



**The Abdus Salam
International Centre for Theoretical Physics**



2023-25

Workshop on Topics in Quantum Turbulence

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Oscillating Bose Condensates: Generation of Vortices and Evidence for Turbulence

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Vortices, clusters of vortices and evidences of turbulence in an oscillating BEC

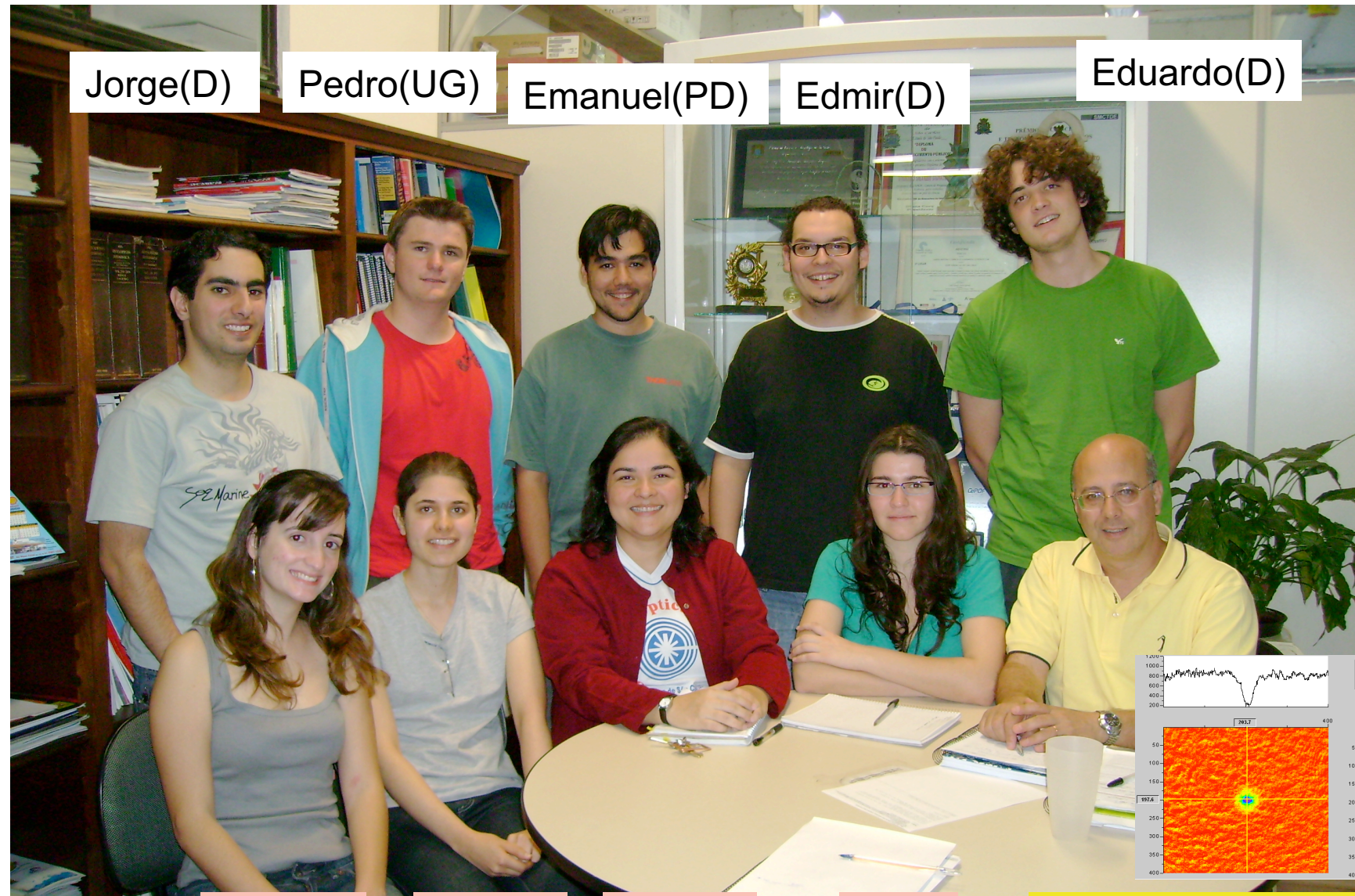
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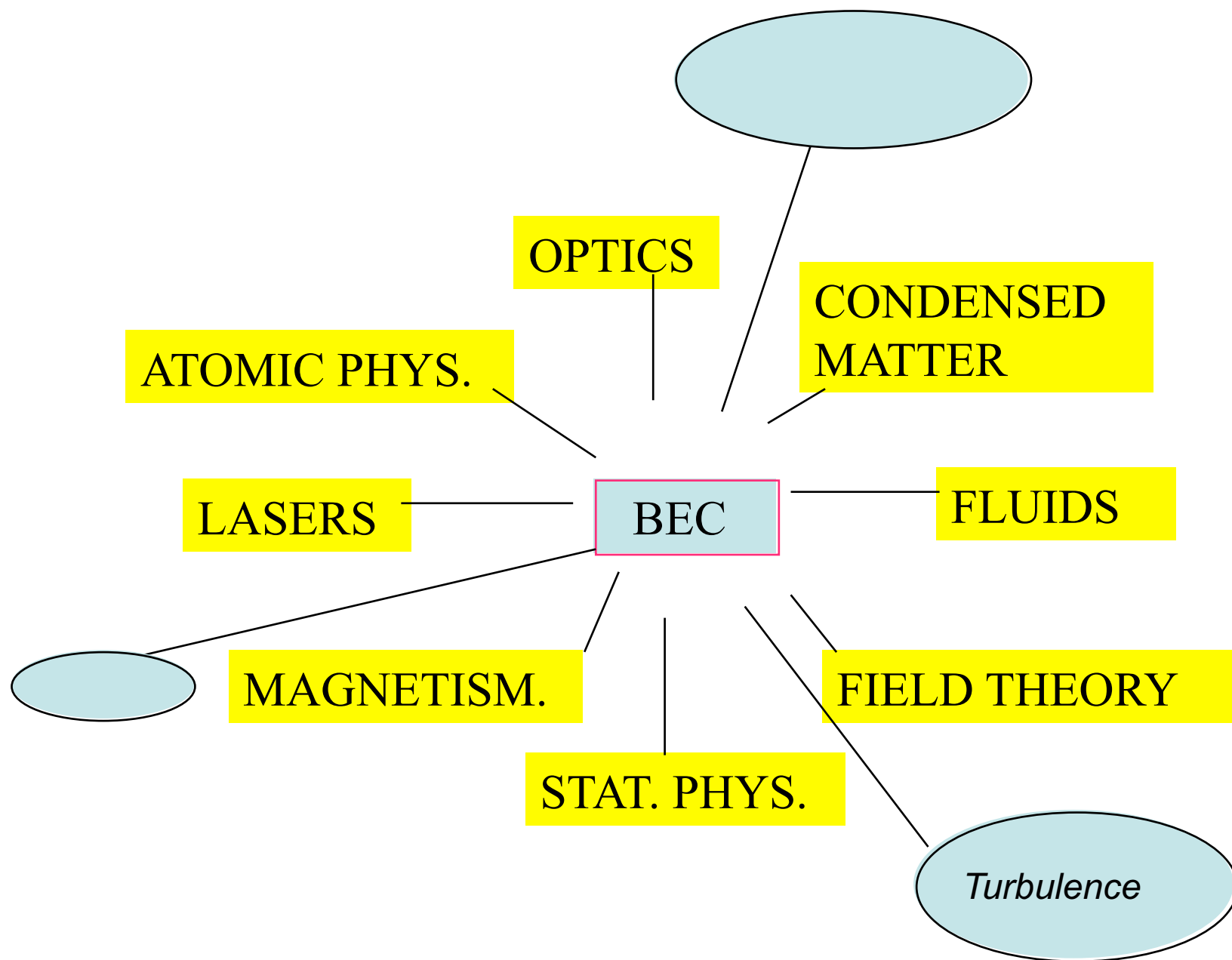
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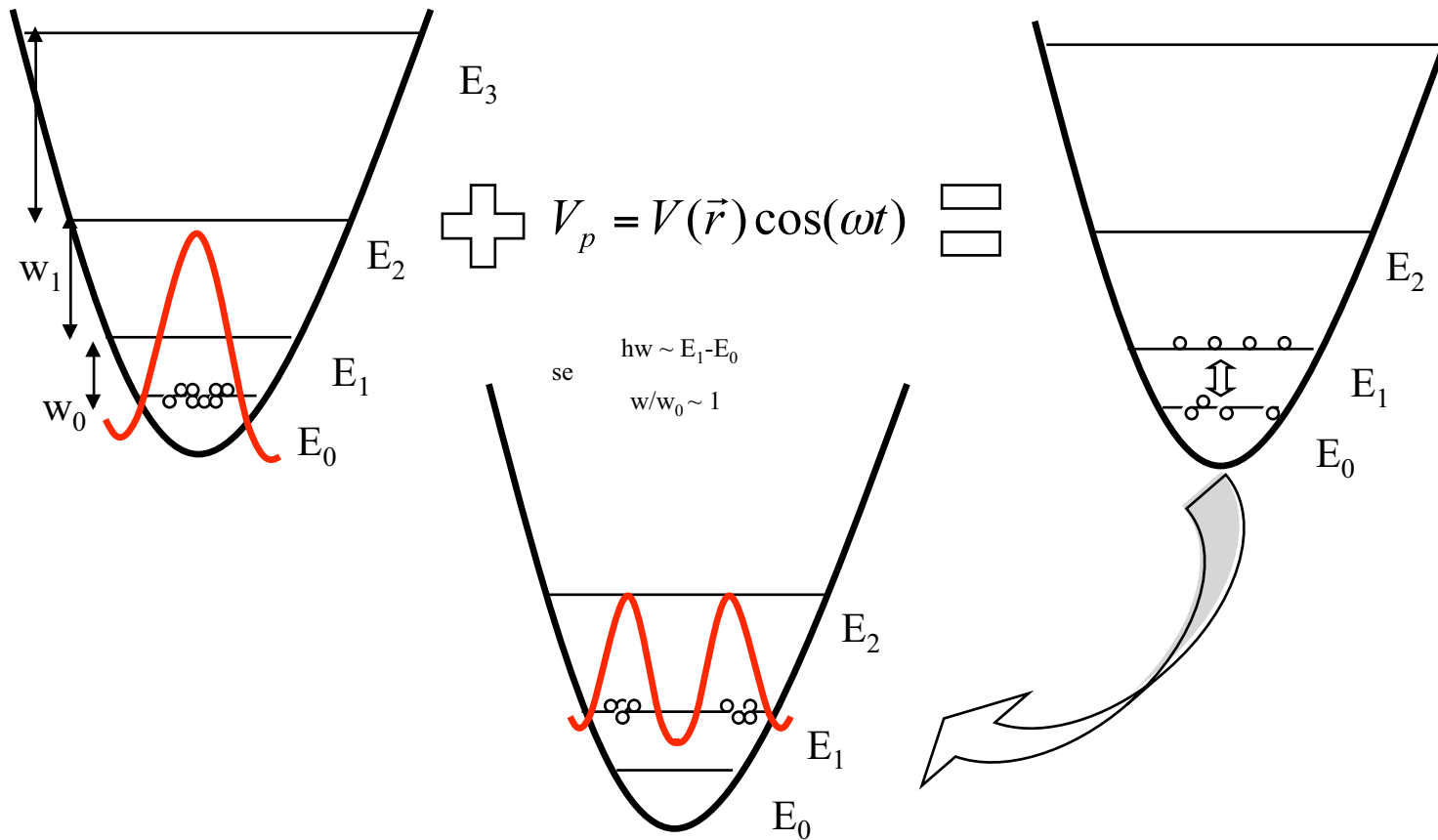
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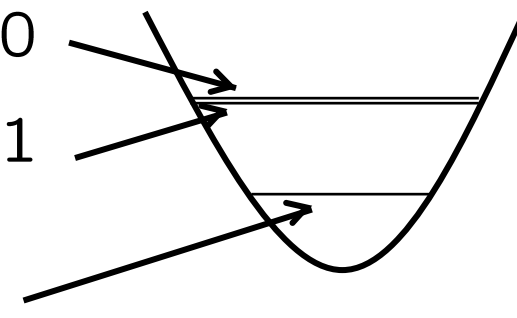


Our initial goal :

Coherent population transfer between two trapped states



But we forgot the vortices !!!!!!!!!!!

$$\begin{array}{lll} x \exp(-r^2/(2a_0^2)) & \longleftrightarrow & n_x = 1, n_y = 0 \\ y \exp(-r^2/(2a_0^2)) & \longleftrightarrow & n_x = 0, n_y = 1 \\ \exp(-r^2/(2a_0^2)) & \longleftrightarrow & n_x = n_y = 0 \end{array}$$


combination $|1_x, 0_y\rangle + i|0_x, 1_y\rangle$

Wave function: $(x + iy) e^{-r^2/(2a_0^2)} = r e^{i\varphi} e^{-r^2/(2a_0^2)}$

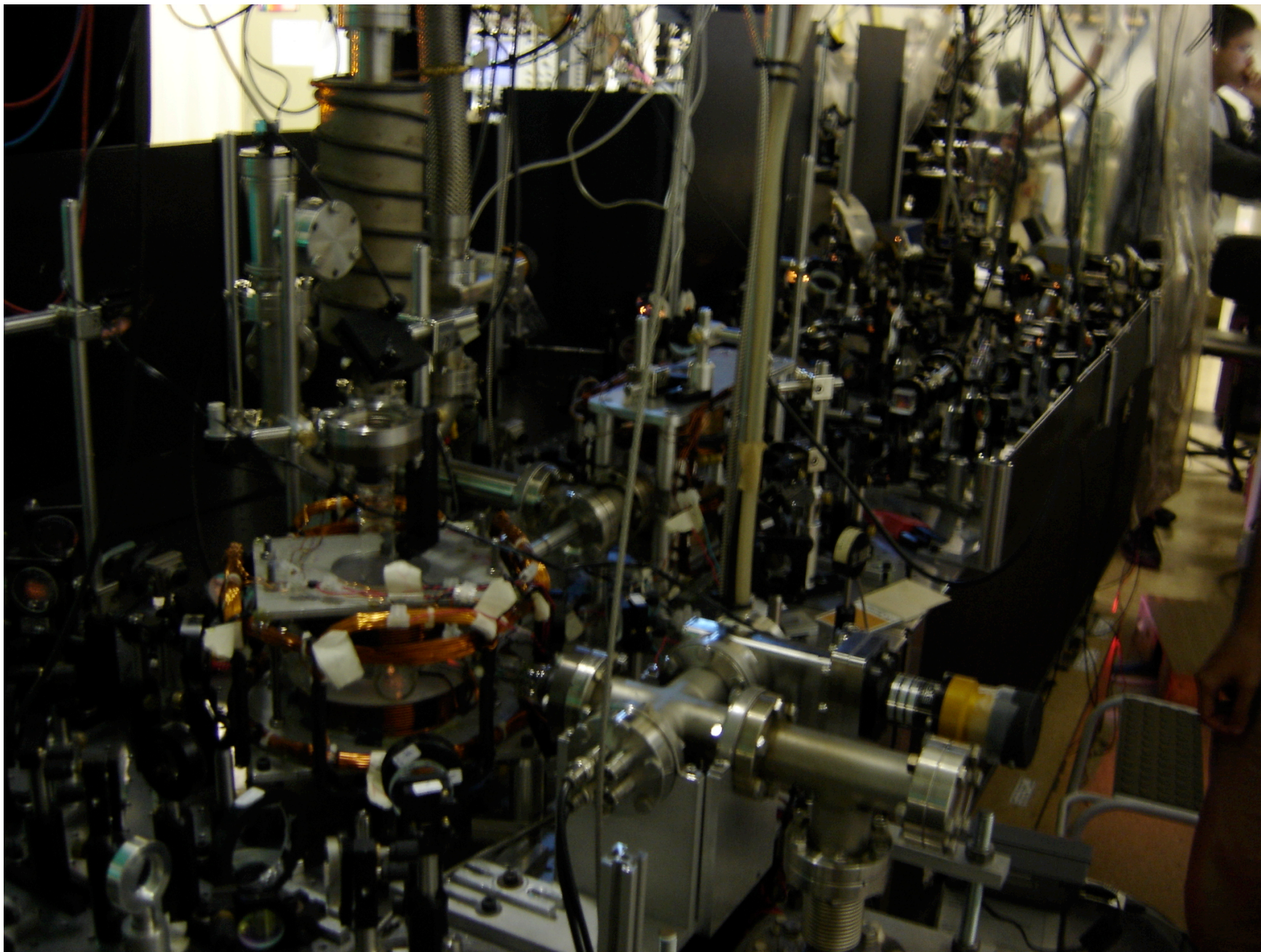
vortex with a charge +1

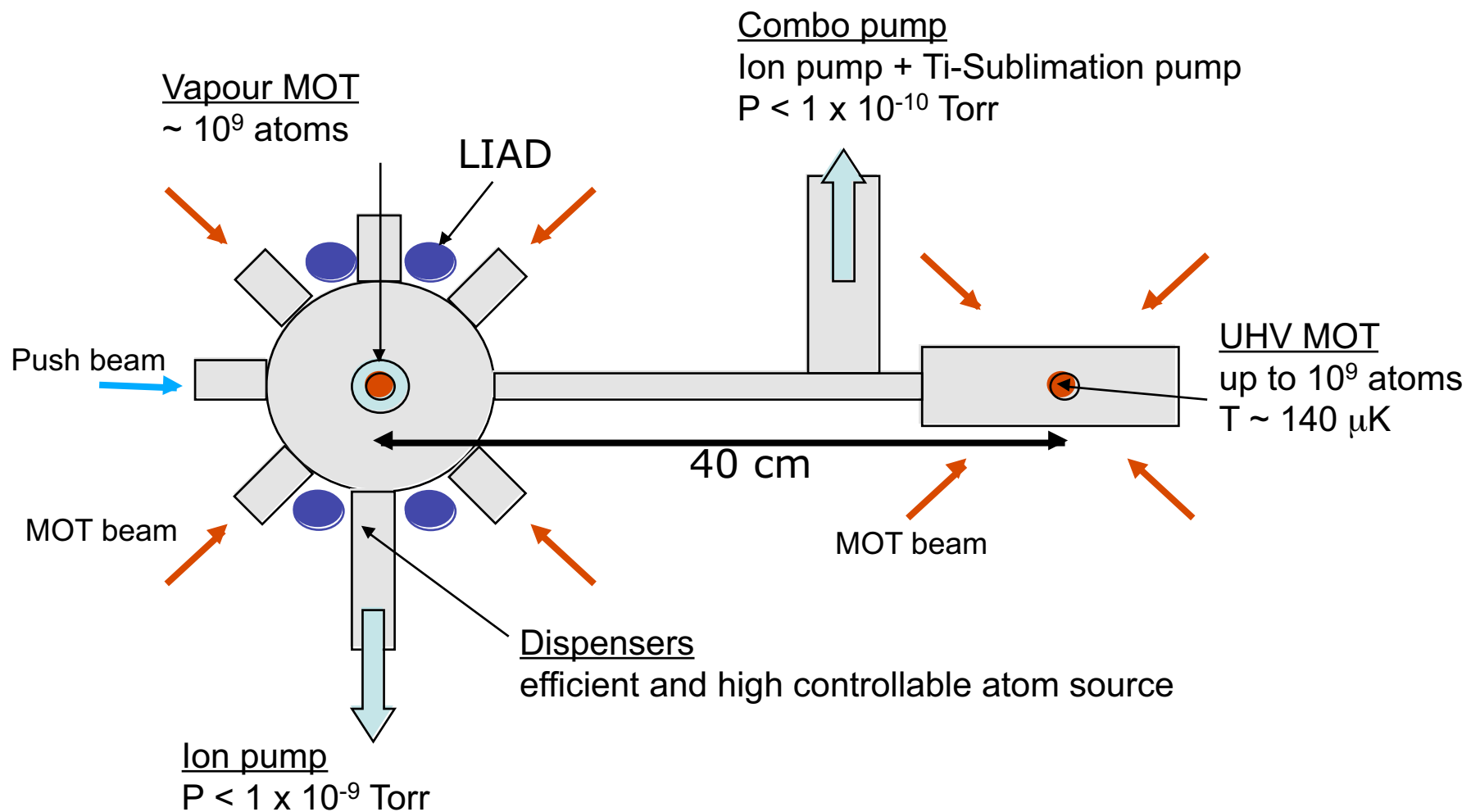
EXPLORATORY PRESENTATION

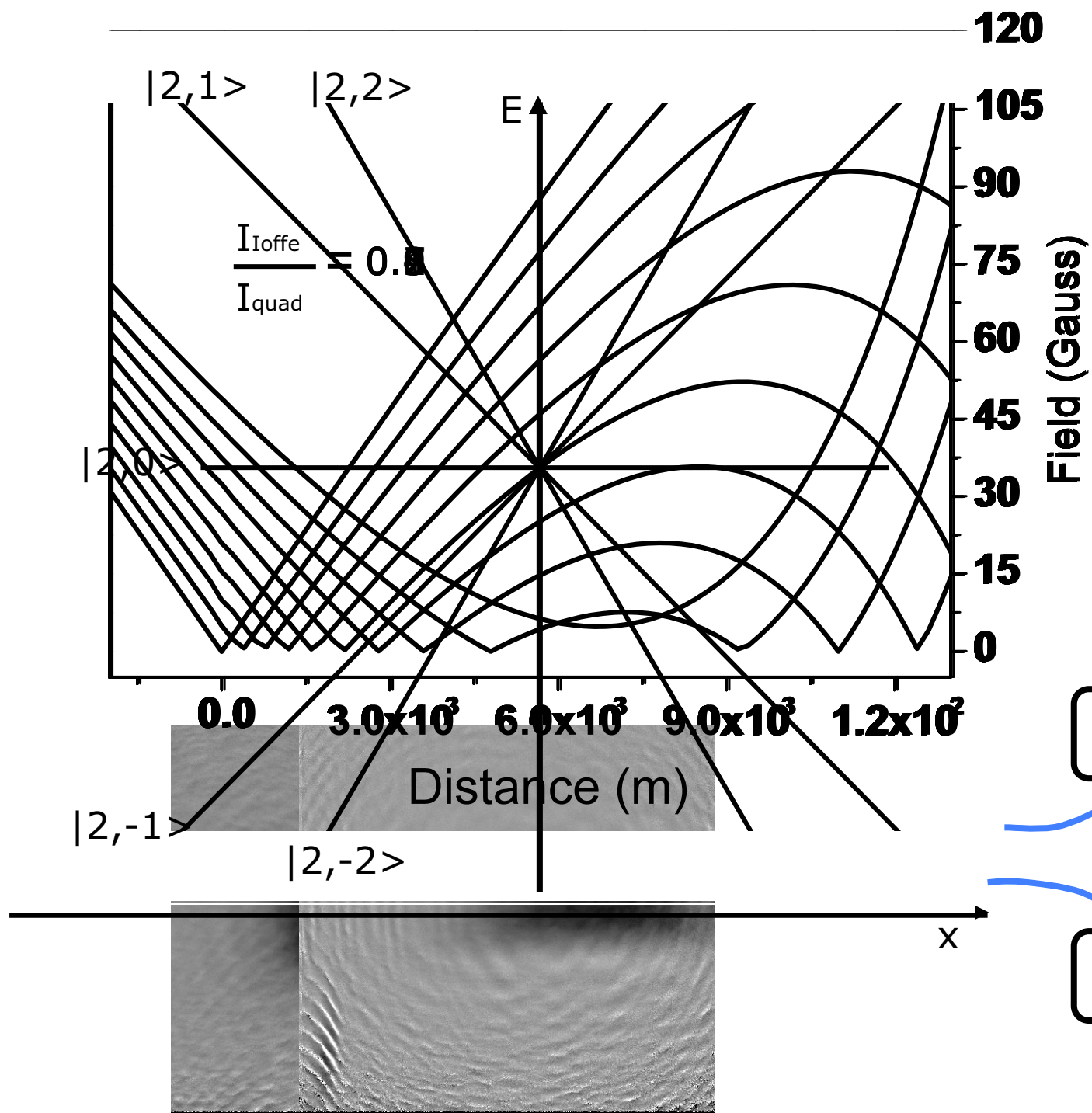
OUTLINE

- 1 - GENERAL CONSIDERATIONS
- 2 - VORTICES FORMED BY OSCILLATIONS
- 3 - ROUTE TO TURBULENCE
- 4 - CLUSTERS OF VORTICES: TRIPOLES
- 5 - FRAGMENTATION

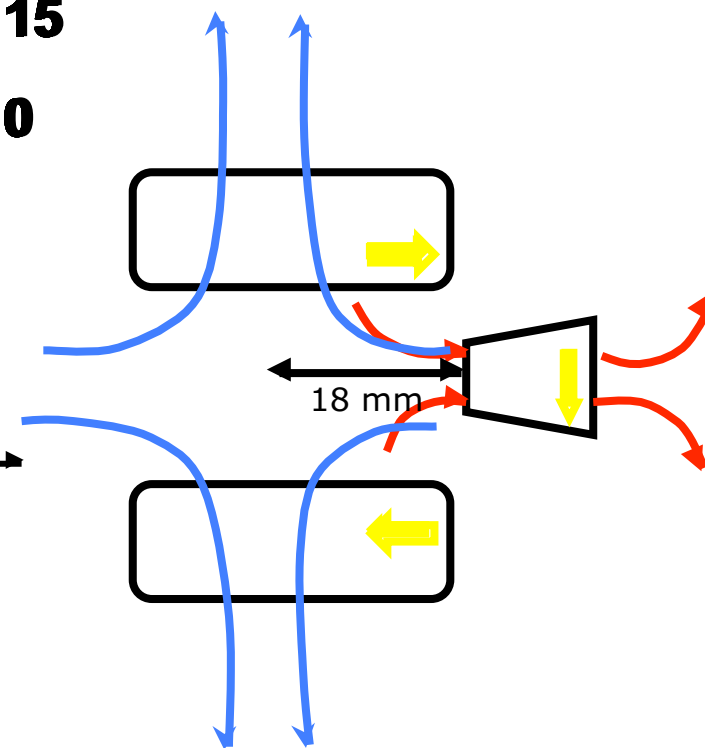
BEC OF Rb







QUIC Trap

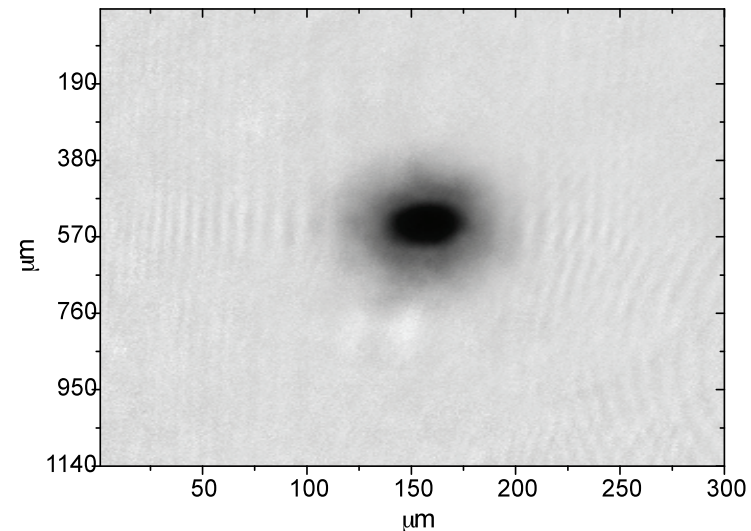
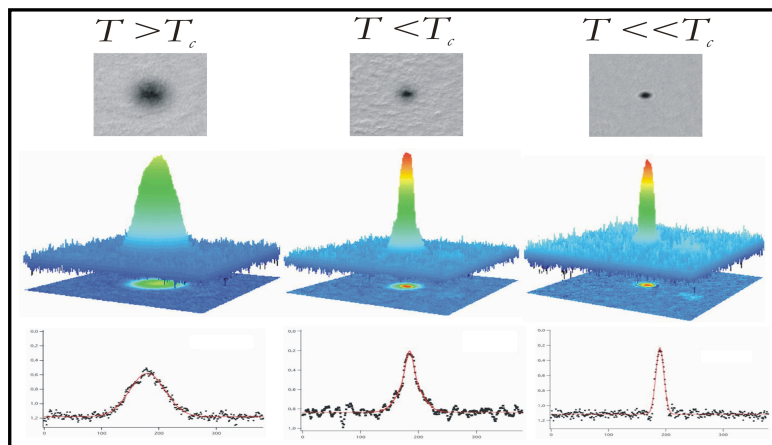


Temporal Sequence

- A full run of the BEC experiment takes 1min
- The first 35s are just for 2nd MOT loading
- The last 24s are for magnetic trapping and evaporation, which takes itself 22s
- The link between these two parts is due to a group of 5 processes that take a total of 10ms

OUTCOME: 3 to 8 10^5 condensate Atoms

$T \sim 80$ to 200 nK



Trapped Bose Condensate and superfluidity

- Investigation of Scissors Mode (rotation of the cloud around the symmetry axis)
(proposed) Trento – Phys. Rev. Lett.
83,4452(1999)
(experiment) Oxford – Phys. Rev. Lett.
84,2056(2000) and Phys. Rev. Lett.
86,3938(2001)

There are many studies of vortices in BECs

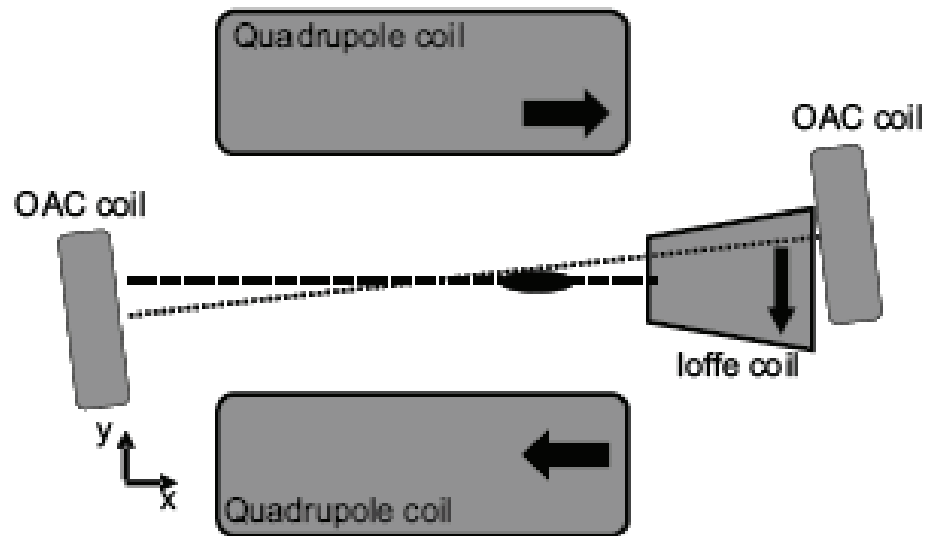
- Measuring angular momentum – PRL85(2000)
- Nucleation by instabilities in the rotation PRL 86 (2001)
- Phase measurement – PRA 64 (2001)
- Dynamics of single vortex line and observation of Kelvin modes – PRL90(2003)
- Lattices – many

How are the vortices formed and how is the dynamics?

- Many experiments and many theoretical papers
- Tsubota's group : PRA 65(2002), PRA 71(2005)
- Fetter – Rev. Mod. Phys (2008) and reference there in..
- Dalibard's group – Theory and experiment
- Gardiner's group – Theory
- Recent: Anderson – Nature(2008); PRL(2007)
- Etc..

Oscillatory Quadrupolar external excitation

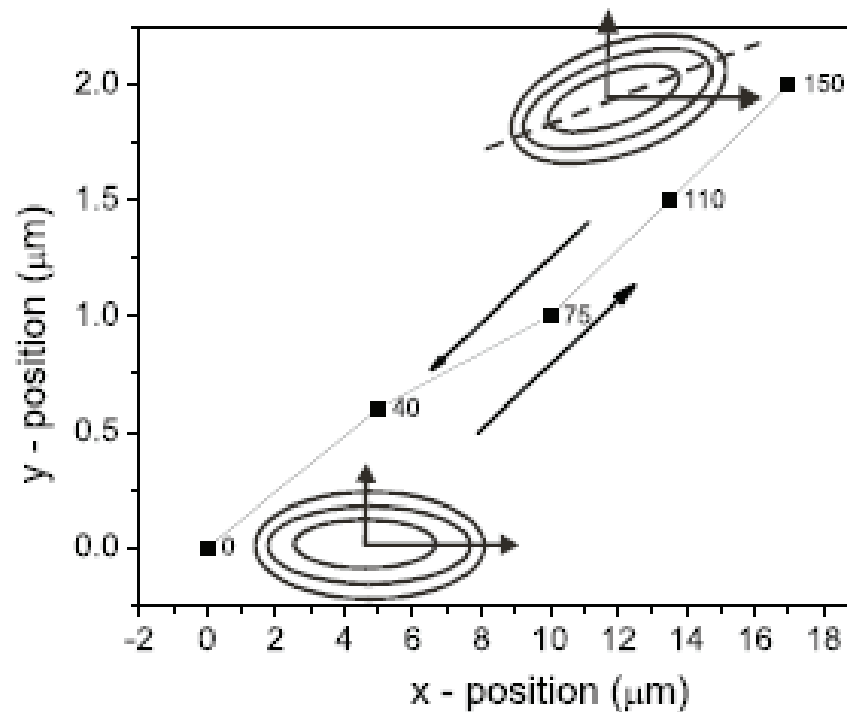
**POSSIBILITY TO EXCITE VORTICES OF BOTH SIGNS:
VORTEX AND ANTI-VORTEX**



Displacement

Rotation

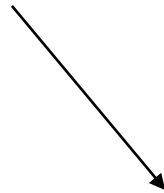
Deformation of the potential



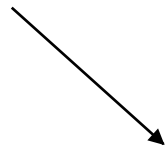
Larger amplitude of oscillation:

- Larger displacement
- Larger deformation of the potential
- Higher acceleration in the rotation

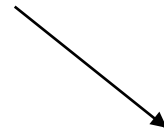
PRODUCING BEC (1 MIN)



EXCITATION (0 TO 70 ms)

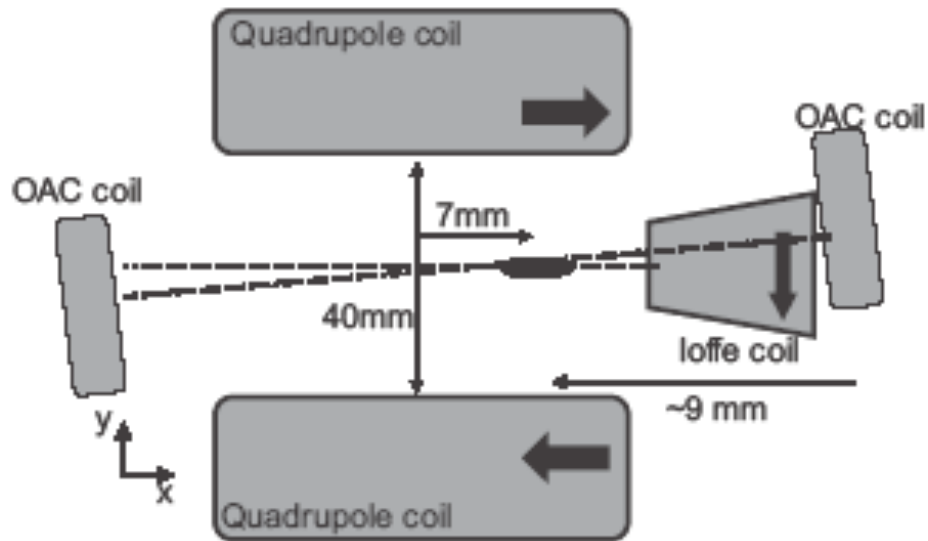


Rest(20 ms)



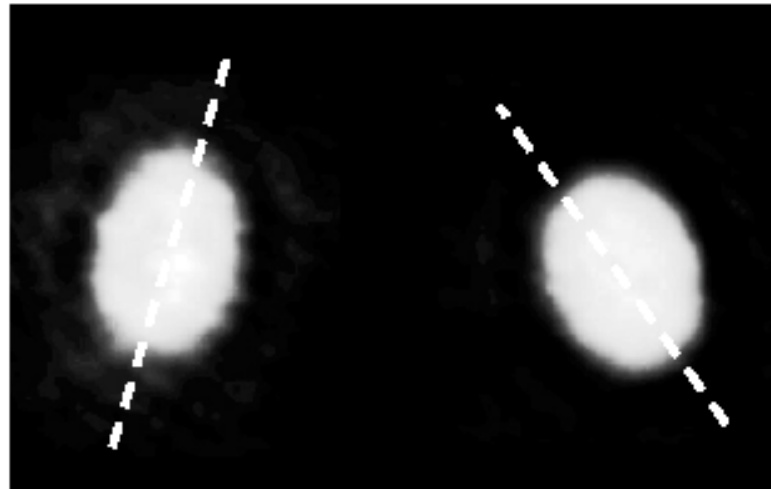
TOF FOLLOED BY ABSORPTION IMAGE

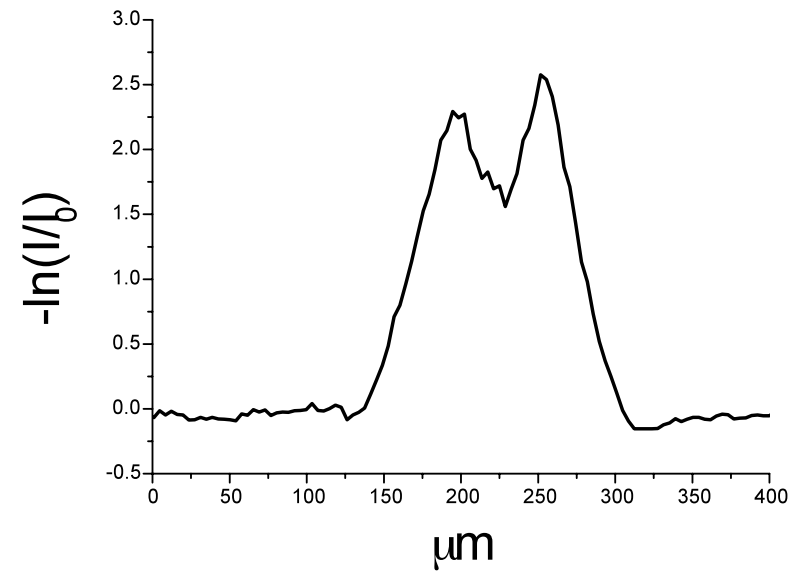
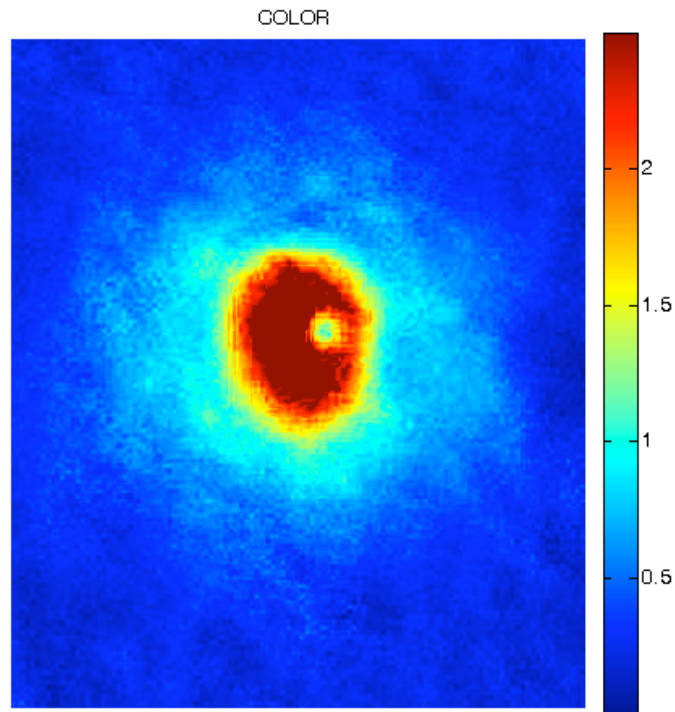
Small amplitudes and/or small times of excitation



Oscillatory banding

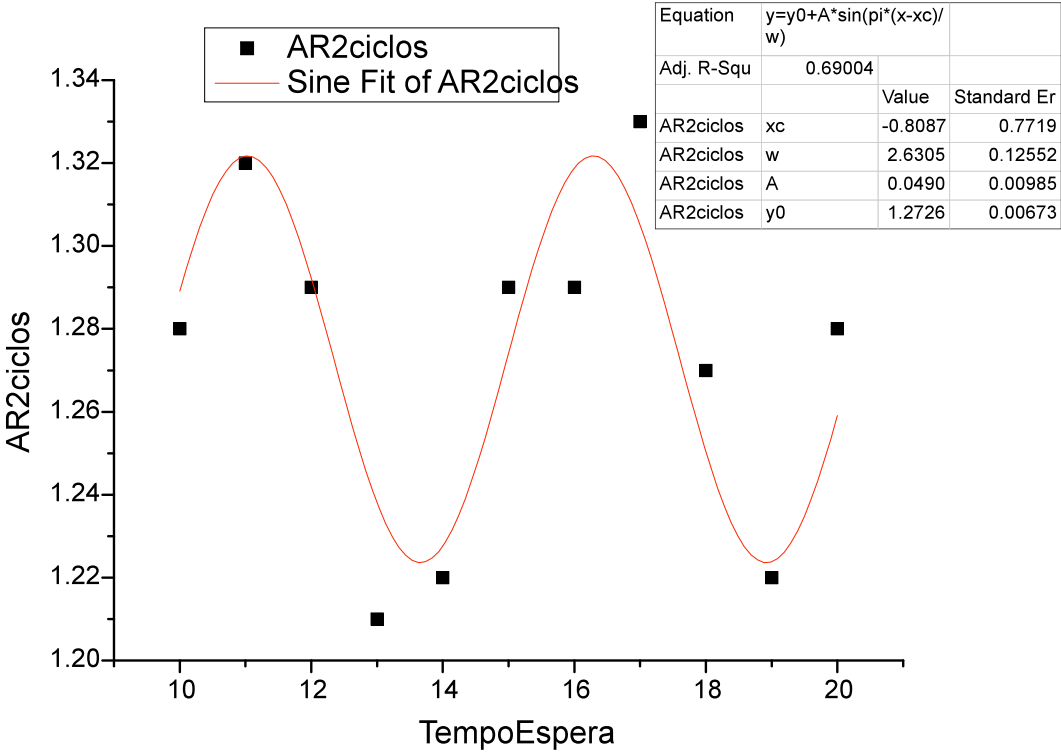
Equivalent to oscillations
generated by sudden rotations →
Scissors Mode





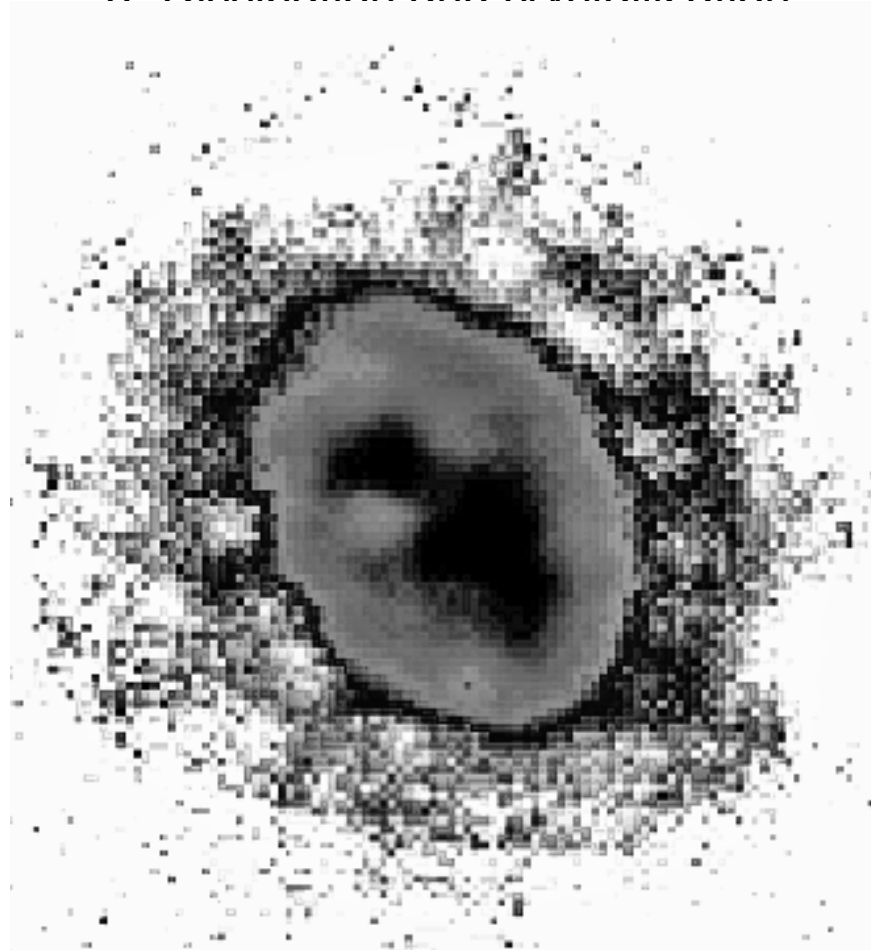
NEXT STEP AFTER BANDING AXIS IS THE OBSERVATION OF A DEEP IN THE ABSORPTION → VORTEX

During oscillations there are excitation of collective
Quadrupoleoscillations



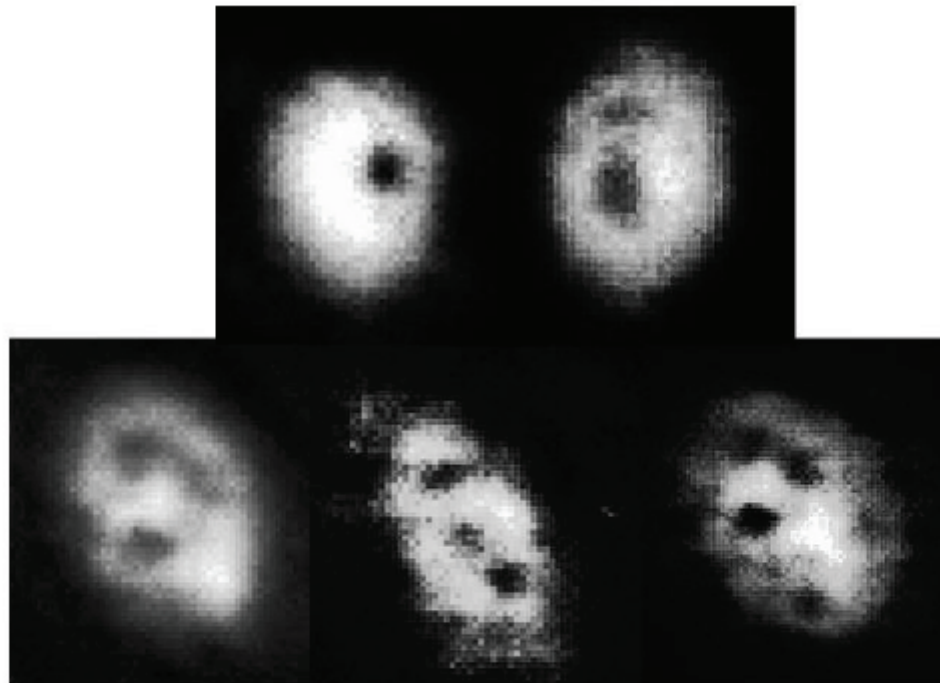
Parker- Adams PRL95(2005) – Stirring BEC

- 1 – Quadrupolar mode breaks down, ejecting energetic atoms to form an outer cloud
- 2- Turbulent cloud containing vortices is formed with a Kolmogorov energy spectrum
- 3- Dissipation and crystallization

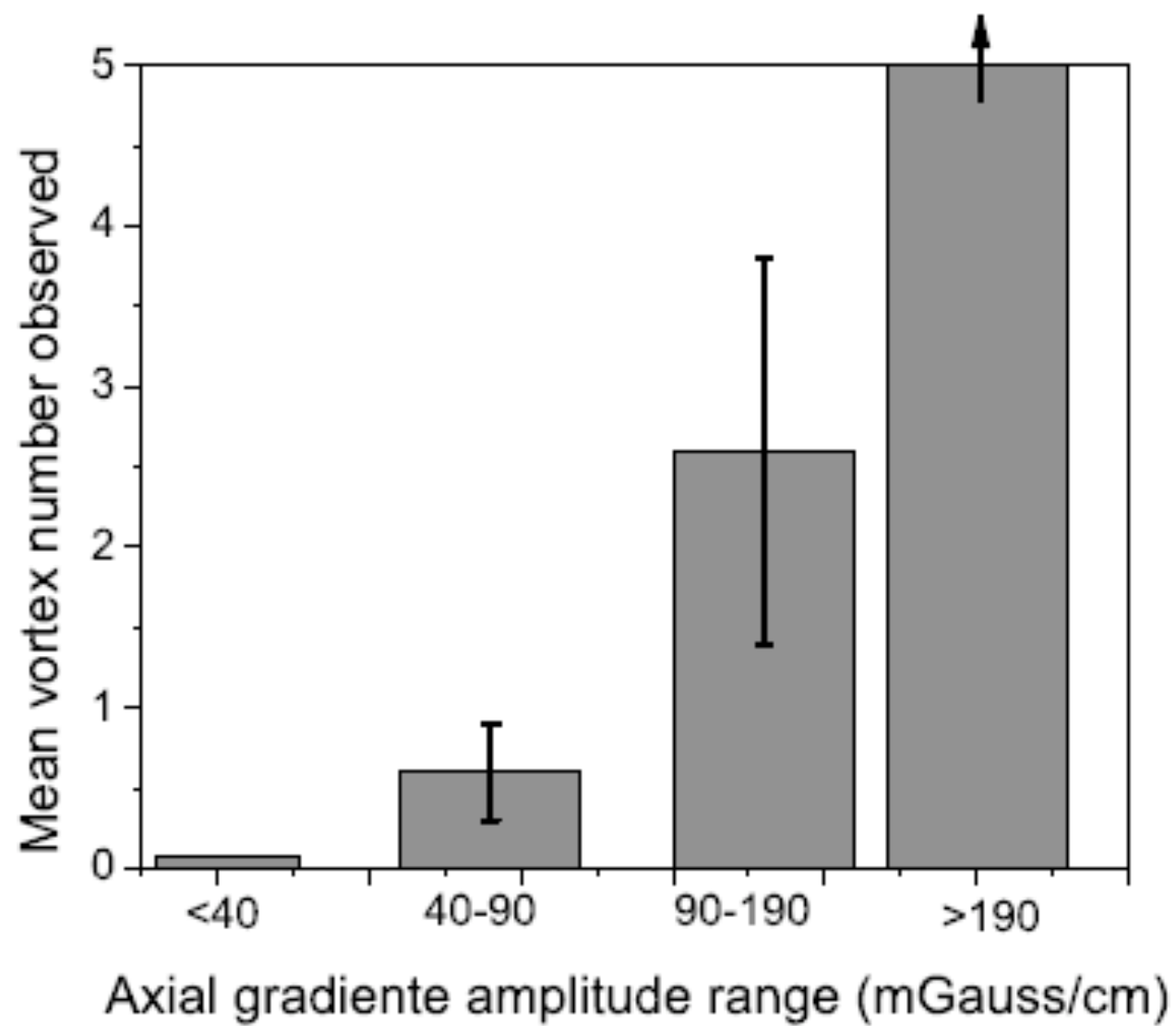


EVOLUTION WITH AMPLITUDE AND TIME OF EXCITATION

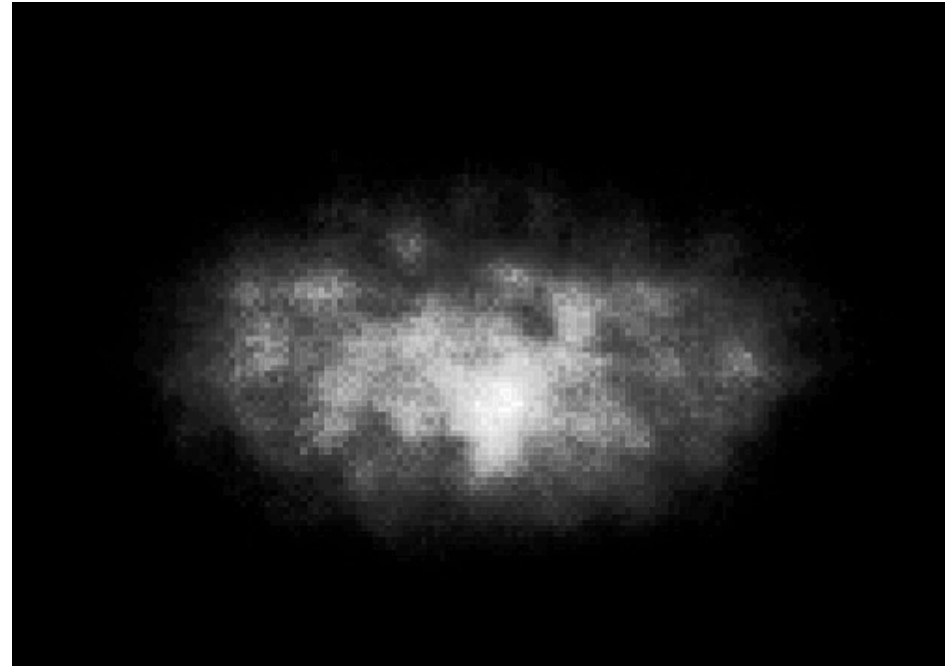
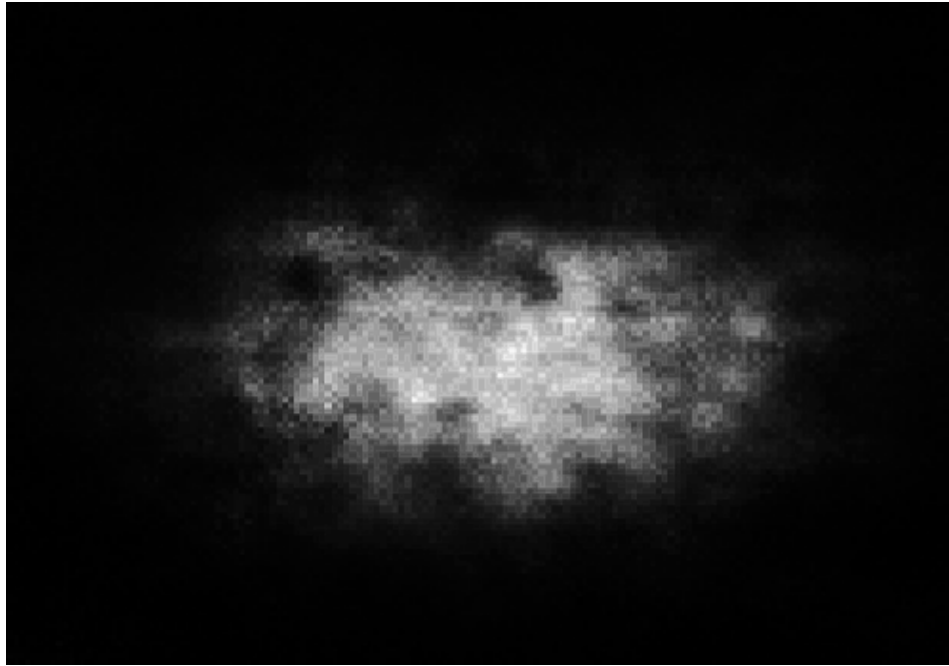
There are a large shot-to-shot fluctuation

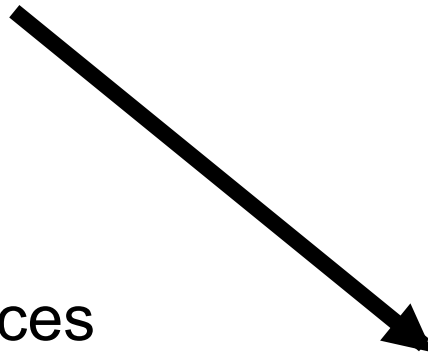
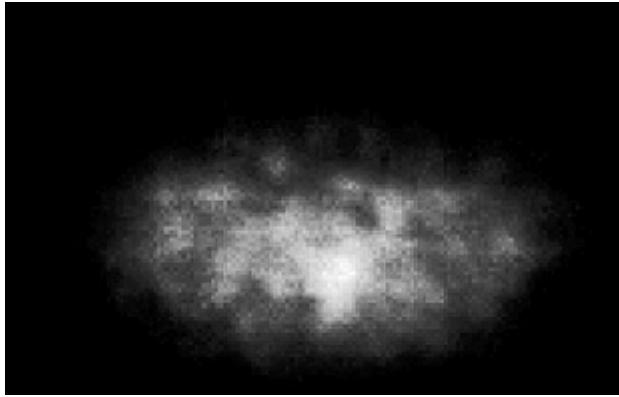


Fixed time of excitation – 20 ms

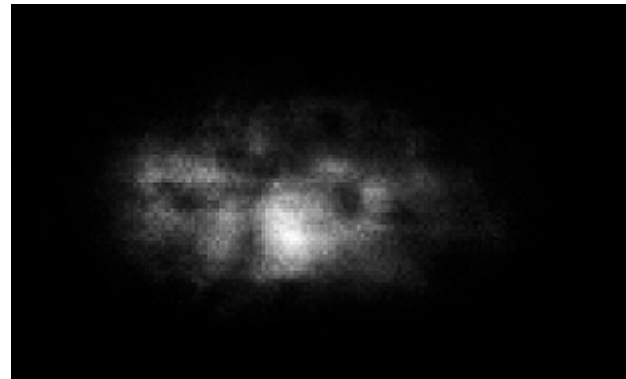


Explosion point → proliferation of many vortices → turbulence



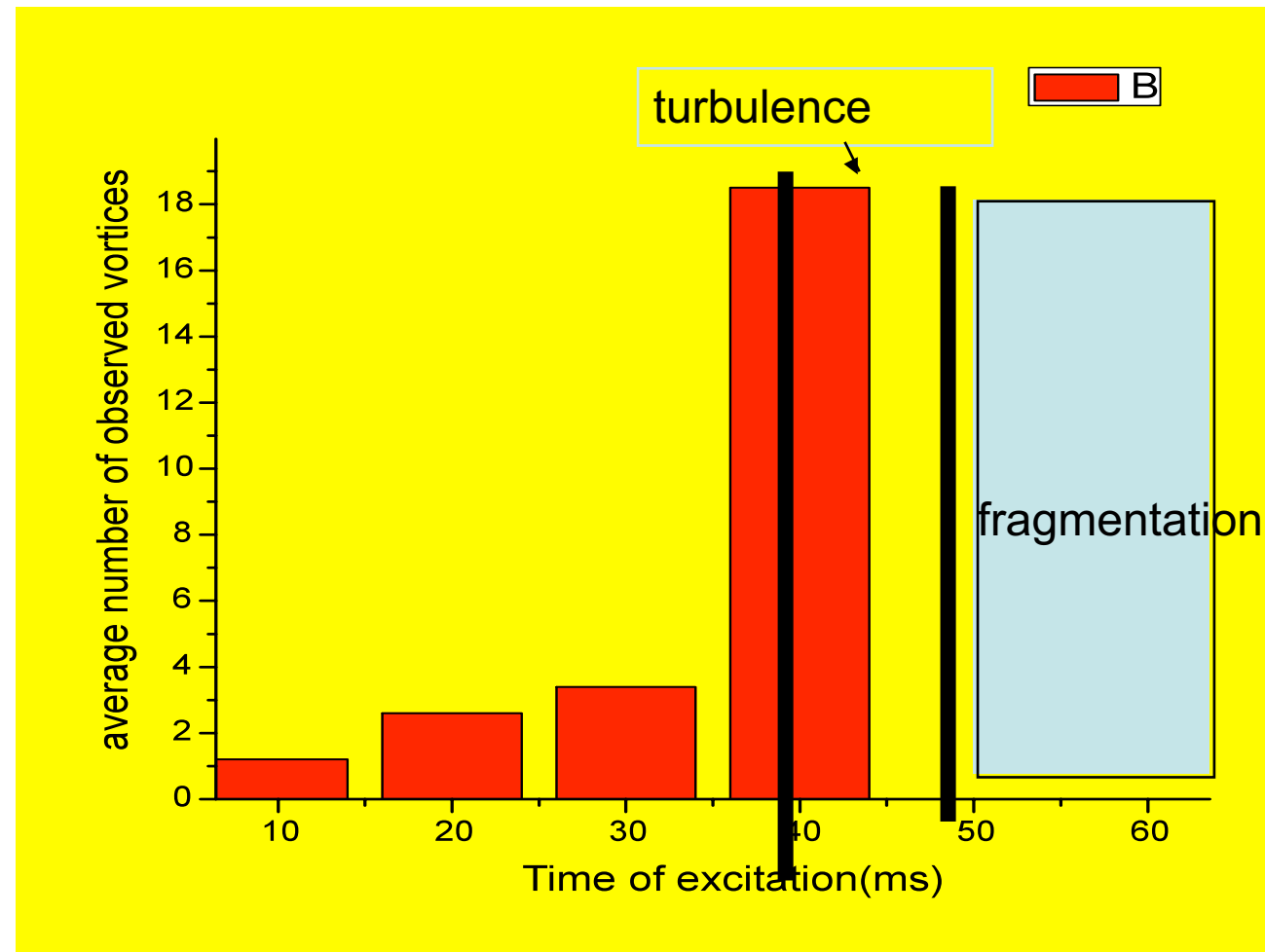


Vortices to tangle vortices

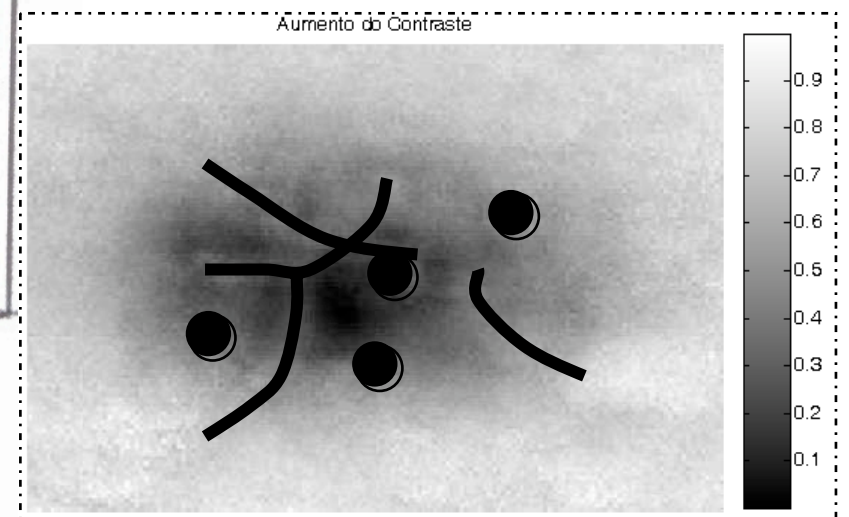
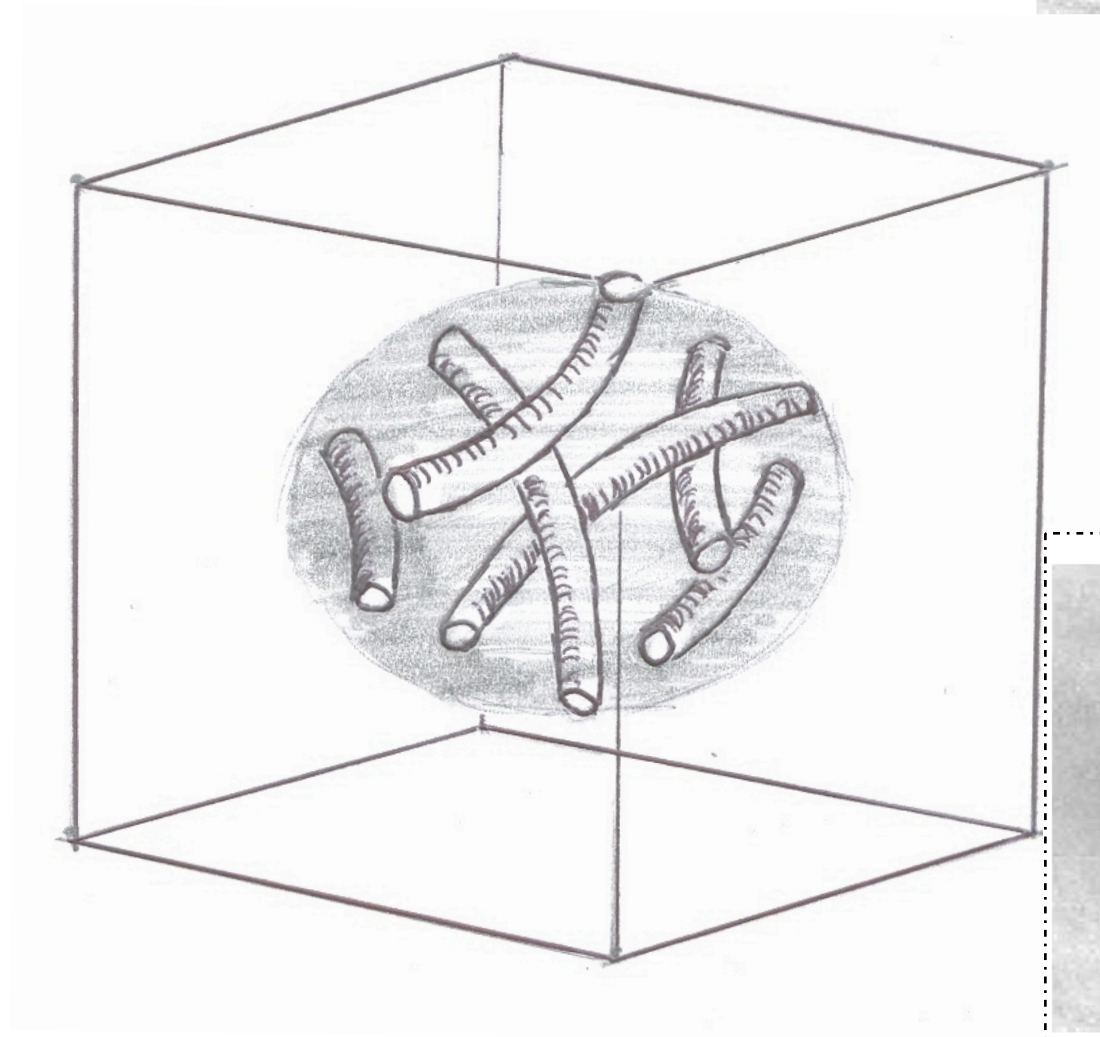
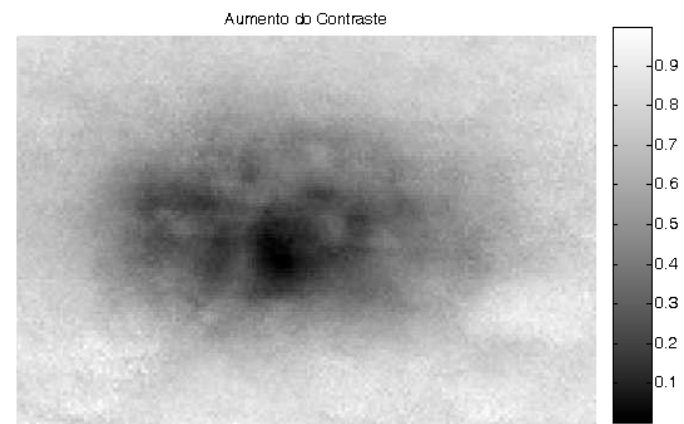


Average Numbers of vortices as a function of excitation time

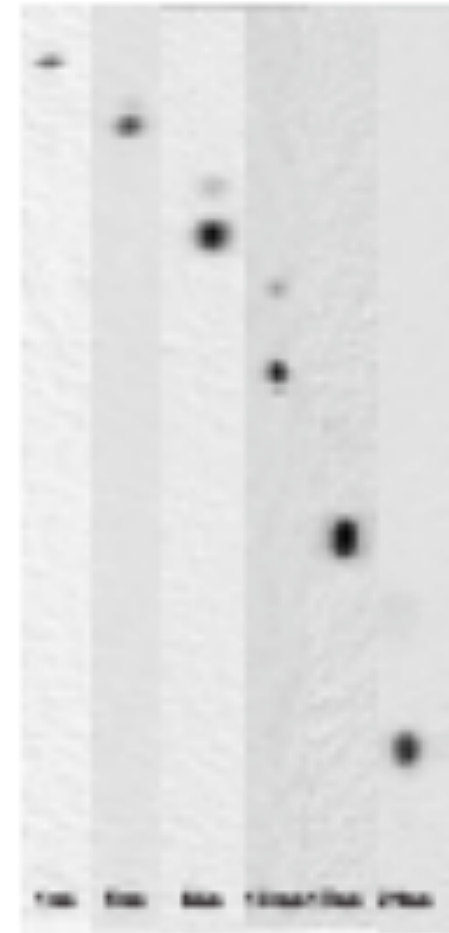
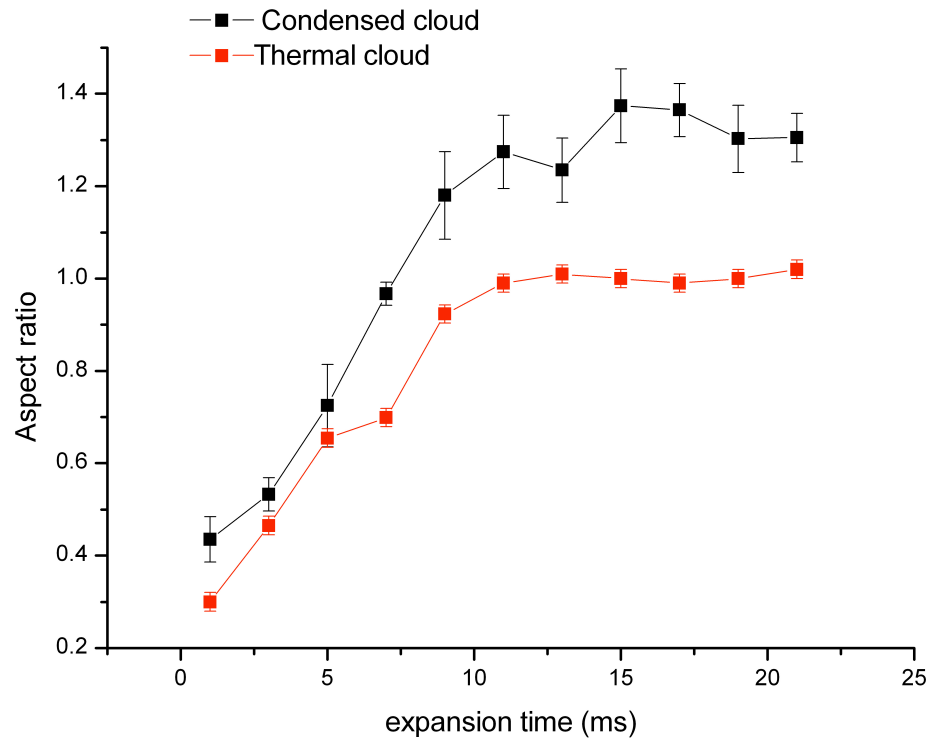
Excitation frequency : 200Hz, Amplitude 250 mV



Tangle vortices



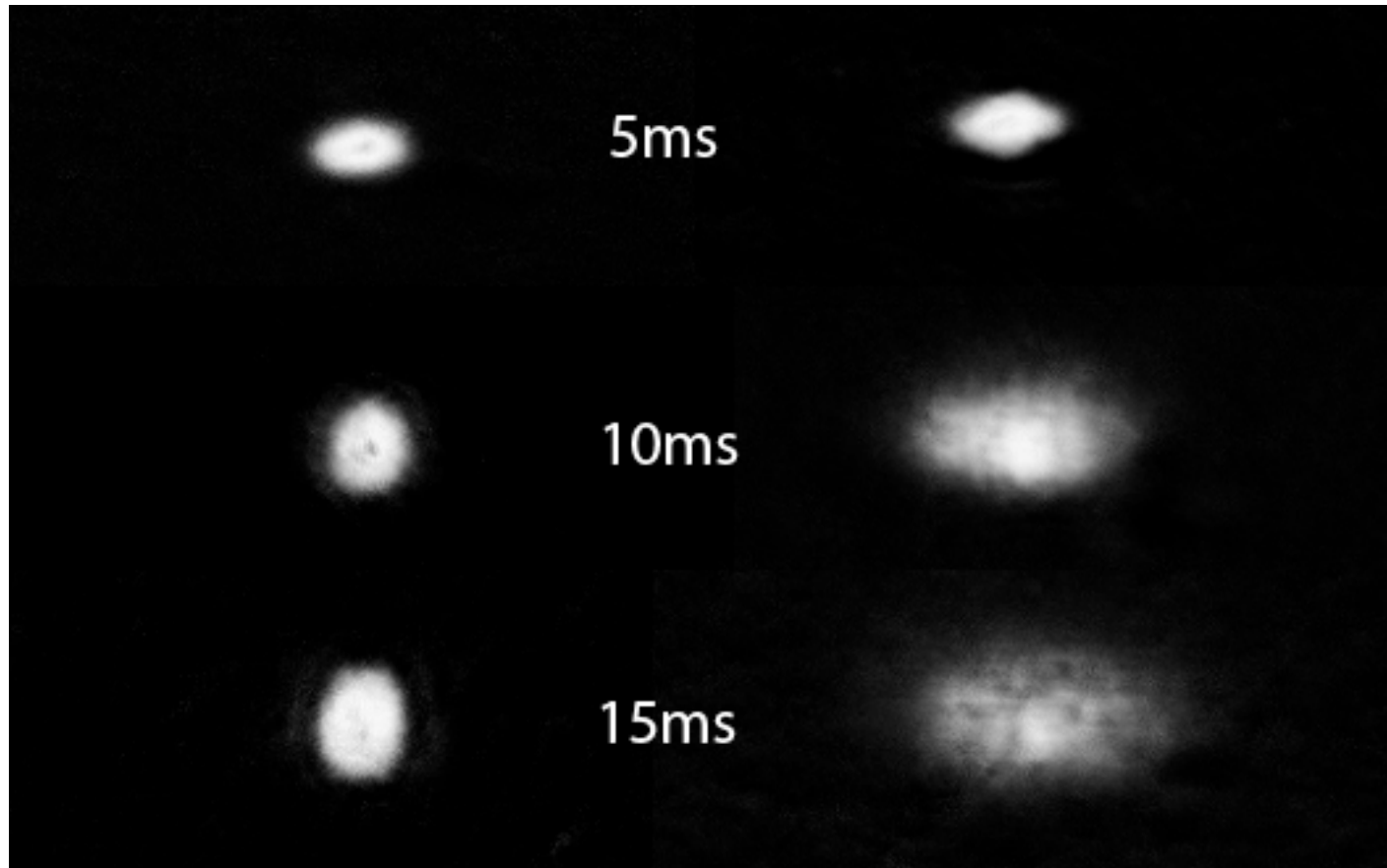
Observation of aspect ratio inversion of the quantum cloud- energy conversion

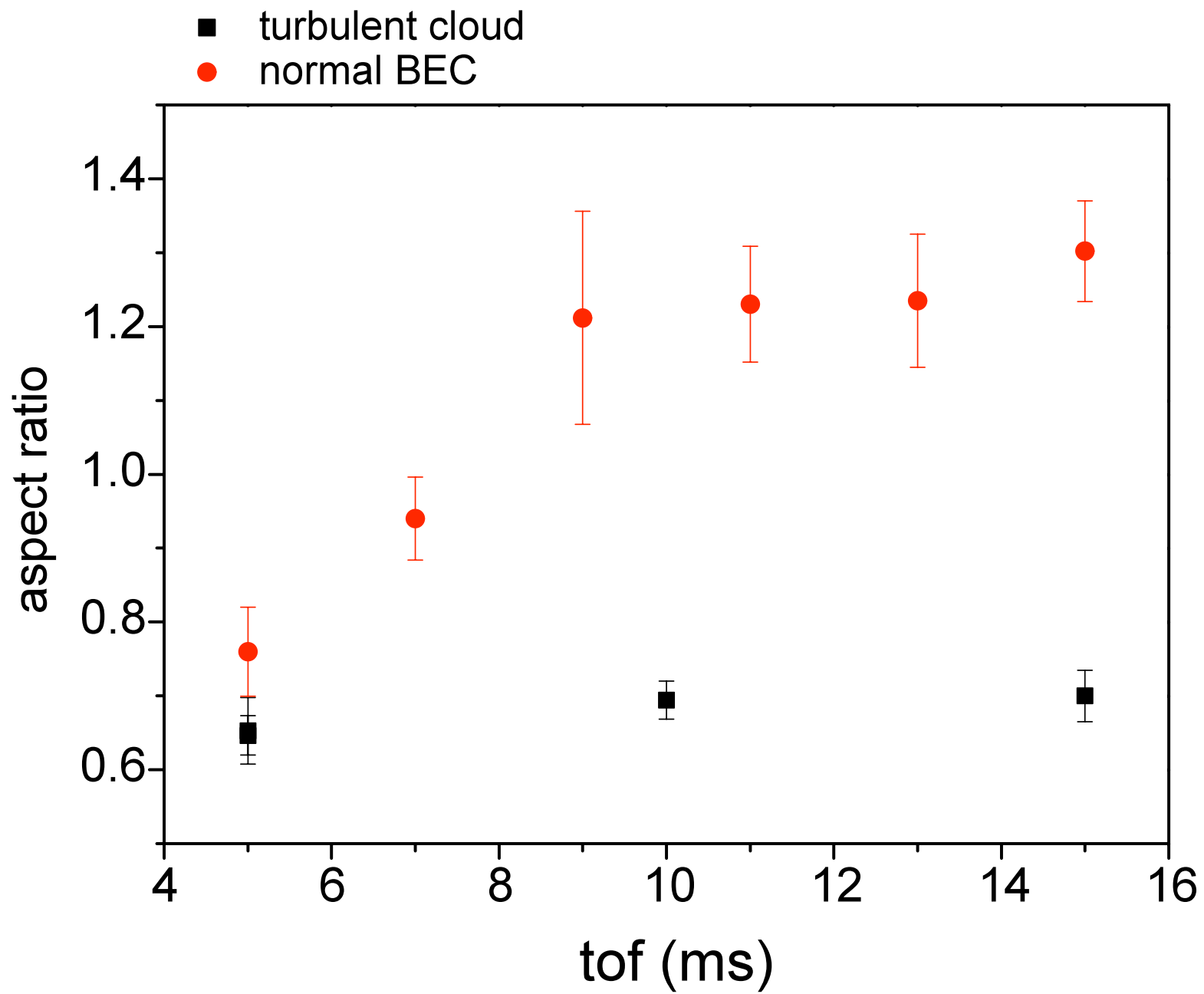


**For a large number of vortices
(turbulent?), the inversion is not
observed**

Regular BEC

Turbulent BEC





Phys. Rev. Lett. 88,070405(2002)

(Edwards, Clark, Pedri, Pitaevskii and Stringari)

- “since the instantaneous moment of inertia is then proportional to the asymmetry of the cross section...”
- “ Preventing the released condensate from attaining a circular cross section..”

Clearly the presence of angular momentum affects the expansion

The absence of inversion in the ratio may be an indicative of Turbulence in the quantum atomic fluid, that would be a new effect in the atomic quantum fluid

Route to QUANTUM TURBULENCE

- EXCITATION IN AT LEAST TWO PLANS
- ENOUGH AMPLITUDE TO TRANSFER MANY UNITS OF ANGULAR MOMENT
- Two axis of oscillations (not equivalent)
- Tangle vortices (Feynman)
- When the vortices become tangle, the flow has a strong random element, varying rapidly from point to point (lost of inversion)

Quantum turbulence in a trapped Bose-Einstein condensate

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(Received 16 March 2007; published 31 October 2007)

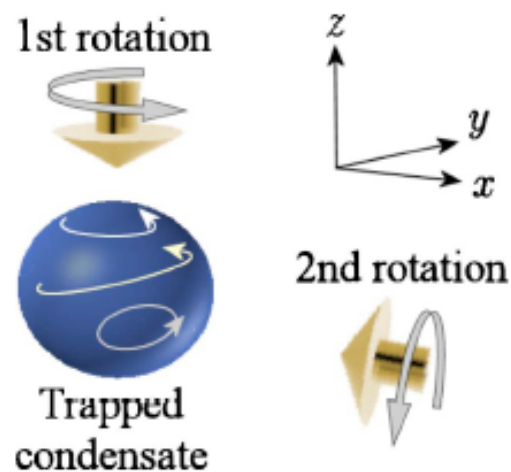


FIG. 1. (Color online). Schematic sketch of the rotation. The first rotation is applied along the z axis and the second rotation is applied along the x axis.

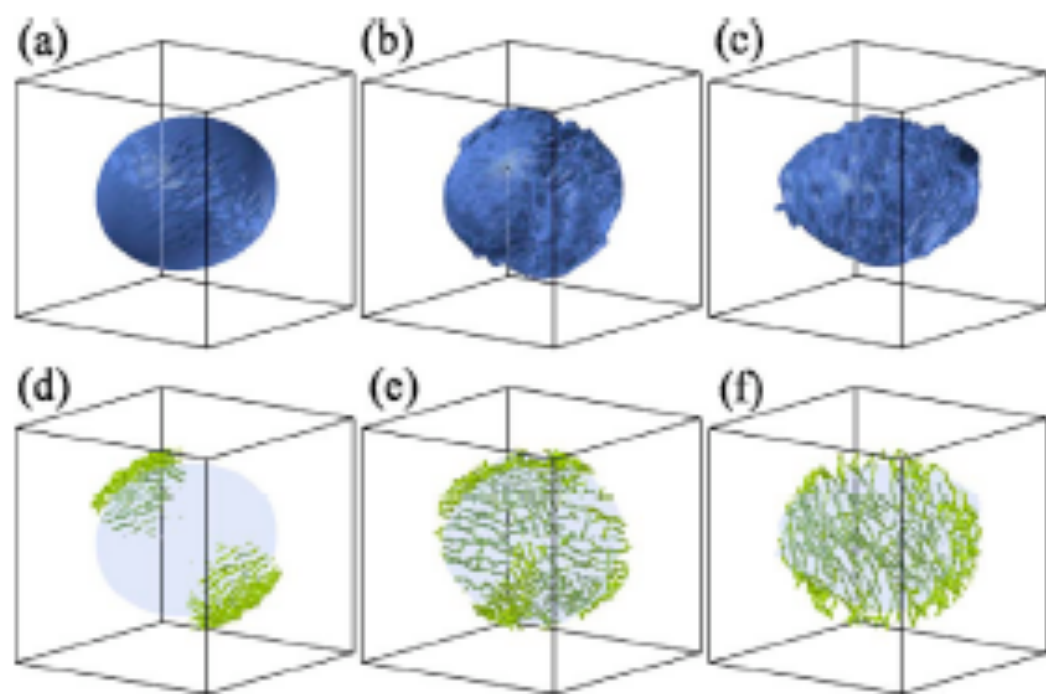
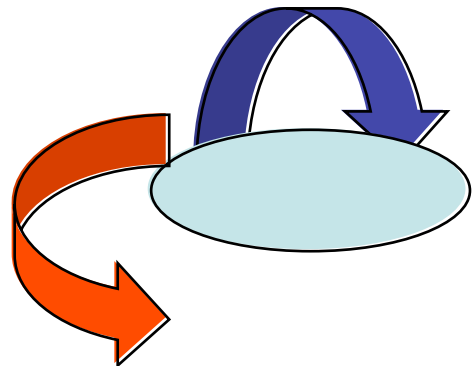
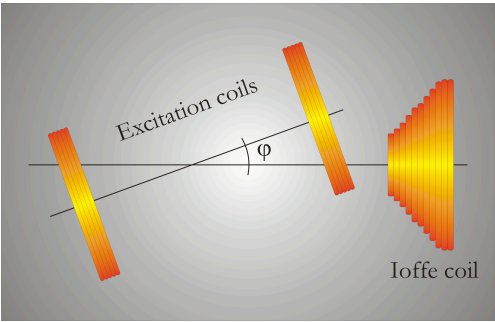


FIG. 4. (Color online). Isosurface plots of 5% of the maximum condensate density (a)–(c) and configuration of quantized vortices inside the Thomas-Fermi radius R_{TF} (d)–(f). (a), (d) $t\omega = 10$; (b), (e) $t\omega = 50$; (c), (f) $t\omega = 300$. The method for identifying vortices in (d)–(f) is the same as that in Fig. 7 in Ref. [15].



CONCLUSIONS:

- EXCITATION OF VORTICES WITHOUT DIRECT ROTATION
- EVOLUTION TO TANGLE VORTICES – lost of inversion property
- FRAGMENTATION
- CLUSTER OF THREE VORTICES: TWO DIFFERENT SPATIAL STRUCTURES

THANKS