functions

<http://spin.riken.bnl.gov/aac/>

Nucleon Spin



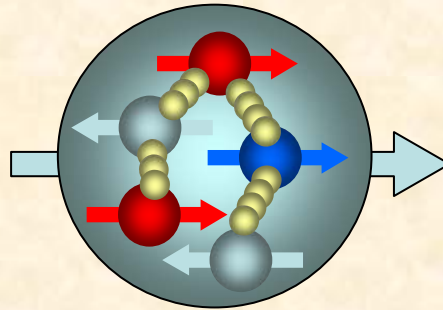
Naïve Quark Model

$$\Delta\Sigma = \Delta u_v + \Delta d_v = 1$$

Electron / muon scattering

$$\Delta\Sigma \approx 0.1 \sim 0.3$$

Almost none of nucleon spin is carried by quarks!



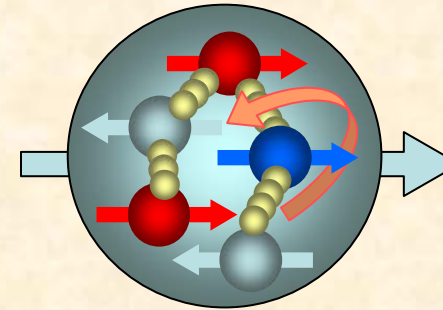
QCD

Sea-quarks and gluons?

Gluon: ΔG

Sea-quarks: Δq_{sea}

Recent data indicate ΔG is small at $x \sim 0.1$.



Orbital angular momenta ?

$$L_q, L_g$$

Future experiments

Nucleon Spin:

$$\frac{1}{2} = \frac{1}{2} \left(\underbrace{\Delta u_v + \Delta d_v + \Delta q_{sea}}_{\Delta\Sigma} \right) + \Delta G + L_q + L_g$$

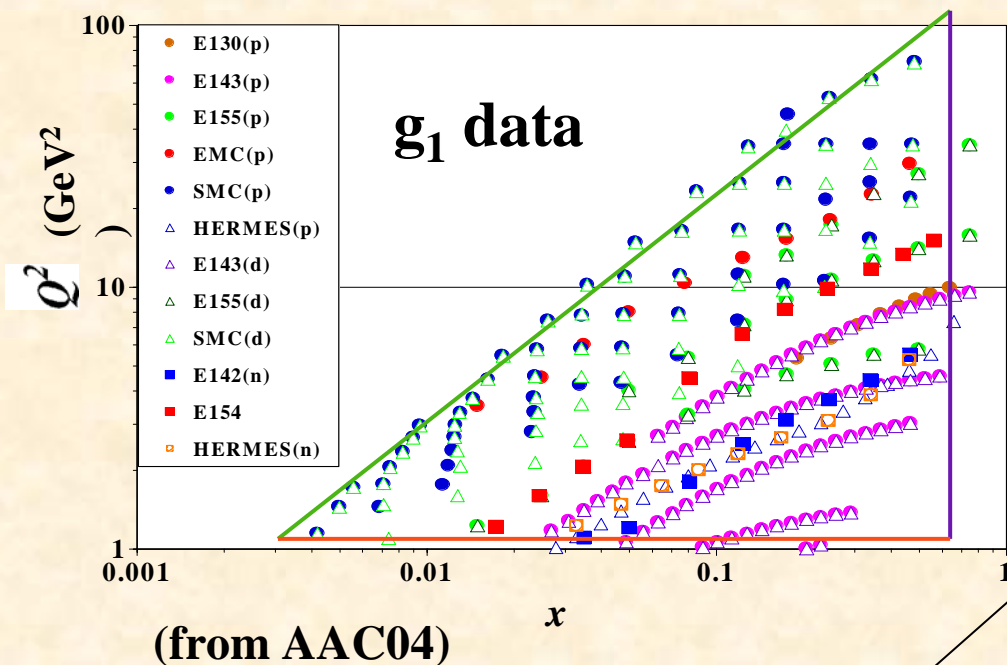
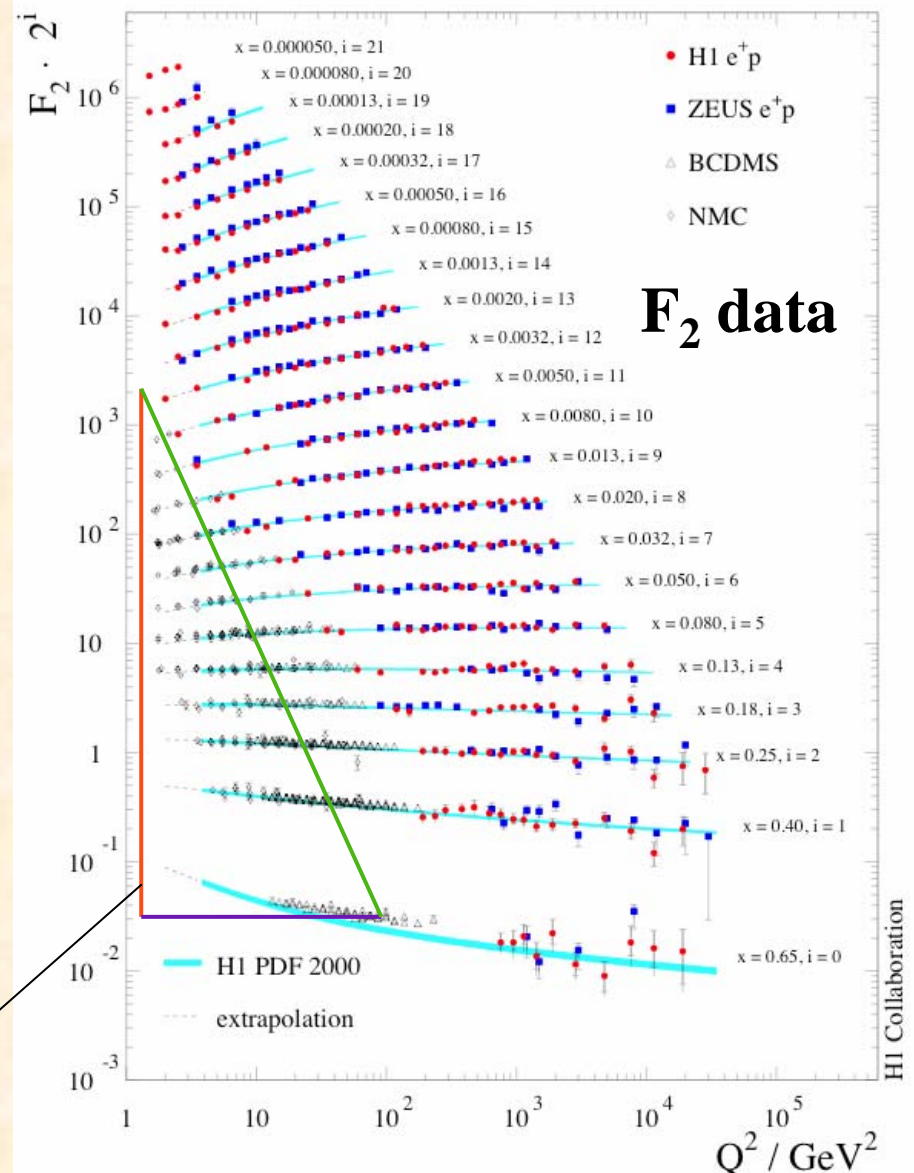
Current polarized data are kinematically limited.

$$x = \frac{Q^2}{2p \cdot q}; \quad \frac{Q^2}{ys}$$

fixed target: $\min(x) = \frac{Q^2}{2M_N E_{lepton}} \leq \frac{1}{2E_{lepton} \text{ (GeV)}}$
 if $Q^2 \geq 1 \text{ GeV}^2$

for E_{lepton} (SMC) = 190 GeV, $\min(x) = \frac{1}{400} = 0.003$

(from H1 and ZEUS, hep-ex/0502008)



(from AAC04)

region of g_1 data

H1 Collaboration

General strategies for determining polarized PDFs

Spin asymmetry A_1 ; $g_1 \frac{2x(1+R)}{F_2}$ $R \equiv \frac{F_L}{2xF_1} = \frac{F_2 - 2xF_1}{2xF_1}$

$$g_1(x, Q^2) = \frac{1}{2} \sum_q e_q^2 \int_x^1 \frac{dy}{y} \left[\Delta q(x/y, Q^2) + \Delta \bar{q}(x/y, Q^2) \right] \left[\delta(1-y) + \frac{\alpha_s(Q^2)}{2\pi} \Delta C_q(y) + \dots \right]$$

$$+ \frac{1}{2} \langle e_q^2 \rangle \int_x^1 \frac{dy}{y} \Delta g(x/y, Q^2) \left[n_f \frac{\alpha_s(Q^2)}{2\pi} \Delta C_g(y) + \dots \right] \quad \langle e_q^2 \rangle = \frac{1}{n_f} \sum_q e_q^2$$

Leading Order (LO)

Next to Leading Order (NLO)

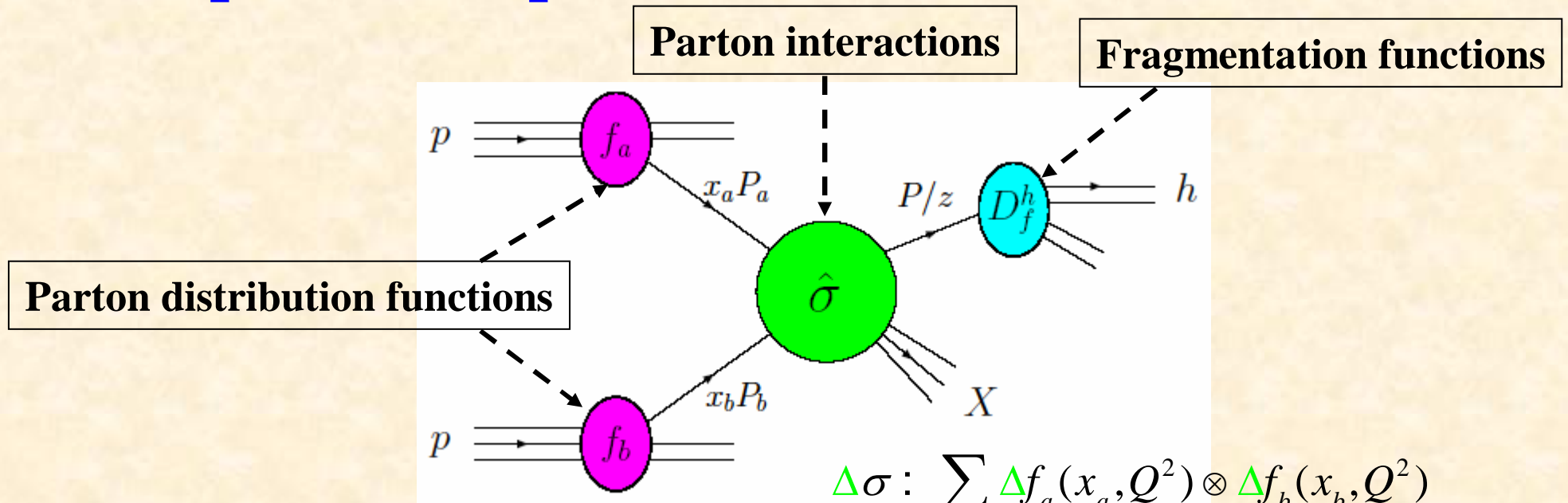
ΔC_q (ΔC_g) = quark (gluon) coefficient function

$$F_2(x, Q^2) = x \sum_q e_q^2 \int_x^1 \frac{dy}{y} \left[q(x/y, Q^2) + \bar{q}(x/y, Q^2) \right] \left[\delta(1-y) + \frac{\alpha_s(Q^2)}{2\pi} C_q^{(2)}(y) + \dots \right]$$

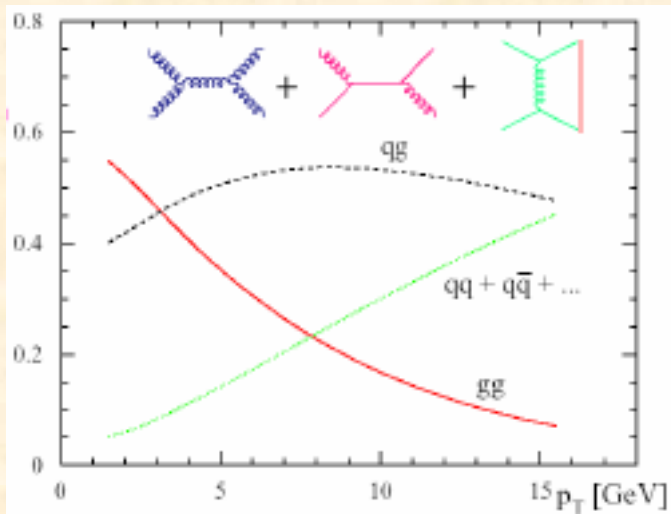
$$+ x \langle e_q^2 \rangle \int_x^1 \frac{dy}{y} g(x/y, Q^2) \left[n_f \frac{\alpha_s(Q^2)}{2\pi} C_g^{(2)}(y) + \dots \right]$$

Unpolarized PDFs

Description of π^0 production



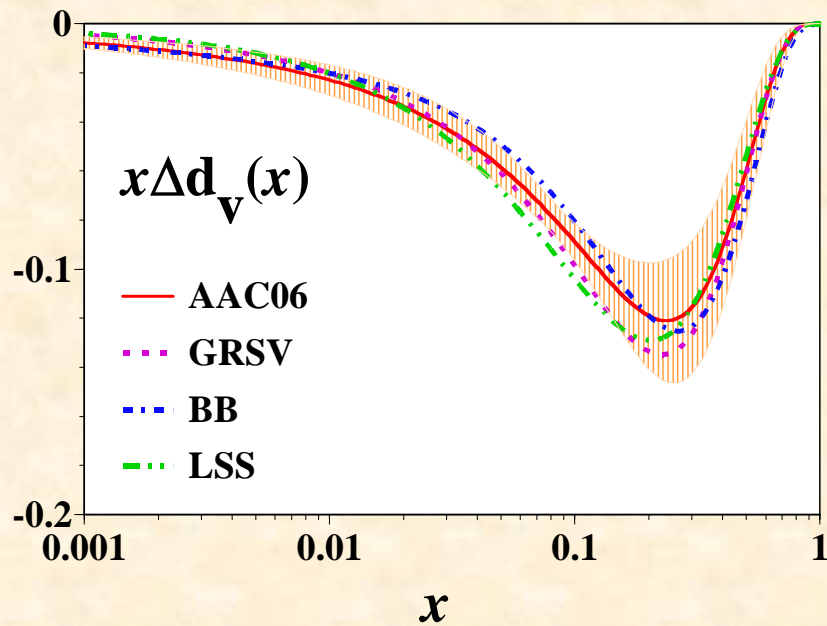
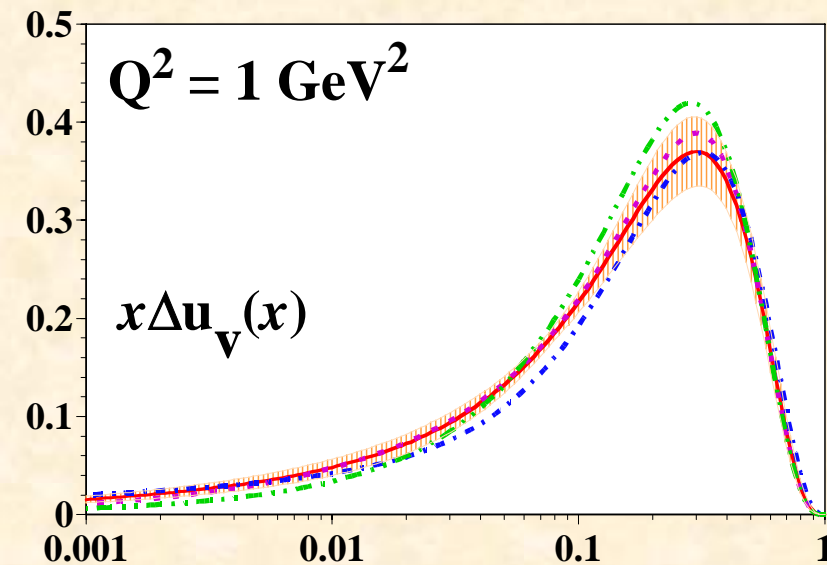
$$\Delta\sigma : \sum_{a,b,c} \Delta f_a(x_a, Q^2) \otimes \Delta f_b(x_b, Q^2) \otimes \Delta\hat{\sigma}(ab \rightarrow cX) \otimes D_c^\pi(z, Q^2)$$



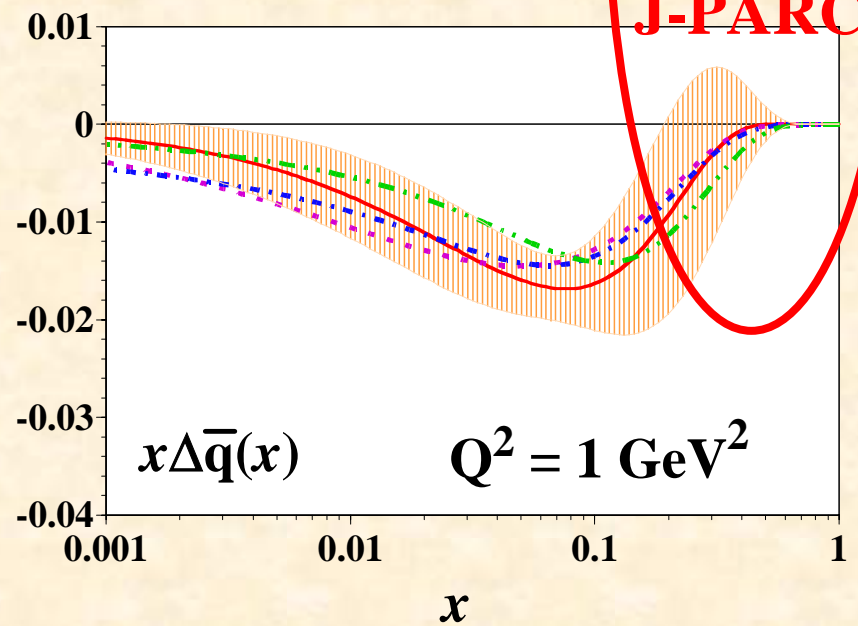
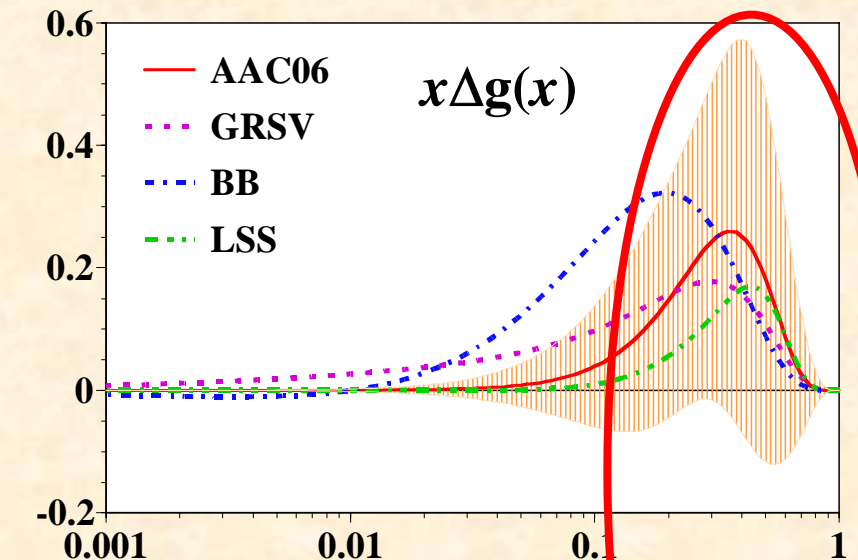
$g + g \rightarrow q(g) + X$ processes are dominant at small p_T
 $q + g \rightarrow q(g) + X$ at large p_T

The π^0 production process is suitable for finding the gluon polarization Δg .

Situation of polarized PDFs



Glueon and antiquark distributions have large uncertainties at large x .



J-PARC

Fragmentation Functions

<http://research.kek.jp/people/kumanos/ffs.html>

Purposes of investigating fragmentation functions

Semi-inclusive reactions have been used for investigating

- **origin of proton spin**

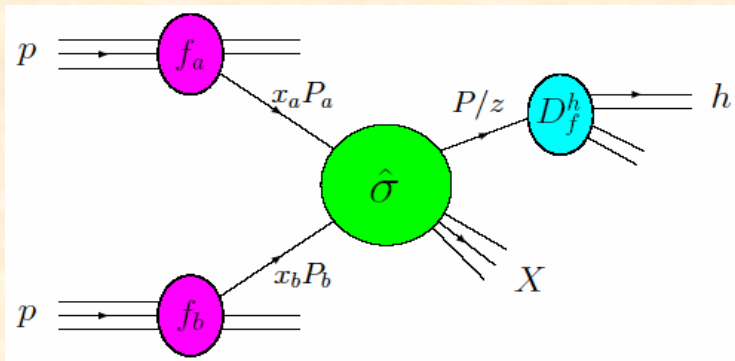
$$\vec{e} + \vec{p} \rightarrow e' + h + X \text{ (e.g. HERMES), } \vec{p} + \vec{p} \rightarrow h + X \text{ (RHIC-Spin)}$$

**Quark, antiquark, and gluon contributions to proton spin
(flavor separation, gluon polarization)**

- **properties of quark-hadron matters** $A + A' \rightarrow h + X$ (RHIC, LHC)

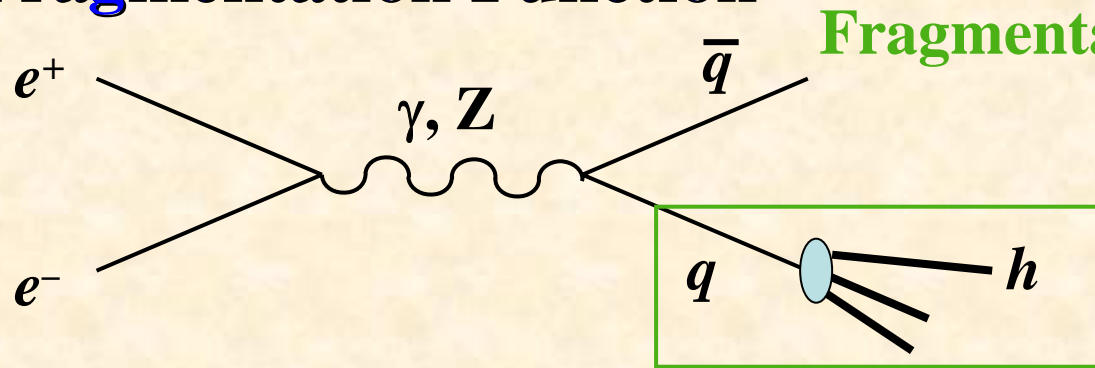
Nuclear modification

(recombination, energy loss, ...)



$$\sigma = \sum_{a,b,c} f_a(x_a, Q^2) \otimes f_b(x_b, Q^2) \otimes \hat{\sigma}(ab \rightarrow cX) \otimes D_c^\pi(z, Q^2)$$

Fragmentation Function



Fragmentation: hadron production from a quark, antiquark, or gluon

$$z \equiv \frac{E_h}{\sqrt{s}/2} = \frac{2E_h}{Q} = \frac{E_h}{E_q}, \quad s = Q^2$$

Fragmentation function is defined by

$$F^h(z, Q^2) = \frac{1}{\sigma_{tot}} \frac{d\sigma(e^+e^- \rightarrow hX)}{dz}$$

σ_{tot} = total hadronic cross section

Variable z

- Hadron energy / Beam energy
- Hadron energy / Primary quark energy

A fragmentation process occurs from quarks, antiquarks, and gluons, so that F^h is expressed by their individual contributions:

$$F^h(z, Q^2) = \sum_i \int_z^1 \frac{dy}{y} C_i\left(\frac{z}{y}, Q^2\right) D_i^h(y, Q^2)$$

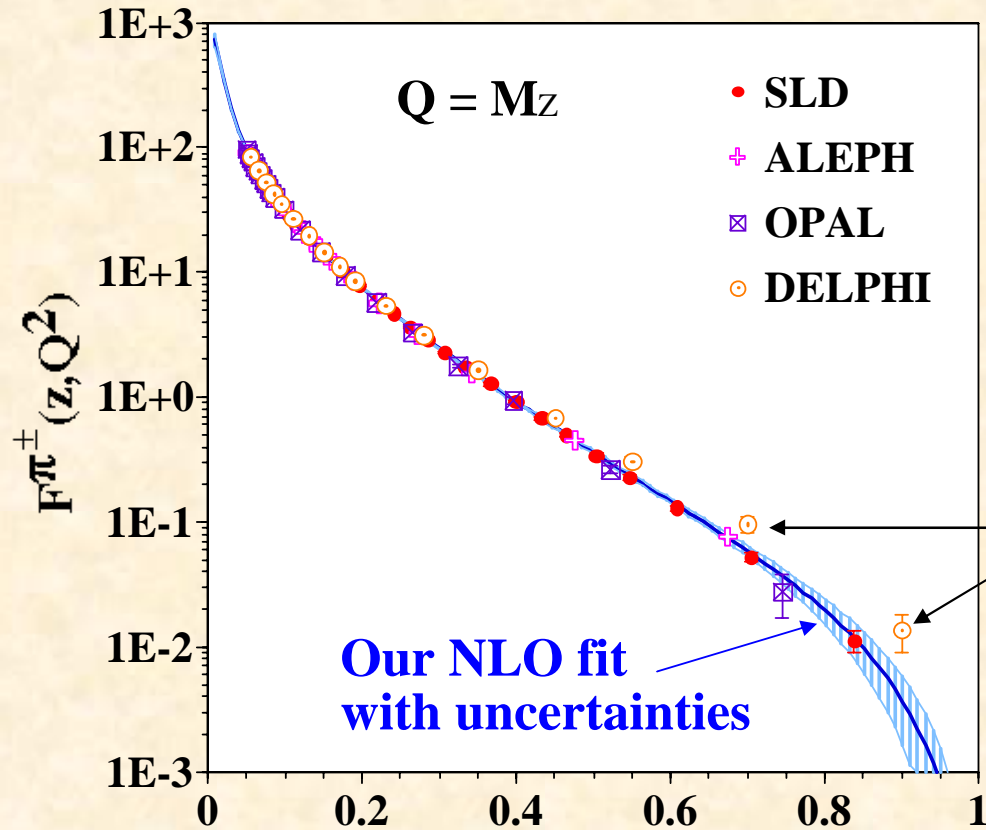
Calculated in perturbative QCD

Non-perturbative
(determined from experiments)

$C_i(z, Q^2)$ = coefficient function

$D_i^h(z, Q^2)$ = fragmentation function of hadron h from a parton i

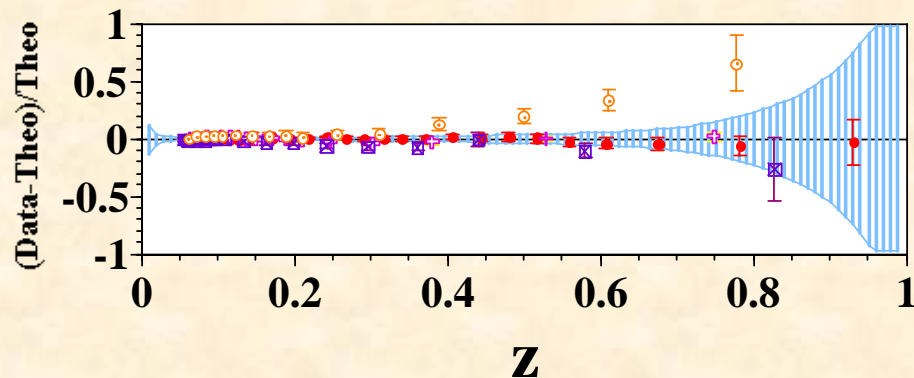
Comparison with pion data



$$F^{\pi^\pm}(z, Q^2) = \frac{1}{\sigma_{tot}} \frac{d\sigma(e^+e^- \rightarrow \pi^\pm X)}{dz}$$

Our fit is successful to reproduce the pion data.

The DELPHI data deviate from our fit at large z .



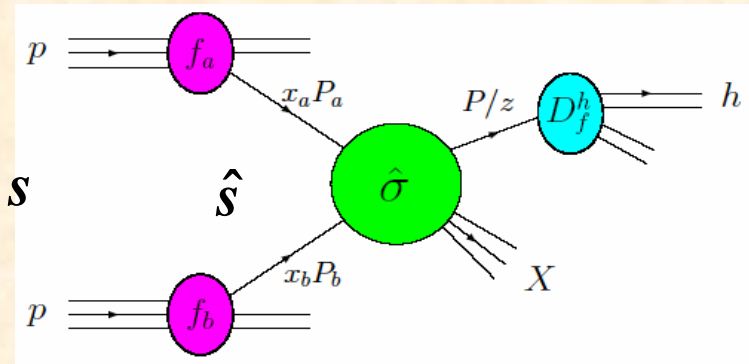
Rational difference between data and theory

$$\frac{F^{\pi^\pm}(z, Q^2)_{\text{data}} - F^{\pi^\pm}(z, Q^2)_{\text{theory}}}{F^{\pi^\pm}(z, Q^2)_{\text{theory}}}$$

Fragmentation functions at J-PARC

Gluon and light-quark
fragmentation functions
have large uncertainties.

Large differences between
the functions of various
analysis groups.



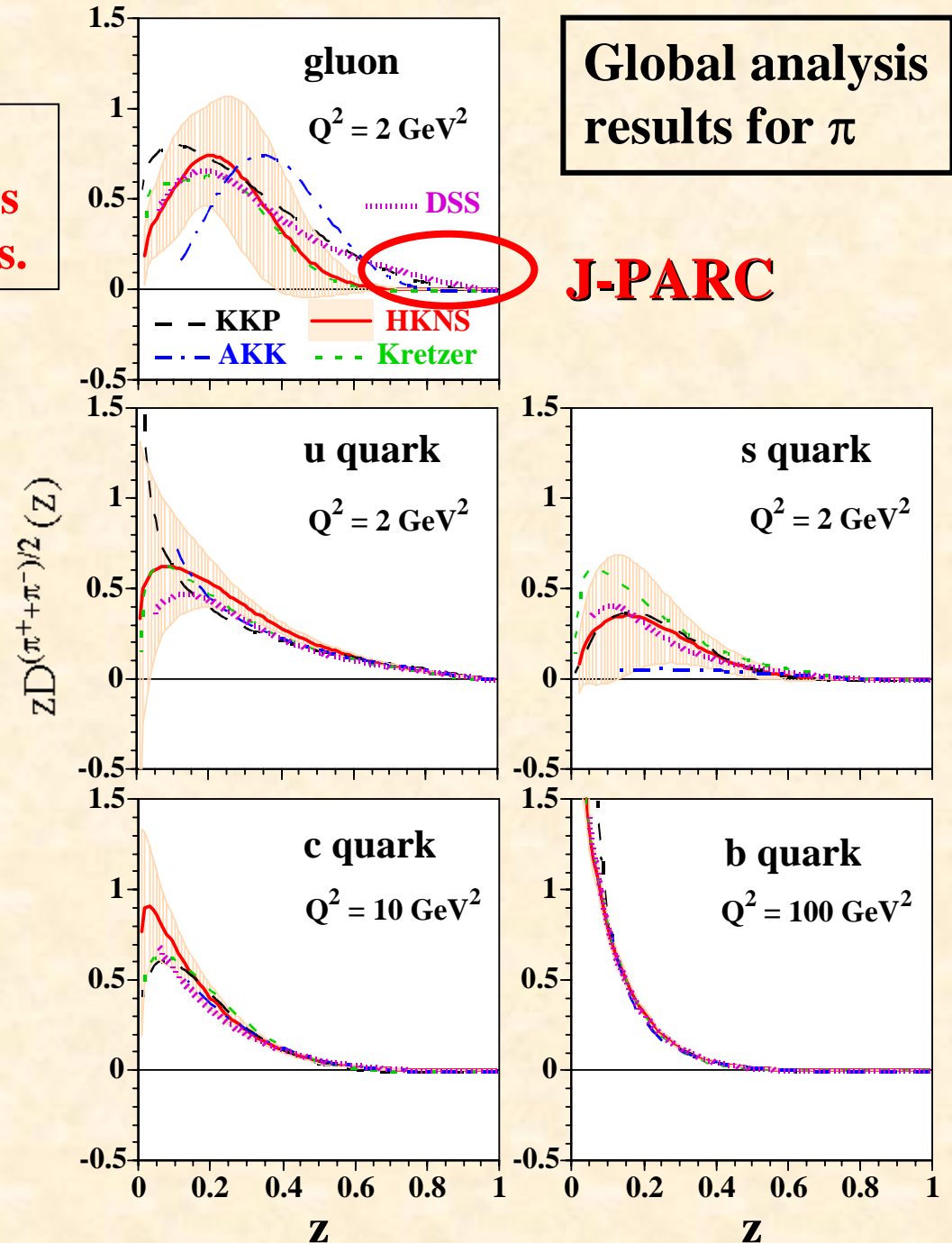
$$\hat{s} = x_a x_b s \sim (0.4)^2 (10 \text{ GeV})^2$$

$$\sqrt{\hat{s}} = 0.4 \cdot 10 = 4 \text{ GeV}$$

$$z \sim \frac{p_T}{\sqrt{\hat{s}}/2} = \frac{p_T}{2} \sim 1 \text{ (large } z\text{)}$$

Global analysis
results for π

J-PARC



**Exotic hadron search
by fragmentation functions**

$f_0(980)$ as an example

Criteria for determining f_0 structure by its fragmentation functions

Possible configurations of f_0 (980)

- (1) ordinary u, d - meson $\frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})$
- (2) strange meson, $s\bar{s}$
- (3) tetraquark ($K\bar{K}$), $\frac{1}{\sqrt{2}}(u\bar{u}s\bar{s} + d\bar{d}s\bar{s})$
- (4) glueball gg

Contradicts with experimental widths

$$\begin{aligned} \Gamma_{\text{theo}}(f_0 \rightarrow \pi\pi) &= 500 - 1000 \text{ MeV} \\ ? \quad \Gamma_{\text{exp}} &= 40 - 100 \text{ MeV} \\ \Gamma_{\text{theo}}(f_0 \rightarrow \gamma\gamma) &= 1.3 - 1.8 \text{ keV} \\ ? \quad \Gamma_{\text{exp}} &= 0.205 \text{ keV} \end{aligned}$$

Contradicts with lattice-QCD estimate

$$\begin{aligned} m_{\text{lattice}}(f_0) &= 1600 \text{ MeV} \\ ? \quad m_{\text{exp}} &= 980 \text{ MeV} \end{aligned}$$

Discuss 2nd moments and functional forms (peak positions) of the fragmentation functions for f_0 by assuming the above configurations, (1), (2), (3), and (4).

Tensor Structure at High-Energies For Spin-1 Hadrons

Note: Proton-beam polarization is not needed.

Polarized deuteron target is enough at J-PARC!

<http://www-conf.kek.jp/J-PARC-HS05/program.html>

Tensor Structure in High-energy Reactions

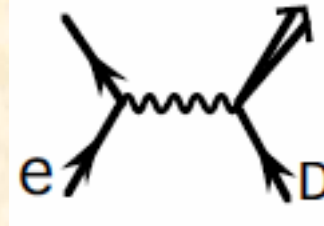
(Note: No polarized proton beam is needed!)

L. L. Frankfurt and M. I. Strikman, NP A405 (1983) 557.

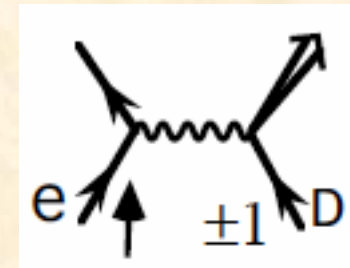
P. Hoodbhoy, R. L. Jaffe, and A. Manohar, NP B312 (1989) 571.

**Structure
Functions
(in e scattering)**

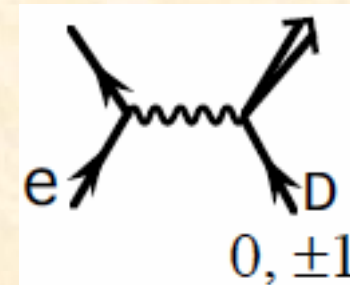
$$F_1 \propto \langle d\sigma \rangle$$



$$g_1 \propto d\sigma(\uparrow, +1) - d\sigma(\uparrow, -1)$$



$$b_1 \propto d\sigma(0) - \frac{d\sigma(+1) + d\sigma(-1)}{2}$$



**Parton
Model**

$$F_1 = \frac{1}{2} \sum_i e_i^2 (q_i + \bar{q}_i)$$

$$q_i = \frac{1}{3} (q_i^{+1} + q_i^0 + q_i^{-1})$$

$$g_1 = \frac{1}{2} \sum_i e_i^2 (\Delta q_i + \Delta \bar{q}_i)$$

$$\Delta q_i = q_{i\uparrow}^{+1} - q_{i\downarrow}^{+1}$$

$$\left[q_{\uparrow}^H(x, Q^2) \right]$$

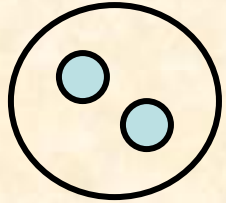
$$b_1 = \frac{1}{2} \sum_i e_i^2 (\delta q_i + \delta \bar{q}_i)$$

$$\delta q_i = q_i^0 - \frac{q_i^{+1} + q_i^{-1}}{2}$$

Tensor Structure in Proton-Deuteron Drell-Yan

b_1 for spin-1 particles

(Note: No polarized proton beam is needed!)



only in S-wave

$$\mathbf{b}_1 = \mathbf{0}$$

1st measurement of b_1 :
(HERMES) A. Airapetian et al.,
PRL 95 (2005) 242001.

Spin asymmetries

$$A_{LL} = \frac{\sum_a e_a^2 [\Delta q_a(x_A) \Delta \bar{q}_a(x_B) + \Delta \bar{q}_a(x_A) \Delta q_a(x_B)]}{\sum_a e_a^2 [q_a(x_A) \bar{q}_a(x_B) + \bar{q}_a(x_A) q_a(x_B)]}$$

$$A_{TT} = \frac{\sin^2 \theta \cos(2\phi) \sum_a e_a^2 [\Delta_T q_a(x_A) \Delta_T \bar{q}_a(x_B) + \Delta_T \bar{q}_a(x_A) \Delta_T q_a(x_B)]}{1 + \cos^2 \theta \sum_a e_a^2 [q_a(x_A) \bar{q}_a(x_B) + \bar{q}_a(x_A) q_a(x_B)]}$$

$$A_{UQ_0} = \frac{\sum_a e_a^2 [q_a(x_A) \delta \bar{q}_a(x_B) + \bar{q}_a(x_A) \delta q_a(x_B)]}{\sum_a e_a^2 [q_a(x_A) \bar{q}_a(x_B) + \bar{q}_a(x_A) q_a(x_B)]}$$

$$\delta q_i = q_i^0 - \frac{q_i^{+1} + q_i^{-1}}{2}$$

Note: $\delta \neq$ transversity in my notation

Unpolarized proton
+ Tensor polarized deuteron

Unique advantage of J-PARC ($\delta \bar{q}$ measurement)

$$A_{UQ_0}(\text{large } x_F) \approx \frac{\sum_a e_a^2 q_a(x_A) \delta \bar{q}_a(x_B)}{\sum_a e_a^2 q_a(x_A) \bar{q}_a(x_B)}$$

$$\int dx b_1^D(x) = 0 + \frac{1}{9} (\delta Q + \delta \bar{Q})_{\text{sea}}$$

F. E. Close and SK, PRD42, 2377 (1990)

Gottfried: $\int \frac{dx}{x} [F_2^p(x) - F_2^n(x)] = \frac{1}{3} + \frac{2}{3} \int dx [\bar{u} - \bar{d}]$

Our works related to this talk

(1) Overview on “Possible Hadron Physics at J-PARC”

SK, Nucl. Phys. A782 (2007) 442.

(2) $u\bar{u}/d\bar{d}$

SK, Phys. Rep. 303 (1998) 183.

(3) Nuclear PDFs

M. Hirai, SK, and M. Miyama, Phys. Rev. D 64 (2001) 034003;

M. Hirai, SK, and T.-H. Nagai, Phys. Rev. C 70 (2004) 044905; C 76 (2007) 065207.

(4) Polarized PDFs, Asymmetry Analysis Collaboration (AAC)

Y. Goto *et al.*, Phys. Rev. D 62 (2000) 034017;

M. Hirai, SK, N. Saito, Phys. Rev. D 69 (2004) 054021; D 74 (2006) 014015.

(5) Global analyses for FFs of π , K , and p + their uncertainties

M. Hirai, SK, T.-H. Nagai, and K. Sudoh, Phys. Rev. D75 (2007) 094009;

Exotic hadron search by using FFs *e.g.* for $f_0(980)$

M. Hirai, SK, M. Oka, and K. Sudoh, Phys. Rev. D77 (2008) 017504.

(6) Sum rule for $b_1(x)$

F. E. Close and SK, Phys. Rev. D 42 (1990) 2377.

General formalism for polarized proton+deuteron Drell-Yan

S. Hino and SK, Phys. Rev. D 59 (1999) 094026; D 60 (1999) 054018.

Summary

J-PARC will be an important facility in hadron and nuclear physics communities.

In high-energy hadron physics

- **Structure functions of hadrons**
- **Fragmentation**
- **Hadron interactions in nuclear medium**
- **Short-range NN interactions**
- **Hadron \rightarrow Quark degrees of freedom**
- **Hadron spin**
- **...**

I introduced some topics. More contributions are needed for the hadron project at J-PARC!

Need to discuss possible topics with 30 GeV, 50 GeV, and 50 GeV polarized proton beams.

The End

The End