

# Probing of anomalous $HZZ$ interactions at high energy colliders

Signaling the Arrival of the LHC Era

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# *HVV* interactions

- $VVH$  and  $VVHH$  interactions are generated from the kinetic term of the Higgs field after symmetry breaking.
- The strength and structure of  $VVH$  interaction depends upon the quantum number of the Higgs field, such as  $CP$ , weak isospin, hypercharge etc.
- After discovery of the Higgs boson the determination of its couplings ( $HVV$ ,  $Ht\bar{t}$ ) will be essential to establish it as the SM Higgs boson.
- The  $HZZ$  coupling can be explored at the LHC in the process:  
$$H \rightarrow ZZ^{(*)} \rightarrow (f_1\bar{f}_1)(f_2\bar{f}_2)$$
- The tensor structure of  $HZZ$  and  $HWW$  couplings can also be studied in vector boson fusion and gluon fusion processes.

# Anomalous Higgs interactions

- Most general  $HZZ$  coupling structure:

$$V_{\mu\nu}^{HZZ} = \frac{igm_Z}{\cos\theta_W} \left[ a g_{\mu\nu} + b \frac{p_\mu p_\nu}{m_Z^2} + c \epsilon_{\mu\nu\alpha\beta} \frac{p^\alpha k^\beta}{m_Z^2} \right],$$

where  $p = q_1 + q_2$  and  $k = q_1 - q_2$ ;  $q_1$  and  $q_2$  are the four-momenta of two  $Z$  bosons respectively.

- At tree-level SM,  $a = 1$  and  $b = c = 0$ .
- $a$  and  $b$ : associated with the coupling of a CP-even Higgs boson;  $c$ : associated with the CP-odd one.
- $b$  and  $c$  can be complex in general.

# Discrete transformation properties of couplings

	$a$	$\Re e(b)$	$\Im m(b)$	$\Re e(c)$	$\Im m(c)$
$CP$	+	+	+	-	-
$\tilde{T}$	+	+	-	-	+

- $a$  and  $b$  are even under  $CP$  whereas  $c$  is odd under  $CP$ .
- $a$ ,  $\Re e(b)$  and  $\Im m(c)$  are even under  $\tilde{T}$  while  $\Im m(b)$  and  $\Re e(c)$  are odd under  $\tilde{T}$ .

# Strategy to construct asymmetries

- **Strategy:** Construct observables (asymmetries) with a given  $CP$  and  $\tilde{T}$  transformation properties that are sensitive to a single anomalous part of the  $HZZ$  vertex with the same  $CP$  and  $\tilde{T}$  transformation properties.
- For each momentum combination ( $\mathcal{C}_i$ ), asymmetry can be constructed as:

$$A_i = \frac{\Gamma(\mathcal{C}_i > 0) - \Gamma(\mathcal{C}_i < 0)}{\Gamma(\mathcal{C}_i > 0) + \Gamma(\mathcal{C}_i < 0)}.$$

$\mathcal{C}_i$ 's have definite  $CP$  and  $\tilde{T}$  transformation properties.

# Probes of $HZZ$ interaction

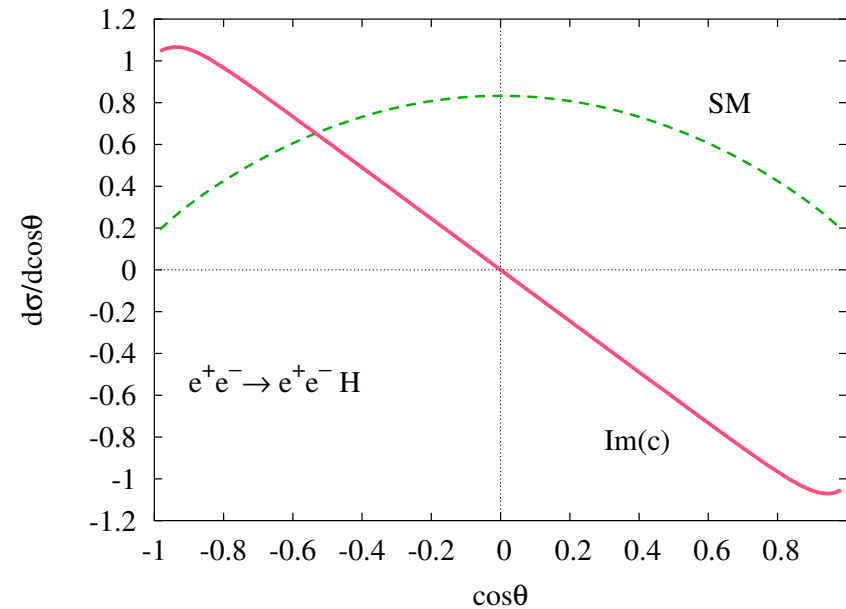
- We have developed general methods to probe the  $HVV$  interactions at the  $e^+e^-$  colliders with/without beam polarization\*.
- The same strategy has been used in the context of the LHC\*\*.

\* Biswal, Choudhury, Godbole et al, Phys. Rev. D 73, 035001 (2006)[arXiv:hep-ph/0509070]; arXiv:0809.0202 [hep-ph], submitted to Phys. Rev. D.

\*\* *Aspects of CP violation in the HZZ coupling at the LHC*, Godbole, Miller and Muhlleitner, JHEP 0712, 031 (2007), [arXiv:0708.0458 [hep-ph]]

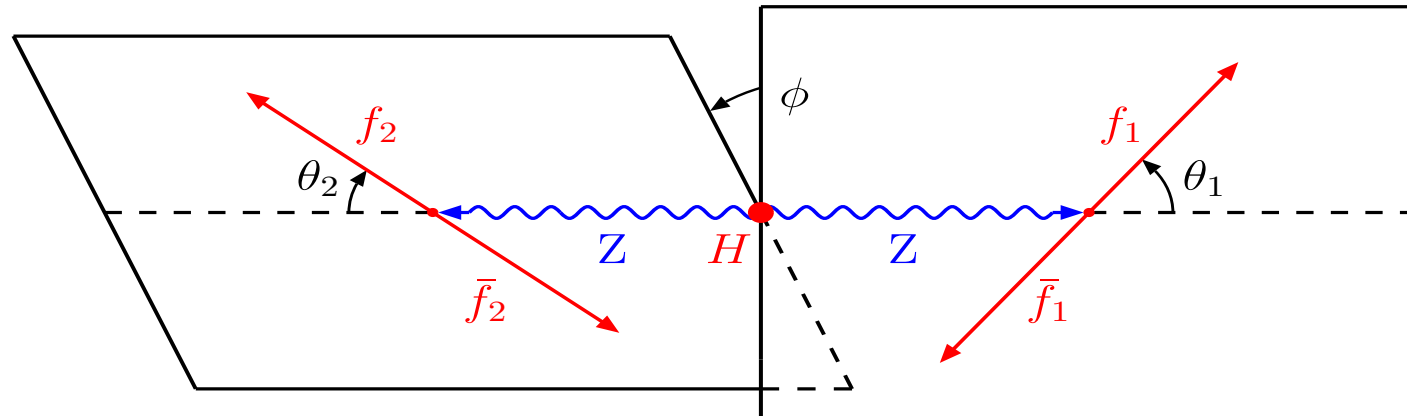
# Example: Probe of $HZZ$ interactions at the ILC

- Process:  $e^+e^- \rightarrow f\bar{f}H^*$ .
- Combination:  $[\vec{p}_{e^-} - \vec{p}_{e^+}] \cdot \vec{p}_H$  ( $CP$ -odd,  $\tilde{T}$ -even)
- Asymmetry:  $A_{FB}(\cos\theta_H) = \frac{\sigma(\cos\theta_H > 0) - \sigma(\cos\theta_H < 0)}{\sigma(\cos\theta_H > 0) + \sigma(\cos\theta_H < 0)}$ ; can probe  $\Im m(c)$ .  
 $F(B)$ :  $H$  is in forward (backward) hemisphere w.r.t. the direction of initial  $e^-$ .



# Example: Probes of $HZZ$ interactions at the LHC

- Process:  $H \rightarrow ZZ^{(*)} \rightarrow [f_1(p_1)\bar{f}_1(p_2)][f_2(p_3)\bar{f}_2(p_4)]$
- Notation:



$\theta_1$  and  $\theta_2$ : polar angles of the fermions  $f_1, f_2$  in the rest frame of the parent  $Z$  boson.

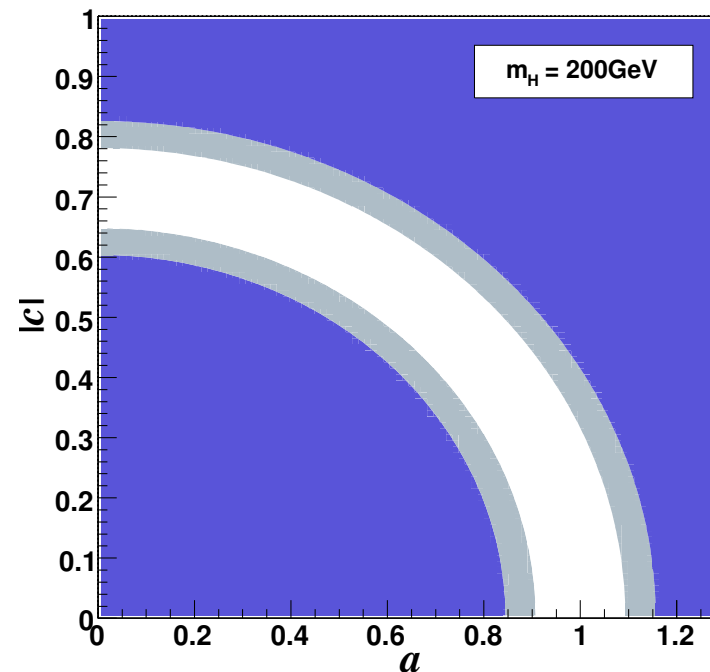
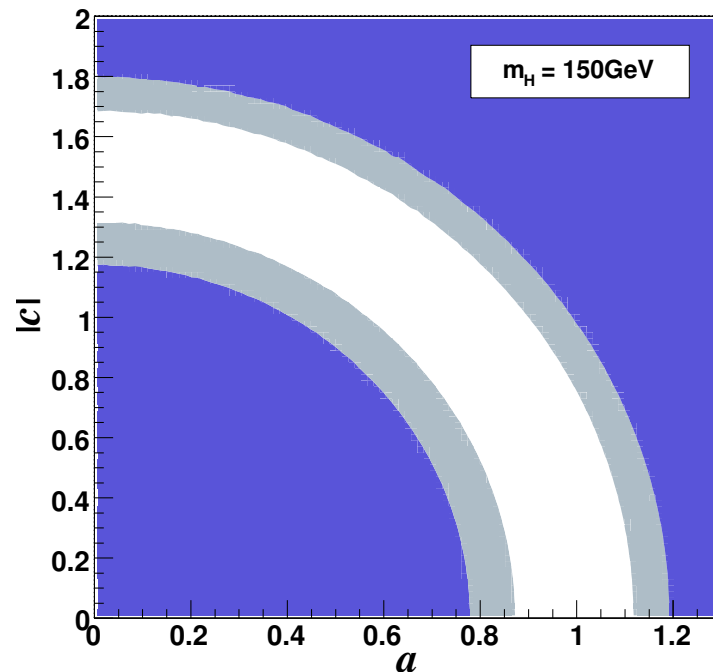
$\phi$ : azimuthal angle between the planes formed from the fermion pairs in the Higgs boson rest frame.



# Sensitivity of total production

Dominant Higgs production process at the LHC:

$$gg \rightarrow H \rightarrow ZZ^{(*)} \rightarrow (f_1 \bar{f}_1)(f_2 \bar{f}_2), \text{ with } f = e \text{ or } \mu.$$



- In the white region one cannot distinguish the corresponding  $a, c$  values from the SM case  $a = 1, c = 0$  at a significance more than  $3\sigma$ .
- Asymmetries are required to probe specific parts of the anomalous couplings directly.

# Probe of $\Im m(c)$

- Process:  $H \rightarrow ZZ^{(*)} \rightarrow [f_1(p_1)\bar{f}_1(p_2)][f_2(p_3)\bar{f}_2(p_4)]$

- Combination:

$$C_1 \equiv \frac{(\vec{p}_{2Z} - \vec{p}_{1Z}) \cdot (\vec{p}_{3H} + \vec{p}_{4H})}{|\vec{p}_{2Z} - \vec{p}_{1Z}| |\vec{p}_{3H} + \vec{p}_{4H}|} = \cos \theta_1 ,$$

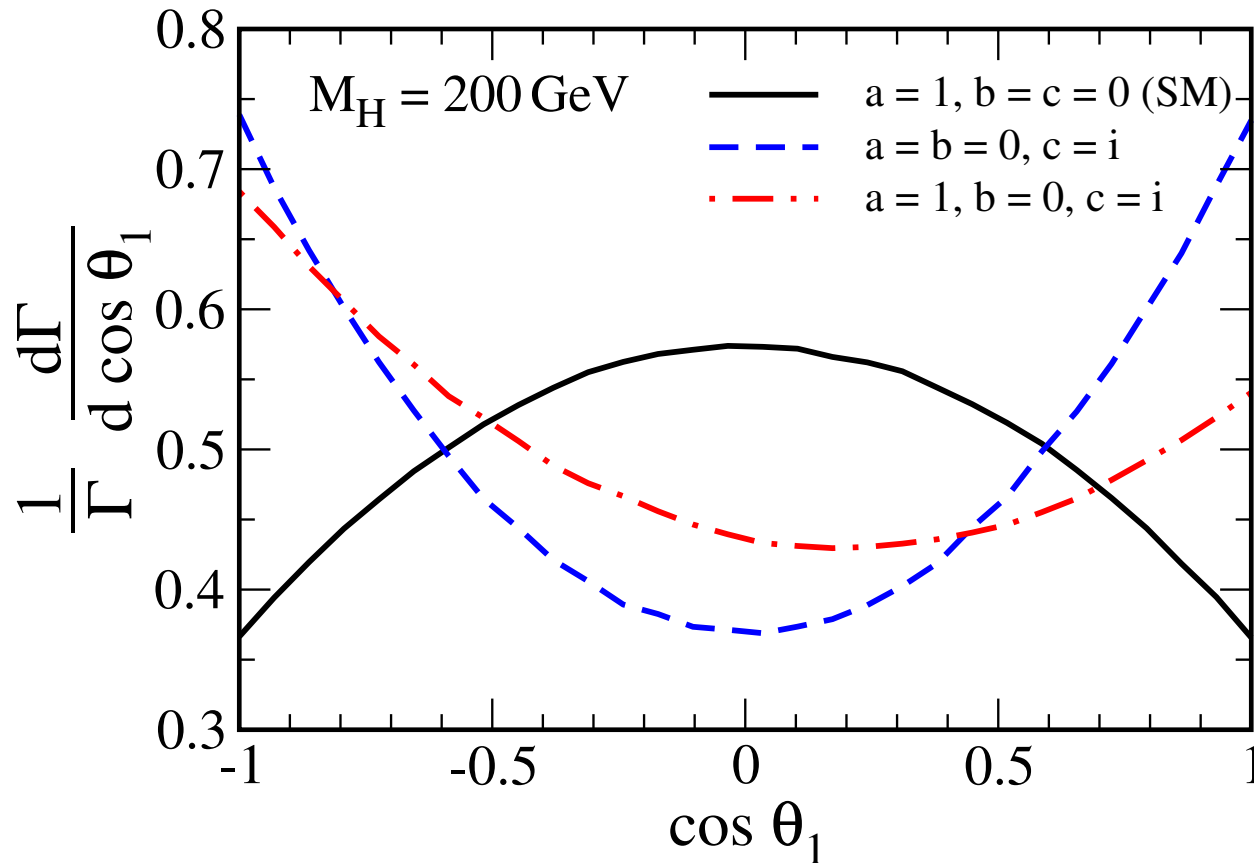
$\vec{p}_{Z/H}$ : is defined in the  $Z$  boson or Higgs boson rest frame.

- Asymmetry:

$$A_1 = \frac{\Gamma(\cos \theta_1 > 0) - \Gamma(\cos \theta_1 < 0)}{\Gamma(\cos \theta_1 > 0) + \Gamma(\cos \theta_1 < 0)} .$$

- $A_1$  is  $CP$ -odd and  $\tilde{T}$ -even; probe of  $\Im m(c)$ .

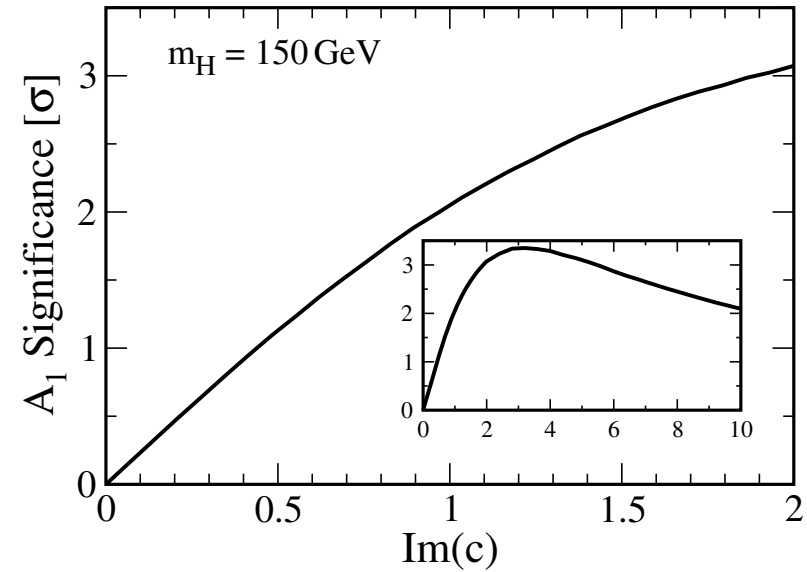
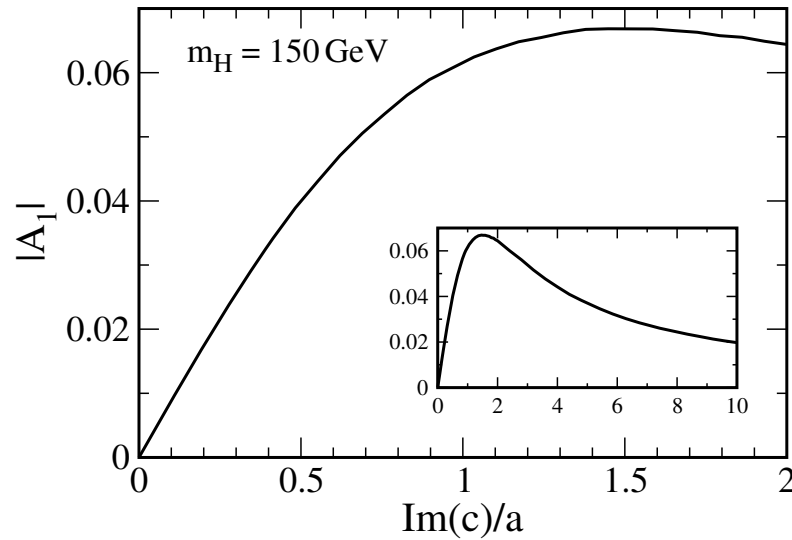
# An asymmetry to probe $\Im m(c)$



- An asymmetry about  $\cos \theta_1 = 0$  for the  $CP$  violating case ( $a = 1, b = 0, c = i$ ).

# Size & significance of the asymmetry ( $\mathcal{A}_1$ )

- Size of the asymmetry:



- $\mathcal{A}_1$  may provide *evidence* for  $CP$  violation ( $> 3 \sigma$  deviation from the SM) if  $\Im m(c) \gtrsim 1.9$  for  $m_H = 150 \text{ GeV}$ .
- Use of  $b\bar{b}$  final state (i.e.  $H \rightarrow ZZ \rightarrow l^+l^-jj$ ) can increase the sensitivity of  $\mathcal{A}_1$ .

# An additional observable

- One can construct simple observables using scalar product/ scalar triple product of momenta of particles.
- Some of these observables are suppressed by small vector coupling of fermion to  $Z$ -boson.
- At the  $e^+e^-$  colliders we have used longitudinal beam polarization to overcome this suppression\*.
- At the LHC one needs to construct more complicated observables to study the  $HZZ$  vertex\*\*.

\* Biswal, Choudhury, Godbole and Mamta, arXiv:0809.0202 [hep-ph], submitted to Phys. Rev. D.

\*\* Godbole, Miller and Muhlleitner, JHEP 0712, 031 (2007), [arXiv:0708.0458 [hep-ph]]

# Observable to probe $\Re e(c)$

- One more combination:

$$\begin{aligned} \mathcal{C}_4 &= \sin^2 \theta_1 \sin^2 \theta_2 \sin \phi \cos \phi (\propto \sin 2\phi) \\ &= \frac{[(\vec{p}_{3H} \times \vec{p}_{4H}) \cdot \vec{p}_{1H}][(\vec{p}_{3H} \times \vec{p}_{4H}) \cdot (\vec{p}_{1H} \times \vec{p}_{2H})]}{|\vec{p}_{3H} + \vec{p}_{4H}|^2 |\vec{p}_{1H} + \vec{p}_{2H}| |\vec{p}_{3Z} - \vec{p}_{4Z}|^2 |\vec{p}_{1Z} - \vec{p}_{2Z}|^2 / 16} . \end{aligned}$$

- Asymmetry:

$$\mathcal{A}_4 = \frac{\Gamma(\mathcal{C}_4 > 0) - \Gamma(\mathcal{C}_4 < 0)}{\Gamma(\mathcal{C}_4 > 0) + \Gamma(\mathcal{C}_4 < 0)}$$

- $\mathcal{A}_4$  is *CP-odd* and  $\tilde{T}$ -*odd*; probe of  $\Re e(c)$ .

# Dependence of the asymmetries on $a, b, c$

● List of observables(\*):

Asymmetry	$a$	$\Re(b)$	$\Im(b)$	$\Re(c)$	$\Im(c)$
$\mathcal{A}_1$	x				x
$\mathcal{A}_2$	x	(x)	(x)	x	(x)
$\mathcal{A}_3$	x	(x)	(x)	x	(x)
$\mathcal{A}_4$	x			x	
$\mathcal{A}_5$	x	(x)	(x)	x	(x)
$\mathcal{A}_6$	x		x		

● (x) denotes a dependence which is suppressed if the additional form factors are small.

\* **Table 1:** Godbole et al, JHEP 0712, 031 (2007), [arXiv:0708.0458 [hep-ph]]

# Summary

- We have developed general methods to probe the  $HVV$  interactions.
- Observables are constructed with a given  $CP$  and  $\tilde{T}$  transformation properties that can probe a single anomalous part of the  $HZZ$  vertex with the same  $CP$  and  $\tilde{T}$  transformation properties.
- General strategy has been used to probe the anomalous Higgs boson interactions at the LHC and at the  $e^+e^-$  colliders.
- Similar procedure has been followed to study the contact  $e^+e^-HZ$  interactions\*.
- We have further studied the  $HVV$  interactions with transverse beam polarization.

\* Rao and Rindani, Phys. Rev. D 77, 015009 (2008) [arXiv:0709.2591 [hep-ph]].



Thank you !