



**The Abdus Salam
International Centre for Theoretical Physics**



1968-55

Conference on Teleconnections in the Atmosphere and Oceans

17 - 20 November 2008

On the skewness of the annular mode.

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Skewness of the extra-tropical winter circulation: role of the Arctic Oscillation and sensitivity to greenhouse warming



Frank Selten and Ruben Pasmanter
KNMI Netherlands



Not all things are normal

What is skewness ?



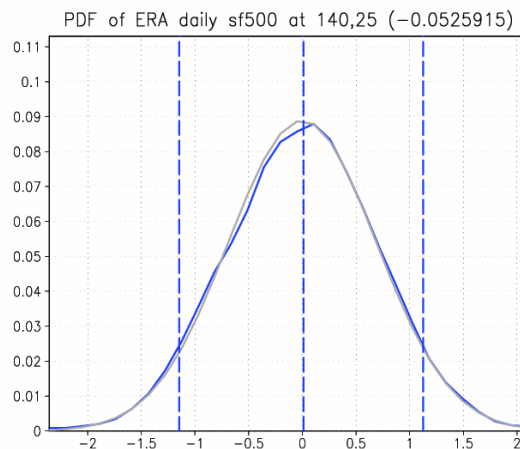
Skewness is a measure of the asymmetry of a distribution

$$\text{Skewness} = \langle (x - \langle x \rangle)^3 \rangle^{1/3} / \text{sd} \quad \text{with} \quad \text{sd} = \langle (x - \langle x \rangle)^2 \rangle^{1/2}$$

Often climate variables are symmetrically distributed

- normal PDF
- PDF at 140E-25N
- 5-50-95 percentiles

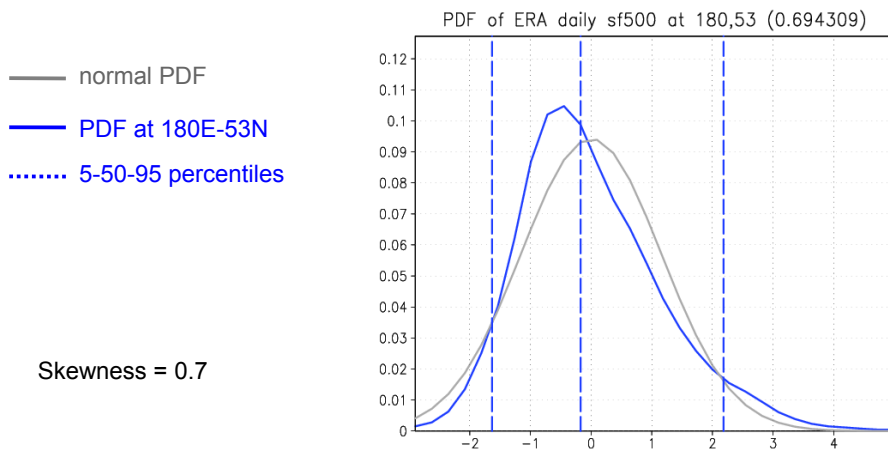
Skewness = 0.



Positive skewness



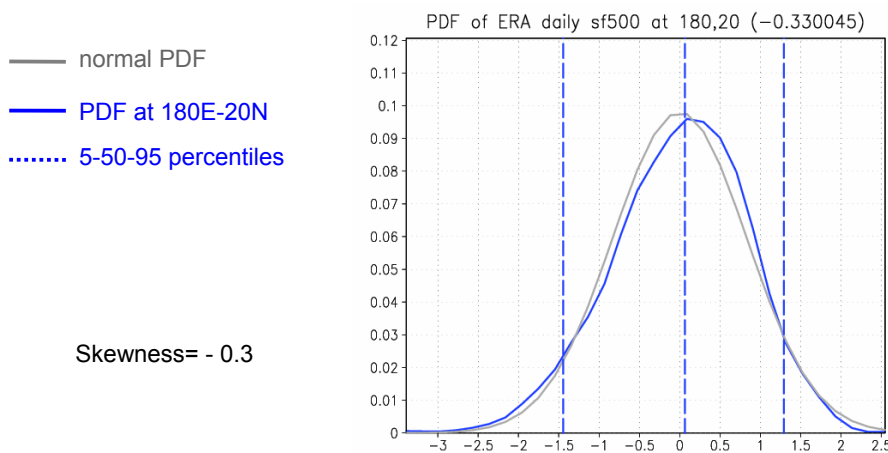
Sometimes large positive anomalies occur more often
The distribution in that case has positive skewness



Negative skewness



Sometimes large negative anomalies occur more often
The distribution in that case has negative skewness
For example: daily DJF 500 hPa streamfunction anomalies



Why study skewness ?

- Interesting in itself
- Is sensitive to the extreme values
- Indication of non-linearity: sign of the anomaly matters
- Teleconnection studies neglect skewness as it is based on linear correlations
- Might find non-trivial response to a forcing
- ...

Quasi-geostrophic atmosphere

Franco Molteni model

$$(1) \quad \frac{\partial q}{\partial t} = -J(\Psi, q) - D(\Psi) + S$$

3 levels, 200, 500 and 800 hPa

Spectral model on sphere, truncated at T21 (1470 variables)

Damping D : Ekman and hyper-viscosity, Newtonian cooling

Forcing S calculated from NH winter daily analyses:

$$(2) \quad \bar{S} = \overline{J(q_{obs}, \Psi_{obs})} + D(\overline{\Psi_{obs}})$$

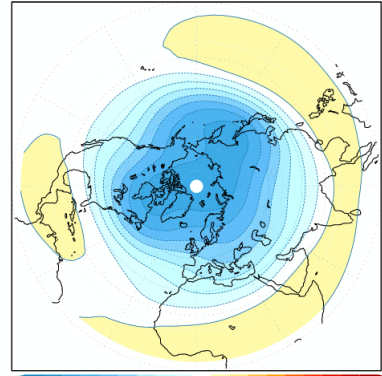
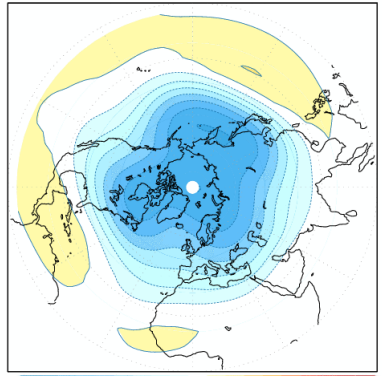
DJF streamfunction at 500 hPa

T21QG

ERA

sf 500 hPa mean T21qgS0 (*1e7)

sf 500 hPa mean ERA (*1e7)



mean

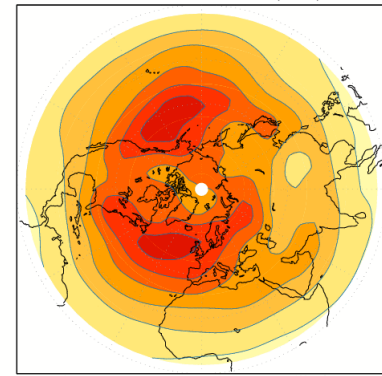
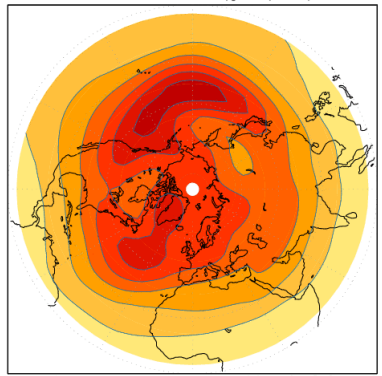
DJF streamfunction at 500 hPa

T21QG

ERA

sf 500 hPa sd T21qgS0 (*2e6)

sf 500 hPa sd ano ERA (*2e6)



standard deviation of 1-90 days time scales

PDF of 1st EOF at 500 hPa in T21qg: sensitive to ΔS

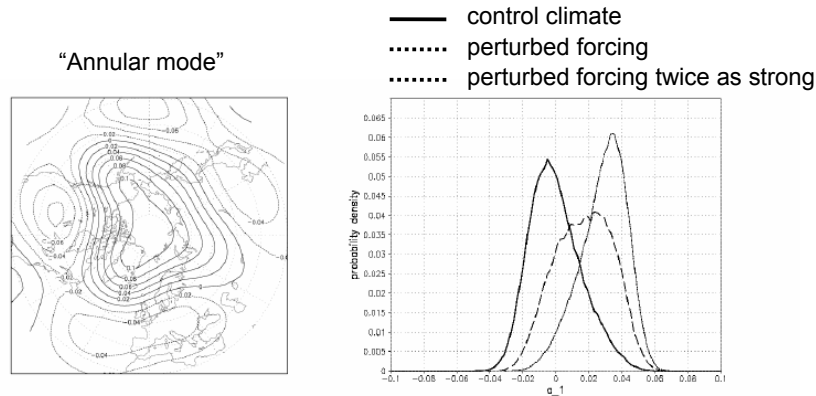


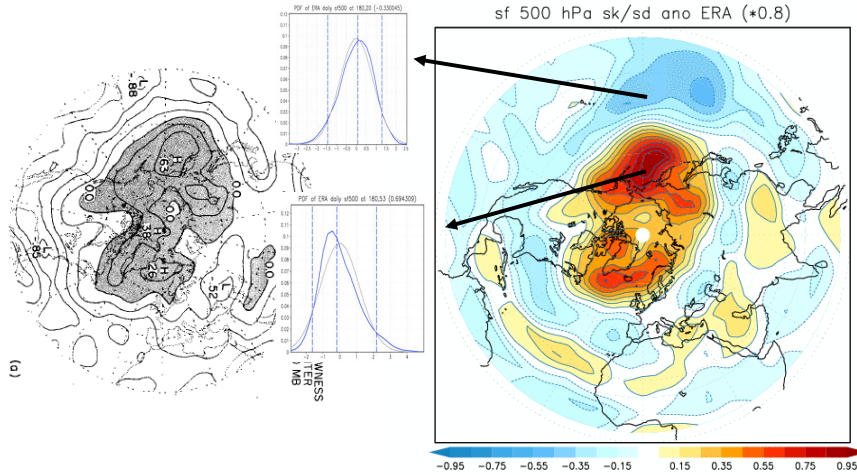
Figure 1: (Left) Dominant EOF of daily streamfunction variations of T21QG. (Right) Probability Density Function of this EOF for the unperturbed forcing case (solid), with 5% perturbation of the forcing with a spatial pattern of this EOF (dashed) and the same forcing perturbation but twice the amplitude (dotted).

Research questions



- What causes the skewness ?
- What makes the skewness change sign ?
- Why is the EOF with the largest skewness the most sensitive ?
- Do these results carry over to more realistic models ?
- Does greenhouse forcing change the skewness ?
- What about skewness in nature ?
- Is it sensitive to external perturbations ?

DJF skewness of daily values



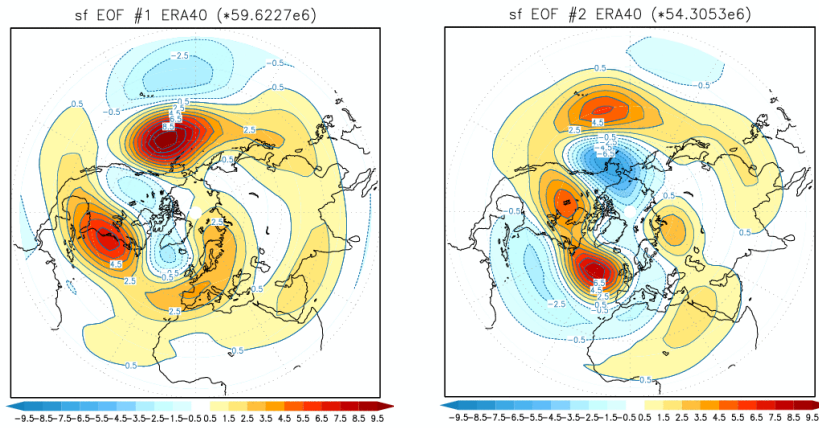
Geopotential height 500 hPa
White (1980) data from 1965-1976

Streamfunction 500 hPa ERA40
Data from 1958-2001: 3960 maps

Which patterns contribute to the local skewness ?

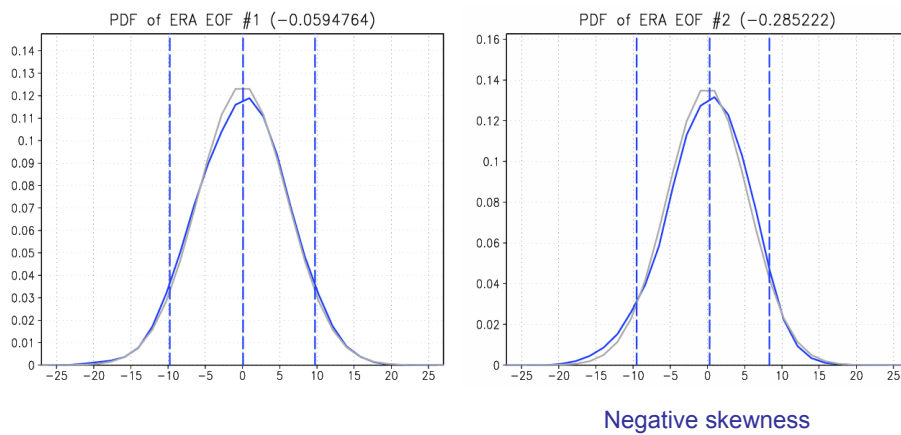


First EOFs 500 hPa DJF streamfunction



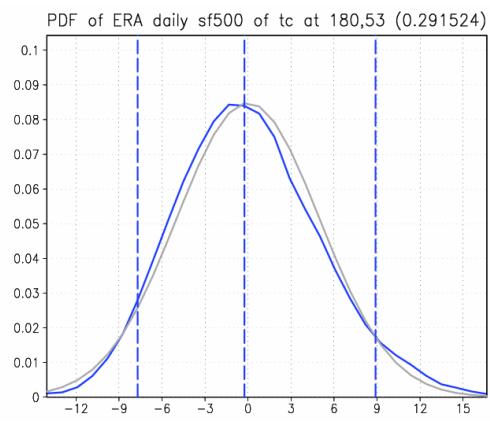
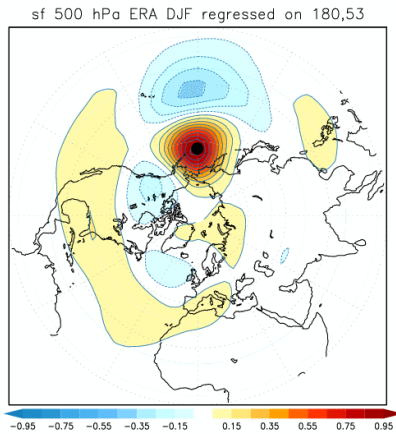
Mixture between PNA and (N)AO

PDF of ERA EOFs

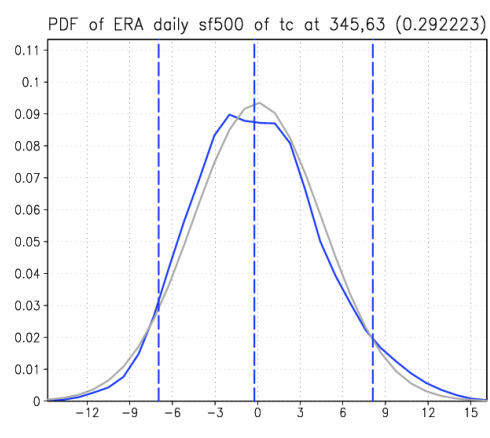
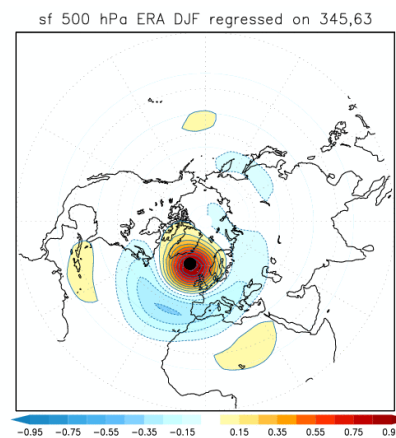


Negative skewness

Teleconnection maps in maximum skewness locations

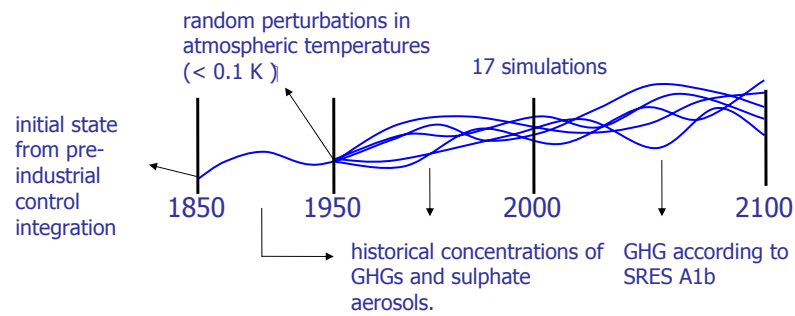


Teleconnection maps in maximum skewness locations



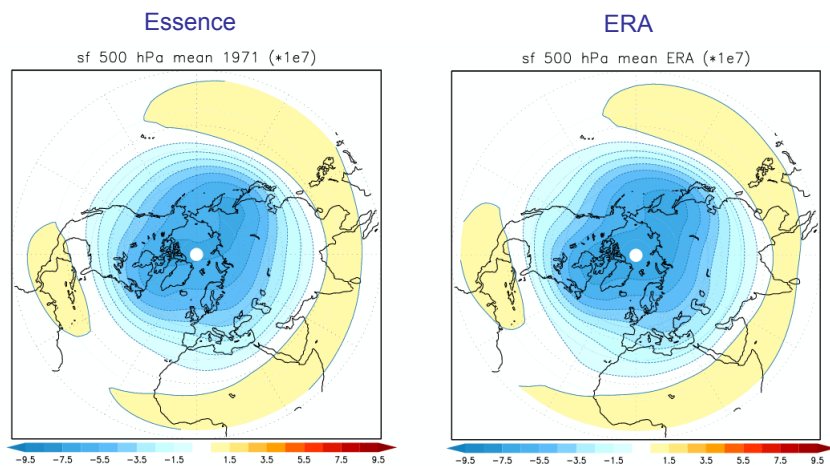
Evaluate AO and skewness in Essence

"ESSENCE project: a 17 member ensemble of climate SRES A1b scenario simulations from perturbed initial conditions using the ECHAM5-MPI-OM model"



<http://www.knmi.nl/~sterl/Essence>

DJF streamfunction at 500 hPa

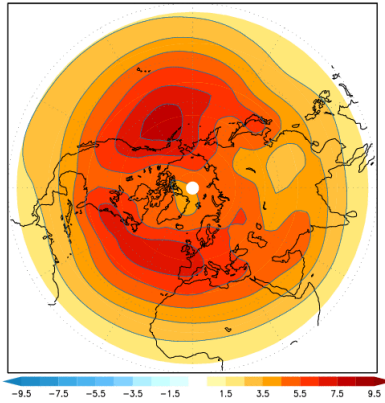


mean

DJF streamfunction at 500 hPa

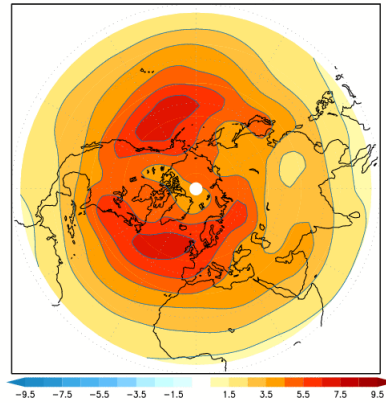
Essence

sf 500 hPa sd ano 1971 (*2e6)



ERA

sf 500 hPa sd ano ERA (*2e6)

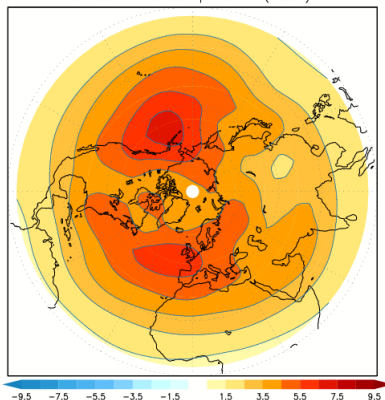


standard deviation of 1-90 days time scales

DJF streamfunction at 500 hPa

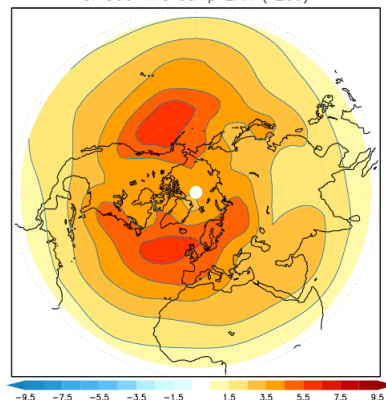
Essence

sf 500 hPa sd lp 1971 (*2e6)



ERA

sf 500 hPa sd lp ERA (*2e6)

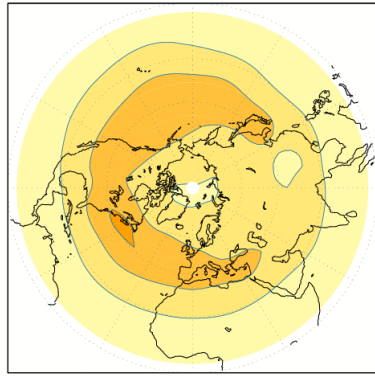


standard deviation of 5-90 days time scales

DJF streamfunction at 500 hPa

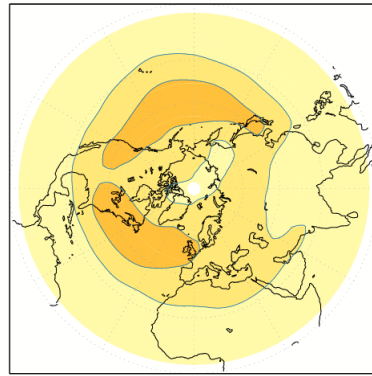
Essence

sf 500 hPa sd hp 1971 (*2e6)



ERA

sf 500 hPa sd hp ERA (*2e6)

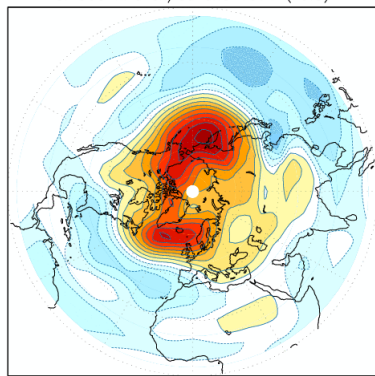


standard deviation of 1-5 days time scales

DJF streamfunction at 500 hPa

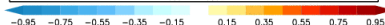
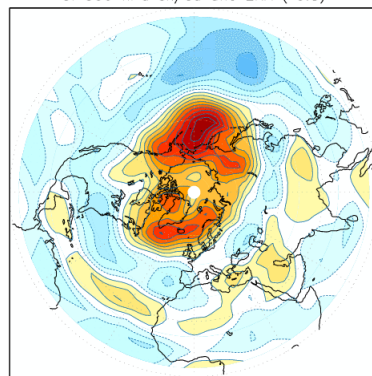
Essence

sf 500 hPa sk/sd ano 1971 (*0.8)



ERA

sf 500 hPa sk/sd ano ERA (*0.8)

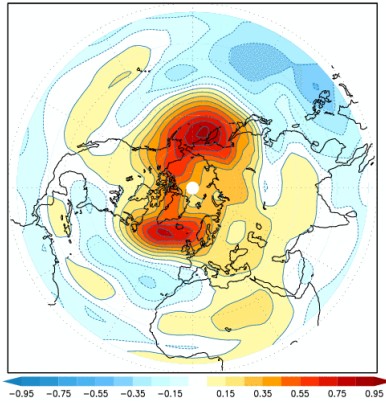


Skewness of 1-90 day timescales normalised to one sd

DJF streamfunction at 500 hPa

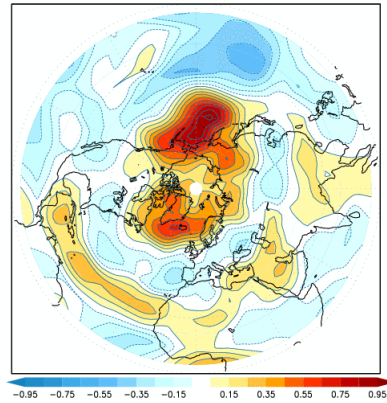
Essence

sf 500 hPa sk/sd lp 1971 (+0.8)



ERA

sf 500 hPa sk/sd lp ERA (+0.8)

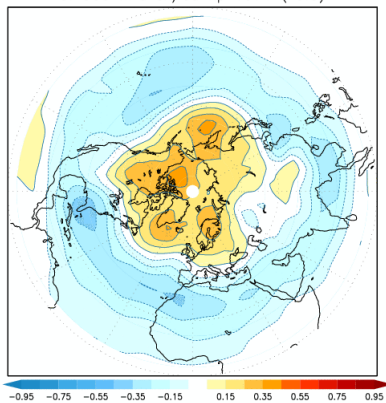


Skewness of 5-90 day timescales normalised to one sd

DJF streamfunction at 500 hPa

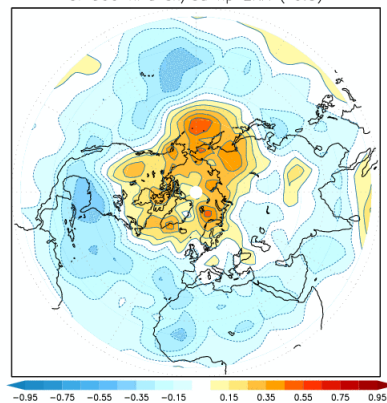
Essence

sf 500 hPa sk/sd hp 1971 (+0.8)



ERA

sf 500 hPa sk/sd hp ERA (+0.8)

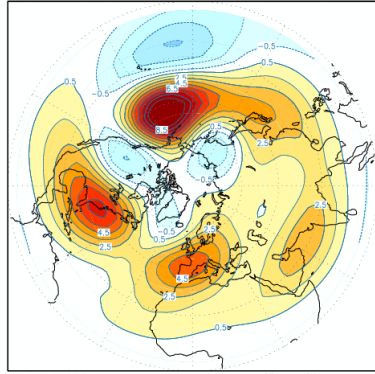


Skewness of 1-5 day timescales normalised to one sd

DJF streamfunction at 500 hPa

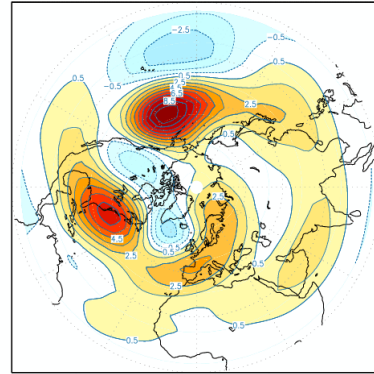
Essence

sf EOF #1 year 1971 ($\ast -67.9106e6$)



ERA

sf EOF #1 ERA40 ($\ast 59.6227e6$)

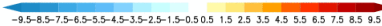
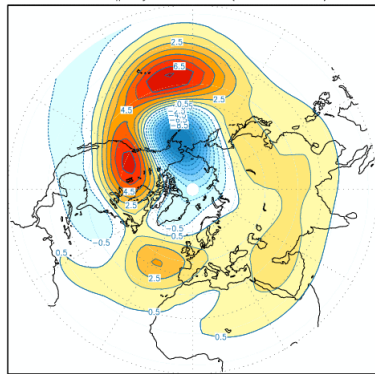


EOF #1

DJF streamfunction at 500 hPa

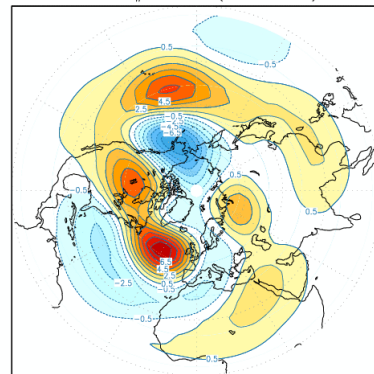
Essence

sf EOF #2 year 1971 ($\ast 63.9655e6$)



ERA

sf EOF #2 ERA40 ($\ast 54.3053e6$)

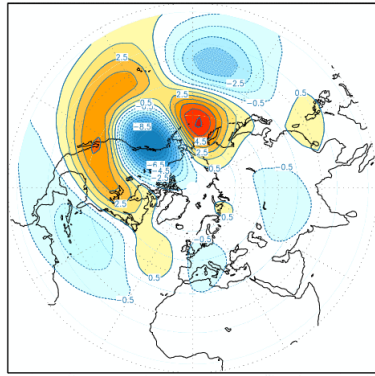


EOF #2

DJF streamfunction at 500 hPa

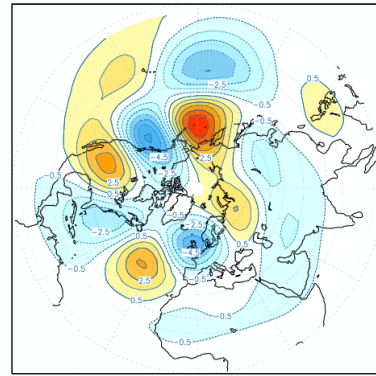
Essence

sf EOF #3 year 1971 (*55.411e6)



ERA

sf EOF #5 ERA40 (*45.7581e6)

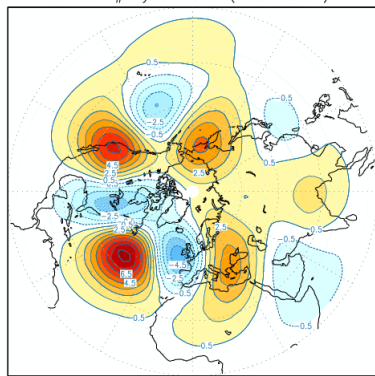


EOF #3

DJF streamfunction at 500 hPa

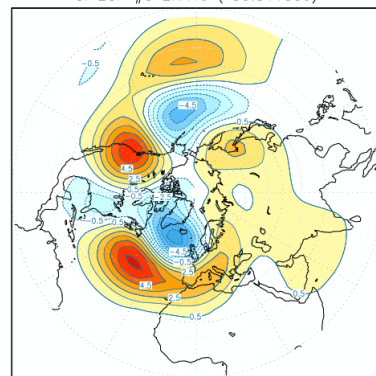
Essence

sf EOF #4 year 1971 (*52.8729e6)



ERA

sf EOF #3 ERA40 (*50.5115e6)

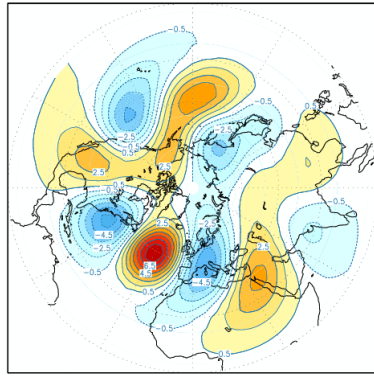


EOF #4

DJF streamfunction at 500 hPa

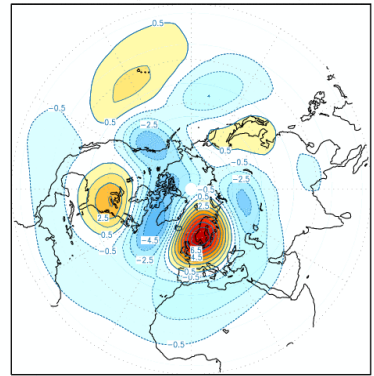
Essence

sf EOF #5 year 1971 ($+50.8631e6$)



ERA

sf EOF #4 ERA40 ($+47.277e6$)

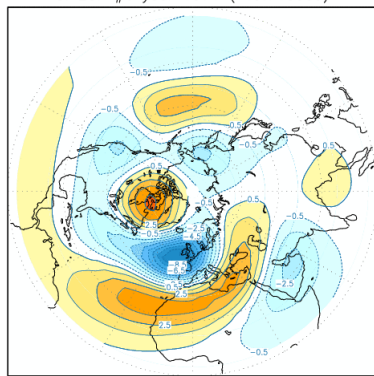


EOF #5

DJF streamfunction at 500 hPa

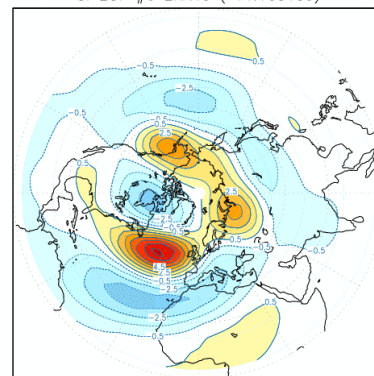
Essence

sf EOF #6 year 1971 ($+49.7153e6$)



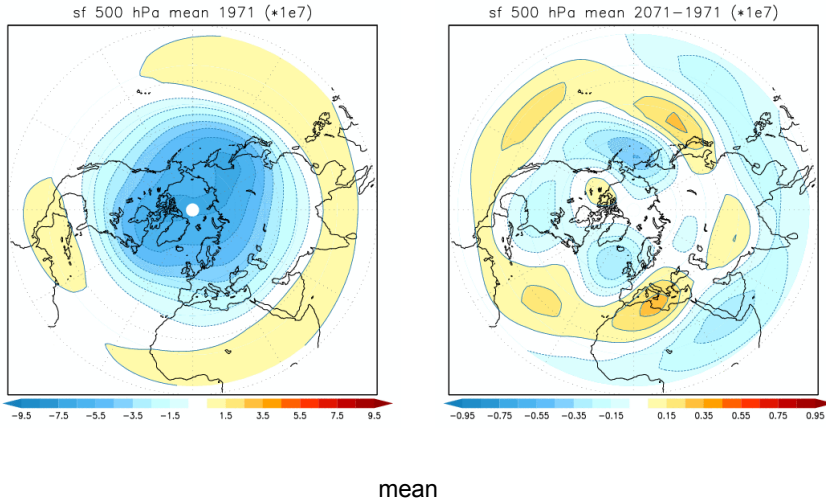
ERA

sf EOF #6 ERA40 ($+44.1601e6$)

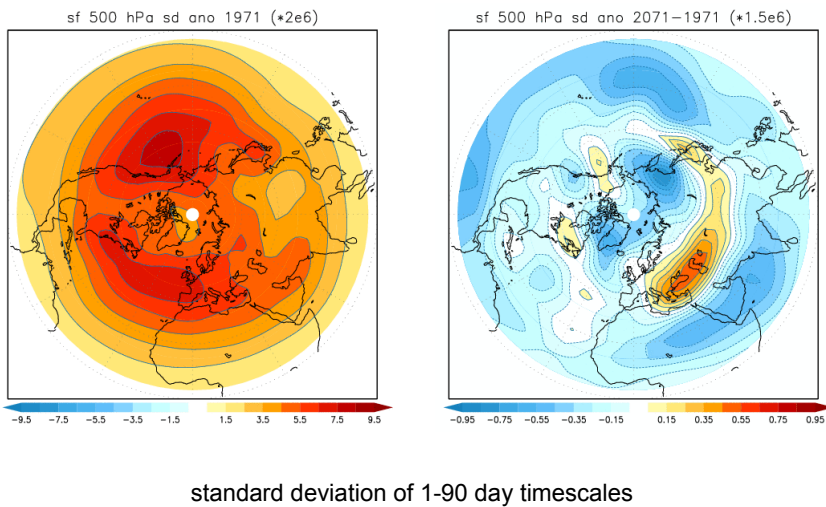


EOF #6

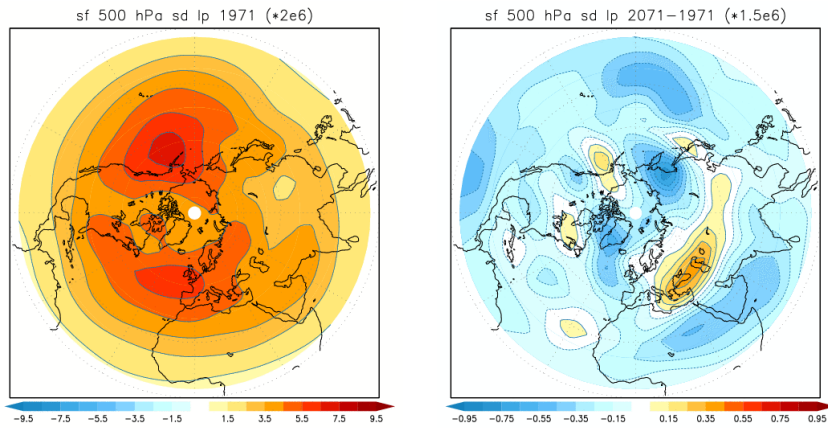
Essence DJF streamfunction 500 hPa climate change



Essence DJF streamfunction 500 hPa climate change

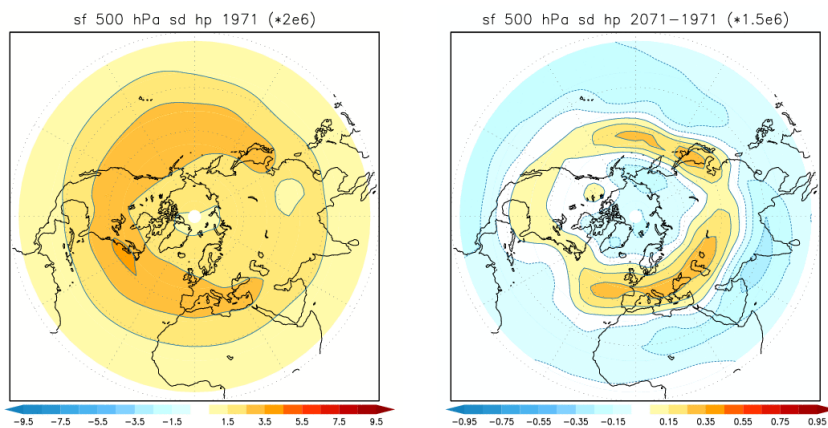


Essence DJF streamfunction 500 hPa climate change



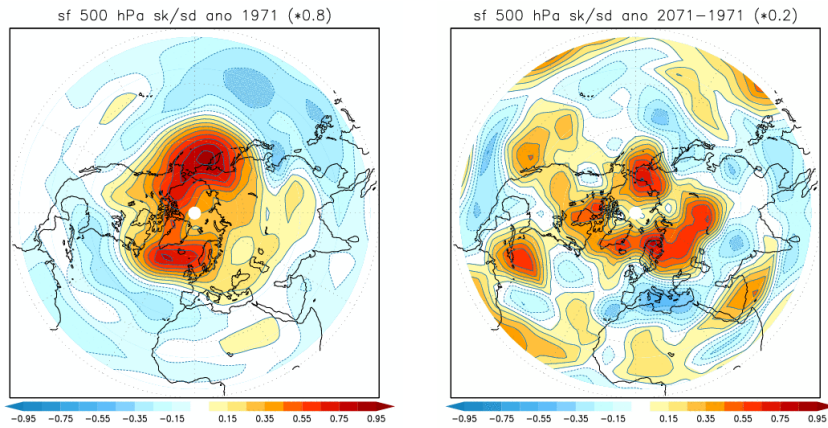
standard deviation of 5-90 day timescales

Essence DJF streamfunction 500 hPa climate change



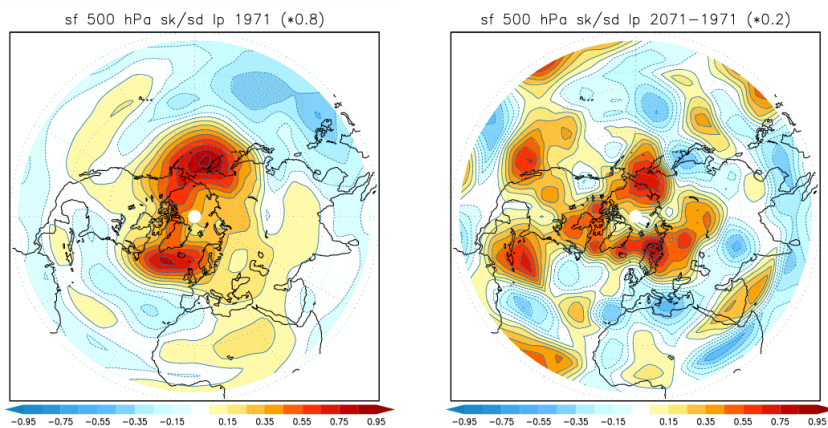
standard deviation of 1-5 day timescales

Essence DJF streamfunction 500 hPa climate change



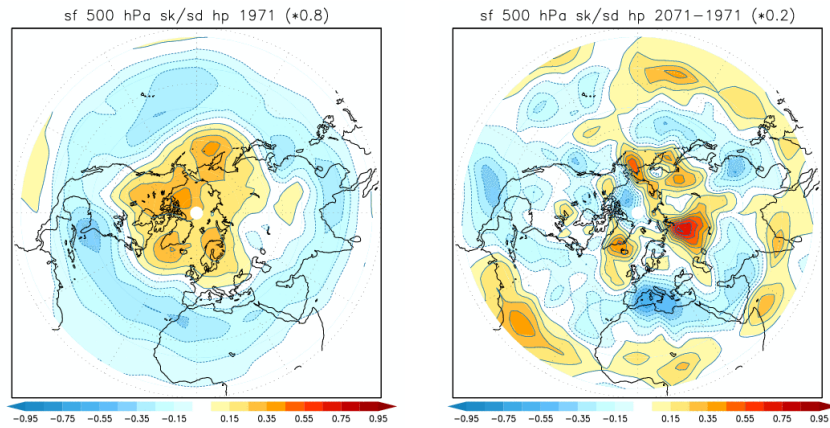
Skewness of 1-90 day timescales normalised to one sd

Essence DJF streamfunction 500 hPa climate change



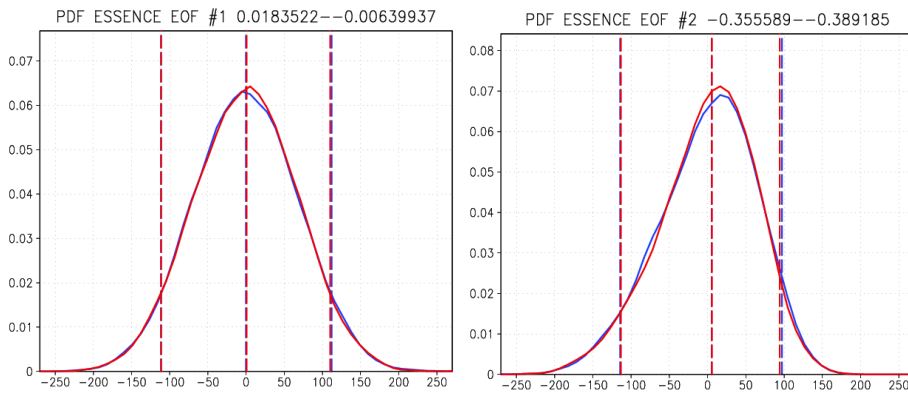
Skewness of 5-90 day timescales normalised to one sd

Essence DJF streamfunction 500 hPa climate change



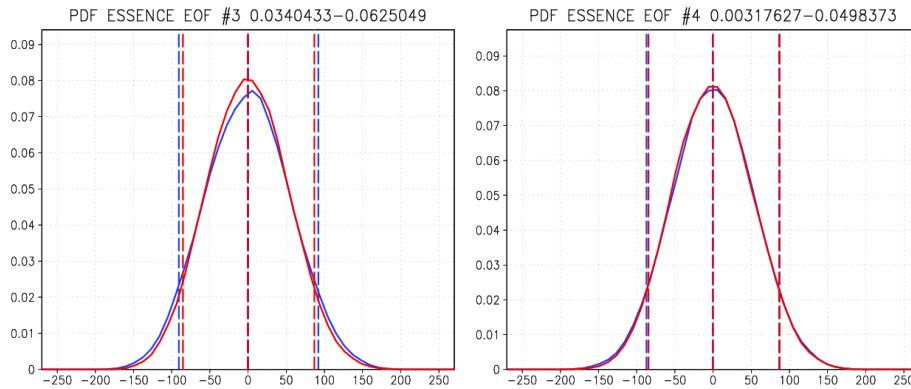
Skewness of 1-5 day timescales normalised to one sd

Essence DJF daily streamfunction 500 hPa EOF PDFs 1971-2071



Hardly any change in the PDF of the first two EOFs

Essence DJF daily streamfunction 500 hPa EOF PDFs 1971-2071



Use T21QG as a tool to understand climate change in Essence



Check that T21QG can reproduce ESSENCE skewness

Check that T21QG can reproduce ESSENCE skewness climate change

Decomposition of S in different terms

$$(1) \quad \frac{\partial q}{\partial t} = -J(\Psi, q) - D(\Psi) + S$$

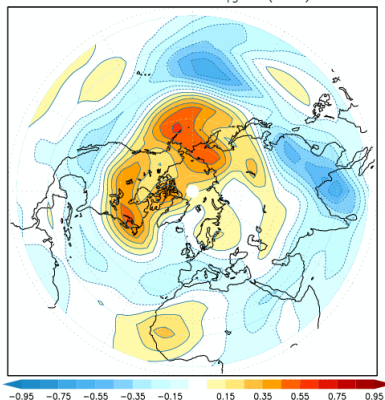
S(t) =

$$S_o + S_{\text{day}}(t) + S_{\text{year}}(t) + (t-t_0)\Delta S_{\text{trend}} + S_{\text{enso}}(t) + R(t)$$

DJF streamfunction at 500 hPa

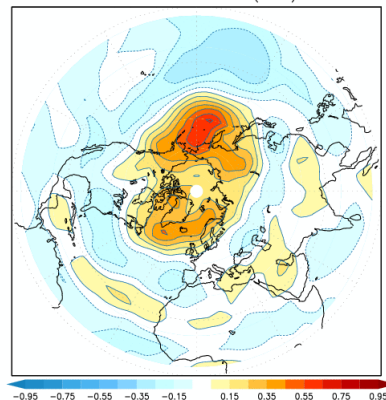
T21QG

sf 500 hPa sk T21qgS0 (+0.8)



ERA

sf 500 hPa sk ERA (+0.8)



skewness

Summary



- Extra-tropical circulation is skewed
- Idealised QG simulations indicate that the skewness in the AO might be sensitive to small forcings
- ESSENCE simulates nature in DJF NH quite well; similar EOFs and skewness
- ESSENCE indicates 20 % change in future skewness
- Skewness is not concentrated in dominant EOFs
- More work needed to identify patterns that produce the skewness in ESSENCE and nature