



*The Abdus Salam  
International Centre for Theoretical Physics*



**1970-12**

## **Signaling the Arrival of the LHC Era**

*8 - 13 December 2008*

## **Beyond the Standard Model at the LHC - III**

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## Examples of non-SUSY signatures

Giacomo Polesello

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## Early discovery

Conditions for new physics to be visible in first LHC year (max  $1 \text{ fb}^{-1}$ )

- «Cross-section  $O(100 \text{ fb})$  for leptonic signatures
- «Small SM backgrounds
- «Clear kinematic signature (peak, edge). No need for counting experiment
- «Signature visible also with not completely understood detector

Examples of well studied and well motivated candidates:

- «Multi-lepton+jets+ $\cancel{E}_T$  SUSY signals with correlated-flavour edge, already considered in previous lectures
- «High mass resonances decaying into two leptons, appearing in many BSM extensions, including Little Higgs, Extra Dimensional models, TechniColour
- «Mini Black Holes in theories with extra-dimensions, events with large cross-sections and particle multiplicities in final state

Typically very clear signatures, but probing 'extreme cases' of requirements on detector performance:

«Lepton performance for in region of high  $p_T$  ( $>500$  GeV):

- Very far from the 50-100 GeV region where detector calibration optimised
- Difficult to find appropriate control samples in data

«Reconstruction of events in environment with very high particles multiplicities and very high energy deposit in the calorimeters

For reliable answers need careful simulation work including detector geometry as-installed, material distortions and residual miscalibration/misalignment effects

# Phenomenology of high mass lepton resonances

Resonances in lepton-lepton invariant mass distribution happens through  $s$ -channel exchange of new particles coupling both to partons and to leptons

## «Gauge boson resonances

– Extended Gauge groups. Examples:

$\leq$ SSM: gauge boson with same coupling as SM  $Z$ . No theoretical motivation, useful benchmark

$\leq E_6$  models: effective  $SU(2)_L \leq U(1)_Y \leq U(1)'$  from breaking of  $E_6$  group

$$\leq E_6 \rightarrow SU(3)_C \leq SU(2)_L \leq U(1)_Y \leq U(1)_\eta \leq U(1)_\eta$$

$\leq$ Lightest  $Z'$ :  $Z' = \cos \eta_{E6} Z'_\eta \leq \sin \eta_{E6} Z'_\eta$ .  $\eta_{E6}$  value defines models:  $Z_\eta, Z_\eta, Z_\eta$

$\leq$ L-R symmetric models:

$$\leq SO(10) \rightarrow SU(3)_C \leq SU(2)_L \leq SU(2)_R \leq U(1). \text{ Model parameter: } \eta = g_R/g_L$$

$\leq$ Little Higgs models

– Kaluza-Klein excitations of  $\eta/Z$  in models with  $SU(2) \leq U(1)$  gauge groups in ED bulk

Couplings of  $\leq$  weak strength, with model-dependent scale factor

Natural width typically order a few % of resonance mass

Direct limits from Tevatron 850-950 GeV depending on model

Indirect limits from EW constraints 500-1800 GeV

For KK models with gauge interaction in bulk  $m(Z') \gtrsim 4$  TeV from EW fits

### «Graviton resonances:

Kaluza Klein (KK) excitations of graviton in models with warped space-time geometry

$\leq$  Coupling of gravitational force, but enhanced by warp factor

$\leq$  No bounds from EW constraints

$\leq$  Distinctive polar angle distribution of decay

Model-dependent limits ranging from several hundred GeV to 1 TeV

### «Technihadron resonances:

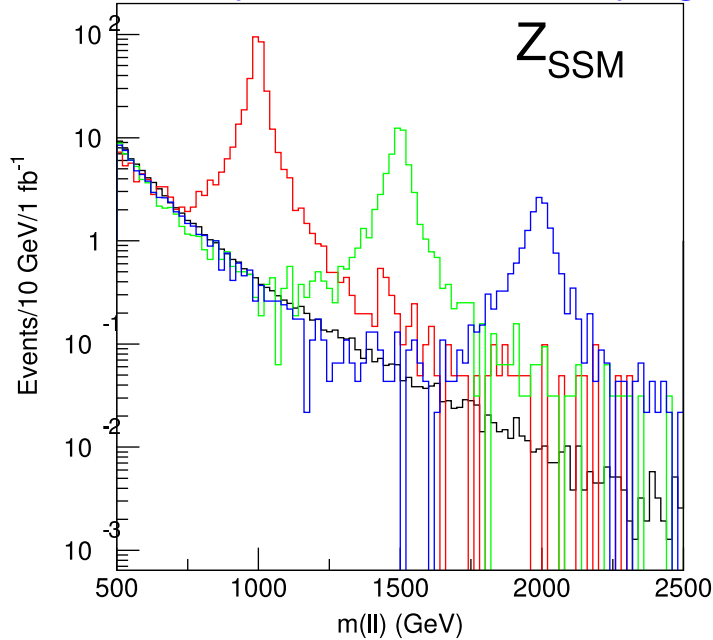
Technihadrons bound together by QCD-like forces are predicted by Technicolor theories. Significant

BR in fermion-antifermion pairs for vector technihadrons

For TechniColor Strawman Model, and a particular choice of parameters, CDF limits of 280 GeV

## $Z'$ at generator level

Consider "Sequential"  $Z'$ , same couplings as Standard Model



Drell-Yan background  $\leq 2$  orders of magnitude lower than signal in peak

Natural width  $\Delta: \Delta/M \leq 0.03$

$\leq$  Experimental Resolution for  $Z \rightarrow e^+e^- < 1\%$

$\leq$  independent of mass

$\leq$  Experimental Resolution for  $Z \rightarrow \eta^+\eta^- \leq 6 \leq 10\%$

for  $m(Z')$  between 1 and 3 TeV

Cross-section for the full  $\eta/Z/Z'$  system from  $m(\ell\ell) > 500$  GeV

Number of events calculated within  $\leq 2\Delta$  of peak value

Mass (GeV)	$\eta$ BR fb	Nev Sig Ev/fb	Nev DY Ev/fb
1000	492	275	2.5
1250	245	112	1.05
1500	157	50	0.5
1750	124	25	0.24
2000	109	13	0.12

## Example: ATLAS $Z' \rightarrow e^+e^-$ analysis

Recent analysis based on detailed detector simulation

Use  $Z_\eta$  model as benchmark, 3 masses 1, 2 and 3 TeV

For a 1 (3) TeV mass 86% (95%) of the events have 2 electrons within  $|\eta| < 2.5$ . Require:

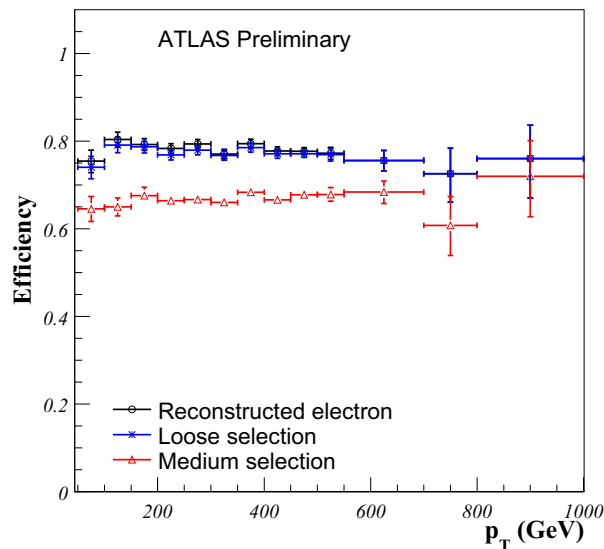
≤ The events pass the trigger requiring one electron with  $p_T > 60$  GeV

≤ Two clusters matched to a track

≤ Two reconstructed *loose* electrons, at least one with  $P_T > 65$  GeV, with opposite charge

Efficiency for signal is ≤ 42 (34)% for  $m = 1(3)$  TeV

Efficiency for electron reconstruction at high  $p_T$

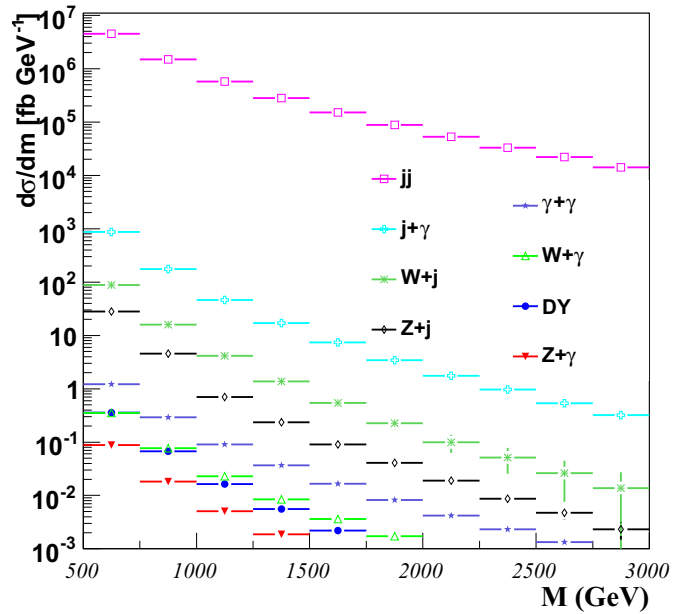


**Loose selection:** based on hadronic leakage and selection shape variables, excellent rejection against high energy pions and wide showers

**Medium selection:** exploit fine granularity of first EM compartment, and apply stricter cluster-track matching. Additional rejection against  $\eta^0 \rightarrow \eta\eta$



# Background studies



Irreducible background is Drell-Yan

Reducible backgrounds, where jet(s) or photon(s) fake an electron in the detector

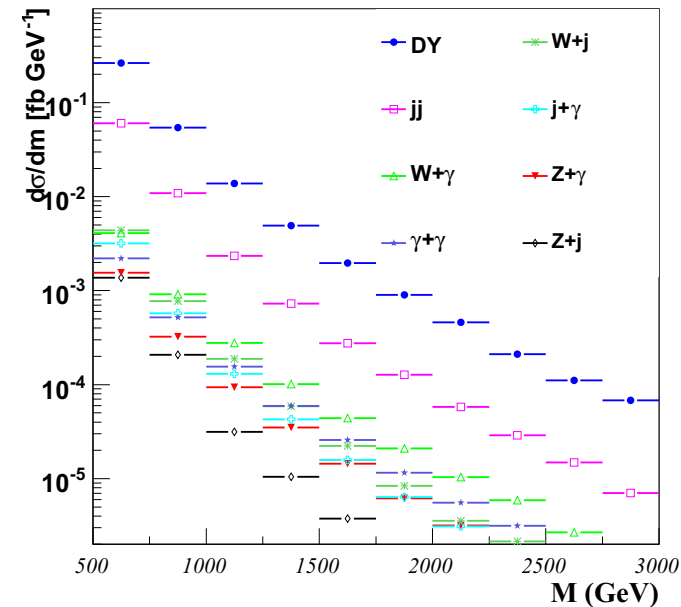
Overwhelming cross-section before identification and kinematic cuts

Apply to each leg rejection factor for applied loose e-id cuts:

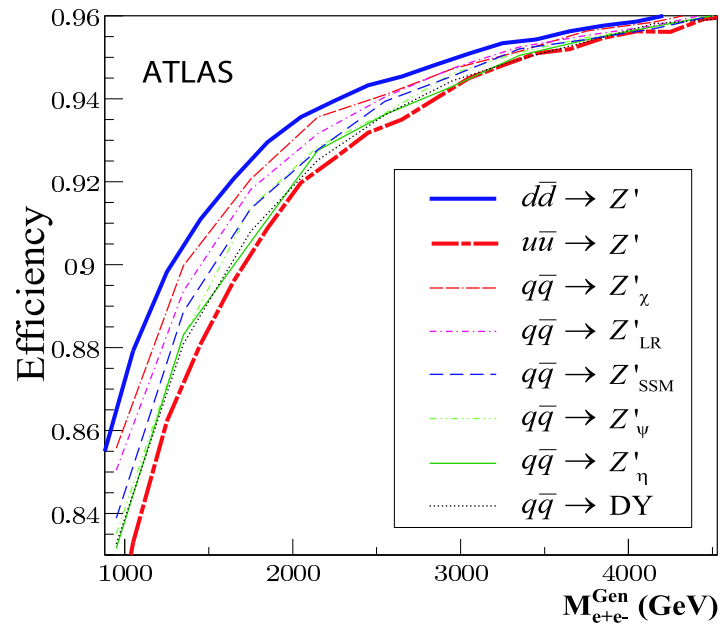
$$\leq R_{e-jet} = 4 \leq 10^3 \leq R_{e-\eta} = 10$$

And apply kinematic cuts

Total contribution less than 30% of irreducible DY



## Signal reach

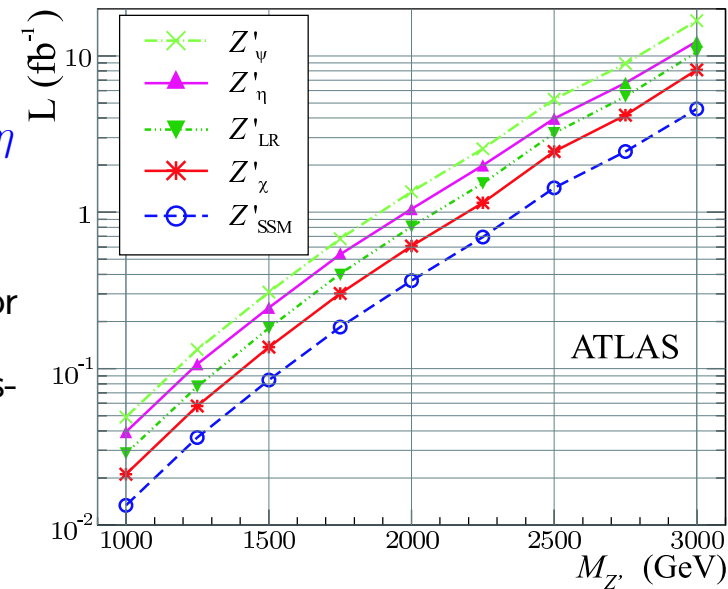


Plot for different models luminosity needed for  $5\sigma$  discovery

Only statistical error. Dominating systematic error from theoretical uncertainties on Drell-Yan cross-section: from  $\leq 8.5\%$  to  $\leq 14\%$ .

Different models have different couplings to  $u$  and  $d$  quarks

Different acceptances for kinematic cuts, to be taken into account in the evaluation of signal reach



## Width and leptonic cross-section

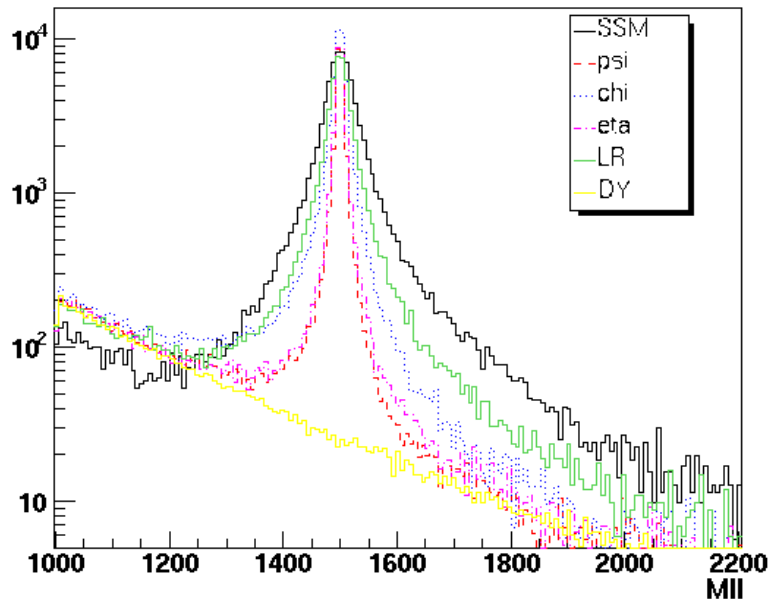
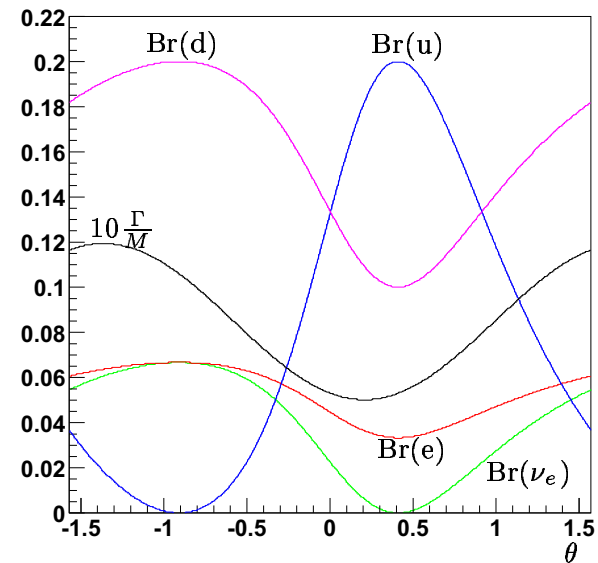
After discovery of peak, focus on variables allowing discrimination of models.

Consider partial decay widths and asymmetries

Partial decay widths

$$\Delta(Z' \rightarrow ff) = N_c \frac{g^2}{\cos^2 \eta_W} \frac{1}{48\eta} (g_V^2 + g_A^2) M$$

Width/branching ratio variations in  $E_6$  models, assuming no exotic decays



Resonance shape for different models (arbitrary normalisation)

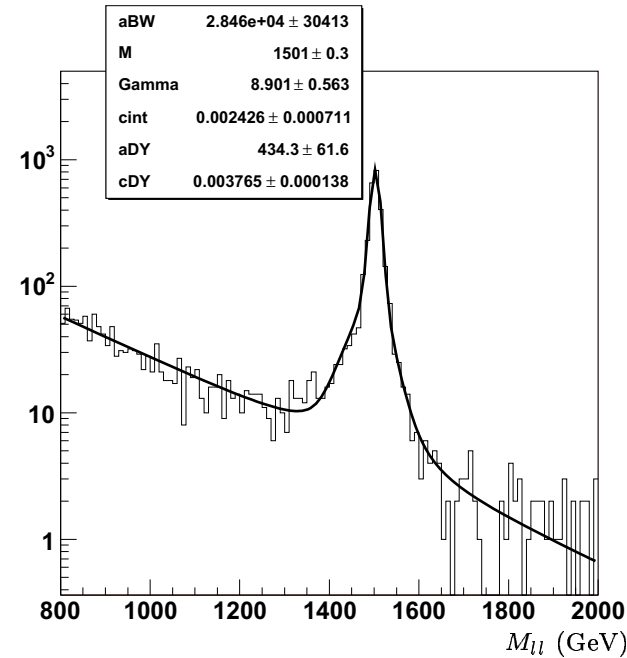
Measure  $\eta_{ee} \leq \Delta$  insensitive to possible decays into exotic particles

# Width and cross-section measurement

Natural width of  $Z'$  and  $\eta_{ll} \leq \Delta$

		$\Gamma/M$	$\eta_{ll} \times \Gamma(\text{fb} \times \text{GeV})$
$M = 1.5 \text{ TeV}$	SSM	0.030	3500
	$\eta$	0.005	180
	$\eta$	0.012	830
	$\eta$	0.006	220
	$LR$	0.020	1500

Natural width  $\geq$  experimental width ( $\leq 0.007$ ).



Breit-Wigner convoluted with exponential (PDF) and parametrisation of experimental resolution

Measure  $\eta_{ll} \leq \Delta$  with 5-10% statistical error with  $100 \text{ fb}^{-1}$  for  $M = 1.5 \text{ TeV}$

Normalize to  $Z$  peak. Results will be dominated by systematic uncertainties. e.g.:

$\leq$  Knowledge of detector resolution

$\leq$  Acceptance estimate (model dependent)

$\leq$  DY shape: PDF's, lepton linearity, higher order corrections

## TeV $\ll$ Extra Dimensions

Standard ADD model:

EW precision measurement test SM gauge fields to distances  $\ll 1/\text{TeV} \Rightarrow$  SM fields can not propagate in "Large" ED and are localized on a brane

Variation on the model: "asymmetric" models where different ED have different compactification radii. Two types of ED:

- $\ll$  "large" ED where only gravity propagates

- $\ll$  "small" ( $R \ll 1/\text{TeV}$ ) extra dimensions where both gravity and SM fields propagate

This scheme could be pictured as a "thick" brane in side which SM fields propagate, immersed in the usual "large" ADD bulk

Various models, depending on which SM fields propagate in the bulk:

- $\ll$  Only gauge fields: describe it today

- $\ll$  Both fermion and gauge fields (UED)

General signature for models with compactified ED: regularly spaced Kaluza Klein excitations of fields propagating in the bulk

KK mass spectra and couplings given by compactification scheme and number of ED

In case of one "small" ED with radius  $R_c \ll 1/M_c$ :

«Excitations equally spaced with masses:

$$M_n^2 = M_0^2 + n^2 M_c^2$$

«Couplings equal to  $\sqrt{2}$  gauge couplings

Minimum excitation mass compatible with EW precision measurement: 4 TeV

Consider excitations for all SM bosons:

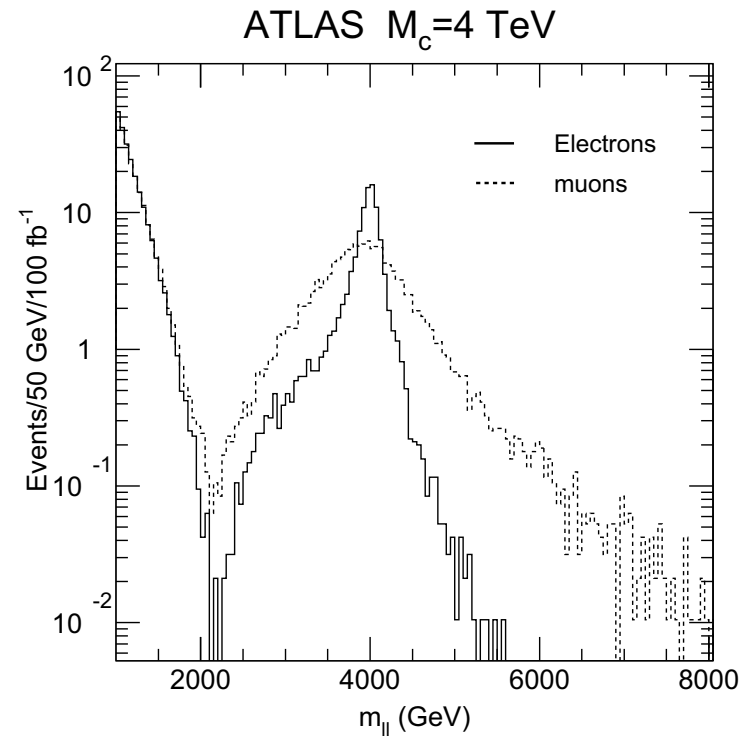
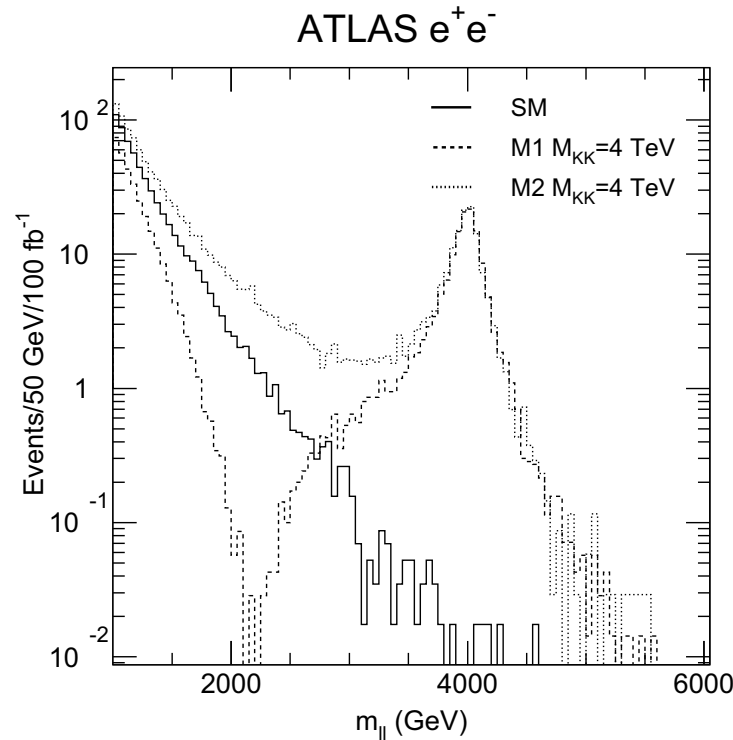
« $Z/\eta$ , discovery channel: decay into  $\ell^+ \ell^-$

« $W$ , discovery channel: decay into  $\ell \eta$

Old exploratory work in parametrized simulation

Minimum excitation mass considered: 4 TeV: natural width

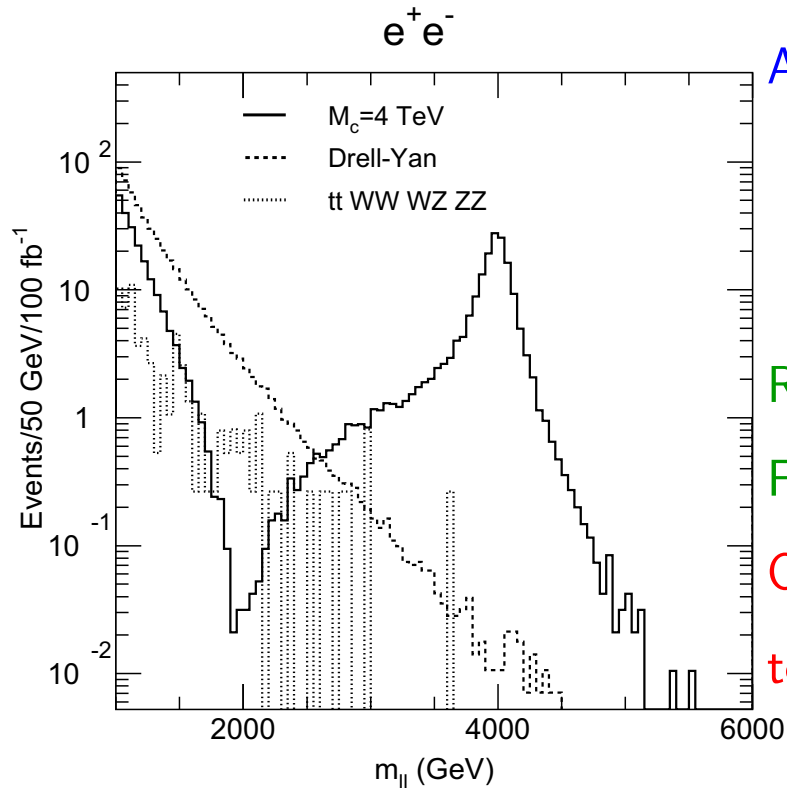
$$\ll 2 \ll \Lambda(W) \ll (M_c/100) \text{ GeV} \ll 200 \text{ GeV}$$



Natural width dominates for  $e^+e^\times$ . Detailed knowledge of electron resolution not needed as long as  $\eta(E)/E$  better better than 2-3%.

Experimental width dominates for  $\eta^+\eta^\times \Rightarrow$  use muons only for discovery, not for measurements

## Data analysis: $Z/\gamma$



### Analysis requirements:

$\leq$  Two leptons with  $P_t > 20$  GeV in  $|\eta| < 2.5$

$\leq m_{\ell\ell} > 1$  TeV

Reducible backgrounds:  $t\bar{t}$ ,  $WW$ ,  $WZ$ ,  $ZZ$

For  $m(e^+e^-) > 1000$  GeV  $\ll$  60 background events

Observe characteristic depletion w.r.t Drell-Yan due to interference effects

Resonance includes excitation of both  $\eta$  and  $Z$ , two resonances can not be resolved

Evaluate number of events in peak as a function of mass of first excitation ( $M_{kk}$ )

Require:  $S/\sqrt{B} > 5$  and  $> 10$  events in peak, summed over two lepton flavours

Reach for  $100 \text{ fb}^{\times 1}$ :  $\ll 5.8$  TeV - Only statistical

In no case second KK peak observable



## Data analysis: $W$

### Analysis requirements:

$\leq$  One lepton with  $P_t > 200$  GeV in  $|\eta| < 2.5$

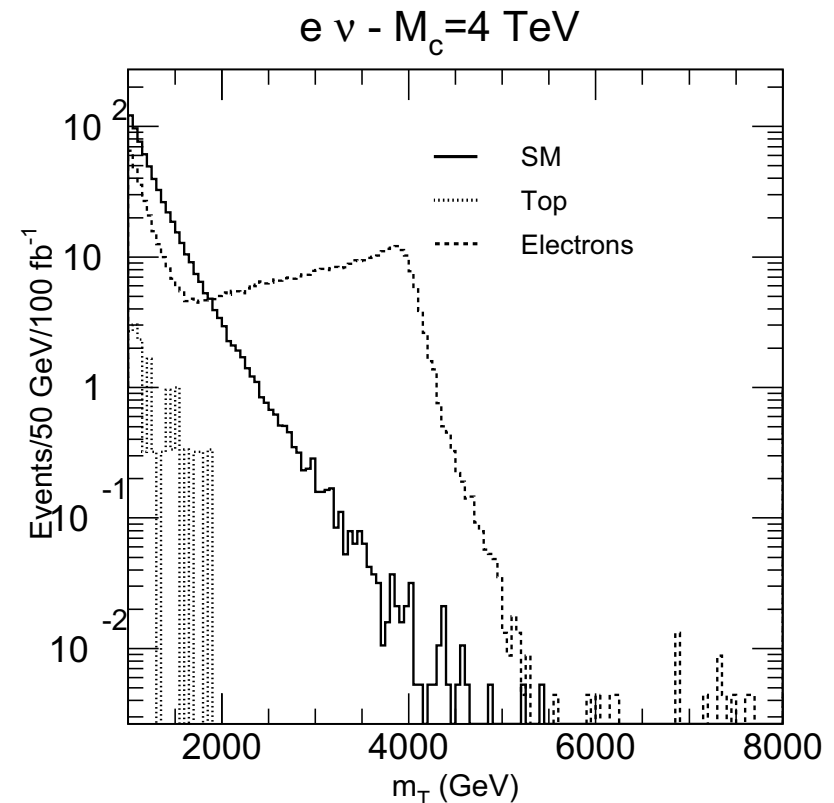
$\leq \cancel{E}_T > 200$  GeV

$\leq m_T(\ell\eta) > 1$  TeV

Where  $m_T = \sqrt{2p_T^\ell p_T^\eta (1 \pm \cos \Delta\eta)}$

If no new physics 500 events from off-shell

SM  $W$  ( $100 \text{ fb}^{\times 1}$ )



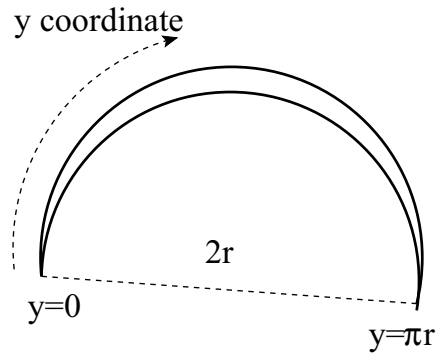
Reducible backgrounds considered:  $t\bar{t}$ ,  $WW$ ,  $ZZ$

For  $m_T(\ell\eta) > 1$  TeV  $\ll 75$  background events, dominated by  $WW$  and  $WZ$

With moderate jet veto at 100 GeV, background reduced to  $\ll 20$  events, but bias for study of Jacobian shape

Reach for  $100 \text{ fb}^{\times 1}$ :  $\ll 5.8$  TeV - Only statistical

# Randall-Sundrum model



One additional dimension in which gravity propagates

ED compactified on  $S^1/Z_2$  (circle folded on itself  $\ll$  orbifold)

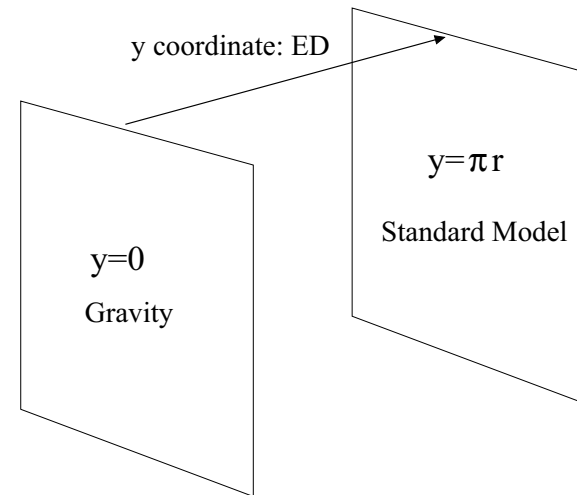
Two branes at extremal values of compactification:

$\ll$  Planck brane:  $y=0$ , where gravity localized

$\ll$  Tev-brane where SM fields (us) constrained

Metric for this scenario is non-factorizable:

$$ds^2 = e^{\times 2ky} \eta_{\eta\eta} dx^\eta dx^\eta \ll dy^2, \quad (1)$$



Exponential term: "warp factor". Parameter  $k$  of order Planck scale governs curvature of space  $R_5$ .  $R_5 = \ll 20k^2$

5D Plank scale  $M_5$  must be larger than inverse radius of curvature  $|R_5| < M_5^2$ ,

otherwise physics dominated by quantum gravity effects

Solving Einstein's equation obtain for reduced 5-dim scale  $\overline{M}_5 \ll M_5/\sqrt{8\eta}$ :

$$\overline{M}_{Pl}^2 = \frac{\overline{M}_5^3}{k} \quad (2)$$

The bound  $|R_5| < M_5^2$  thus becomes  $k/\overline{M}_{Pl} \ll 0.1 \Rightarrow$  Very small hierarchy

The scale of all physical processes on the TeV brane described by:

$$\Lambda_\eta \ll \overline{M}_{Pl} e^{\times k R_c \eta} \quad \Lambda_\eta \ll 1 \text{ TeV then implies } kR = 10.$$

Model defined in terms of:

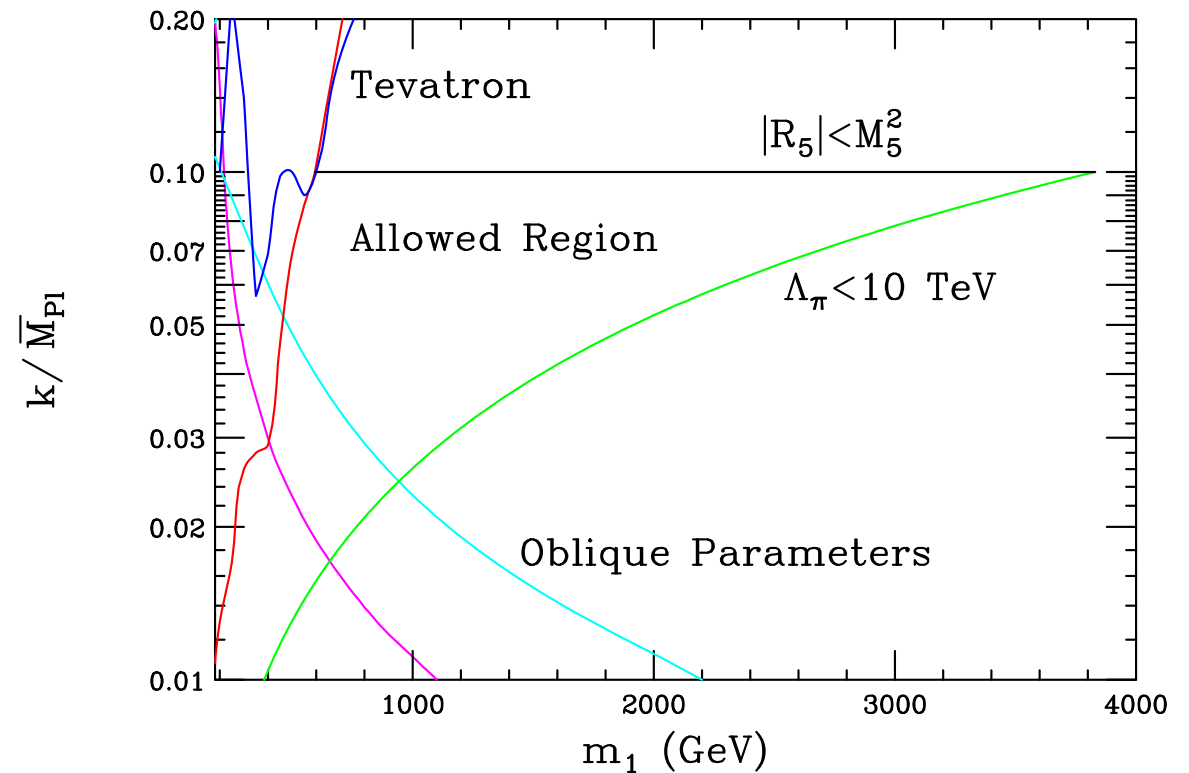
$$\ll \Lambda_\eta \ll k/\overline{M}_{Pl}.$$

By requiring:

$$\Lambda_\eta < 10 \text{ TeV (hierarchy)}$$

closed region in  $(m_1, k/\overline{M}_{Pl})$

plane, with  $m_1 = 3.83 \frac{k}{\overline{M}_{Pl}} \Lambda_\eta$



## Randall-Sundrum phenomenology: Narrow graviton states

Masses of KK graviton obtained from Bessel expansion, replacing Fourier expansion of flat geometry. Mass  $m_n$  of excitation  $G^{(n)}$  at:

$$m_n = x_n k e^{\times k \eta r_c} = x_n \frac{k}{M_{Pl}} \Lambda_\eta$$

where  $x_n$  are the roots of the first order Bessel function.  $x_1 = 3.83$

$\Rightarrow \ll \text{TeV}$  scale for mass of first excitation, accessible to LHC

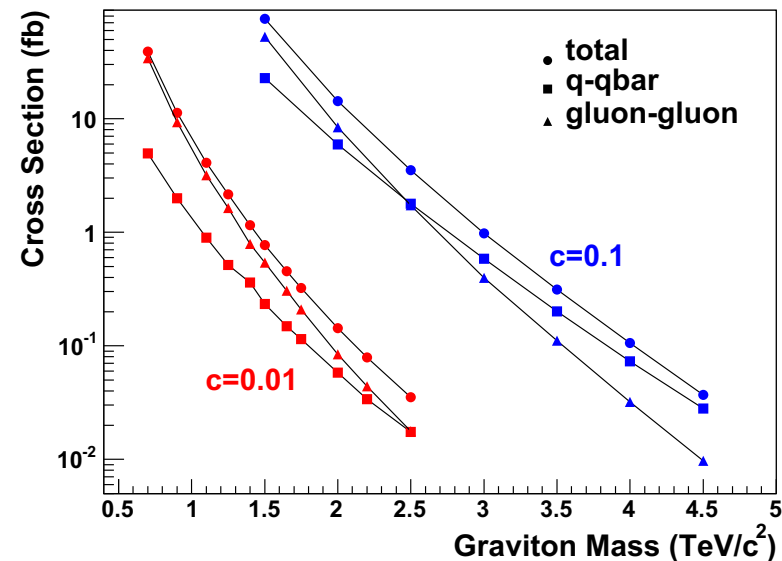
Couplings of  $G^{(n)}$  to SM fields  $\ll 1/\Lambda_\eta$ ,

widths and cross-sections as for  $Z'$ :

$\ll$  sizable cross-section at the LHC

$\ll$  Narrow resonances

Coupling driven by factor  $c = k/M_{Pl}$



## $G(1) \rightarrow e^+e^-$ in CMS (full simulation)

Graviton couples to all SM particles

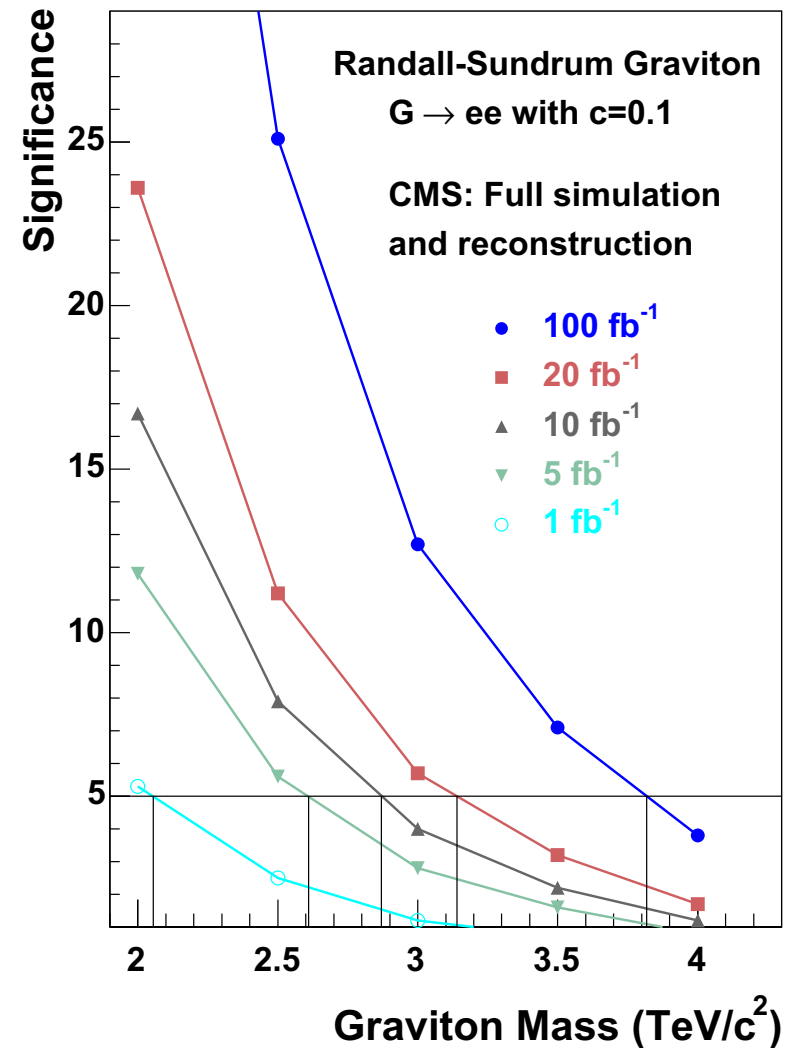
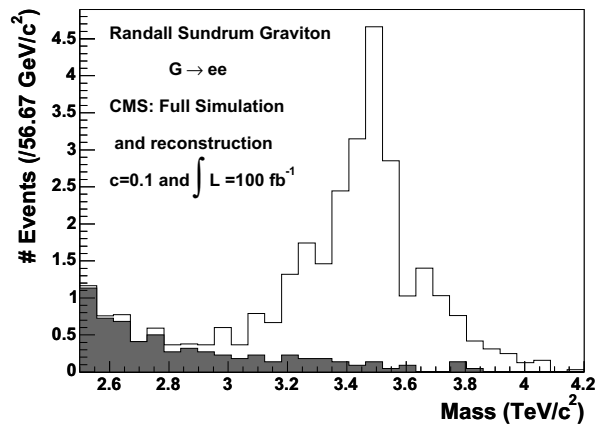
Most favourable channel  $G(1) \rightarrow e^+e^-$ :

«Optimal experimental resolution

«Minimal background

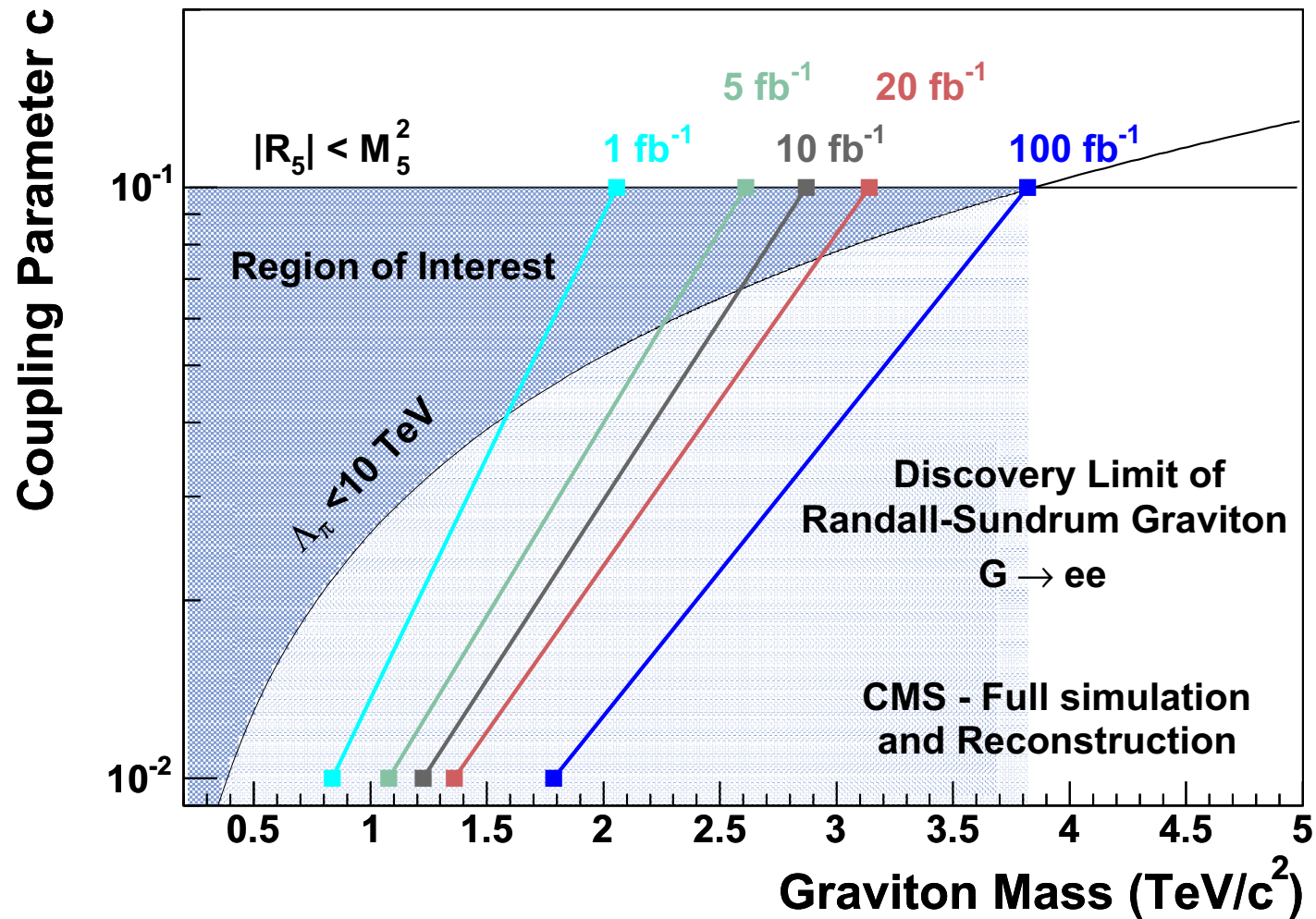
Study achievable significance as a function  
of mass of first excited state

Use  $c = 0.1$  and  $c = 0.01$  for couplings



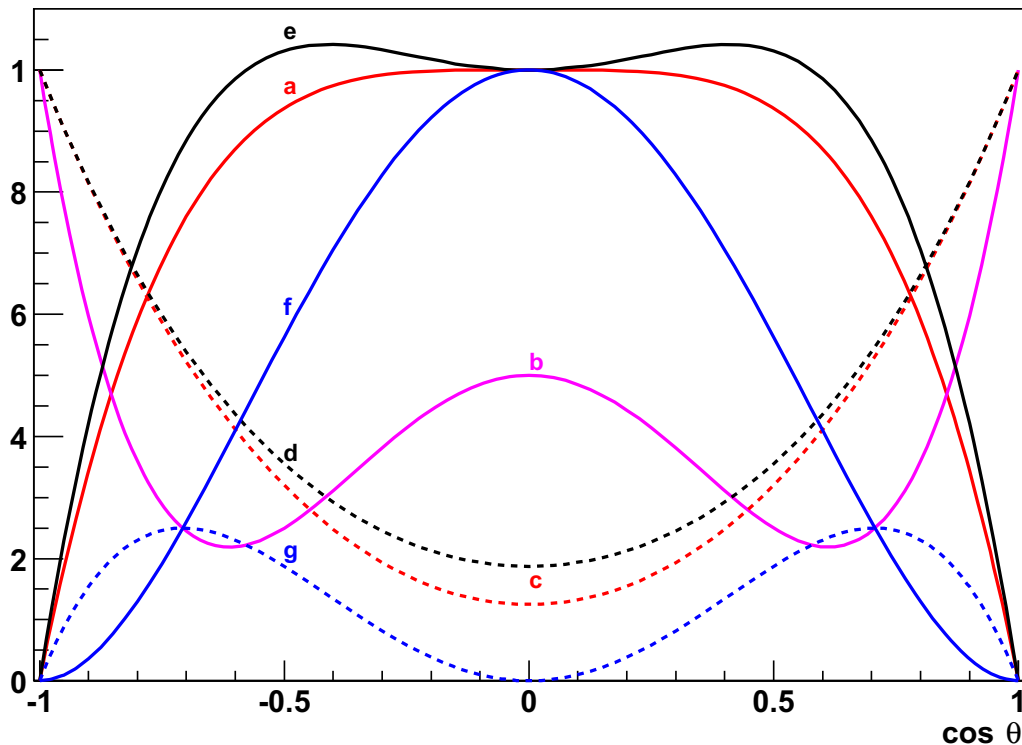
## Coverage of parameter space

With one year at the LHC (high lumi) full coverage of parameter space



# Spin determination of graviton resonance

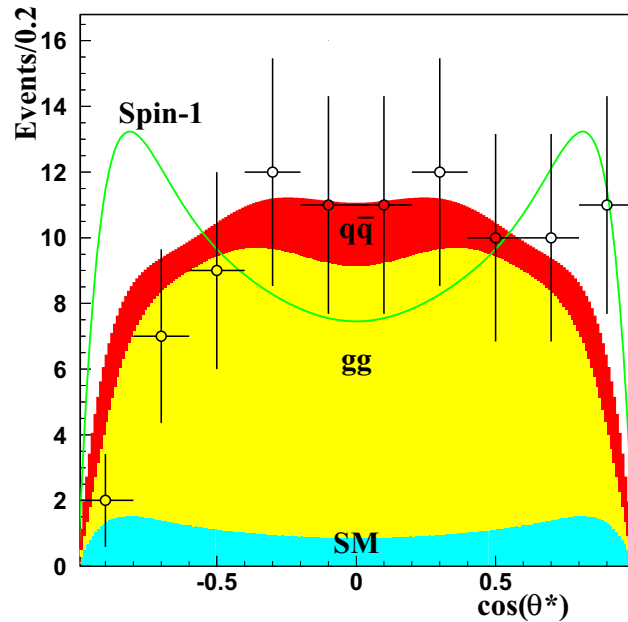
Graviton is spin-2 particle. Angular distribution of decay products depends on production mechanism, and on spin and mass of decay products



Process	Distribution	Plot
$gg \rightarrow G \rightarrow f\bar{f}$	$\sin^2 \eta^* (2 \times \eta^2 \sin^2 \eta^*)$	a
$q\bar{q} \rightarrow G \rightarrow f\bar{f}$	$1 + \cos^2 \eta^* \times 4\eta^2 \sin^2 \eta^* \cos^2 \eta^*$	b
$gg \rightarrow G \rightarrow \eta\eta, gg$	$1 + 6 \cos^2 \eta^* + \cos^4 \eta^*$	c
$q\bar{q} \rightarrow G \rightarrow \eta\eta, gg$	$1 \times \cos^4 \eta^*$	a
$gg \rightarrow G \rightarrow WW, ZZ$	$1 \times \eta^2 \sin^2 \eta^* + \frac{3}{16} \eta^4 \sin^4 \eta^*$	d
$q\bar{q} \rightarrow G \rightarrow WW, ZZ$	$2 \times \eta^2 (1 + \cos^2 \eta^*) + \frac{3}{2} \eta^4 \sin^2 \eta^* \cos^2 \eta^*$	e
$gg \rightarrow G \rightarrow HH$	$\sin^4 \eta^*$	f
$q\bar{q} \rightarrow G \rightarrow HH$	$\sin^2 \eta^* \cos^2 \eta^*$	g

$\eta$  is  $v/c$  of decay products

Gluon fusion dominates, contribution from  $q\bar{q}$  flattens distribution

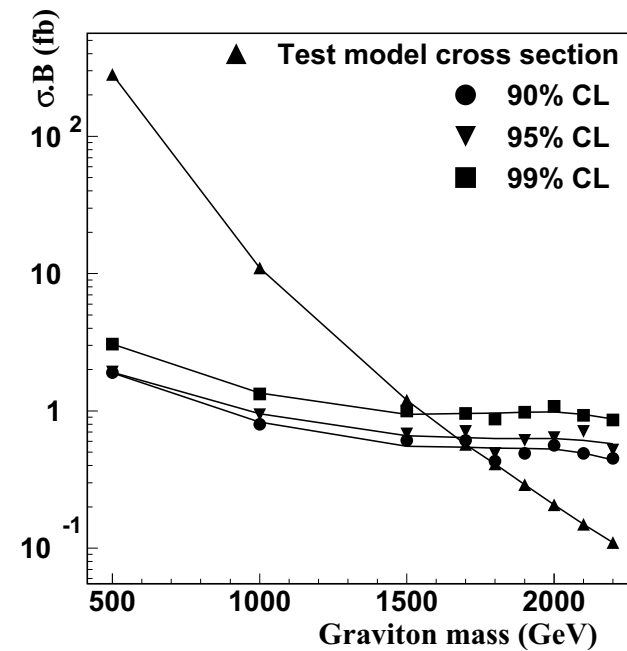


Polar angle distribution of  $e^+e^-$  after the acceptance cuts are applied

For  $m_1 = 1500$  GeV and  $100 \text{ fb}^{-1}$  can distinguish from spin 1 case

Test spin hypotheses with a likelihood technique

Spin-1 hypothesis can be ruled out at 90% CL up to  $m_1 = 1720$  GeV





# Black Holes

Geometrical semi-classical reasoning:

Possibility of black hole formation when two colliding partons have impact parameter smaller than the radius of a black hole

Consider two colliding partons with CMS energy  $\sqrt{\hat{s}} = M_{BH}$

Dimensional analysis: partonic X-section for formation of black hole of mass  $M_{BH}$  is

$$\eta(\hat{s} = M_{BH}^2) \ll \eta R_s^2$$

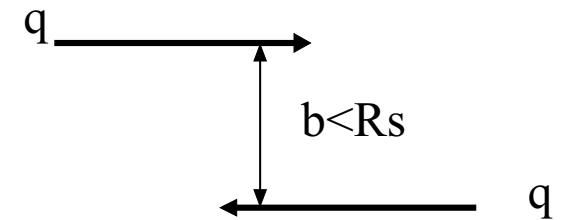
Where  $R_S$  is Schwarzschild radius of black hole

$$R_S \ll \frac{1}{\sqrt{\eta} M_P} \left[ \frac{M_{BH}}{M_P} \right]^{\frac{1}{n+1}}$$

In extra-dimension theories  $M_P \ll \text{TeV} \Rightarrow$ , for  $M_{BH} \ll M_P$ ,  $\eta \ll (\text{TeV})^{\times 2} \ll 400 \text{ pb}$

Potentially large production cross-section

Theoretical debate on geometrical formation factors. Possible big suppression

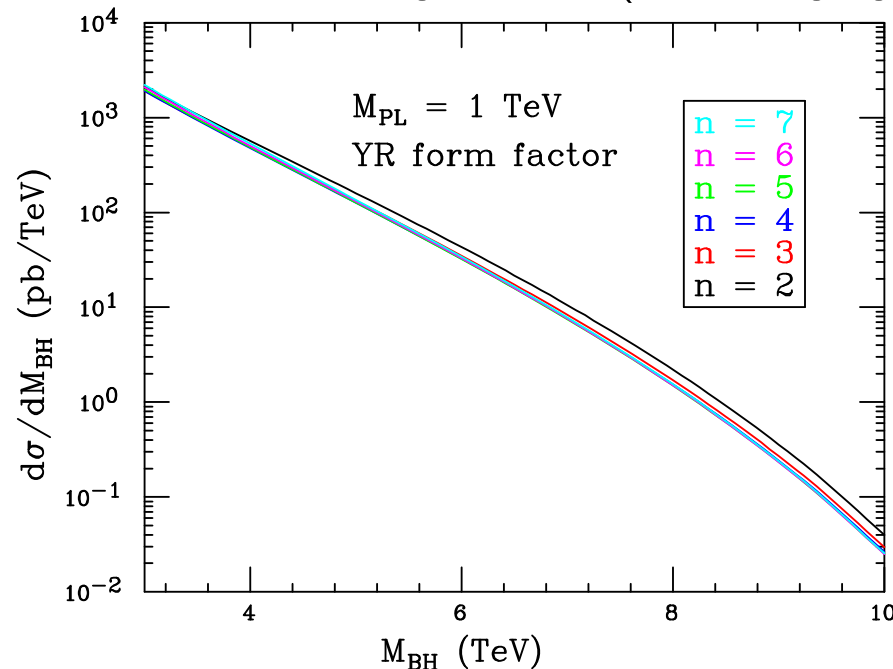


# Black Hole production

Convolve the parton-level cross-section with parton distribution functions

For  $n > 2$  dimensions little dependence on  $n$  because of assumed form of formation

factor in CHARYBDIS generator (Cambridge group)



At high luminosity,  $> 1$  black hole per second with  $M_{BH} > 5$  TeV

Preliminary ATLAS study based on detailed simulation of different CHARYBDIS BH

samples with  $M_{BH} > 5$  TeV and various values of  $n : 2, 4, 7$

## Black Hole decay

Decay through Hawking radiation

Details of decay extremely model-dependent.

Simplifying assumptions: all partonic energy goes into BH formation, all Hawking radiation through SM Particles on the brane

Thermal radiation: black body energy spectrum

$$\frac{dN}{dE} \propto \frac{\eta E^2}{(e^{E/T_H} \ll 1)} T_H^{n+6} \quad (3)$$

$\ll$  applies to fermions and bosons,  $T_H$  is the Hawking temperature

$$T_H = \frac{n+1}{4\eta r_s} \propto M_{BH}^{\times \frac{1}{n+1}} \quad (4)$$

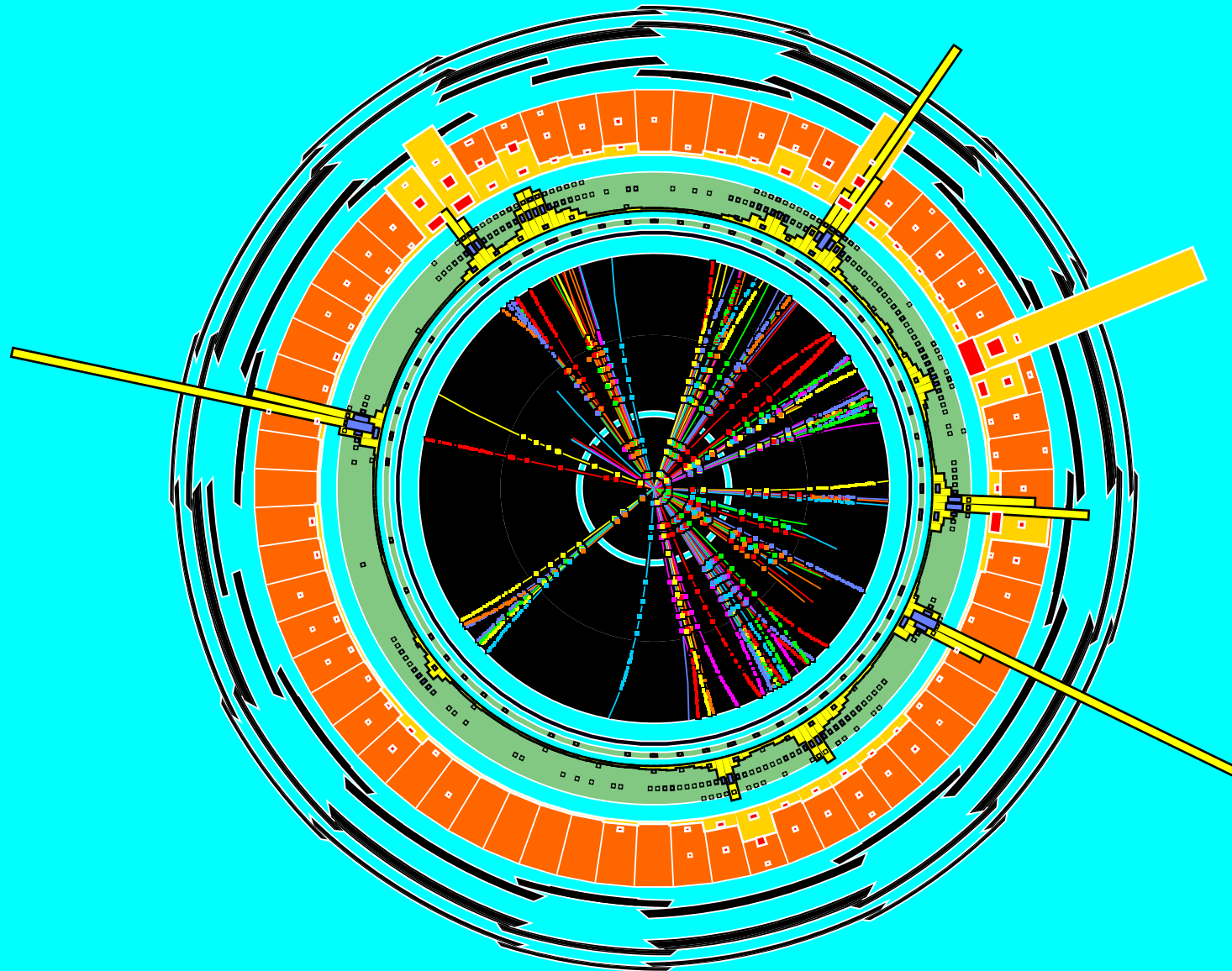
$\eta$  is *grey-body factor*: absorption factor from propagation in curved space

$T_H$  increases with increasing  $n \rightarrow$  more energetic particles produced  $\rightarrow$  lower multiplicity for fixed  $M_{BH}$

ATLAS

Atlantis

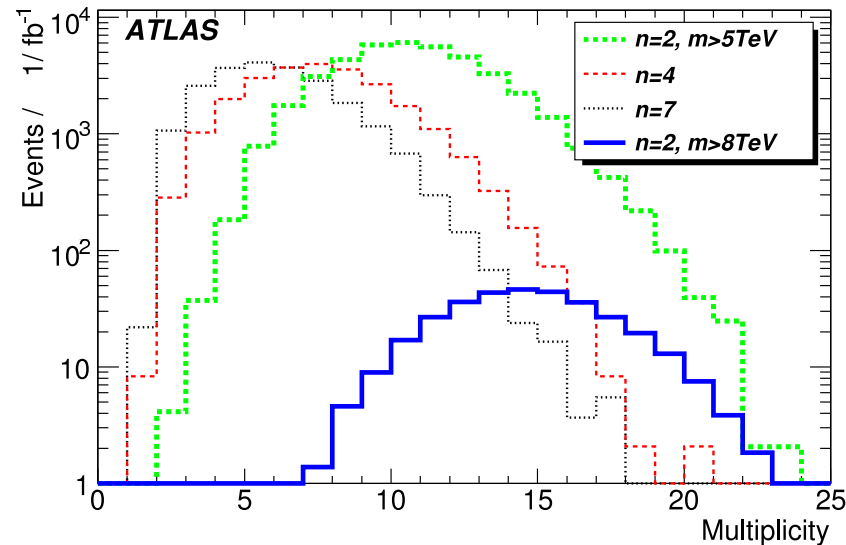
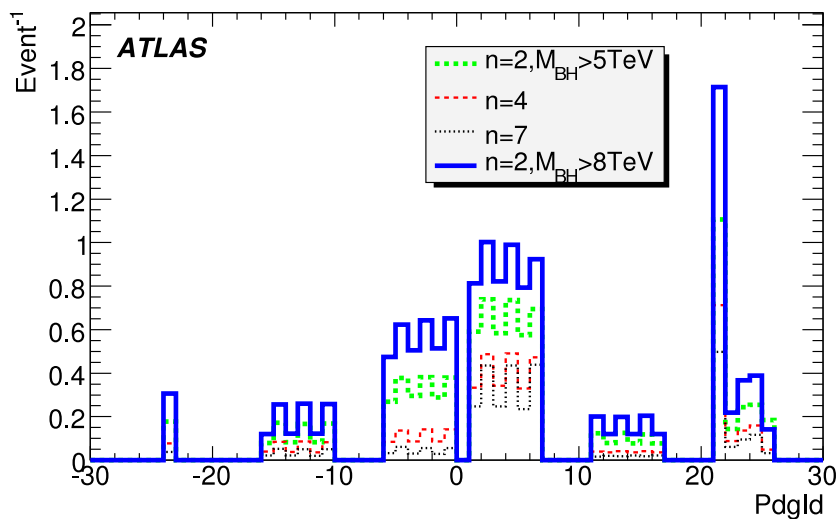
Event: BlackHole\_000001\_000001.xml



## Event characteristics of BH decays

«Approximately democratic decay in all types of particles, depending on the degrees of freedom ( $q=6$ ,  $g=8$ ), similar  $p_T$  spectrum for all types of particles

«Large multiplicities of reconstructed objects (jets, electrons, muons, photons) in final state, falling with  $n$ , as BH decays at higher temperature



$1 \leq |PdgID| \leq 6$ : quarks,  $11 \leq |PdgID| \leq 16$ : leptons,  $21 \leq |PdgID| \leq 25$ : gauge bosons, higgs

In principle very spherical events, but shape of events strongly dependent on BH parameters

## Event selection

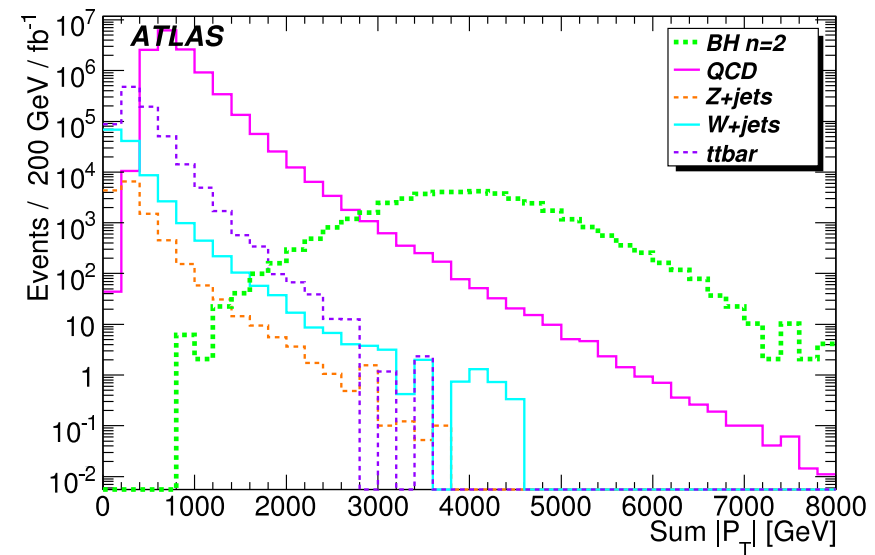
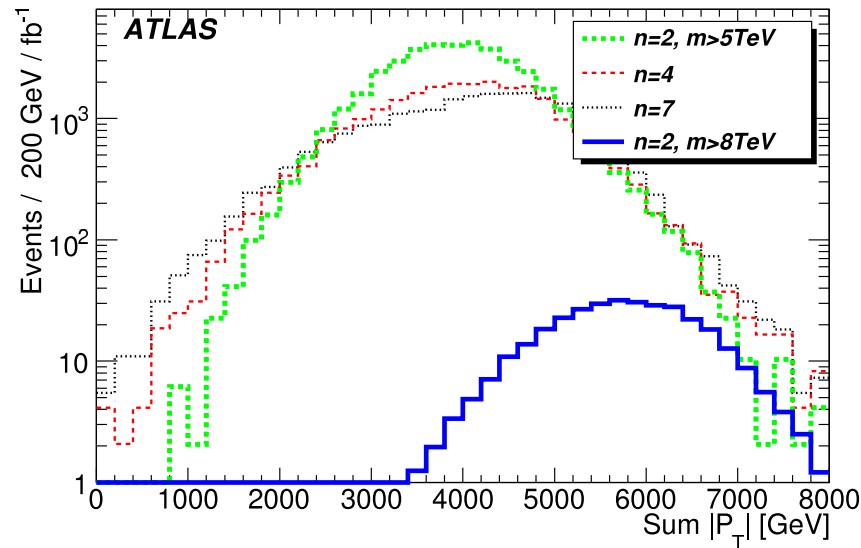
First step is trigger. Given high mass of events, trigger request of one jet with

$p_T > 400$  GeV has 99% for all generated samples

Backgrounds from QCD,  $W + jets$ ,  $Z + jets$ ,  $t\bar{t}$  considered

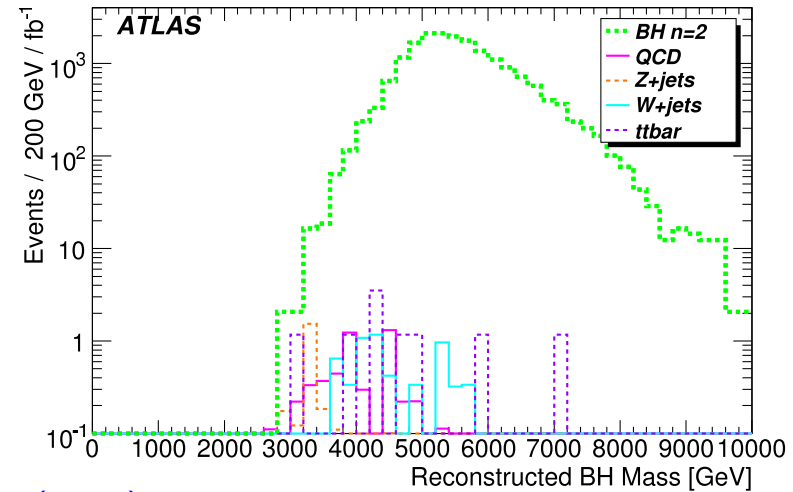
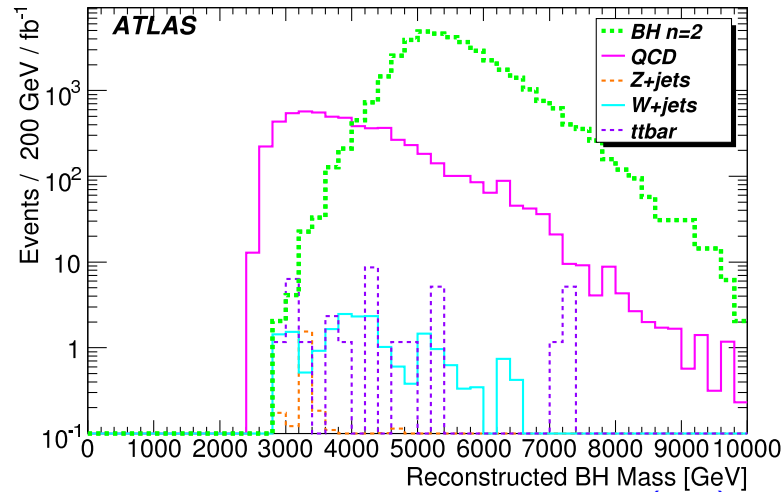
Rejection of SM background based on exploiting high mass of black holes

Use as discriminant variable  $\Sigma |P_T|$ , scalar sum of the  $P_T$  of objects in an event



Require  $\Sigma |P_T| > 2.5$  TeV to separate signal from background

After cut on  $\Sigma |P_T|$  significant QCD background. Require lepton with  $P_T > 50$  GeV



Plot of reconstructed BH mass before (left) and after (right) lepton requirement

For  $M_{BH} > 5$  TeV, efficiency for lepton cut  $\leq 50(17)\%$  for  $n = 2(7)$ , Additional factor 1000 for rejection on QCD

Black holes can be discovered above the 5 TeV threshold with a few  $\text{pb}^{\times 1}$  of data.

$\ll 1 \text{ fb}^{\times 1}$  needed if production threshold is 8 TeV

Statement based on assumed correctness of the decay model and of the predicted tail of QCD at high  $\Sigma |P_T|$ . Needs to be substantiated by measurement with real data

Large uncertainties on acceptance from parameters of modelling of BH decay at high  $n$

# Parameter measurement

Consider the possibility of measuring the number of extra-dimensions  $n$

For given  $M_{BH}$   $T_h$  depends on  $n$

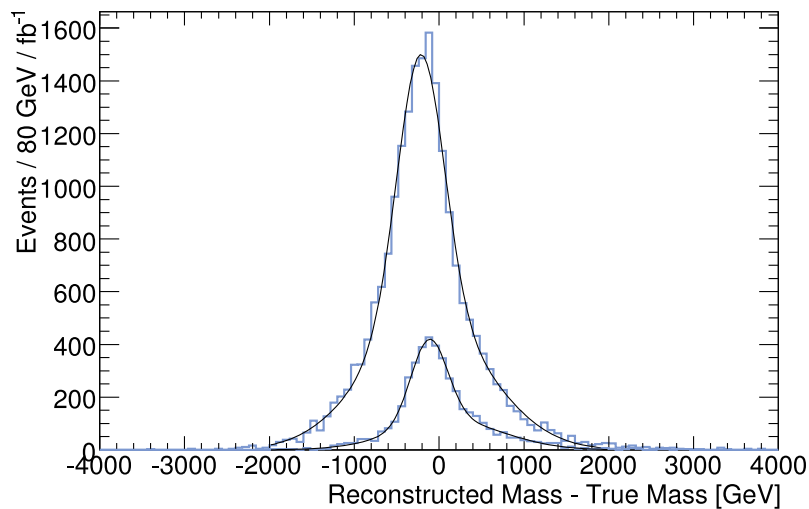
If we detect events with emissions near  $M_{BH}/2$ , the energy of the emission is a measure of  $T_h$

For this measurement give up lepton requirement (bias), and ask  $\Sigma |P_T| > 2.5$  TeV

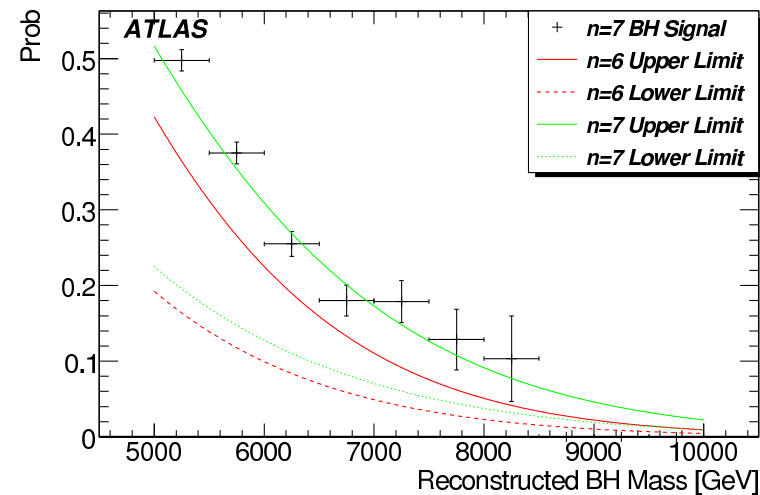
Accurate mass resolution needed: require  $\cancel{E}_T < 100$  GeV

Fit BH mass resolution with two gaussians. The width of the narrow gaussian goes from 276 to 215

GeV after  $\cancel{E}_T$  requirement



Plot of emission probability as a function of BH shows sensitivity to  $n$



Value of  $M_{Pl}$  needed for measurement should be measurable from production cross-section



## Conclusions

Among many possible signatures for new physics concentrate on two signatures which can be discovered with early data

High mass lepton resonances as classical example

Detailed studies involving many different possible sources show good potential with the very first data

In case of discovery necessary to measure couplings of  $Z'$  to understand underlying physics

Extra Dimension theories offer an attractive way of solving the hierarchy problem based on the space-time geometry of space

Among the most striking possibilities is the production of micro black holes

A detailed experimental study shows that few  $pb^{×1}$  could be sufficient for the discovery of black holes

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Backup

## Kaluza-Klein towers

Features of compactified extra-dimensions, due to periodicity condition of fields in extra dimension:  $\eta(y + 2\pi R) = \eta(y)$  where  $y$  is extra dimension

Spacing of Kaluza-Klein states can be understood with heuristic considerations

Standing waves in box:

«Wavelengths  $\eta$  such as the size  $L \ll 2\pi R$  of the box is a multiple of  $\eta$

«The wave number  $k$  satisfies  $k \ll 2\pi/R = n/R$  with  $n$  integer

«Energy is quantized  $E = \hbar k$

Compact dimensions can be assimilated to a finite box.

«Expect in compactified dimension particles with mass spectrum characteristic of standing waves, i.e. quantized in units of  $1/R$

These oscillations are called Kaluza-Klein modes

## Case of a single ED

Standard relativistic formula  $E^2 = \mathbf{p}^2 + m_0^2$  reads:

$$E^2 = \mathbf{p}^2 + p_5^2 + m_0^2$$

Where  $p_5$  is momentum in fifth dimension, quantised as  $p_5 = \hbar k_5 = n\hbar/R$

Thus in center of mass ( $\mathbf{p} = 0$ ) one obtains the following energy spectrum:

$$E^2 = \left[ m_0^2 + \frac{n^2 \hbar^2}{R^2} \right]$$

A 5-dimensions field is identified in 4 dimensions to a tower of particles regularly spaced in mass squared, the gap being the inverse of the compact dimension size

⇒ For each field propagating in the bulk, with mass  $m_0$ , if  $m_0 \ll 1/R$  in the theory will appear an infinite sequence of states with masses  $1/R, 2/R, 3/R, \dots$

Study whether, for the different implementations of the model these KK states can be detected at the LHC