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**Nonlinear dynamics and complex behaviors  
in magnetized plasmas of fusion interest**

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# Nonlinear dynamics and complex behaviors in magnetized plasmas of fusion interest \*

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\* Acknowledgments: S. Briguglio, L. Chen, G. Fogaccia, T.S. Hahm, A.V. Milovanov, G. Vlad, R.B. White



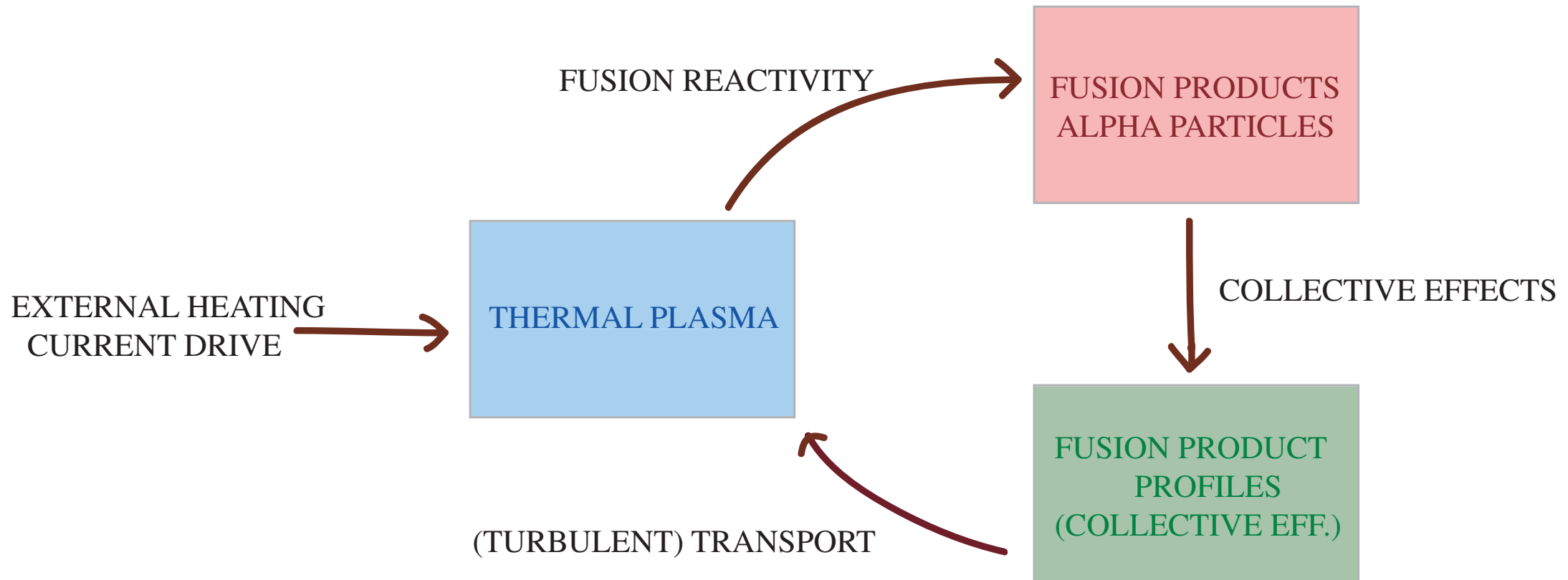
Associazione EURATOM ENEA sulla Fusione



ASICTP, TS July 2008

# Nonlinear Dynamics of Burning Plasmas I

- A burning plasma is a **complex self-organized system** where among the crucial processes to understand there are **(turbulent) transport** and **fast ion/fusion product induced collective effects**.



# Nonlinear Dynamics of Burning Plasmas II

- Reactor relevant conditions require fast ion (MeV energies) and charged fusion products good confinement:
  - Identification of **burning plasma stability boundaries** with respect to energetic ion collective mode excitations and their **nonlinear dynamic behaviors** above the stability thresholds
  - Obvious impact on the **operation-space boundaries**, since collective losses may lead to significant wall loading and damaging of plasma facing materials in addition to degrading fusion performance
- Mutual interactions between collective modes and energetic ion dynamics with drift wave turbulence and turbulent transport should not deteriorate the thermonuclear efficiency:
  - MeV ion energy tails introduce a **dominant electron heating** and different weighting of the electron driven micro-turbulence w.r.t. present experiments
  - They also generate **long time-scale nonlinear behaviors** typical of self-organized complex systems



# The roles of simulation and theory

- These phenomena can be analyzed, at least in part, in present day experiments and provide nice examples of **mutual positive feedbacks between theory, simulation and experiment**.
- In a **burning plasma**, however, **unique features** not reproducible in existing experiments are:
  - energetic ion power density profiles and characteristic wavelengths of the collective modes
  - local power balance dominated by electron heating (fast ions) and self-organization of radial profiles of the relevant quantities: consequence on turbulence spectra and turbulent transport
- Crucial roles of **predictive capabilities based on numerical simulations** as well as of **fundamental theories for developing simplified yet relevant models**, needed for insights into the basic processes
- Importance of using **existing and future experimental evidences** for modeling verification and validation



# Outline

- Collective behaviors and fast ion transport:
  - The shear Alfvén fluctuation spectrum: Alfvén Eigenmodes and resonant modes
  - Fast ion transport: diffusion and avalanches
  - Open issues in fast ion transport studies
- Mutual interactions between collective modes and energetic ion dynamics with drift wave turbulence and turbulent transport
- Examples of broader applications of fundamental physics in fusion science
- **Additional material:** lecture notes from ICTP Autumn College on Plasma Physics, Oct. 13 - Nov. 7 2003 (available for distribution)
  - Role of resonant vs non-resonant wave-particle interactions in electromagnetic turbulence
  - Collective effects and self-consistent energetic particle dynamics in burning plasmas



Collective behaviors and fast ion transport

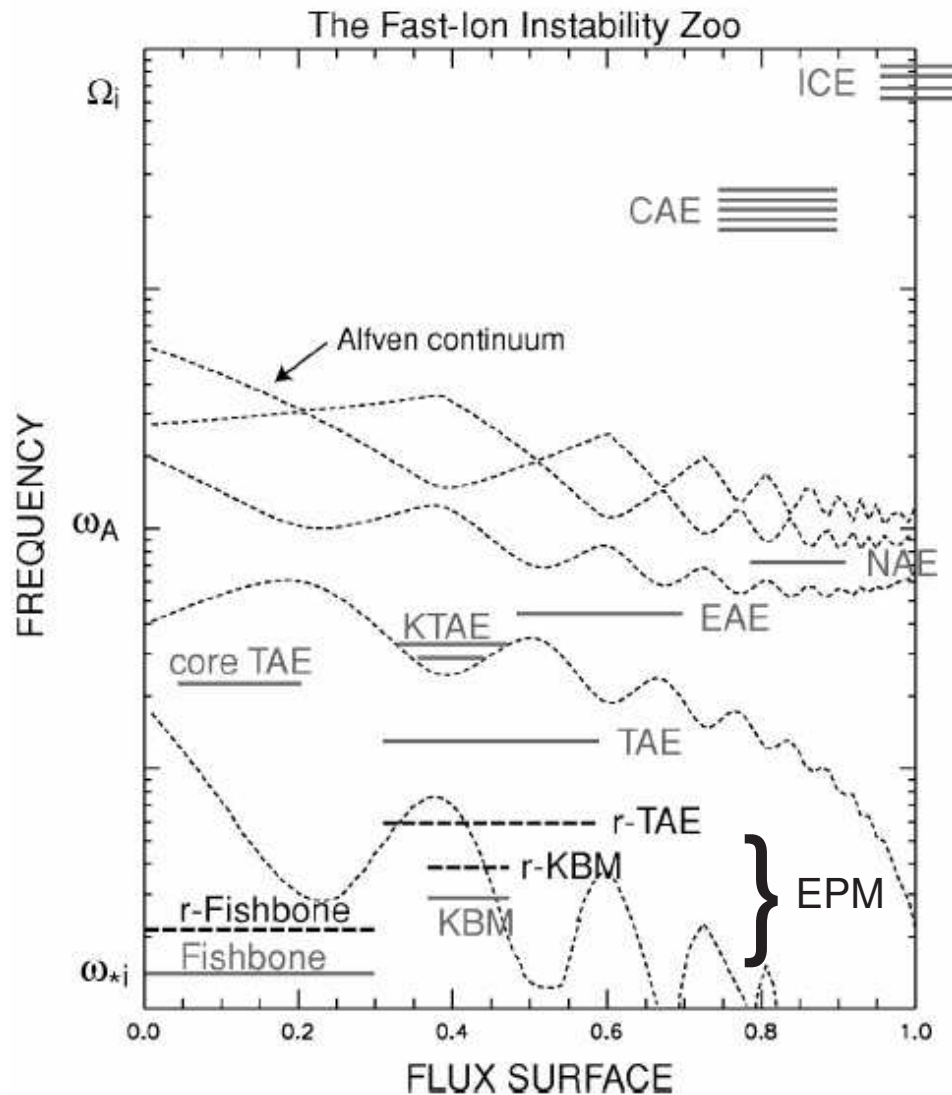
# The role of shear Alfvén waves

- Collective behaviors due to energetic ions in burning plasmas: shear Alfvén (SA) waves play a crucial role:
  - Resonant wave particle interaction of  $\approx$  MeV ions with SA inst. due to  $v_E \approx v_A$  ( $k_{\parallel} v_A \approx \omega_E$ )
  - Group velocity is along  $B$ -field lines ( $\omega = k_{\parallel} v_A$ ): particles stay in resonance
- Toroidal geometry plays a crucial role: SA waves propagate along  $B$  as in a 1D lattice and sample periodic potential structures with influence on SA spectrum and linear as well as non-linear dispersion
- Focus on non-linear dynamics and fast ion transport: conclusions largely apply to MHD modes





# Shear Alfvén spectrum: continuum with gaps



- Frequency gaps are due to lattice symmetry breaking
- Linear theory reasonably well understood: few technical aspects need to be refined for more realistic comparisons with EXP
- Unified description: discrete gap modes vs. resonant (driven) continuum modes.
- Alfvén Eigenmodes (AE): weakly damped gap modes excited by fast ions; fixed frequency
- Energetic Particle Modes (EPM): fast ions drive overcomes continuum damping; resonant particle characteristic frequency
- Nonlinear dynamics and fast ion transport: reflect different nature of AE and EPM

W.W. Heidbrink, *Phys. Plasmas* **9**, 2113, (2002)



# Fast ion transports in burning plasmas

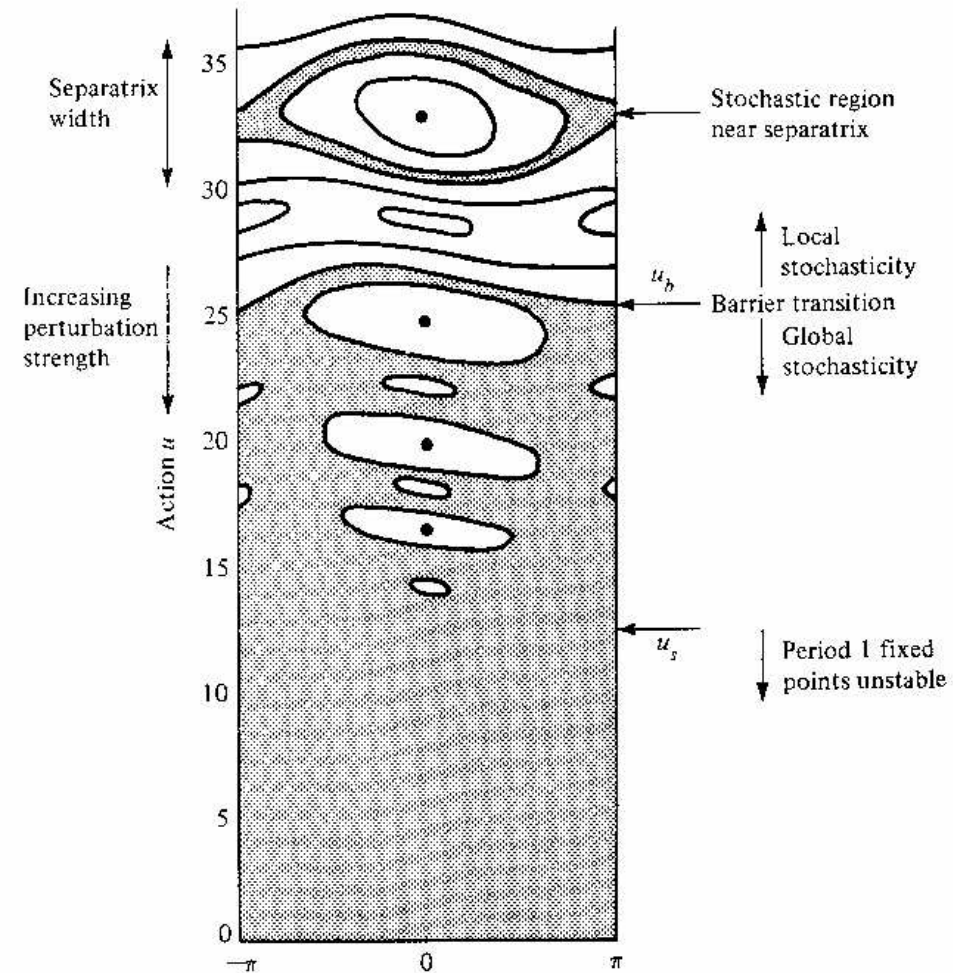
- AE modes are predicted to have small saturation levels and yield negligible transport unless stochastization threshold in phase space is reached: H.L. Berk and B.N. Breizman, Phys. Fluids B **2**, 2246, (1990) and D.J. Sigmar, C.T. Hsu, R.B. White and C.Z. Cheng, Phys. Fluids B, **4**, 1506, (1992).



# Phase space structures: fast ion resonant interactions with AE

D.J. Sigmar, *et al.* 1992, *PFB* 4, 1506 ; C.T. Hsu and D.J. Sigmar 1992, *PFB* 4, 1492

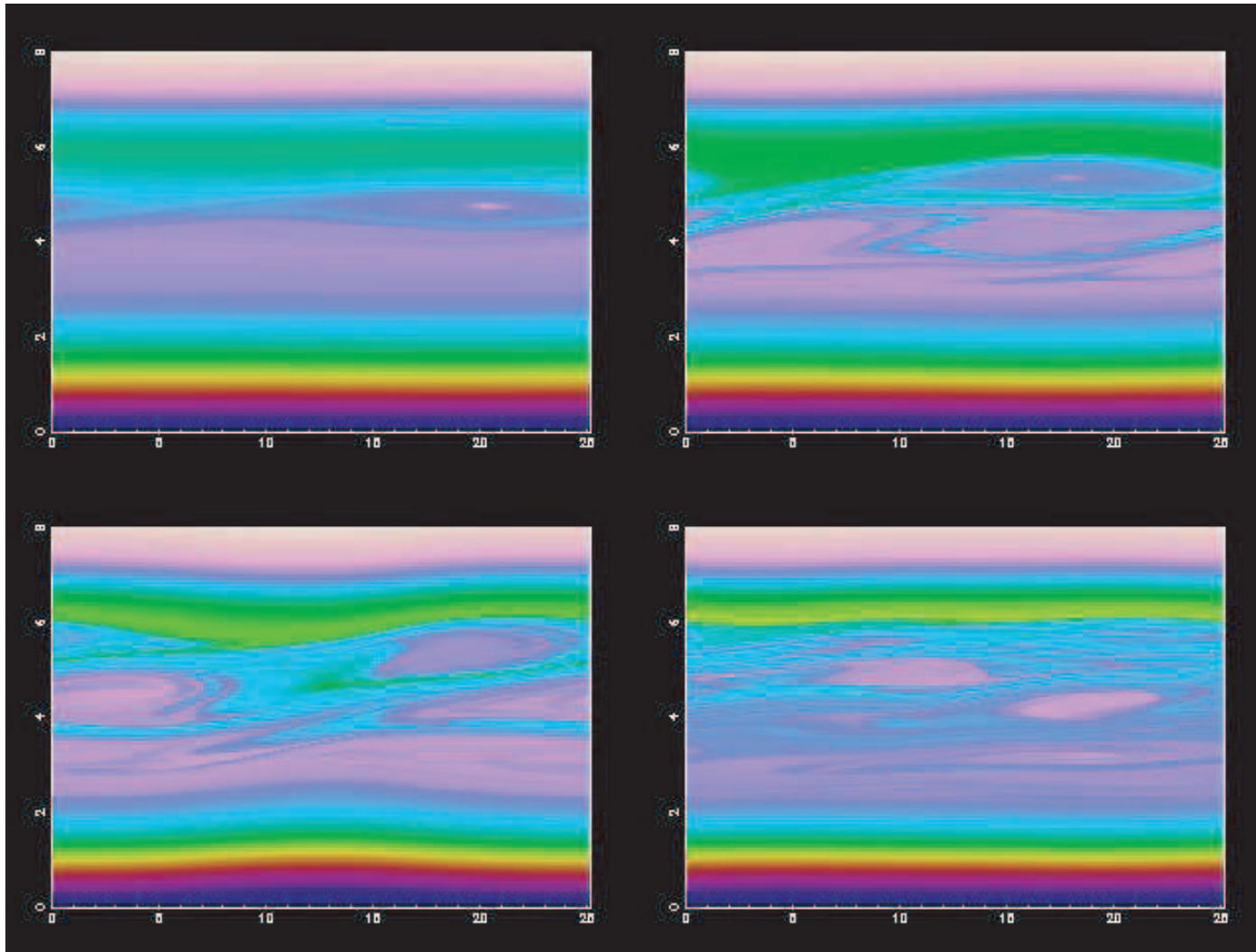
- Transient losses  $\approx \delta B_r/B$ : resonant drift motion across the orbit-loss boundaries in phase space
- Diffusive losses  $\approx (\delta B_r/B)^2$  above a stochastic threshold, due to stochastic diffusion in phase space across orbit-loss b.
- Uncertainty in the stoch. threshold:  $(\delta B_r/B) \lesssim 10^{-4}$  in the multiple mode case. Possibly reached via phase space explosion: “domino effect” (H.L. Berk, *et al.* 1996, *PoP* 3, 1827)
- SOC models for transport event and related PDF?



Lichtenberg & Lieberman 1983, Sp.-Ver. NY



# Simulation results: strongly unstable 1D system



- Creation of phase space structures changes the distribution function thereby permitting otherwise disallowed modes to grow ( R.G.L. Vann, *et al.* 2005 Intl. Sherwood Conf.)

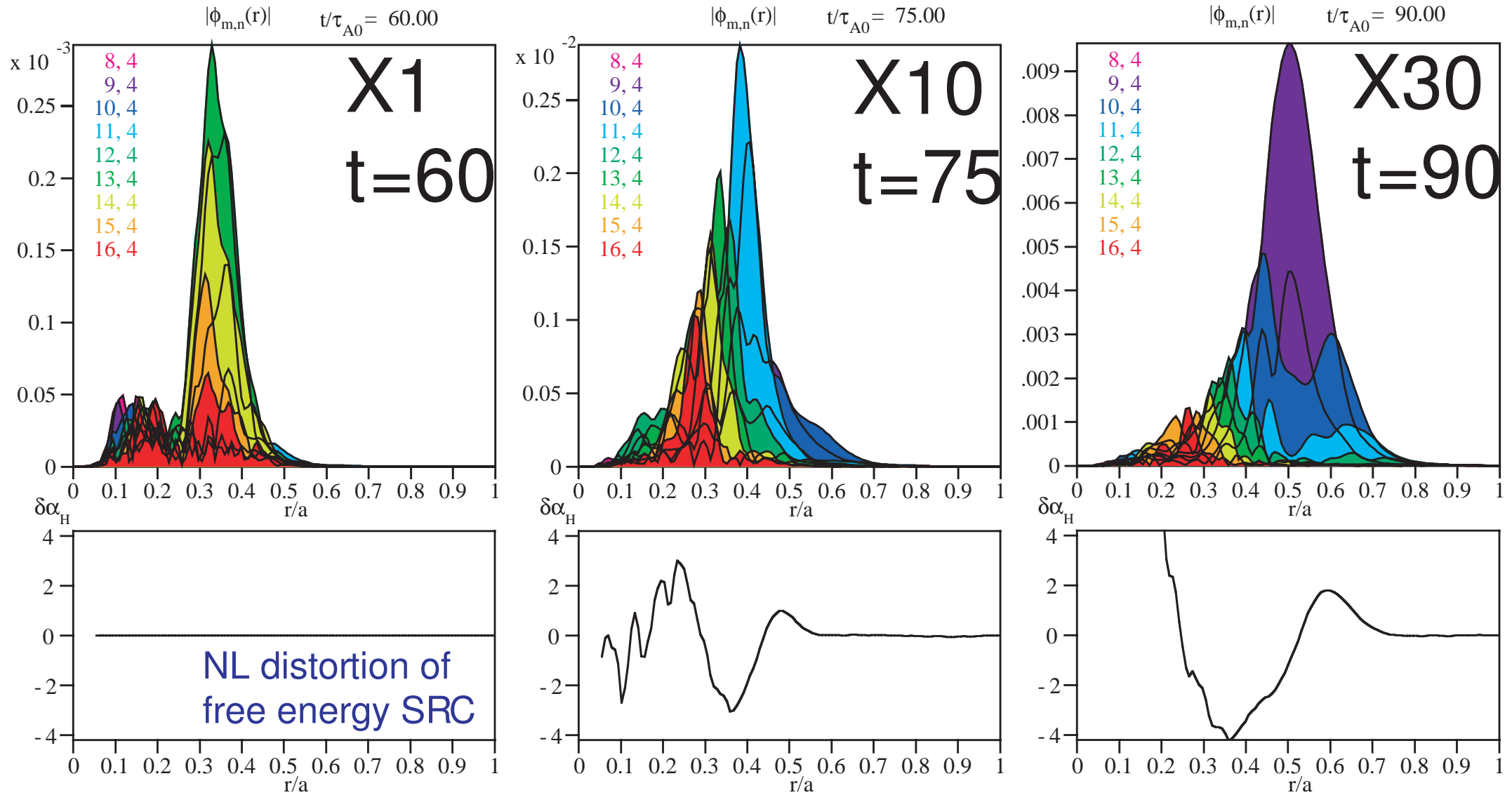


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- Strong energetic particle redistributions are predicted to occur above the EPM excitation threshold in 3D Hybrid MHD-Gyrokinetic simulations: S. Briguglio, F. Zonca and G. Vlad, Phys. Plasmas **5**, 1321, (1998).

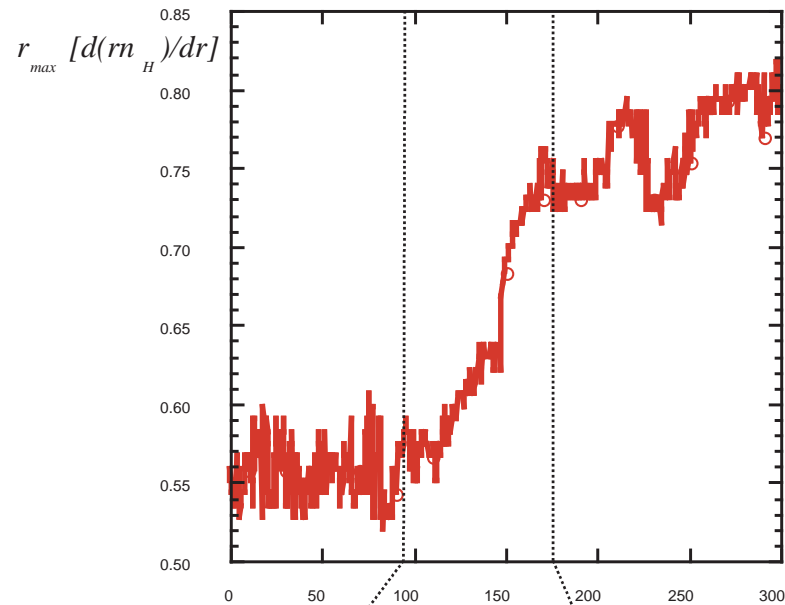
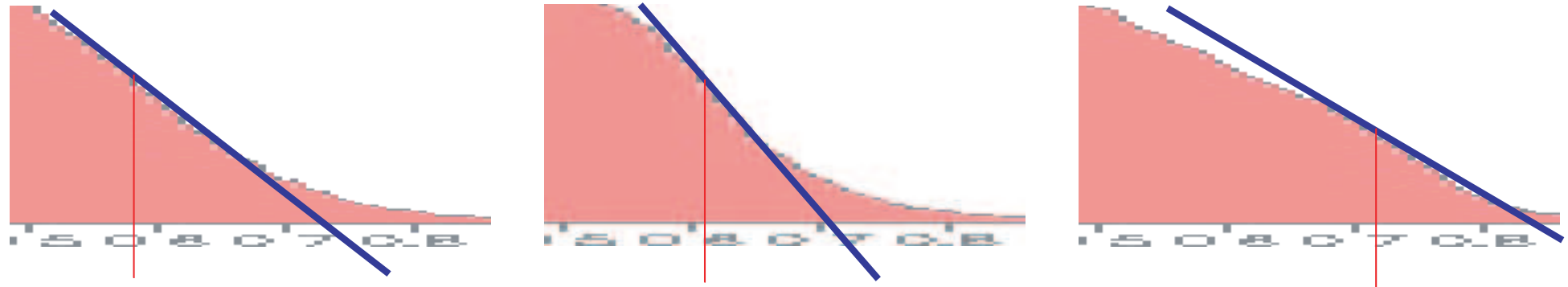


# Avalanches and NL EPM dynamics

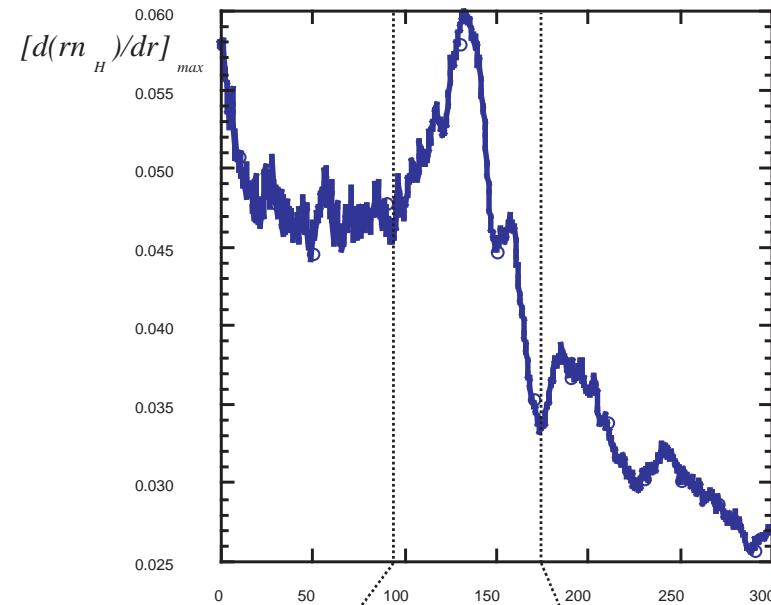


□ Importance of toroidal geometry on wave-packet propagation and shape

# Propagation of the unstable front



linear phase  
convective phase  
diffusive phase



linear phase  
convective phase  
diffusive phase

□ Gradient steepening and relaxation: spreading ... similar to turbulence



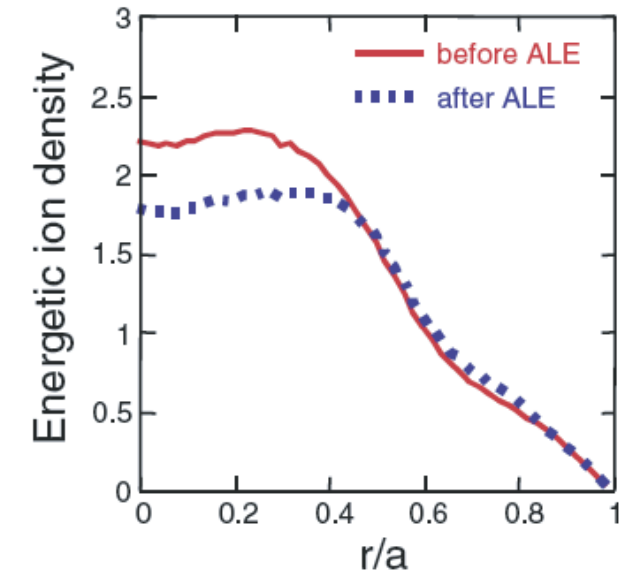
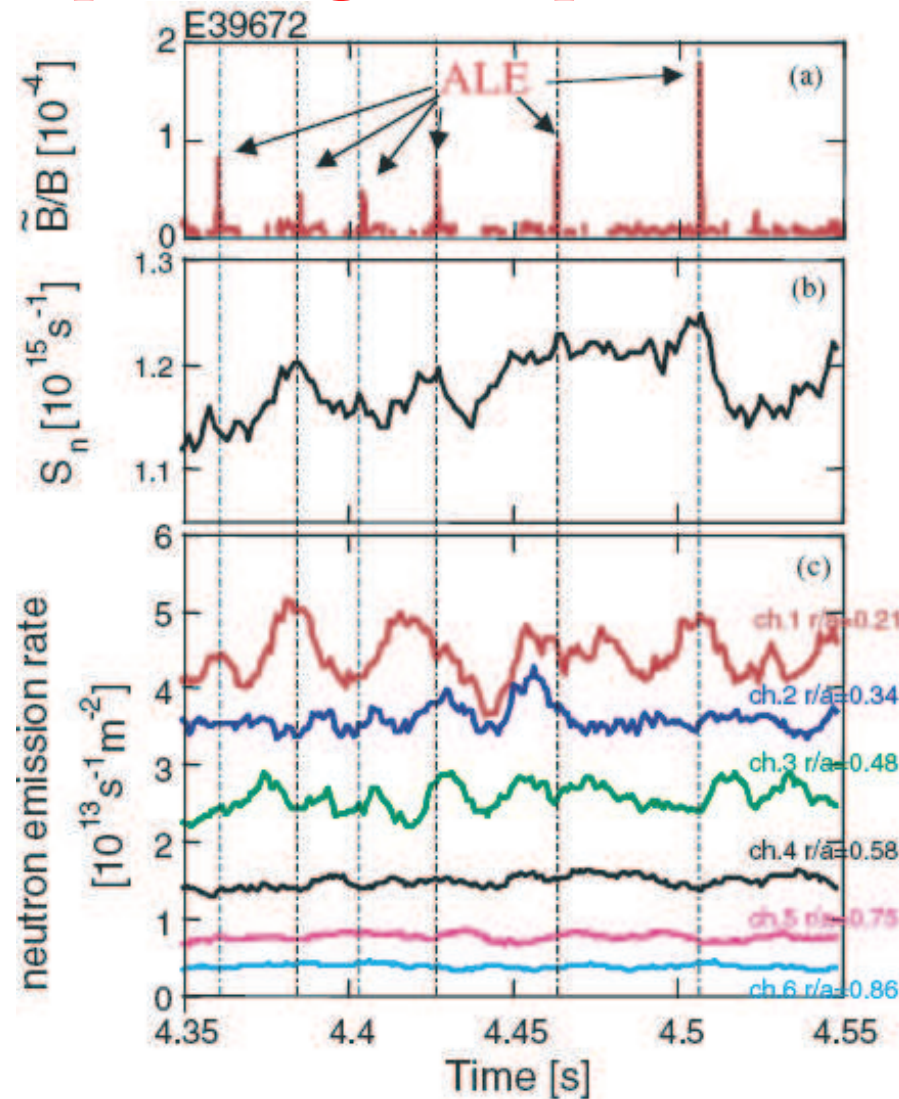
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- Nonlinear Dynamics of Burning Plasmas: energetic ion transport in burning plasmas has two components:
  - slow diffusive processes due to weakly unstable AEs and a residual component possibly due to plasma turbulence (Vlad *et al.* *PPCF* **47** 1015 (2005); Estrada-Mila *et al.*, *Phys. Plasmas* **13**, 112303, (2006)).
  - rapid transport processes with ballistic nature due to coherent nonlinear interactions with EPM and/or low-frequency long-wavelength MHD: fast ion avalanches & experimental observation of Abrupt Large amplitude Events (ALE) on JT60-U (K. Shinohara *etal* *PPCF* **46**, S31 (2004))





# Abrupt Large amplitude Events (ALE) in JT60-U



Courtesy of M. Ishikawa, K. Shinohara and JT60-U

K. Shinohara *etal* PPCF 46, S31 (2004)

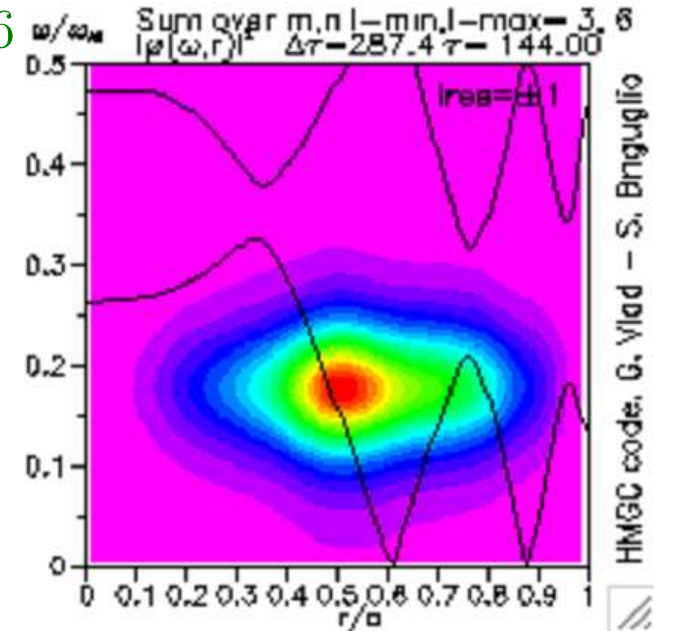


# Fast ion transport: 3D simulation and experiment

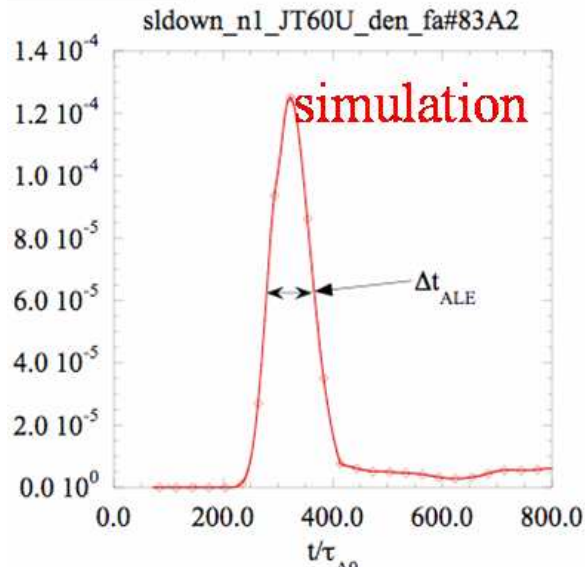
S. Briguglio, G. Fogaccia, G. Vlad *et al*, EPS⊕IAEA⊕APS 2006

- Abrupt Large amplitude Events (ALE) in JT60-U:
  - $n = 1$  mode,  $\beta_{H0} = 8\pi P_{H0}/B^2 \approx 3\%$ ;
  - linear growth rate  $\gamma \approx 0.106\tau_{A0}^{-1}$ ;
  - half width of the pulse  $\Delta t_{ALE} \approx 64.5\mu s$ ;
  - experimental range  $\Delta t_{ALE} \approx 50 \div 200\mu s$ ;
  - energetic particle profiles compare well before and after ALE burst

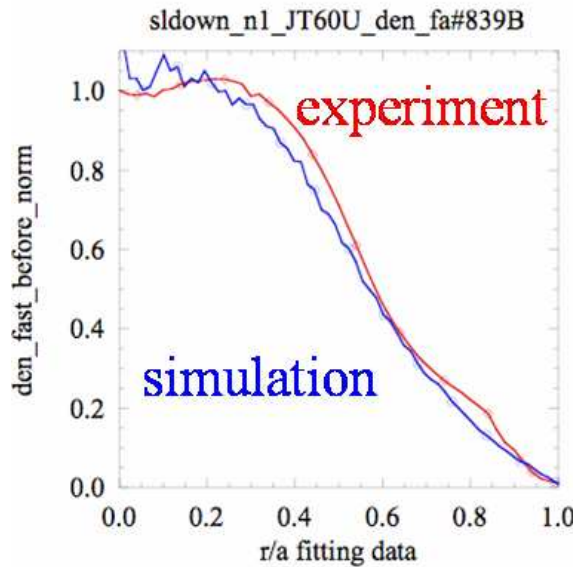
K. Shinohara *etal* PPCF 46, S31 (2004)



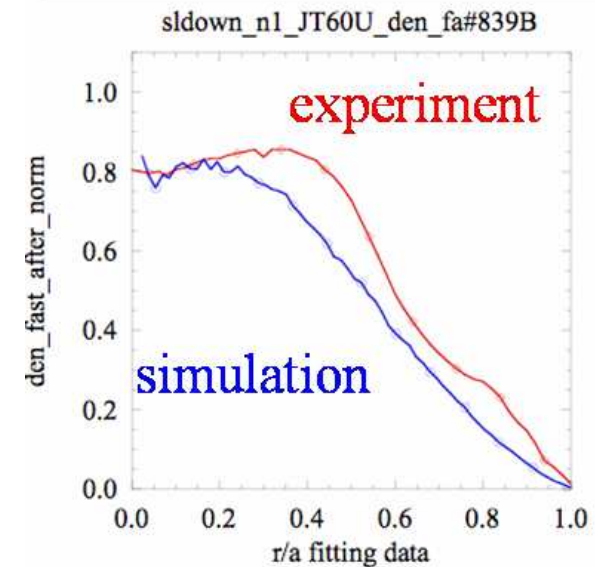
— v1-dt144 power spectrum maxima (a.u.)



— den\_fast\_before\_norm — dentot\_t=60



— den\_fast\_after\_norm — dentot\_t=600



# Some open issues for fast ion transport

- Single mode vs. multi-mode nonlinear dynamics:
  - dense spectrum of modes of characteristic frequency and location
  - coherent vs. incoherent wave-particle interaction
  - structure formation in phase space
  
- Wave-particle resonances  $\Rightarrow$  nonlinear phase-space dynamics of charged particles  $\Rightarrow$  trapping, stochastic motion; etc.
  
- Nonlinear dynamics of Energetic Particle Modes:
  - importance of rare but large and potentially dangerous transport events
  - coherent non-linear wave-particle interactions



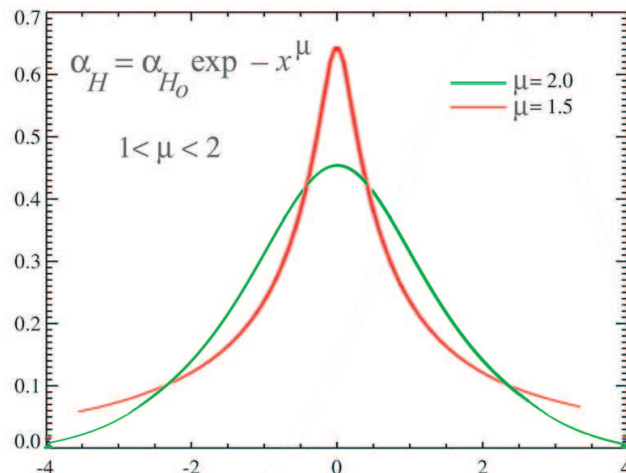
# Fast ion transport: some broader applications

A.V. Milovanov et al., (2006)

- Convective amplification of the EPM wave-packet and ballistic particle transport in Avalanche process is described by the **complex Ginzburg-Landau equation (GLE)**

$$\partial_{\xi}^2 A_n = i \frac{\gamma_L}{D} \left( \frac{\Delta\gamma_L}{\gamma_L} + \frac{L_{NL}^2}{\gamma_L} \partial_{\xi}^2 (\gamma_L |A_n|^2) \right) A_n + \frac{\Delta\omega}{D} A_n \quad \begin{aligned} \xi &= r - v_{gr} t \\ \gamma_L &\propto \alpha_H = -R_0 q^2 (d\beta_H/dr) \end{aligned}$$

- For Gaussian source function  $\alpha_H = \alpha_{H0} \exp[-(\xi - \xi_0)^2]$ , the GLE reduces to its canonical form; for generalized stretched Gaussian distribution, i.e.,  $\alpha_H = \alpha_{H0} \exp[-|\xi - \xi_0|^{\mu}]$  ( $1 < \mu < 2$ ), the **GLE is rewritten in terms of fractional derivative operators**:



$$\nabla^2 A = q^2 A - p^2 A \nabla^{2-\mu} |A|^2$$

Fractional derivative Riesz Operator

$$\nabla^{2-\mu} |A|^2 = \frac{1}{\Gamma(1-\mu)} \nabla \int_{-\infty}^x \frac{|A|^2(x_0)}{(x-x_0)^{2-\mu}} dx_0$$

- The fractional derivative GLE incorporates the **key features of non-Gaussianity and long-range dependence** in thresholded nonlinear dynamical systems



Mutual interactions of collective modes with drift wave turbulence

# Physics issues behind fluctuations non-linear interactions

- Interaction between collective modes and thermal plasma turbulence:
  - collective modes due to energetic particles
  - plasma turbulence due to thermal components
  
- Intrinsic separation of spatial scales (orbit size) in the free energy source: interaction occurs
  - if the time scales become comparable such as for Alfvén ITG (e.m. ITG)
  - if mediated by the 3rd entities such as zonal structures: zonal flows, fields, corrugations of radial profiles

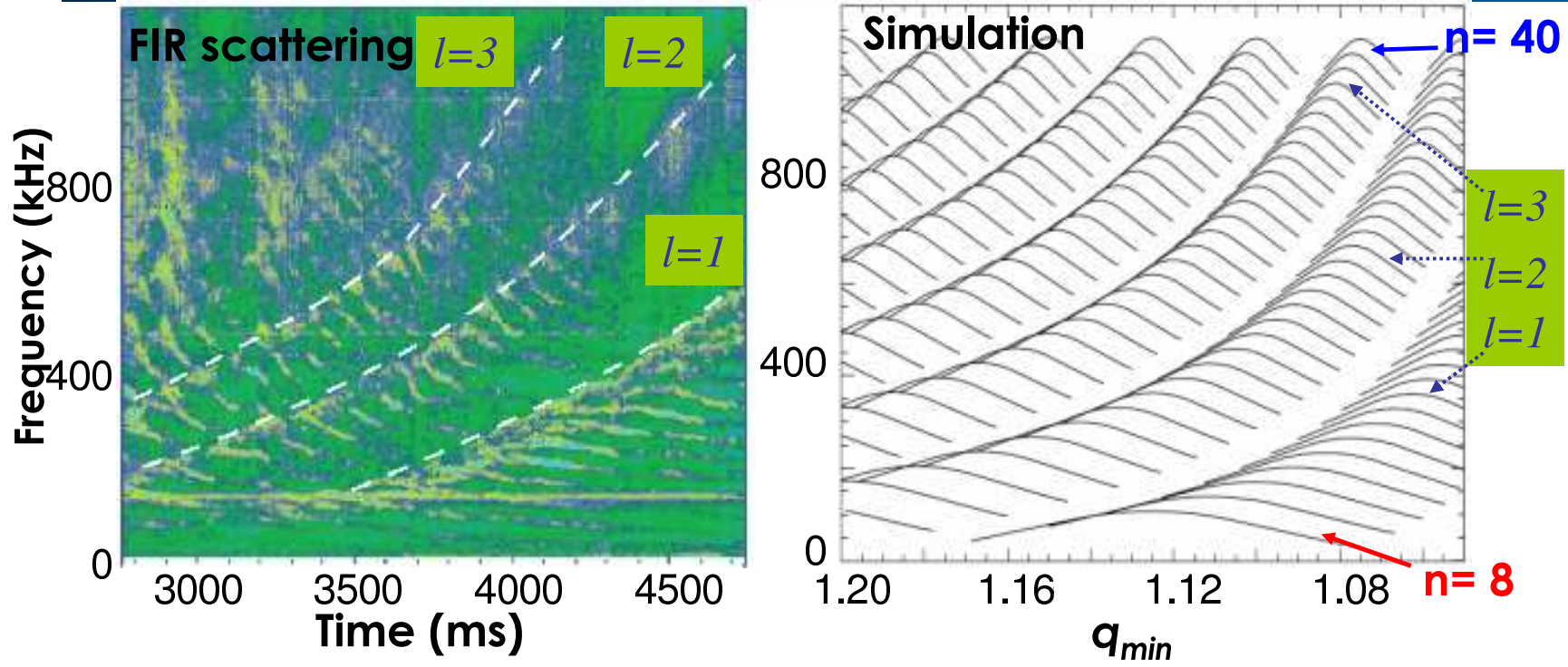


# Mutual interactions of collective modes with DW turbulence

- E.m. plasma turbulence: theory predicts excitation of Alfvénic fluctuations in a wide range of mode numbers near the low frequency accumulation point of s.A. continuum,  $\omega \simeq (7/4 + T_e/T_i)^{1/2}(2T_i/m_i)^{1/2}/R$  (F. Zonca, L. Chen, *et al.* 96, *PPCF* **38**, 2011; ... 99, *PoP* **6**, 1917):
  - by energetic ions at long wavelength: finite Beta AE (BAE)/EPM
  - by thermal ions at short wavelength: Alfvén ITG
- Magnetic flutter: may be relevant for electron transport (B.D. Scott 2005, *NJP* **7**, 92; V. Naulin, *et al.* 2005, *PoP* **12**, 052515)
- Recent observations on DIII-D confirm these predictions (R. Nazikian, *et al.* 06, *PRL* **96**, 105006)



# A "Sea of Core Localized Alfvén Eigenmodes" Observed in DIII-D Quiescent Double Barrier (QDB) plasmas

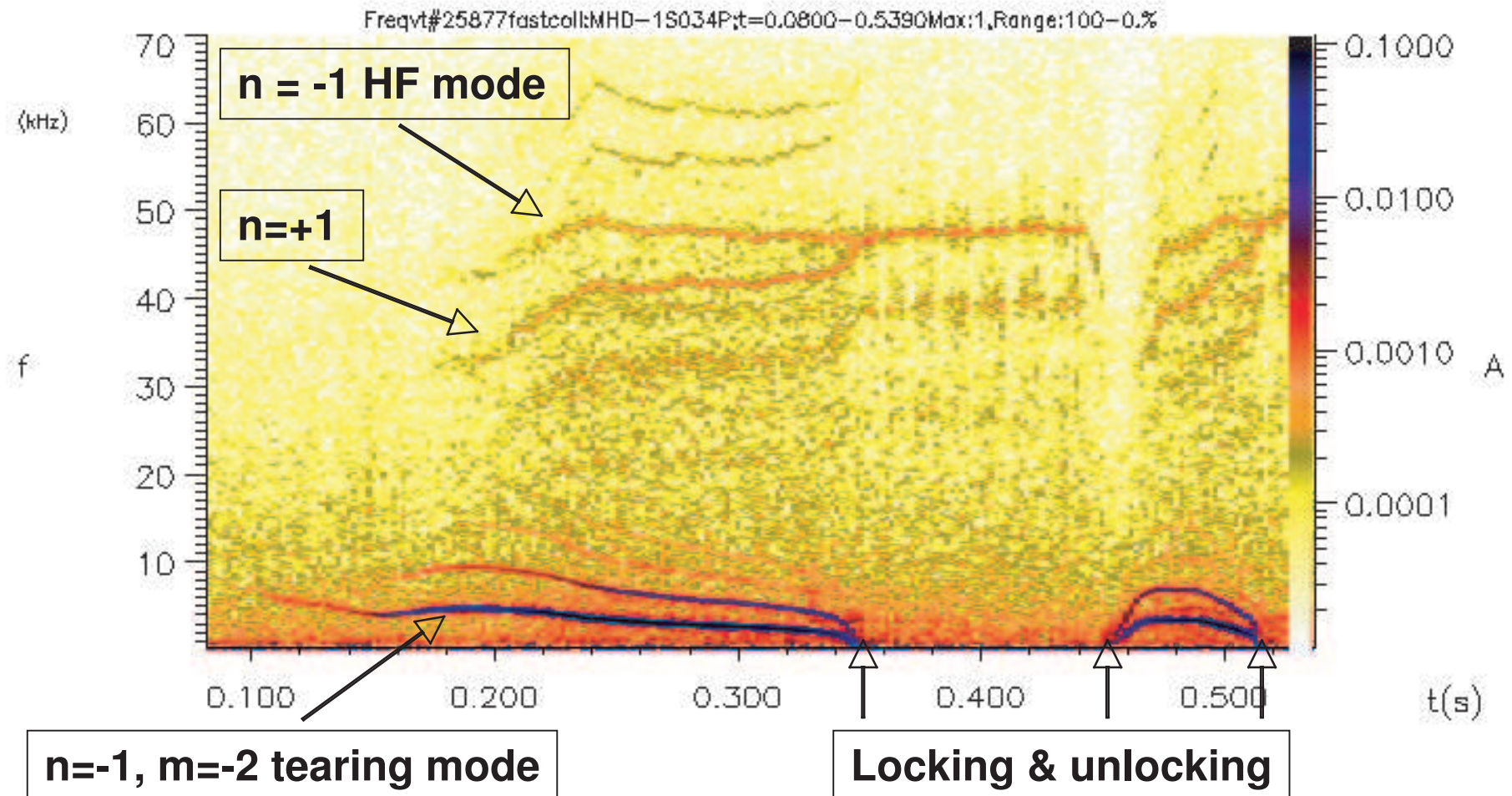


- Bands of modes  $m=n+l$ ,  $l=1, 2, \dots$   $\omega_{n+1} - \omega_n \approx \omega_{rot}$  (CER)
- Neutral beam injection opposite to plasma current:  $V_{||} \approx 0.3V_A$





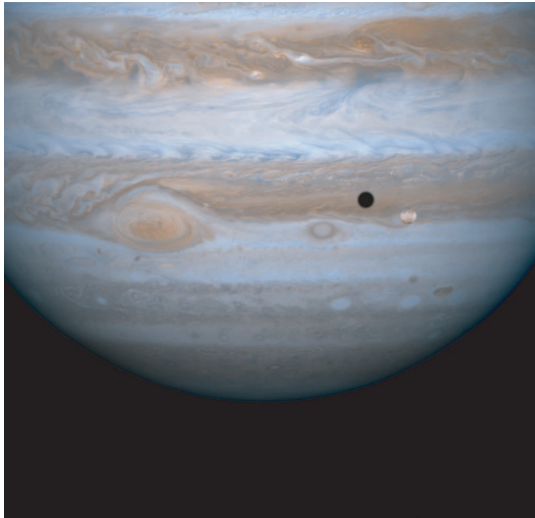
- The same modes are excited by a large amplitude magnetic island on FTU (P. Buratti, *et al.* 2005, *NF 45* 1446; S. Annibaldi, EPS 2006, O2.016).



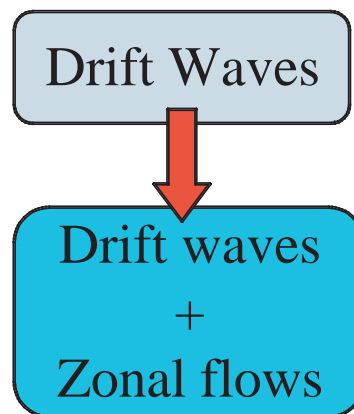
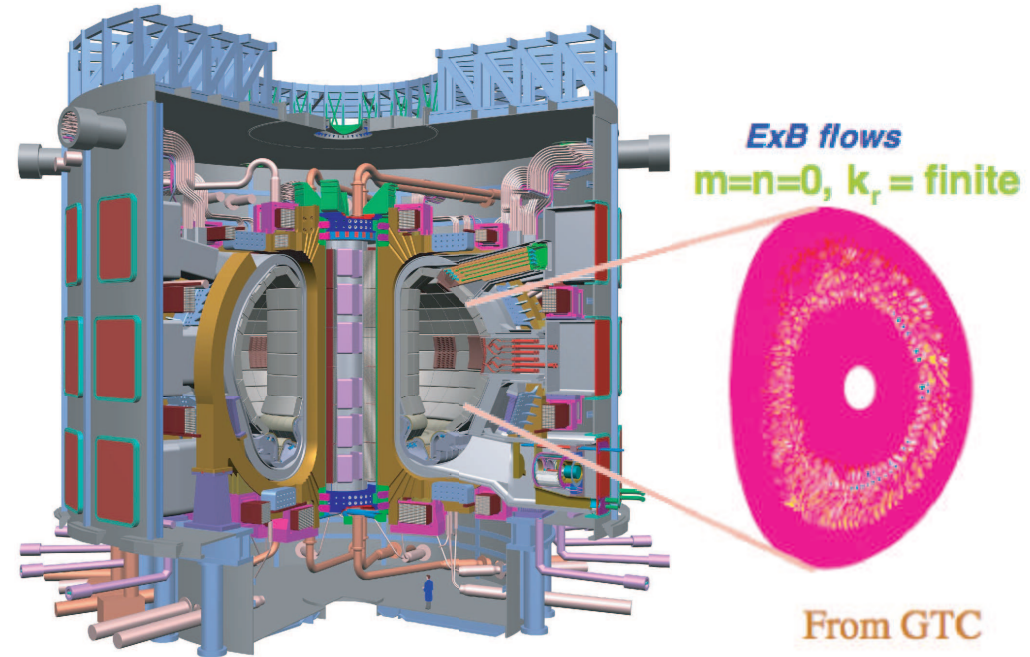
P. Smeulders, *et al.* 2002, *ECA 26B*, D5.016



# Zonal Flows are common in plasmas



Zonal Flows on Jupiter



## Paradigm Change

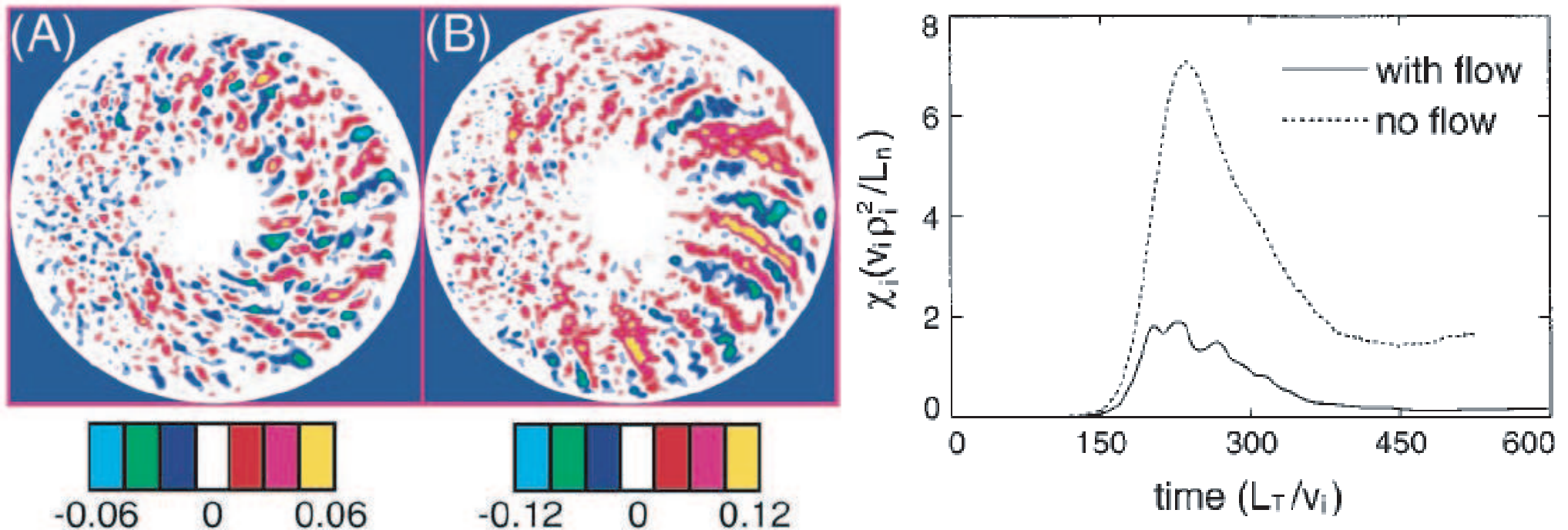
P.H. Diamond, *et al.* 2005  
PPCF 47, R35

## ZFs peculiarities

- No direct radial transport
- No linear instability
- Turbulence driven



# Zonal Flows regulate turbulence: effect on transport



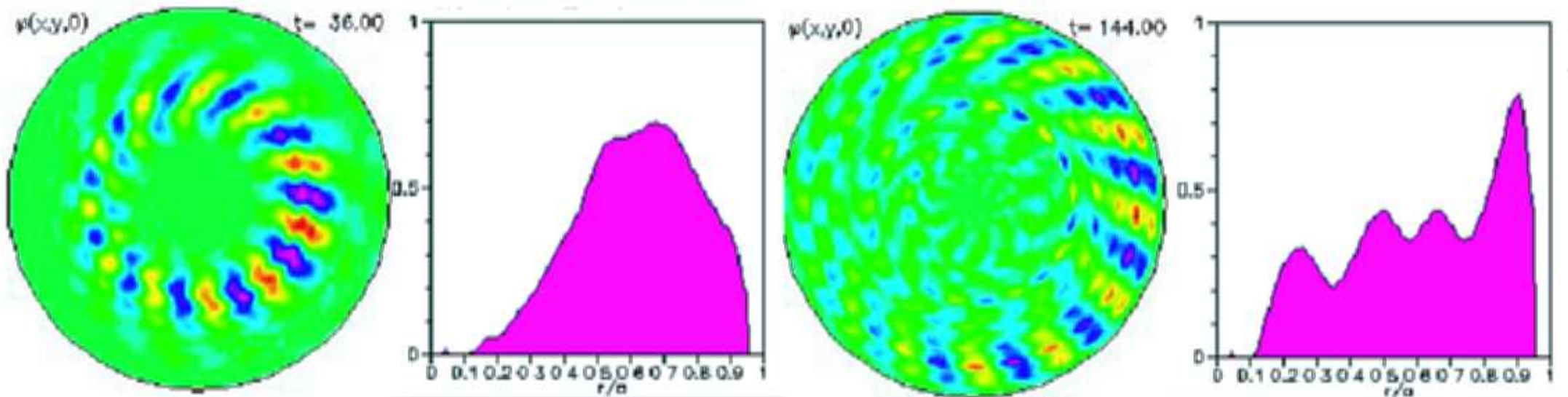
Z. Lin, *et al.* 1998, *Science* **281**, 1835



## Long time scale behaviors

- Depending on proximity to marginal stability, AE and EPM nonlinear evolutions can be predominantly affected by
  - spontaneous generation of zonal flows and fields (L. Chen, *et al.* 2001, *NF* **41**, 747; P.N. Guzdar, *et al.* 2001, *PRL* **87**, 015001)
  - radial modulations in the fast ion profiles (F. Zonca, *et al.* 2000, *Theory of Fusion Plasmas*, 17)

EPM NL dynamics (F. Zonca, *et al.* 2000, *Theory of Fusion Plasmas*, 17)



- AITG and strongly driven MHD modes behave similarly



# Zonal Flows and Zonal Structures

- Very disparate space-time scales of AE/EPM, MHD modes and plasma turbulence: complex self-organized behaviors of burning plasmas will be likely dominated by their nonlinear interplay via zonal flows and fields
- Crucial role of toroidal geometry for Alfvénic fluctuations: fundamental importance of magnetic curvature couplings in both linear and nonlinear dynamics (B.D. Scott 2005, *NJP* **7**, 92; V. Naulin, *et al.* 2005, *PoP* **12**, 052515)
- Long time scale behaviors of zonal structures are important for the overall burning plasma performance: generators of nonlinear equilibria
- The corresponding stability determines the dynamics underlying the dissipation of zonal structures in collision-less plasmas and the nonlinear up-shift of thresholds for turbulent transport (L. Chen, *et al.* IAEA 2006, 2007 *NF* **47**, 886)
- Impact on burning plasma performance



# Conclusions

- Burning plasmas are complex self-organized systems, whose investigation requires a conceptual step in the analysis of magnetically confined plasmas.
- Integrated numerical simulations are crucial to investigate these new physics; while fundamental theories provide the conceptual framework and the necessary insights.
- Verification against experimental observations in present day machines is a necessary step for the validation of physical models and numerical codes for reliable extrapolations to burning plasmas.
- Lack of understanding of some complex burning plasma behaviors can be likely filled in by increasingly complicated and more realistic modeling of plasma conditions as computing performances improve.
- However, some other unexplained behaviors may be just indications of fundamental conceptual problems: mutual positive feedbacks between theory, simulation and experiment will be necessary.
- Burning plasma physics is an exciting and challenging field: many examples of fundamental problems with broader applications and implications.

