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Satellite Navigation Science and Technology for Africa

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Introduction to Clocks, GPS time, Precise Time Applications (Part 1)

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#### **Time and Time Transfer**

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# Legal Note

These viewgraphs are intended to cover technical aspects of the timekeeping art, but to specifically exclude legalities and/or government policy. If by accident any public timekeeping policy is alluded to, such allusions should be considered the personal opinions of Dr. Matsakis and not a representation of current or future policies of the U.S. Naval Observatory, Department of Defense, or U.S. government.

# **Course Outline**

A. What is Time?

#### **B.** Pictorial Representation of Timekeeping Math

- Characterizing Clocks
  - Noise types
  - Stability measures
- Generation of timescales, including UTC
- Steering Clocks
- **C. Time Transfer** 
  - Telephones, modems
  - Internet: NTP
  - GPS
  - Two Way Satellite Time Transfer

#### **D.** Timing in the Future

Appendix 1: Parade of Clocks

Appendix 2: Philosophy of Time, including Relativity

Appendix 3: Statistical Details

Appendix 4: Timescale Details

Appendix 5: Control Theory

Appendix 6: Time Transfer Details

#### What Is Time?

According to Webster's New Collegiate Dictionary: "The measured or measurable period during which an action, process, or condition exists"

**According to Demetrios Matsakis:** 

**"That coordinate which can be most simply related to the evolution of closed systems"** 

#### Time as Defined by Measurement

"The second is the duration of 9,192,631,770 periods of radiation corresponding to the transition between the two hyperfine levels of the ground state of the undisturbed cesium-133 atom" Time is the phase of this radiation.



# Why not just use the Earth's rotation?

# Length of Day (LOD) 1620-2006



Sources: F.R. Stephenson and L.V. Morrison, *Phil. Trans. R. Soc. London* A313, 47 – 70 (1984), http://maia.usno.navy.mil, and ftp://maia.usno.navy.mil/ser7/finals.all

#### Schematic Illustration Of The Forces That Perturb The Earth's Rotation



Source: Thomas Gold, Nature

#### Polar Motion (1984-2002)



Source: http://giub.geod.uni-bonn.de/vlbi/IVS-AC/combi-all/start.html

# Variations in Length of Day



# Modern Life has LONGER days

- Tides are oceans following moon
  - "Crashing" into coastline and seafloor
- Tides slow down the rotating Earth
  - Days get longer, 1 day approaches 1 month
  - Moon's orbit gets further away
  - Sun and other bodies also have effects
- Earth has lost 14 hours since 1815 BC
  - From Chinese solar-eclipse records
- ~100 million years ago, day lasted only 20 hours
  - From fossilized nematodes

#### Even the cheapest atomic clock is more precise than the Earth



1. Light from <sup>87</sup>Rb lamp contains both 3-1 and 2-1 lines.

2.85Rb Cell filters out the 2-1 line and transmits the 3-1 line.



- The filtered light "optically pumps" the "Rb atoms in the resonance cell from level 1 to 3.
- A Microwave signal at a frequency of 6.84 GHz is injected into the cell and induces transition from level 2 to 1.
- When the injected wave frequency matches the difference of the 2-1 line, the photo-diode detects a reduction in the intensity of the transmitted light.

#### Source: www.accubeat.com

#### Cesium Standard



Source: John Vig

#### Hydrogen Maser Frequency Standard



Figure 11.2 The basic elements of a hydrogen maser

# **Time & Frequency Units**

TIME				FREQUENCY	
				$f=(t_b-t_a)/\Delta T$	
Second	1.0 s	S	10 <sup>0</sup> s	1 s/day	1.16 10-5
Millisecond	.001 s	ms	10 <sup>-3</sup> s	1 ms/day	1.16 10 <sup>-8</sup>
Microsecond	.000001 s	us	10 <sup>-6</sup> s	1 us/day	1.16 10 <sup>-11</sup>
Nanosecond	.000000001 s	ns	10 <sup>-9</sup> s	1 ns/day	1.16 10 <sup>-14</sup>
Picosecond	.00000000001 s	ps	10 <sup>-12</sup> s	1 ps/day	1.16 10 <sup>-17</sup>
Femtosecond	.00000000000001s	fs	10 <sup>-15</sup> s	1 fs/day	1.16 10 <sup>-20</sup>

# Modified Julian Day (MJD)

- Julian Day = JD = days since 4713 BC
  - Invented by Joseph Scalinger, circa 1600
  - JD increments at noon
  - Better for astronomers who observe at night
- Modified Julian Day = MJD = JD-2400000.5
  - Days since 1858.8, November 18, 1858
  - Increments at midnight
  - Better for most people

#### **Precision vs. Accuracy**



Source: John Vig's Tutorial

### Three Complementary Ways To Characterize Clock Time Series

I. Inspection II. Fourier Transform III. Variances of Differences: AVAR, TVAR, MVAR, HADAMARD, TOTDEV, etc.

#### **Illustrative Clock Data**



# **Five Fundamental Noise Types**

#### Combined, they can model clock noise



Noise in clock phase (time) also termed phase modulation (PM) Noise in clock frequency also termed frequency modulation (FM)



#### "With five parameters I can fit an elephant." - Enrico Fermi

#### **Fourier Transform?**

Works for every function F(x)

•F(x) = sum of sines and cosines

•F(x)=  $\Sigma [A_k * sin(2\pi kx) + B_k * cos(2\pi kx)]$ 

•F(x)=  $\Sigma [A_k * sin(2\pi kx + \delta_k)]$ 

Standard for many applications

### **Fourier Transform of Noise Models**

#### Power Spectral Density is square of plotted amplitude (technique works better for periodic variations)



#### How to Quantitatively Measure a Clock's Time/Frequency Accuracy/Precision?

It could be measured by the data's Root Mean Square (RMS), which is also the square root of the variance (VAR).

Unfortunately, if a clock changes frequency systematically over its life, its time and frequency RMS and VAR are unbounded.

Every clock we know of does this.

### **Rephrase The Question**

How much does the frequency vary from one interval, of duration  $\tau$ , to the next interval?

- That's the Allan Deviation (ADEV)
- ADEV=square root of the Allan Variance (AVAR)
- ADEV is also written  $\sigma_v(\tau)$
- AVAR is also written  $\sigma^2_{v}(\tau)$  )

#### **Example: Clock Whose Frequency Increases**



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#### **Example: Averaging Adjacent Frequency Bins**



Time (Arbitrary Units)

How does the Allan Deviation (ADEV, or  $\sigma_y(\tau)$ ), depend upon the kind of noise in the time series?

### Allan Deviation of Random Walk and Random Run



# **Typical Maser Sigma-Tau Pattern**

White Noise dominates over shortest averaging times RandomWalk FM=Random Run PM over longest averaging times



### Problem

Allan Deviation can't distinguish between white phase noise and flicker phase noise.

#### **NO PROBLEM**

Use Modified Allan Deviation (MDEV)

#### **How MDEV is Defined**

Like ADEV, except replace each freq by an average of frequencies of nearby points

If you multiply MDEV by  $\tau/sqrt(3)$ , you get the

Time Deviation, TDEV. TVAR is the square of TDEV.

# How does the Time Deviation (TDEV), depend upon the kind of noise in the data?

### **Example: TDEV of White Phase and Random Walk Noise Models**



# TDEV distinguishes White PM from other noise types



**TDEV**= Time Deviation

# **One of Many Statistical Pitfalls**

All of the discussed measures are insensitive to overall Phase/time slopes, so there is no harm in removing or adding such slopes to data. In fact, you usually should remove slopes to avoid binning quantization problems.

BUT... If you detrend data with a higher-order fit, you will artificially force the statistic towards 0 for large tau. You should *never* remove a second-order term to compute an Allan deviation.
#### **Stability of Various Frequency Standards**



Source: <a href="http://www.ieee\_uffc.org/fc">http://www.ieee\_uffc.org/fc</a> (John Vig and R. Sydnor) 35

## What is a Timescale?

•A useful average of clocks

- •Usually a weighted average of observed minus predicted data.
- •Timescales must not jump
- •Goal is to measure time better than any individual clock
  - •Can't optimize everything at the same time
  - •Should be optimized for goals of interest
    - •Measure "absolute time" of a clock ensemble?
    - •Produce a constant frequency?
      - •How much do you care what that constant is?
    - •Track a reference clock or timescale (steering)?
    - •Trade precision for robustness?
    - •Save money on computers and mathematicians?

# **Continuity Constraint**

- •Timescale must not jump
- •A clock model helps when
  - Clocks are added
  - Clocks are removed
  - Clock weights are changed
  - A clock misbehaves

•By making identification easy

•Some prediction algorithms in use today (details in appendix): •Polynomial

•BIPM (Algos), USNO (Percival Algorithm)

•Exponential Filter

•NIST, NICT

•Adaptive ARIMA (Auto-Regressive Integrated Moving Average) •INPL

•Kalman Filter

•GPS Composite Clock, IGS

## In Modeling, Try To Work with White Noise

• Quantities are well-defined

- Most theorems apply only to white noise
- If the noise or parameter variation isn't white, whiten it if possible:
  - A. Add another parameter
  - B. Replace data by their Nth order differences

(e.g. convert time to frequency)

C. Chose the time-interval where it is white

#### **Continuity from Averaging Frequencies**



1. Phase data from two clocks (simple average would jump when clock 2 availability changes

- 2. Data of the two clocks after conversion to frequency (freq point= difference of 2 time points)
  - 3. Average the frequencies of the two clocks



4. Sum frequency average to create time average (Plotted with original phase data of two clocks)

## **Clock Weights in Timescales**

Optimal weighting depends upon •Clock Statistics •If Gaussian, weight by (1.0 /Variance) •Stability interval of interest •Could weight by 1.0/(Allan Variance) •Effects if highly weighted clock fails •If you can determine it is failing •How well above are known

## **Timescale Summary**

Timescale algorithms can differ in:

- 1. Continuity constraint
- 2. Clock prediction method
- 3. Clock weighting
- 4. Data editing

#### Each of these points is a matter of active research.

# Coordinated Universal Time (UTC)

- International Time Standard
  - Treaty of the Meter
- •Computed by International Bureau of Weights and Measures (BIPM)
  - •BIPM located near Paris France
  - Data from ~50 institutions
  - Data from > 200 atomic clocks
- Computed and distributed by months
  - •5-day spacing, precise to 0.1 ns
  - •Emailed 10-15 days after month ends

#### **Contributors To EAL (UTC) By Weight**



## **How BIPM Computes UTC**

- Step 1: Generate EAL
  - EAL=Echelon Atomique Libre
    - French for Free Atomic Time Scale
  - EAL=Average of "secondary standards"
    - Clocks whose calibration is not maintained
- Step 2: Generate TAI
  - TAI=International Atomic Time
  - Adjusts frequency of EAL towards primary standards
  - Primary standards have calibrated frequency
    - Maintained by few institutions
- Step 3: Generate UTC (next viewgraph)

#### How the BIPM Computes UTC from TAI

- Problem: 1 day=24\*60\*60\*9,192,631,700 cs oscillations
  - What happens if the Earth slows down (or speeds up)?
- Compromise solution: Add and subtract seconds
  - Do not change the frequency of cesium atom
  - UTC=TAI+ integer number of seconds
  - Decided by Time Lords in 1971/2
- Additional second is called a *Leap Second* 
  - So far, have only inserted, never subtracted a second
- Could add at the end of any month
  - But so far have only added at end of December or June
  - Decision is made by the Earth Rotation Service (IERS)
- Some people want to stop adding leap seconds

# **Multi-Cultural Time**

Free-running time scales: EAL(BIPM), A.1(USNO), AT1(NIST), TA(Lab\_X)

- Based only on available clock data, with no overt steering

International Atomic Time (TAI) and Coordinated Universal Time (UTC)

- EAL is average of all "secondary standards", or clocks that are not accurately and independently calibrated against definition of second.
- UTC is EAL after steering towards "primary frequency standards" of the PTB, NIST, SU, and BNM. Computed every month in 5-day points and distributed in middle of following month.
- UTC=TAI with leap seconds to correct for variable Earth rotation Terrestrial Time (TT)
  - UTC recomputed with hindsight, but offset by 32.184 seconds for historical continuity with Ephemeris time.

Real-time realizations of UTC

- Steered time scales such as UTC(USNO), UTC(NIST), UTC(Lab\_X)

All are Atomic Time, as they all get time from atomic oscillations

Usually, adjusting the rate of a clock to bring its phase (time) or frequency closer to a reference clock.

But one can also step the clock in time (phase),

or accelerate it by changing the frequency's rate of change

### **Steering Definitions**

#### Synchronization Alignment of two sources of time

Syntonization Alignment of two sources of frequency *Equivalent to* Alignment of two sources of time, except for unknown calibration bias

### Why do we steer clocks?

To create synchrony and syntony.

For most communication applications, syntony is all that is required.

For navigation and GPS synchrony is crucial, yet you can't maintain synchrony without syntony.

### **Omnipresence of Steering**

#### **TAI = EAL + frequency steers to primary frequency standards**

(calibrated to meet definition of the second )
(EAL = ave of >200 clocks, including USNO's)

UTC = TAI + leap seconds

(crude steers, in phase, to Earth's rotation)

UTC(k) = TA(k) + steers to UTC = realization of UTC by laboratory k (TA(k) = ave of Lab\_k's clocks)

**GPS\* = Unsteered GPS clocks + steers to UTC(USNO) [in acceleration]** (Composite Clock= implicit average of steered satellite and monitor station clocks)

Telephone's Time = crystal + steers to UTC(k) or GPS\*

Atomic Clock's time = clock's crystal + steers to atomic frequencies

(GPS\* denotes GPS Time with leap seconds added)

## Proportional Steering (similar to PID Steering)

Change frequency of clock by: G<sub>X</sub> times its Time Offset + G<sub>Y</sub> times its Frequency Offset

ALL steering involves a trade-off between frequency stability, time stability, and control effort. For proportional steering, Linear Quadratic Gaussian (LQG) theory can compute the optimal gains ( $G_X$  and  $G_Y$ ) for your stability goals.

See Koppang and Leland, 1999, IEEEE Trans. Ultrason. Ferroelect., Freq. Control 46, pp 517-522. See also Appendix IV.

## **Improvement Due to Steering**



#### **GPS Steering**



#### GPS Time As Measured, modulo 1 sec



**Broadcast Corrections to Correct to UTC(USNO) improve** performance to almost 1 ns RMS.

## **GPS** Timescale

26+ satellite clocks

- Cesium and Rubidium
- 11 monitor sites (as a result of AII)
  - Cesiums, except for masers at AMC and USNO-DC
  - Pre-AII had only 5 monitor sites

Real-time constraints

- 15-minute quantization
- Satellite uploads typically 1/day/satellite
  - User often gets day-old information
  - Consistency between satellites required

## **GPS Clock Models**

Three parameters/clock: time, frequency, drift

- These correct the clock data
- Every new or reset clock corrected to GPS Time and Frequency

GPS used to have a Master Clock

- Its clock state was fixed, with unchanging parameters
- Concept quickly abandoned as not robust enough

GPS Composite Clock (GPS Time)

- All component clocks treated the same by Kalman Filter
- Composite Clock is weighted average of all corrected clocks
  - Implicit timescale no need for Kalman Filter to compute
- Realized by every corrected satellite or site clock

- Used to compute GPS Time, with steering Estimates clocks, satellite orbits, "nuisance parameters"
- Does not yet estimate troposphere
- Variations map strongly into site clock estimate
   No external measure of truth
  - USNO time input comes later
- Reference: Brown, ION-GPS, 1991

# What is a Kalman Filter?

#### Mathematical description of how every sane person thinks

- You have an initial opinion
  - I always thought Paris was a beautiful city
- You allow for evolution
  - They are restoring some of the artwork, and building a memorial to Dianna
  - They are encouraging bicycles, but traffic and pollution are probably still bad
  - So Paris should be a little more beautiful now
- You know how confident you are of that opinion
  - I'm not very sure, because I had only seen Paris in old Hollywood movies
  - I can't trust newspaper stories about what they are doing
- You gather some new data
  - I visit BIPM
- You form a new opinion and stronger confidence evaluation
  - I know Paris is extremely beautiful
- You realize that things can change
  - I think Paris will become more beautiful, because they are buying more artwork

# Kalman filters are Least Squares

- If no evolution, exactly equivalent to Least Squares
- Example:
  - You have averaged N data points
    - Call your average <old\_ave>
  - You get a new data point, "x"
  - Could average the N+1 data points
    - Computer has to have stored all N old data points
  - Kalman alternative: (x+N\*<old\_ave>)/(N+1)
    - Computer only needs to store 2 old things: N and <old\_ave>
- Filter developed for navigation in the 50's/60's (http://en.wikipedia.org/wiki/Kalman\_filter)

# Kalman Filter Formalism

You have your best parameter estimate(s) x, which can be a vector

- Predict current state from past data (with evolution)
  - Example:  $x_{\text{predict}}(t) = x(t-\tau) + \tau * y(t-\tau)$
- Estimate uncertainty of that prediction
  - Example:  $[\sigma_x(t)]^2 = [\sigma_x(t-\tau)]^2 + [\tau * \sigma_y(t-\tau)]^2 + Q$
  - Q allows for unmodelled changes to parameters

You then make measurement, z, and relate it to parameter estimates

- Example: z = H\*x(t) + noise
- The difference between z and H\*x is called the innovation

Update your parameters

- Example:  $x(t) = x_predict(t) + K*(z-H*x_predict(t))$
- If the innovation is 0, you won't be changing your parameter estimates
- If the innovation is not 0, the Kalman Gain (K) decides how you change
- Example:  $x(t) = x_predict(t) + K*(z-H*x_predict(t))$

Increase your confidence

 $-\sigma_x(t)$  reduced as Gauss would predict

Optimal in well-modeled white Gaussian world, with uncorrelated data

- Usually, none of those assumptions is 100% valid

## KF – notation and definitions

Introduction to Random Signal Analysis and Kalman Filtering, Robert Grover Brown

$$\mathbf{x}_{k+1} = \boldsymbol{\phi}_k \mathbf{x}_k + \mathbf{w}_k \tag{5.4.1}$$

The observation (measurement) of the process is assumed to occur at discrete points in time in accordance with the linear relationship

$$\mathbf{z}_k = \mathbf{H}_k \mathbf{x}_k + \mathbf{v}_k \tag{5.4.2}$$

Some elaboration on notation and the various terms of Eqs. (5.4.1) and (5.4.2) is in order:

 $\mathbf{x}_k = (n \times 1)$  process state vector at time  $t_k$ .

- $\phi_k = (n \times n)$  matrix relating  $\mathbf{x}_k$  to  $\mathbf{x}_{k+1}$  in the absence of a forcing function. (If  $\mathbf{x}_k$  is a sample of continuous process,  $\phi_k$  is the usual state transition matrix.)
- $\mathbf{w}_k = (n \times 1)$  vector—assumed to be a white (uncorrelated) sequence with known covariance structure.
- $\mathbf{z}_k = (m \times 1)$  vector measurement at time  $t_k$ .
- $\mathbf{H}_k = (m \times n)$  matrix giving the ideal (noiseless) connection between the measurement and the state vector at time  $t_k$ .
  - $\mathbf{v}_k = (m \times 1)$  measurement error—assumed to be a white sequence with known covariance structure and uncorrelated with the  $\mathbf{w}_k$  sequence.

#### KF – P's and Q's

Introduction to Random Signal Analysis and Kalman Filtering, Robert Grover Brown

The covariance matrices for the  $w_k$  and  $v_k$  vectors are given by

$$E[\mathbf{w}_k \mathbf{w}_i^T] = \begin{cases} \mathbf{Q}_k & i = k\\ 0, & i \neq k \end{cases}$$
(5.4.3)

$$E[\mathbf{v}_k \mathbf{v}_i^T] = \begin{cases} \mathbf{R}_k, & i = k\\ 0, & i \neq k \end{cases}$$
(5.4.4)

$$E[\mathbf{w}_k \mathbf{v}_i^T] = 0, \quad \text{for all } k \text{ and } i \qquad (5.4.5)$$

. . . .

$$\mathbf{e}_{k}^{-} = \mathbf{x}_{k} - \hat{\mathbf{x}}_{k}^{-} \tag{5.4.6}$$

.

and the associated error covariance matrix is\*

$$\mathbf{P}_{k}^{-} = E[\mathbf{e}_{k}^{-} \mathbf{e}_{k}^{-T}] = E[(\mathbf{x}_{k} - \hat{\mathbf{x}}_{k}^{-})(\mathbf{x}_{k} - \hat{\mathbf{x}}_{k}^{-})^{T}]$$
(5.4.7)  
$$\hat{\mathbf{x}}_{k} = \hat{\mathbf{x}}_{k}^{-} + \mathbf{K}_{k}(\mathbf{z}_{k} - \mathbf{H}_{k}\hat{\mathbf{x}}_{k}^{-})$$
(5.4.8)

where

.

 $\hat{\mathbf{x}}_k =$  updated estimate  $\mathbf{K}_k =$  blending factor (yet to be determined)

.

### Q's in terms of Hadamard Variance

$$\begin{bmatrix} q_1 \tau + q_2 \tau^3 / 3 + q_3 \tau^5 / 20 & q_2 \tau^2 / 2 + q_3 \tau^4 / 8 & q_3 \tau^3 / 6 \\ q_2 \tau^2 / 2 + q_3 \tau^4 / 8 & q_2 \tau + q_3 \tau^3 / 3 & q_3 \tau^2 / 2 \\ q_3 \tau^3 / 6 & q_3 \tau^2 / 2 & q_3 \tau \end{bmatrix}$$

 $_{\rm H}\sigma_{\rm v}^2(\tau) = (10/3)q_0\tau^{-2} + q_1\tau^{-1}$ 

 $+ (1/6)q_2\tau + (11/120)q_3\tau^3$ 

For 
$$\alpha = 2, 0, -2, -4$$

**References for Hadamard and Allan Variances** 

- 1) Van Dierendonck, McGraw and Brown, PTTI-84
- 2) Walter, PTTI-92
- 3) Hutsell, PTTI-95
- 4) Zucca and Tavella, 2005, Trans. UFFC 52, pp 289-296 63

## **Standard KF Operation**

#### **200** THE DISCRETE KALMAN FILTER



Figure 5.7. Kalman filter loop.

Introduction to Random Signal Analysis and Kalman Filtering, Robert Grover Brown

## **KF Without Prior Knowledge**

#### 6.2 ALTERNATIVE FORM OF THE DISCRETE KALMAN FILTER 219



Figure 6.1. Alternative Kalman filter recursive loop.

Introduction to Random Signal Analysis and Kalman Filtering, Robert Grover Brown

## **Infinite Covariance Problem**

N clocks imply N-1 measurable clock differences

The weighted average of the N clocks is not measurable

If clock states are with respect to unmeasurable reference, the average covariance will grow without bound

**Solutions** 

- Subtract out the overall unmeasurable covariance
  - Brown, ION-GPS, 1991
  - Greenhall papers on "Covariance x-Reduction", 2003 and 2006
- Reference clocks to average
  - Adds another equation

- Free to shift each clock's time, frequency, and drift by x, y, and z by same amount
- Has no effect on observables input to Kalman Filter
- Does change what the GPS user sees GPS Time, if unsteered, would just follow the weighted average of all its clocks

#### **Clock corrections do not affect Composite Clock**

#### Example

- 2 clocks, A and B, weights w and (1-w)
  - Clock B can be considered all other clocks averaged together
- GPS Time is  $w^*A + (1-w) *B$
- Assume clock A has variation x
  - All users see pre-correction data from A varying by x
  - And GPS Time therefore will appear to vary by w \*x
- Kalman Filter corrections will not change this
  - Corrects clocks because difference A-B changes by x
  - Clock A correction is (1-w)\*x
  - Clock B correction is -w \*x
  - Net correction to GPS Time is zero
    - Do the math: w\*(1-w)\*x –(1-w) \* w \* x=0
- So GPS Time, the corrected average, changes by w\*x
  - Composite clock changes as the weighted average of its uncorrected clocks

#### GPS Satellite Clock Stability (~IGS)



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#### **Broadcast GPS Performance**



#### **GPS III will be much better**
## **Unsteered GPS Composite Clock**



## The solution: UTC(USNO)

GPS Composite clock steered to UTC(USNO) Daily uploads GPS-UTC(USNO)

GPS steered in acceleration, not frequency

- Add  $+10^{-19}$  /s or  $-10^{-19}$  /s to acceleration of every clock
- Bang-bang steering
- Minimizes frequency changes between daily uploads
- GPS-III to have cross-links
  - Single upload to change all satellite clock messages

Picture and details on next two viewgraphs

## **Bang-Bang Examples: 3 Cases**



## GPS "Bang-Bang" Algorithm

Acceleration-based, so as to optimize frequency stability when satellites are updated at different times **Accelerate clocks by either**:

+ 1 . E - 19 s/s - 1 . E - 19 s/s or zero (rarely).

#### **Sign of Acceleration**

- I. If GPS moving away from UTC (USNO), accelerate to approach it.
- II. If GPS is approaching UTC (USNO), sign of acceleration is opposite to slope, except that if doing so constantly thereafter would result in GPS - UTC (USNO) never becoming zero, in which case acceleration has same sign as slope.

#### GPS Time As Measured, modulo 1 sec



**Broadcast Corrections to Correct to UTC(USNO) improve** performance to almost 1 ns RMS.

## **Time Transfer**

**Definition:** The comparison of two sources of time.

Terminology: Clock (A) - Clock (B)
+ Value: Clock (A) is ahead of Clock (B)
- Value: Clock (B) is ahead of Clock (A)

## **Definition:** The relative change in time between two time sources.

 $[(Clk(A) - Clk(B))_{T2} - (Clk(A) - Clk(B))_{T1}]/(T2 - T1)$ + Value: Clk(A) is higher in frequency than Clk(B)

- Value: Clk(B) is higher in frequency than Clk(A)

#### The medium should not be the message ...



a) One-Way Time Transfer



b) Common-View Time Transfer



c) Two-Way Time Transfer

## **Time Balls**



Operational for USNO: 1845 - 1936 Ceremonial at USNO: 2000 - ?

## **Telephone Time Transfer**

- I. Voice Announcers: 1 second at best
  - human response time a factor
- II. Modems: As good as 1 ms, provided
  - Sender's system delay subtracted (USNO's delay is 1.7 +- .4 ms)
  - Can use remote loopback feature to measure line delay
  - No satellite connection (would add about .25 seconds)

## **Network Time Protocol (NTP)**

- Computer to Computer Time Transfer

   via LAN or Internet
- Server synchronized to UTC (USNO) via GPS receiver, or to UTC (NIST) via modem, or directly to any realization of UTC
- User sends NTP signal to server, analyzes response to get time
  - Limited by non-reciprocity in path
  - If over LAN: <1 msec
  - If over Internet: 1-100 msec
    - Gets worse as number of hops increases
    - Vagaries of internet routing can result in long-lasting biases
    - Transoceanic can be much worse if go by wildly different routes

## **NTP Assumes Reciprocity**



network delay:  

$$\delta = (T_4 - T_1) - (T_3 - T_2)$$
  
 $\Theta = \frac{(T_2 - T_1) + (T_3 - T_4)}{2}$ 

## **NTP: Illustrative Data**



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## **NTP Applications**

- Millions of direct users
  - Such as your children and the White House
  - Unknown number of secondary users
- Some uses and applications of NTP
  - LAN networks monitoring, control, database
  - Teleconferencing, radio and TV programming
  - Bank and stock market computers
  - Encryption
  - Time-stamping for patents, etc.
  - Interactive simulation
  - Electrical power grid synchronization

## IEEE 1588, "Improved NTP"

- Intended for small networks
- •Fixed packet size,
- Keeps time-transfer processes at physical layer
- Each server sets its clock to that of closest server
- Only one route between servers
  - reciprocity is assured
  - impedes internet-wide applications
- Much greater precision: 20-100 ns
- •Under development: <u>http://ieee1588.nist.gov</u>
- Large-network analog being initiated
  - •See http://www.dspcsp.com/tictoc

#### **One-way Earth-based Radio Broadcasts**

I. Low-Frequency (code only)

WWVB (NIST) 60 kHz Accuracy: 500 microsec if known location Precision: 1 microsec

LORAN (U.S. Coast Guard)

100kHz
No time tags\*
Use Time of Coincidence
Accuracy: <300 ns\*</li>
Precision: 100 ns\*
Limited by weather patterns\*
\* E-Loran will enhance

II. High-Frequency (code & voice) WWV and WWVH (NIST) CHU (Canada) 2.5-20 MHz Accuracy: a few milliseconds Limited by number of ionospheric hops in travel path

III. European and Asian Services DCF77 (Germany) 77.5 kHz

http://www.ptb.de/en/org/4/44/442/dcf77\_1\_e.htm

#### **Detailed View Of Individual Loran Pulse**



## **Enhanced Loran**

- Long-term funding assured in February 2008
  - Ends >8 years of uncertainty
- Better clocks at transmitters
- All-in-view rather than chain concept
- Users can have H-field (static free) antennas
- Broadcasts GPS corrections
- Broadcasts time directly
- Broadcasts more refined Loran corrections

## Time is at the Core of GPS



GPS receivers measure distance from satellites A, B, and C by the pseudoranges a, b, and c. Pseudoranges are measured as travel times, and converted to distances.

If the receiver is at known position and calibrated, time can be obtained from observing one satellite.

If the receiver's time is known and its timing delays are calibrated, its antenna's position is at the intersection of spheres centered on the satellites with radii a, b, and c.

If the receiver's time and position are not known, they can be inferred from observations of four satellites - but the time offset must be calibrated.

## How does GPS set time on a satellite?

- 1. Observe and compute each satellite's time as broadcast
  - Raw data are pseudoranges
  - Correct for travel time with broadcast orbits, ionosphere, relativity, etc.
    - These are in the navigation and ephemeris messages
  - Apply broadcast clock corrections from subframe 1 of navigation message
  - This is GPS Time as broadcast by the satellite and seen by receiver
- 2. The GPS Master Control Station uses these same corrections to compute GPS Time with the Kalman Filter (MCSKF)
  - GPS Time at the MCSKF is a weighted average of each satellite's corrected time
- 3. GPS MCS uploads new subframe 1 values, and they are broadcast
- 4. The difference between GPS Time and UTC(USNO) is broadcast in the navigation message subframe 4, page 18
- 5. The GPS receiver subtracts them to get UTC(USNO) as broadcast from the satellite
- 6. User can get better values by averaging over satellites

## **GPS Timing Receivers**

- Extract either UTC (USNO) or GPS Time
  - GPS Time is for navigational solutions only and does not include leap seconds
    - Users who mistake GPS time with UTC sometimes think their receiver is off by 10's of seconds.
- Time Comparison: 2 ways
  - 1. Receiver's internal time interval counter (You input your own signal, it compares)
  - 2. Receiver's output 1-PPS signal

(You compare to your own signal, externally)

## **Receiver Calibration: 2 ways**

#### 1. Absolute Calibration

2. Relative Calibration

#### Determine Receiver Component Delays

- antenna delay
- antenna cable delay
- receiver internal delays
- delays to any external measurement systems

#### Calibrated GPS Simulator Required

## **Relative Calibration**

#### Determine correction relative to a standard receiver through "side-by-side" comparisons

## **Relative Calibration**

- Common clock
- Common antenna, or precise antenna coordinates
- Track same satellites with both receivers

## Time Transfer via GPS

- Direct Access
  - Observe time directly off GPS code
  - Best to average over satellites
- Melting Pot or All-in-View
  - Average over satellites and/or time to obtain GPS-Clock
  - ClockA ClockB = (GPS ClockB) (GPS ClockA)
- Common View
  - Averages difference with individual satellites instead of differencing the average of individual satellites
  - ClockA ClockB = AVE{(Sat\_i ClockB)-(Sat\_i ClockA)}

## **GPS** Common-View



## **Some Sources of Error**

Multi-path Calibration Environment (temp, humidity, etc.) **Ionosphere & Troposphere Corrections** Antenna position Satellite clock errors Satellite position (orbit) errors

## **Ionospheric Modeling Geometry**



- Highly variable
  - 11-year cycle
  - Much less at night
  - Latitude (and longitude) dependant
  - Stronger at low satellite elevation
- Klobuchar model (broadcast)
  - ballpark accuracy: 10 ns
- Wavelength-dependent (L1 vs. L2)
  - Allows very exact removal
  - If you have two-frequency data
  - Civilians will shortly have twofrequency data from L5
  - Carrier phase techniques can infer

## Dry and Wet Components of the Troposphere



6.6 nanoseconds vertical delay, on average. Stronger at low elevations
90% due to nitrogen, proportional to ground pressure.
10% due to water, not proportional to ground humidity and anticorrelated with ground pressure. Can fit using elevation dependence.

# Price of mismodeled atmosphere and/or ionosphere:

- You will get the wrong time and the wrong position, and the error will be systematic
- The position offset will mostly be in the vertical direction (if you observe GPS satellites evenly over the sky).

## Multipath



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## Multipath

- Optimal antenna location:
  - ground level
  - empty parking lot
- Receivers have rejection algorithms
- Affects code more than phase
- Actually helps in urban canyons! "better late than never"

## **GPS** Carrier-Phase

#### SIGNALS/OBSERVABLES



## **GPS C/A Code Transition**



#### **Source: Powers et al., EFTF-02**

## **GPS** Carrier-Phase Time Transfer




http://igscb.jpl.nasa.gov

# WAAS for Time Transfer

Satellites at fixed position, so

- Can use directional antenna
  - harder to jam
- Can use high-gain antenna
  - more signal to noise
- Continuous coverage
  - carrier-phase simplified
- Steered to GPS time, UTC (USNO)
  - excellent backup potential



UTC(USNO)-WAAS NT (offset removed)

### **Two-Way Satellite Time Transfer**



# USNO Two-Way Satellite Time Transfer Earth Terminals





#### USNO BASE STATION ANTENNAS USNO MOBILE EARTH STATION

## Sagnac Effect



### Galilean, not "relativistic frame-dragging"

## **TDEV for Time Transfer Modes**



# **GPS Frequency and Time Users**

#### **Communications and IT**

Cell phones and pagers Large bandwidth transmissions Network Time Protocol (NTP) Satellite communication systems Military communication systems

#### Surveillance

Space debris, and worse Missile launches, good and bad Nuclear explosion detections

#### Science and Engineering

Power Grid Synchronization Generation of UTC Very Long Baseline Interferometry Pulsar Observations Neutrino detectors Gravity Wave Search DoD and Civilian Laboratories \* Earth rotation, UT1 \* Ionosphere measurements \* Troposphere measurements \*

\*use GPS carrier-phase data

# Appendices

- I. Parade of Clocks
- II. Philosophy of Time (and Relativity)
- **III.** Statistical Details
- IV. Timescale Details
- V. Control Theory
- VI. Time Transfer Details