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International Centre for Theoretical Physics**



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**International Workshop on Advanced Polymer Science and
Turbulent Drag Reduction**

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**Turbulent Drag Reduction by Dilute Addition of High Polymers: Theory,
Experiments, Simulations and Predictions**

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Turbulent Drag Reduction by Dilute Addition of High Polymers: Theory, Experiments, Simulations and Predictions

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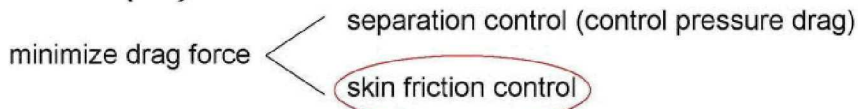
Turbulence and Heat Transfer
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- Turbulent drag reduction by dilute addition of high polymers
- Review of turbulence research
- Invariant modeling of turbulence
- The limiting state of turbulence at the wall
- Polymer-turbulence interaction
- Parameterization of polymer-turbulence interaction for maximum drag reduction effect
- Further examples of turbulent drag reduction and related flow phenomena
- Turbulent drag reductions by surface-embedded grooves
- Conclusions and final remarks

Drag Reduction (DR)



Long chain polymers in turbulent wall bounded flows

- turbulent DR up to 80% with a few ppm of polymer
- act in turbulent boundary layer

Application Area:

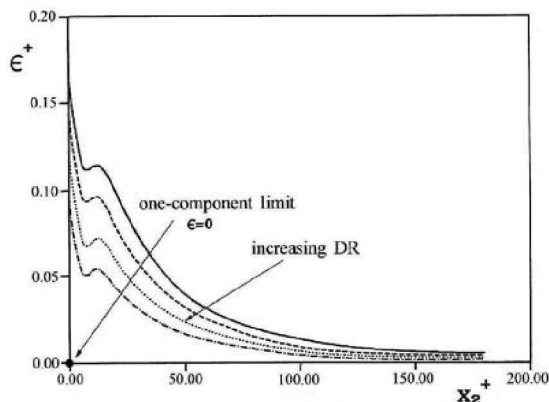
Transalaska Pipeline: 30% energy savings



The average energy dissipation rate $\bar{\Phi}$ can be expressed as the work done against the wall shear stress τ_w per unit mass of fluid:

$$\bar{\Phi} = \frac{1}{V} \int \rho \left[\nu \left(\frac{d\bar{U}_1}{dx_2} \right)^2 + \nu \frac{\partial u_i}{\partial x_k} \frac{\partial u_i}{\partial x_k} \right] dV \cong \frac{A_w \tau_w U_B}{\rho V}$$

$$\varepsilon \sim \nu \left(\frac{d\bar{U}_1}{dx_2} \right)^2$$



$$\varepsilon \cong \frac{u_\tau^3}{Kx_2}$$

Distribution of the turbulent dissipation rate versus difference from the wall

- | | | | |
|---|---|--------|--|
| <ul style="list-style-type: none"> • O. Reynolds (1895) • L. Prandtl (1925) • G. Taylor (1935) • Th. Von Karman (1930) • H. L. Dryden • G. B. Shubauer • H. K. Skramstad | } | (1940) | <ul style="list-style-type: none"> • A. N. Kolmogorov (1941) • P. Y. Chou (1945) • G. K. Batchelor (1946-1962) • A. A. Townsend (1947-) • J. Rotta (1951) • E. Hopf (1952) • R. E. Kraichnan (1953) • J. Laufer (1954) • P. S. Klebanoff (1955) |
| <ul style="list-style-type: none"> • B. I. Davidov (1961) • S. Corrsin (1942 - 1985) • L. G. Kovaszny (1959 - 1980) • P. Bradshaw (1965 -) • F. H. Harlow (1965) • B. Spalding (1965 - 1975) • S. Kline • W. C. Reynolds • W. Rundstadler | } | (1967) | <ul style="list-style-type: none"> • J. L. Lumley (1967 -) • J. W. Deordorff (1970) • S. A. Orszag (1972) • U. Schumann (1973) • R. S. Rogallo (1981) |

Turbulence decomposition suggested by O. Reynolds (1895):

$$U_i = \bar{U}_i + u_i, \quad P = \bar{P} + p$$

when applied to the Navier-Stokes equations leads to the closure problem

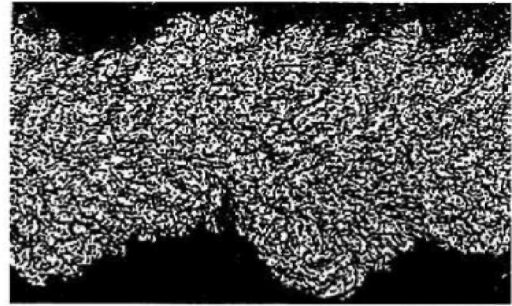
$$\begin{aligned} \bullet \quad \frac{\partial \bar{U}_i}{\partial t} + \bar{U}_k \frac{\partial \bar{U}_i}{\partial x_k} &= -\frac{1}{\rho} \frac{\partial \bar{P}}{\partial x_i} + \frac{\partial}{\partial x_k} \left(\nu \frac{\partial \bar{U}_i}{\partial x_k} - \underbrace{\bar{u}_i u_k}_? \right), \quad \frac{\partial \bar{U}_i}{\partial x_i} = 0 \\ \bullet \quad \frac{\partial \bar{u}_i \bar{u}_j}{\partial t} + \bar{U}_k \frac{\partial \bar{u}_i \bar{u}_j}{\partial x_k} &= -\bar{u}_j \bar{u}_k \frac{\partial \bar{U}_i}{\partial x_k} - \bar{u}_i \bar{u}_k \frac{\partial \bar{U}_j}{\partial x_k} - \underbrace{\frac{\partial \bar{u}_i \bar{u}_j \bar{u}_k}{\partial x_k}}_{T_{ij} ?} - \frac{1}{\rho} \left(\bar{u}_j \frac{\partial \bar{P}}{\partial x_i} + \bar{u}_i \frac{\partial \bar{P}}{\partial x_j} \right) - \underbrace{2\nu \frac{\partial \bar{u}_i}{\partial x_k} \frac{\partial \bar{u}_j}{\partial x_k}}_{\Pi_{ij} ?} + \nu \frac{\partial^2 \bar{u}_i \bar{u}_j}{\partial x_k \partial x_k} \\ \bullet \quad \frac{\partial \bar{u}_i \bar{u}_j \bar{u}_\ell}{\partial t} + \bar{U}_k \frac{\partial \bar{u}_i \bar{u}_j \bar{u}_\ell}{\partial x_k} &= \bar{u}_i \bar{u}_j \frac{\partial \bar{u}_\ell}{\partial x_k} + \bar{u}_j \bar{u}_\ell \frac{\partial \bar{u}_i}{\partial x_k} + \bar{u}_i \bar{u}_\ell \frac{\partial \bar{u}_j}{\partial x_k} - \bar{u}_j \bar{u}_i \bar{u}_k \frac{\partial \bar{U}_i}{\partial x_k} - \bar{u}_i \bar{u}_j \bar{u}_k \frac{\partial \bar{U}_\ell}{\partial x_k} - \bar{u}_\ell \bar{u}_i \bar{u}_k \frac{\partial \bar{U}_j}{\partial x_k} \\ &\quad - \underbrace{\frac{\partial \bar{u}_i \bar{u}_j \bar{u}_\ell \bar{u}_k}{\partial x_k}}_{T_{ij\ell} ?} - \frac{1}{\rho} \left(\bar{u}_\ell \bar{u}_j \frac{\partial \bar{P}}{\partial x_i} + \bar{u}_\ell \bar{u}_i \frac{\partial \bar{P}}{\partial x_j} + \bar{u}_i \bar{u}_j \frac{\partial \bar{P}}{\partial x_\ell} \right) - \underbrace{2\nu \left(\bar{u}_i \frac{\partial \bar{u}_j}{\partial x_k} \frac{\partial \bar{u}_\ell}{\partial x_k} + \bar{u}_j \frac{\partial \bar{u}_i}{\partial x_k} \frac{\partial \bar{u}_\ell}{\partial x_k} + \bar{u}_\ell \frac{\partial \bar{u}_i}{\partial x_k} \frac{\partial \bar{u}_j}{\partial x_k} \right)}_{\Pi_{ij\ell} ?} + \nu \frac{\partial^2 \bar{u}_i \bar{u}_j \bar{u}_\ell}{\partial x_k \partial x_k} \end{aligned}$$

Kolmogorov's two-equation model of turbulence

$$\frac{D\bar{v}_i}{Dt} = F_i - \frac{\partial}{\partial x_i} \left(\frac{\bar{p}}{\rho} + b \right) + A \sum_j \frac{\partial}{\partial x_j} \left[\frac{b}{\omega} \left(\frac{\partial \bar{v}_i}{\partial x_j} + \frac{\partial \bar{v}_j}{\partial x_i} \right) \right]$$

$$\frac{D\omega}{Dt} = -\frac{7}{11}\omega^2 + A' \sum_j \frac{\partial}{\partial x_j} \left[\frac{b}{\omega} \frac{\partial \omega}{\partial x_j} \right]$$

$$\frac{Db}{Dt} = -b\omega + \frac{A}{3} \frac{b}{\omega} \epsilon + A'' \sum_j \frac{\partial}{\partial x_j} \left[\frac{b}{\omega} \frac{\partial \epsilon}{\partial x_j} \right]$$

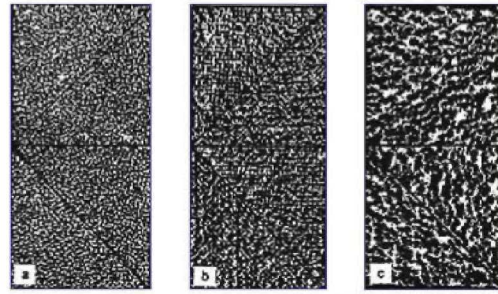


Corrsin and Kistler (1964)

Flow visualisation of small-scale structure of turbulence at large Re

The missing source term in the ω equation:

One of the central unresolved issues in the formulation of the closure approximations involved in the dynamic equations for the turbulent dissipation rate is related to the early work on turbulence theory reported by Kolmogorov (1942). In his pioneering paper, which nowadays stands as a pattern for the two-equation model of turbulence, he omitted the production terms in the equation for the characteristic frequency ω of the energy-containing range, which served for determination of the turbulent dissipation rate.



Tennekes and Lumley (1972)

(a) Isotropic pattern, (b) and (c) are anisotropic patterns

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ON VELOCITY CORRELATIONS AND TUE SOLUTIONS OF THE EQUATIONS OF TURBULENT FLUCTUATLON*

BY

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$$\frac{\partial \bar{U}_i}{\partial t} + \bar{U}^j \bar{U}_{i,j} = -\frac{1}{\rho} \bar{p}_{,i} + \frac{1}{\rho} \tau_{i,j}^j + \nu \nabla^2 \bar{U}_i, \quad \bar{U}^j_{,j} = 0$$

$$-\frac{1}{\rho} \frac{\partial \tau_{ik}}{\partial t} - \frac{1}{\rho} (\bar{U}_{i,j} \tau_{ik}^j + \bar{U}_{k,j} \tau_{ik}^j) - \frac{1}{\rho} \bar{U}^j \tau_{ik,j} + (\overline{w^j w_i w_k})_{,j} = -a_{mik}^n \bar{U}_{,n}^m - b_{ik} - \frac{\nu}{\rho} \nabla^2 \tau_{ik} + \frac{2\nu}{3\lambda^2} (k-5) q^2 g_{ik} - \frac{2\nu k}{\lambda^2} \overline{w_i w_k},$$

$$5 \frac{\partial}{\partial t} \left(\frac{q^2}{\lambda^2} \right) + 5 \bar{U}^j \frac{\partial}{\partial x^j} \left(\frac{q^2}{\lambda^2} \right) - \frac{14G}{\lambda^2} \bar{U}_{i,k} \overline{w^i w^k} - \frac{70F}{3\sqrt{3}} \frac{q^3}{\lambda^3} = -\frac{2\nu}{3} E \frac{q^2}{\lambda^4},$$

$$\frac{\partial}{\partial t} \overline{w_i w_k w_l} + \bar{U}_{i,j} \overline{w^j w_k w_l} + \bar{U}_{k,j} \overline{w^j w_l w_i} + \bar{U}_{l,j} \overline{w^j w_i w_k} + \bar{U}^j (\overline{w_i w_k w_l})_{,j} + (\overline{w^j w_i w_k w_l})_{,j} =$$

$$-b_{mikl}^n \bar{U}_{,n}^m - c_{ikl} + \frac{1}{\rho^2} (\tau_{i,j}^j \tau_{kl} + \tau_{k,j}^j \tau_{li} + \tau_{l,j}^j \tau_{ki}) + \nu g^{mn} (\overline{w_i w_k w_l})_{,mn},$$

Reference	Flow	Reynolds number	Reference	Flow	Reynolds number
Rogallo (1981)	Homogeneous turbulence		Kim, McIn & Moser (1987)	Channel flow	$R_\tau \approx 3250$
Lee (1985)	Plain strain (B2D1,B2D2,B2D3 and B2D4)	$R_\lambda \approx 28-40$	Antonia <i>et al.</i> (1992)	Channel flow	$R_\tau \approx 7880$
	Axisymmetric contraction (CD11,CD12,CD13, CD14,CD21,CD22, CD23 and CD24)	$R_\lambda \approx 10-20$	Gilbert & Kleiser (1991)	Channel flow	$R_\tau \approx 3830$
	Shear (BSH9,BSH10, BSH11and BSH12)	$R_\lambda \approx 40-120$	Kasagi <i>et al.</i> (1990)	Channel flow	$R_\tau \approx 1740, 2680, 3240$
	Rotation (BR1,BR2,BR3, BR4 and BR6)	$R_\lambda \approx 13-18$	Moser, Kim & Mansour (1998)	Channel flow	$R_\tau \approx 12500$
	Relaxation to isotropy (RX11A,.....RX24A, RX11C,.....RX24C, RX11F,.....RX24F)	$R_\lambda \approx 7-22$	Eggels <i>et al.</i> (1994)	Pipe flow	$R_\tau \approx 6950$
			Eggels, Boersma	Rotating pipe flow	$R_\tau \approx 5300, 5575, 5860$
			& Nieuwstadt (1994)		$N = 0., 0.32, 0.61$
			Orlandi & Fatica (1997)	Rotating pipe flow	$R_\tau \approx 5000$
					$N = 0., 0.5, 1.0, 2.0$
			Spalart (1988)	Boundary layer	$R_\theta \approx 300, 670, 1410$
			Spalart (1986)	Sink flow	$R_\theta \approx 380, 415, 690$
			Le & McIn (1994)	Backward-facing step	$R_\tau \approx 5100$
			Rogers & Moser (1994)	Plane mixing layer	$R_\tau \approx 20000$
			Ye <i>et al.</i> (1996)	Rayleigh-Bénard convection	$R_\lambda \approx 8-47$ $P_r \approx 0.006-0.7$

These databases contain complete three-dimensional random flow fields from which it is possible to extract any information required for checking physical ideas and fundamental assumptions that are used in the development of turbulence closure.

The stress equation reads:

$$\frac{\partial \overline{u_i u_j}}{\partial t} + \overline{U_k} \frac{\partial \overline{u_i u_j}}{\partial x_k} \cong P_{ij} + a_{ij} P_{ss} + \mathcal{F} \left(\frac{1}{3} P_{ss} \delta_{ij} - P_{ij} \right) + (C - 2A\epsilon_h) a_{ij} - \frac{2}{3} \epsilon_h \delta_{ij} \\ + c_q \frac{\partial \overline{u_i u_j}}{\partial x_k} \frac{k^2}{q^2} \frac{1}{\epsilon_h} J \frac{\partial k}{\partial x_k} + \frac{1}{2} \nu \frac{\partial^2 \overline{u_i u_j}}{\partial x_k \partial x_k}$$

The dissipation equation can be approximated as:

$$\frac{\partial \epsilon_h}{\partial t} + \overline{U_k} \frac{\partial \epsilon_h}{\partial x_k} \cong -2A \frac{\epsilon_h \overline{u_i u_k}}{k} \frac{\partial \overline{U_i}}{\partial x_k} - \psi \frac{\epsilon_h^2}{k} + c_\epsilon \frac{\partial}{\partial x_k} \frac{k^2}{\epsilon_h} J \frac{\partial \epsilon_h}{\partial x_k} + \frac{1}{2} \nu \frac{\partial^2 \epsilon_h}{\partial x_k \partial x_k}$$

$$A \approx 1 + \underbrace{\left\{ 1 - 9 \left[\frac{1}{2} \Pi_a - \text{III}_a \right] \right\}}_J (\mathcal{W} - 1)$$

$$\mathcal{F} \approx \frac{3}{5} + \frac{18}{5} \left(\frac{1}{2} \Pi_a - \text{III}_a \right)$$

$$C \approx \left[1 - 9 \left(\frac{1}{2} \Pi_a - \text{III}_a \right) \right] (4.78 \mathcal{W} - 4.78) \epsilon_h$$

$$\psi \approx (1 - F) (\psi)_{2C} + F (\psi)_{\text{axi}}$$

$$F = \frac{1 - 9 \left(\frac{1}{2} \Pi_a - \text{III}_a \right)}{1 - 9 \left[\frac{3}{4} \left(\frac{4}{3} \text{III}_a \right)^{2/3} - \text{III}_a \right]}$$

$$(\psi)_{2C} \approx \frac{\sqrt{5}}{25} R_\lambda \mathcal{W} + 2(1 - \mathcal{W})$$

$$(\psi)_{\text{axi}} \approx \left\{ 1 - 9 \left[\frac{3}{4} \left(\frac{4}{3} \text{III}_a \right)^{2/3} - \text{III}_a \right] \right\} (1.8 - 0.4 \mathcal{W}), \quad \text{III}_a \geq 0$$

$$(\psi)_{\text{axi}} \approx 2.5 - \left\{ 1 - 9 \left[\frac{3}{4} \left(\frac{4}{3} \text{III}_a \right)^{2/3} - \text{III}_a \right] \right\} (0.7 + 0.5 \mathcal{W}), \quad \text{III}_a \leq 0$$

$$\frac{\lambda}{L} \approx -0.0489 R_\lambda + \frac{1}{2} (0.00956 R_\lambda^2 + 10.186)^{1/2}$$

$$\mathcal{W} = 0.626 \frac{\lambda}{r}$$

$$c_\epsilon \approx 0.09$$

The stress equations for a fully developed channel flow:

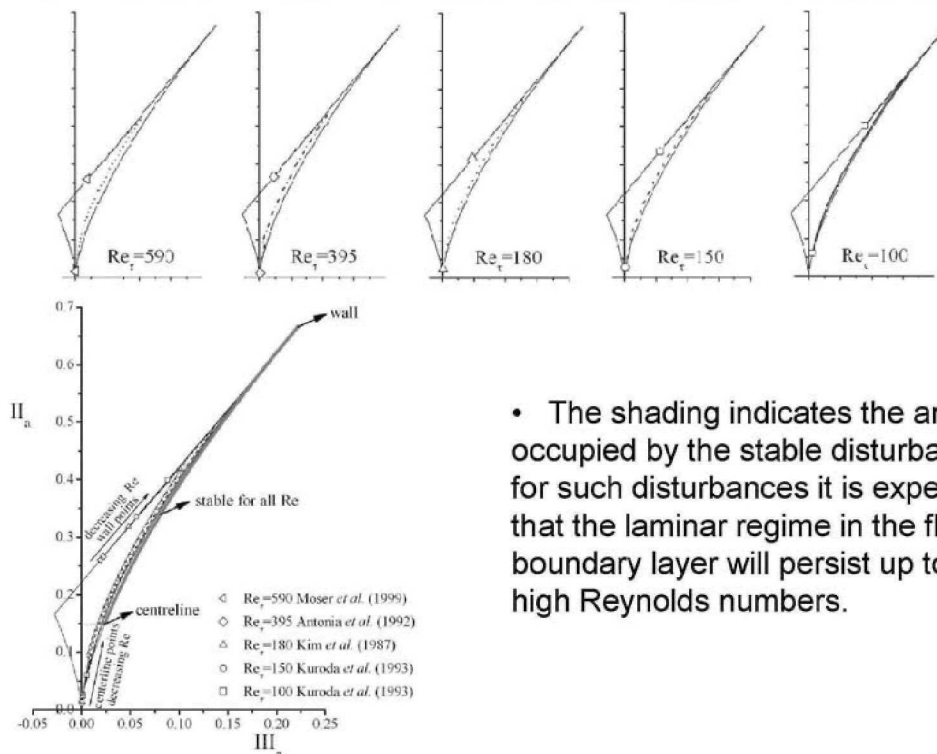
$$\frac{\partial \overline{u_1^2}}{\partial t} \simeq P_{11} + a_{11}P_{ss} + \mathcal{F}\left(\frac{1}{3}P_{ss} - P_{11}\right) + (C - 2A\epsilon_h)a_{11} - \frac{2}{3}\epsilon_h - \frac{\partial}{\partial x_2} \frac{\overline{u_1^2}}{q^2} \overline{u_s u_s u_2} + \frac{1}{2}\nu \frac{\partial^2 \overline{u_1^2}}{\partial x_2^2}$$

$$\frac{\partial \overline{u_2^2}}{\partial t} \simeq a_{22}P_{ss} + \frac{1}{3}\mathcal{F}P_{ss} + (C - 2A\epsilon_h)a_{22} - \frac{2}{3}\epsilon_h - \frac{\partial}{\partial x_2} \frac{\overline{u_2^2}}{q^2} \overline{u_s u_s u_2} + \frac{1}{2}\nu \frac{\partial^2 \overline{u_2^2}}{\partial x_2^2}$$

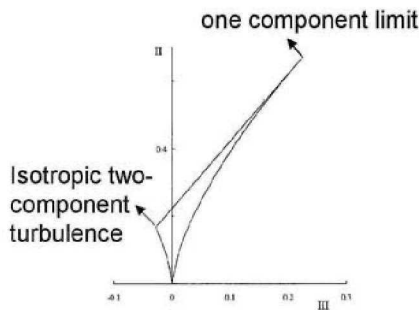
$$\frac{\partial \overline{u_3^2}}{\partial t} \simeq a_{33}P_{ss} + \frac{1}{3}\mathcal{F}P_{ss} + (C - 2A\epsilon_h)a_{33} - \frac{2}{3}\epsilon_h - \frac{\partial}{\partial x_2} \frac{\overline{u_3^2}}{q^2} \overline{u_s u_s u_2} + \frac{1}{2}\nu \frac{\partial^2 \overline{u_3^2}}{\partial x_2^2}$$

$$\frac{\partial \overline{u_1 u_2}}{\partial t} \simeq P_{12} + a_{12}P_{ss} - \mathcal{F}P_{12} + (C - 2A\epsilon_h)a_{12} - \frac{\partial}{\partial x_2} \frac{\overline{u_1 u_2}}{q^2} \overline{u_s u_s u_2} + \frac{1}{2}\nu \frac{\partial^2 \overline{u_1 u_2}}{\partial x_2^2}$$

Away from the wall the system resembles the statistical dynamics of initially isotropic turbulence strained by axisymmetric expansion.



- The shading indicates the area occupied by the stable disturbances: for such disturbances it is expected that the laminar regime in the flat plate boundary layer will persist up to very high Reynolds numbers.

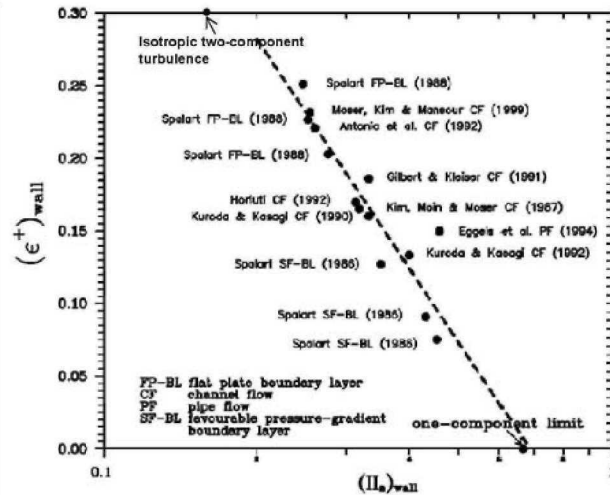


Expansion of velocity fluctuations near the wall:

$$u_1 = a_1 x_2 + a_2 x_2^2 + a_3 x_2^3 + \dots$$

$$u_2 = b_2 x_2^2 + b_3 x_2^3 + \dots$$

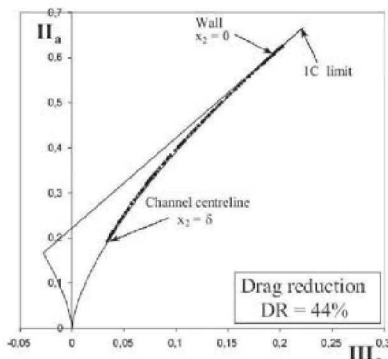
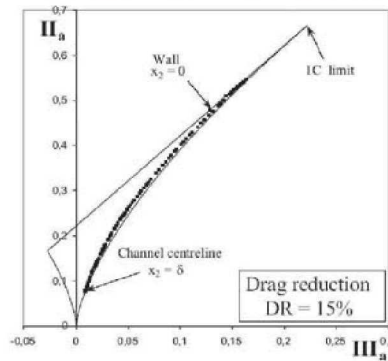
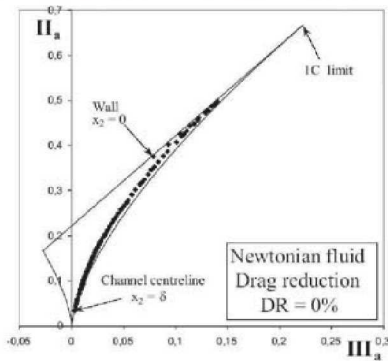
$$u_3 = c_1 x_2 + c_2 x_2^2 + c_3 x_2^3 + \dots$$



Numerical data bases confirm that ϵ vanishes as the one-component state is approached

- Requesting that $\overline{u_i u_j}$ and $\overline{\epsilon_{ij}}$ are statistically axisymmetric we find that

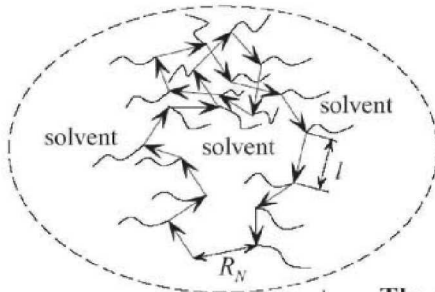
$$a_1, b_2, c_1, \dots, a_n, b_{n+1}, c_n \rightarrow 0 \quad \text{and} \quad k = \frac{1}{2} \frac{(\epsilon)_{\text{wall}}}{\nu} x_2, \quad (\epsilon)_{\text{wall}} = \nu (a_1^2 + c_1^2) \rightarrow 0 \quad \text{as} \quad x_2 \rightarrow 0$$



The trend in the data at the wall strongly support the conclusion that DR increases as turbulence approaches the one component limit.

The polymer molecule in solution at equilibrium

→ monomer of length l N monomers of length l



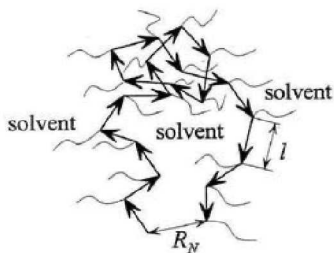
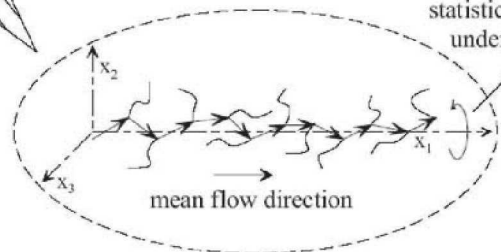
$$R_F = N^{3/5} l$$

$$(\tau_{zmm})_{pol} = \frac{\eta_s R_F^3}{k_B T}$$

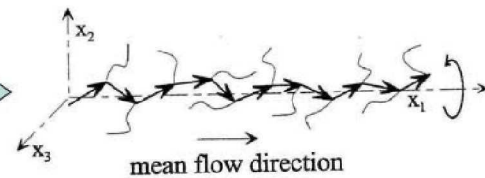
η_s - the solvent viscosity
 k_B - Boltzmann constant
 T - absolute temperature

The stretched polymer molecule in the near-wall region of turbulent pipe flow

$$(\tau)_{pol} \geq (\tau)_{tur}$$



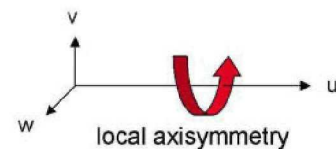
$$\tau_{tur} \leq \tau_{pol}$$



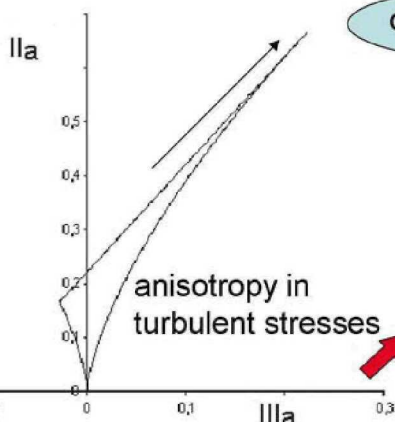
conceptual scenario

restructuring
of small
scale
turbulence

at the wall



anisotropy in length
scales



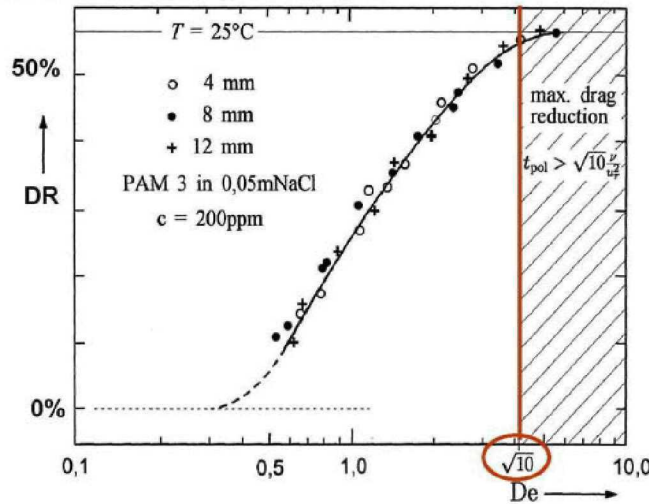
Theoretical Prediction

$t_{tur} \approx t_K \leq t_{pol}$
 $(t_K)_{wall} = \frac{\eta_K^2}{D} \approx \sqrt{10} \frac{D}{u_c^2}$

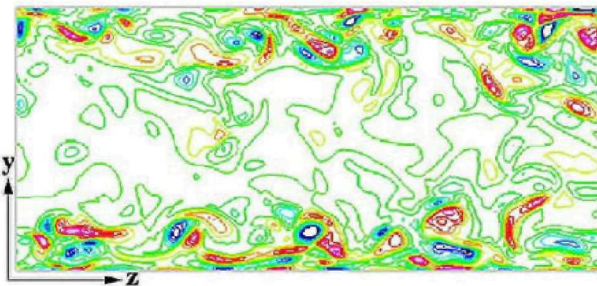
max DR for $t_{tur} \approx t_K \leq t_{pol}$

Deborah number $De(DR_{max}) \geq \sqrt{10}$

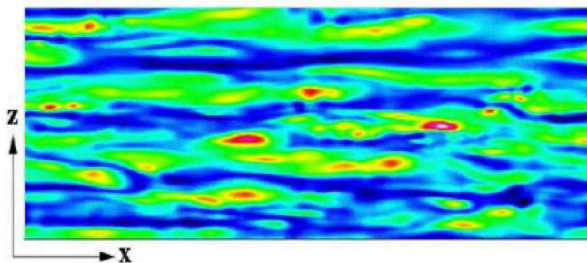
Experimental Results (Durst et al. 1982)



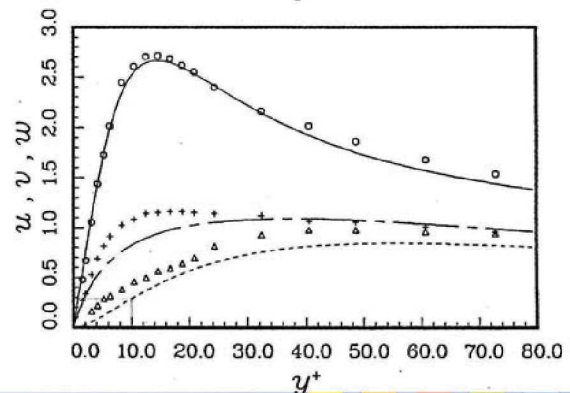
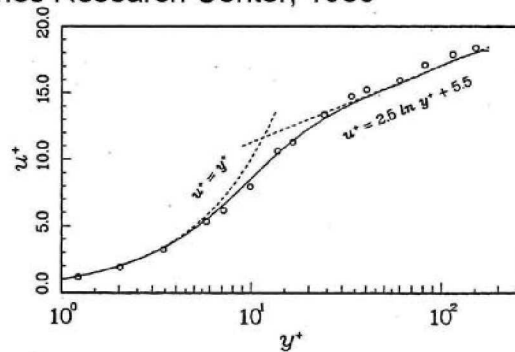
Kim, Moin and Moser, Nasa Ames Research Center, 1986



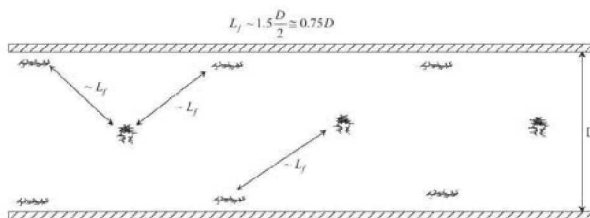
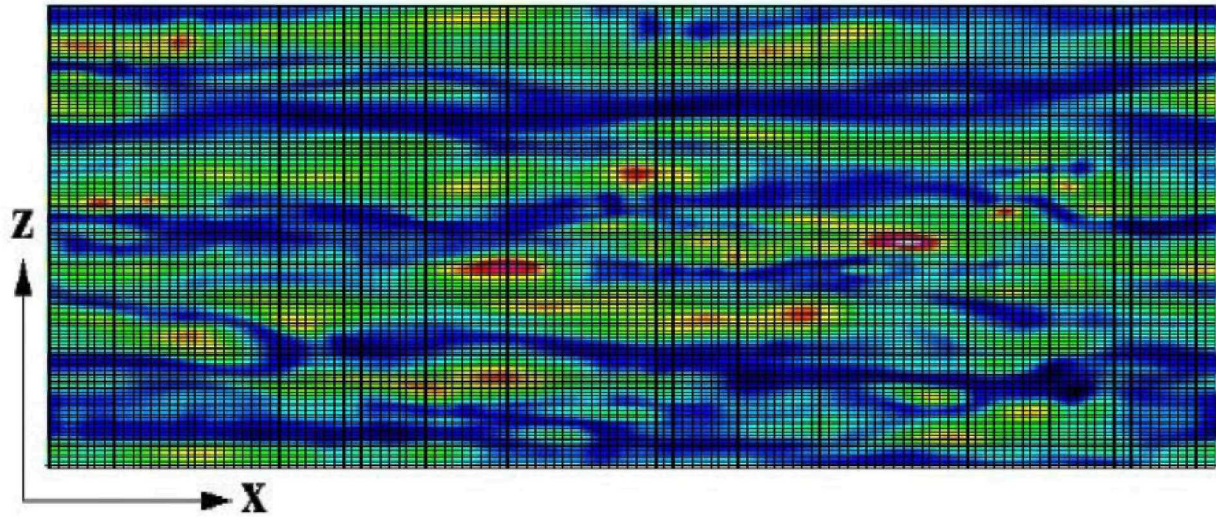
Color contours of the streamwise vorticity in the direct numerical simulations of fully developed channel flow



Color shades of the skin friction in the direct numerical simulations of fully developed channel flow



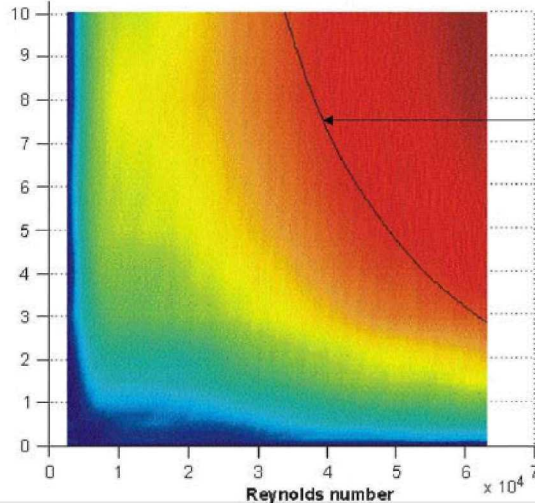
Kim, Moin and Moser, Nasa Ames Research Center, 1986



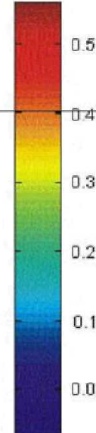
Interaction between polymer and turbulence in dissipation range (η_k):

$$\frac{c_{POL}}{V} \approx \left(\frac{\eta_K}{L_j} \right)^3 \quad Re \uparrow \Rightarrow \frac{c}{V} \downarrow$$

Concentration PPM



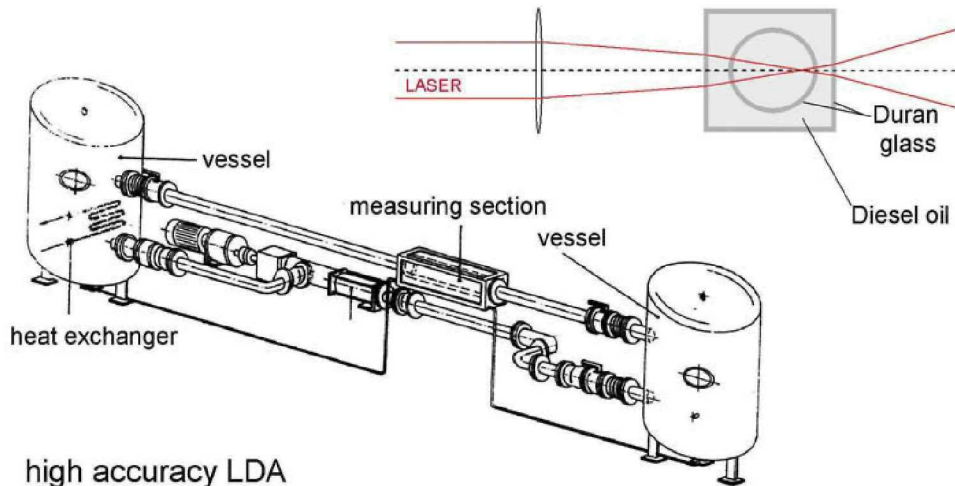
DR-effect



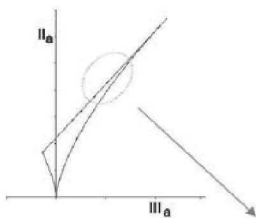
prediction of polymer concentration for max DR

Tilli et al. 2003, PAA

refractive index matched pipe flow facility

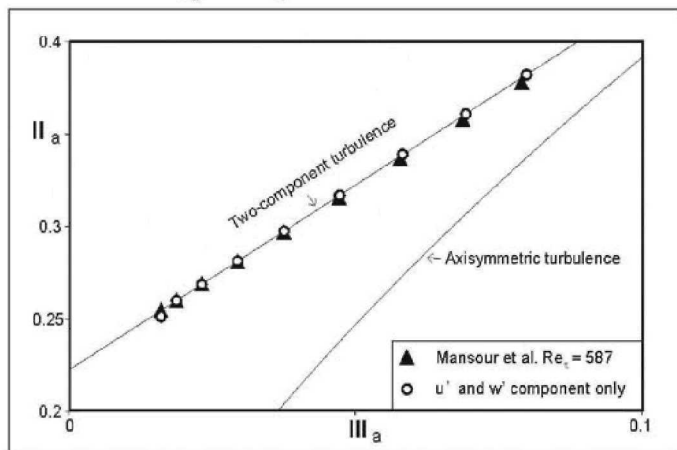


high accuracy LDA measurements in the viscous sublayer, $y=150\mu\text{m}$



Anisotropy tensor

$$a_{ij} = \frac{\overline{u_i u_j}}{q^2} - \frac{1}{3} \delta_{ij}$$



for points in viscous sublayer a_{ij} can be based on **u' and w' component** only

Drag Reduction DR

$$DR = 1 - \frac{\tau_{w,pol}}{\tau_w}$$

$$\tau_w = \mu \frac{\partial U}{\partial x}$$

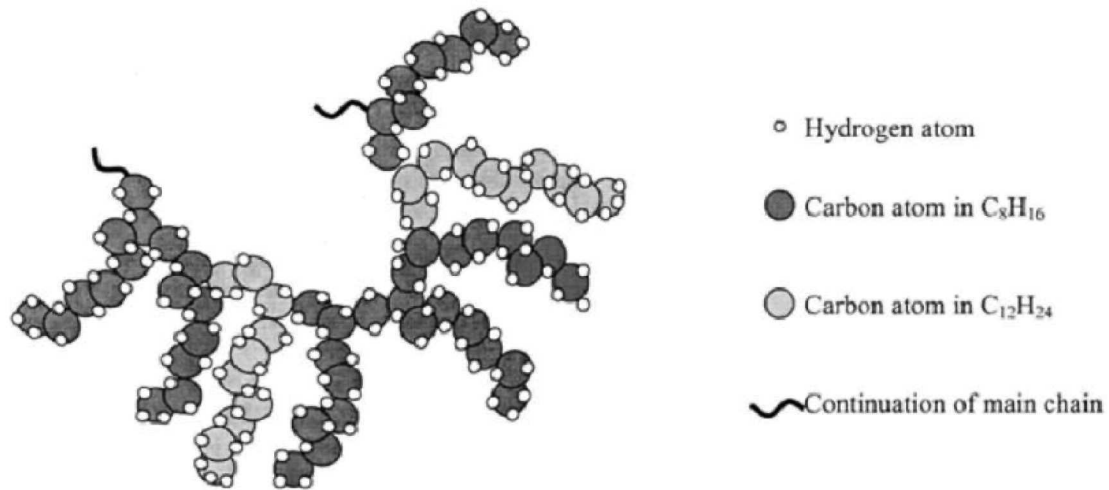
in viscous sublayer it holds:

$$y^+ = U^+$$

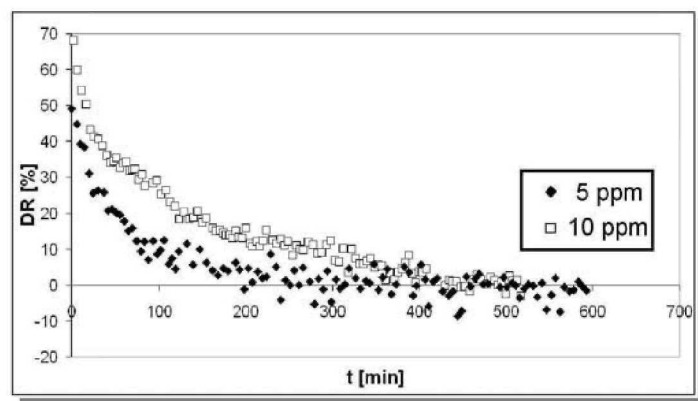
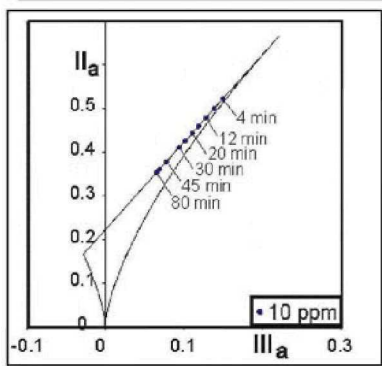
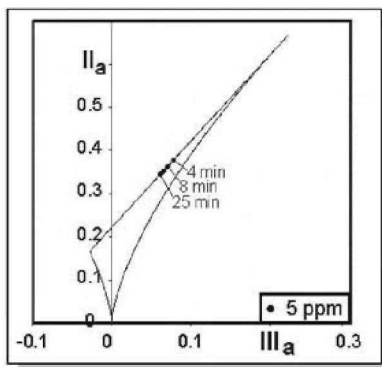
$$y = C \cdot U$$

measure **mean velocity U** in one point of viscous sublayer

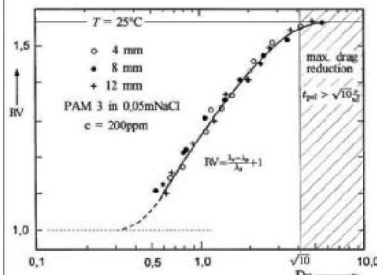
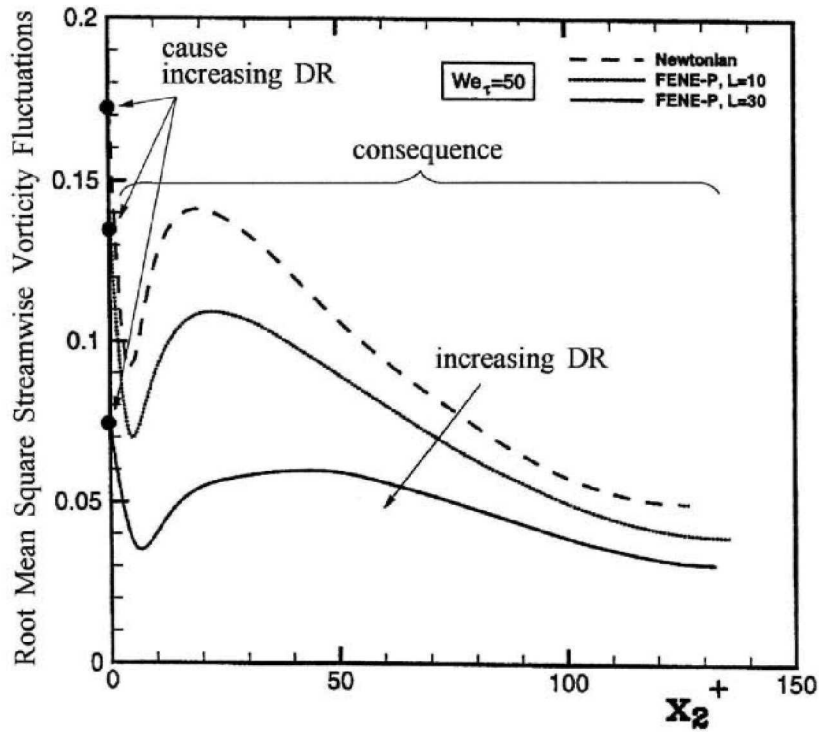
Illustration of the molecular structure of a FORTUM polymer sample



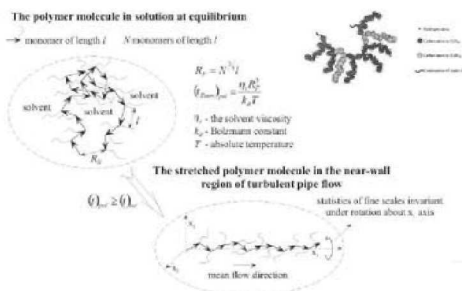
$$M \approx 25 \times 10^6 \text{ g mol}^{-1}, M_{\text{dodecane}} = 168.4320 \text{ g mol}^{-1}, M_{\text{octane}} = 112.2880 \text{ g mol}^{-1}, l = 2 \times 1.54 \text{ \AA}, r_{d/o} = C_{12}H_{24}/C_8H_{16} = 1/3, N_{\text{monomer}} = M_{\text{polymer}} / [r_{d/o}M_{\text{octane}} + (1 - r_{d/o})M_{\text{dodecane}}].$$



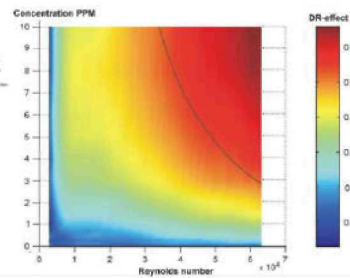
Anisotropy decreases with the degradation of the polymer



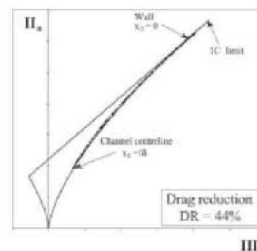
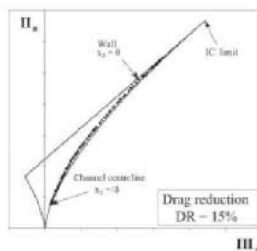
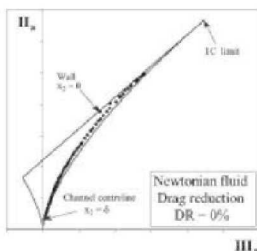
Drag reduction versus a polymer time scale



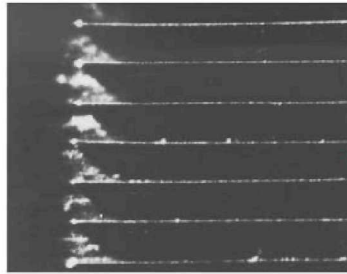
Behaviour of a polymer in a solution at equilibrium and its response to stretching by turbulent motions at small scales very close to the wall



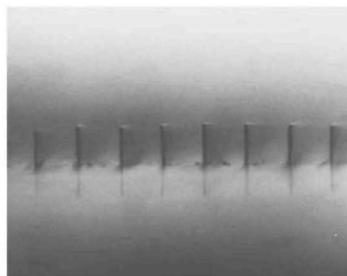
The optimum concentration of a polymer



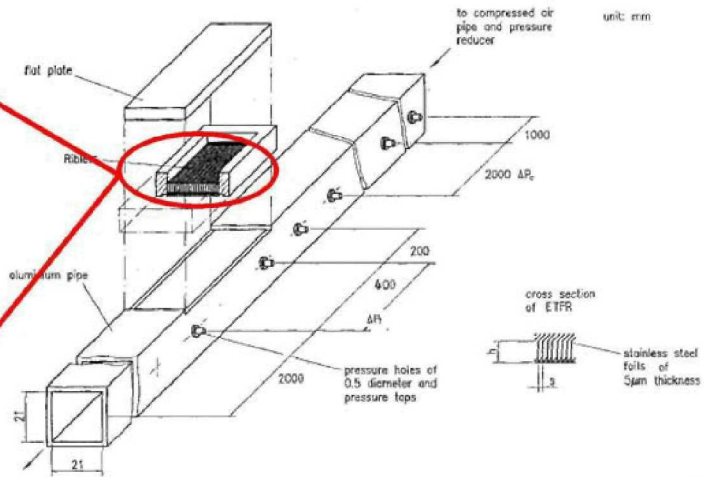
Anisotropy invariant mapping of turbulence in a channel flow with drag reduction



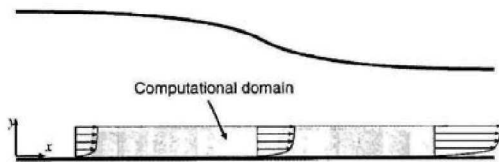
Top view of riblets



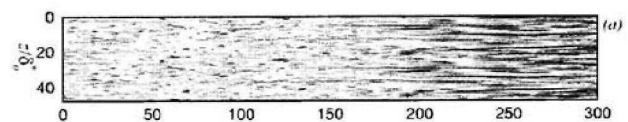
Front view of riblets



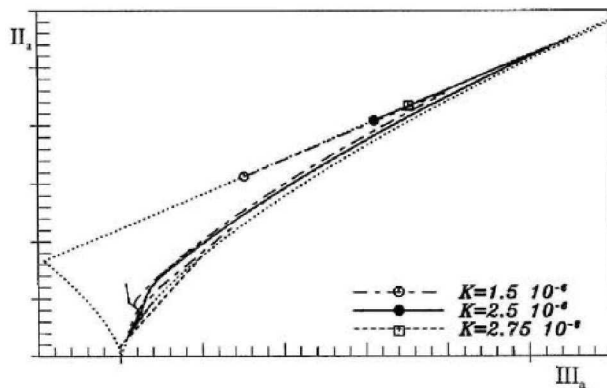
Schematic drawing of test section facility



Sketch of the physical configuration



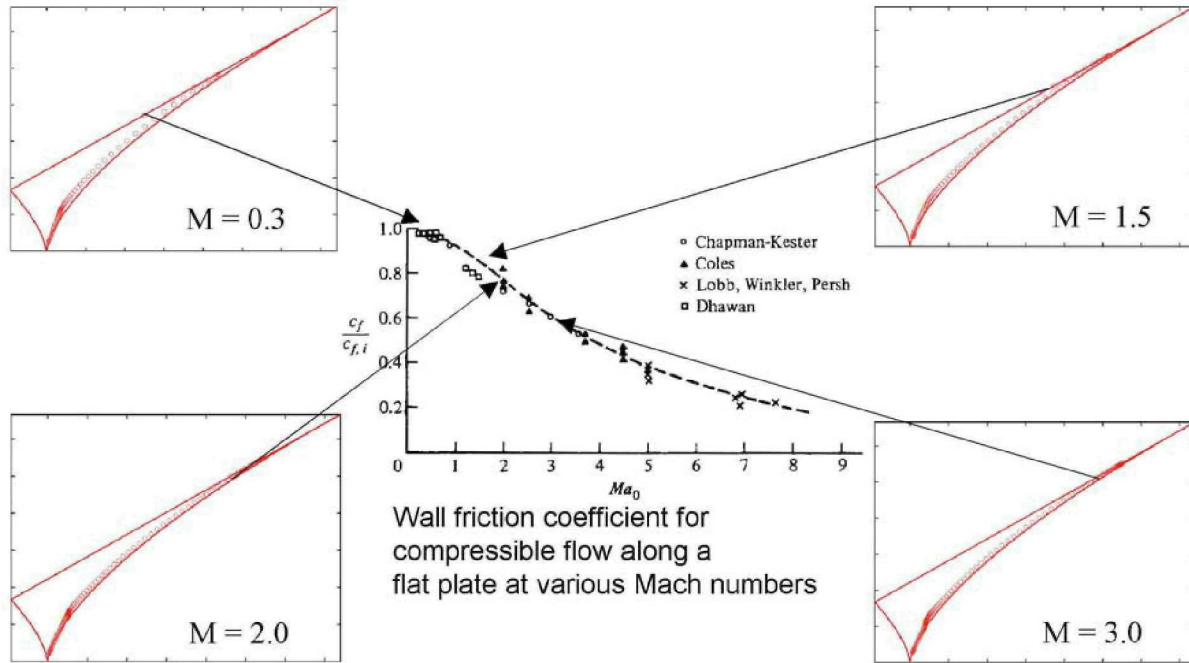
Instantaneous streamwise velocity fluctuations



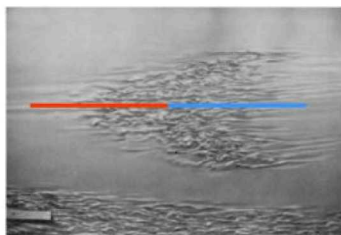
$$K = \frac{\nu}{U_\infty^2} \frac{dU_\infty}{dx}$$

$$(K)_{crit} \geq 3.75 \times 10^{-6}$$

Traces of the joint variations of the invariants for a turbulent boundary layer developing under favorable pressure gradient



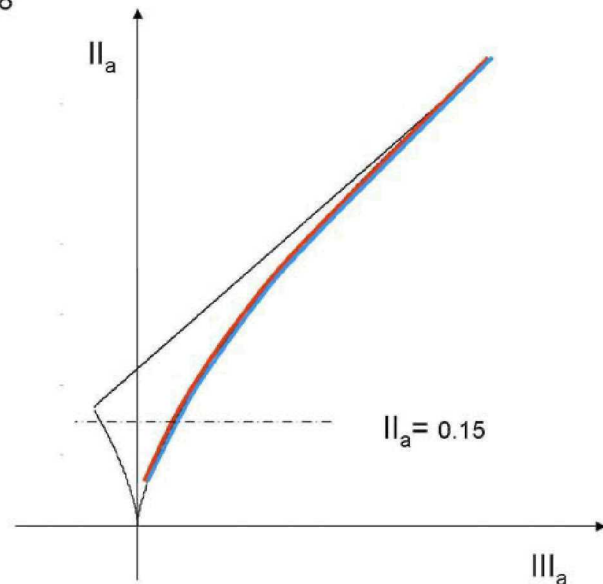
Cantwell, Coles, Dimotakis JFM 87, 1978



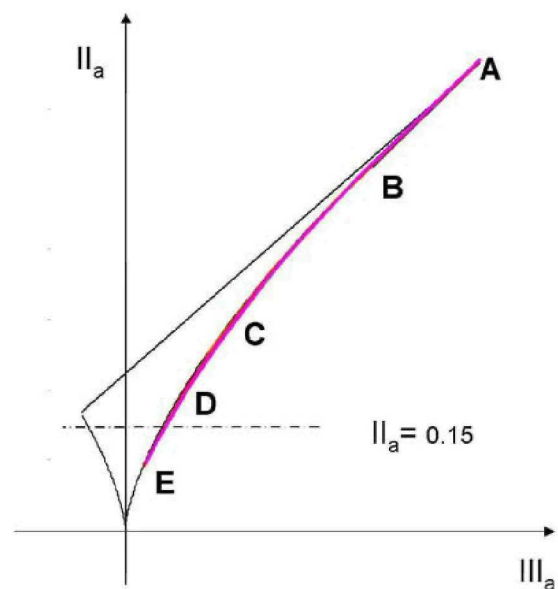
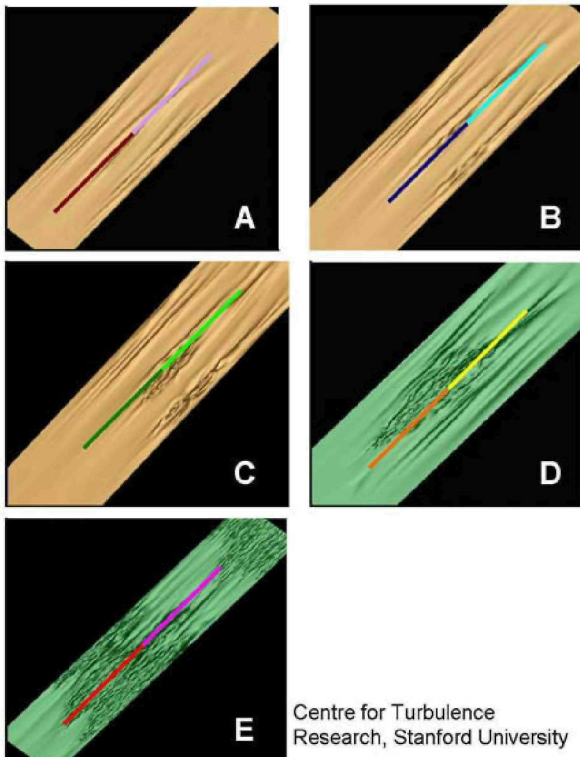
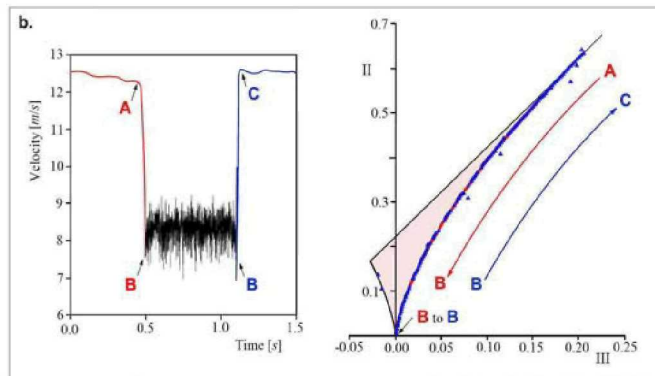
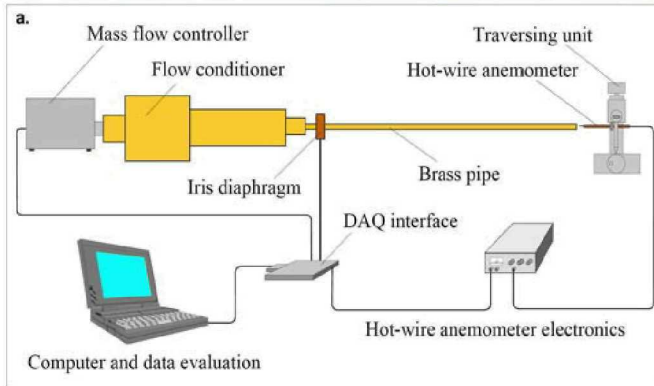
low Reynolds number



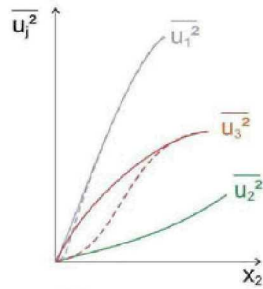
high Reynolds number



Note that transition and breakdown to turbulence is associated with decrease of anisotropy at the front side of the spot and laminarization process proceeds with increase of the anisotropy at the trailing side of the spot.



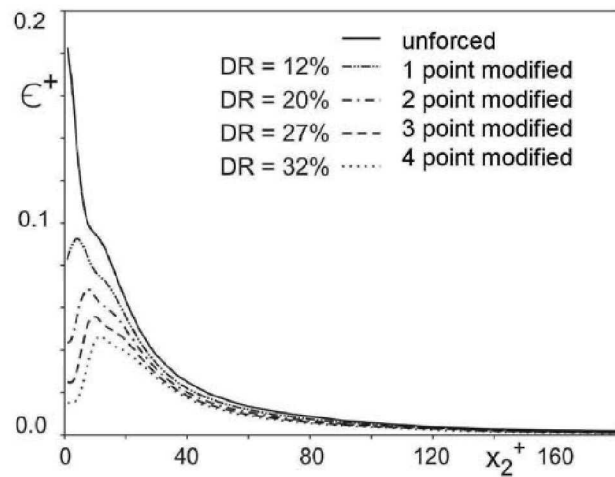
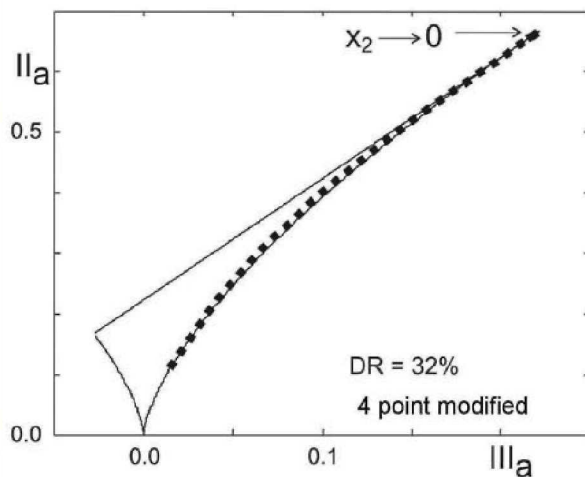
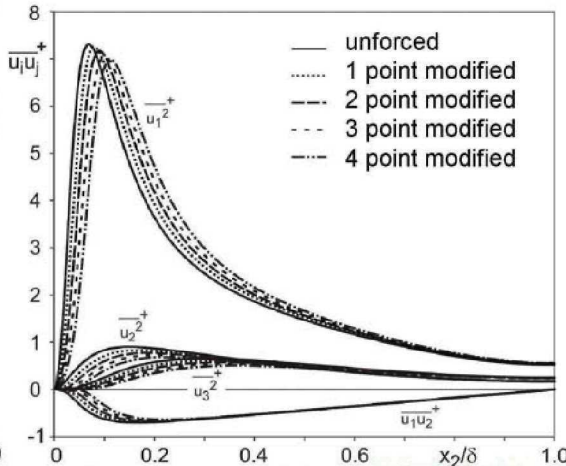
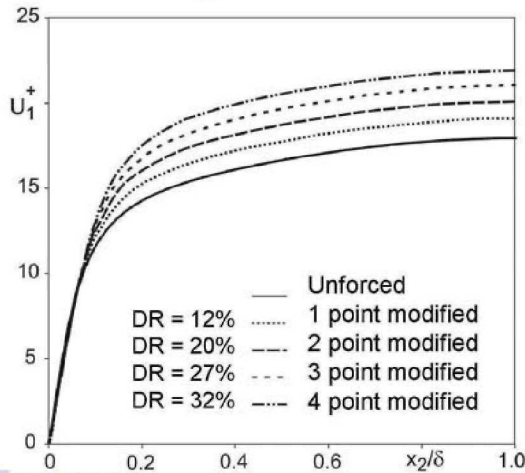
Centre for Turbulence Research, Stanford University



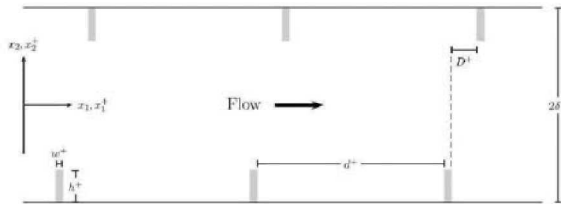
Channel Flow ($Re_\tau = 180$) with artificial boundary conditions:
Points in the viscous sub layer were modified: $u_3 \rightarrow u_2$

→ τ_w takes on the following

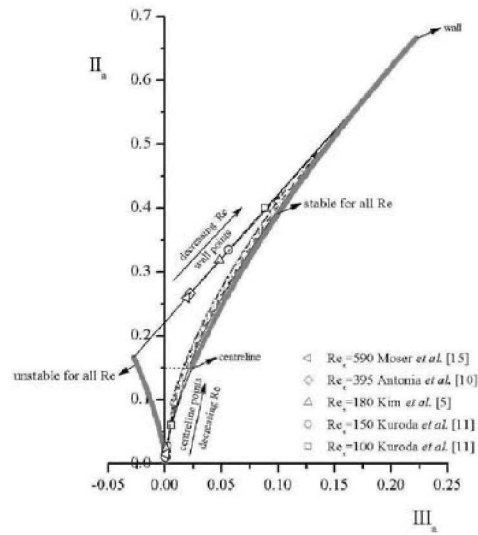
$$DR = 1 - \left(\frac{\tau_w}{(\tau_w)_{unforced}} \right)$$



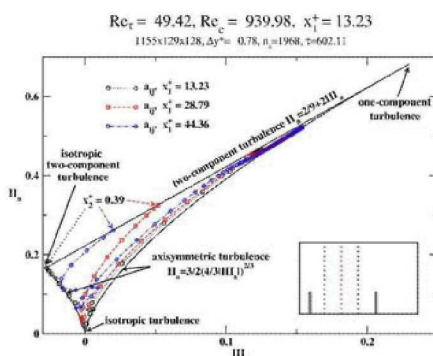
Small variations near the wall lead to significant drag reduction



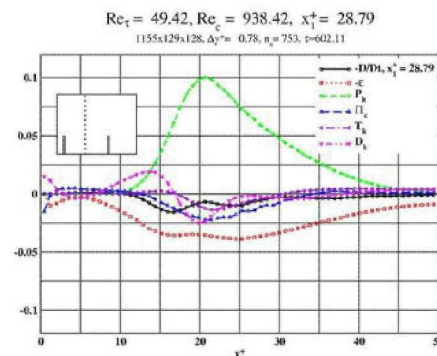
Configuration of the roughness elements mounted at the walls of a plane channel flow



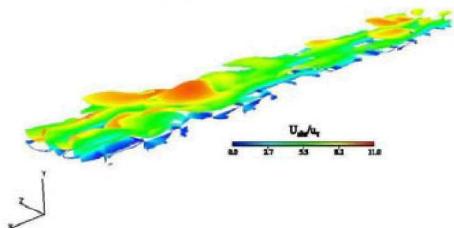
Anisotropy invariant mapping of turbulence in a plane channel flow at low Reynolds numbers



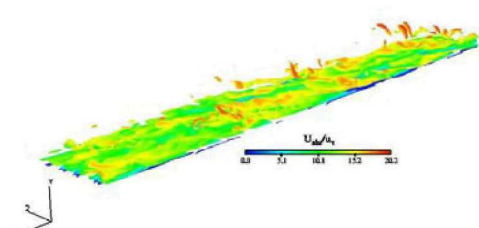
Development of turbulence across the anisotropy invariant map



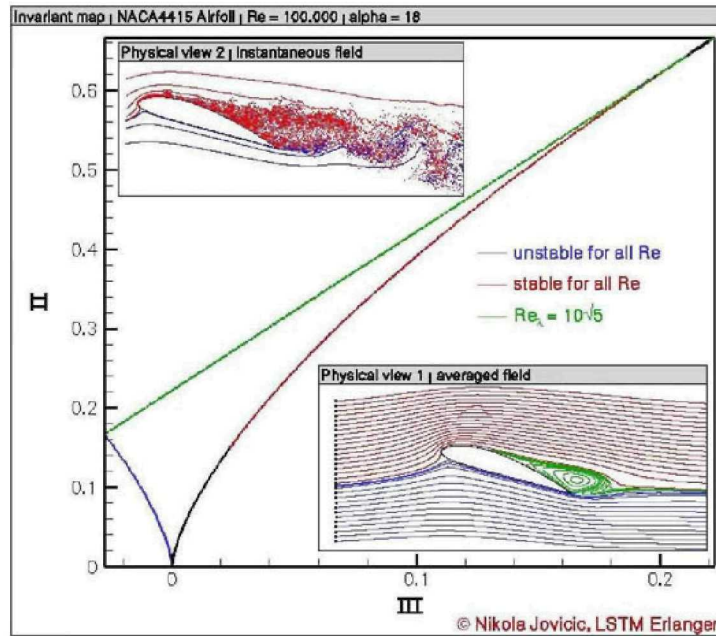
Terms contributing to the balance of the energy equation



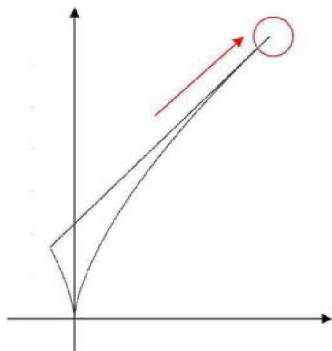
Isosurface of instantaneous vorticity at $Re = 940$



Isosurface of instantaneous vorticity at $Re = 6600$

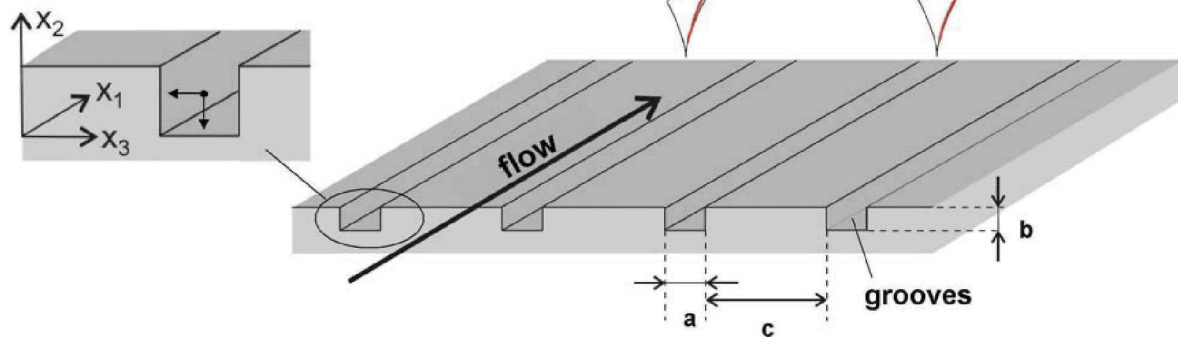


To start the video, click on the picture!



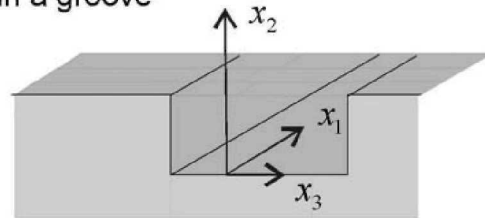
scientific goal and “engineering dream”:
Realize one-component limit at the wall and obtain very high DR

one possible technical realization:
channel flow with surface modification



Basic equations for fully developed flow in a groove

$$\frac{\partial \bar{U}_2}{\partial x_2} + \frac{\partial \bar{U}_3}{\partial x_3} = 0$$



$$\bar{U}_2 \frac{\partial \bar{U}_1}{\partial x_2} + \bar{U}_3 \frac{\partial \bar{U}_1}{\partial x_3} = -\frac{1}{\rho} \frac{\partial \bar{P}}{\partial x_1} - \frac{\partial \overline{u_1 u_2}}{\partial x_2} - \frac{\partial \overline{u_1 u_3}}{\partial x_3} + \nu \left(\frac{\partial^2 \bar{U}_1}{\partial x_2^2} + \frac{\partial^2 \bar{U}_1}{\partial x_3^2} \right) \quad (1)$$

$$\bar{U}_2 \frac{\partial \bar{U}_2}{\partial x_2} + \bar{U}_3 \frac{\partial \bar{U}_2}{\partial x_3} = -\frac{1}{\rho} \frac{\partial \bar{P}}{\partial x_2} - \frac{\partial \overline{u_2^2}}{\partial x_2} - \frac{\partial \overline{u_2 u_3}}{\partial x_3} + \nu \left(\frac{\partial^2 \bar{U}_2}{\partial x_2^2} + \frac{\partial^2 \bar{U}_2}{\partial x_3^2} \right) \quad (2)$$

$$\bar{U}_2 \frac{\partial \bar{U}_3}{\partial x_2} + \bar{U}_3 \frac{\partial \bar{U}_3}{\partial x_3} = -\frac{1}{\rho} \frac{\partial \bar{P}}{\partial x_3} - \frac{\partial \overline{u_2 u_3}}{\partial x_2} - \frac{\partial \overline{u_3^2}}{\partial x_3} + \nu \left(\frac{\partial^2 \bar{U}_3}{\partial x_2^2} + \frac{\partial^2 \bar{U}_3}{\partial x_3^2} \right) \quad (3)$$

Rotta 1972

no secondary motion: $\bar{U}_2 = \bar{U}_3 = 0$

from last slide, combine equations (2) and (3):

$$\frac{\partial^2 (\overline{u_2^2} - \overline{u_3^2})}{\partial x_2 \partial x_3} + \frac{\partial^2 \overline{u_2 u_3}}{\partial x_3^2} - \frac{\partial^2 \overline{u_2 u_3}}{\partial x_2^2} = 0$$

obvious solution that satisfies boundary conditions:

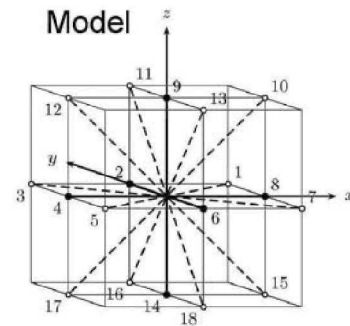
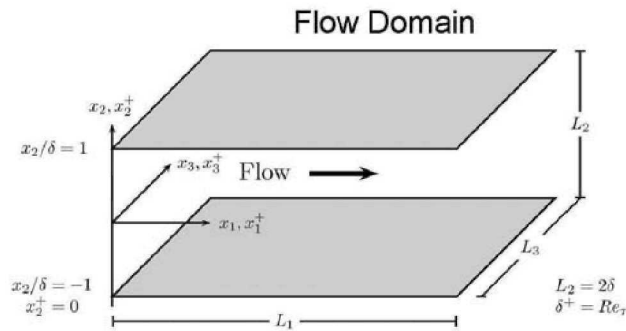
axisymmetric turbulence, where

$$\overline{u_2^2} = \overline{u_3^2} \quad \text{and} \quad \overline{u_2 u_3} = 0$$

$$\text{with} \quad \overline{u_1^2} > \overline{u_2^2} = \overline{u_3^2}$$

For such a configuration of axisymmetric turbulence
the wall is located at the 1C limit!

Simulation of a turbulent channel flow based on the Lattice Boltzmann Method



D3Q19

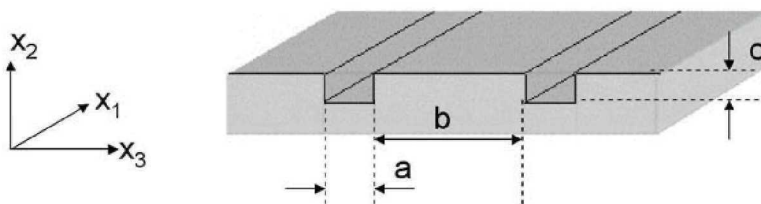
extremely high resolution with

$$N_1 \times N_2 \times N_3 = 4096 \times 364 \times 360$$

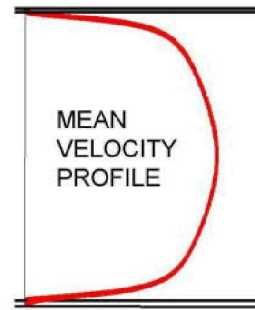
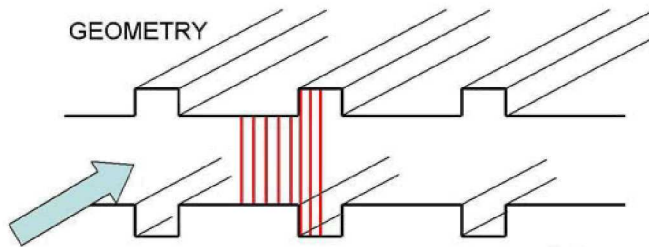
grid points possible

Dr. Peter Lammers, HLRS Stuttgart

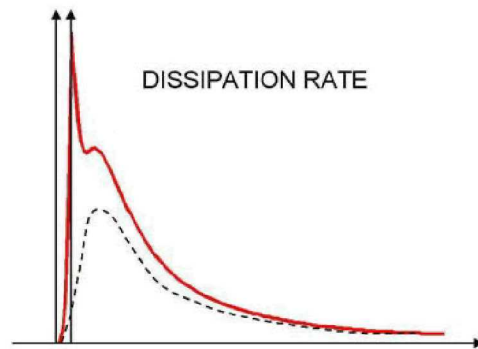
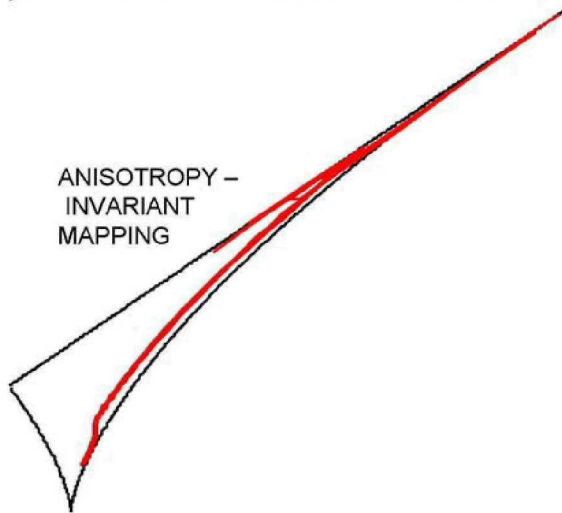
Configurations for simulations with grooved walls:



Reynolds number	resolution $N_1 \times N_2 \times N_3$	resolution in wall units	a in wall units	b in wall units	c in wall units
6690	4096x264x240	1.4	8	13	5
6650	4096x264x240	1.4	5	14	5
5230	4096x364x360	0.8	4	15	4

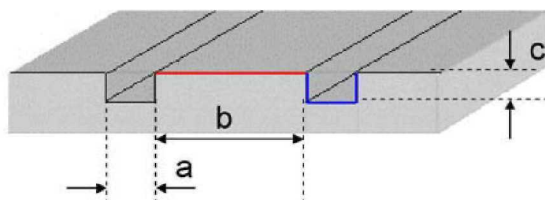


ANISOTROPY - INVARIANT MAPPING



Reynolds number	a in wall units	b in wall units	c in wall units
6690	8	14	5
6650	5	14	5
5230	4	15	4

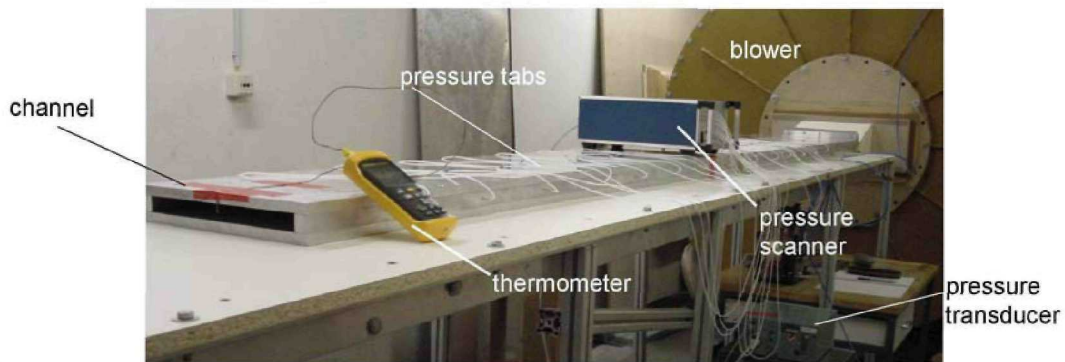
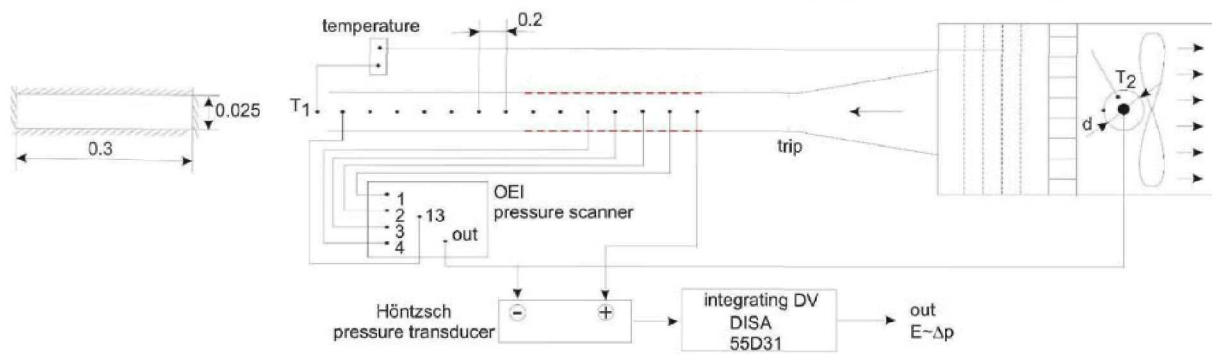
DR simulation
24%
18%
16%



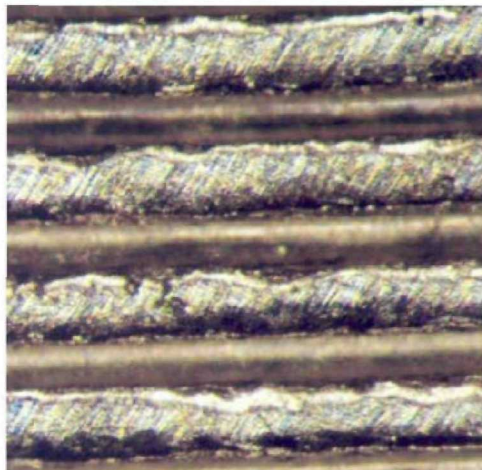
$$DR_{\max} \approx 1 - \frac{b}{a+b} = \frac{a}{a+b}$$

assumptions:

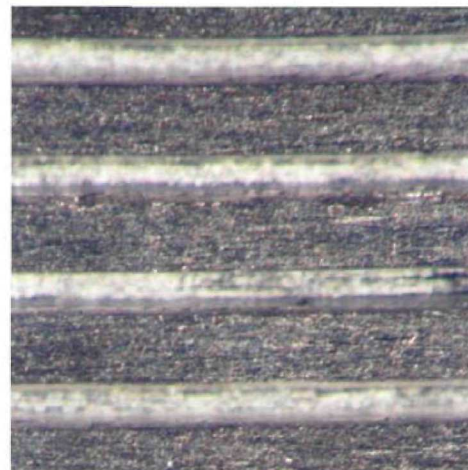
- DR as in flat channel
- negligible drag



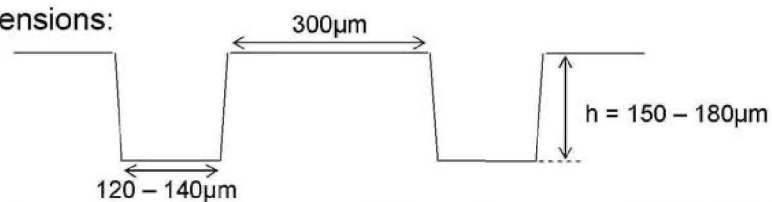
non-polished surface

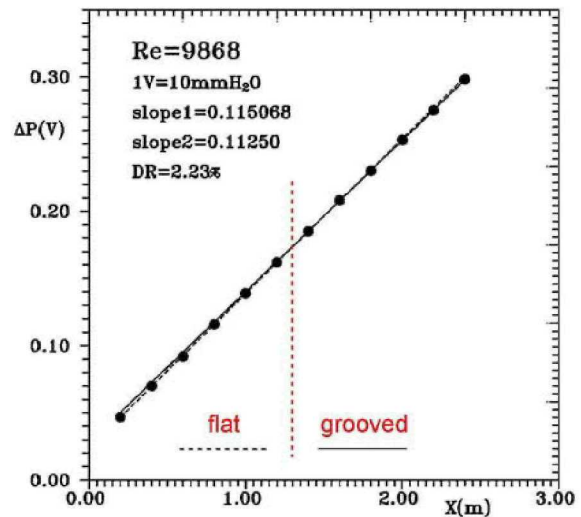
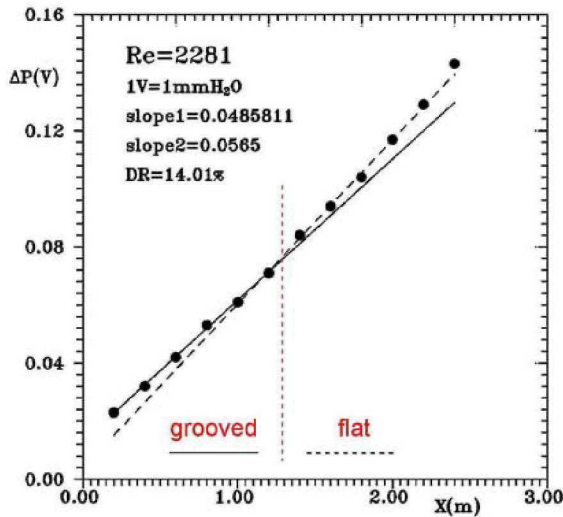
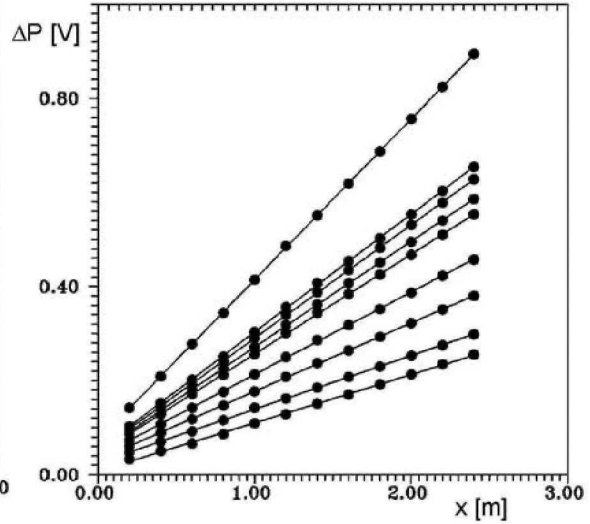
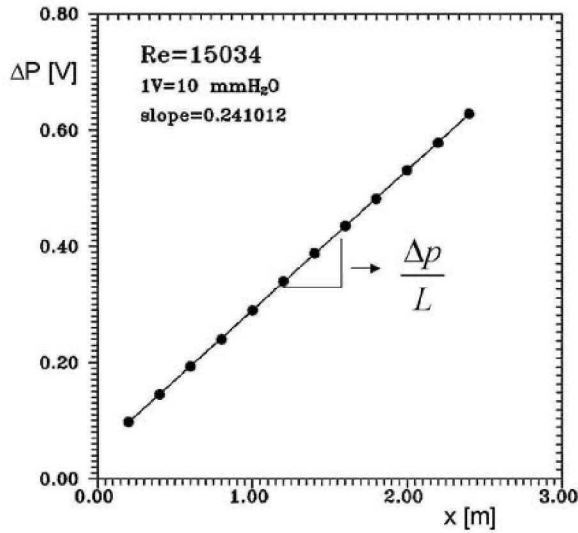


polished surface

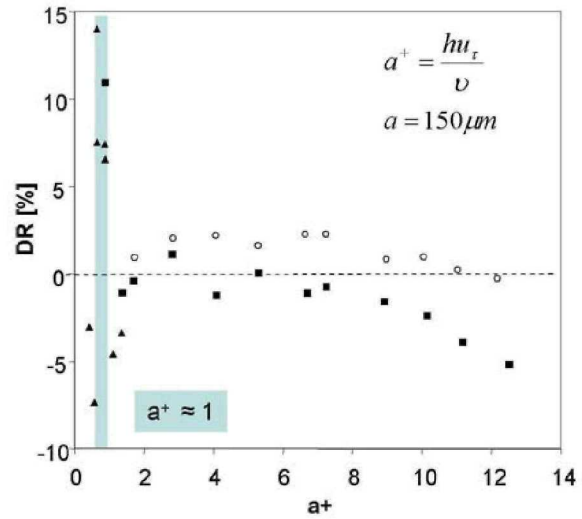
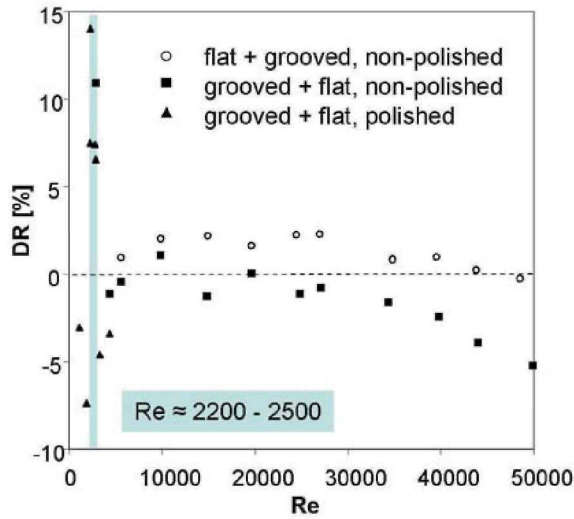


dimensions:

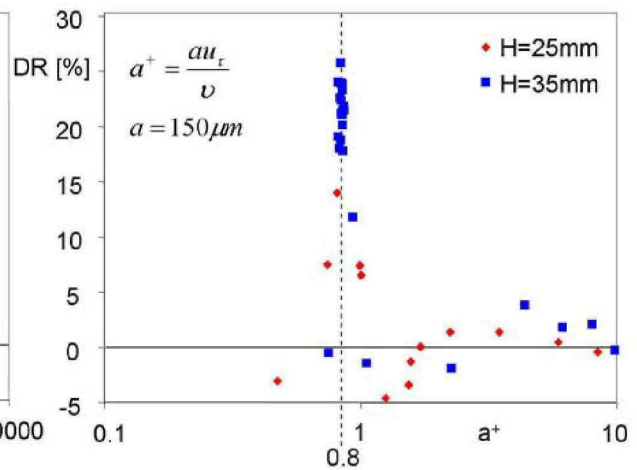
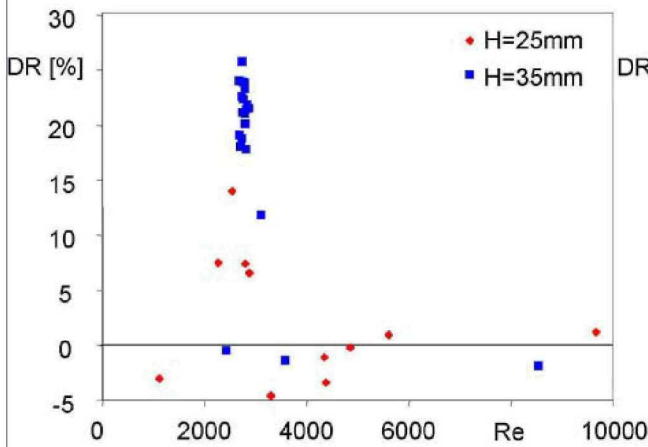




$$DR = 1 - \frac{slope_{grooved}}{slope_{flat}} = 1 - \frac{(\Delta p / \Delta L)_{grooved}}{(\Delta p / \Delta L)_{flat}}$$



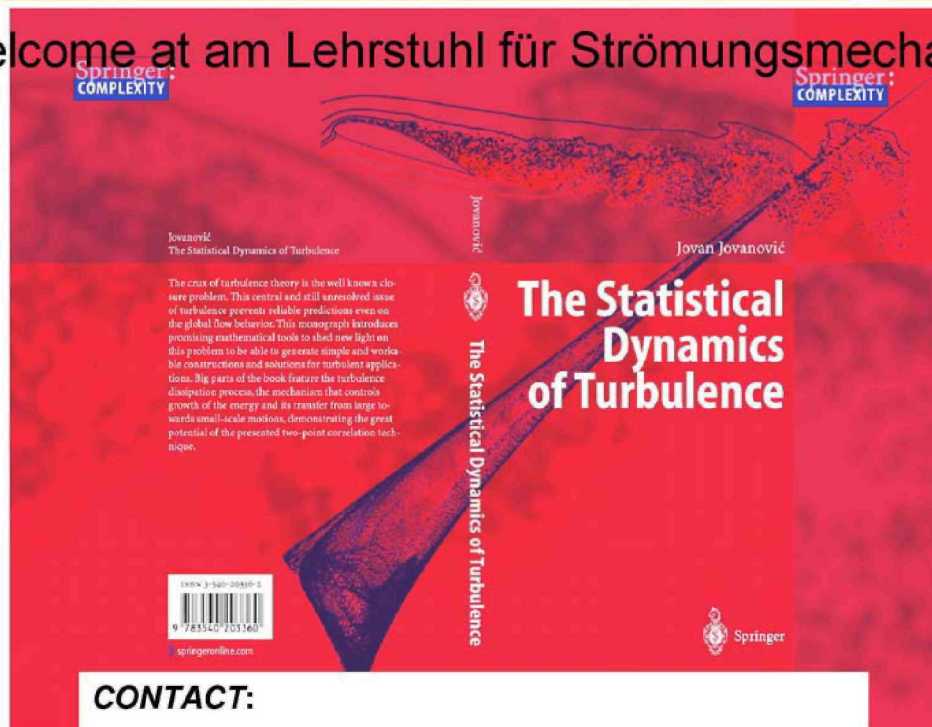
High DR values only in very narrow range around $Re \approx 2200 - 2550$ and $a^+ \approx 1$
 Kolmogorov scale $\eta_k^+ \approx 1.6$



High DR is gained, when $a^+ \approx 0.8$
 Kolmogorov Scale $\eta_k^+ \approx 1.5$

- Experiments and DNS data show increase in anisotropy with increasing DR
- DR is highest when 1C state is approached, where $(\epsilon)_{\text{wall}}$ vanishes
- Trend explained with the scenario that polymers restructure dissipation range of spectrum (local axisymmetry)
- Experimental verification of the interaction level through prediction of optimum polymer concentration and its relaxation time for max DR
- Engineering use: determine best polymer and optimum concentration without trial and error
- Numerical simulations and experiments show that surface structuring can produce large DR effect which is very attractive for engineering implementation

Welcome at am Lehrstuhl für Strömungsmechanik



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Strömungstechnik

Bettina Maria Frohnapfel

**Flow Control of
Near-Wall Turbulence**

Strömungskontrolle wandnaher Turbulenz

SHAKER
VERLAG

CONTACT:

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