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International Centre for Theoretical Physics



**2036-21**

**International Workshop: Quantum Chromodynamics from Colliders  
to Super-High Energy Cosmic Rays**

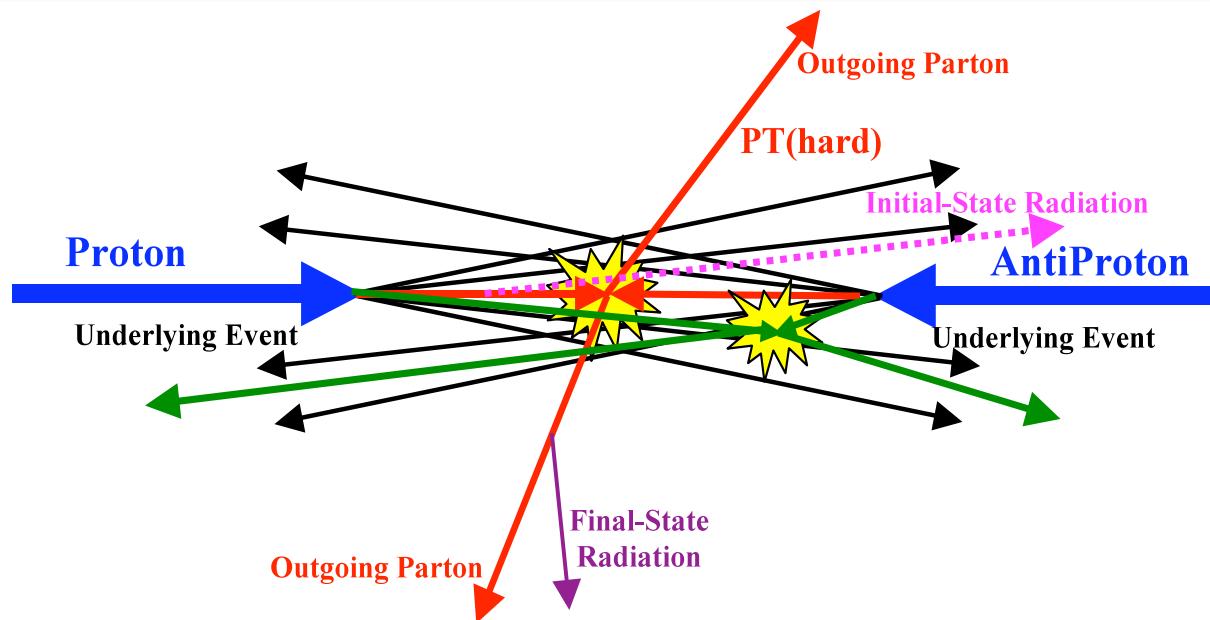
**25 - 29 May 2009**

**Multiple Parton Interactions, top-antitop, W+4j and Z+4j productions at the LHC**

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# Multiple Parton Interactions, top-antitop, W+4j and Z+4j production at the LHC



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# Facts and questions

- MPI established experimentally eg:  $\gamma + 3j$
- Each interaction hard enough to be treated by perturbative QCD
- $\sigma_{\text{DPI}} = \sigma_1 \sigma_2 / \sigma_{\text{eff}} / k$        $\sigma_{\text{eff}} \approx 14.5 \text{ mb}$       CDF       $k=1,2$
- $\sigma_{\text{TPI}} = \sigma_1 \sigma_2 \sigma_3 / \sigma'^2_{\text{eff}} / k$        $\sigma'_{\text{eff}} = \sigma_{\text{eff}}$  ?

Treleani argues for  $\sigma_{\text{eff}} \approx 12 \text{ mb}$  at the LHC

- Can MPI be a background to interesting physics ?
- Can MPI be studied in more complex environment than  $2 \rightarrow 2 \otimes 2 \rightarrow 2$  ?

Flavour dependence, x-dependence

## Method: $\sigma_1 \otimes \sigma_2 \otimes \dots$

- Generate events for the two processes separately: eg jj, jjW with MadEvent
- Superimpose one event from each sample
- No check on energy conservation (trivial to add)
- No flavour correlations (Treleani up to 40% reduction)
- No color correlations (irrelevant at generator level)
- Analyze: impose cuts on combined events

lv+4j can be produced in MPI as:

$jj \otimes jjW$

$jjj \otimes jW$

$jjjj \otimes W$

$jj \otimes jj \otimes W$

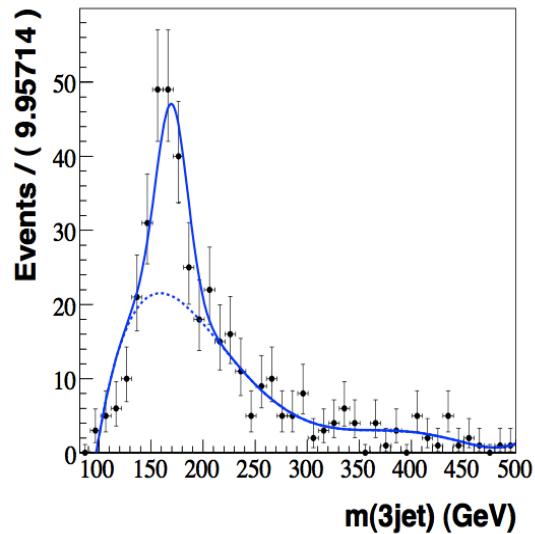
$W \rightarrow \mu\nu$  only

JHEP04(2009) 098  
+ Z4j unpublished

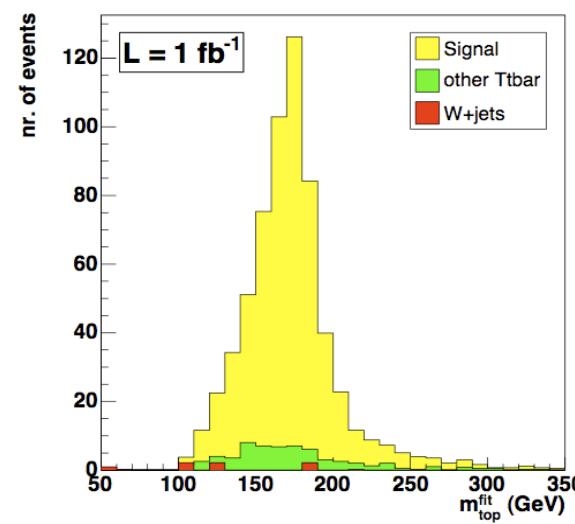
Single Parton Interactions: PHANTOM & MadEvent

# t-tbar production: an ideal playground

- Early measurement at the LHC
- $M_{top}$  is a fundamental parameter for the SM
- Best channel: semileptonic  $l\nu + 4j$
- Main background  $W+4j$ : 5 body final state



$100 \text{ pb}^{-1}$  No b-tagging  
Reconstruct from mass of jet triplet with largest pT  
Main background:  $W+4j$

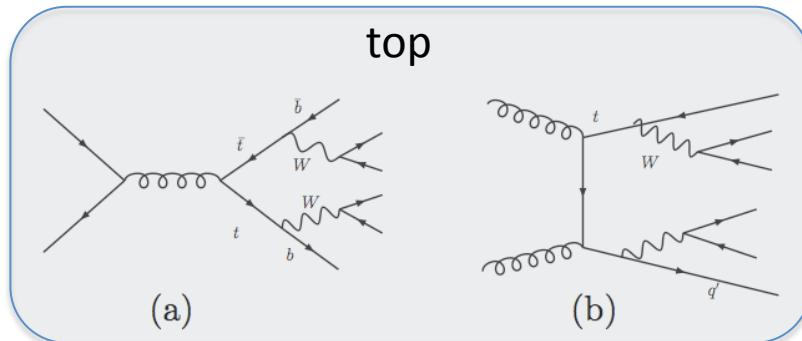


$1 \text{ fb}^{-1}$  b-tagging  
Full reconstruction of final state  
Main background: misidentification and combinatorics

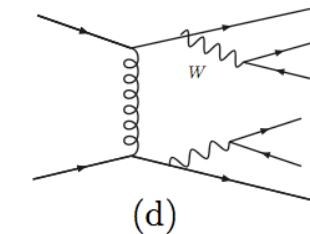
$$\alpha^4 \alpha_s^2$$

Three perturbative  
orders contribute to 4j+lν

top

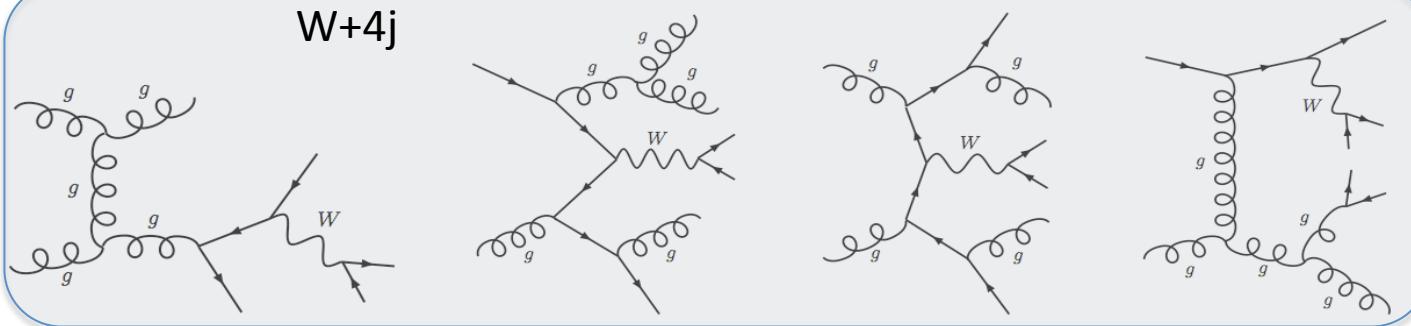


(c)

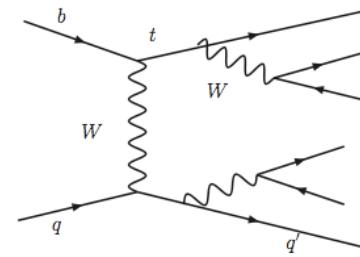
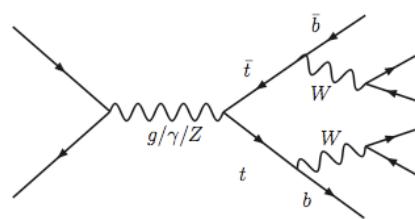


(d)

$W+4j$



$$\alpha^2 \alpha_s^4$$



$$\alpha^6$$

MPI

$$\begin{aligned} p_{Tj} &\geq 30 \text{ GeV}, \quad |\eta_j| \leq 5.0, \\ p_{T\ell} &\geq 20 \text{ GeV}, \quad |\eta_\ell| \leq 3.0, \\ M_{jj} &\geq 60 \text{ GeV} \end{aligned}$$

generation cuts

LHC luminosity:  
 Low  $30 \text{ fb}^{-1}/\text{year}$   
 High  $100 \text{ fb}^{-1}/\text{year}$   
 Total  $300 \text{ fb}^{-1}/\text{year}$

Process	Cross section	Combined
$jj$	$1.44\text{e}8 \text{ pb}$	$4.03 \text{ pb}$
$jj(\mu^-\bar{\nu}_\mu + \mu^+\nu_\mu)$	$6.54\text{e}2 \text{ pb}$	
$jjj$	$7.64\text{e}6 \text{ pb}$	$0.68 \text{ pb}$
$j(\mu^-\bar{\nu}_\mu + \mu^+\nu_\mu)$	$1.82\text{e}3 \text{ pb}$	
$jjjj$	$1.16\text{e}6 \text{ pb}$	$0.88 \text{ pb}$
$\mu^-\bar{\nu}_\mu + \mu^+\nu_\mu$	$1.09\text{e}4 \text{ pb}$	

Process	Cross section	Combined
$jj$	$1.44\text{e}8 \text{ pb}$	$0.27 \text{ pb}$
$jj$	$1.44\text{e}8 \text{ pb}$	
$\mu^-\bar{\nu}_\mu + \mu^+\nu_\mu$	$1.09\text{e}4 \text{ pb}$	

Process	Cross section	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_S^2)$	$25.0 \text{ pb}$	$22.0 \text{ pb}$
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$	$64.7 \text{ pb}$	$58.9 \text{ pb}$
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)_{\text{DPI}}$	$5.6 \text{ pb}$	$5.3 \text{ pb}$
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)_{\text{TPI}}$	$0.27 \text{ pb}$	$0.26 \text{ pb}$
$\mathcal{O}(\alpha_{EM}^6)$	$0.22 \text{ pb}$	$0.20 \text{ pb}$

$\sigma < \sigma_1 \sigma_2 / \sigma_{\text{eff}}$

t-tbar

W+4j

DPI

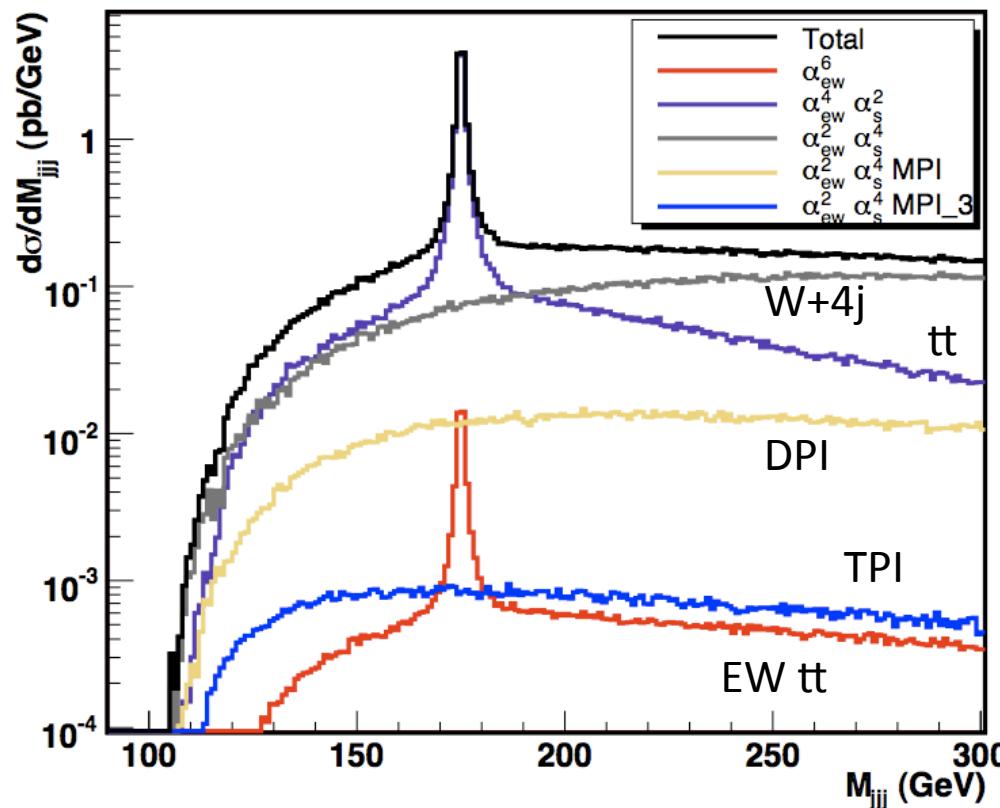
TPI

EW negligible

$\Delta R(jj) > 0.5 \quad \Delta R(jl^\pm) > 0.5$

↑  
Isolation cuts

M<sub>jjj</sub>



$M_{top} = 175$  GeV

$M_{jjj}$  = mass of jet triplet with max pT

$W \rightarrow \mu\nu$  only

Process	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_S^2)$	10.8 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$	0.76 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$ DPI	0.12 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$ TPI	0.01 pb
$\mathcal{O}(\alpha_{EM}^6)$	0.04 pb

$170 \text{ GeV} < M_{jjj} < 180 \text{ GeV}$

$W+4j / tt \approx 7\%$

$MPI/tt \approx 1\%$

Not a problem for mass measurement

Cross section ?

Negligible when b-tagging available

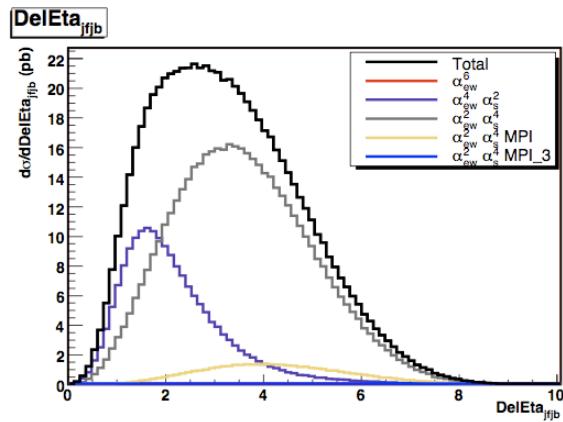
# Looking for MPI in |v+4j

- Get rid of t-tbar  
 $|M_{jjj} - M_t| > 10 \text{ GeV}$
- MPI gives larger separation of forward/backward jets  
 $|\Delta\eta(j_f, j_b)| > 3.8$

Process	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_s^2)$	1.16 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$	24.01 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)_{\text{DPI}}$	2.91 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)_{\text{TPI}}$	0.16 pb
$\mathcal{O}(\alpha_{EM}^6)$	0.05 pb

Basic cuts      Iso cuts

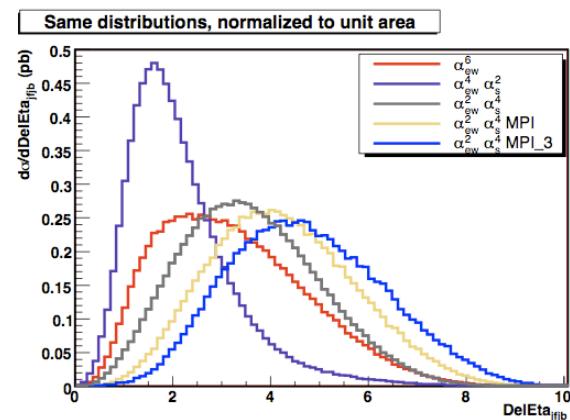
Process	Cross section	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_s^2)$	25.0 pb	22.0 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$	64.7 pb	58.9 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)_{\text{DPI}}$	5.6 pb	5.3 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)_{\text{TPI}}$	0.27 pb	0.26 pb
$\mathcal{O}(\alpha_{EM}^6)$	0.22 pb	0.20 pb



S/B  $^{1/2} = 5.8(6.1)$

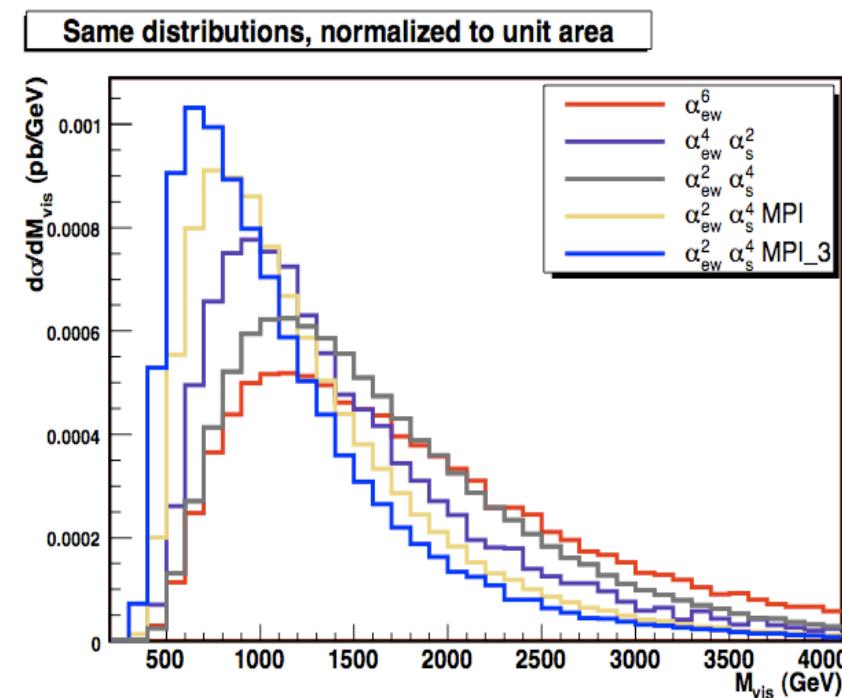
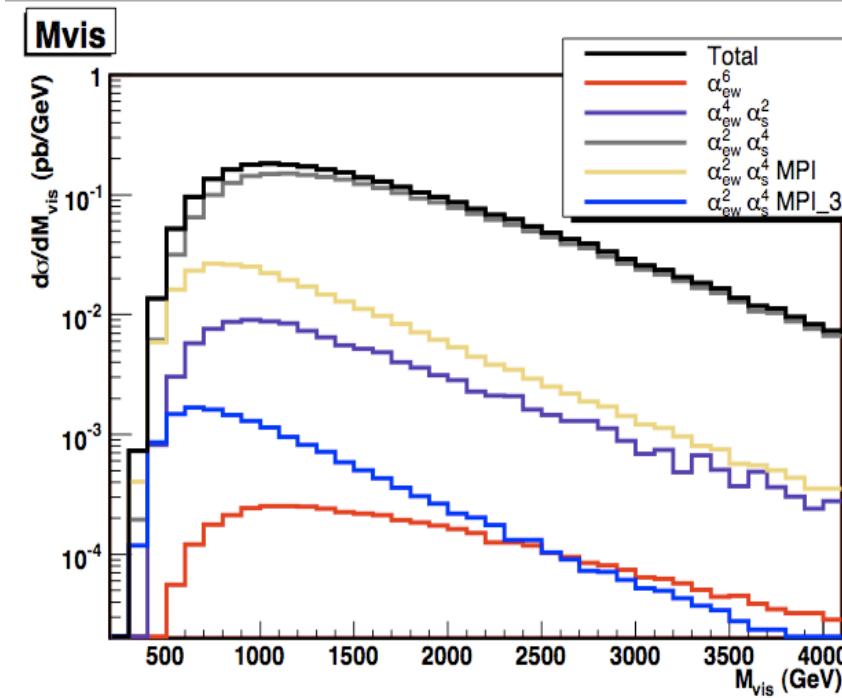
L=100 pb $^{-1}$

MPI/4jW=1/8



Visible mass:  
 $3j+l^\pm$

MPI softer



$jj \otimes jjW$  is dominant  $\rightarrow$  expect  $\Delta\varphi = \pi$  jet pair

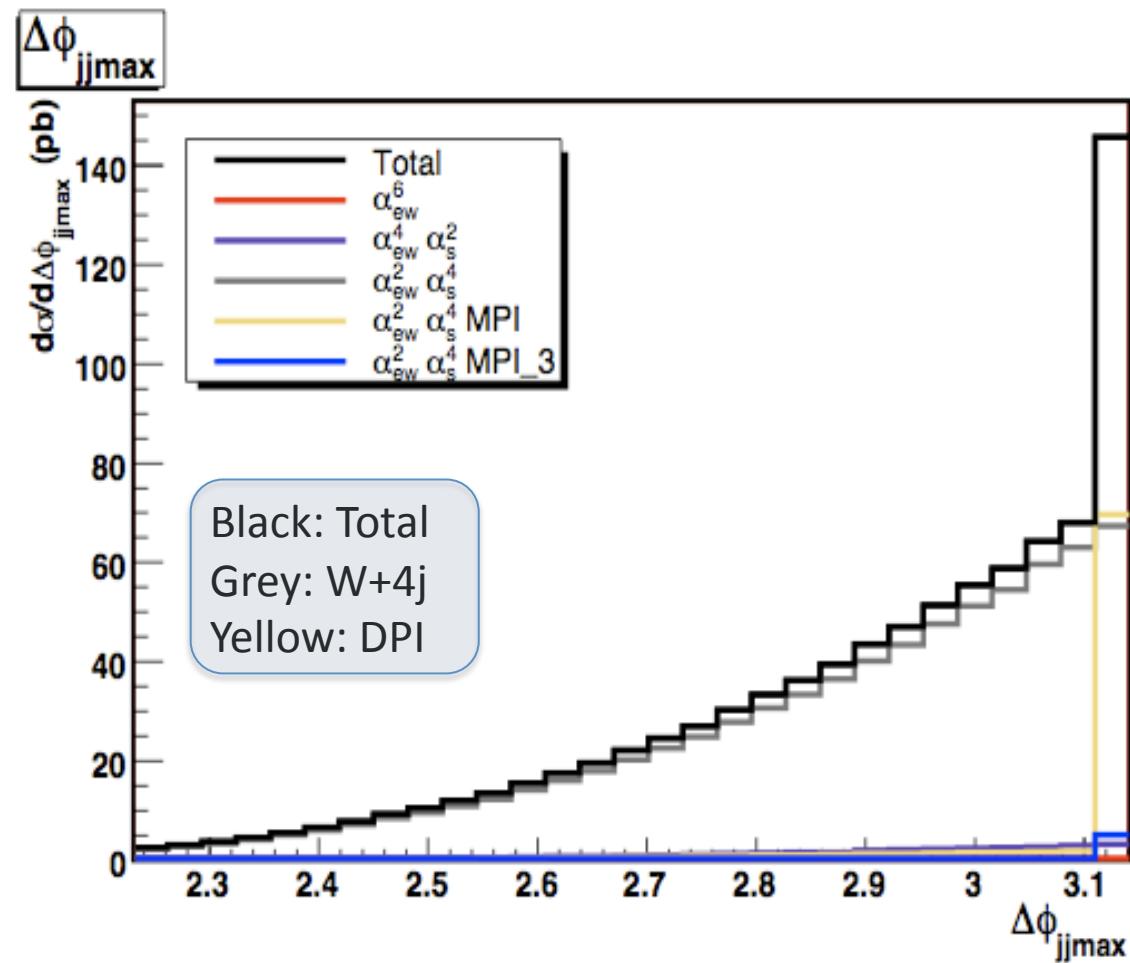
as in  $\gamma + 3j$  or  $Z + 3j$

$jjj \otimes jW$   
 $jjjj \otimes W$  } no such feature

$$|\Delta\phi(jj)_{\max}| > 0.9 \cdot \pi$$

Process	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_s^2)$	0.75 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$	15.61 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$ DPI	2.61 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$ TPI	0.16 pb
$\mathcal{O}(\alpha_{EM}^6)$	0.03 pb

$$\text{MPI/tot} = 17\%$$



# Triple Parton Interactions: so far unobserved

Two jet pairs back to back in the transverse plane

DY W with “zero” pT (also in DPI: less effective)

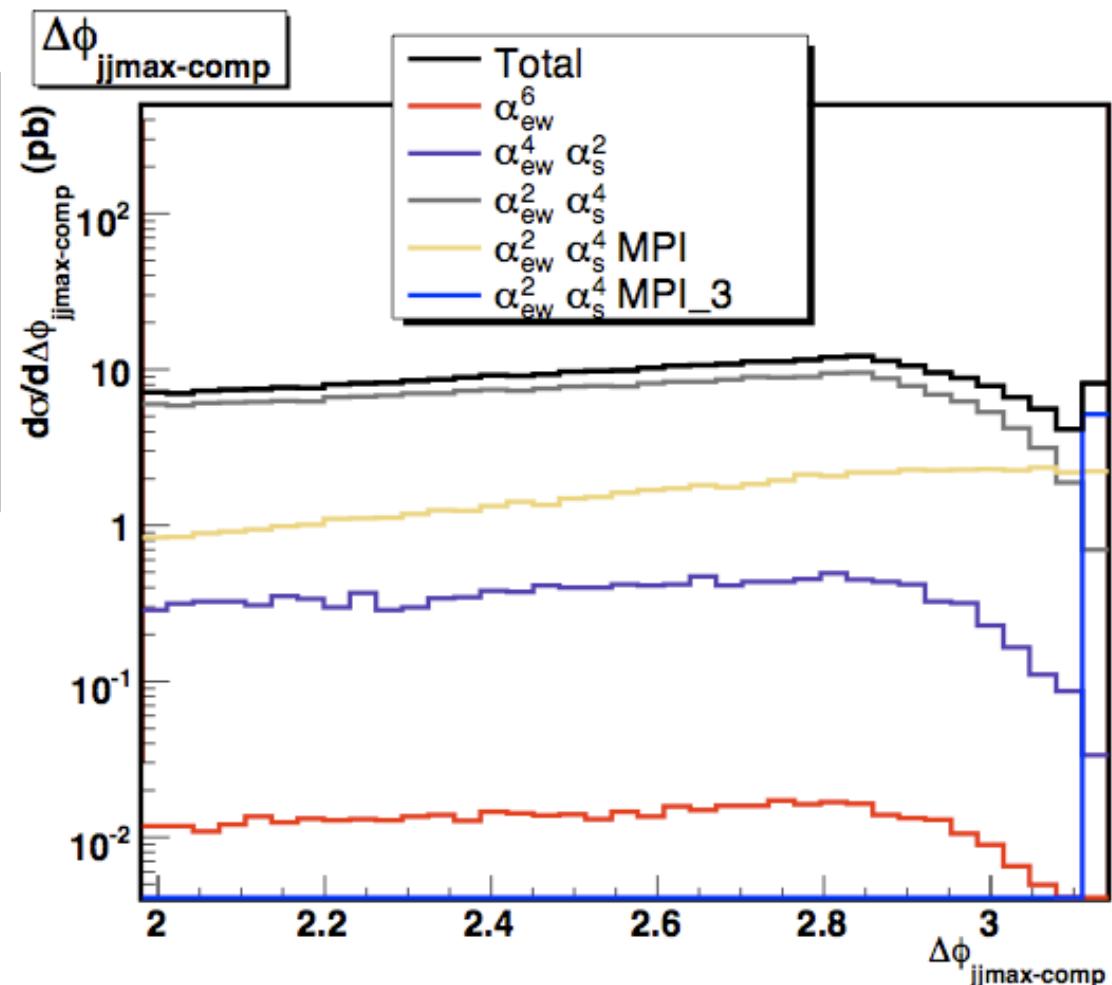
Process	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_s^2)$	0.75 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$	15.61 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$ DPI	2.61 pb
$\mathcal{O}(\alpha_{EM}^2 \alpha_s^4)$ TPI	0.16 pb
$\mathcal{O}(\alpha_{EM}^6)$	0.03 pb

$$|\Delta\phi(jj)_{\max}| > 0.9 \cdot \pi$$

TPI/DPI/Bkg  
1 / 16 / 100

16k events for  $L=10 \text{ fb}^{-1}$

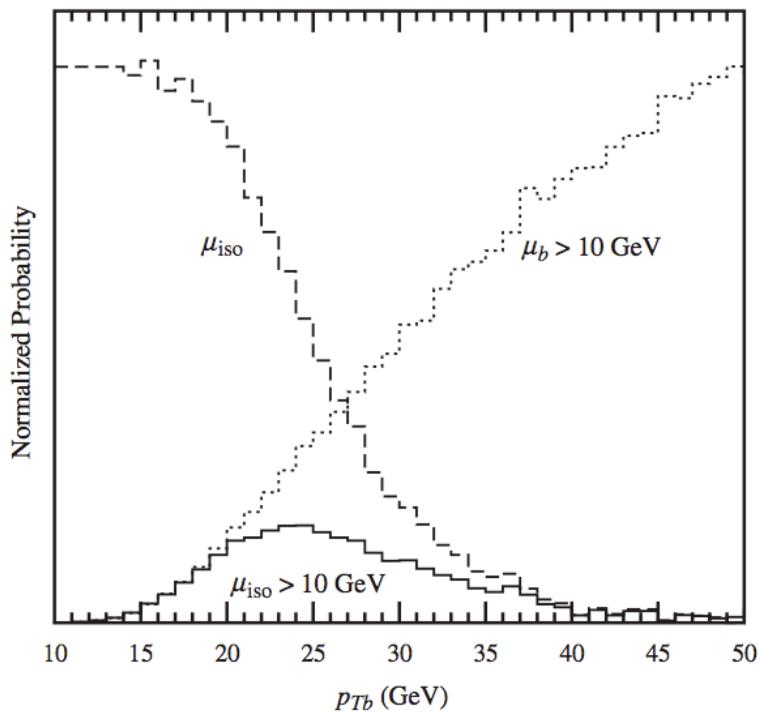
TPI more than 50% of last bin: 2 deg.



# CAVEAT: isolated leptons from b-hadron decay

Sullivan,Berger  
PRD78(2008)034030

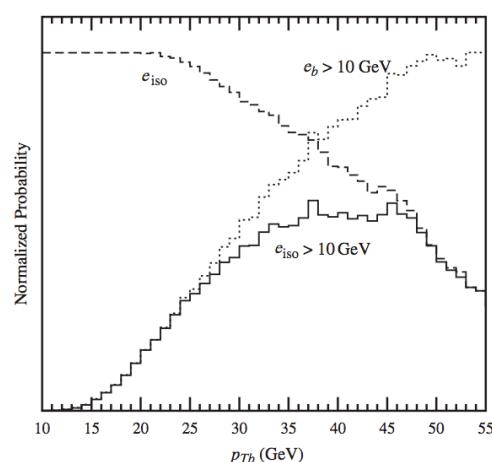
PHYSICAL REVIEW D 78, 034030 (2008)



$$\text{BR}(b\text{-had} \rightarrow \mu) = 9\text{--}14\%$$

Isolation = geometrical iso ( $\Delta R$ ) OR  
Energy iso

More isolated electrons because of  
•Lower Energy Iso Thresholds  
(higher noise in ECAL)  
•More fakes from charged pions



We use a 20 GeV  $p_T$ , threshold which  
is safer

# Looking for MPI in $Z(l^+l^-) + 4j$

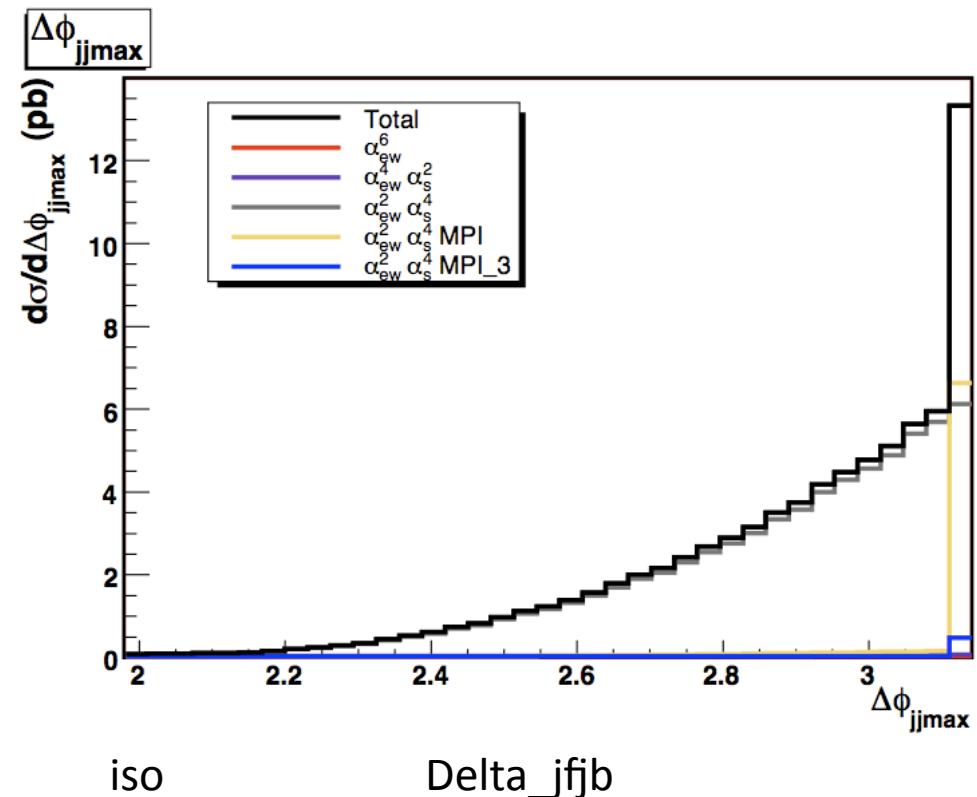
$p_{T_j} \geq 30 \text{ GeV}, \quad |\eta_j| \leq 5.0,$

$p_{T_\ell} \geq 20 \text{ GeV}, \quad |\eta_\ell| \leq 3.0,$

$M_{jj} \geq 60 \text{ GeV}, \quad M_{ll} \geq 20 \text{ GeV}$

$\Delta R(jj) > 0.5 \quad \Delta R(jl^\pm) > 0.5$

$|\Delta\eta(j_f j_b)| > 3.8$



Basic

iso

Delta\_jfjb

Process	Cross section	Cross section	Cross section
$\mathcal{O}(\alpha_{EM}^4 \alpha_S^2)$	106.6 fb	87.7 fb	26.3 fb
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$	6404.67 fb	5626.6 fb	2209.7 fb
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$ DPI	515.5 fb	469.1 fb	272.7 fb
$\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$ TPI	23.2 fb	21.4 fb	15.1 fb
$\mathcal{O}(\alpha_{EM}^6)$	16.5 fb	13.9 fb	7.6 fb

$S/B \sqrt{s} = 5.8(6.1)$   
 $L = 1 \text{ fb}^{-1}$

$\text{MPI}/4jW = 1/8$

Z's much easier to identify; No bkg from b-quark decays

# Conclusions

MPI provide a small but non negligible background to t-tbar if no b-tag available

MPI can be studied in W+4j and Z+4j channels above QCD background exploiting  $\Delta\varphi=\pi$  jet pairs

TPI can hopefully be measured in W+4j production

More careful analysis including correlations between interactions needed

# Looking for MPI in $W^+W^+ + 2j$

Can only be produced with at least two additional jet in SPI:  $\alpha_s^2 \alpha^4, \alpha^6$

In DPI it can be produced as DY $\otimes$ DY:  $\alpha^4$       leptonic decays included

