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Exercises

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Exercises: Codeposition and Plasma Interaction with Deposited/Mixed Materials (JW Davis)

- 1.1)
 - a) Based on a maximum implantation energy of ~ 1 keV/T, and ignoring diffusion/permeation, show that retention due to implantation is not a major concern in ITER.
 - b) Consider the case where neutron damage leads to an internal trap concentration of ~ 0.005 traps/metal atom, and diffusion leads to such traps being filled to a depth of $\ell = \sqrt{D t}$ where $D = 2.9 \times 10^{-7} \exp(-0.39 \text{ eV} / kT) \text{ m}^2 / \text{s}$, and $T = 500\text{K}$. ($\rho_W = 19300 \text{ kg/m}^3$)
- 1.2) Estimate the amount of tritium used per full power, 400s, ITER shot. What % of the injected tritium is retained (assuming 1 g is retained). Base your calculations on a divertor pressure of 2 Pa and a pumping speed of $75 \text{ m}^3/\text{s}$.
- 1.3) Given a 1 GW_e fusion power plant, with a 10 kg in-vessel tritium inventory limit, calculate the maximum allowable deposition rate to allow one year of continuous operation.). Base your calculations on a $T_{\text{injected}}/T_{\text{consumed}}$ ratio of 25:1.
- 2.1)
 - a) Calculate the ionization mean-free-path for a Be atom with 1 eV entering the scrape-off plasma of a fusion reactor: $n_e = 10^{19} \text{ m}^{-3}$, $T_e = 100 \text{ eV}$.
 - b) Calculate the dissociation mfp for a CH_4 molecule (0.2 eV) entering the scrape-off plasma.
 - c) Repeat a) and b) for a divertor plasma with $n_e = 10^{20} \text{ m}^{-3}$, $T_e = 2 \text{ eV}$.
 - d) Given a uniform SOL with a thickness of 2 cm, what fraction of 1 eV Be atoms will penetrate to the core plasma.
- 2.2)
 - a) Given a core impurity content of 1% Be and $n_e \sim 10^{20} \text{ m}^{-3}$ just inside the last closed flux surface, estimate the flux of Be to the divertor plates for a tokamak the size of ITER. Assume a SOL thickness of 2 cm and $D_{\text{Be}} \sim 1 \text{ m}^2/\text{s}$.
 - b) If this impurity flux is distributed uniformly over the CFC target area, how long will it take to build up a 10 nm thick Be coating? ($\rho_{\text{Be}} = 1850 \text{ kg/m}^3$)
- 2.3) Carbon atoms are sputtered from a surface where there is a 3 T magnetic field with grazing incidence. If the C atoms leave the wall with $\sim 1 \text{ eV}$, how small does the ionization mfp need to be for the majority of atoms to be promptly redeposited? What plasma conditions are implied?
- 3.1) ITER is limited to an in-vessel inventory of 700 g T. Assume all of this T is contained in codeposits having a density of 1.2 g/cm^3 , a T/C = D/C ratio of 0.1, and coverage area of 10 m^2 . How thick will the deposits be?
- 4.1) Using SRIM (www.srim.org), estimate the rate of W atom sputtering due to 1 keV D^+ ions for a) pure W, b) 90 at% W and 10 at% C, c) 50 at% W and 50 at% C.
- 4.2) Repeat 4.1) for 1 keV C^+ ions.

Table 1: ITER surface Areas (Federici, 2001)

Component	Approximate Surface Area
First Wall (Be)	680 m ²
Divertor Target (CFC)	55 m ²
Divertor side wall, baffle (W)	50 m ²
Divertor dome (W)	30 m ²
Divertor private region, liner (W)	60 m ²

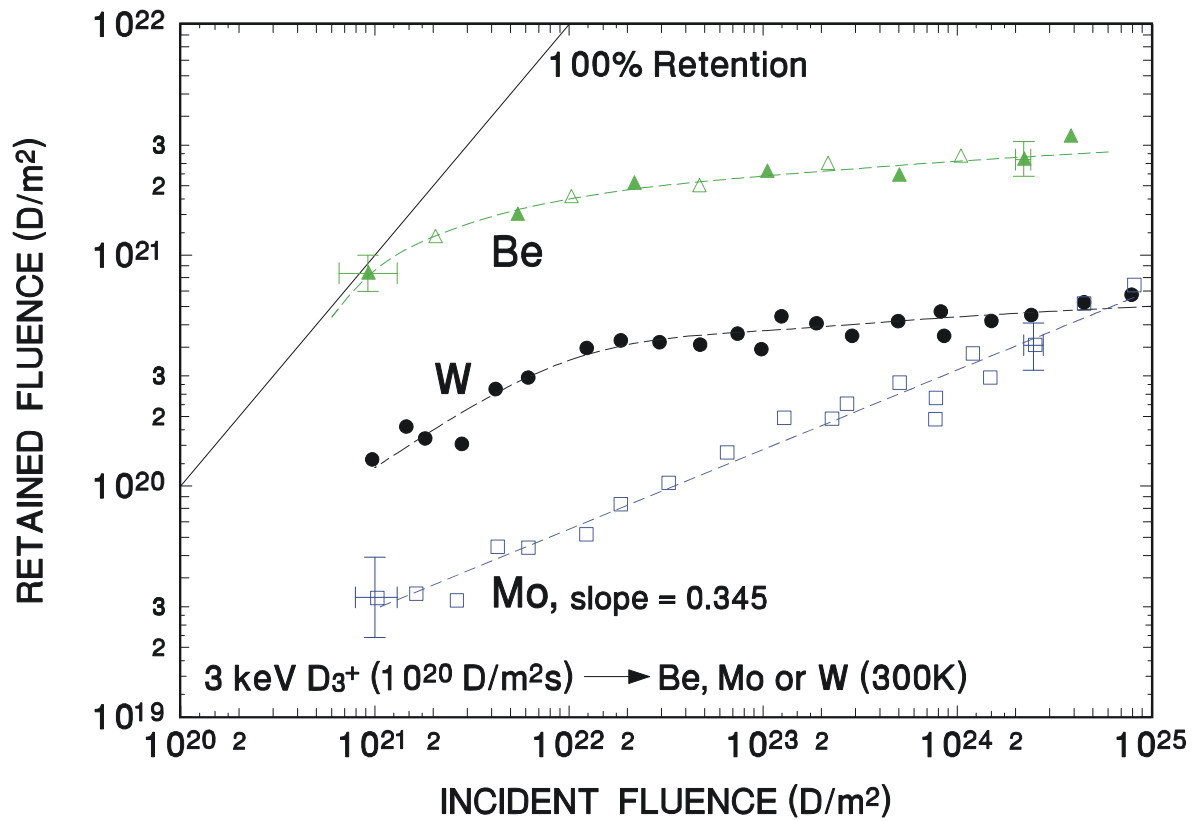


Figure 1: 1 keV D⁺ retention in Be, Mo and W at room temperature as a function of incident fluence. From Haasz and Davis, J. Nucl. Mater., 241-243 (1997) 1076.

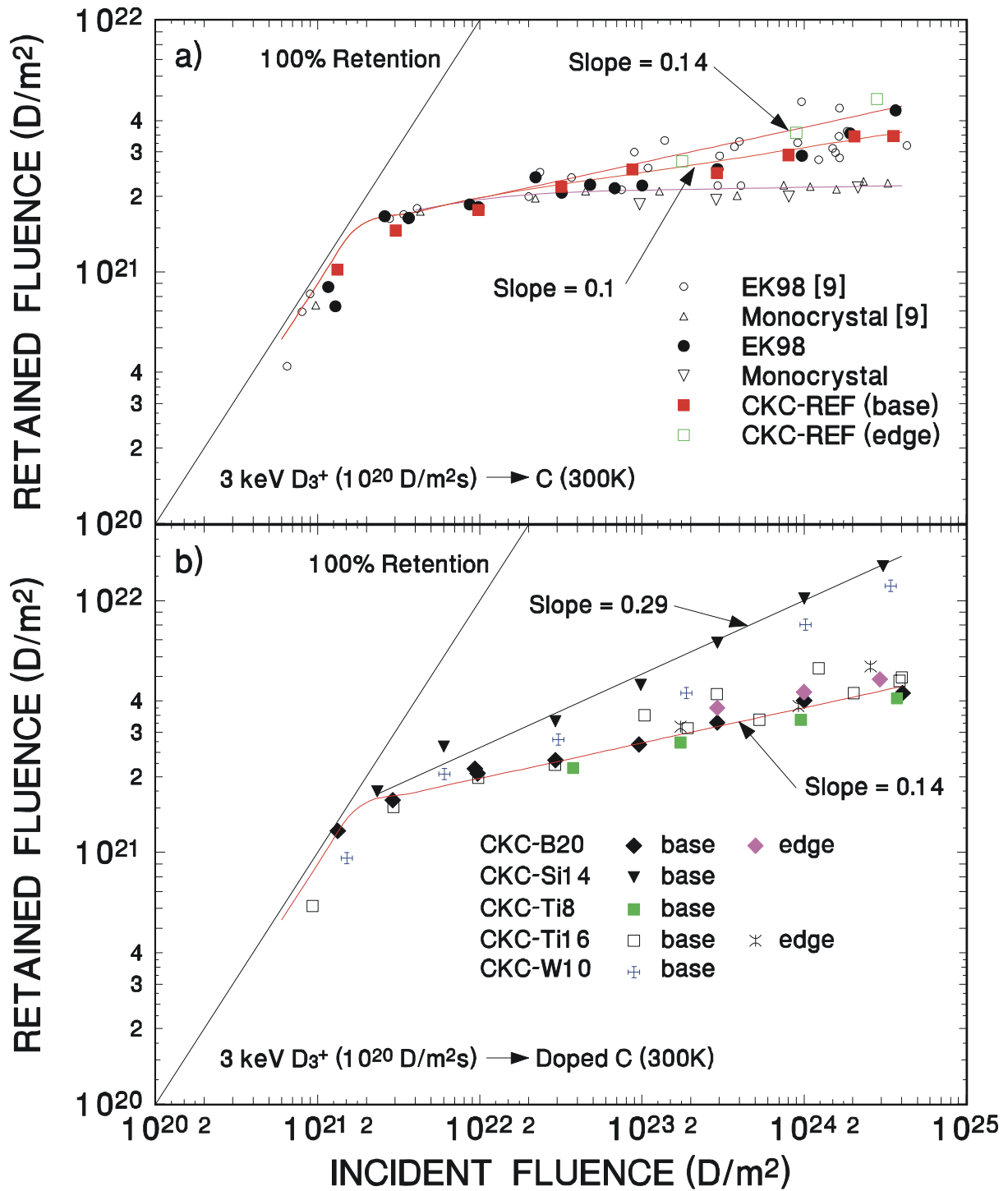


Figure 2: 1 keV D^+ retention in various graphites at room temperature as a function of incident fluence. From Haasz and Davis, J. Nucl. Mater., 232 (1996) 219.

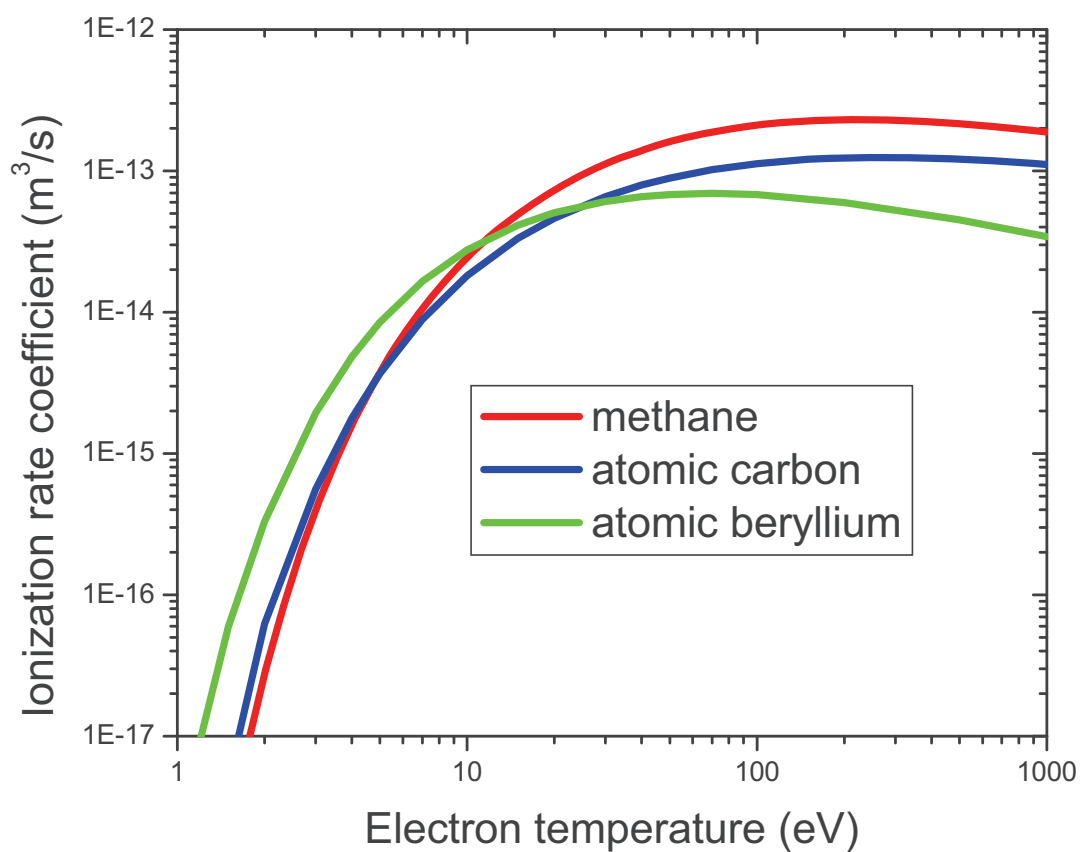


Figure 3: Ionization rate coefficients for CH_4 molecules, C atoms and Be atoms due to electron impact ionization. Atomic data from open-ADAS, methane data from <http://www.eirene.de>.

Exercises: Codeposition and Plasma Interaction with Deposited/Mixed Materials (JW Davis)

- 1.1) a) Based on a maximum implantation energy of ~ 1 keV/T, and ignoring diffusion/permeation, show that retention due to implantation is not a major concern in ITER.
- b) Consider the case where neutron damage leads to an internal trap concentration of ~ 0.005 traps/metal atom, and diffusion leads to such traps being filled to a depth of $\ell = \sqrt{Dt}$ where $D = 2.9 \times 10^{-7} \exp(-0.39 \text{ eV} / kT) \text{ m}^2 / \text{s}$, and $T = 500\text{K}$. ($\rho_W = 19300 \text{ kg/m}^3$)

a) At low temperature, 1keV T^+ implantation leads to saturated retention levels $\sim 10^{21} \text{ T/m}^2$ in Be, W; perhaps as high as 10^{22} T/m^2 in CFC materials.

Total wall area in ITER $\sim 875 \text{ m}^2$

$\Rightarrow$ retention $\leq 875 \times 10^{22} \text{ T atoms}$

$$M_T = 3 \times 1.67 \times 10^{-27} \Rightarrow 0.044 \text{ kg} \ll 1 \text{ kg}$$

Note that implantation is a "one time only" effect; this amount does not get implanted with every discharge.

b) $D = 2.9 \times 10^{-7} \exp(-0.39 \text{ eV} / 8.62 \times 10^{-5} \text{ eV/K} \cdot 500 \text{ K}) = 3.4 \times 10^{-11} \text{ m}^2/\text{s}$

$$\therefore \ell \leq \sqrt{Dt} = \sqrt{3.4 \times 10^{-11} \times 10,000 \times 400 \text{ s}} = 0.012 \text{ m} = 1.2 \text{ cm}$$

Number of W atoms: $19300 \text{ kg/m}^3 \Rightarrow \frac{19300}{184 \times 1.67 \times 10^{-27}} = 6.3 \times 10^{28} \text{ W/m}^3$

surface area $\sim 500 \text{ m}^2 \Rightarrow 500 \text{ m}^2 \times 0.012 \text{ m} = 6 \text{ m}^3$
 $\Rightarrow 3.8 \times 10^{29} \text{ W atoms.}$

$0.005 \text{ traps/W atom} \Rightarrow 0.0025 \text{ T atoms/W atom}$

$\Rightarrow 9.4 \times 10^{26} \text{ T atoms}$

$\Rightarrow 9.4 \times 10^{26} \times 3 \times 1.67 \times 10^{-27} = 4.7 \text{ kg}$

- 1.2) Estimate the amount of tritium used per full power, 400s, ITER shot. What % of the injected tritium is retained (assuming 1 g is retained). Base your calculations on a divertor pressure of 2 Pa and a pumping speed of 75 m³/s.

$$\text{pressure } 2\text{ Pa} \rightarrow \frac{2}{10^5} \times 2.7 \times 10^{25} = 5.4 \times 10^{20} \text{ molecules/m}^3$$
$$\Rightarrow \sim 5.4 \times 10^{20} \text{ T/m}^3 \quad (\text{assume DT molecules})$$

$$\text{pumping speed } 75 \text{ m}^3/\text{s} \Rightarrow 75 \text{ m}^3/\text{s} \times 400 \text{ s} = 30,000 \text{ m}^3$$

$$\text{T throughput: } 5.4 \times 10^{20} \text{ T/m}^3 \times 30,000 \text{ m}^3 = 1.6 \times 10^{25} \text{ T atoms}$$
$$\Rightarrow 0.081 \text{ kg}$$

$\Rightarrow$ Approximately 80g of T will need to be injected into the torus during a discharge to maintain a steady pressure.

$\Rightarrow$ For 1g retained per shot, $\sim 1\%$ injected T retained

- 1.3) Given a 1 GW_e fusion power plant, with a 10 kg in-vessel tritium inventory limit, calculate the maximum allowable deposition rate to allow one year of continuous operation.). Base your calculations on a $T_{\text{injected}}/T_{\text{consumed}}$ ratio of 25:1.

Amount of T burned per day :

$$\text{Energy per day} : 3 \times 10^9 \text{ W} \times 24 \times 60 \times 60 = 2.6 \times 10^{14} \text{ J}$$

$$\text{Energy per T} : 12.58 \times 10^6 \text{ eV} \times 1.6 \times 10^{-19} \text{ J/eV} = 2.8 \times 10^{-12} \text{ J}$$

$$\therefore T \text{ per day} = \frac{2.6 \times 10^{14}}{2.8 \times 10^{-12}} \approx 10^{26} \text{ atoms}$$

$$@ 5 \times 10^{-27} \text{ kg/atom} \Rightarrow 0.5 \text{ kg/day}$$

$$T \text{ flow through} : 25 \times 0.5 = 12.5 \text{ kg/day.}$$

$$\text{For 1 year} : 365 \times 12.5 \approx 4563 \text{ kg}$$

$$\text{Allowable retention} = 10 \text{ kg}$$

$$\Rightarrow \frac{10}{4563} \approx 0.2 \%$$

- 2.1) a) Calculate the ionization mean-free-path for a Be atom with 1 eV entering the scrape-off plasma of a fusion reactor: $n_e = 10^{19} \text{ m}^{-3}$, $T_e = 100 \text{ eV}$.
 b) Calculate the dissociation mfp for a CH_4 molecule (0.2 eV) entering the scrape-off plasma.
 c) Repeat a) and b) for a divertor plasma with $n_e = 10^{20} \text{ m}^{-3}$, $T_e = 2 \text{ eV}$.
 d) Given a uniform SOL with a thickness of 2 cm, what fraction of 1 eV Be atoms will penetrate to the core plasma.

Mean free path: $\lambda = \frac{v_{\text{beam}}}{n_e \langle \sigma v_e \rangle}$

a) $T_e = 100 \text{ eV} \Rightarrow \langle \sigma v_e \rangle_{\text{Be}}^{12} \approx 7 \times 10^{-14} \text{ m}^3/\text{s}$

1 eV Be atom: $v = \sqrt{\frac{2E}{m}} = \sqrt{\frac{2 \times 1.6 \times 10^{-19}}{9 \times 1.67 \times 10^{-27}}} = 4600 \text{ m/s}$

$\therefore \lambda_{12} = \frac{4600}{10^{19} \cdot 7 \times 10^{-14}} = 6.6 \times 10^{-3} \text{ m} = \boxed{6.6 \text{ mm}}$

b) $T_e = 100 \text{ eV} \Rightarrow \langle \sigma v_e \rangle_{\text{CH}_4}^{12} \approx 2 \times 10^{-13} \text{ m}^3/\text{s}$

0.2 eV CH_4 : $v = \sqrt{\frac{2 \cdot 0.2 \cdot 1.6 \times 10^{-19}}{16 \times 1.6 \times 10^{-27}}} = 1550 \text{ m/s}$

$\therefore \lambda_{12} = \frac{1550}{10^{19} \cdot 2 \times 10^{-13}} = 7.7 \times 10^{-4} \text{ m} = \boxed{0.8 \text{ mm}}$

c) $T_e = 2 \text{ eV} \Rightarrow \langle \sigma v_e \rangle_{\text{Be}}^{12} = 4 \times 10^{-16} \text{ m}^3/\text{s}$

$\langle \sigma v_e \rangle_{\text{CH}_4}^{12} = 2 \times 10^{-17} \text{ m}^3/\text{s}$

$\lambda_{12}^{\text{Be}} = \frac{4600}{10^{20} \cdot 4 \times 10^{-16}} = 0.12 \text{ m} = \boxed{12 \text{ cm}}$

$\lambda_{12}^{\text{CH}_4} = \frac{1550}{10^{20} \cdot 2 \times 10^{-17}} = 0.775 \text{ m} = \boxed{80 \text{ cm}}$

d) $\Gamma = \Gamma_0 e^{-x/\lambda} \Rightarrow \frac{\Gamma}{\Gamma_0} = e^{-20/6.6} = 0.048 \Rightarrow \boxed{\sim 5\%}$

- 2.2) a) Given a core impurity content of 1% Be and $n_e \sim 10^{20} \text{ m}^{-3}$ just inside the last closed flux surface, estimate the flux of Be to the divertor plates for a tokamak the size of ITER. Assume a SOL thickness of 2 cm and $D_{\text{Be}} \sim 1 \text{ m}^2/\text{s}$.
- b) If this impurity flux is distributed uniformly over the CFC target area, how long will it take to build up a 10 nm thick Be coating? ($\rho_{\text{Be}} = 1850 \text{ kg/m}^3$)

a) At edge of SOL: $D_{\text{Be}} \approx 1 \text{ m}^2/\text{s}$
 $n_{\text{Be}} \approx 0.01 \times 10^{20} \text{ m}^{-3} \approx 10^{18} \text{ m}^{-3}$

Flux into SOL $\approx D_{\text{Be}} \times \frac{\Delta n_{\text{Be}}}{\Delta x} \times \text{Area of plasma}$
 $\approx 1 \text{ m}^2/\text{s} \times \frac{10^{18} \text{ m}^{-3}}{0.02 \text{ m}} \times 500 \text{ m}^2 = 2.5 \times 10^{22} \text{ Be/s}$

b) 10 nm layer on 55 m²

$\Rightarrow 10^{-8} \text{ m} \times 55 \text{ m}^2 \times 1850 \text{ kg/m}^3 = 0.001 \text{ kg}$

$\Rightarrow \frac{0.001 \text{ kg}}{9 \times 1.67 \times 10^{-27}} = 6.7 \times 10^{22} \text{ Be atoms}$

$\therefore \frac{6.7 \times 10^{22}}{2.5 \times 10^{22}} \approx \boxed{2.7 \text{ s}}$

- 2.3) Carbon atoms are sputtered from a surface where there is a 3 T magnetic field with grazing incidence. If the C atoms leave the wall with ~ 1 eV, how small does the ionization mfp need to be for the majority of atoms to be promptly redeposited? What plasma conditions are implied?

$$\Gamma_L = \frac{m v_{\perp}}{q B} \quad v_{\perp} \approx \sqrt{\frac{2E}{m}} = \sqrt{\frac{2 \cdot 1 \cdot 1.6 \times 10^{-19}}{12 \times 1.67 \times 10^{-27}}} \\ \approx 4000 \text{ m/s}$$

$$\Rightarrow \Gamma_L = \frac{12 \times 1.67 \times 10^{-27} \cdot 4000}{1.6 \times 10^{-19} \cdot 3} = 1.7 \times 10^{-4} \text{ m} = 0.17 \text{ mm}$$

$\therefore$ we need to have $\lambda_{iz} \lesssim 10^{-4} \text{ m}$

$$\text{For } T_e \gtrsim 10 \text{ eV}, \quad \lambda_{iz} \approx \frac{v_{Te}}{n_e} \gtrsim 10^{-13} \text{ m}^2/\text{s}$$

$$\lambda = \frac{v}{n_e \lambda_{iz}} \Rightarrow n_e \approx \frac{v}{\lambda \lambda_{iz}} \\ \approx \frac{4000}{10^{-4} \cdot 10^{-13}} \\ = 4 \times 10^{20} \text{ m}^{-3}$$

This would be a very intense plasma to have right next to a solid surface.

- 3.1) ITER is limited to an in-vessel inventory of 700 g T. Assume all of this T is contained in codeposits having a density of 1.2 g/cm^3 , a T/C = D/C ratio of 0.1, and coverage area of 10 m^2 . How thick will the deposits be?

$$700 \text{ g T} \Rightarrow \frac{0.7 \text{ kg}}{5 \times 10^{-27} \text{ kg}} = 1.4 \times 10^{26} \text{ T atoms}$$

$$\frac{T}{C} = 0.1 \Rightarrow 1.4 \times 10^{27} \text{ C atoms.}$$

$$\begin{aligned} \text{total mass} &: 1.4 \times 10^{26} \times 3 \times 1.67 \times 10^{-27} \\ &+ 1.4 \times 10^{26} \times 2 \times 1.67 \times 10^{-27} \\ &+ 1.4 \times 10^{27} \times 12 \times 1.67 \times 10^{-27} \\ \hline &29.2 \text{ kg} \end{aligned}$$

$$\text{density } 1200 \text{ kg/m}^3 \Rightarrow \frac{29.2}{1200} = 0.024 \text{ m}^3$$

$$\text{deposition area} : 10 \text{ m}^2 \Rightarrow \text{thickness } \frac{0.024}{10} = 0.0024$$

$$\Rightarrow \boxed{2.4 \text{ mm}}$$

4.1) Using SRIM, estimate the rate of W atom sputtering due to 1 keV D^+ ions for a) pure W, b) 90 at% W and 10 at% C, c) 50 at% W and 50 at% C.

4.2) Repeat 4.1) for 1 keV C^+ ions.

10,000 particles.

Incident particle	Target	Yields at 0°	Yields at 60°
1 keV D^+	W	$y^W = 0.012$	$y^W = 0.015$
	90%W, 10%C (10 to 1)	$y^W = 0.011$ $y^C = 0.0013$	$y^W = 0.016$ $y^C = 0.0026$
	50%W, 50%C (1 to 1)	$y^W = 0.0078$ $y^C = 0.011$	$y^W = 0.012$ $y^C = 0.027$
1 keV C^+	W	$y^W = 0.46$ $y^C = 0.39$ backscatter	$y^W = 0.57$ $y^C = 0.58$ backscatter
	90%W, 10%C (10 to 1)	$y^W = 0.74$ $y^C = 0.04$ $y^C = 0.30$ backscatter	$y^W = 0.53$ $y^C = 0.05$ $y^C = 0.56$ backscatter
	50%W, 50%C (1 to 1)	$y^W = 0.38$ $y^C = 0.32$ $y^C = 0.20$ backscatter	$y^W = 0.34$ $y^C = 0.46$ $y^C = 0.44$ backscatter