



*The Abdus Salam*  
*International Centre for Theoretical Physics*



1957-7

**Miniworkshop on Strong Correlations in Materials and Atom Traps**

*4 - 15 August 2008*

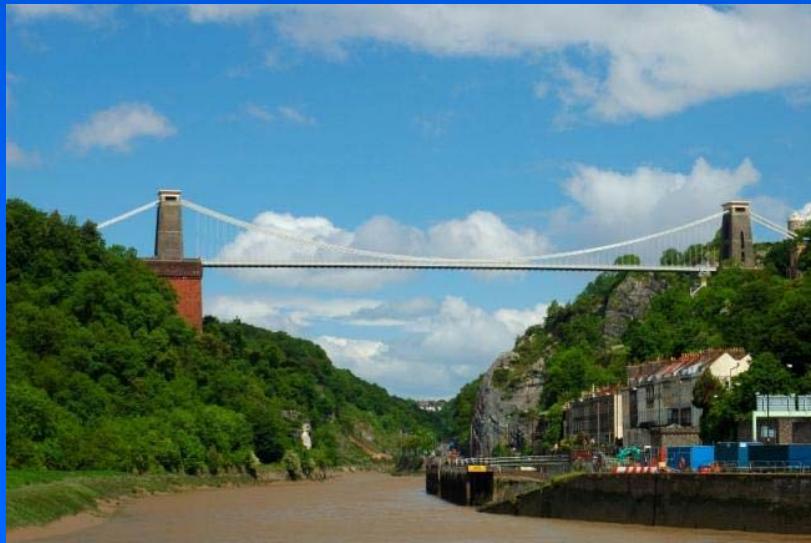
**New Structures in the Magnetic Excitations of La<sub>2-x</sub>Sr<sub>x</sub>CuO<sub>4</sub>**

HAYDEN Stephen Michael

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H.H.Wills Physics Laboratory  
Royal Fort, Tyndall Avenue, BS8 1TL Bristol  
UNITED KINGDOM*

# New Structures in the Spin Excitations of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

Stephen Hayden  
University of Bristol



# Talk Plan

- Introduction
- Spin Fluctuations in  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$
- Spin Excitations and the Pseudogap  
(one gap/two gap models)
- Spin fluctuation and the resonance in  
 $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$

B. Vignolle et al.,  
Nat. Phys. 3, 163 (2007)

O. J. Lipscombe et al.,  
PRL 99, 067002 (2007)

# Collaborators

Baptiste Vignolle (Bristol)

Oliver Lipscombe (Bristol)

Neil Headings (Bristol)

Toby Perring (ISIS)

Chris Frost (ISIS)

Gabriel Aeppli (London)

Des McMorrow (London)

Niels Christensen (PSI)

Henrik Rønnow (Geneva)

Bella Lake (HMI, Berlin)

PengChen Dai (U of Tennessee)

Herb A Mook (Oak Ridge)

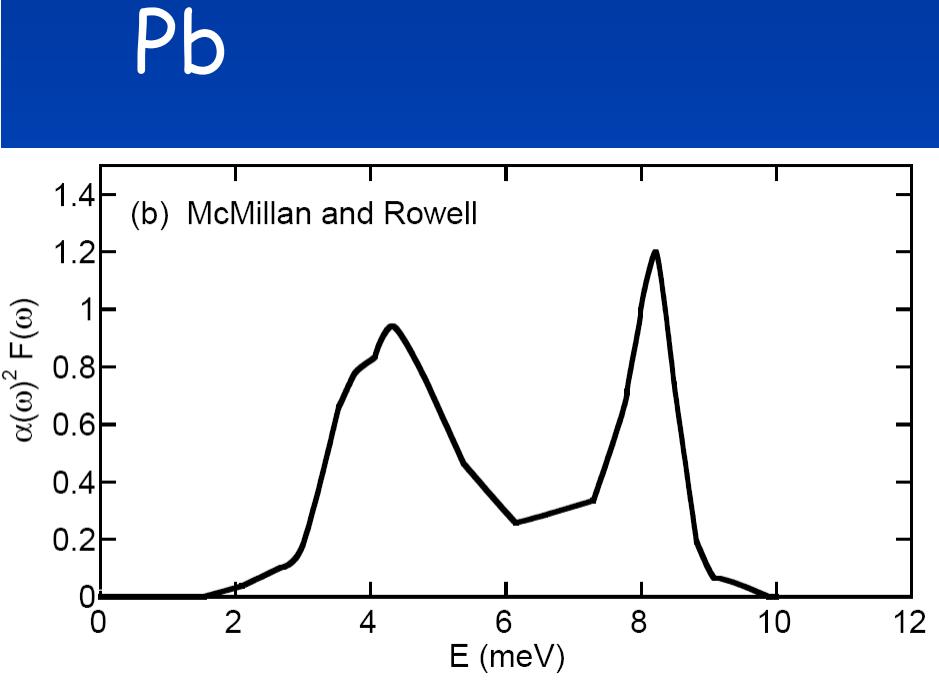
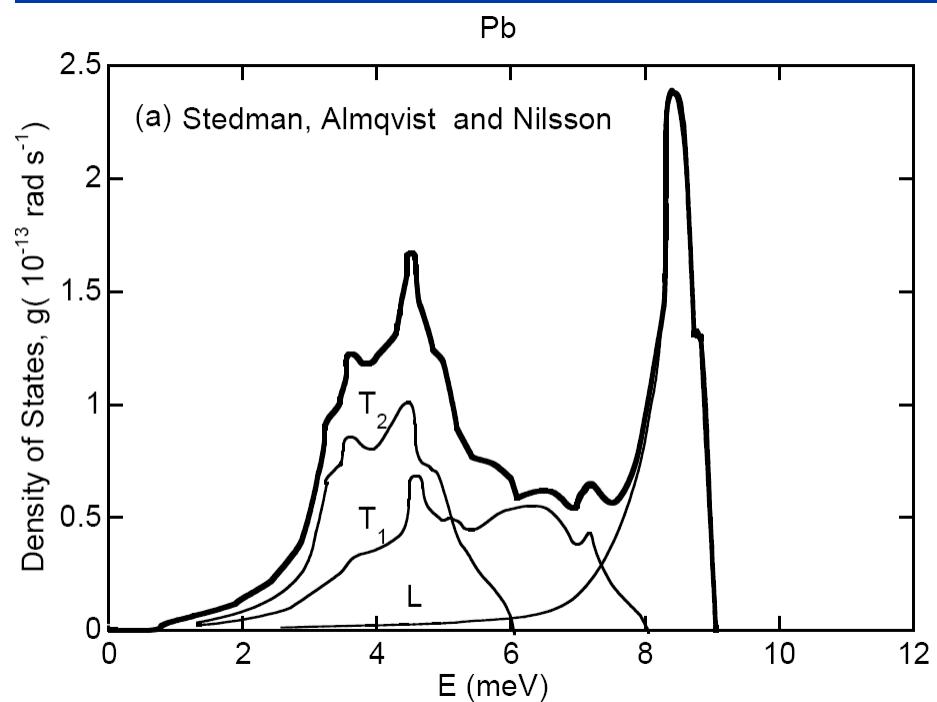
F. Dogan (Missouri-Rolla)

M. Mangkorntong (Tokyo)

M. Nohara (Tokyo)

Hide Takagi (Tokyo)

# 1) What excitations are relevant to pairing in the cuprates?



- phonon DOS,  $F(\omega)$
- $\alpha^2(\omega) F(\omega)$  from SIS tunnelling

SIS Tunnelling in Conventional Superconductors

## Direct Probes of Bosonic Excitations

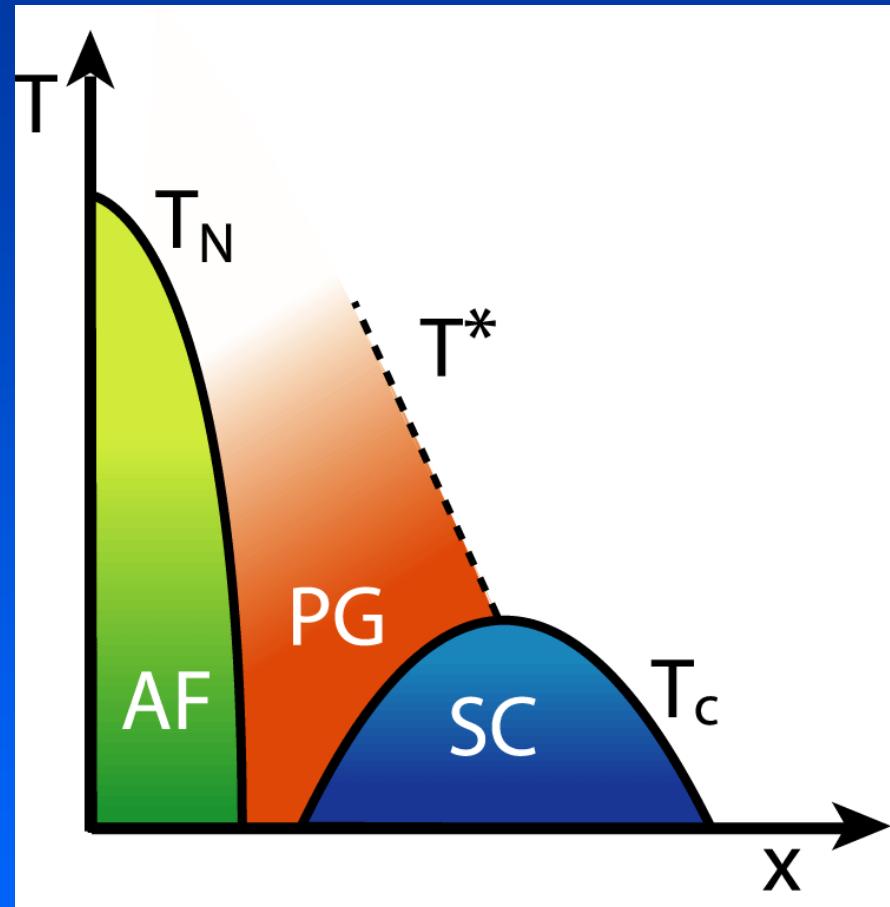
- neutrons
- x-rays
- Raman
- NMR
- .....

## Electronic (quasiparticle) spectroscopies

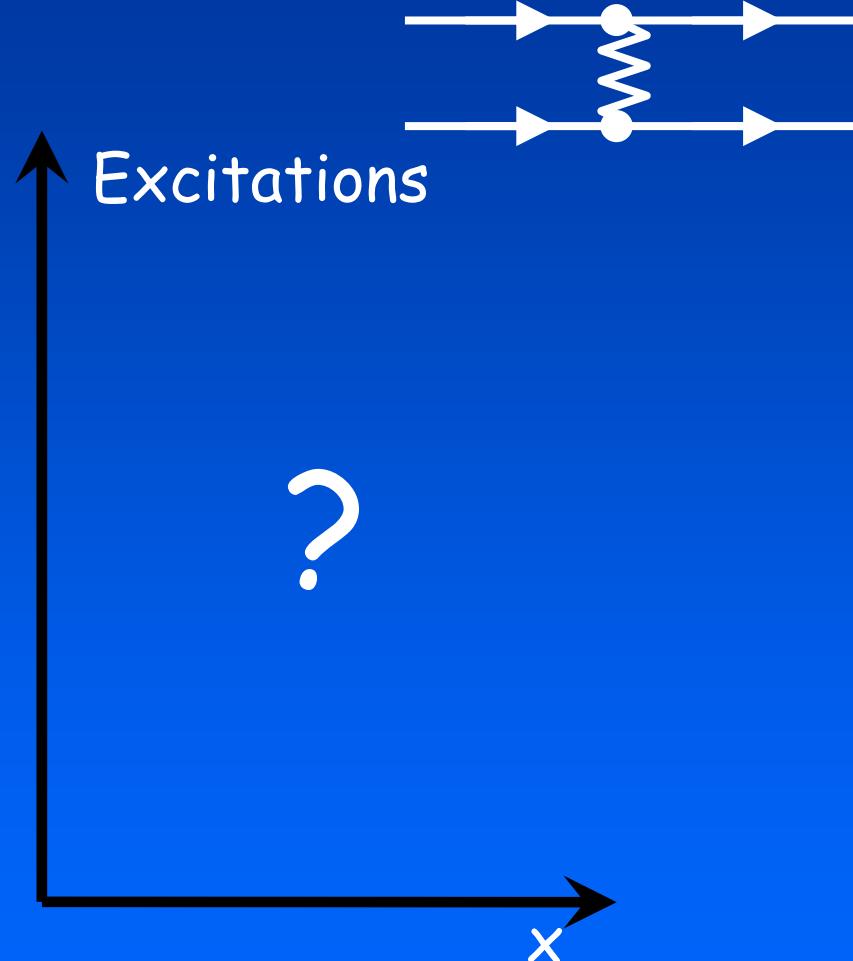
- ARPES
- Tunnelling
- Optical conductivity
- de Haas-van Alphen

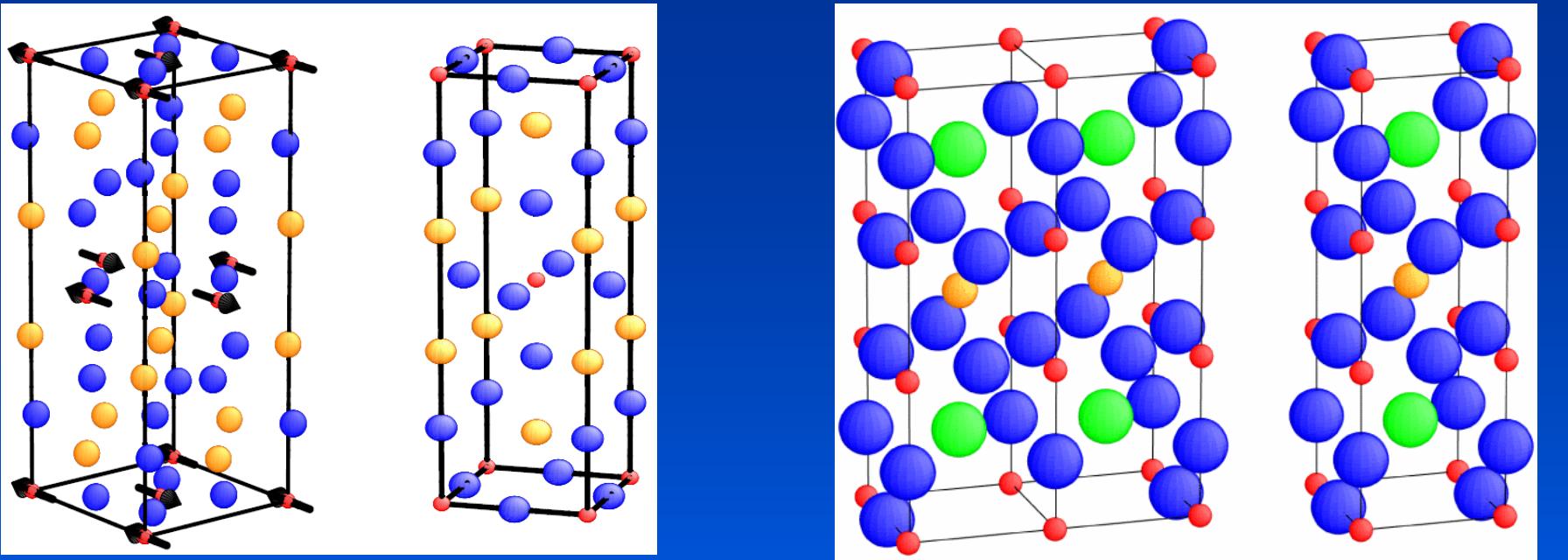


2 )What is the relationship between the (magnetic) excitations and the phase diagram of the cuprates?

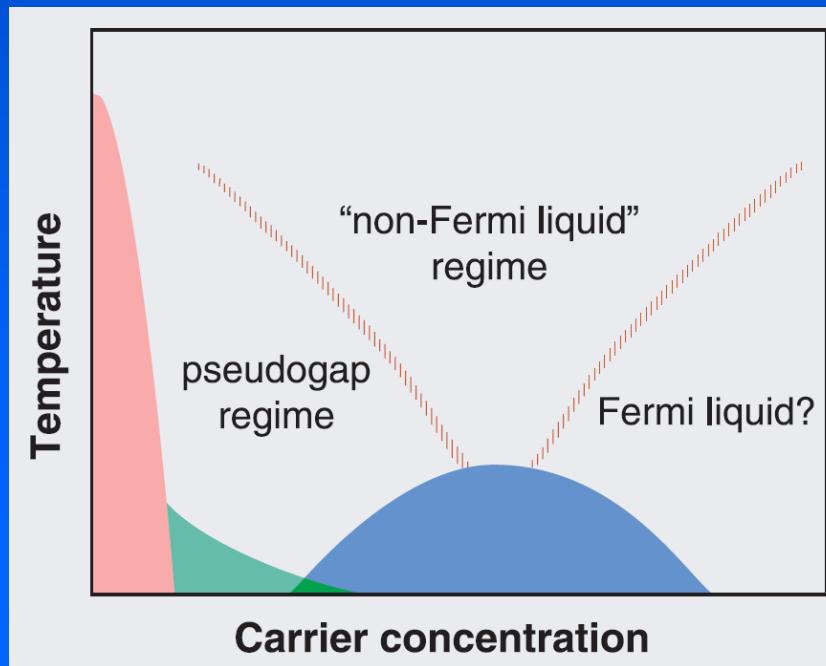


$\Rightarrow$  pseudogap

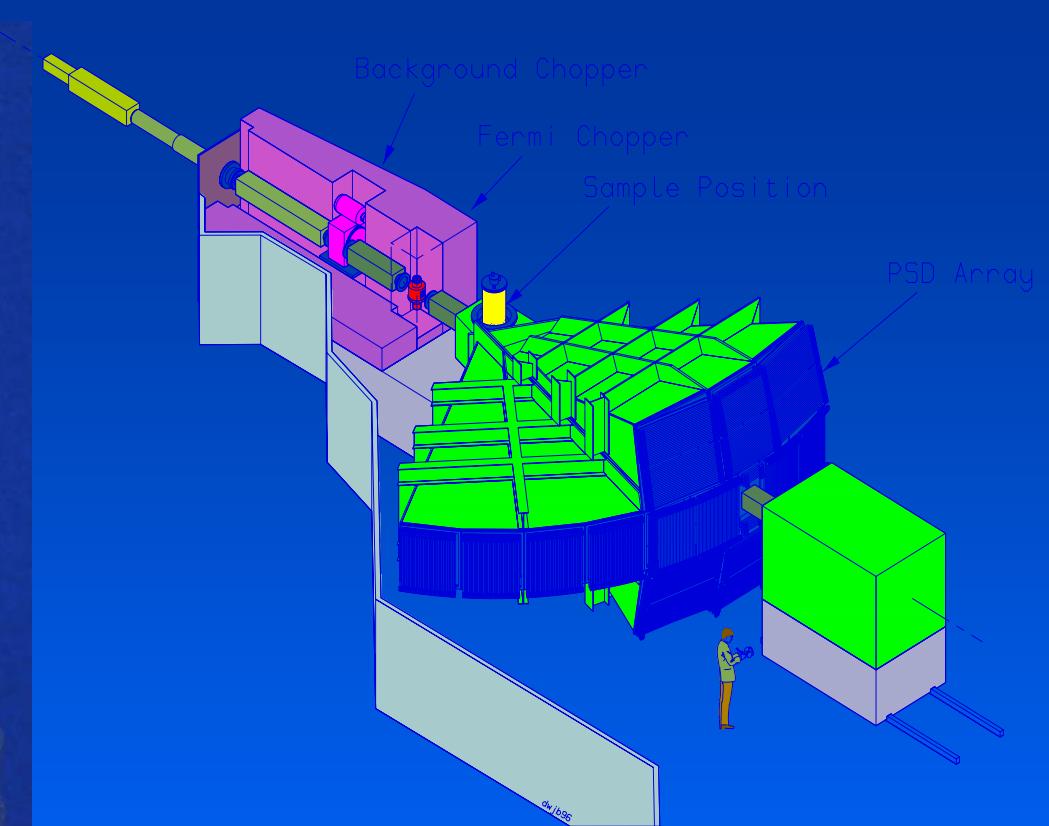




$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



$\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$



MAPS

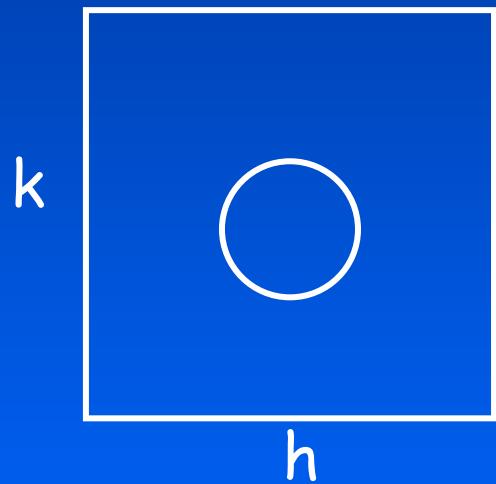
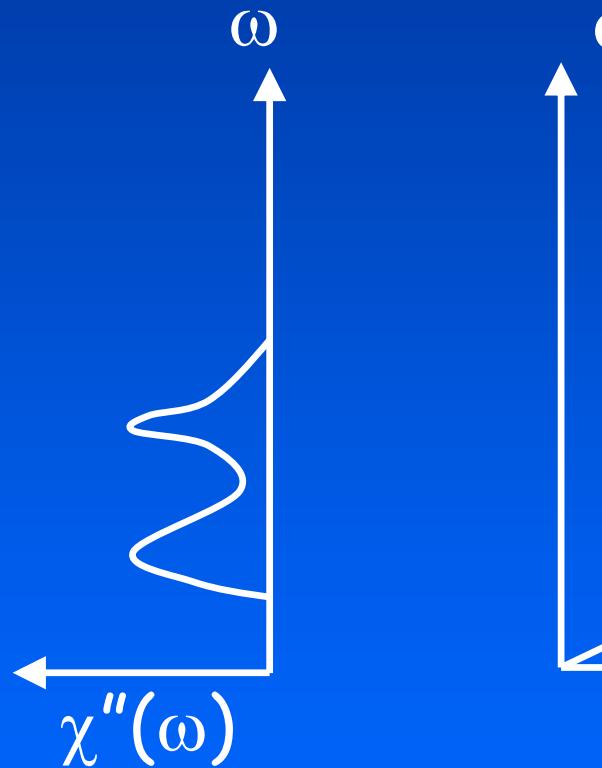
72 g  $\text{La}_{1.78}\text{Sr}_{0.22}\text{CuO}_4$

# What does inelastic neutron scattering tell us?

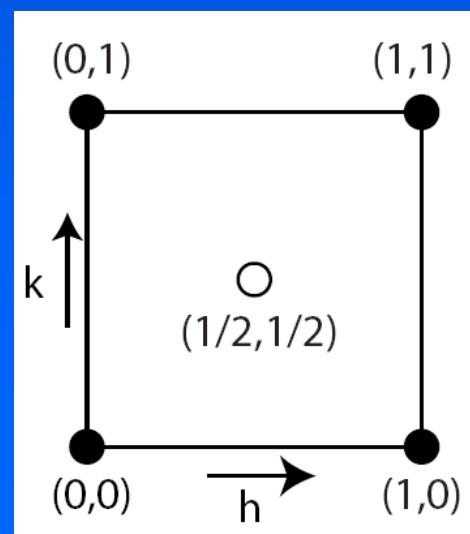
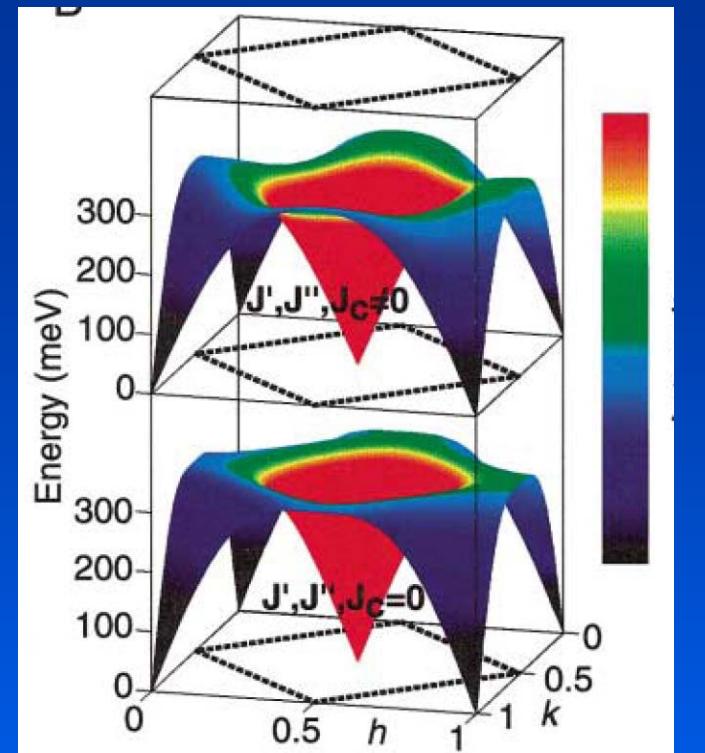
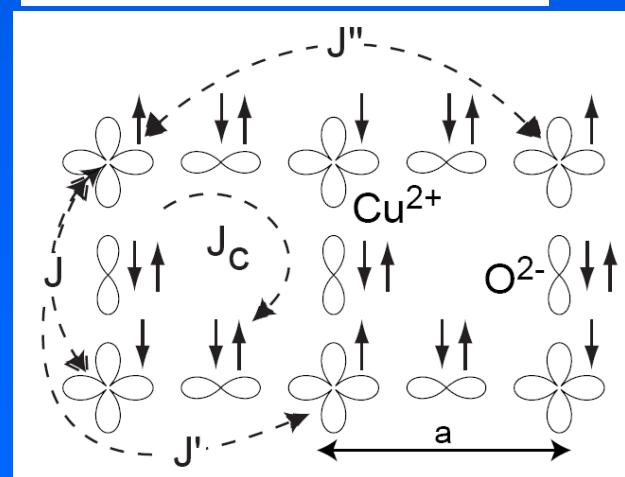
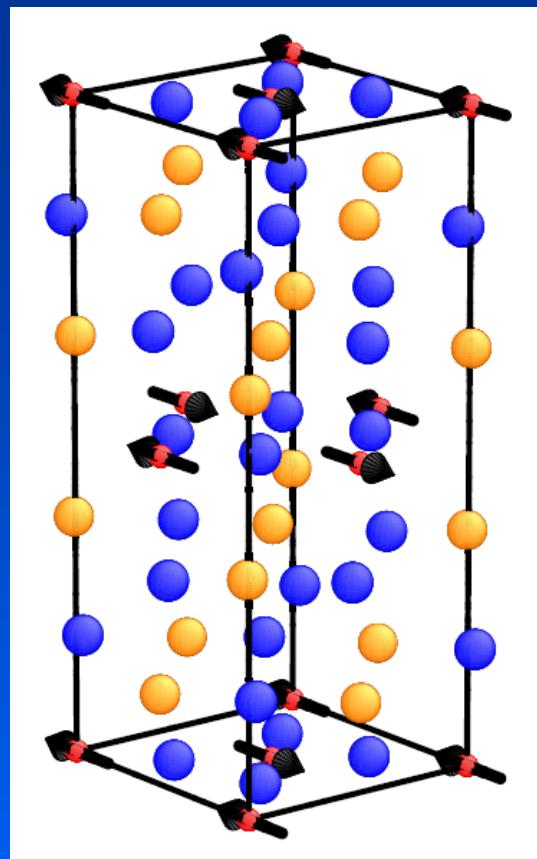
$$\frac{d^2\sigma}{d\Omega \, dE} = (\gamma r_e)^2 \frac{k_f}{k_i} |F(\mathbf{Q})|^2 \left( \frac{2/\pi g^2 \mu_B^2}{1 - \exp(-\hbar\omega/kT)} \right) \chi''(\mathbf{Q}, \omega)$$

$$\chi''_{\text{local}}(\omega) = \frac{\int_{BZ} \chi''(\mathbf{Q}, \omega) \, d\mathbf{Q}}{\int_{BZ} d\mathbf{Q}}$$

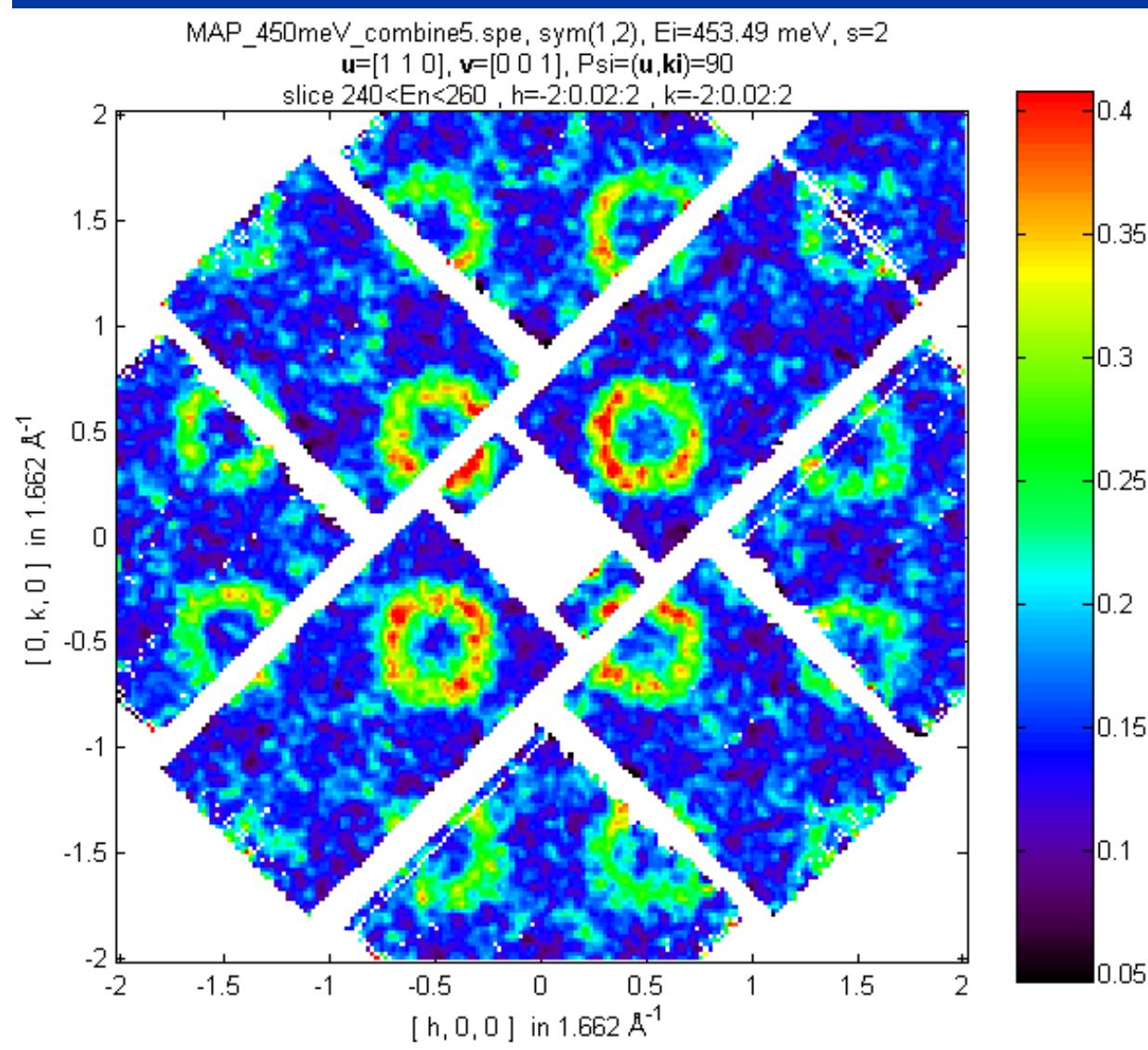
# The response function $\chi''(q,\omega)$



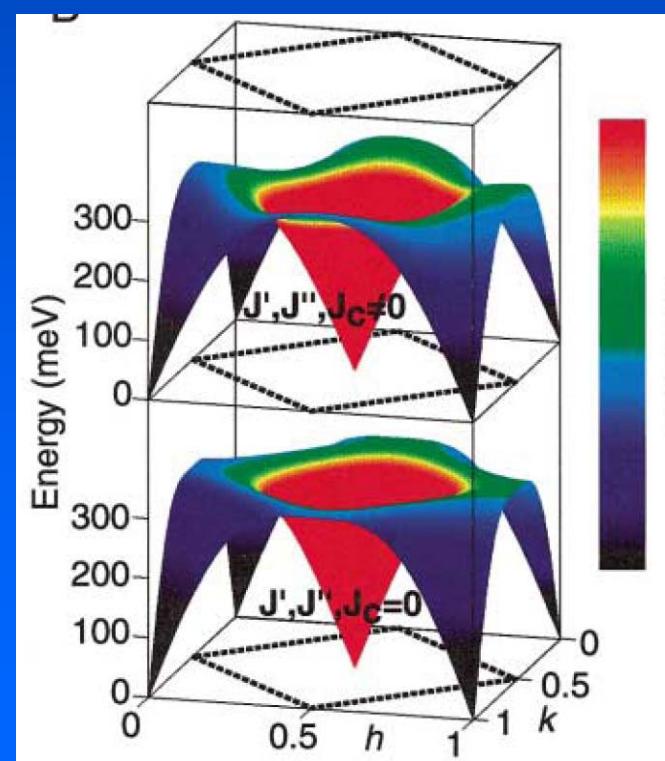
# Example: spin waves in $\text{La}_2\text{CuO}_4$



# Example: spin waves in $\text{La}_2\text{CuO}_4$

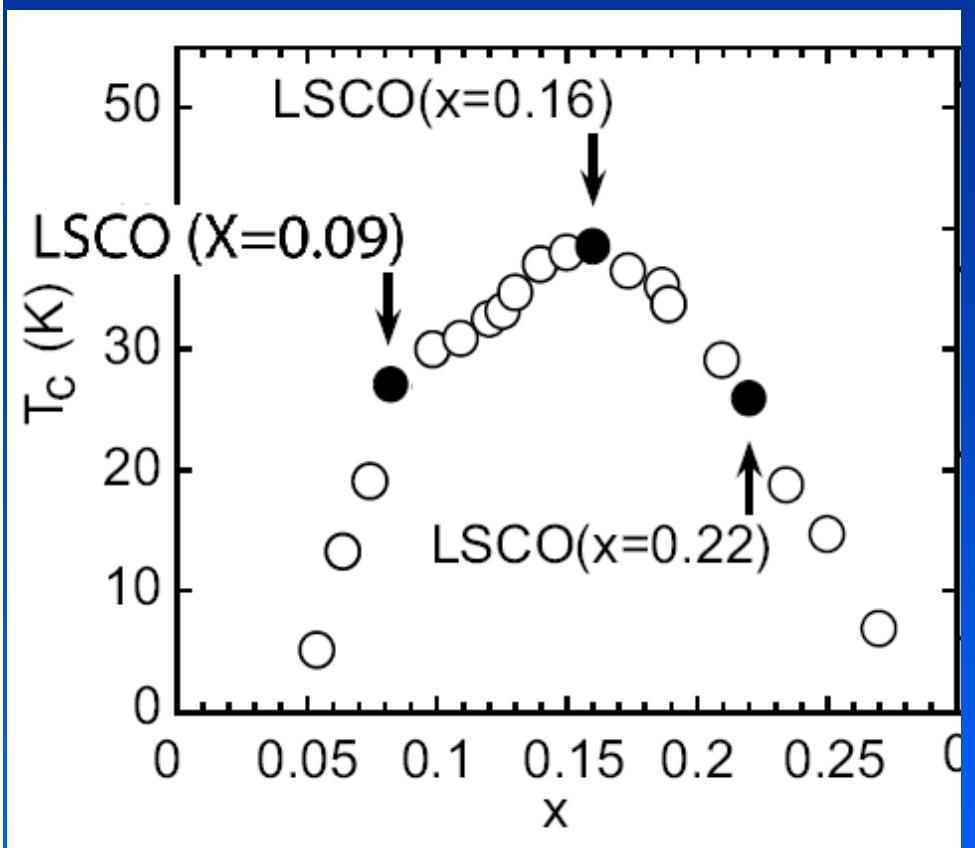
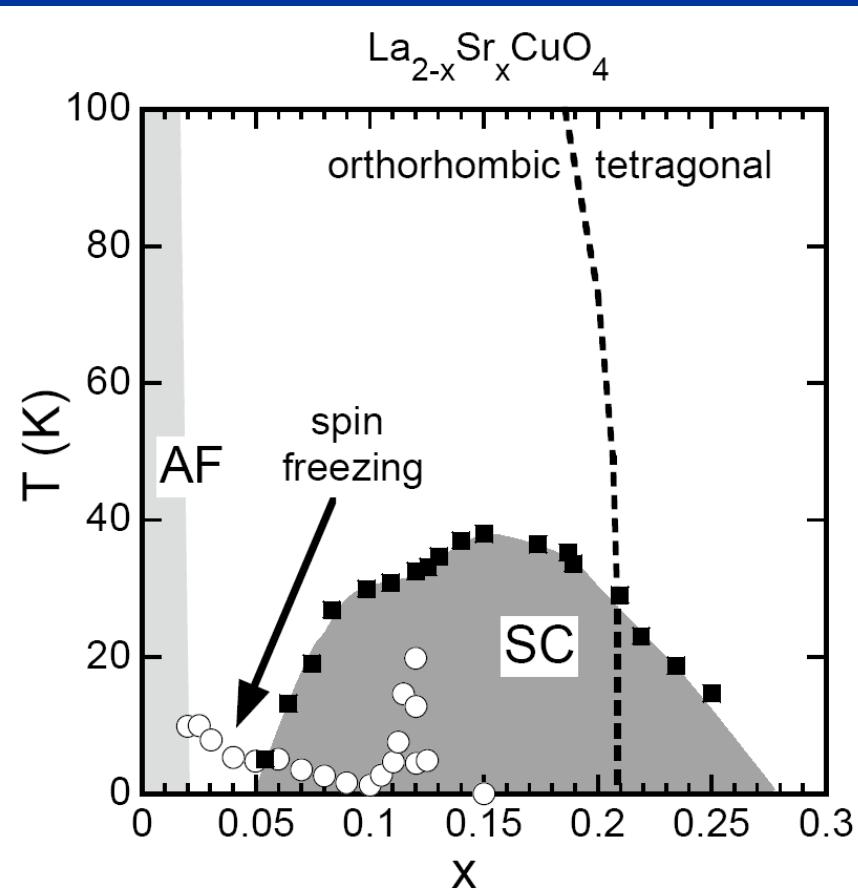


$E=250$  meV

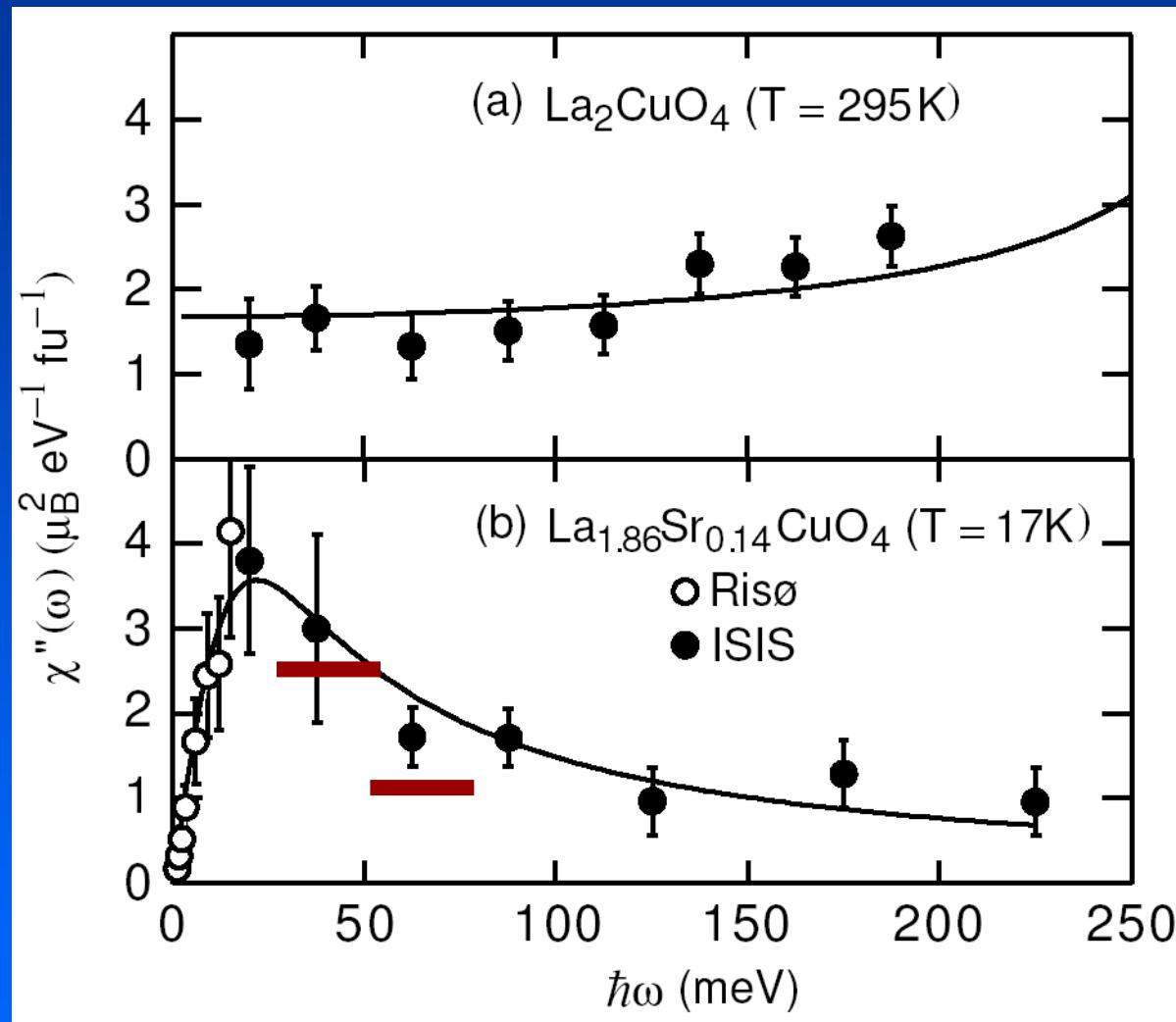


Spin Fluctuations in  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$   
(new stuff)

# $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



# Spin excitations in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

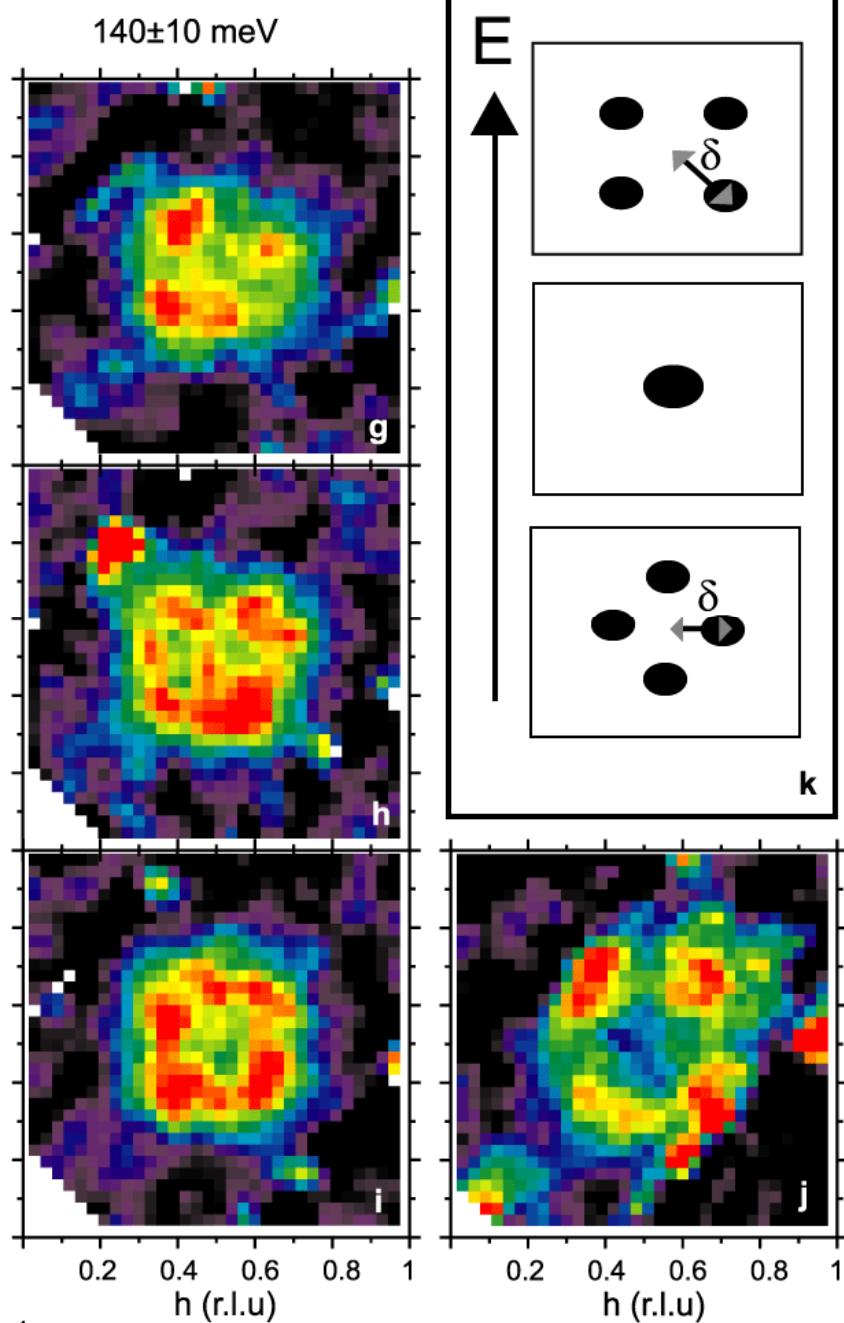
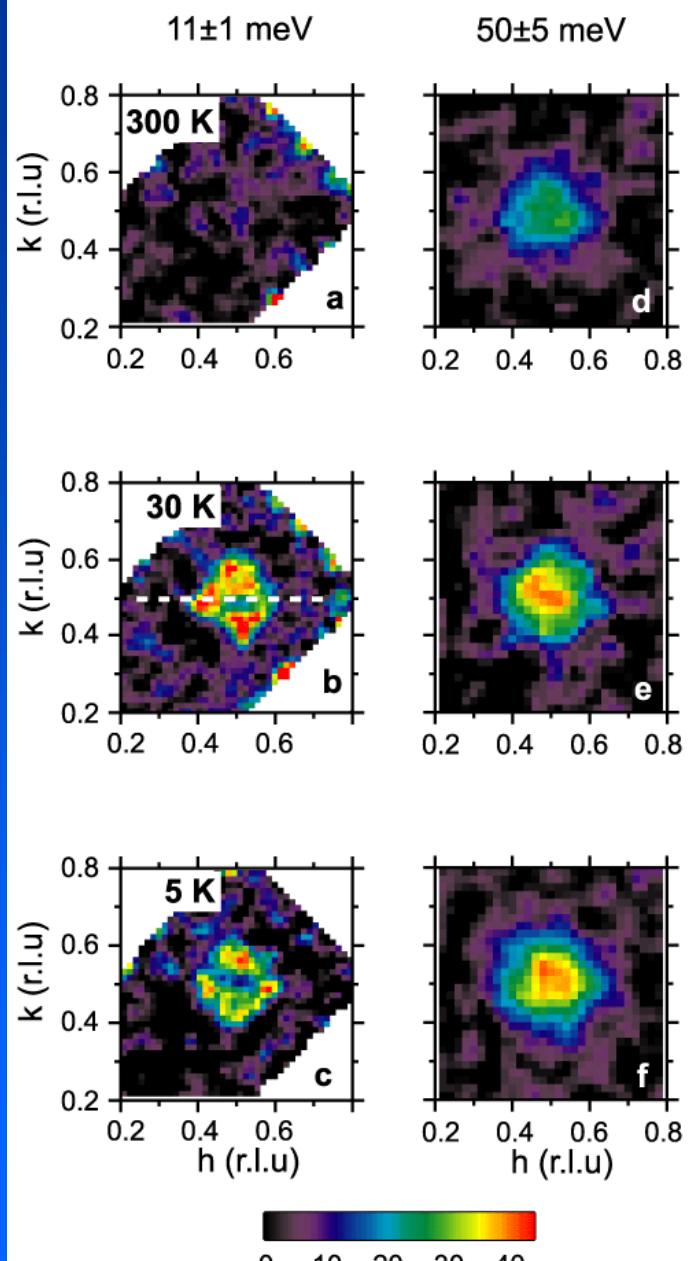


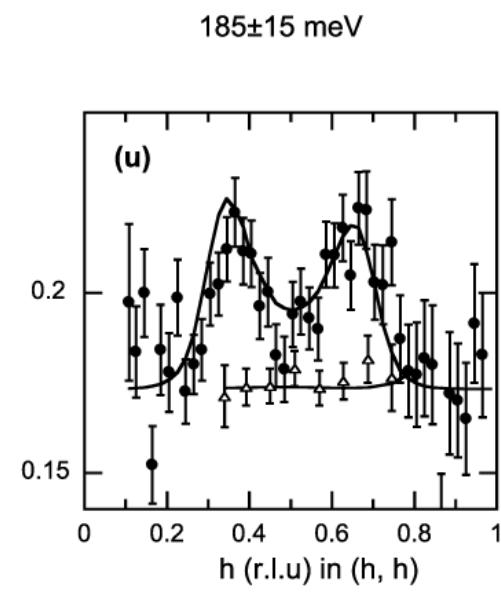
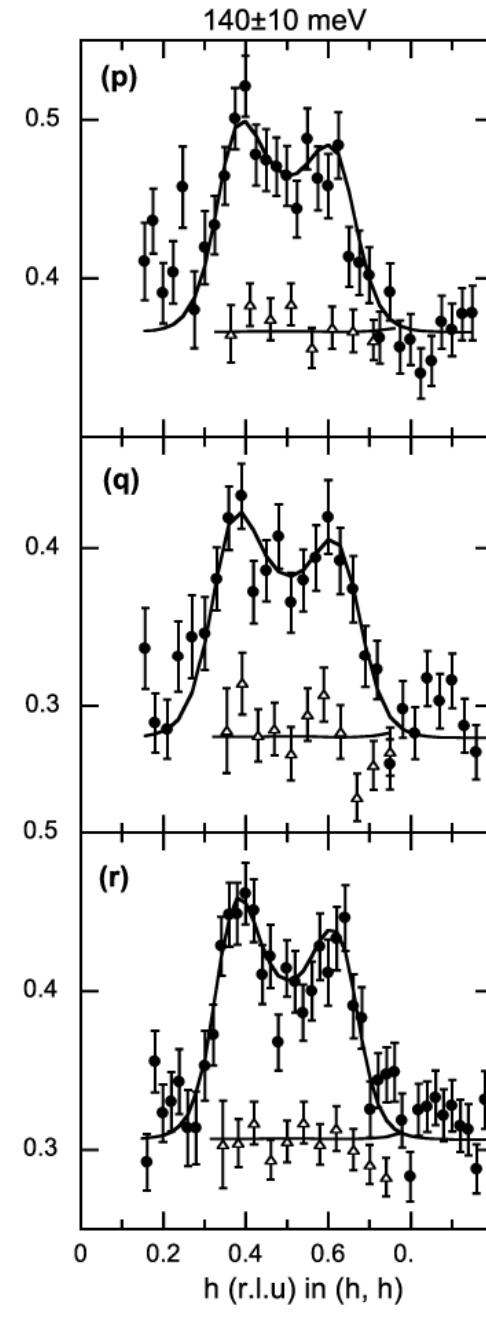
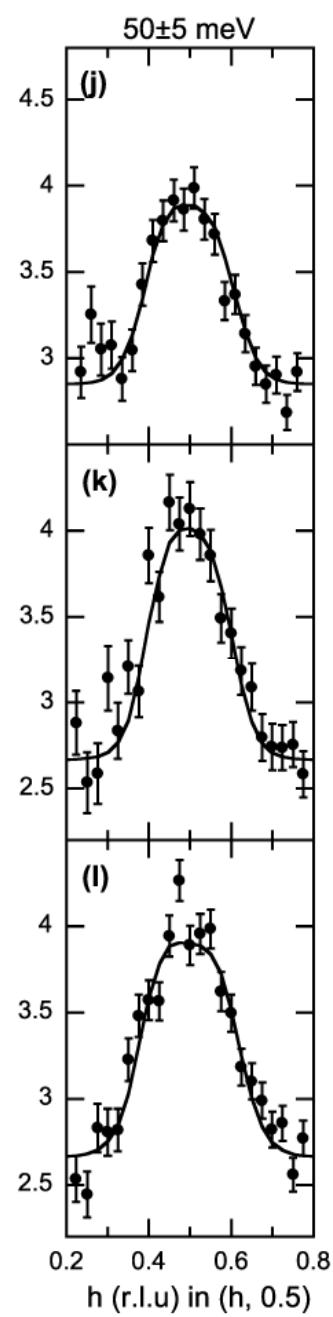
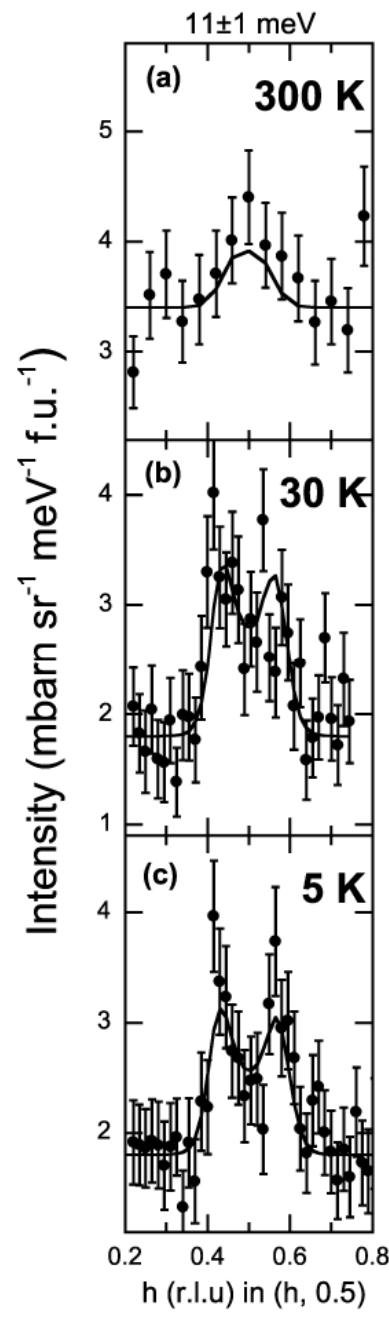
$\text{La}_{1.91}\text{Sr}_{0.09}\text{CuO}_4$  (underdoped)

$\text{La}_{1.84}\text{Sr}_{0.16}\text{CuO}_4$  (optimal)

$\text{La}_{1.78}\text{Sr}_{0.22}\text{CuO}_4$  (overdoped)

**$\text{La}_{1.91}\text{Sr}_{0.09}\text{CuO}_4$**





## Modified Lorentzian Cross Section (Sato-Maki Cross section)

$$\chi''(\mathbf{Q}, \omega) = \chi_\delta(\omega) \frac{\kappa^4(\omega)}{[\kappa^2(\omega) + R(\mathbf{Q})]^2}$$

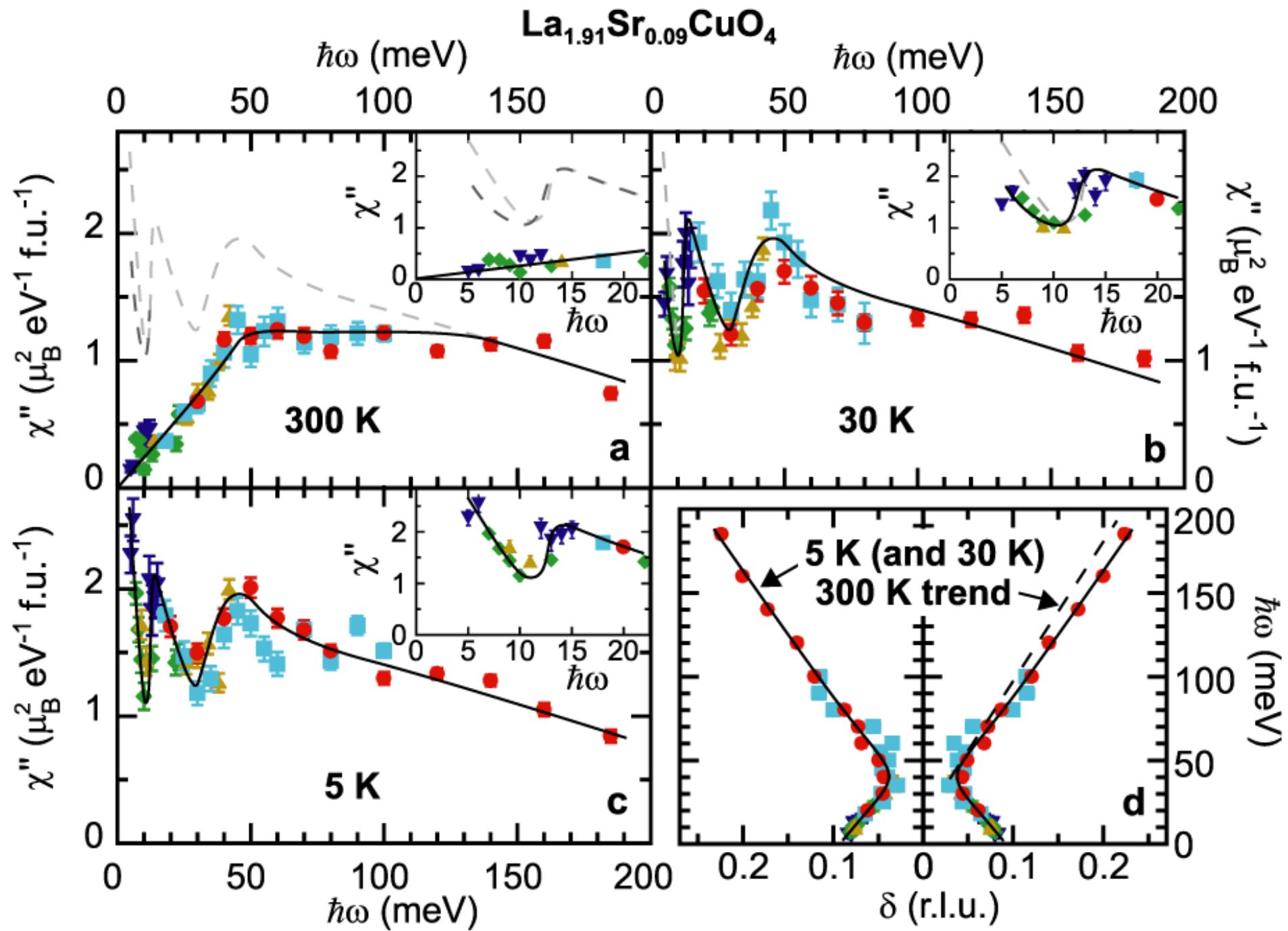
$$R(\mathbf{Q}) = \frac{[(h - \frac{1}{2})^2 + (k - \frac{1}{2})^2 - \delta^2]^2 + \lambda(h - \frac{1}{2})^2(k - \frac{1}{2})^2}{4\delta^2}$$

$\chi_\delta(\omega)$  amplitude

$\delta$  incommensurability

$\kappa(\omega)$  inverse correlation length

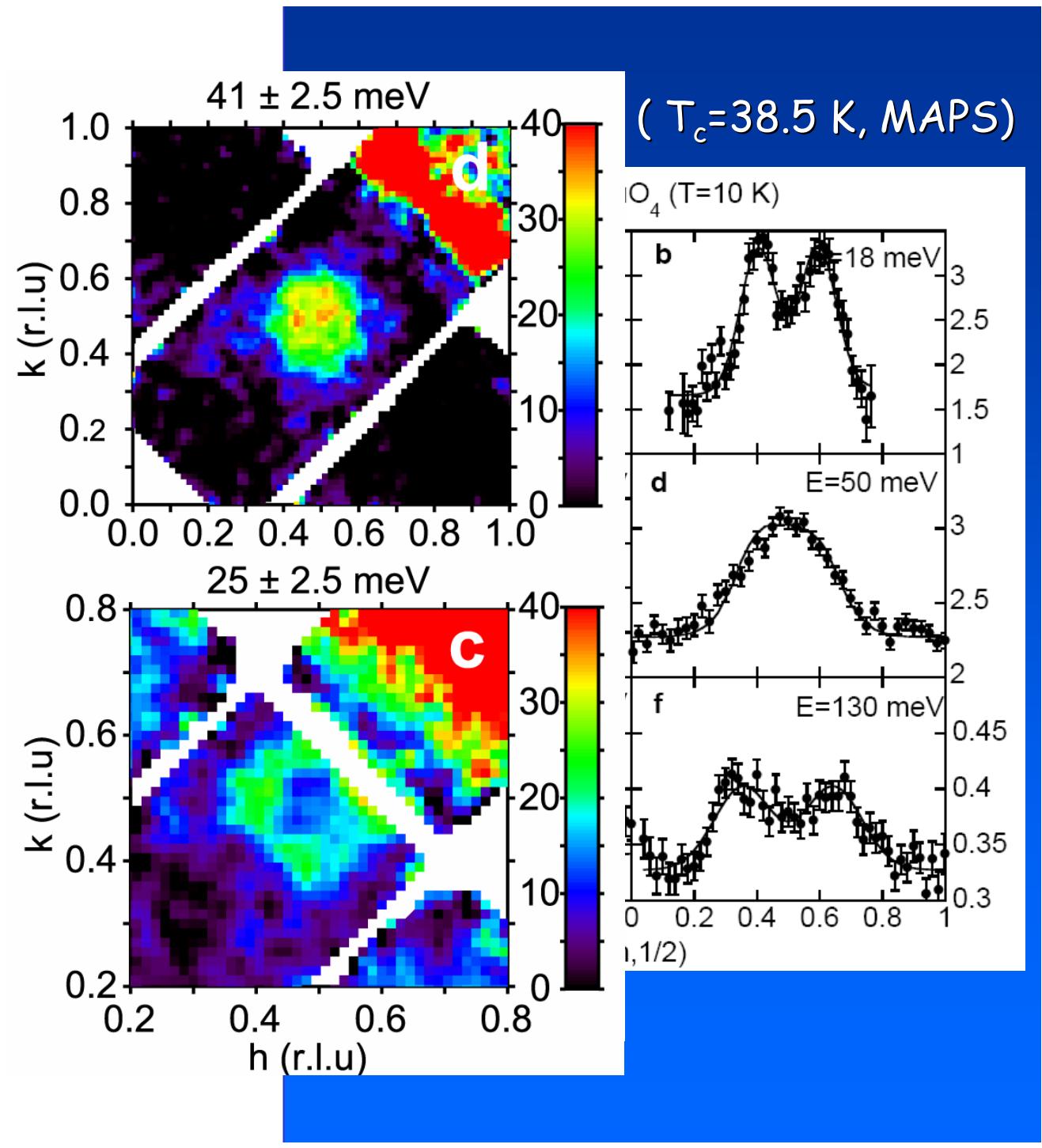
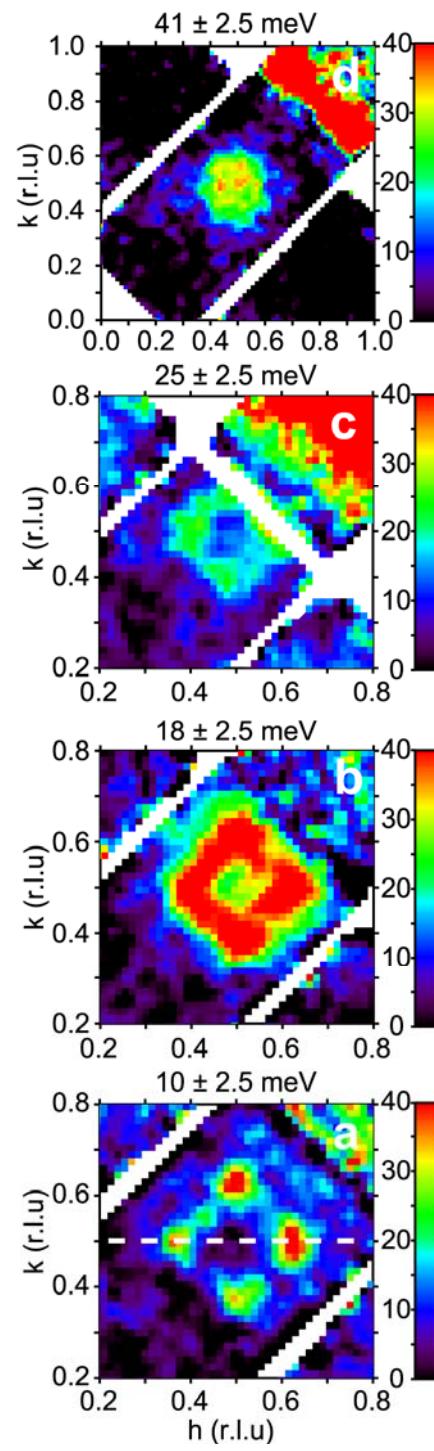
$\lambda$  anisotropy parameter

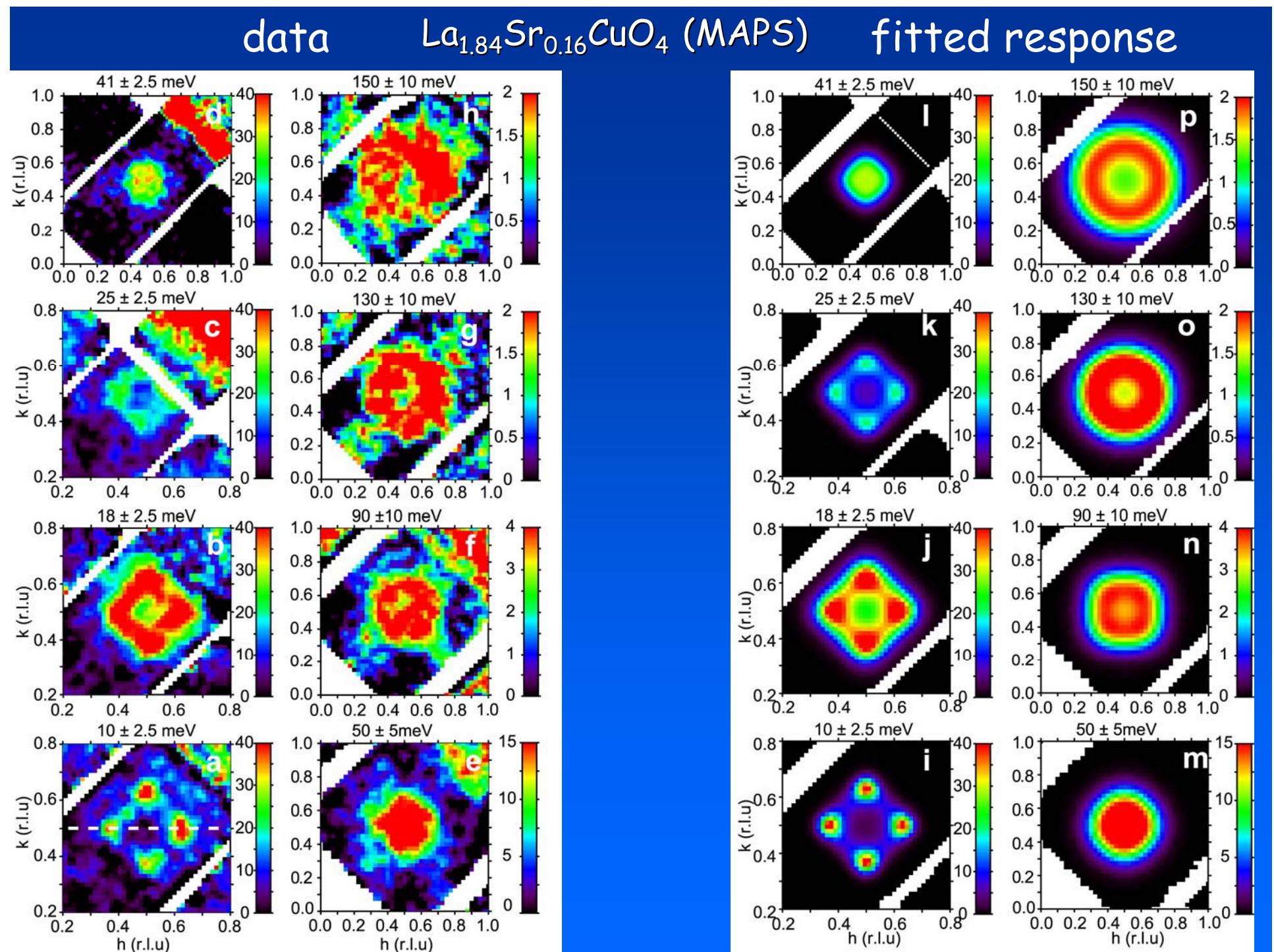


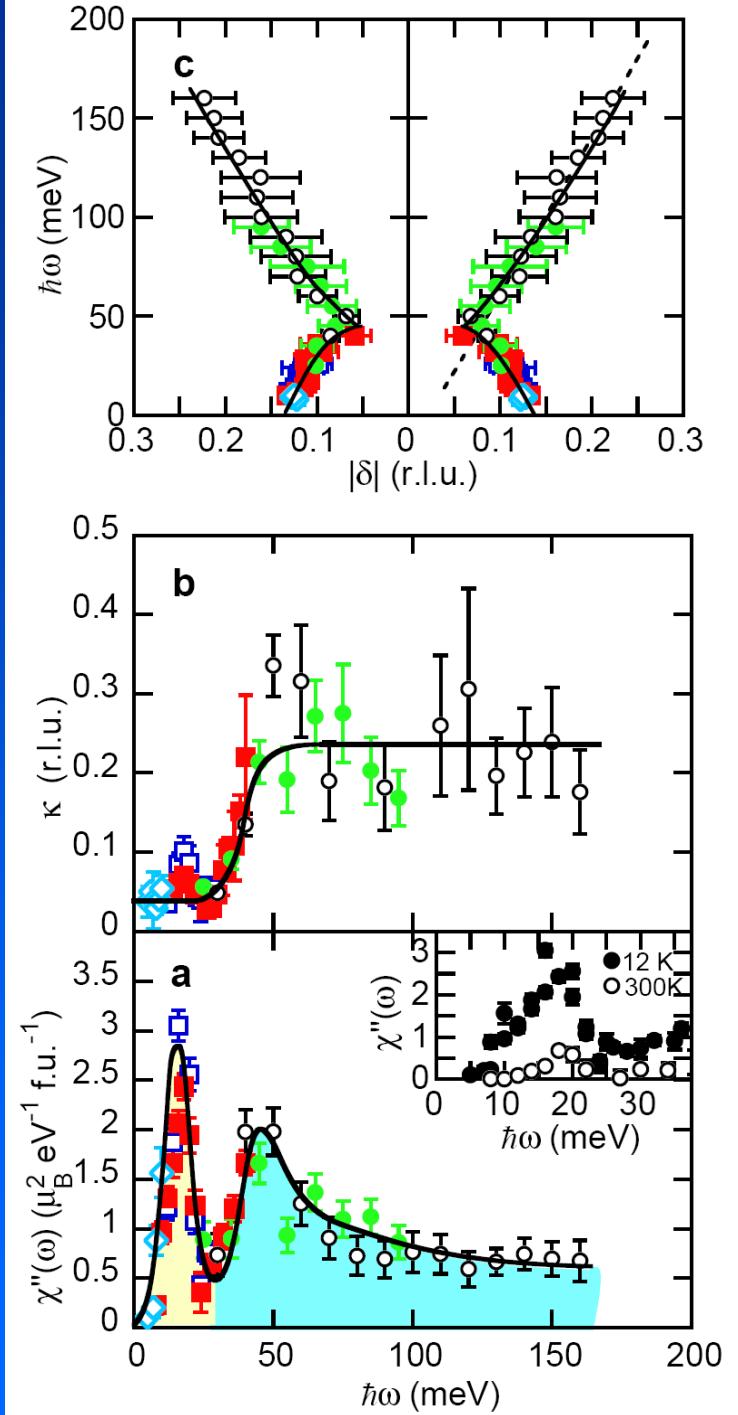
$\text{La}_{1.91}\text{Sr}_{0.09}\text{CuO}_4$  (underdoped)

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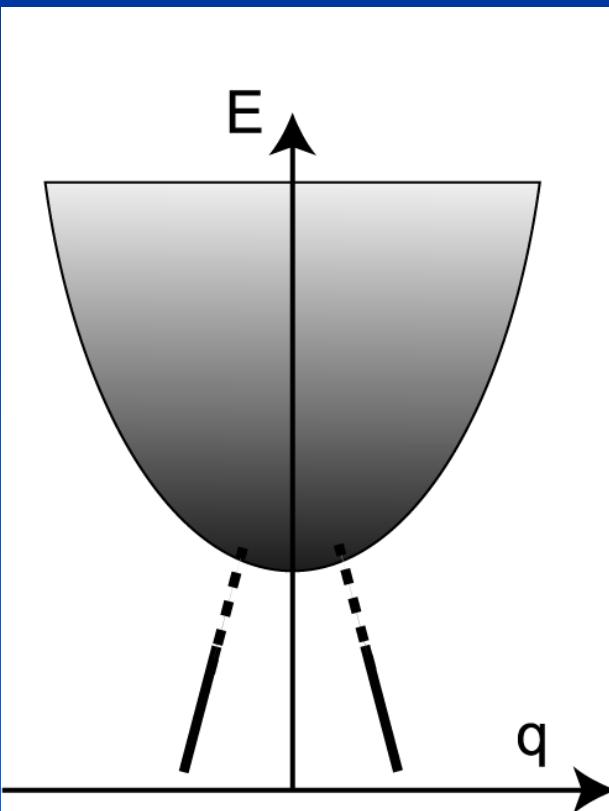
$\text{La}_{1.78}\text{Sr}_{0.22}\text{CuO}_4$  (overdoped)





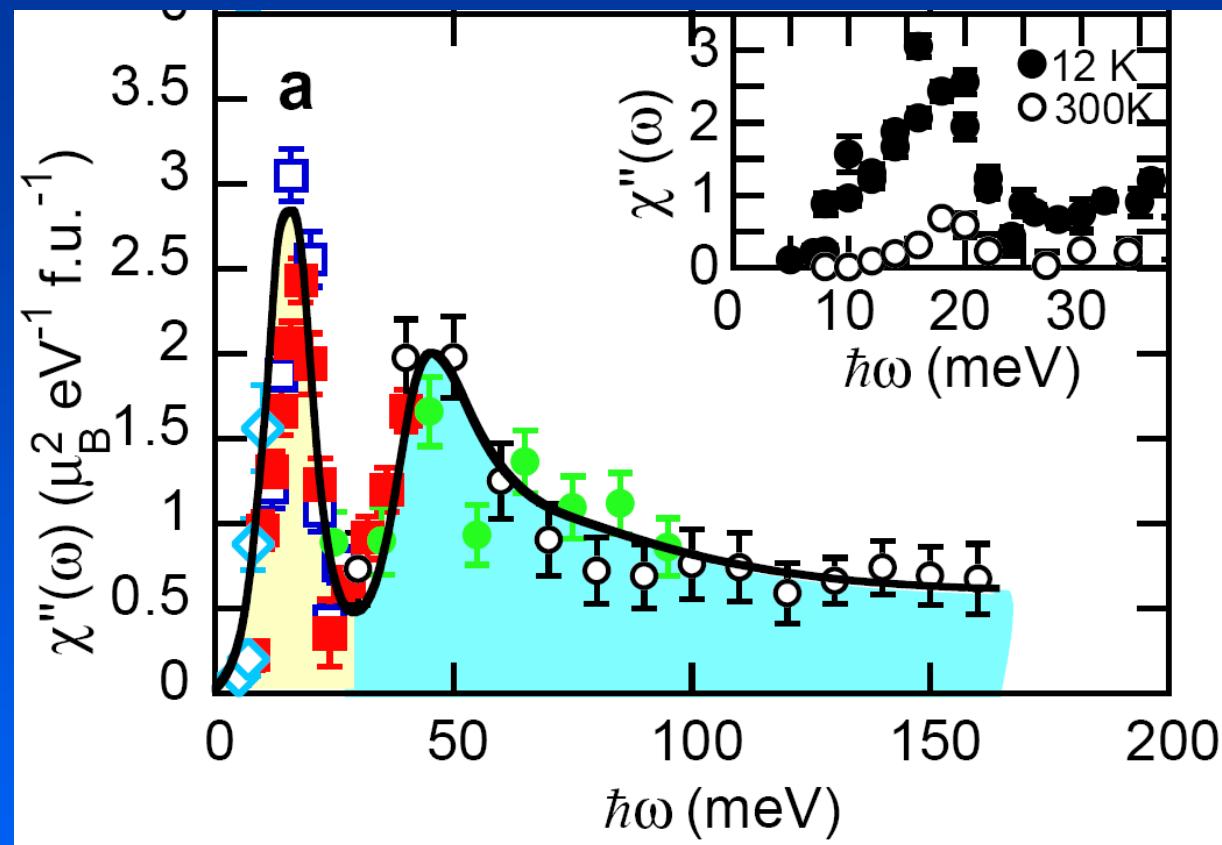


fitted parameters



$$\chi''(\omega) = \int \chi''(\mathbf{Q}, \omega) d^3 Q / \int d^3 Q$$

# $\text{La}_{1.84}\text{Sr}_{0.16}\text{CuO}_4$



## key features

- double-peaked structure (two energy scales 18,50 meV)
- rapid broadening of pattern near 40 meV
- possible “rotation of pattern” at high energies

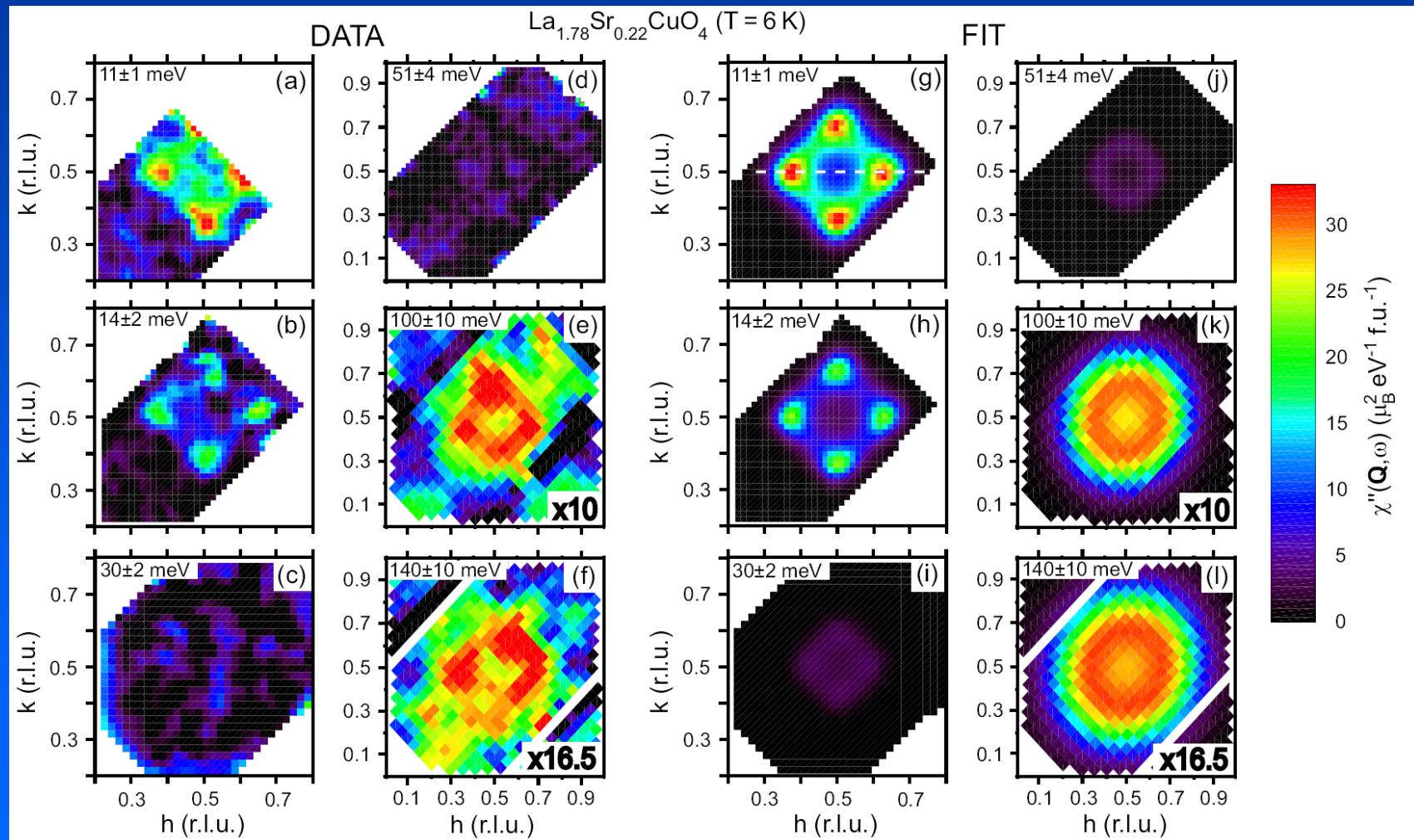
$\text{La}_{1.91}\text{Sr}_{0.09}\text{CuO}_4$  (underdoped)

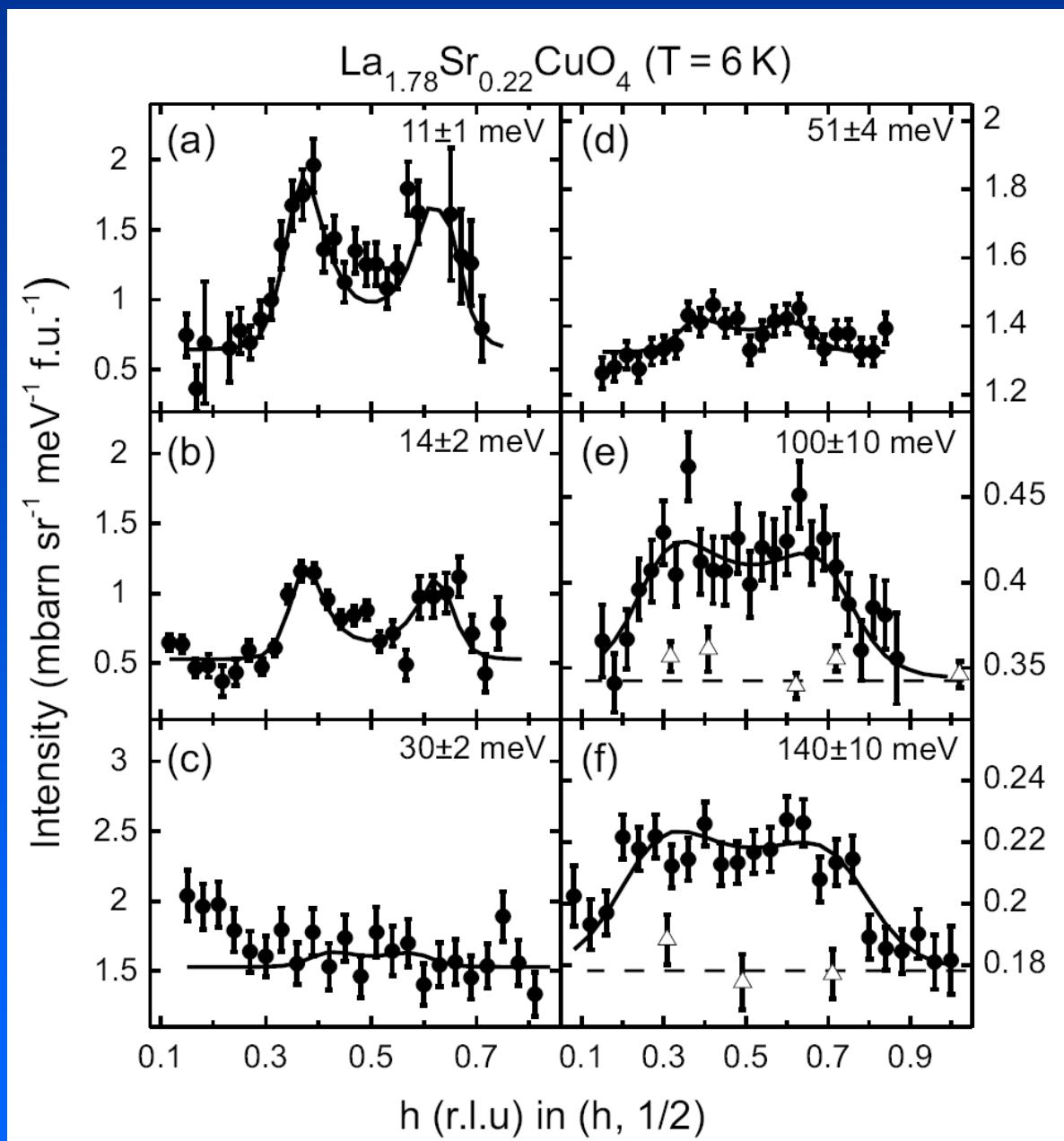
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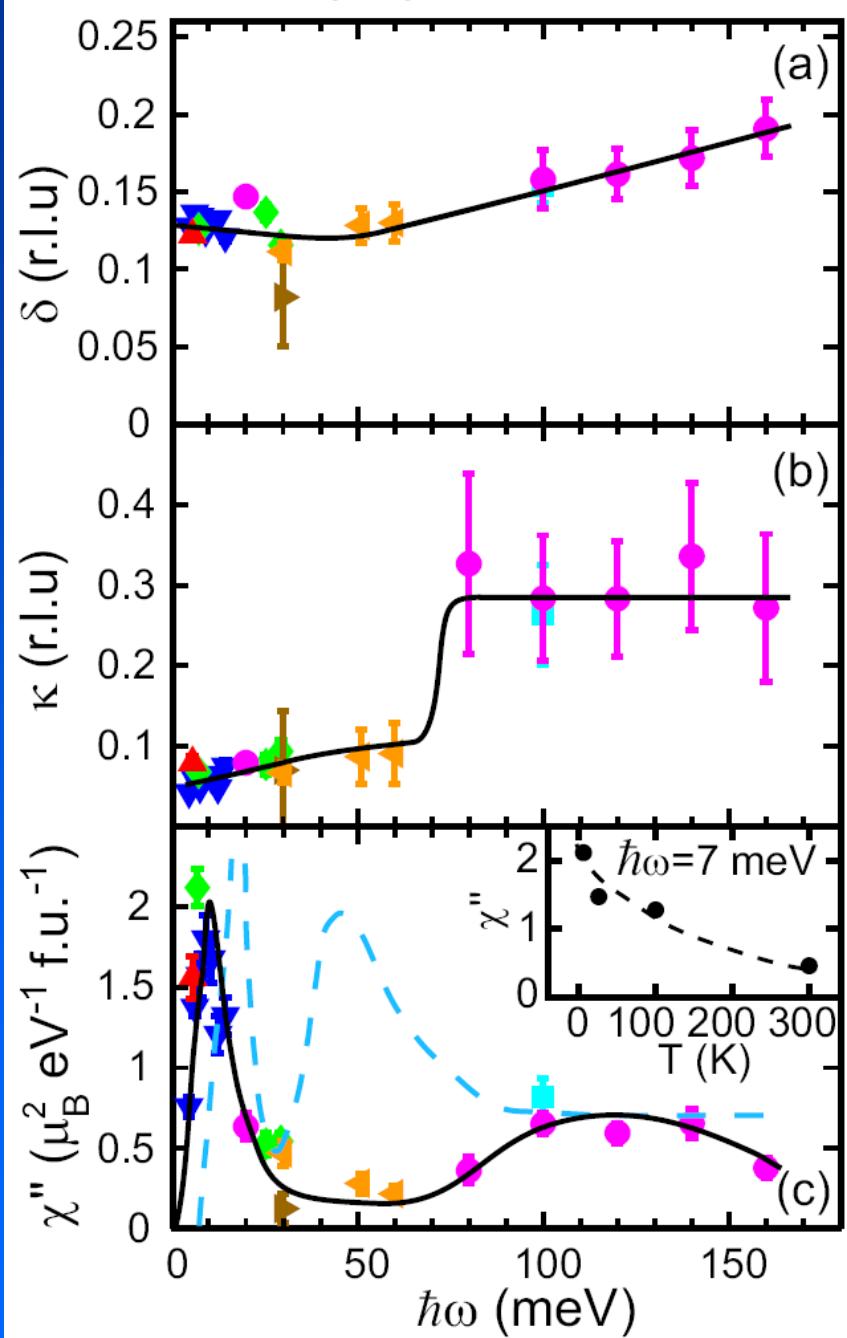
$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  ( $x=0.22$ ,  $T_c=26\text{K}$ )

Overdoped Sample

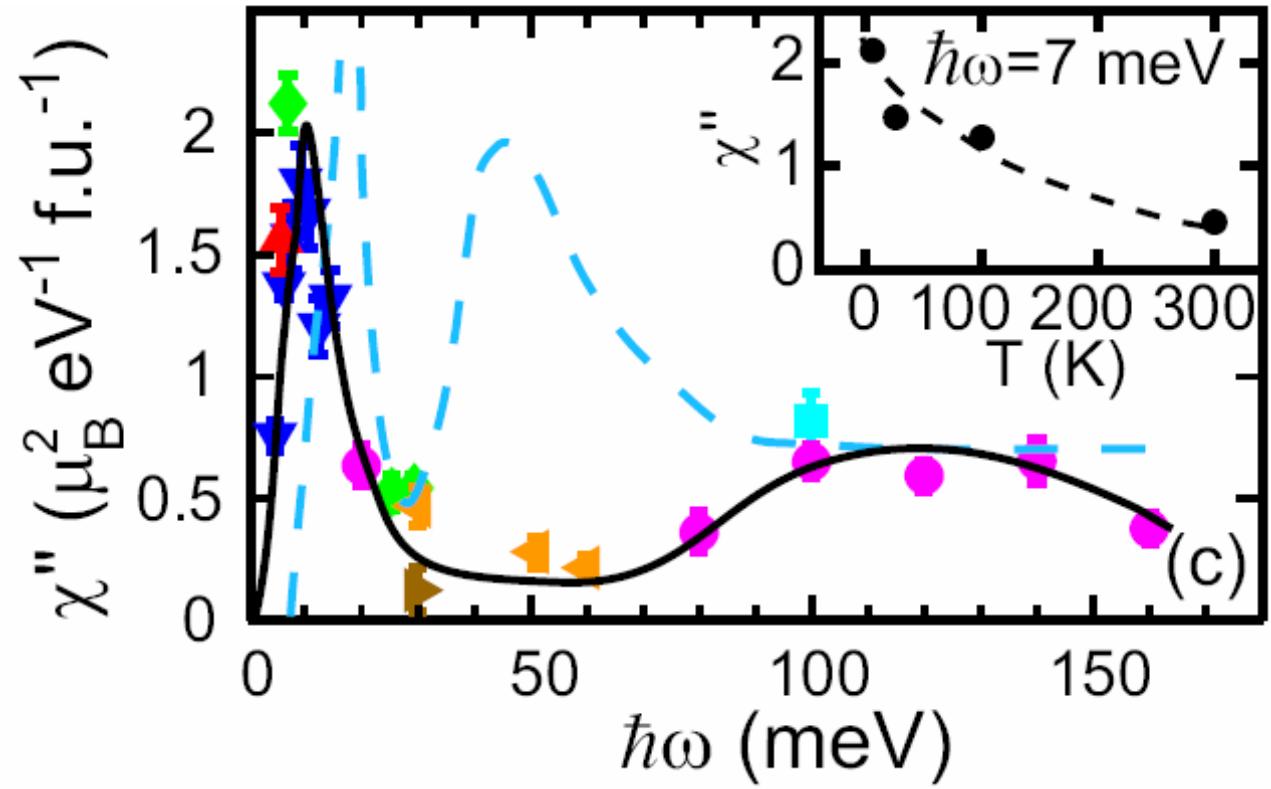




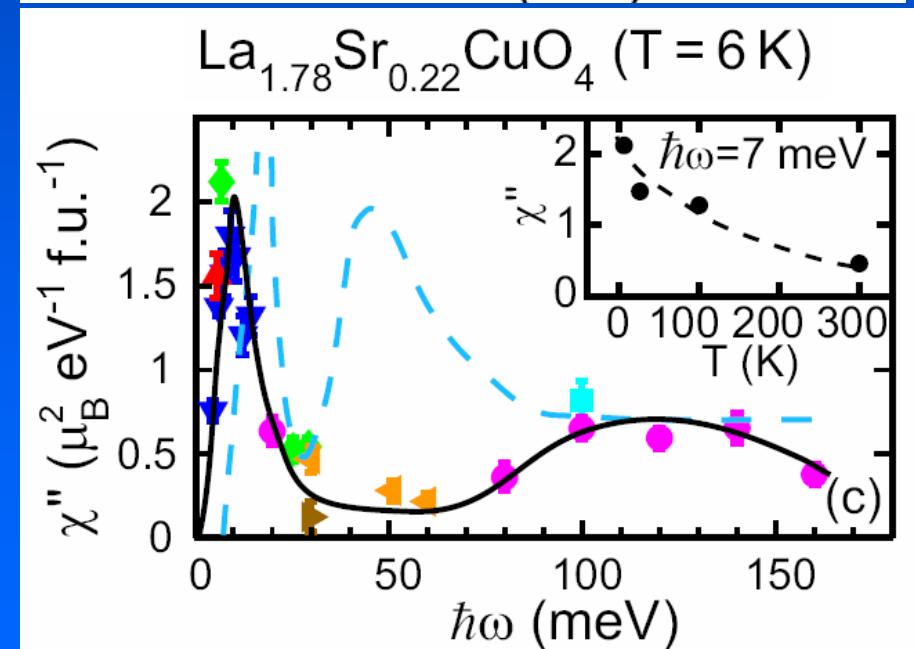
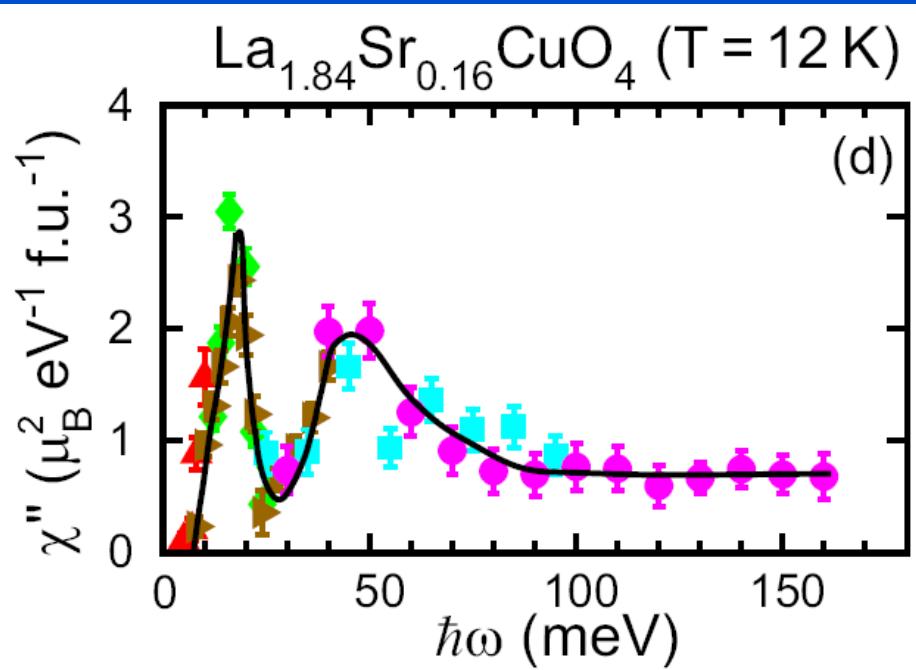
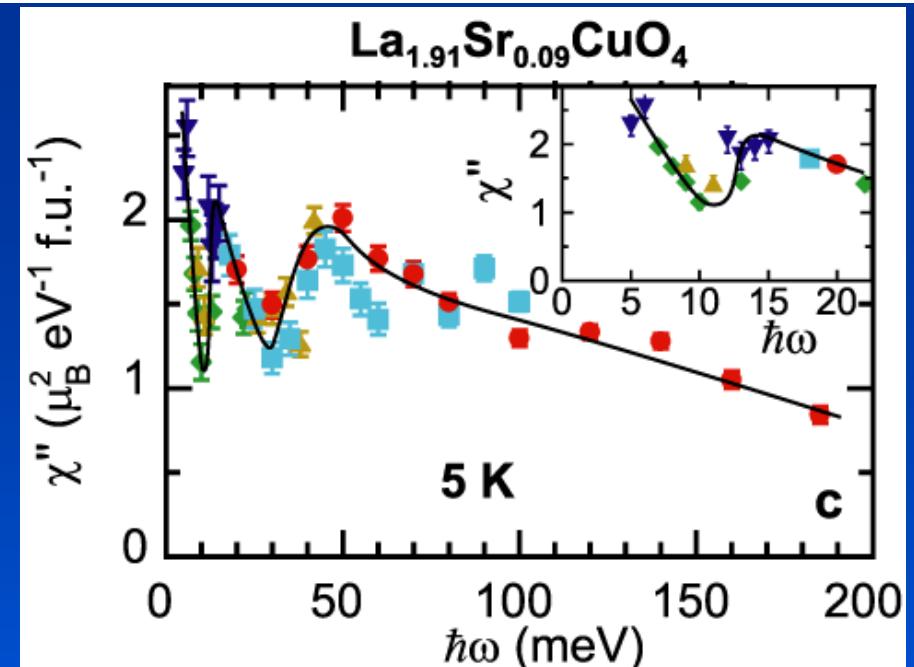
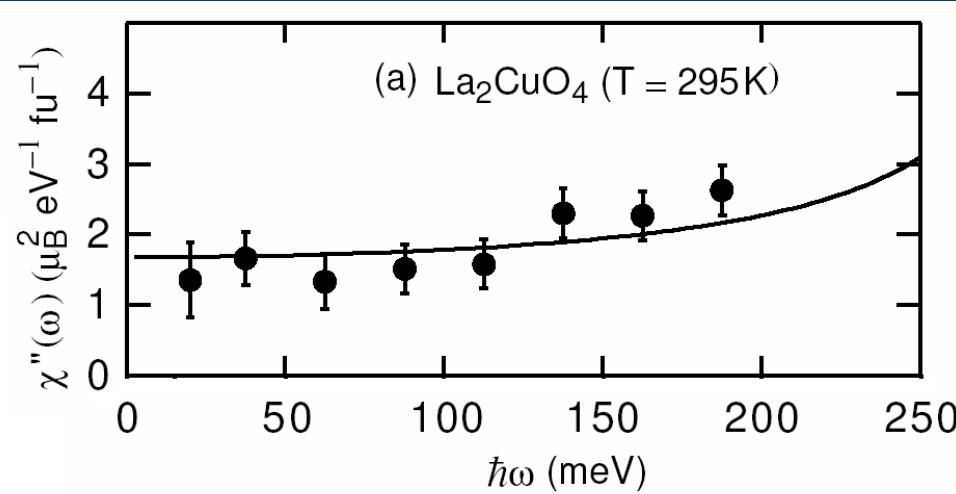
$\text{La}_{1.78}\text{Sr}_{0.22}\text{CuO}_4$  ( $T = 6 \text{ K}$ )



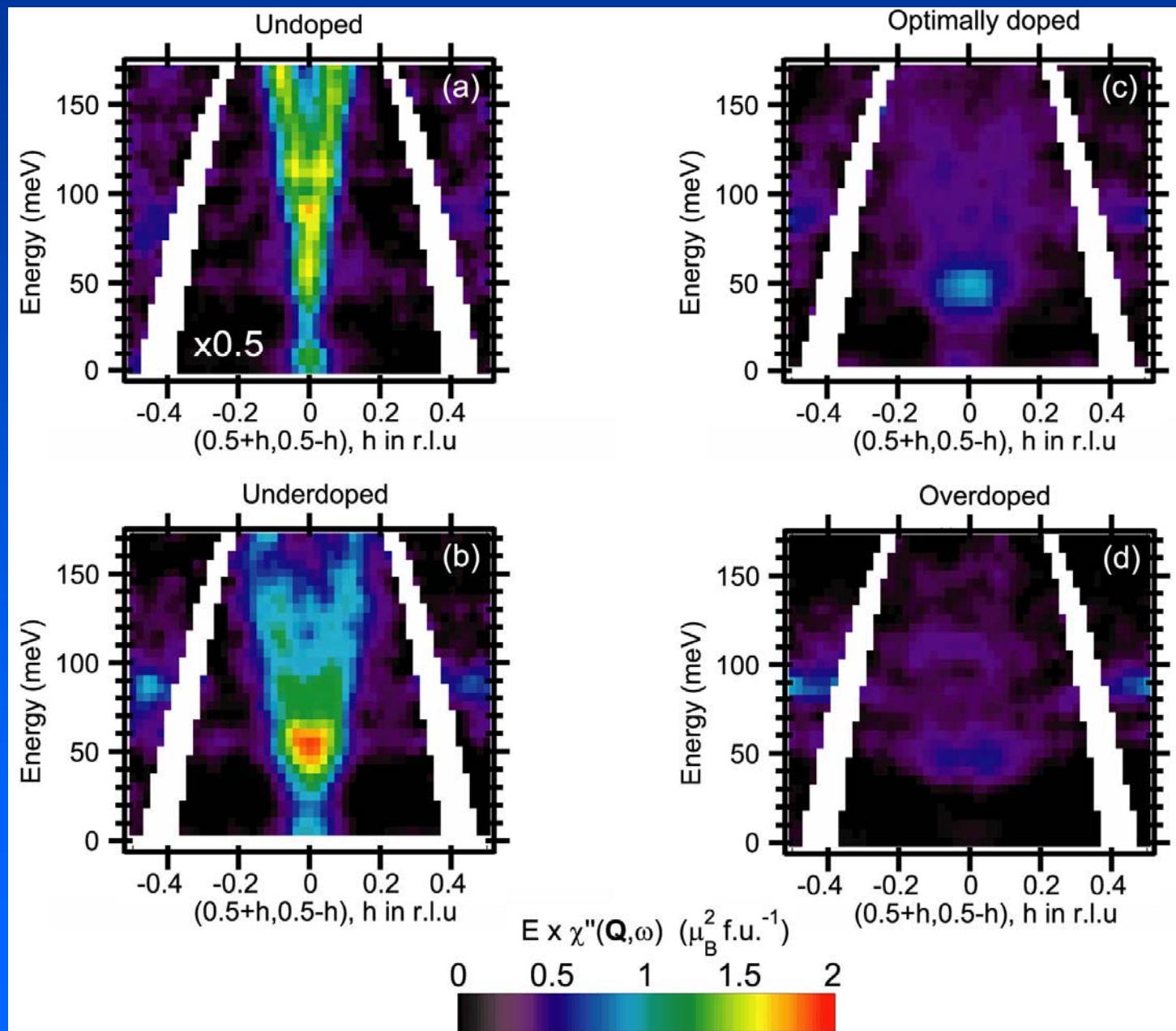
$\text{La}_{1.78}\text{Sr}_{0.22}\text{CuO}_4$  ( $T = 6 \text{ K}$ )



## Evolution with doping

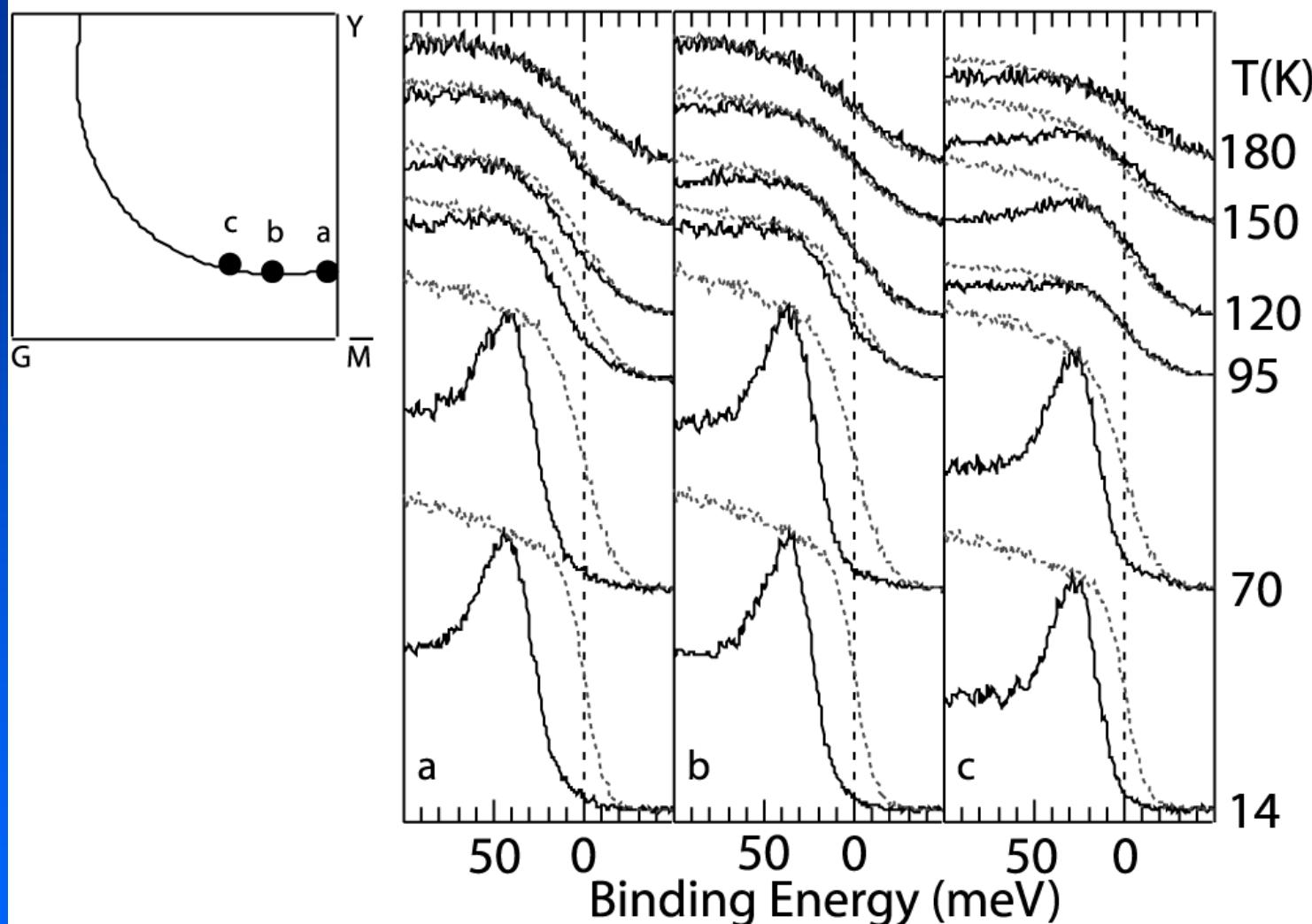


# The evolution of $\chi''(q,\omega)$ in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ with doping



# *Spin Excitations and the Pseudogap*

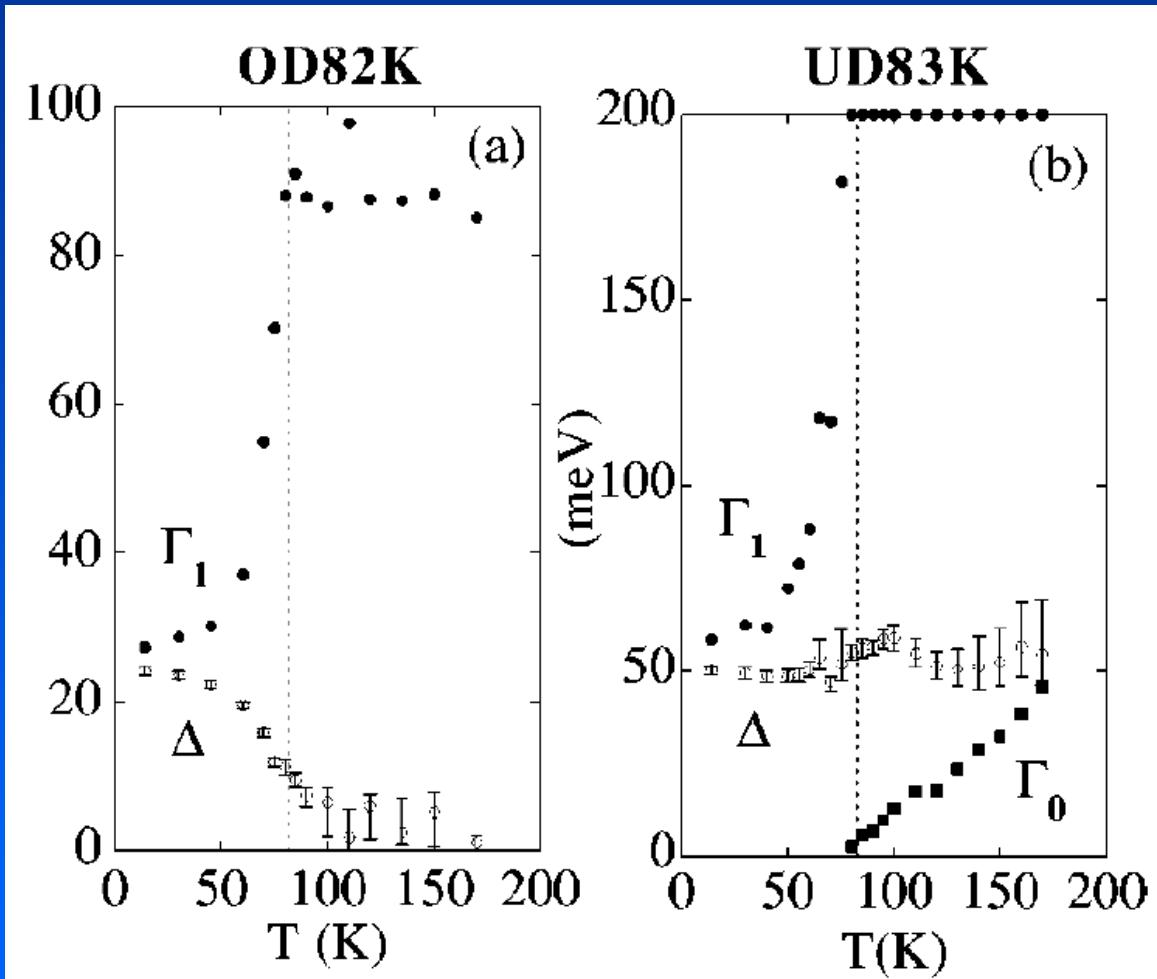
# $\text{Bi}_2\text{Sr}_2\text{Ca}\text{Cu}_2\text{O}_{8+\delta}$



APRES Pseudogap in Bi2212

Norman et al, Nature 392, 157 (1998)

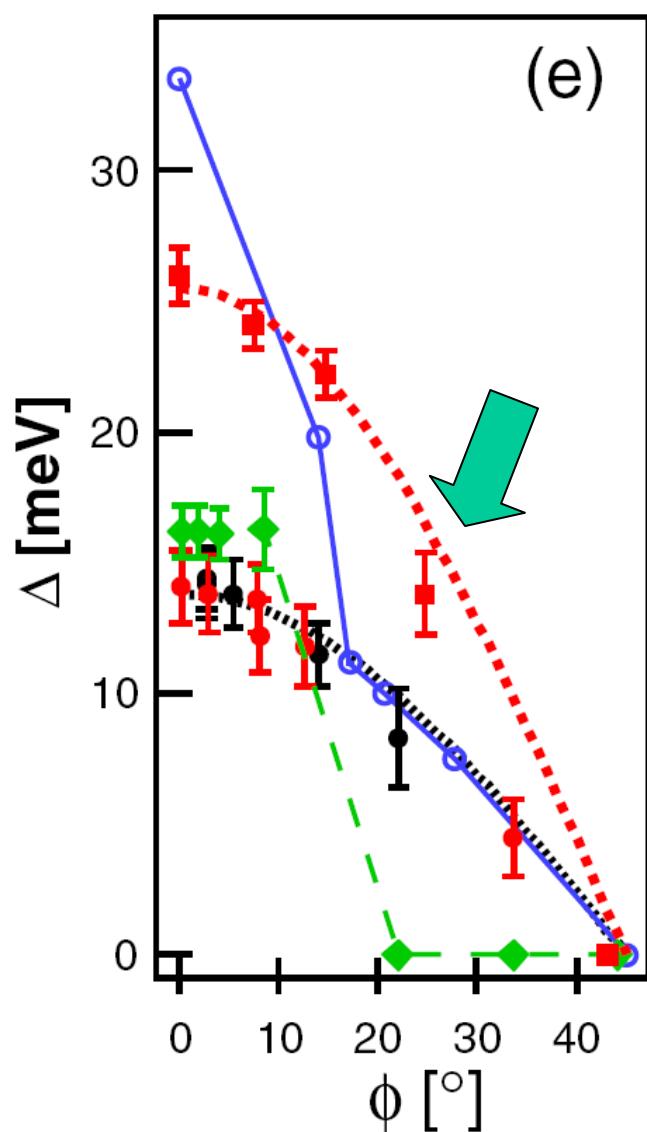
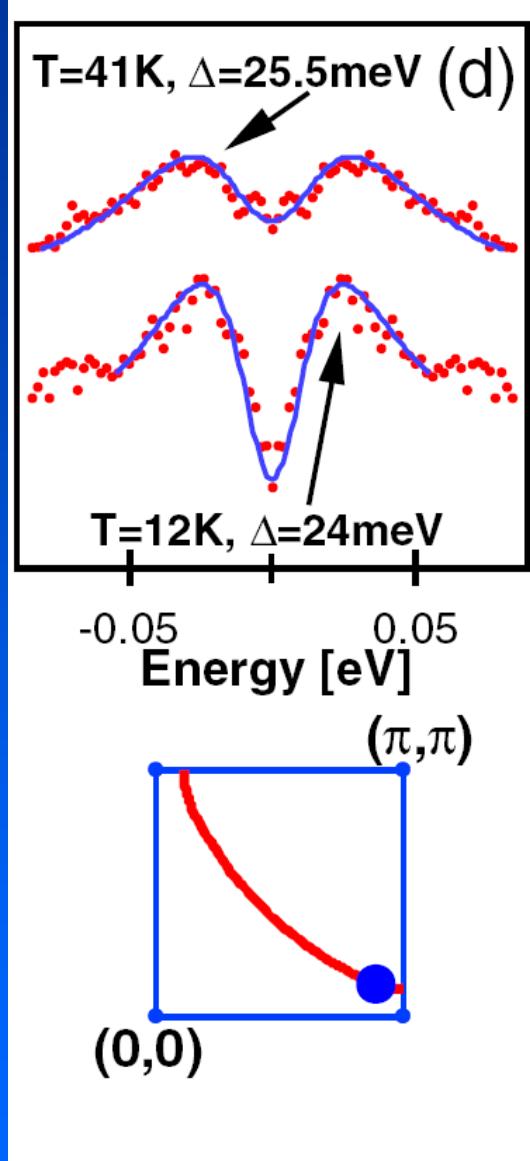
## Phenomenological self energy



$$\Sigma(\mathbf{k}, \omega) = -i\Gamma_1 + \Delta^2 / (\omega + i\Gamma_0)$$

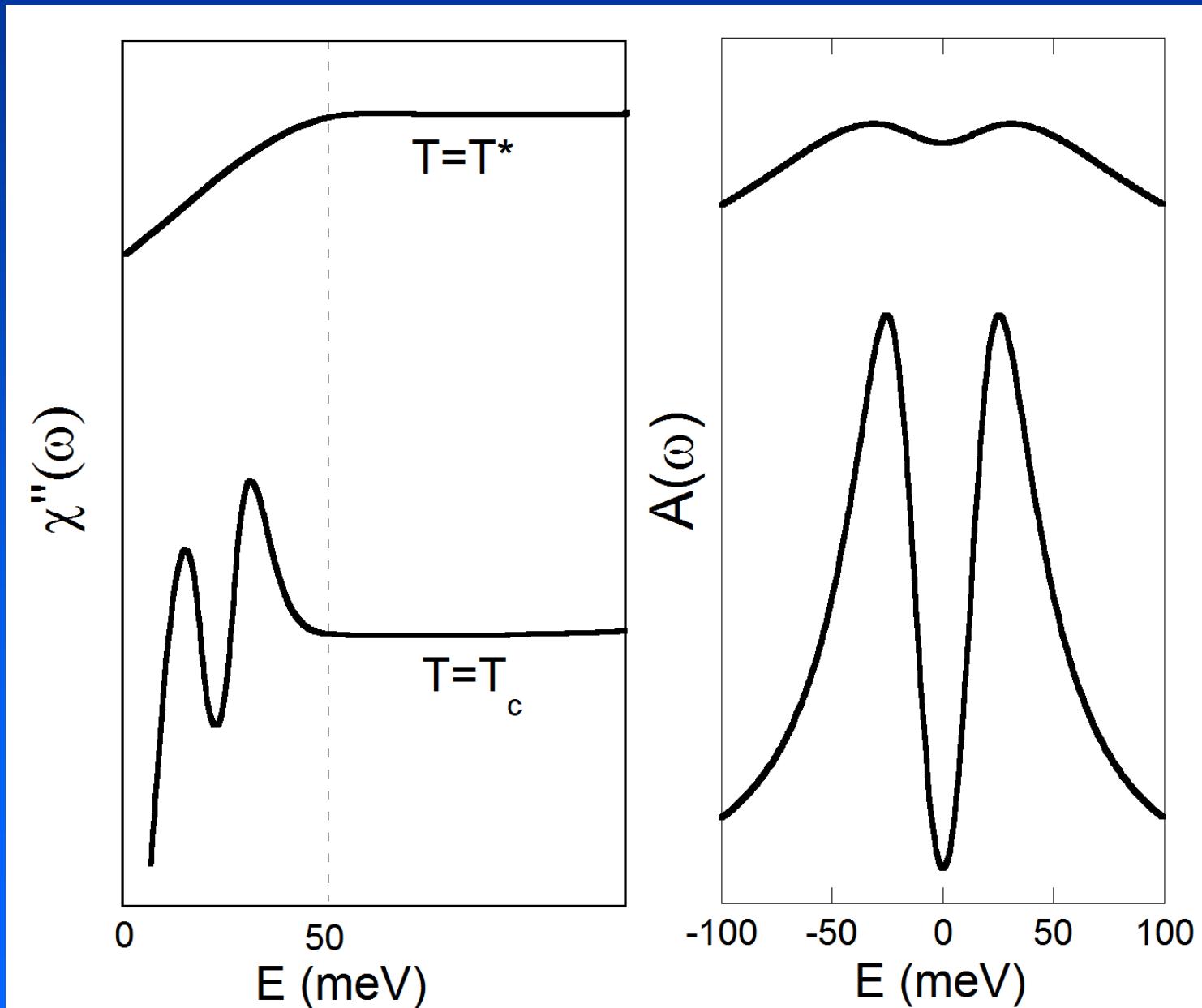
M. R. Norman *et al.* PRB 57, R11093 (1998).

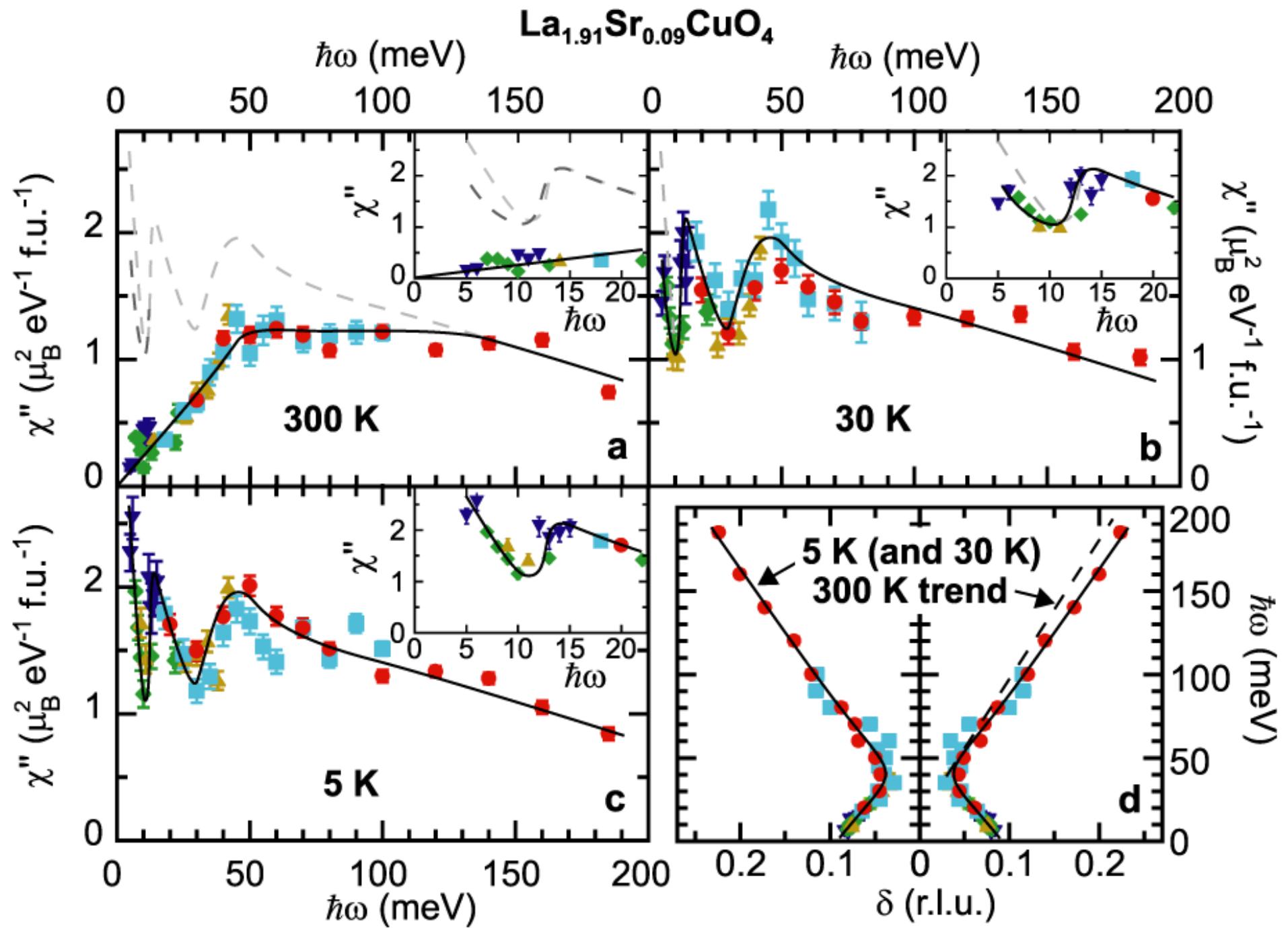
# Pseudo gap and ARPES in $\text{La}_{1.895}\text{Sr}_{0.105}\text{CuO}_4$



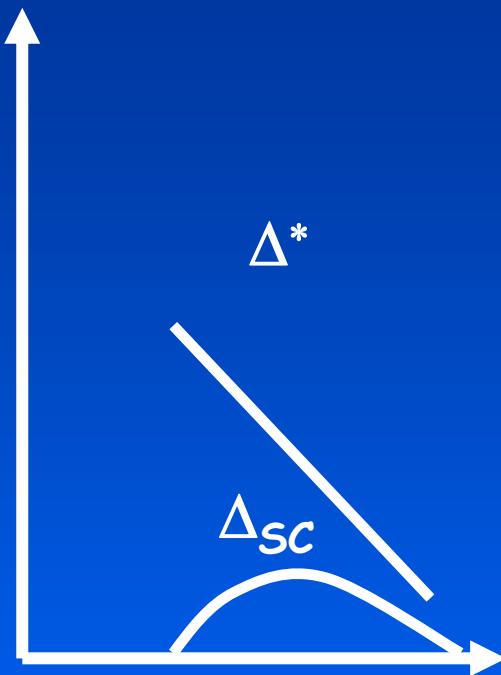
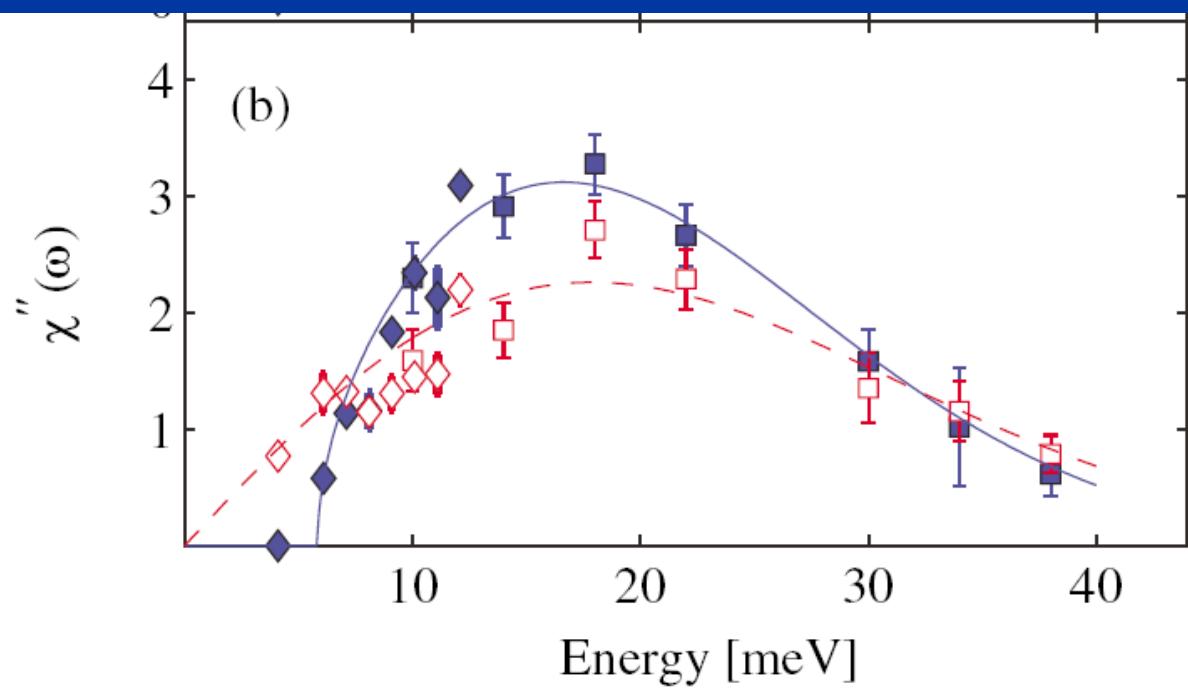
Shi et al. PRL 101, 047002 (2008)

# Effect of Pseudogap



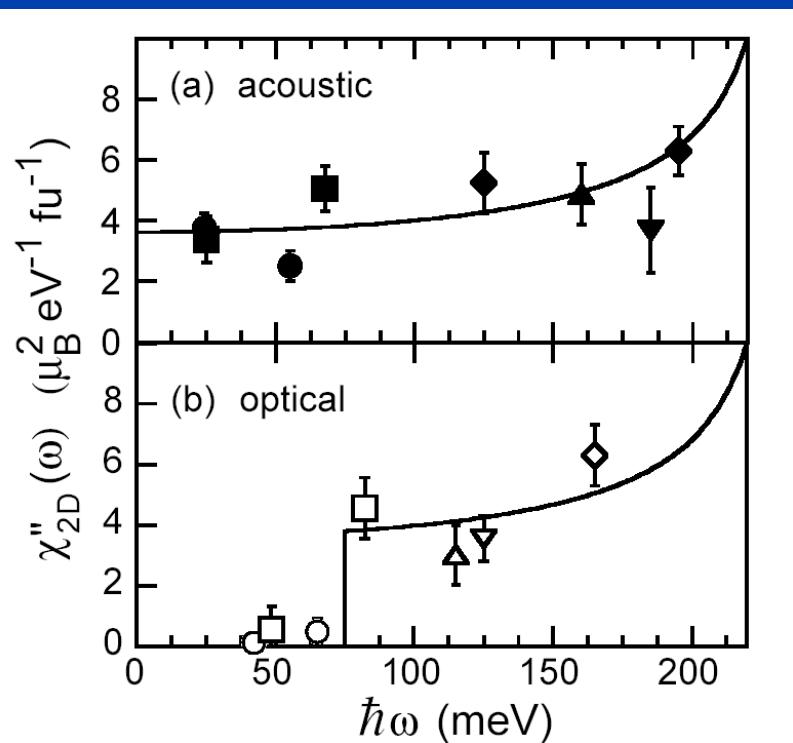


# Superconducting Gap- One Gap or Two ..... ?



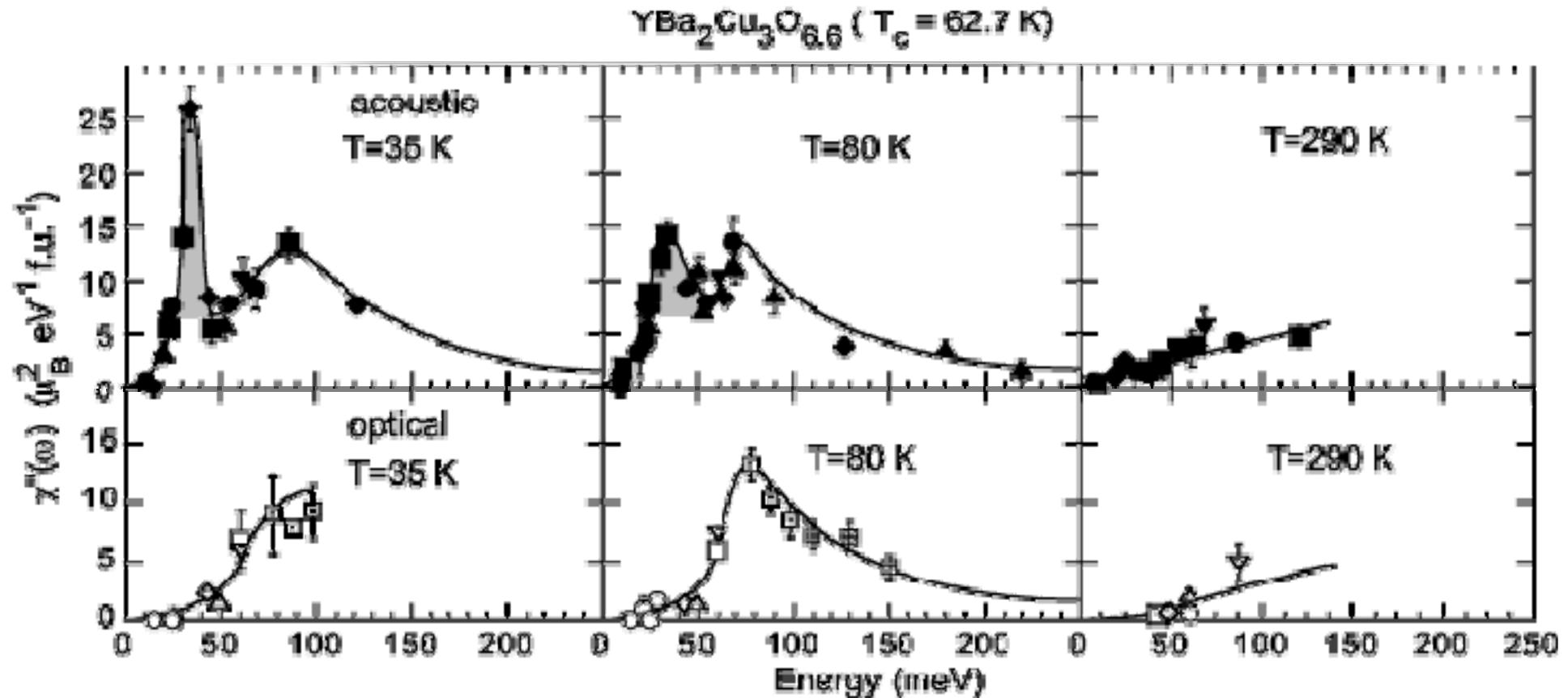
# Spin Fluctuations and the Resonance in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ (older stuff)

# The local susceptibility of $\gamma\text{Ba}_2\text{Cu}_3\text{O}_{6.15}$ (antiferromagnet)



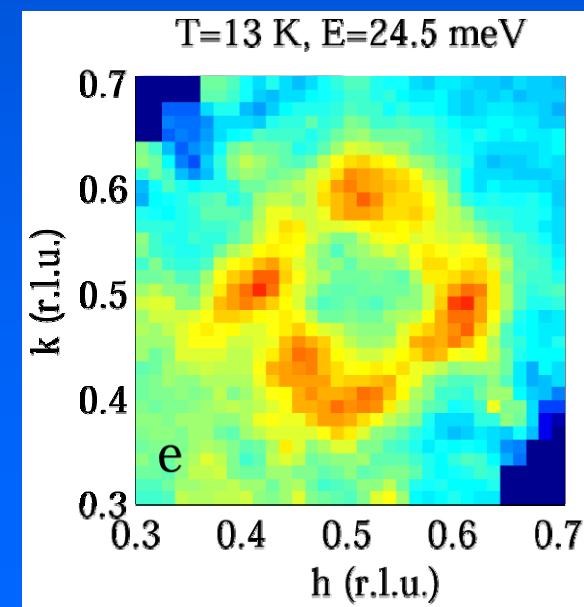
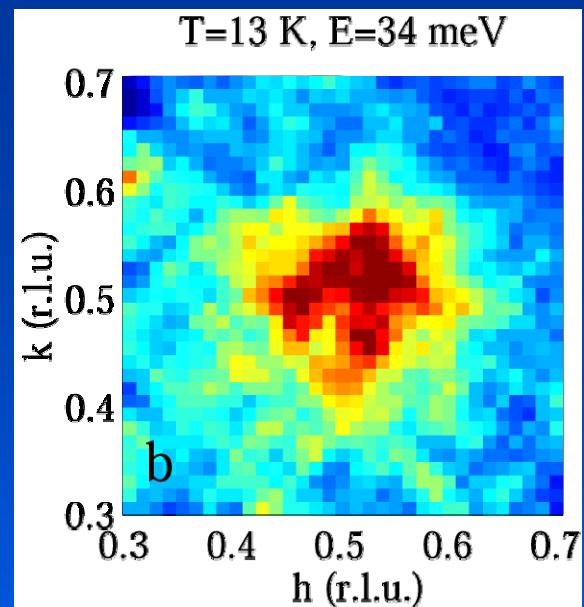
S. M. Hayden, G. Aeppli, T. G. Perring, H. A. Mook, F. Dogan,  
Phys. Rev. B 54, R6905-R6908 (1996).

# The local susceptibility of $\text{YBa}_2\text{Cu}_3\text{O}_{6.6}$



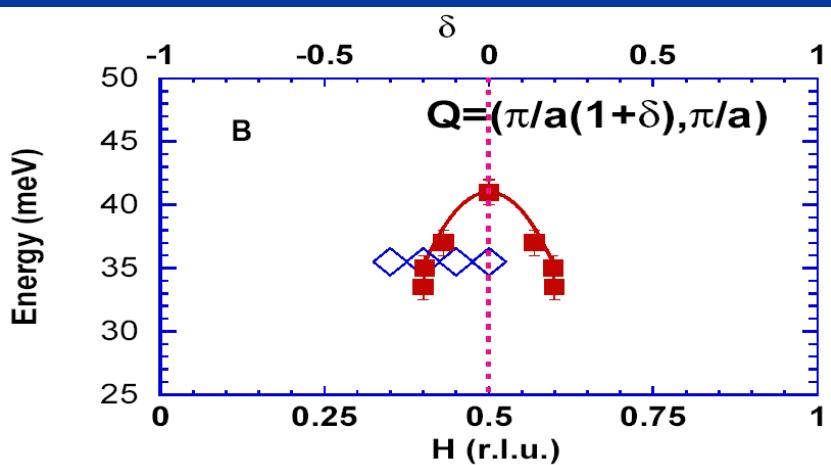
P. Dai, H. A. Mook, S. M. Hayden, G. Aeppli, T. G. Perring, R. D. Hunt, F. Dogan,  
Science 284, 1344 (1999); see also Bourges, PRB (1997) and Stock, PRB (2004)

$\gamma\text{Ba}_2\text{Cu}_3\text{O}_{6.6}$



YBCO cuts

$\gamma\text{Ba}_2\text{Cu}_3\text{O}_{6.85}$

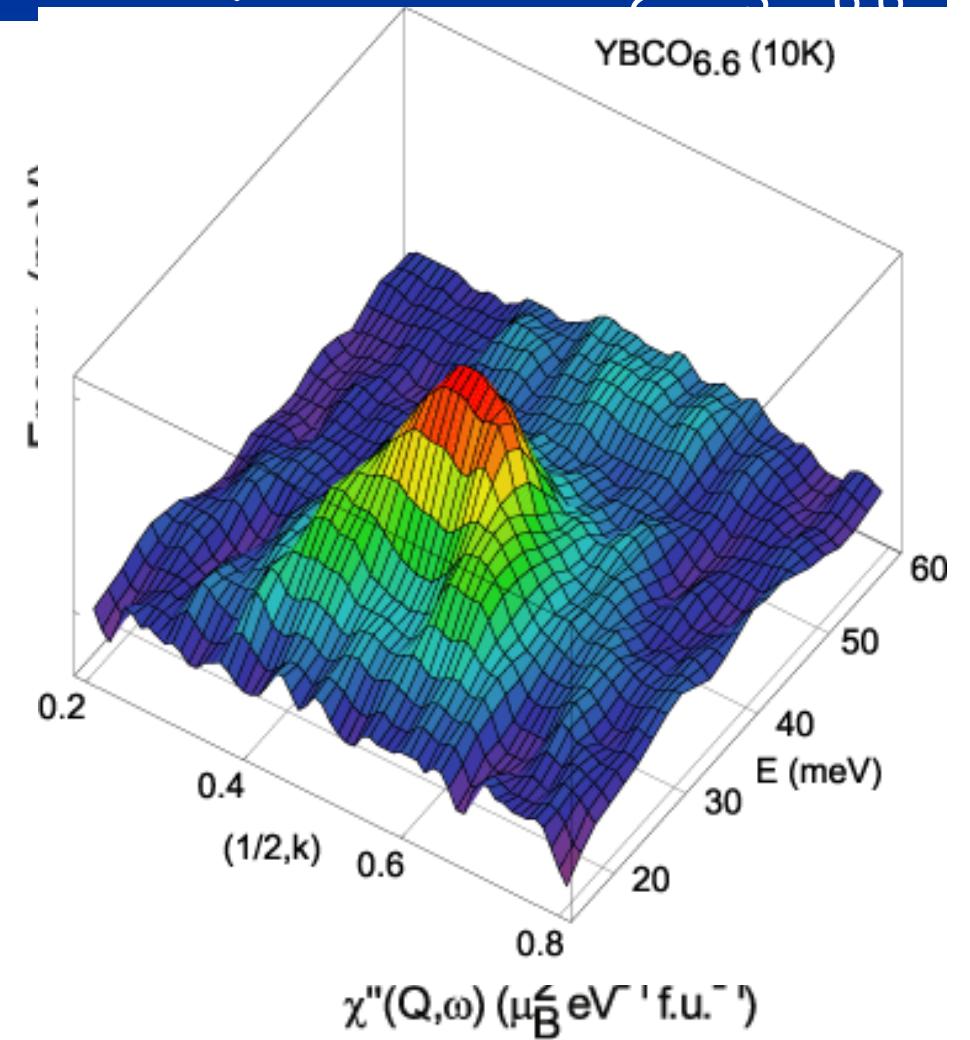
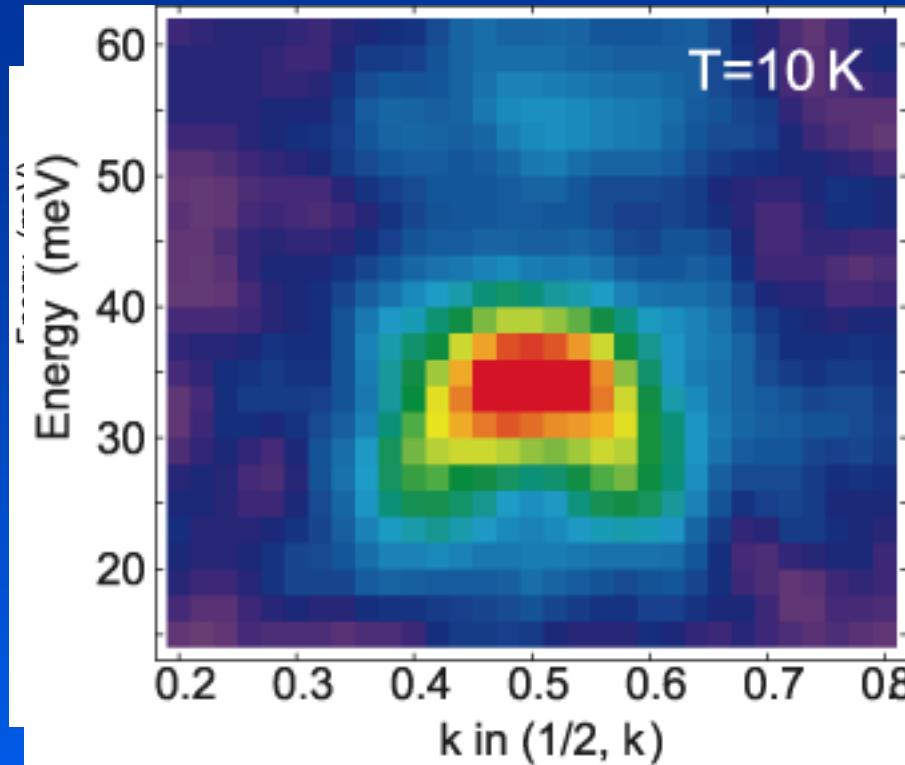


P. Bourges, Y. Sidis, H. F. Fong, L. P. Regnault, J. Bossy, A. Ivanov, and B. Keimer, 2000, *Science* **288**, 1234.

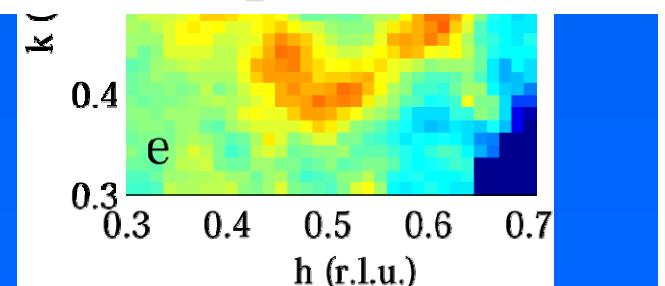
The formation of the resonance mode in  $\gamma\text{Ba}_2\text{Cu}_3\text{O}_{6.6}$

H. A. Mook, P. Dai., S. M. Hayden, G. Aeppli, T. G. Perring, F Dogan, Nature **395**, 580-582 (1998).

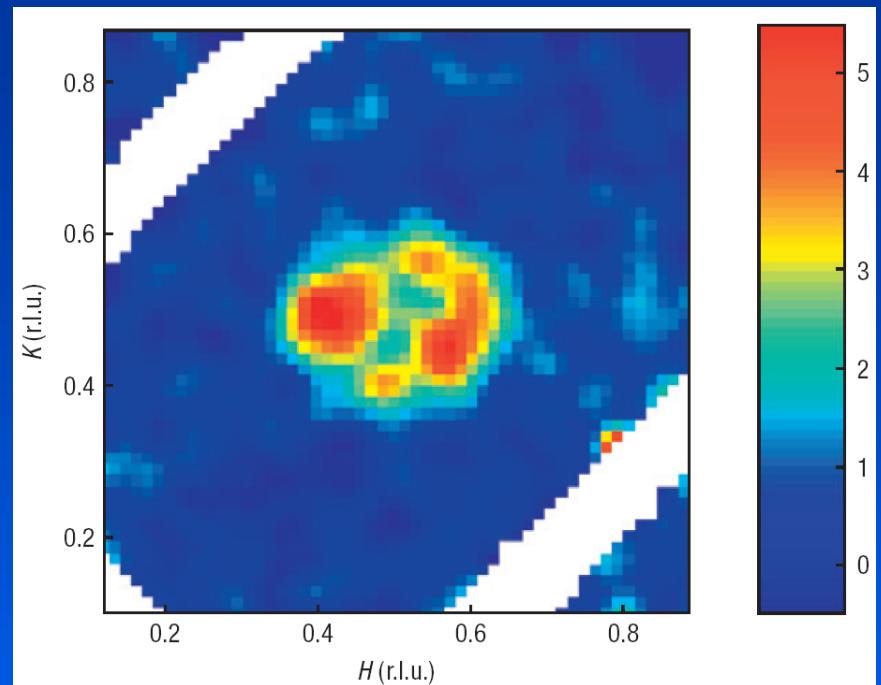
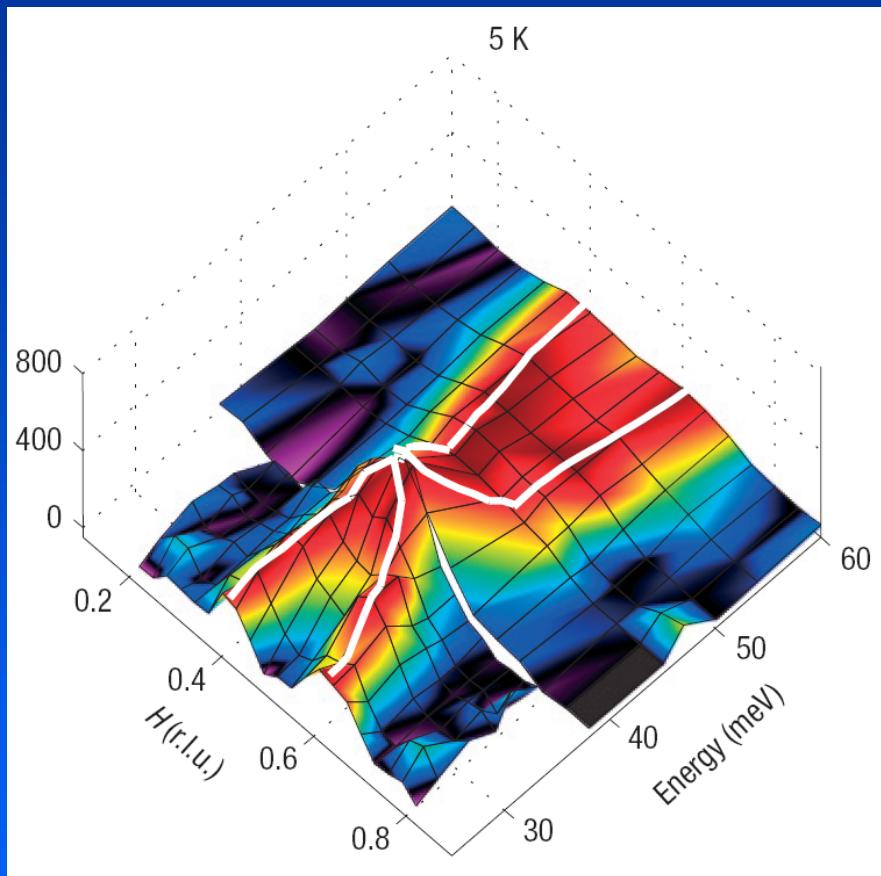
# The formation of the resonance mode in $\text{YBa}_2\text{Cu}_3\text{O}_{6.6}$



Hayden et al, Nature 429, 534 (2004)



# $\gamma\text{Ba}_2\text{Cu}_3\text{O}_{6.6}$

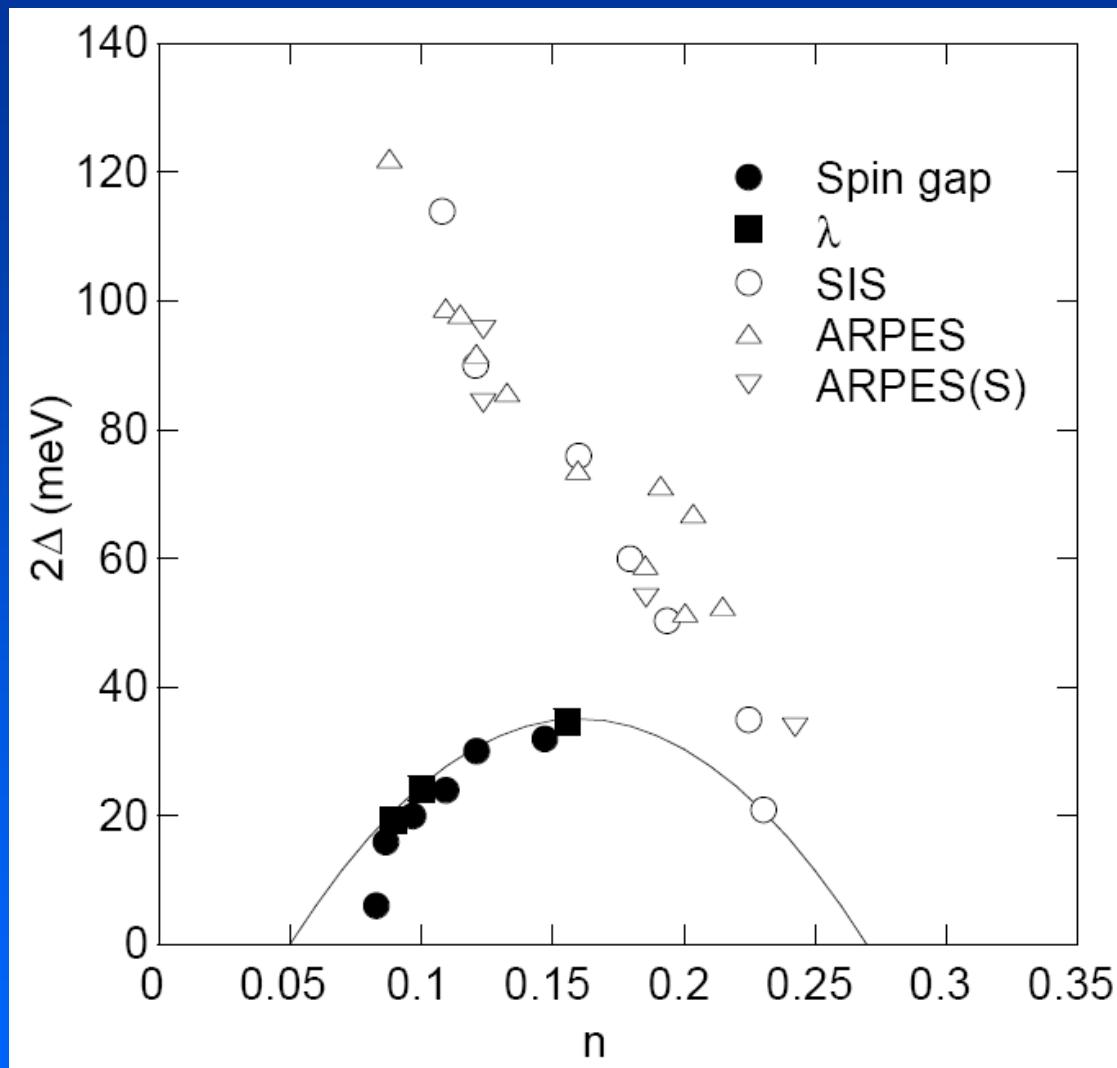


$E = 34 \text{ meV}$

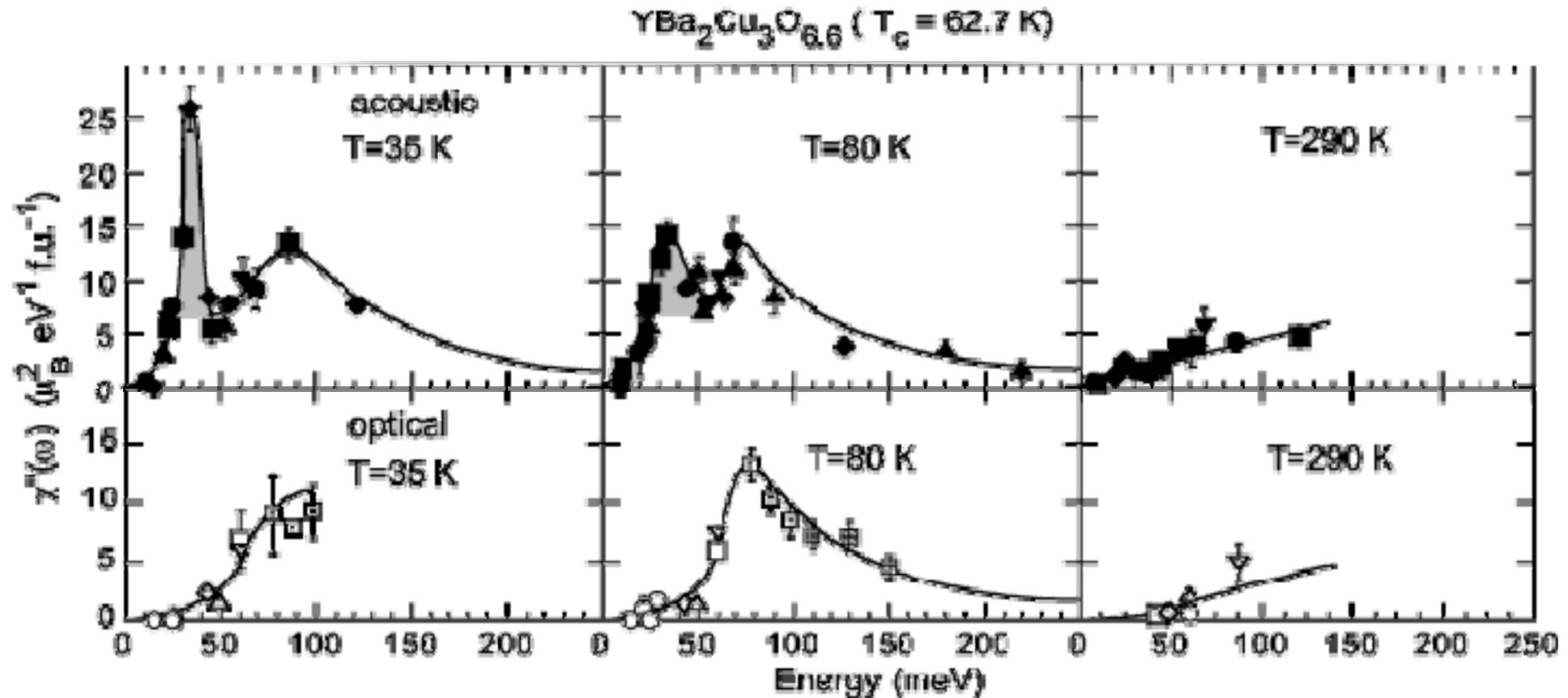
similar results on detwinned crystals:-

V. Hinkov et al. Nature Physics 3, 780 (2007)

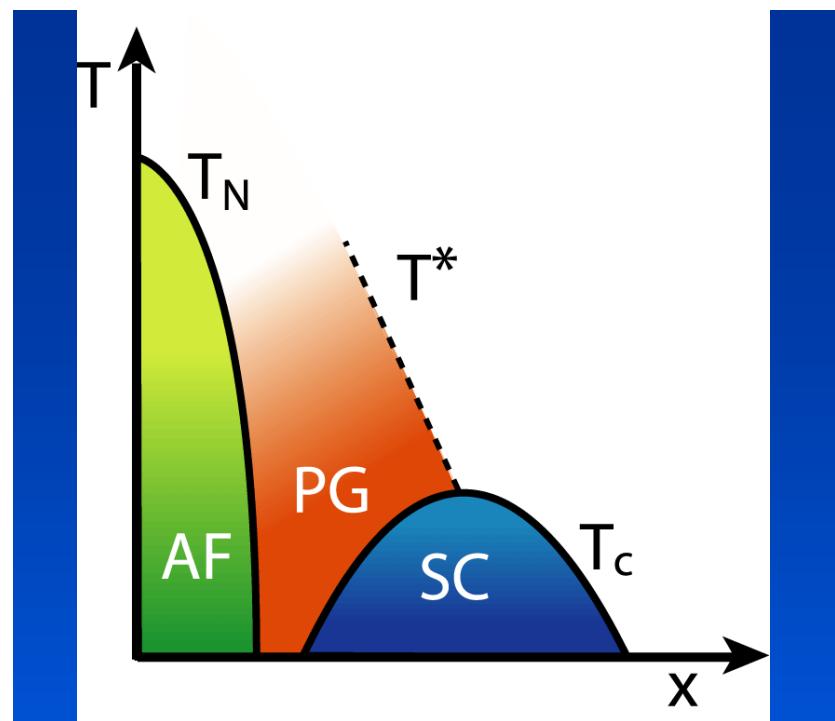
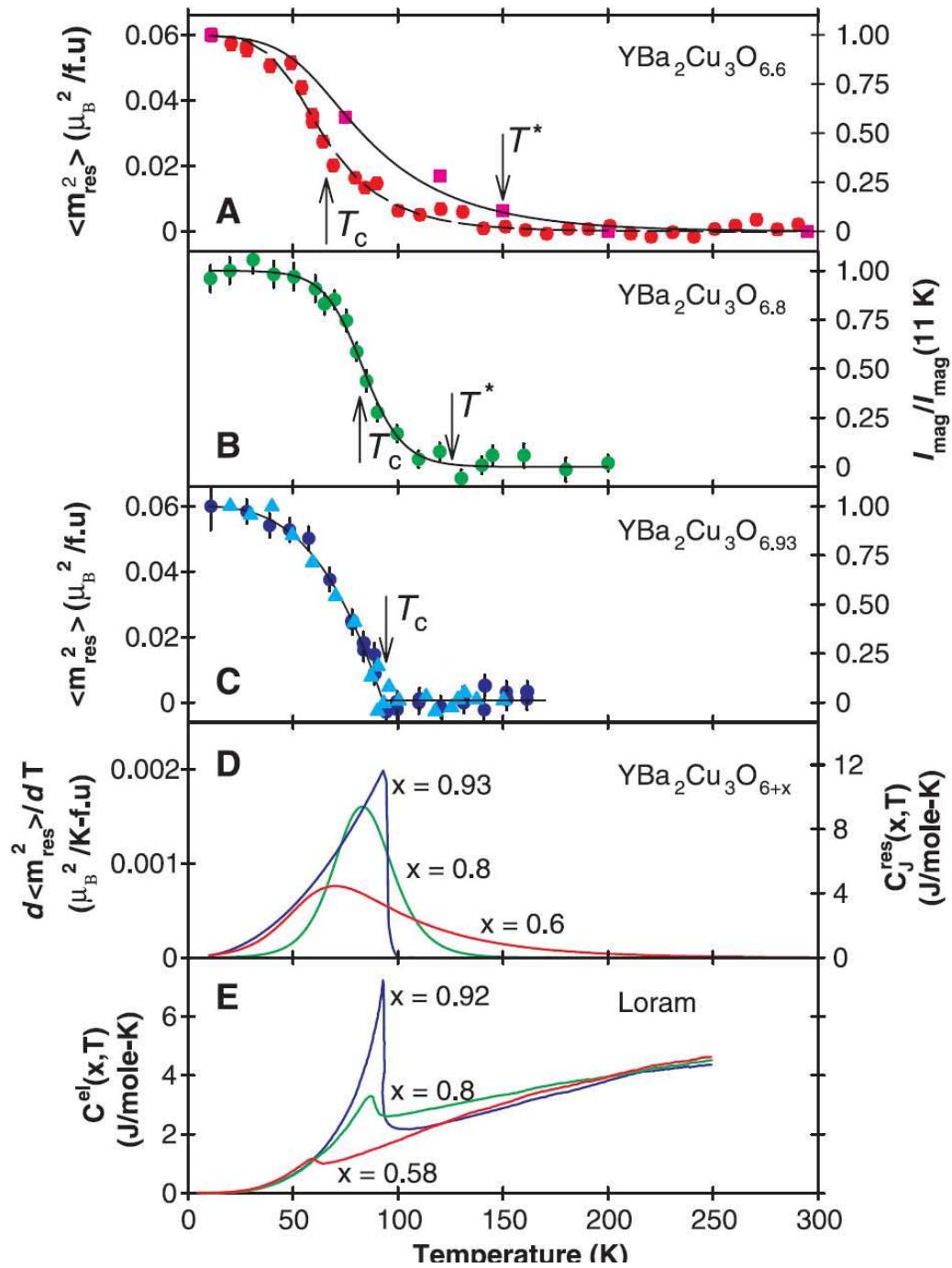
## "Superconducting spin gap"



# The local susceptibility of $\text{YBa}_2\text{Cu}_3\text{O}_{6.6}$



P. Dai, H. A. Mook, S. M. Hayden, G. Aeppli, T. G. Perring, R. D. Hunt, F. Dogan,  
Science 284, 1344 (1999); see also Bourges, PRB (1997) and Stock, PRB (2004)

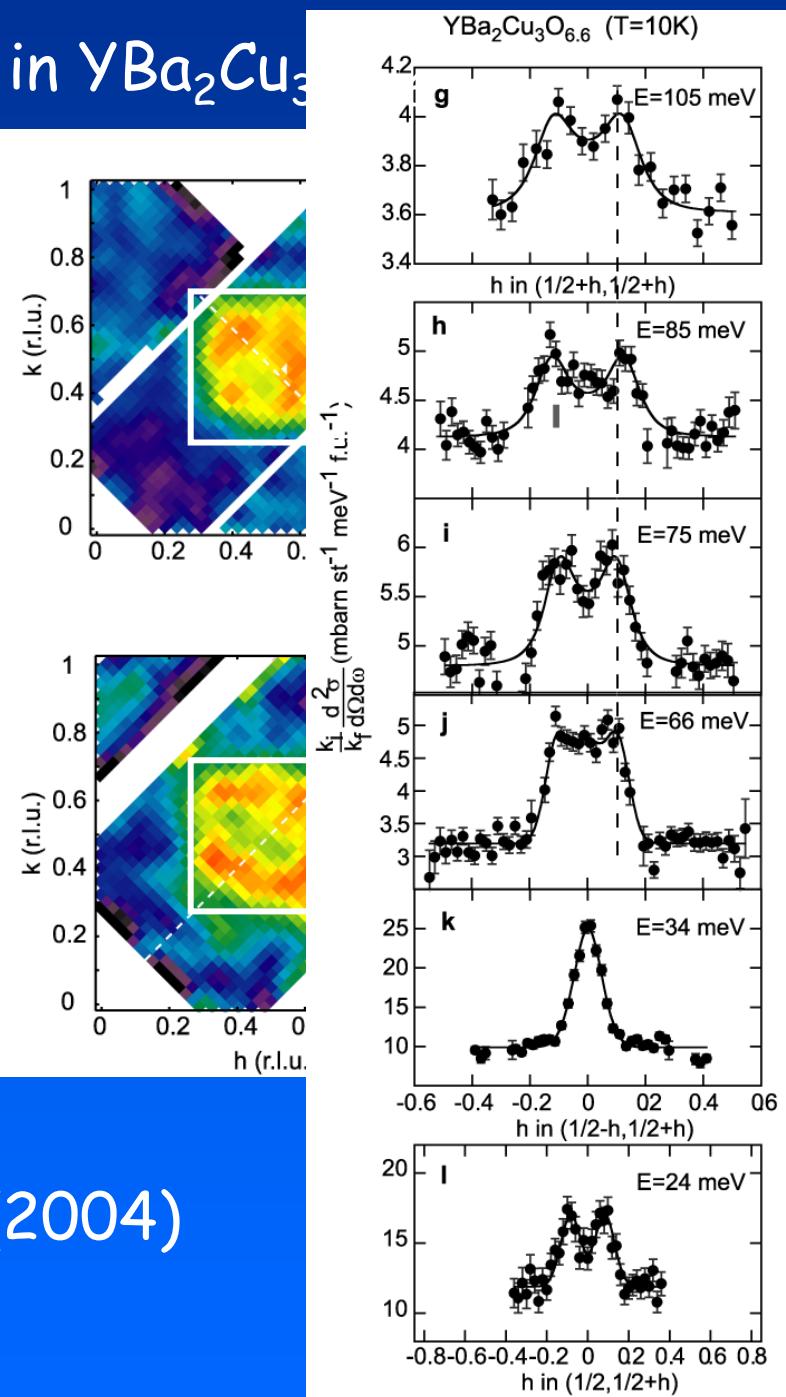
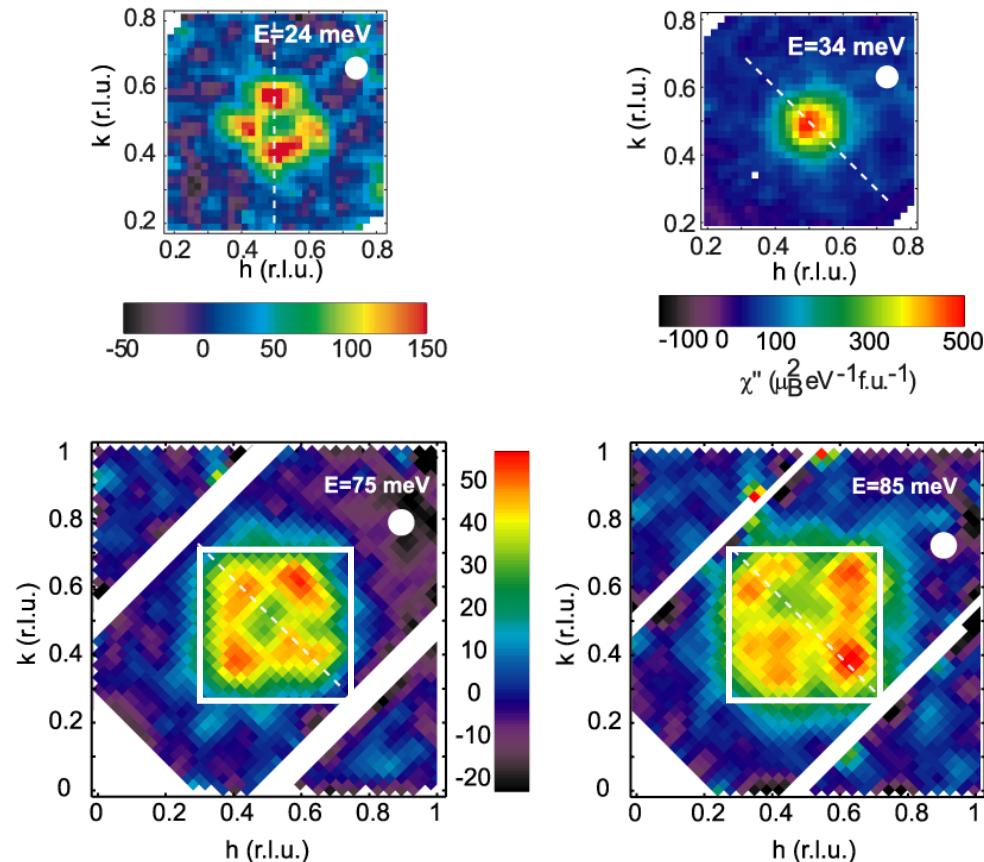


Resonance Intensity

Dai et al., Science 284,  
1344 (1999)

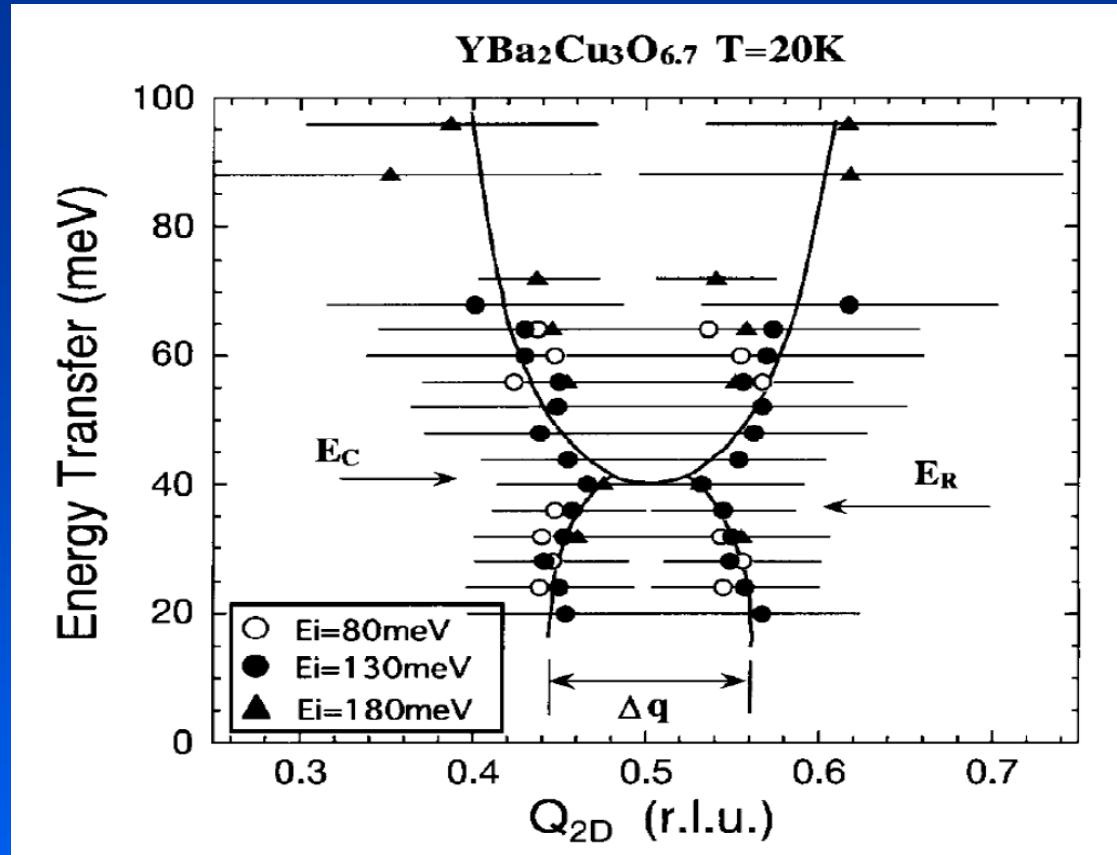
# High-energy magnetic excitations in $\text{YBa}_2\text{Cu}_3$

$\text{YBa}_2\text{Cu}_3\text{O}_{6.6}$  ( $T=10 \text{ K}$ )



Hayden et al, Nature 429, 534 (2004)

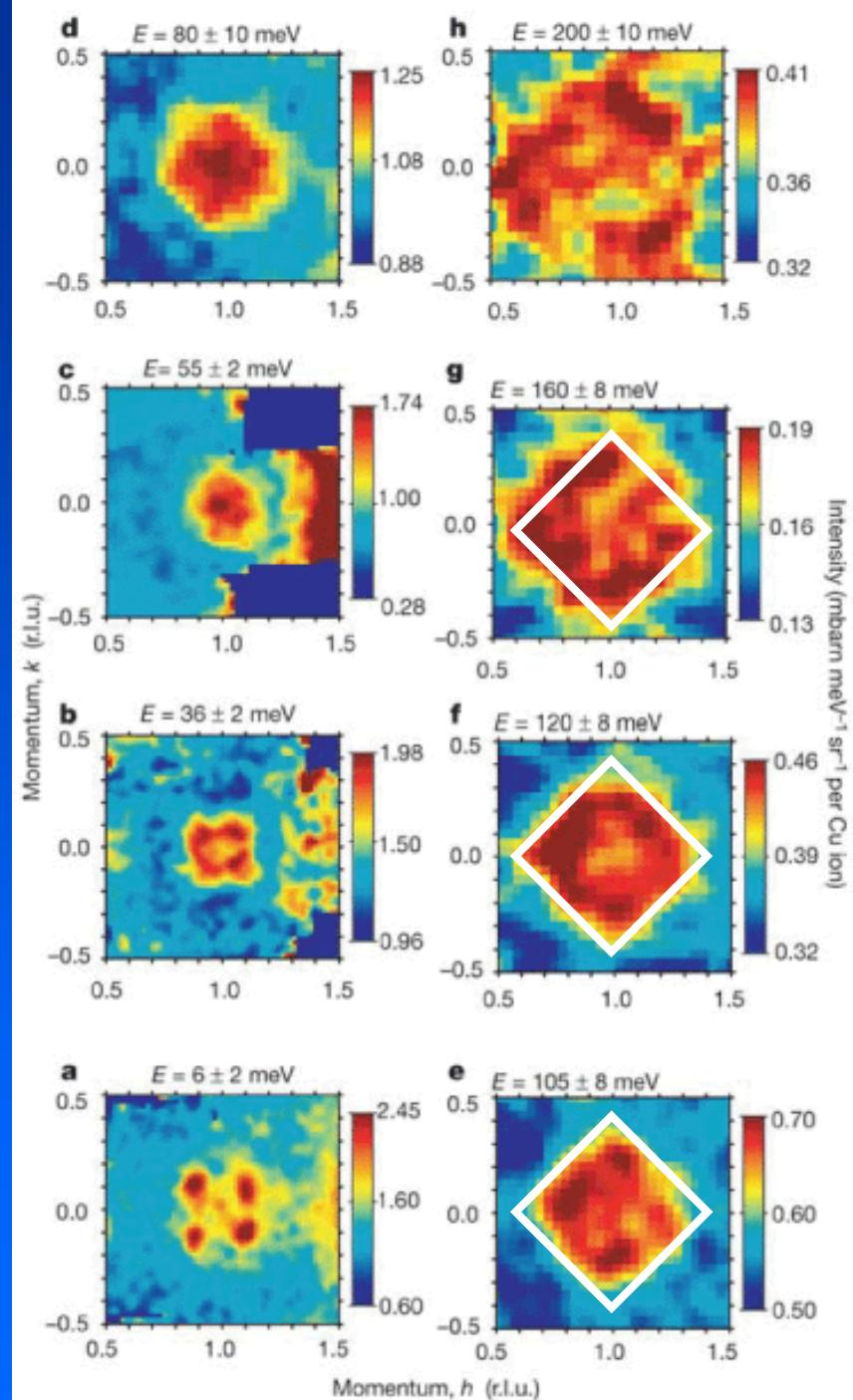
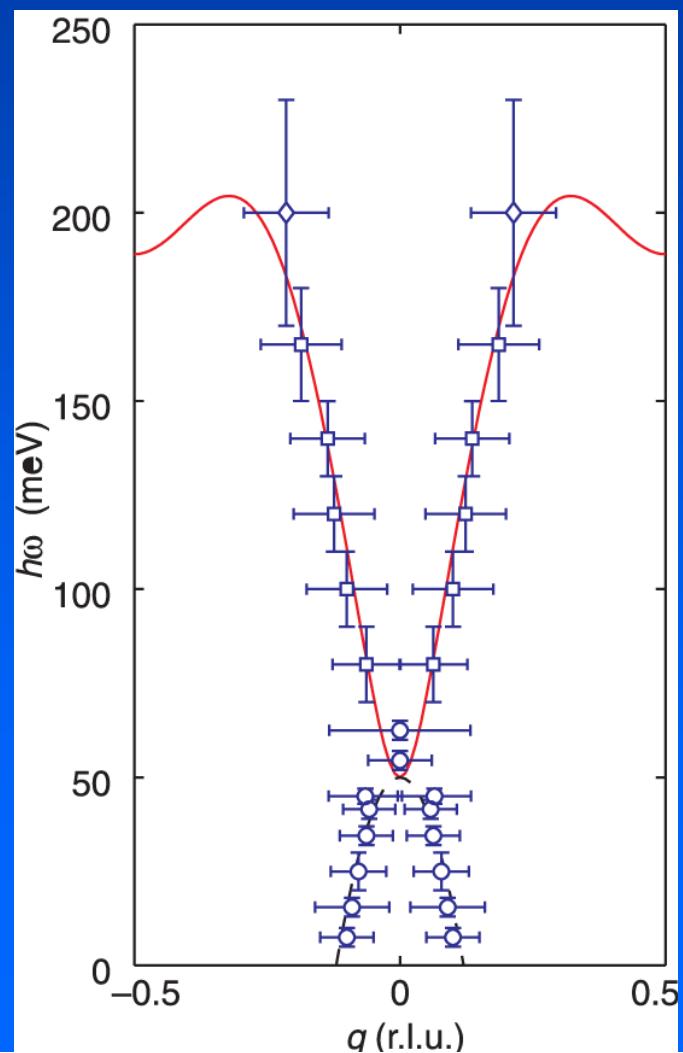
# Hourglasses.....



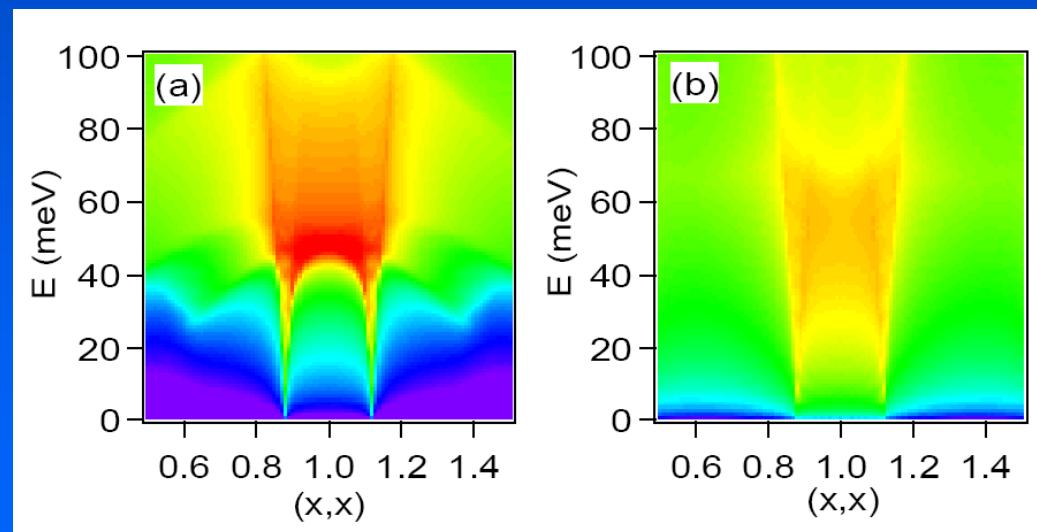
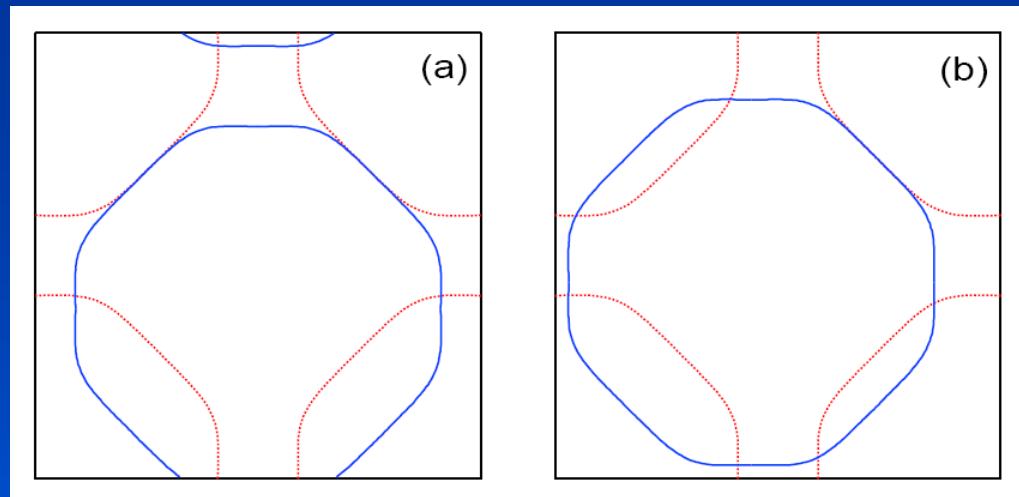
M. Arai et. al, PRL (1999)

# $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$

J. M. Tranquada , H. Woo, T. G. Perring ,  
H. Goka ,G.D.Gu, G.Xu, M. Fujita, K. Yamada,  
Nature 429, 534 (2004).



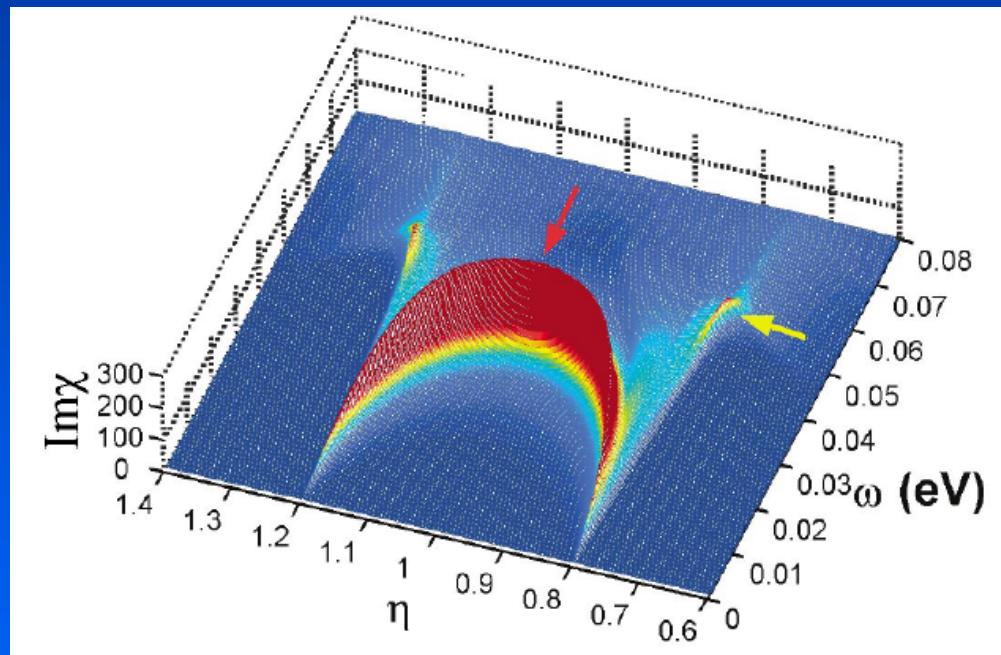
# RPA calculations of $\chi(q,\omega)$



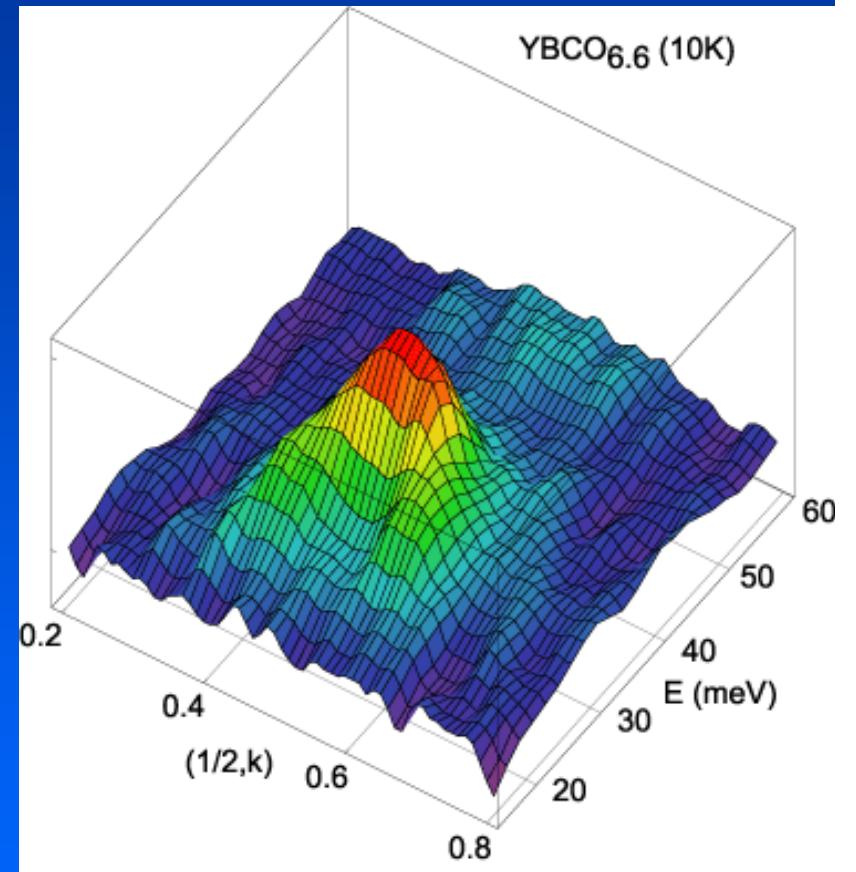
Results depend on details  
of band structure  $\Rightarrow$   
Accurate knowledge  
required

e.g. M. R. Norman, PRB 2007

# Is there a "Resonance" mode in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ ?

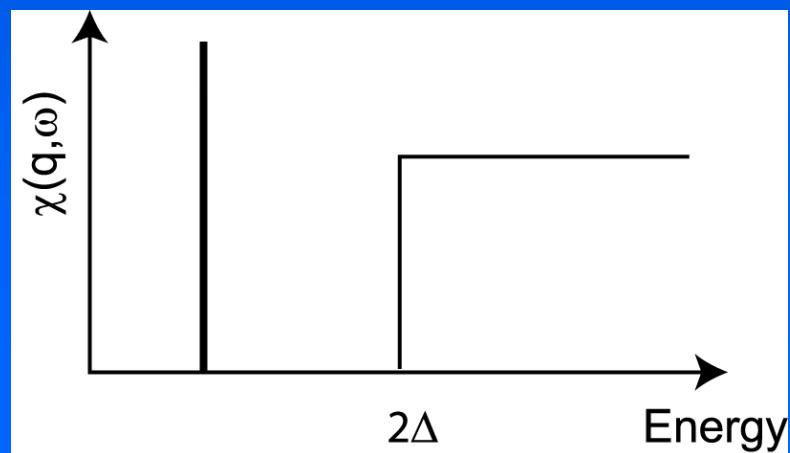
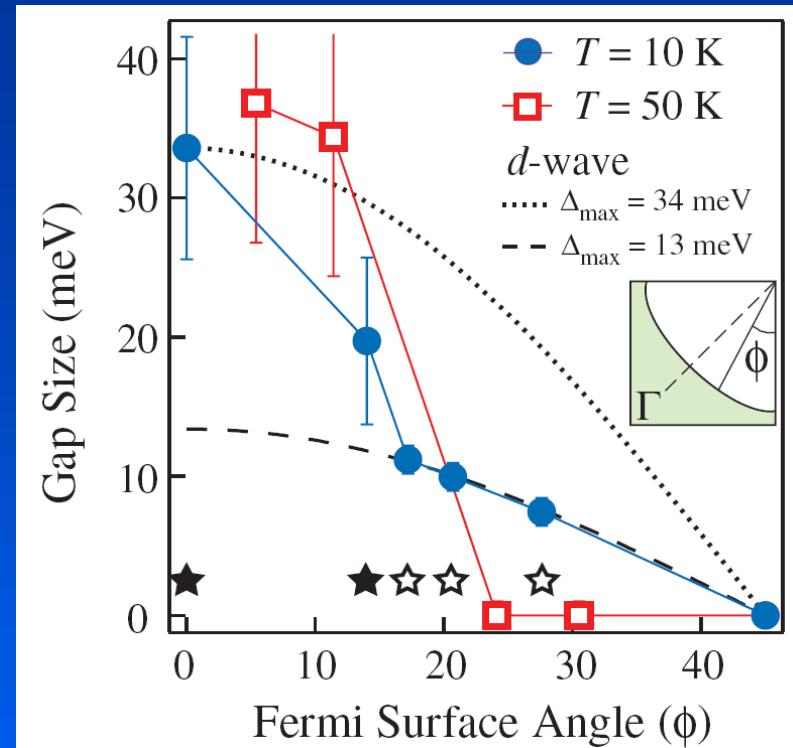
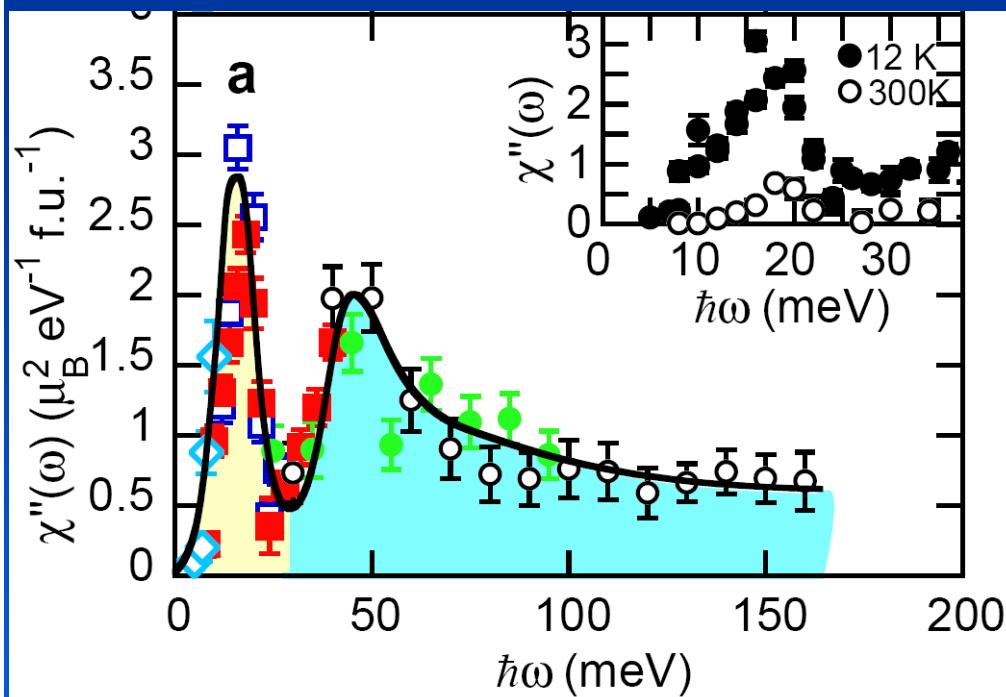


e.g. I. Emelin et al., PRL 94, 147001 2005



S. M. Hayden, et al, Nature 429, 531 2004.

Possibly ....



LSCO ARPES  
K. Terashima et al., prl 99, 017003 (2007)

# Summary

# Summary

- double-peaked structure at optimal doping
- overdoping results in the collapse of the 50 meV peak

Is 50 meV peak responsible for SC?

