



The Abdus Salam
International Centre for Theoretical Physics



1957-19

Miniworkshop on Strong Correlations in Materials and Atom Traps

4 - 15 August 2008

First-principles study of the electronic structure of the Iron-based pnictides

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First-principles study of the electronic structure of the iron-based pnictides

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arXiv:0803.3325, to appear in Phys. Rev. Lett.

arXiv:0806.3285, to appear in Phys. Rev. B

arXiv:0806.3860, to appear in J. Phys. Soc. Jpn

arXiv:0806.4750, to appear in J. Phys. Soc. Jpn

- ◆ K. Kuroki (Univ. Electro-Commun.)
- ◆ S. Onari (Nagoya Univ.)
- ◆ H. Usui (Univ. Electro-Commun.)
- ◆ H. Kontani (Nagoya Univ.)
- ◆ Y. Tanaka (Nagoya Univ.)
- ◆ H. Aoki (Dept. Phys., Univ. Tokyo)

- ◆ K. Nakamura (Dept. Appl. Phys., Univ. Tokyo)
- ◆ M. Imada (Dept. Appl. Phys., Univ. Tokyo)

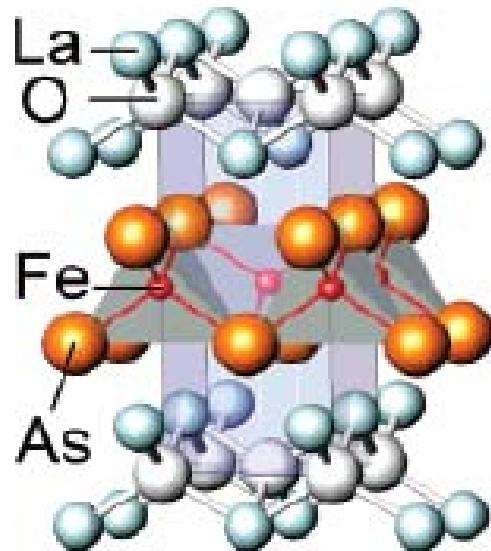
- ◆ V. Vildosola (CPHT, Ecole Polytechnique)
- ◆ L. Pourovskii (CPHT, Ecole Polytechnique)
- ◆ S. Biermann (CPHT, Ecole Polytechnique)
- ◆ A. Georges (CPHT, Ecole Polytechnique)

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- ◆ M. Kubota (IMSS, Tsukuba)
- ◆ K. Ono (IMSS, Tsukuba)
- ◆ Y. Kamihara (Tokyo Inst. Tech.)
- ◆ M. Hirano (Tokyo Inst. Tech.)
- ◆ H. Hosono (Tokyo Inst. Tech.)

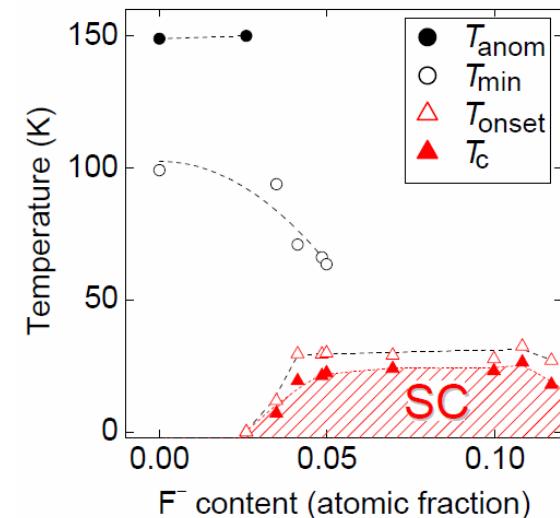
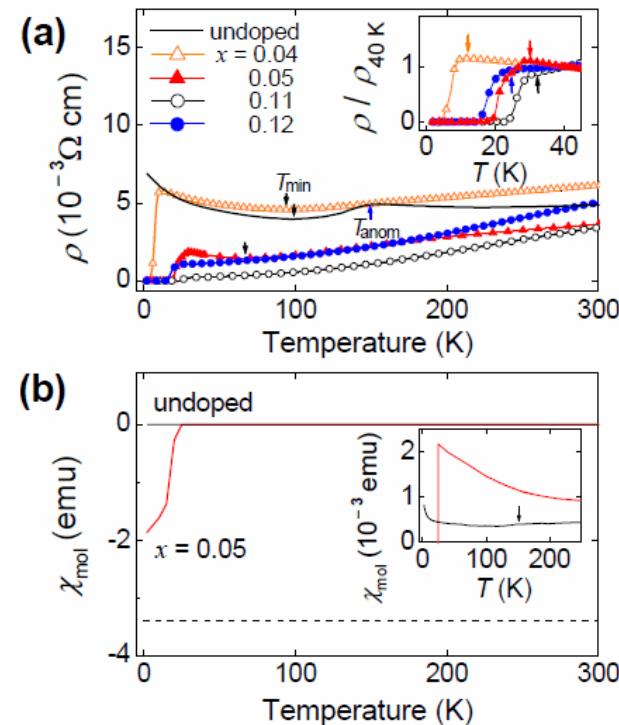
- ◆ Introduction
- ◆ Construction of an effective model from first-principles
 - Minimal model which describes low energy physics:
Which d-orbitals are involved?
 - Estimation of interaction parameters:
How large is U , U' , J ?
- ◆ Multi-band RPA study on unconventional superconductivity
 - Symmetry of Δ

Iron-based layered superconductor

Kamihara et al, JACS 130 3296 (2008)



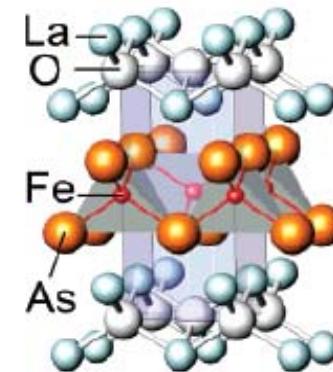
LaFeAs [O_{1-x}F_x] ($x=0.05-0.12$)



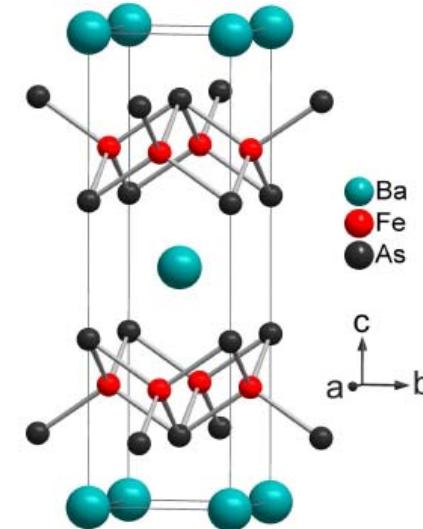
$T_c \sim 26 \text{ K}$

High T_c: raising up to ~55K

- RFeAsO_{1-x}F_x
 - Substitution of La with other rare-earths
T_c=51K (R=Nd), 55K (R=Sm), etc.
- RFeAsO_{1-δ}
 - Oxygen vacancies instead of F doping
- “122”, ThCr₂Si₂-type
 - AFe₂As₂, A=alkaline earth metal
- “111”, PbFCl-type
 - LiFeAs (without chemical doping)
- “11”, PbO-type
 - FeSe
- Under pressure
 - LaFeAsO_{1-x}F_x: T_c=26K → 43K
 - Undoped 122-type: T_c=0K → 30K
 - Undoped 11-type: T_c=8K → 27K



“111” (RFeAsO)

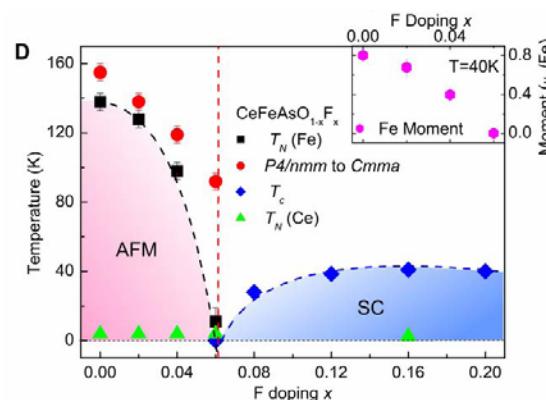


“122” (AFe₂As₂)

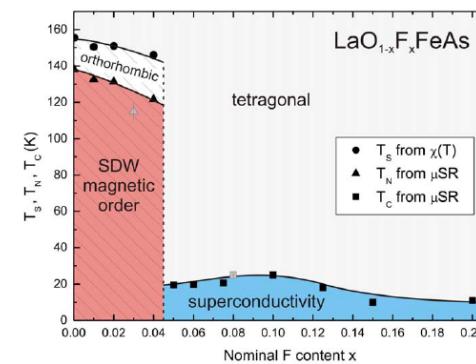
Problems in DFT calculations

✚ Magnetic moment overestimated

- 1.5-2.0 μ_B , whether in doped or undoped cases
- Experimentally, AF is observed only at very low doping levels and is weak ($\sim 0.3 \mu_B$ for LaFeAsO, $\sim 0.9 \mu_B$ for NdFeAsO, $\sim 0.9 \mu_B$ for BaFe₂As₂)



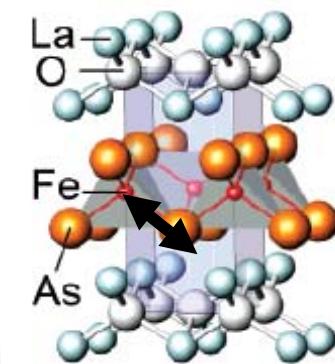
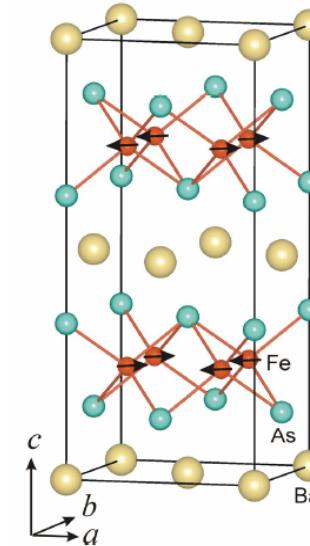
Zhao et al, arXiv:0806.2528



Luetkens et al, arXiv:0806.3533

✚ Fe-Pn bond length

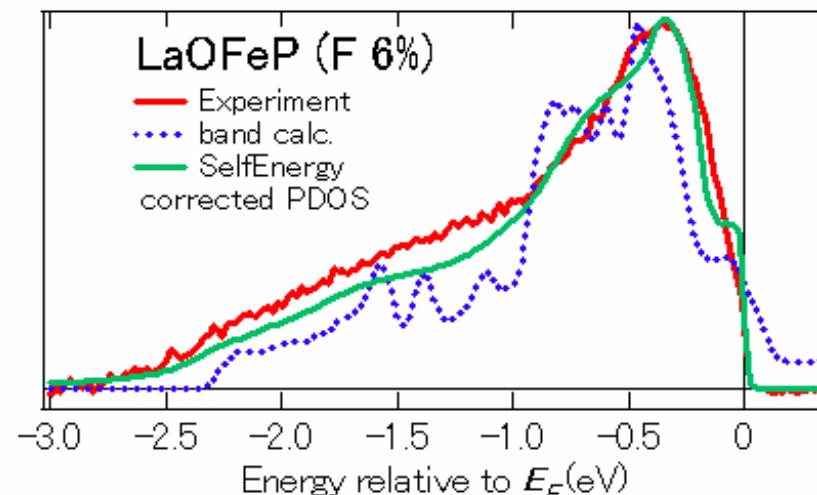
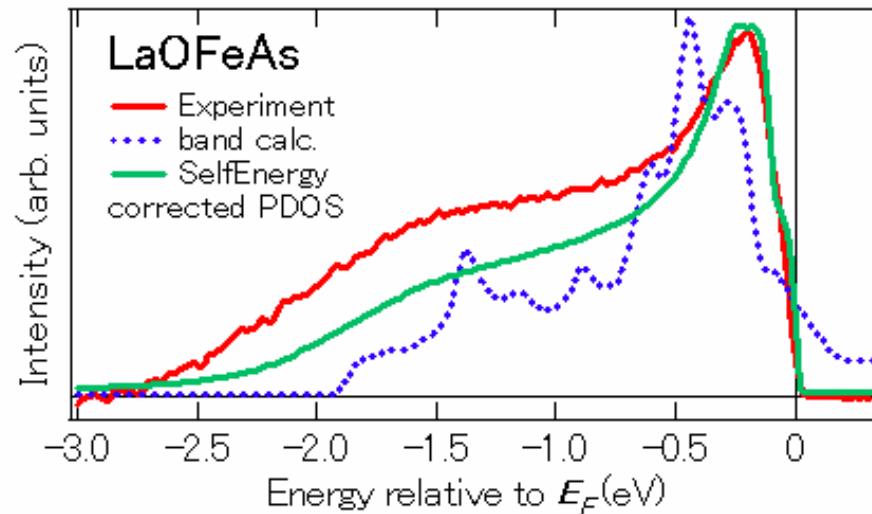
- Underestimated in structure optimization (up to 0.15 Å)



P. Aliaa

LDA: a good starting point for theoretical studies?

- ◆ PES Yoshida et al, arXiv:0806.3860, to appear in J. Phys. Soc. Jpn



LDA DOS qualitatively agree with PES
No Hubbard band observed

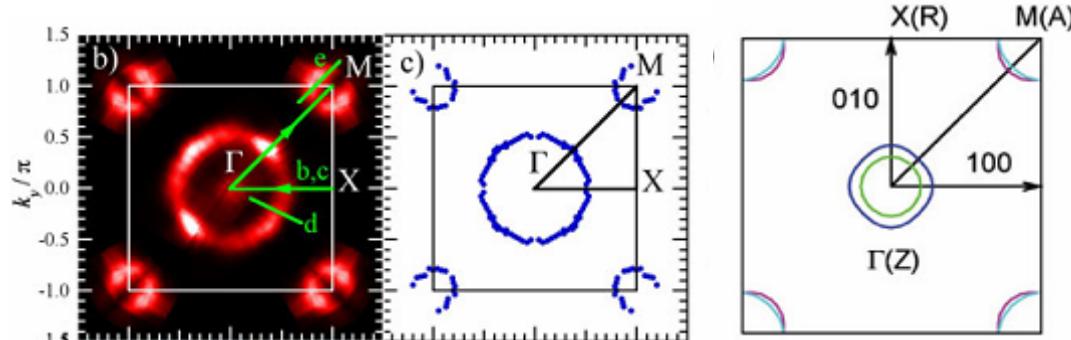
LDA: a good starting point for theoretical studies?



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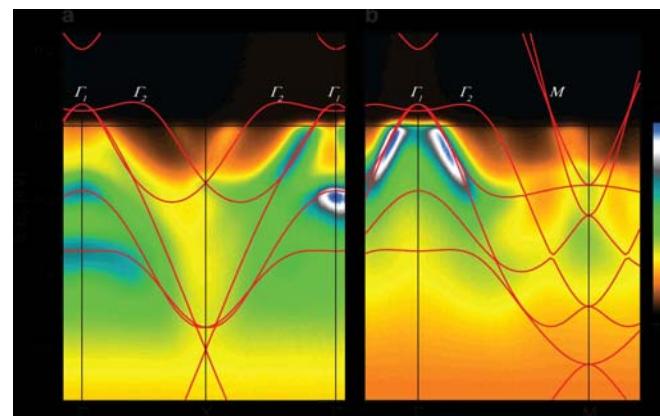
◆ ARPES

■ NdFeAsO_{1-x}F_x



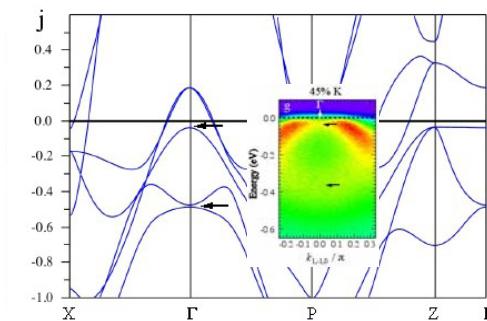
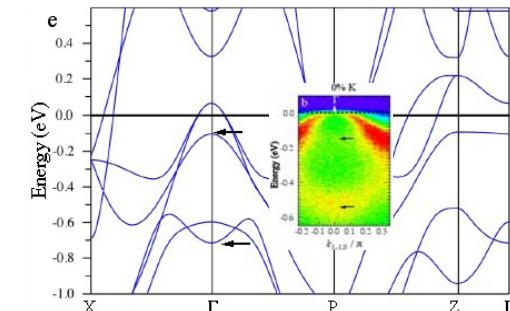
Liu et al, arXiv:0807.2009

■ LaFeOP



Liu et al, arXiv:0806.3453

■ Ba_{1-x}K_xFe₂As₂

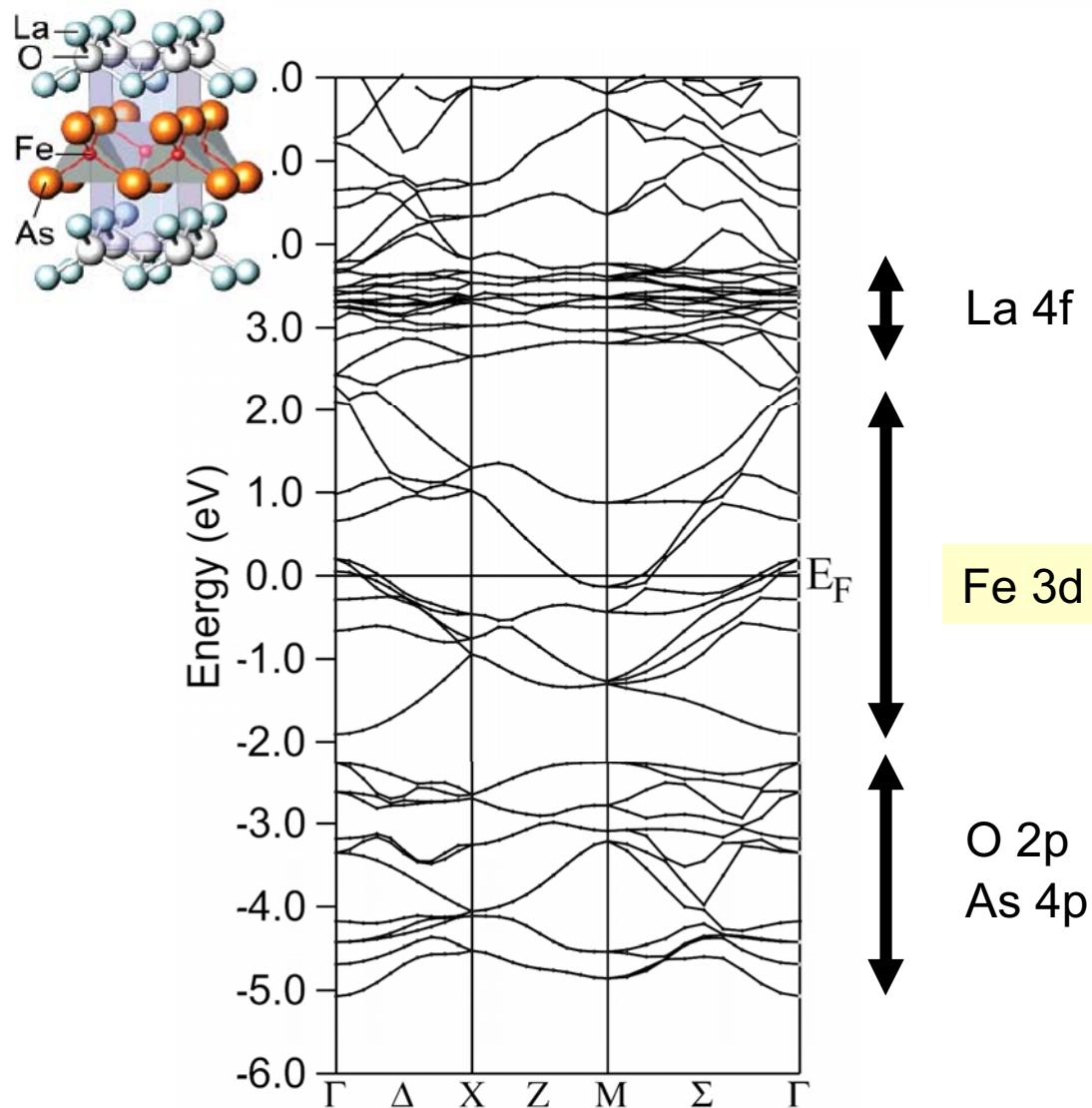


Liu et al, arXiv:0806.3453

LDA captures essential
features of ARPES

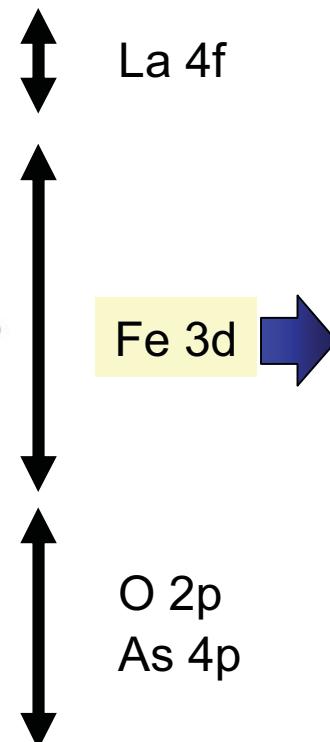
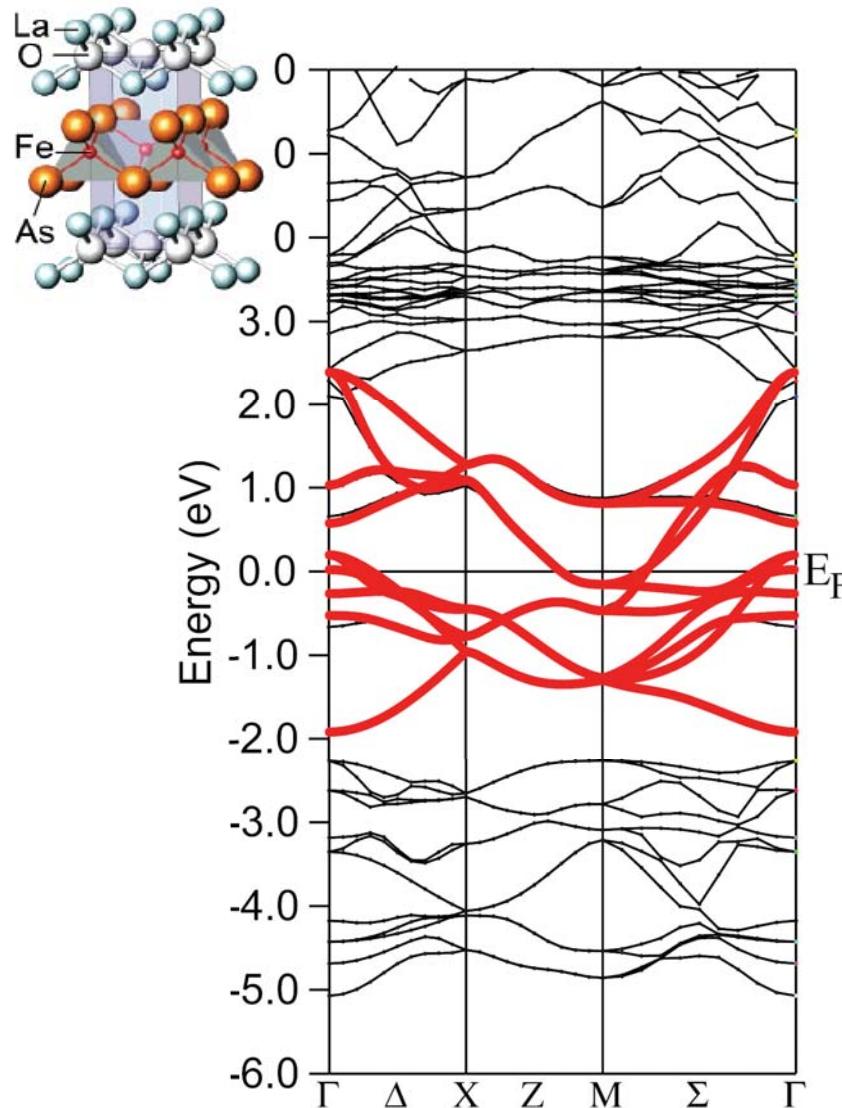
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LDA band structure & MaxLoc Wannier functions



Complicated band structure
10 bands around E_F
(2 Fe atoms in the unit cell)

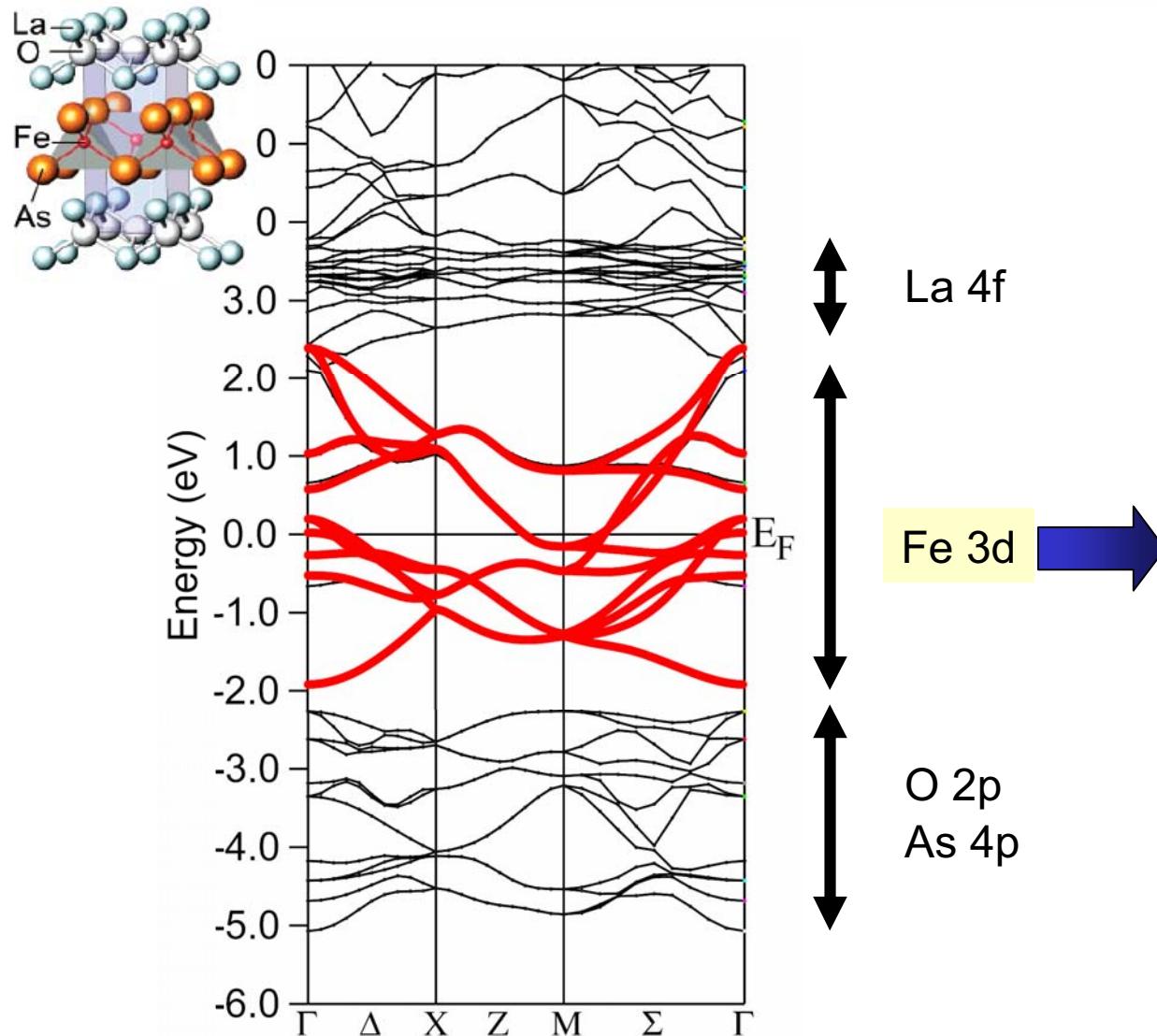
LDA band structure & MaxLoc Wannier functions



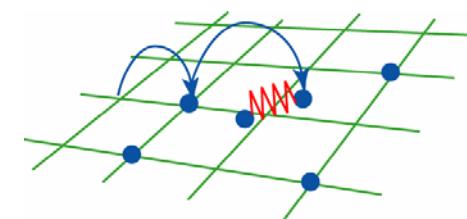
$$H_0 = \sum_{\sigma} \sum_{RR'} \sum_{nm} t_{mRnR'} c_{\sigma nR}^{\dagger} c_{\sigma mR'}$$

 10 band model
 ↓
 5 band model (BZ unfolding)
 ↓
 4,3,2 band model ?

LDA band structure & MaxLoc Wannier functions



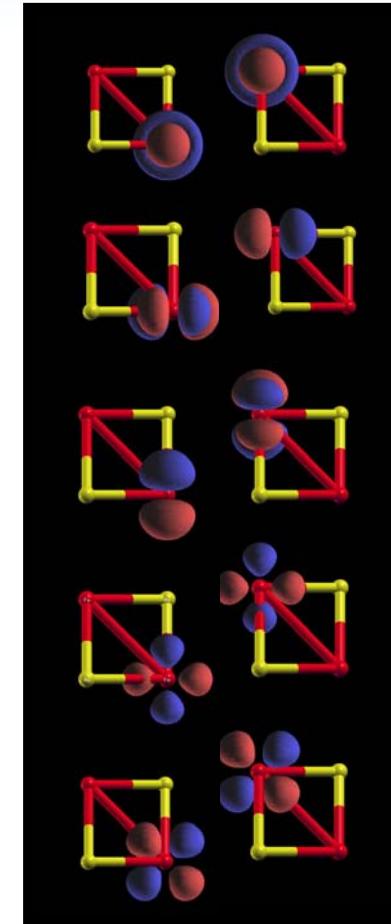
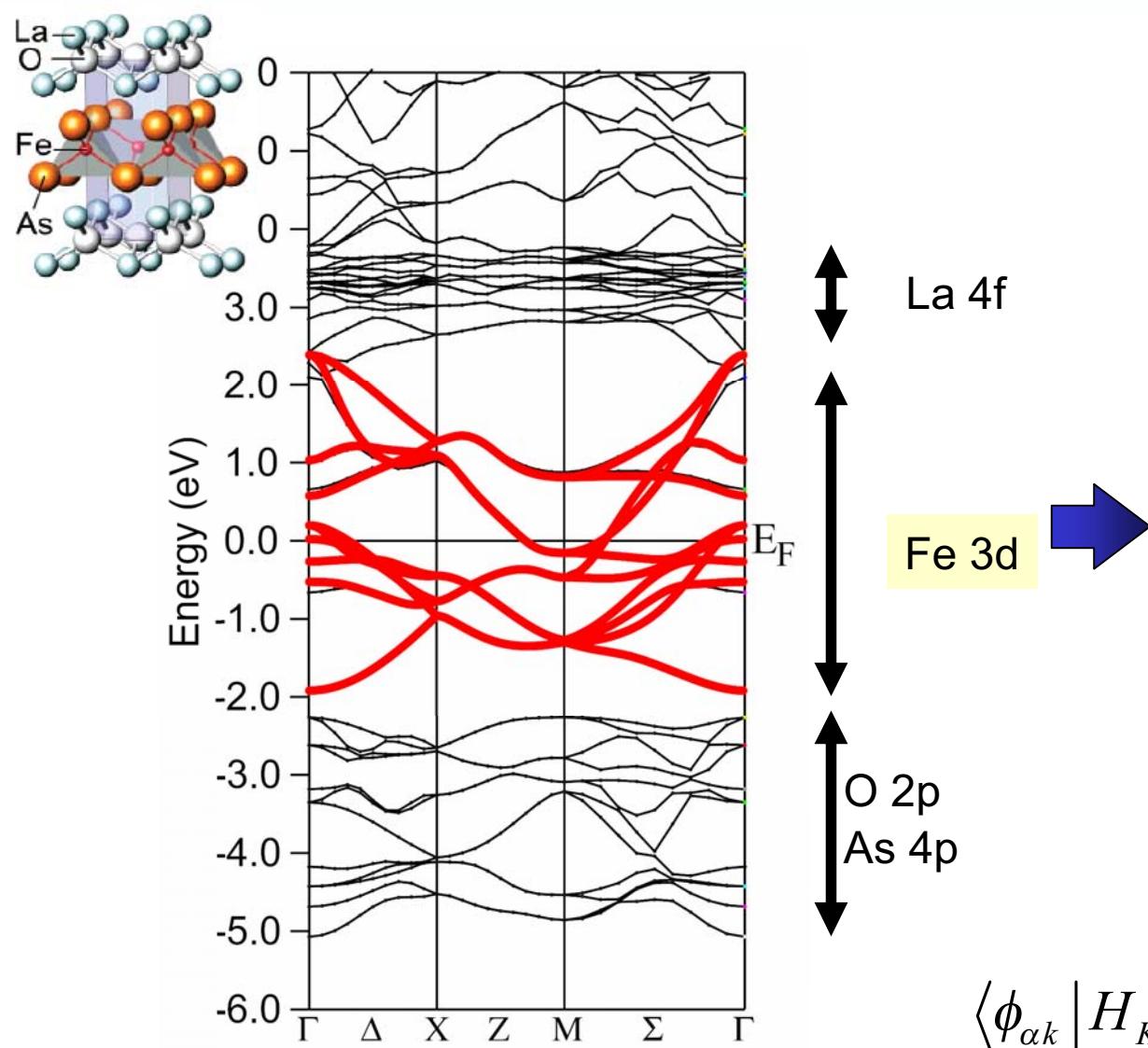
$$H_0 = \sum_{\sigma} \sum_{RR'} \sum_{nm} t_{mRnR'} c_{\sigma nR}^{\dagger} c_{\sigma mR'}^{}$$



$$c_{\sigma nR}^{\dagger} |0\rangle \quad ?$$

Maximally localized
Wannier functions
(Marzari-Vanderbilt, 97)

LDA band structure & MaxLoc Wannier functions

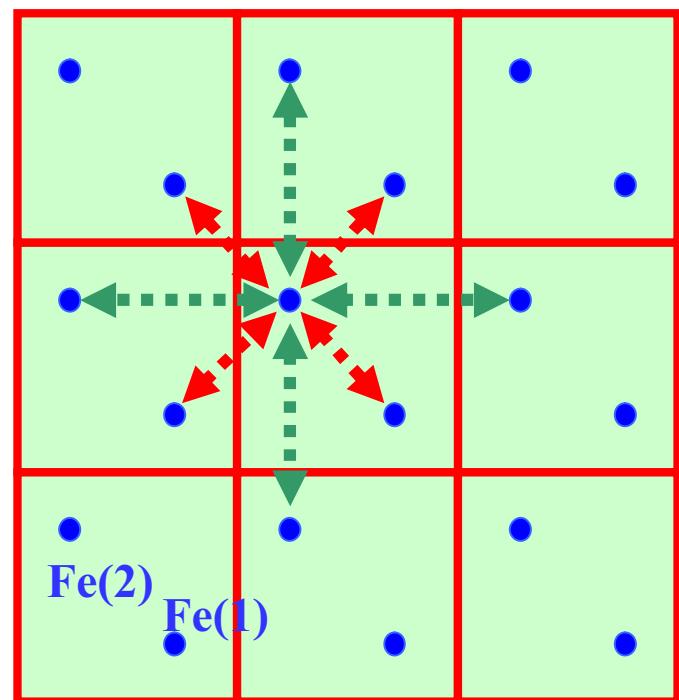


$$\langle \phi_{\alpha k} | H_{KS} | \phi_{\alpha k} \rangle \xrightarrow{\text{blue arrow}} \langle w_{\mu i} | H_{KS} | w_{\nu j} \rangle$$

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Transfer hoppings

$$t_{\mu i v j} = \langle w_{\mu i} | H_{KS} | w_{v j} \rangle$$



Kuroki, RA et al, arXiv:0803.3325 to appear in PRL
 Nakamura-RA-Imada, arxiv:0806.4750 to appear in JPSJ

Nearest

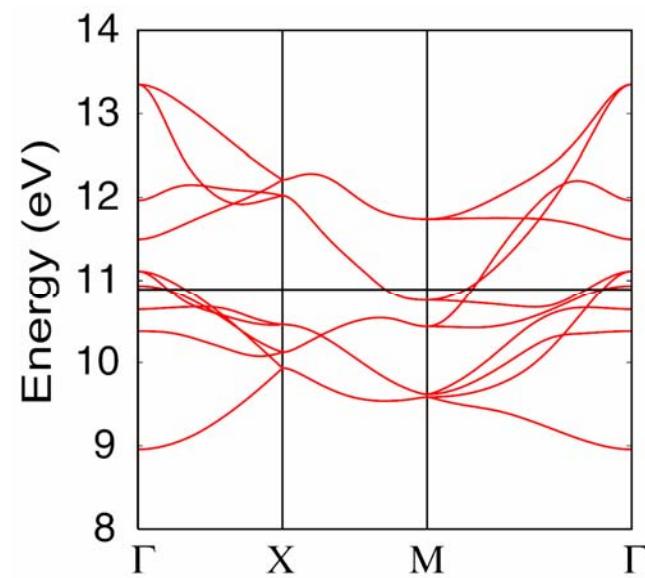
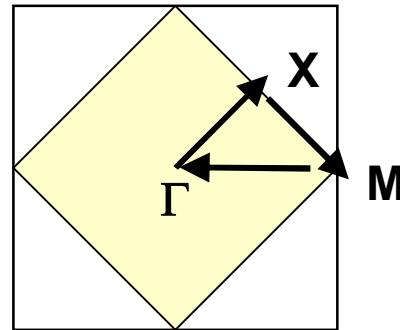
	xy	yz	z^2	zx	x^2-y^2
xy	-0.315	-0.255	-0.299	-0.254	0.000
yz	-0.255	-0.211	-0.077	-0.134	0.176
z^2	-0.299	-0.077	0.076	-0.077	-0.000
zx	-0.254	-0.134	-0.077	-0.211	-0.176
x^2-y^2	0.000	0.176	-0.000	-0.176	-0.185

Next Nearest

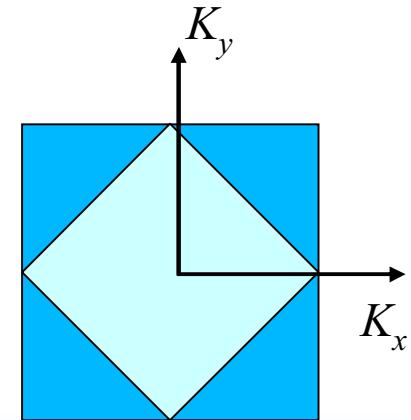
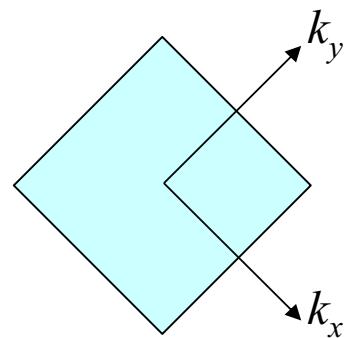
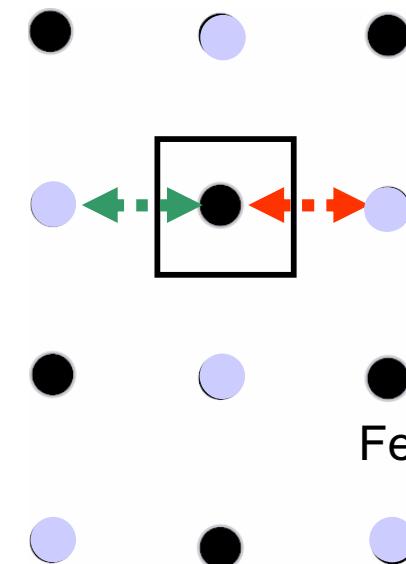
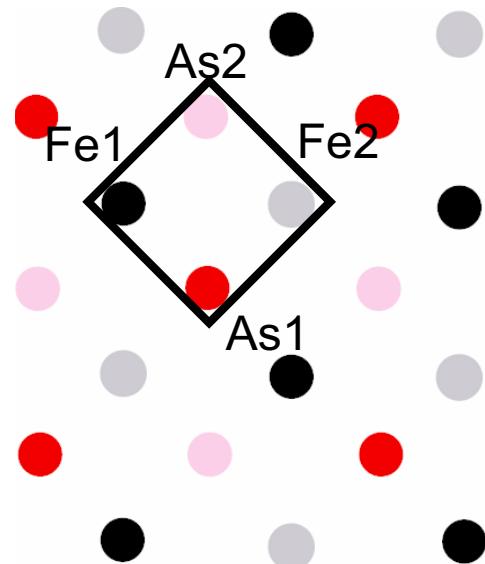
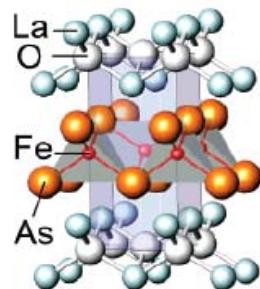
-0.059	-0.141	-0.000	0.000	0.000
0.141	0.148	0.000	0.000	0.000
-0.000	0.000	-0.003	-0.145	-0.181
0.000	0.000	0.145	0.331	-0.011
0.000	0.000	-0.181	0.011	0.131

in eV

BZ unfolding

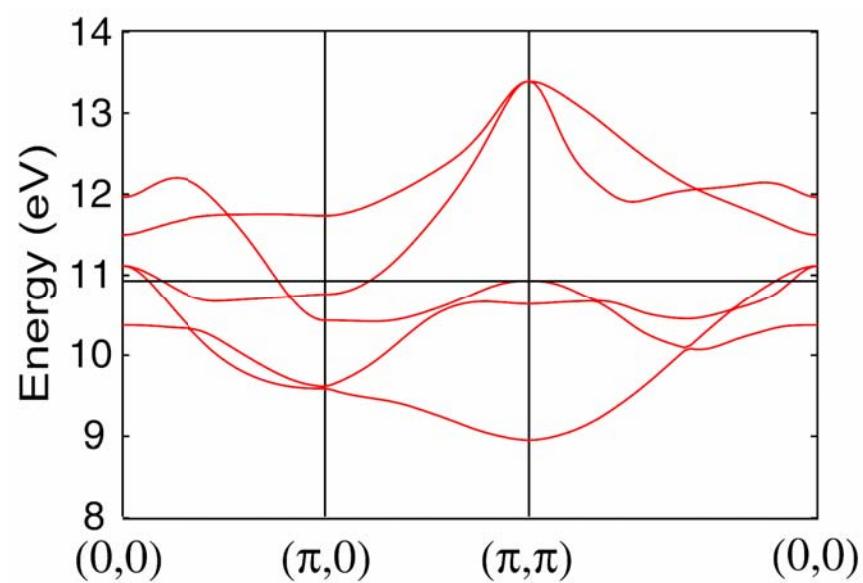
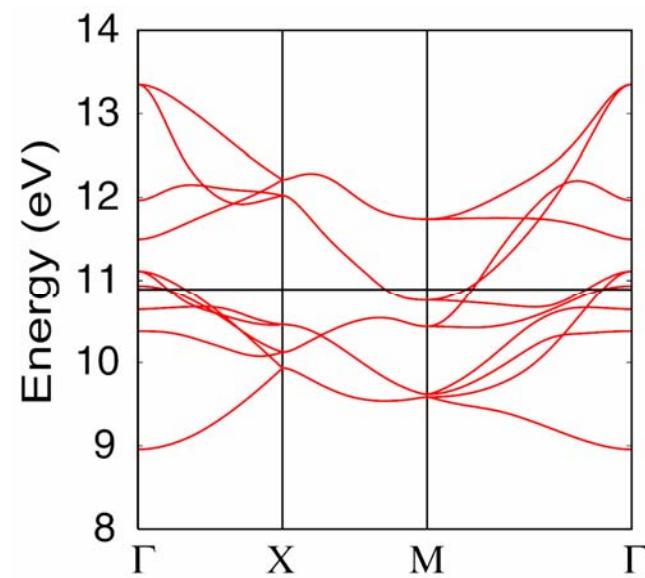
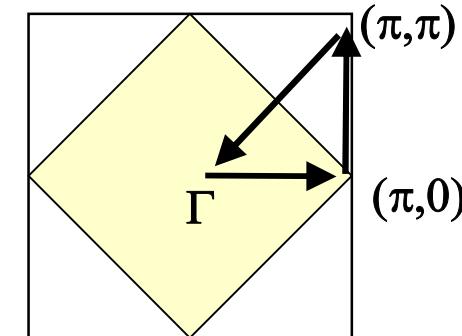
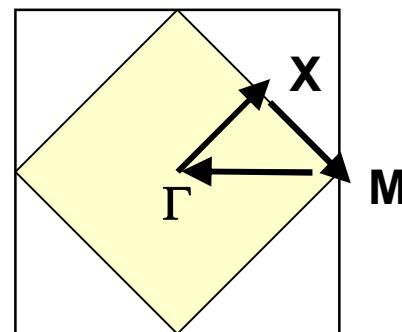


BZ unfolding

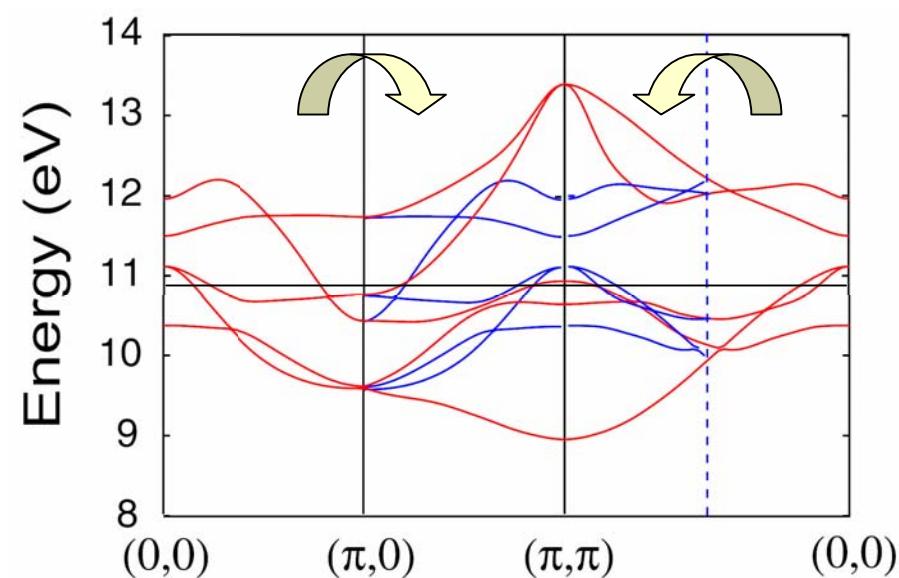
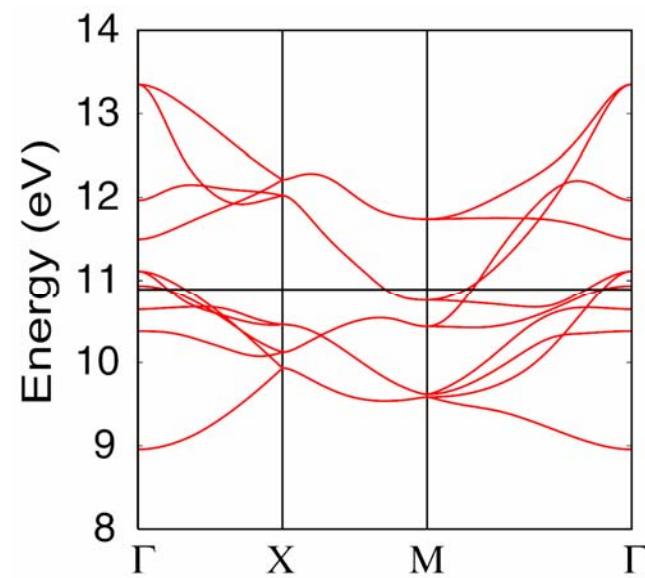
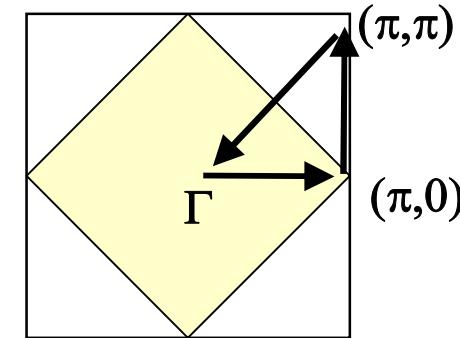
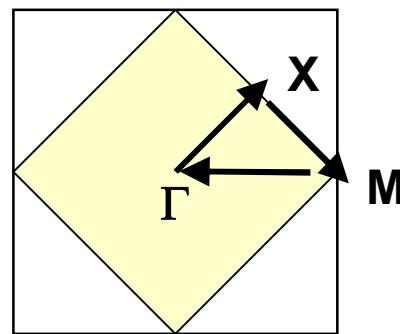


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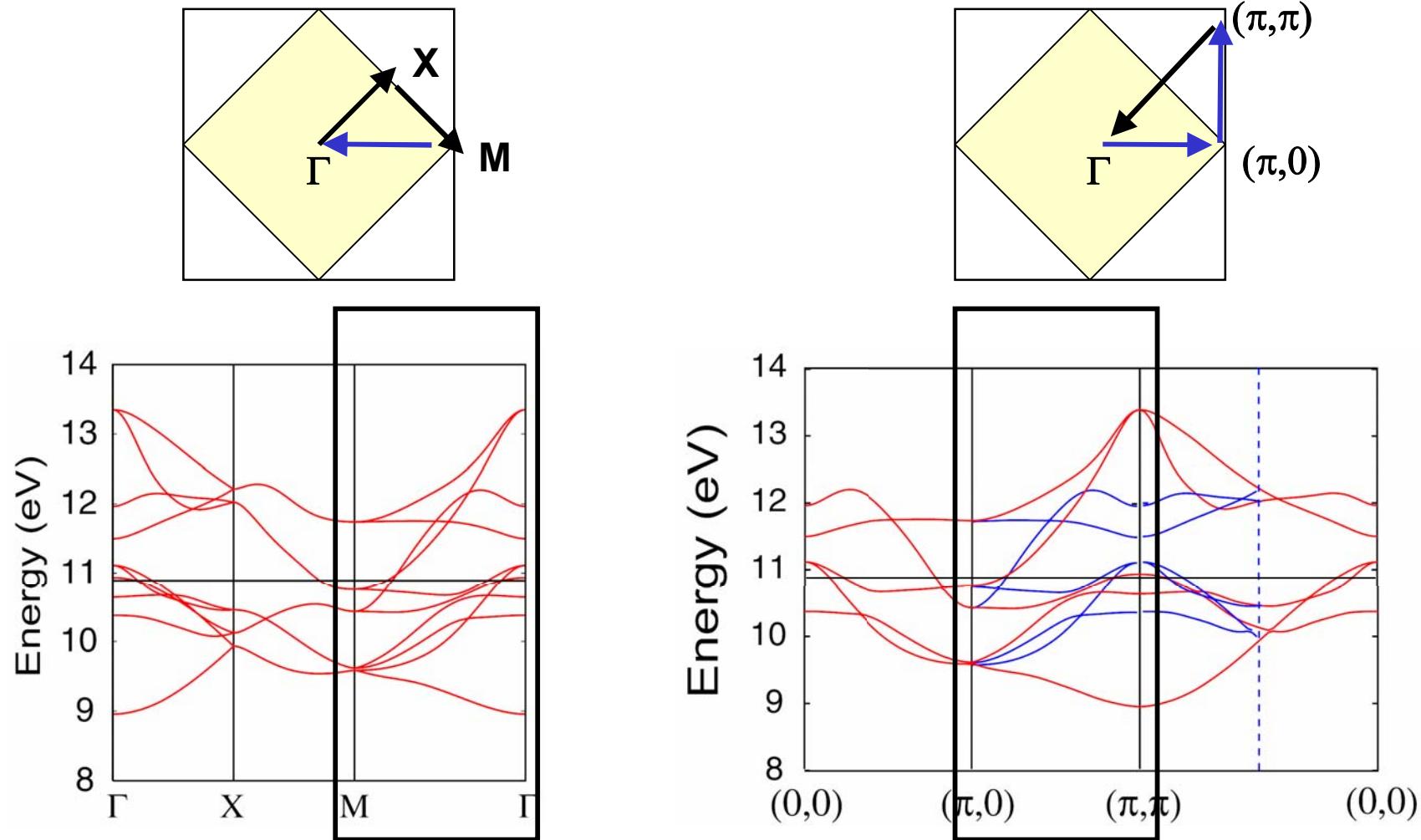
BZ unfolding



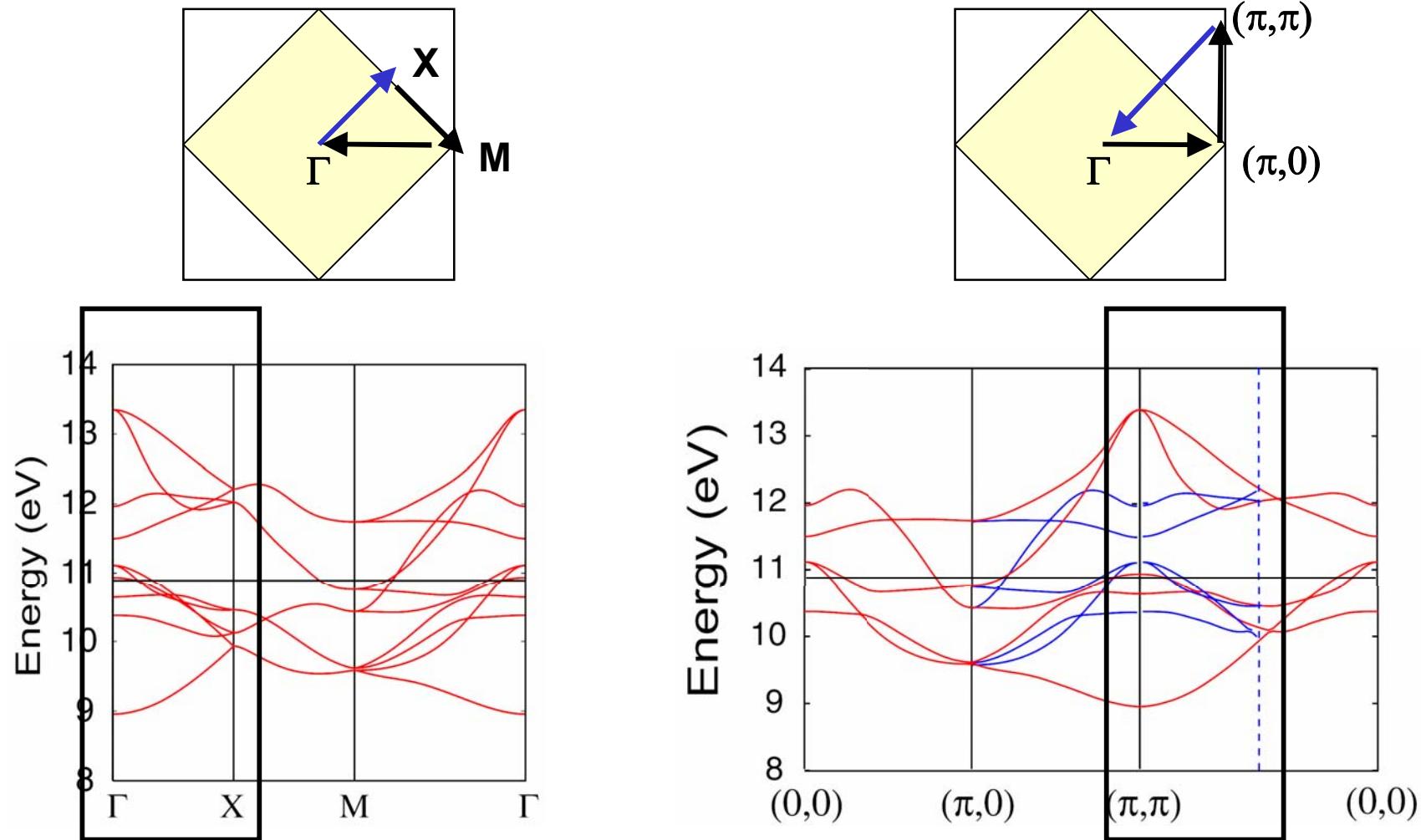
BZ unfolding



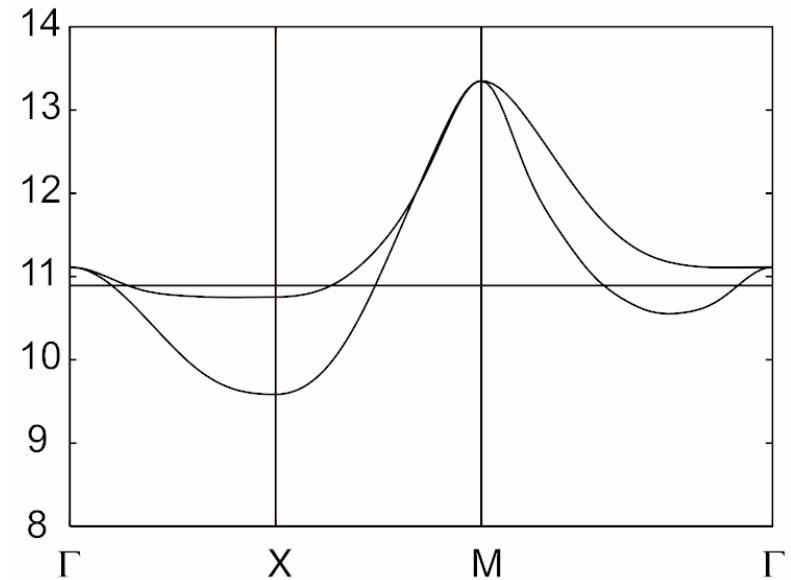
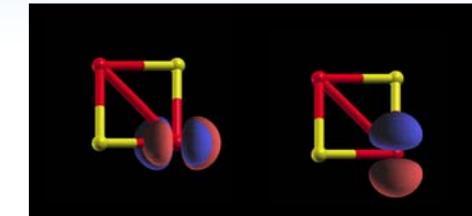
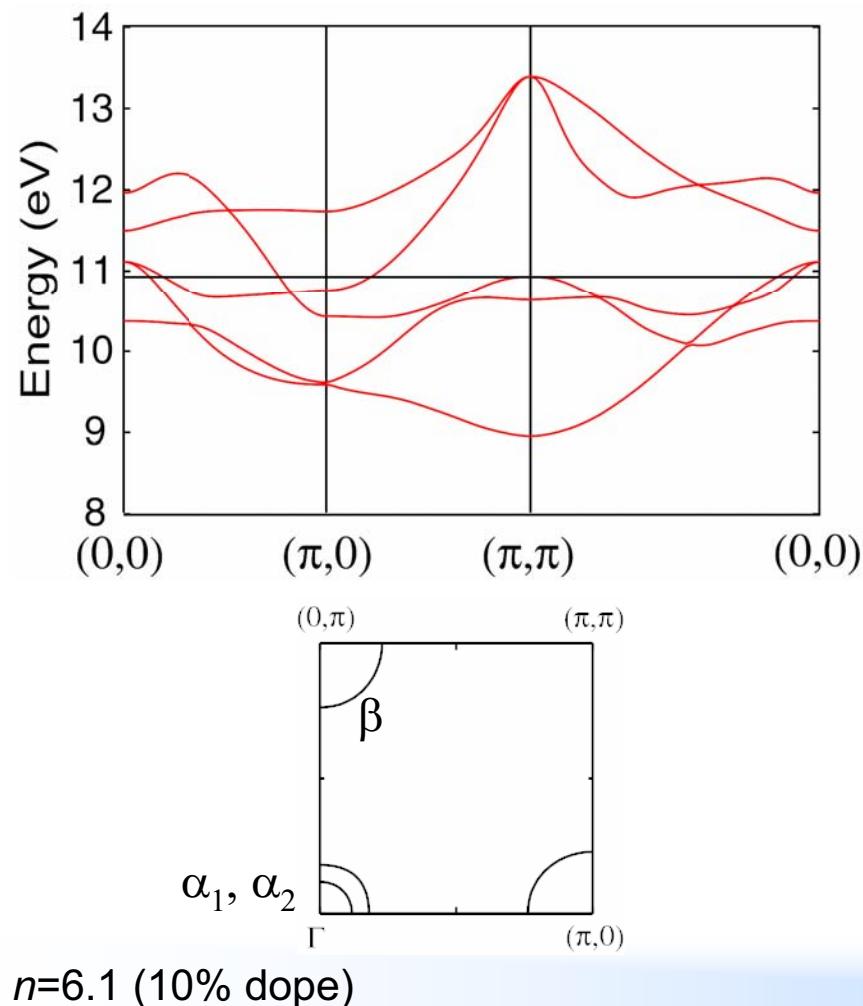
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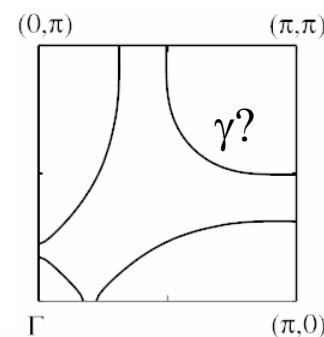
BZ unfolding



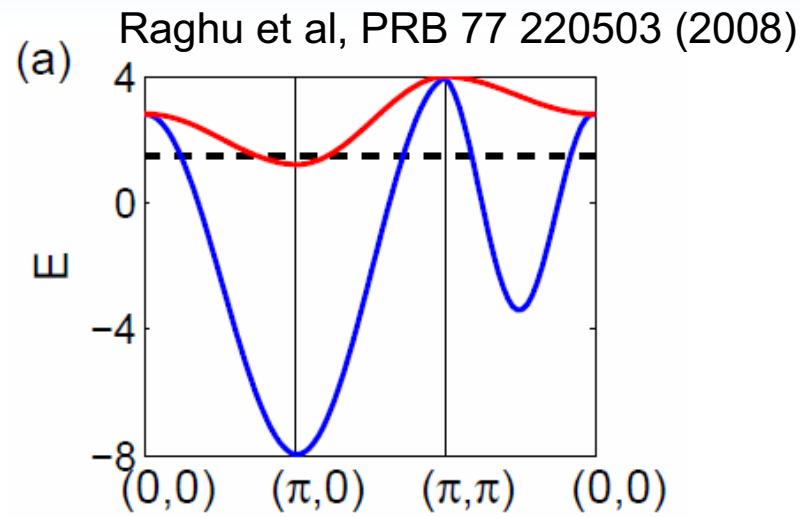
2 band model ($d_{yz}+d_{xz}$)



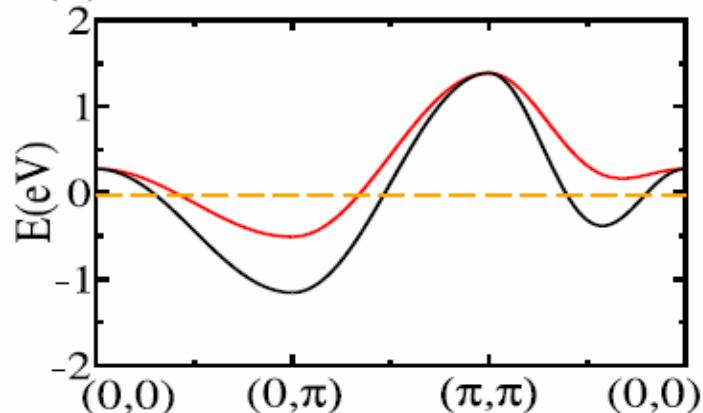
- ✗ α_2 absent
- ✗ Large β
- ✗ γ ?



2 band model ($d_{yz}+d_{xz}$)

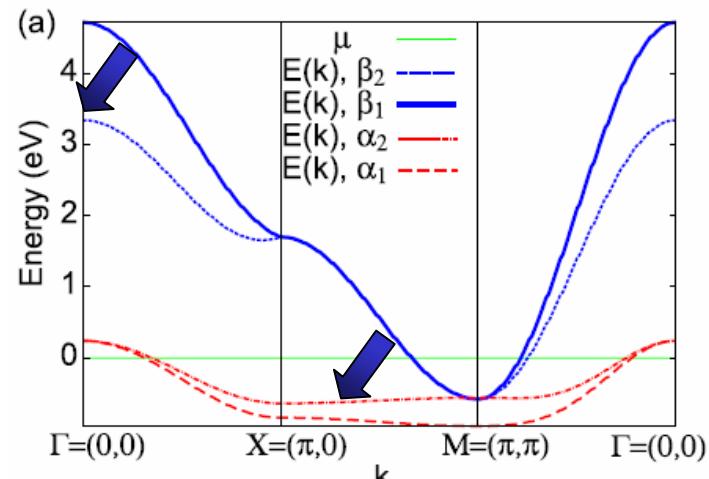


(b) Daghofer et al, arXiv:0805.0148

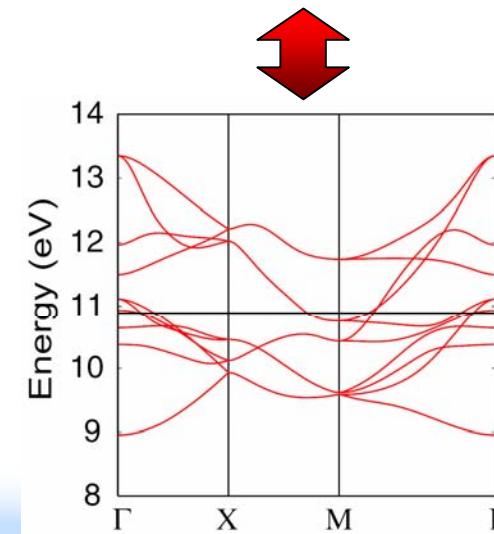


one FS around Γ
FS appears around (π,π)

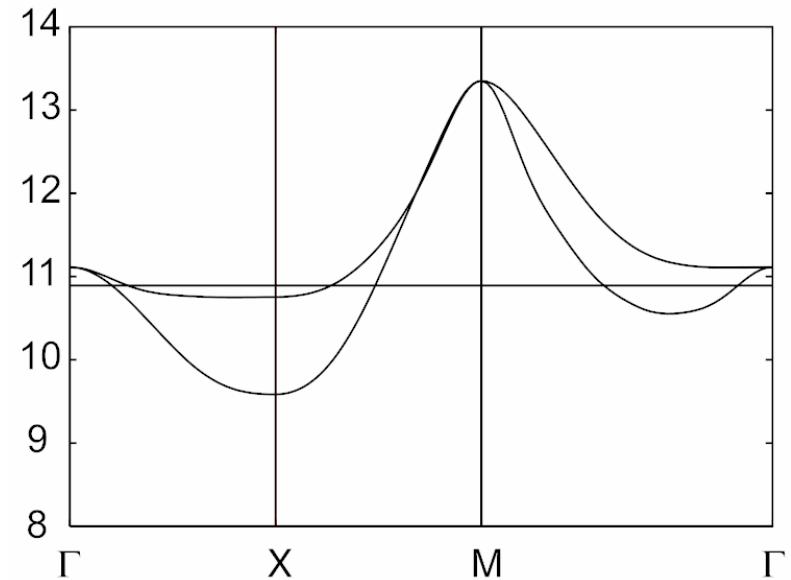
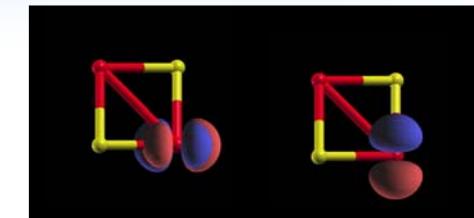
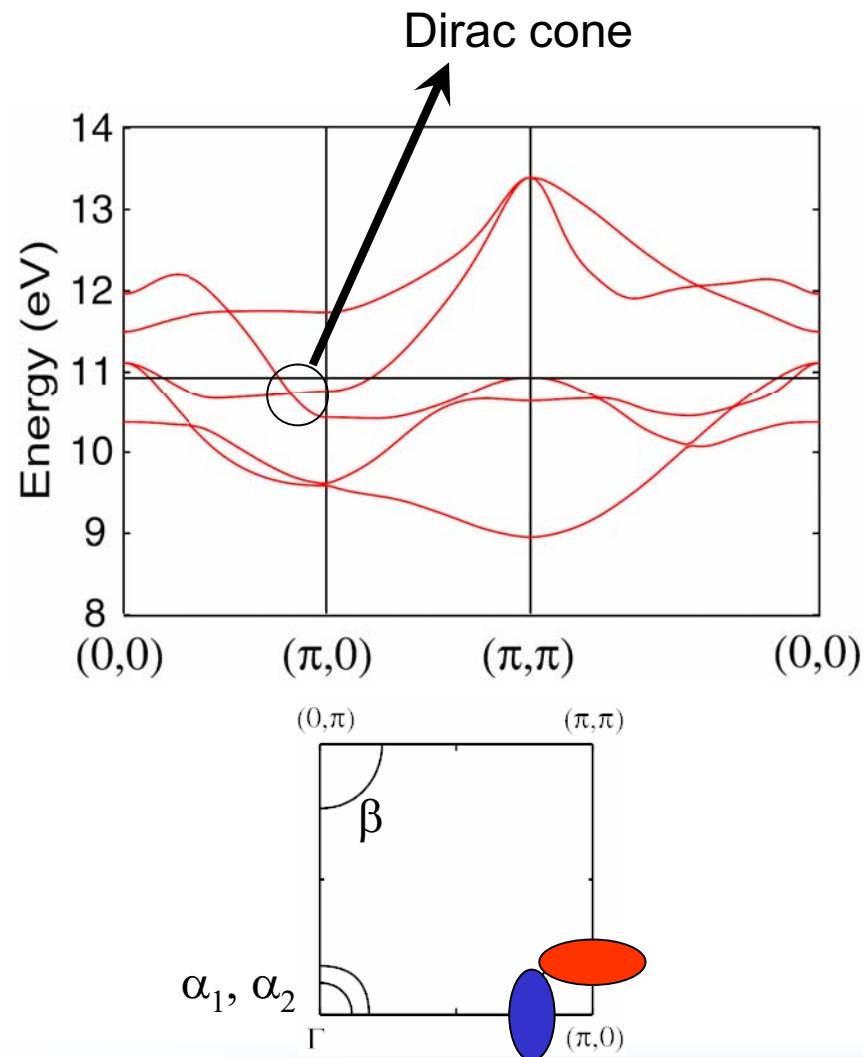
Korshunov et al, arXiv:0804.1793



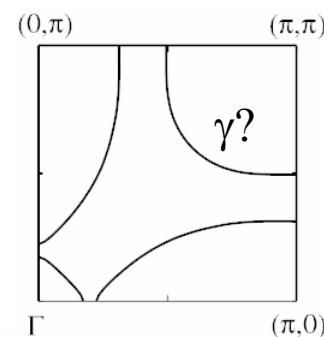
4 band model from 10 bands
Bonding-antibonding split along X-M



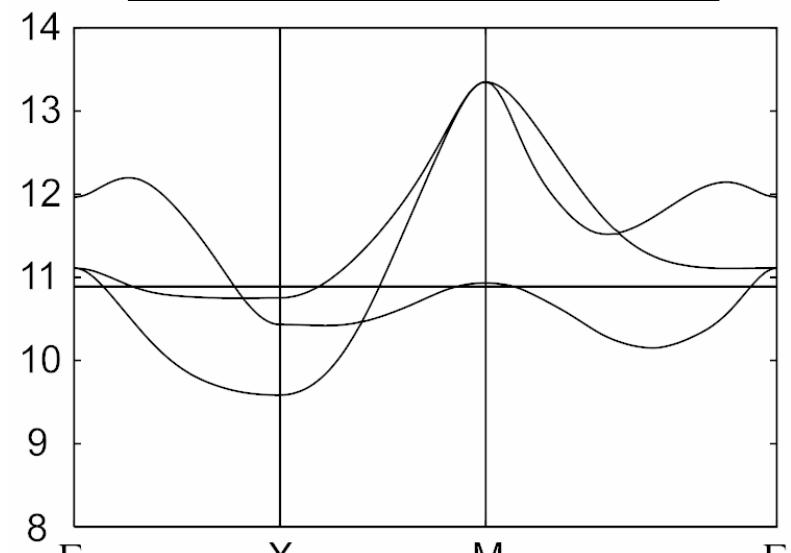
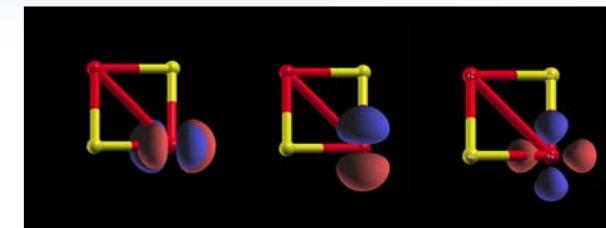
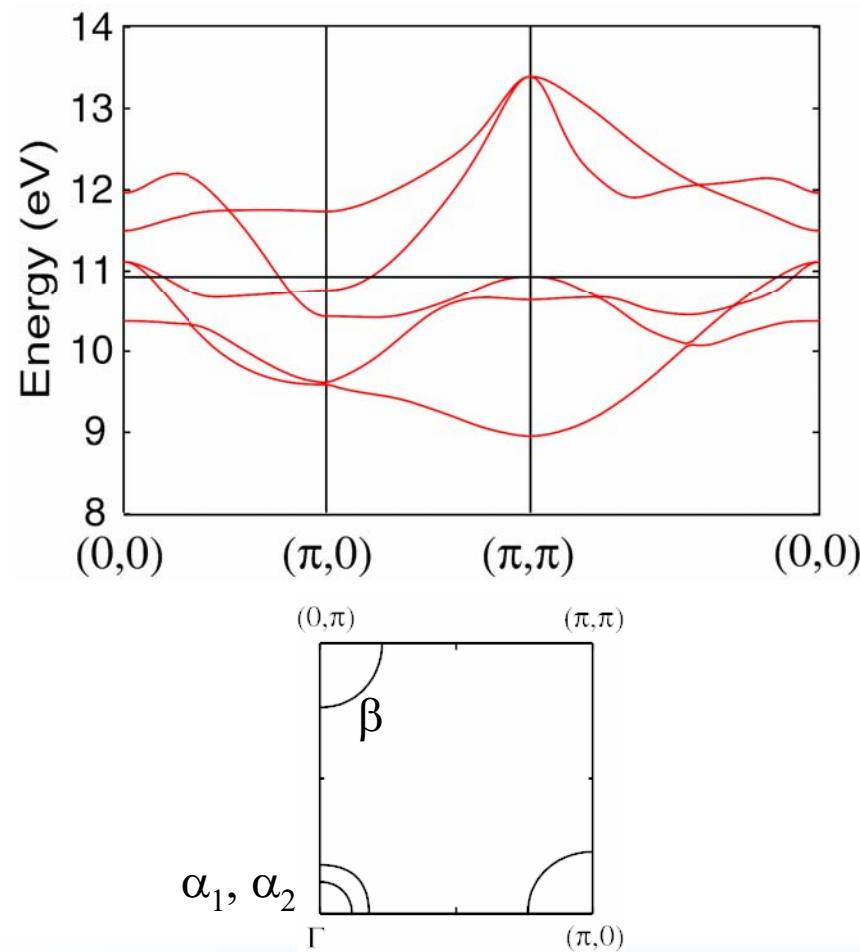
2 band model ($d_{yz}+d_{xz}$)



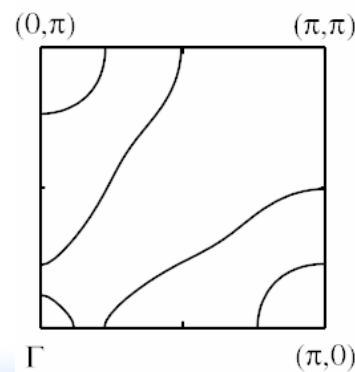
- ✗ α_2 absent**
- ✗ Large β**
- ✗ γ ?**



3 band model ($d_{yz} + d_{xz} + d_{x^2-y^2}$)

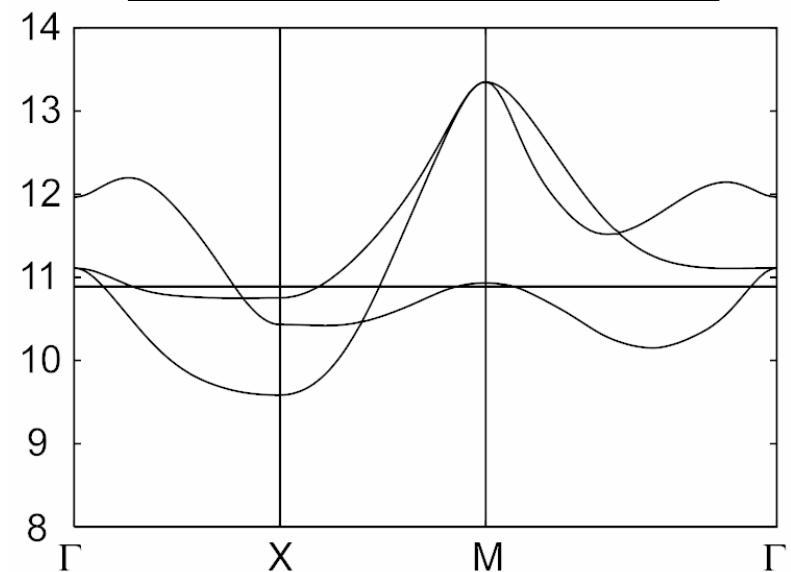
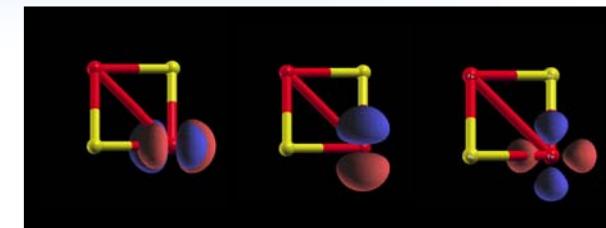
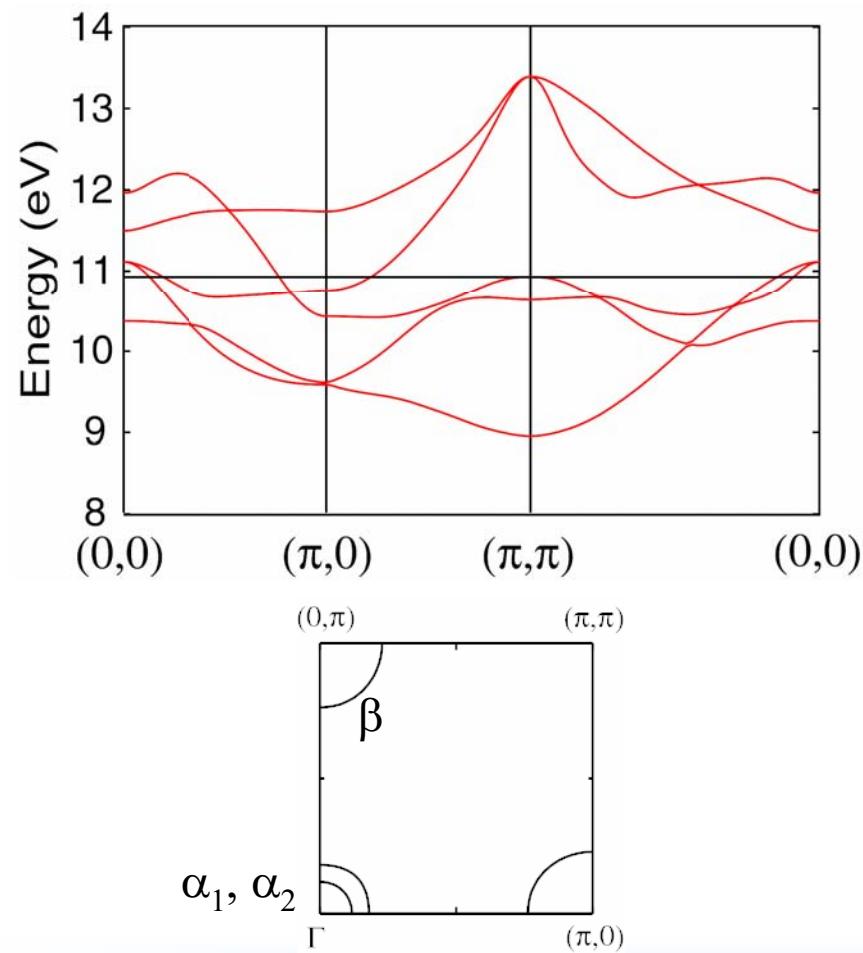


- $\times \alpha_2$ absent
- $\times \gamma ?$
- \checkmark Small β

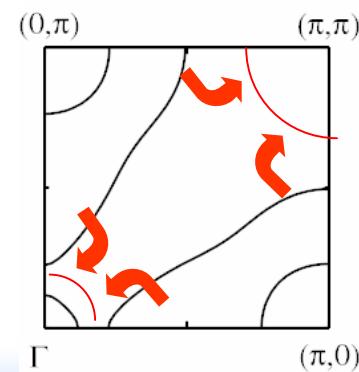


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3 band model ($d_{yz} + d_{xz} + d_{x^2-y^2}$)



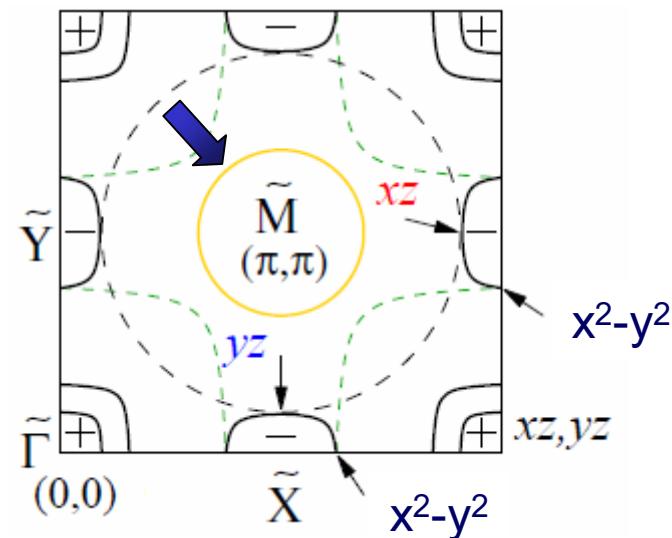
- ✗ α_2 absent
- ✗ γ ?
- ✓ Small β



3 band model ($d_{yz}+d_{xz}+d_{x^2-y^2}$)

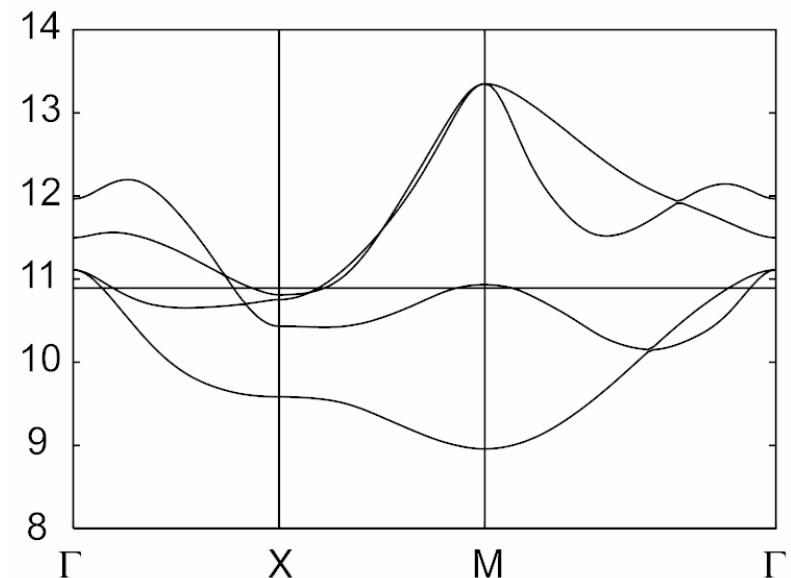
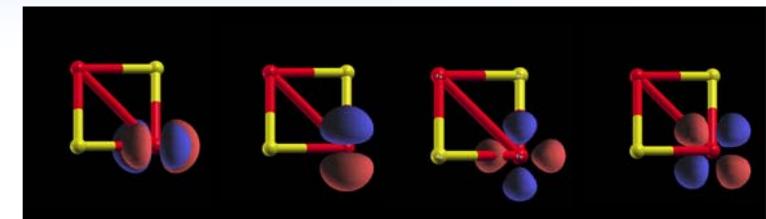
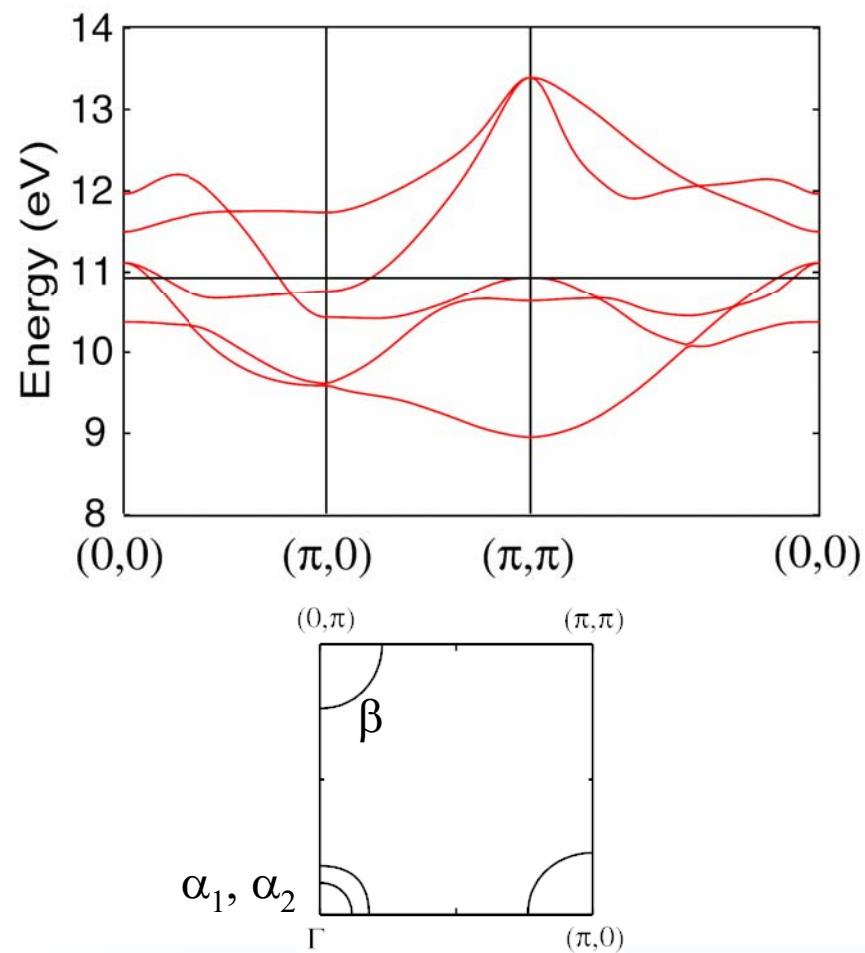
Lee & Wen, arXiv:0804.1739

To make α_1, α_2 around Γ and β around X , we have to consider $d_{x^2-y^2}$



$d_{yz}+d_{xz}$ makes FS around M

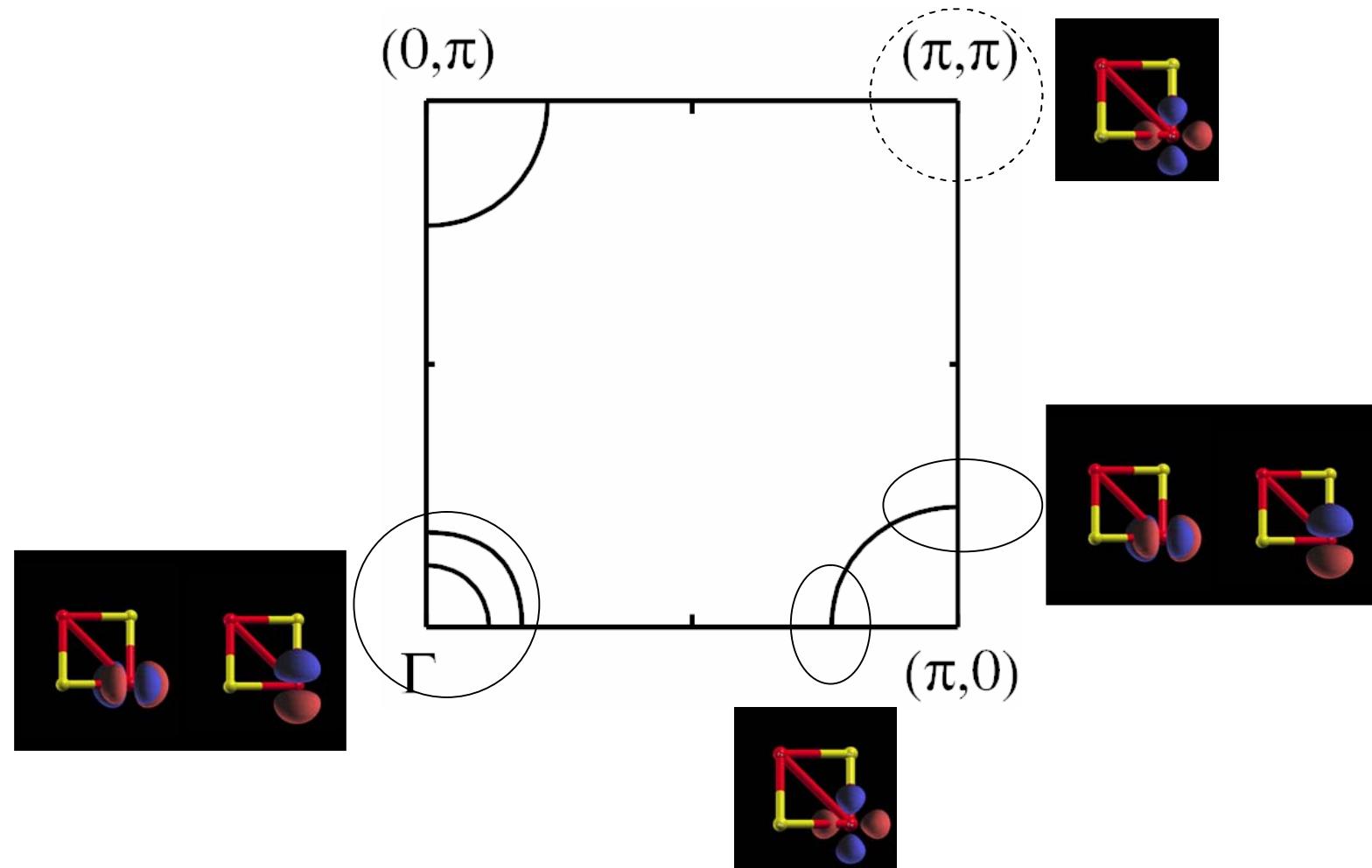
4 band model ($d_{yz}+d_{xz}+d_{x^2-y^2}+d_{xy}$)



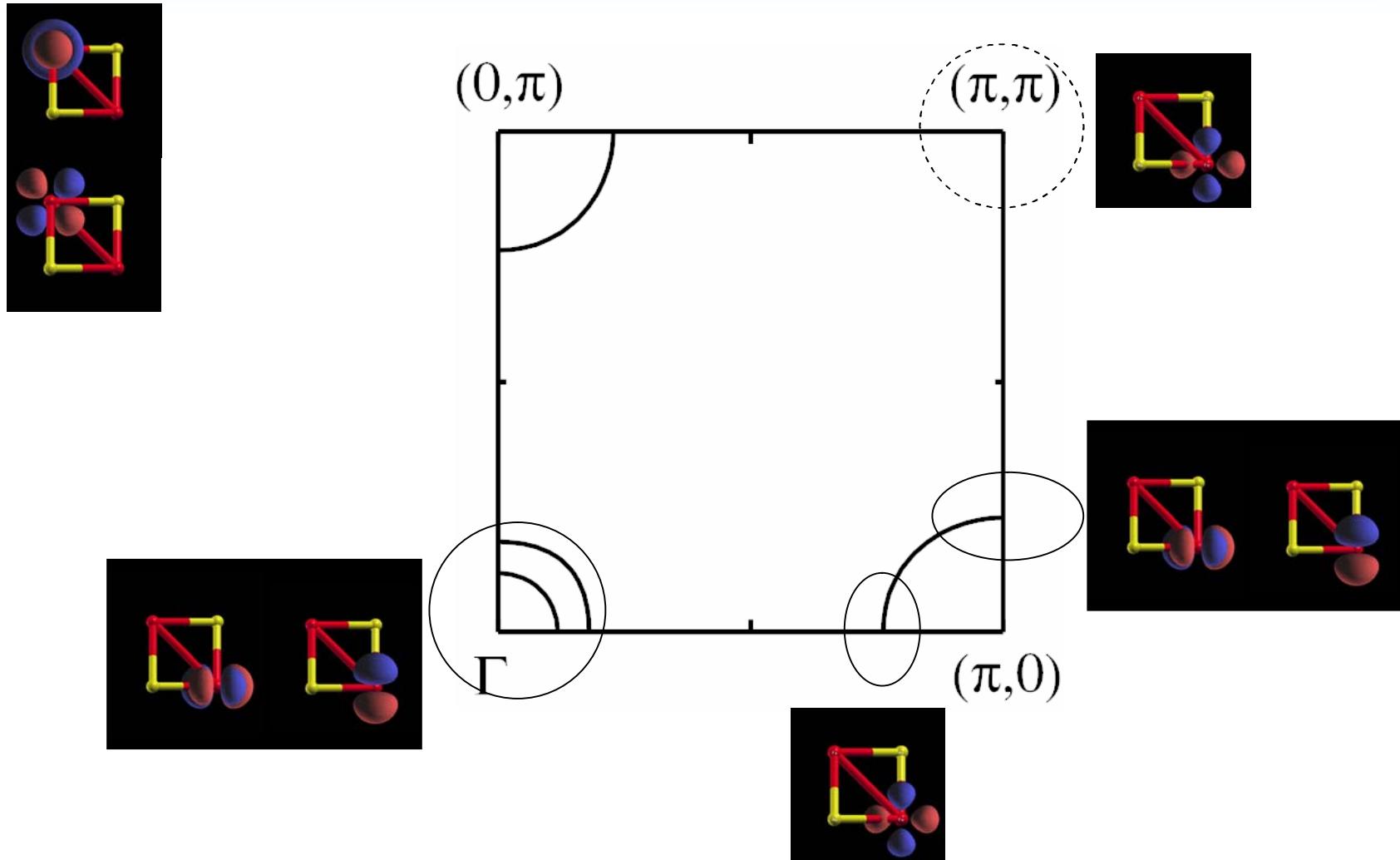
✗ β_2 ?

- ✓ small β
- ✓ No γ
- ✓ α_1 & α_2

Character of the Fermi surface



Character of the Fermi surface

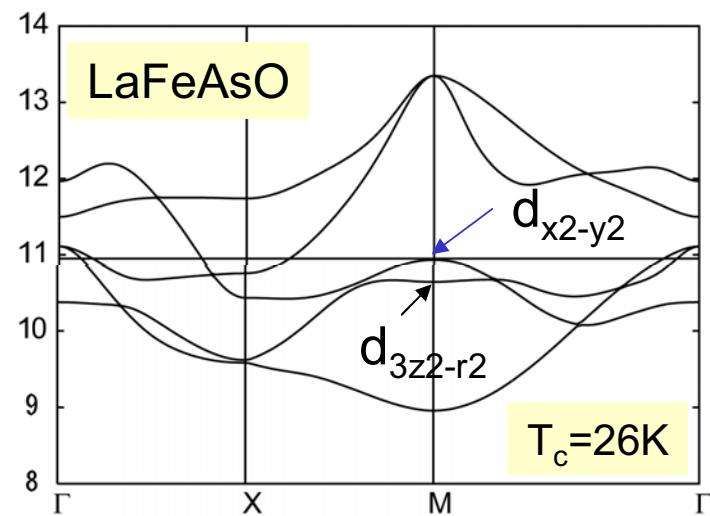
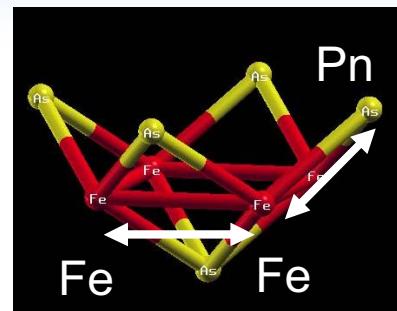


Effective model involves all five 3d orbitals

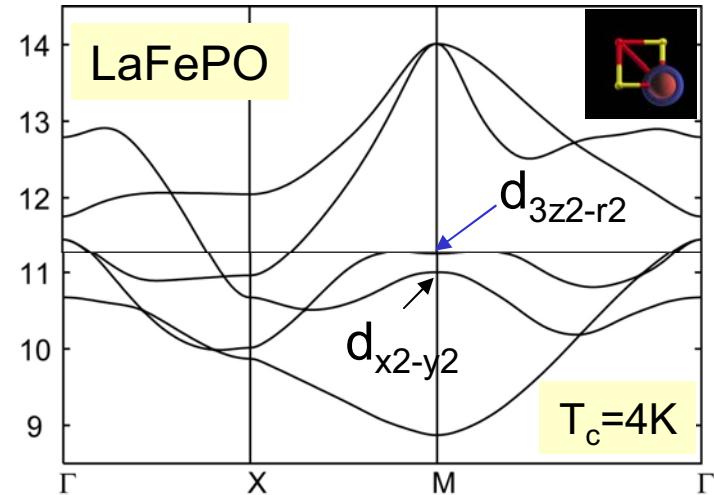
cf) Tesanovic et al, cond-mat/0804.4678

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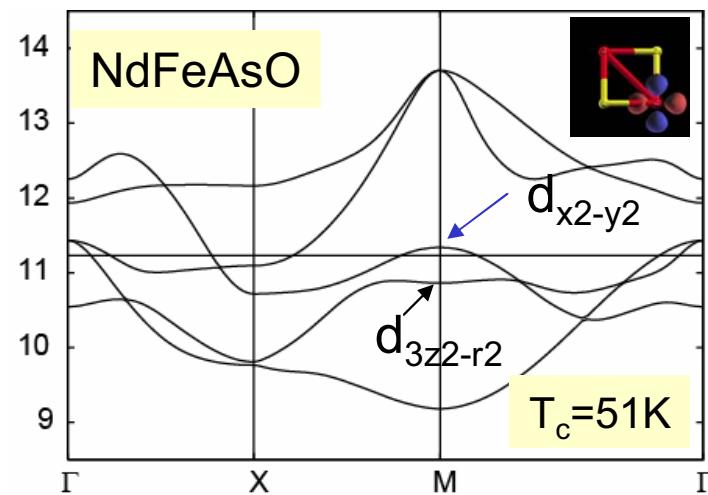
Material dependence



Fe-Fe: 4.04 Å
Fe-As: 2.41 Å



Fe-Fe: 3.96 Å
Fe-P: 2.29 Å



Fe-Fe: 3.95 Å
Fe-As: 2.40 Å

Ab initio construction of an effective model



$$\begin{aligned} \mathcal{H} = & \sum_{\sigma} \sum_{\mathbf{R}\mathbf{R}'} \sum_{nm} t_{m\mathbf{R}n\mathbf{R}'} a_{n\mathbf{R}}^{\sigma\dagger} a_{m\mathbf{R}'}^{\sigma} \\ & + \frac{1}{2} \sum_{\sigma\rho} \sum_{\mathbf{R}\mathbf{R}'} \sum_{nm} \left\{ U_{m\mathbf{R}n\mathbf{R}'} a_{n\mathbf{R}}^{\sigma\dagger} a_{m\mathbf{R}'}^{\rho\dagger} a_{m\mathbf{R}'}^{\rho} a_{n\mathbf{R}}^{\sigma} \right. \\ & \left. + J_{m\mathbf{R}n\mathbf{R}'} (a_{n\mathbf{R}}^{\sigma\dagger} a_{m\mathbf{R}'}^{\rho\dagger} a_{n\mathbf{R}}^{\rho} a_{m\mathbf{R}'}^{\sigma} + a_{n\mathbf{R}}^{\sigma\dagger} a_{n\mathbf{R}}^{\rho\dagger} a_{m\mathbf{R}'}^{\rho} a_{m\mathbf{R}'}^{\sigma}) \right\} \end{aligned}$$

Ab initio construction of an effective model



$$\begin{aligned}\mathcal{H} = & \sum_{\sigma} \sum_{\mathbf{R}\mathbf{R}'} \sum_{nm} t_{m\mathbf{R}n\mathbf{R}'} a_{n\mathbf{R}}^{\sigma\dagger} a_{m\mathbf{R}'}^{\sigma} \\ & + \frac{1}{2} \sum_{\sigma\rho} \sum_{\mathbf{R}\mathbf{R}'} \sum_{nm} \left\{ U_{m\mathbf{R}n\mathbf{R}'} a_{n\mathbf{R}}^{\sigma\dagger} a_{m\mathbf{R}'}^{\rho\dagger} a_{m\mathbf{R}'}^{\rho} a_{n\mathbf{R}}^{\sigma} \right. \\ & \quad \left. + J_{m\mathbf{R}n\mathbf{R}'} (a_{n\mathbf{R}}^{\sigma\dagger} a_{m\mathbf{R}'}^{\rho\dagger} a_{n\mathbf{R}}^{\rho} a_{m\mathbf{R}'}^{\sigma} + a_{n\mathbf{R}}^{\sigma\dagger} a_{n\mathbf{R}}^{\rho\dagger} a_{m\mathbf{R}'}^{\rho} a_{m\mathbf{R}'}^{\sigma}) \right\}\end{aligned}$$

Constrained RPA

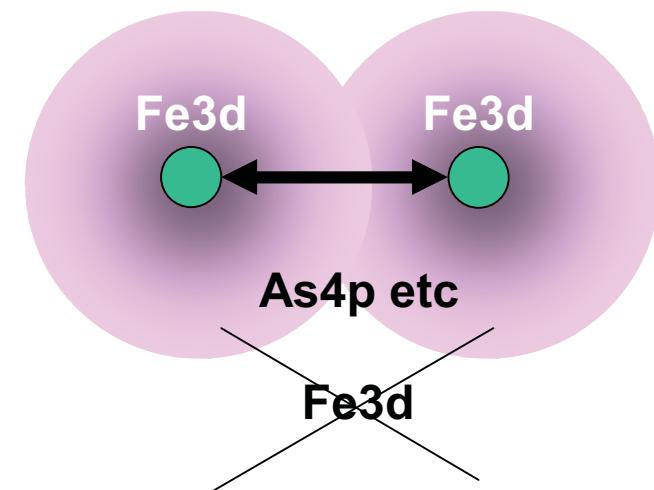
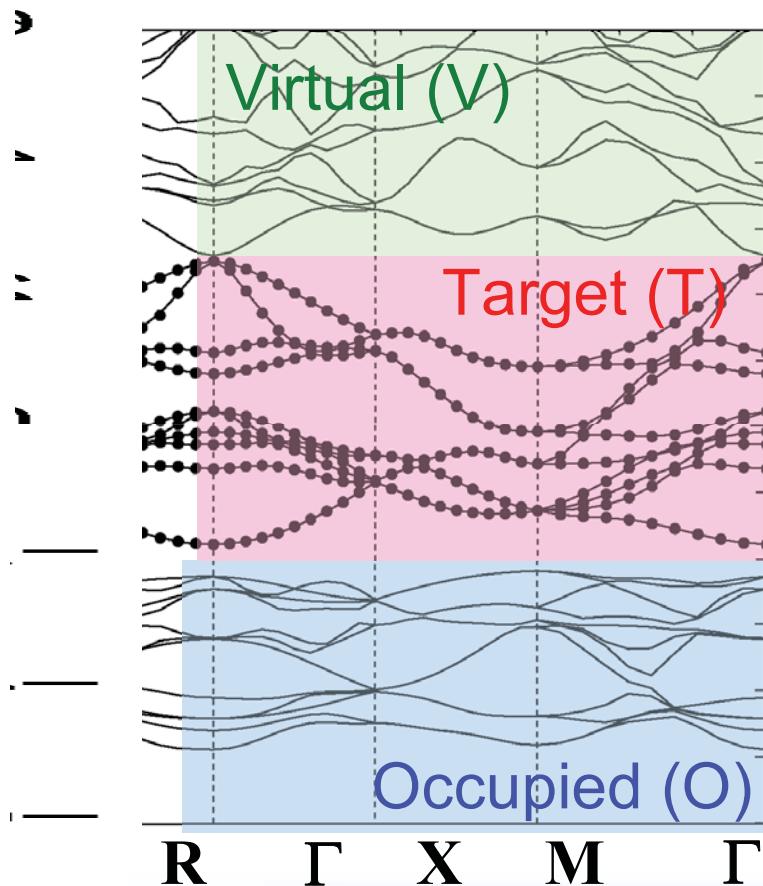
Aryasetiawan et al, PRB 70, 195104 (2004)
Solovyev-Imada, PRB 71, 045103 (2005)



$$W = (1 - \nu \chi)^{-1} \nu$$

Full RPA polarizability:

$$\chi = \sum_i^{occ} \sum_j^{unocc} \frac{\psi_i(r) \psi_j^*(r) \psi_i^*(r') \psi_j(r')}{\omega - \varepsilon_j + \varepsilon_i \pm i\delta}$$



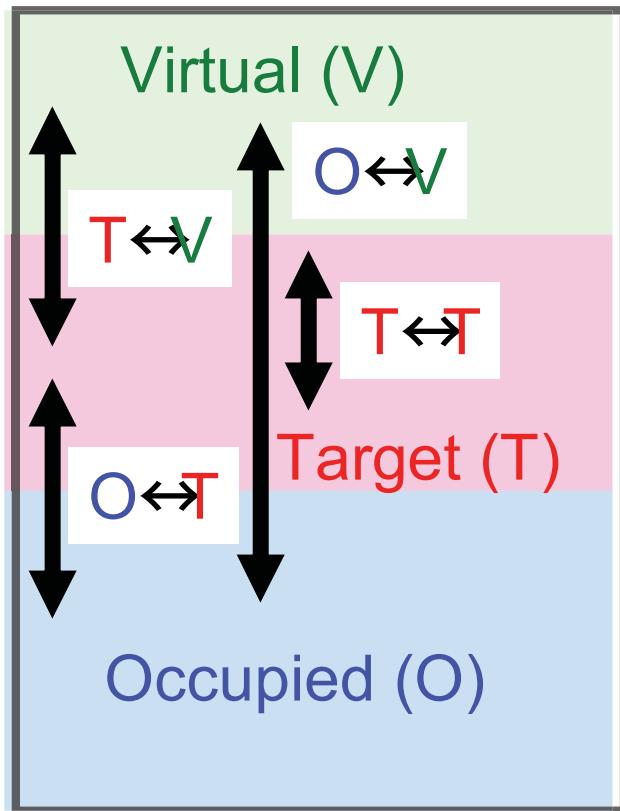
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Constrained RPA

Aryasetiawan et al, PRB 70, 195104 (2004)
 Solovyev-Imada, PRB 71, 045103 (2005)



$$W = (1 - \nu \chi)^{-1} \nu$$



Full RPA polarizability:

$$\chi = \sum_i^{occ} \sum_j^{unocc} \frac{\psi_i(r)\psi_j^*(r)\psi_i^*(r')\psi_j(r')}{\omega - \varepsilon_j + \varepsilon_i \pm i\delta}$$



$$\chi = \sum_{O \leftrightarrow T} + \sum_{T \leftrightarrow V} + \sum_{O \leftrightarrow V} + \sum_{T \leftrightarrow T}$$

$$\chi_r = \sum_{O \leftrightarrow T} + \sum_{T \leftrightarrow V} + \sum_{O \leftrightarrow V} \quad \chi_d = \sum_{T \leftrightarrow T}$$

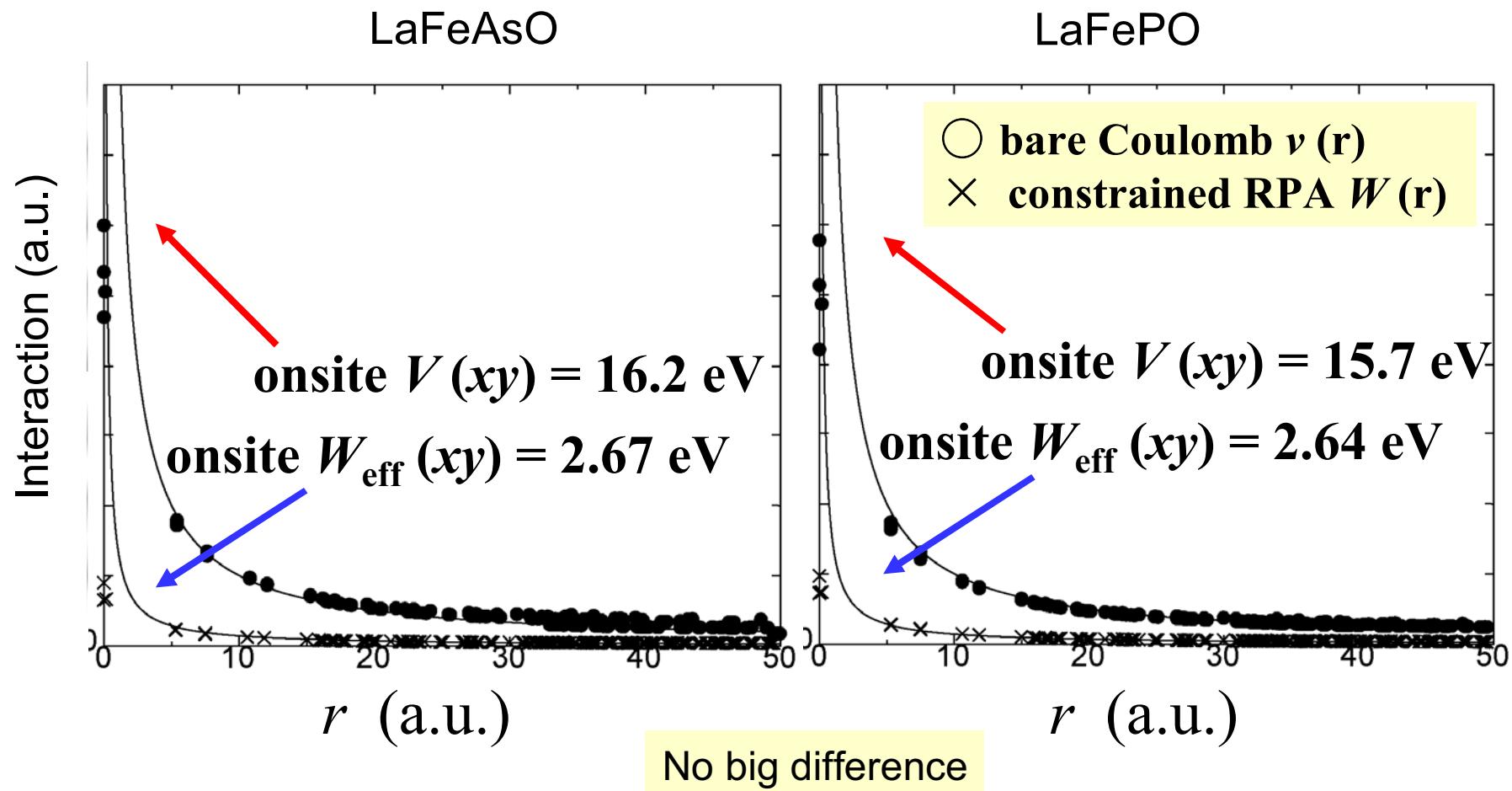
$$W_{eff} = (1 - \nu \chi_r)^{-1} \nu$$

$$W = \frac{\nu}{1 - \nu \chi} = \frac{W_{eff}}{1 - W_{eff} \chi_d}$$

$$U_R = \langle w_{\mu 0} w_{\mu 0} | W_{eff} | w_{\nu R} w_{\nu R} \rangle$$

R. Arita

Constrained RPA: Result



Nakamura-RA-Imada, arxiv:0806.4750 to appear in JPSJ

cf) Sawatzky et al, arXiv:0808.1390

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cf) Sawatzky et al, arXiv:0808.1390

$$U = U_0 - 2E_p$$

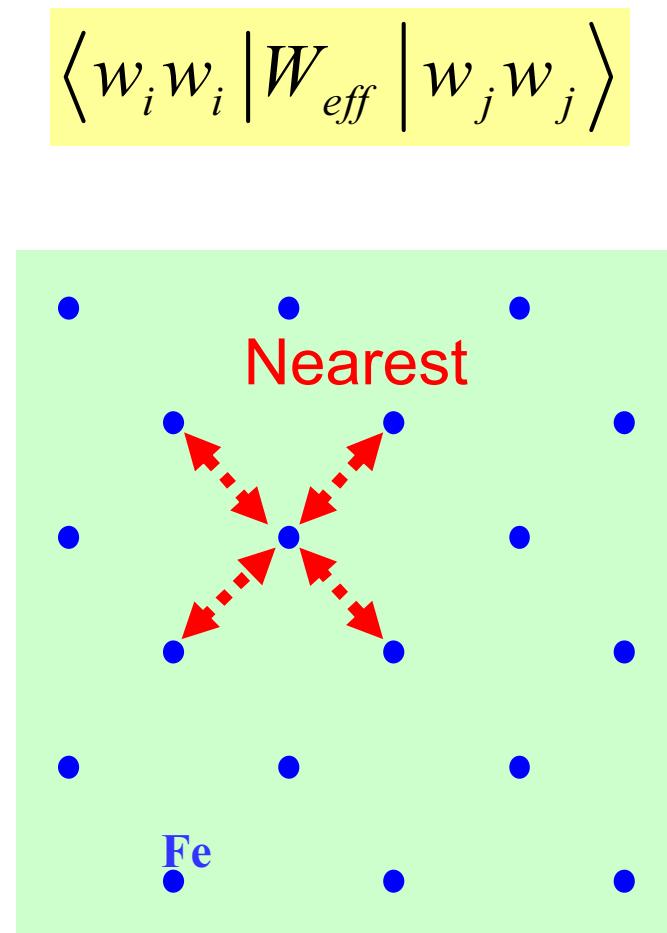
$$E_p \sim \frac{1}{2} \sum_{i=1}^4 \alpha_i E_i^2 \quad \alpha : \text{polizability}$$

$$E_i = e / R^2 \quad R: \text{Fe-Pn distance}$$

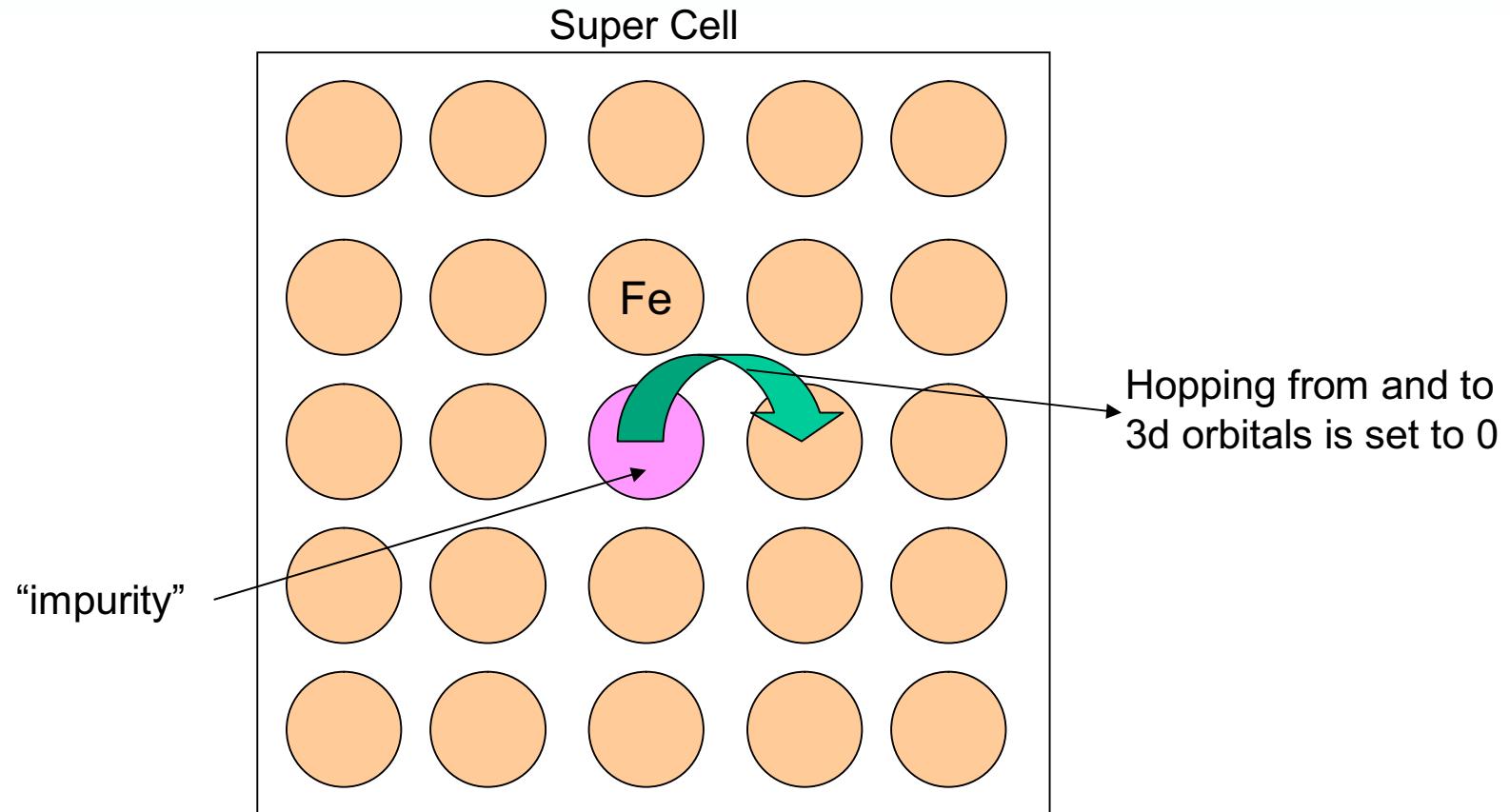
Large atomic radius of Pn \rightarrow large α \rightarrow large screening

$\alpha(\text{P}) < \alpha(\text{As})$, but $R(\text{Fe-P}) < R(\text{Fe-As}) \rightarrow U(\text{LaFePO}) \sim U(\text{LaFeAsO})$

Constrained RPA: Result



LaFeAsO					
	Onsite U				
xy	2.66	2.00	1.98	2.00	2.11
yz	2.00	2.27	2.22	1.84	1.71
z^2	1.98	2.22	2.66	2.22	1.71
zx	2.00	1.84	2.22	2.27	1.71
x^2-y^2	2.10	1.71	1.71	1.71	1.83
Nearest neighbor V					
	0.713	0.684	0.678	0.684	0.703
	0.684	0.665	0.662	0.669	0.672
	0.677	0.662	0.654	0.662	0.672
	0.684	0.669	0.662	0.665	0.672
	0.703	0.671	0.672	0.672	0.688
in eV					



Change the 3d charge on the impurity, keeping the system neutral,
do a self-consistent calculation
and calculate the change in the 3d energy level $\rightarrow U(3d)$.

$$U = \frac{\partial^2 E_{LDA}(n_d)}{\partial n_d^2}$$

$$U' \sim 0.5\text{eV}, J \sim 0.5\text{eV}$$

$$\hat{H}_0 = \sum_{ijmm'\sigma} t_{ijmm'} c_{im\sigma}^\dagger c_{jm'\sigma} + h.c$$

$$\hat{H}_U \equiv U \sum_{im} n_{im\uparrow} n_{im\downarrow} + \sum_{i,m < m', \sigma} [U' n_{im\sigma} n_{im'-\sigma} + (U' - J) n_{im\sigma} n_{im'\sigma}]$$

$$\hat{H}_J \equiv J \sum_{i,m \neq m'} (c_{im\uparrow}^\dagger c_{im'\downarrow}^\dagger c_{im\downarrow} c_{im'\uparrow} + c_{im\uparrow}^\dagger c_{im\downarrow}^\dagger c_{im'\downarrow} c_{im'\uparrow})$$

Green's function:

$$G(k) = \frac{1}{i\omega_n + \mu - \epsilon^0(\mathbf{k})}$$

dispersion:

$$\epsilon_{\mu\nu}^0(\mathbf{k}) = \sum_{\mathbf{r}_i - \mathbf{r}_j} t_{ij}^{\mu\nu} e^{i(\mathbf{r}_i - \mathbf{r}_j) \cdot \mathbf{k}}$$

irreducible susceptibility: $\hat{\chi}_{l_1 l_2, l_3 l_4}^0(q) = -\frac{T}{N} \sum_k G_{l_1 l_3}(k+q) G_{l_4 l_2}(k)$

spin susceptibility:

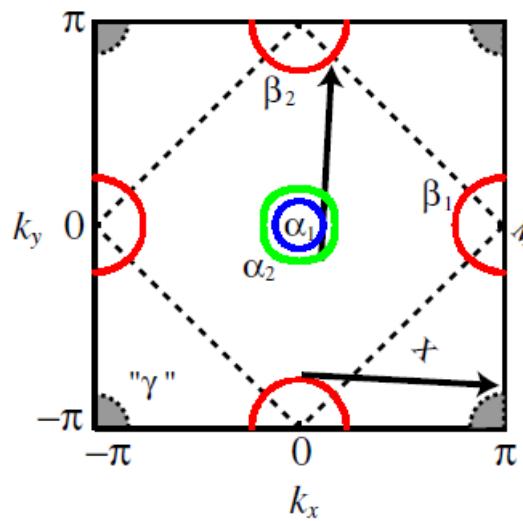
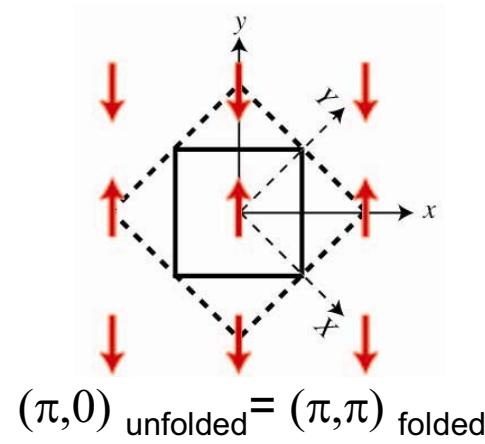
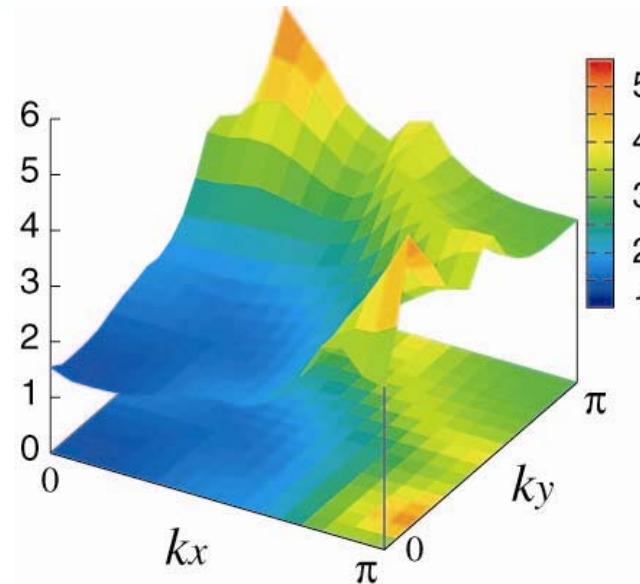
$$\hat{\chi}^s(q) = \frac{\hat{\chi}^0(q)}{1 - \hat{S}^0 \hat{\chi}^0(q)}$$

charge (orbital) susceptibility:

$$\hat{\chi}^c(q) = \frac{\hat{\chi}^0(q)}{1 + \hat{C}^0 \hat{\chi}^0(q)}$$

RPA result: spin susceptibility

$n=6.1$ (10% dope)



effective interaction for singlet:

$$\hat{V}^s(q) = \frac{3}{2}\hat{S}^0\hat{\chi}^s(q)\hat{S}^0 - \frac{1}{2}\hat{C}^0\hat{\chi}^c(q)\hat{C}^0 + \frac{1}{2}(\hat{S}^0 + \hat{C}^0)$$

effective interaction for triplet:

$$\hat{V}^t(q) = -\frac{1}{2}\hat{S}^0\hat{\chi}^s(q)\hat{S}^0 - \frac{1}{2}\hat{C}^0\hat{\chi}^c(q)\hat{C}^0 + \frac{1}{2}(-\hat{S}^0 + \hat{C}^0)$$

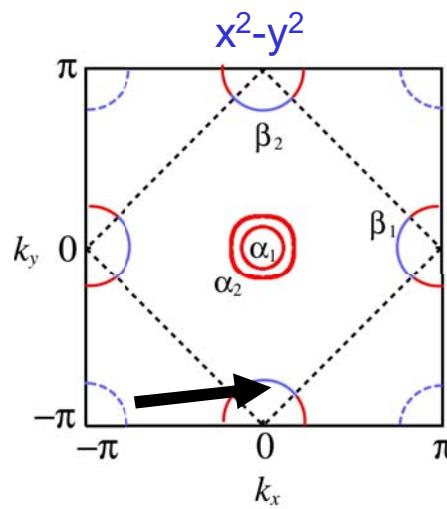
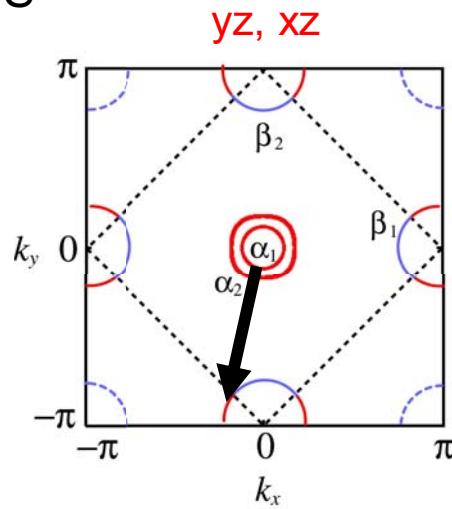
linearized Eliashberg eq. :

$$\lambda\Delta_{l_1l_4}(k) = -\frac{T}{N}\sum_q \sum_{l_2l_3l_5l_6} \hat{V}_{l_1l_2,l_3l_4}^{s(t)}(q)G_{l_2l_5}(k-q)\Delta_{l_5l_6}(k-q)G_{l_3l_6}(q-k)$$

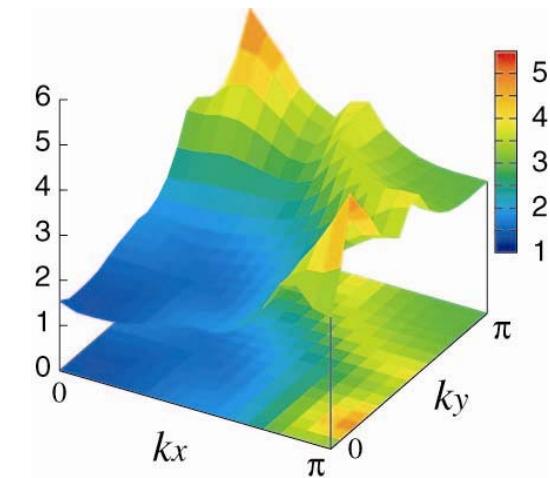
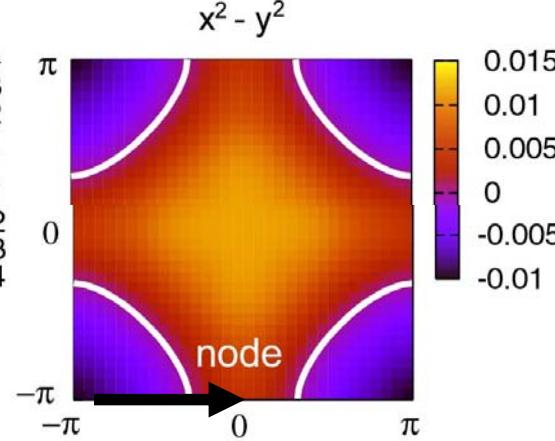
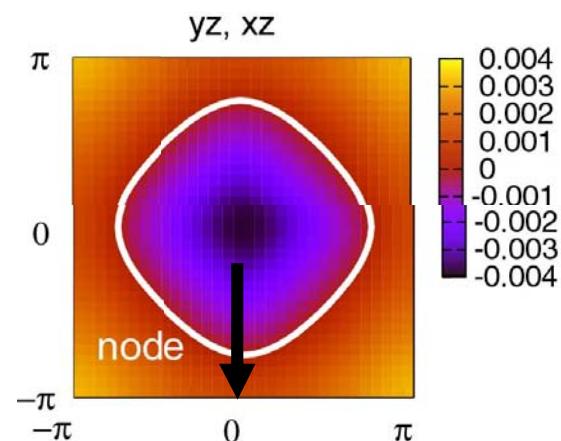
$T=T_c$ when $\lambda=1$

RPA result: gap function

FS



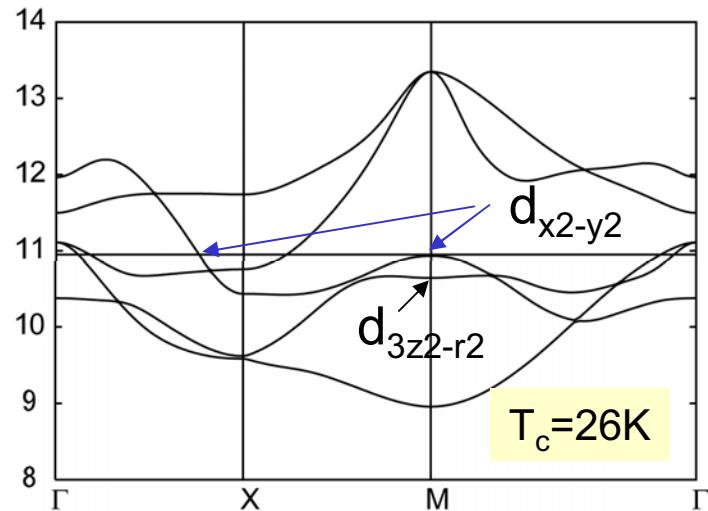
Δ_{ii}



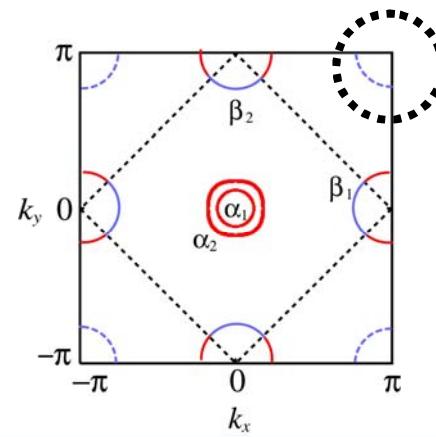
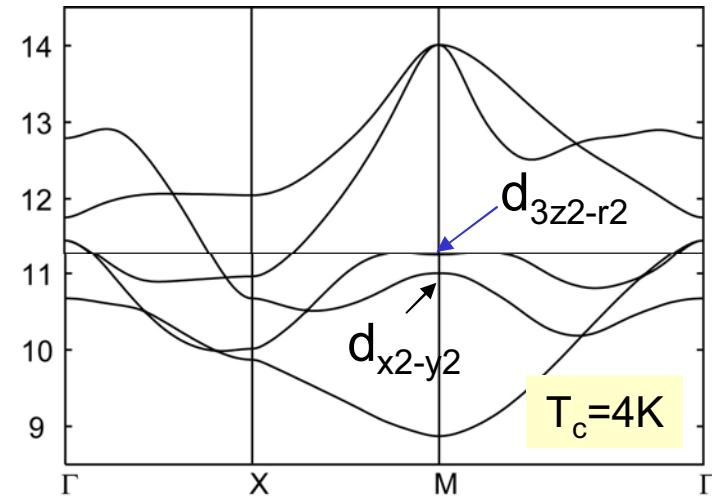
Kuroki, RA et al, arXiv:0803.3325
to appear in PRL

LaFeAsO vs LaFePO

LaFeAsO



LaFePO



Possibility of unconventional superconductivity

- ARPES e.g. H. Ding et al, EPL 83 47001 (2008)
- Andreev reflection e.g. Y.Y. Chen et al, Nature 453, 1224 (2008)
- Micro wave Penetration depth e.g. K. Hashimoto et al, arXiv:0806.3149

} Nodeless SC ?

Possibility of extended-s: e.g. Mazin et al., arXiv:0803.2740, Kuroki et al., arXiv:0803.3325, Korshunov et al., arXiv:0804.1793, Chubukov et al., arXiv:0807.3735, Parker et al., arXiv:0807.3729, Sknepnek et al., arXiv:0807.4566, Parish et al., arXiv:0807.4572

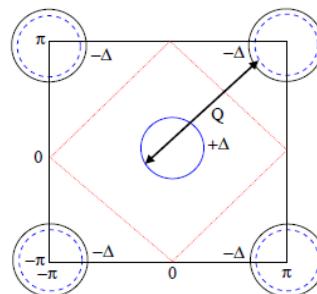
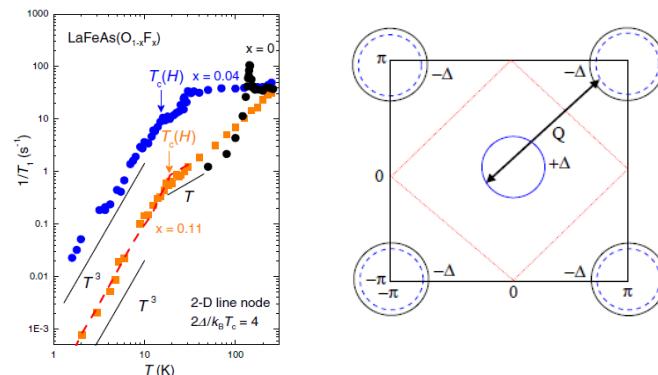
Possibility of S: Wang et al., arXiv:0807.0498

Nuclear Magnetic Resonance

- Absence of coherence peak
- $1/T_1 \sim T^3$

} nodes intersect FS?

Nakai et al, JPSJ 77 073701(2008)
Matano et al, arXiv:0806.0249
Grafe et al, PRL101 047003 (2008)



Chubukov et al.: arXiv:0807.3735
Parker et al.: arXiv:0807.3729
Parish et al.: arXiv:0807.4572

"sign change in Δ + unitary impurity scattering"

- Weak Co-doping effect on T_c Kawabata et al, arXiv:0807.3480

- ✚ Model construction based on ab-initio downfolding
 - Effective model seems to involve all five 3d orbitals
 - moderately correlated ($U/W \sim 1/2$)

- ✚ Possibility of extended-s SC
 - $d_{x^2-y^2}$, d_{yz} , d_{xz} orbital must be considered