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to Super-High Energy Cosmic Rays**

25 - 29 May 2009

**Multiple Scattering & Collective Effects in pp
Scattering at the LHC**

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Multiple scattering and collective effects in pp scattering at the LHC

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Hirano, Y. Karpenko, M. Bleicher, S. Haussler

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1 Airshower simulation with EPOS

Missing muons

Situation in 2006:

- none of the existent models (QGSJET, SIBYLL) can consistently describe all cosmic ray airshower data,

in particular:

- data show considerably more muon production compared to simulations.

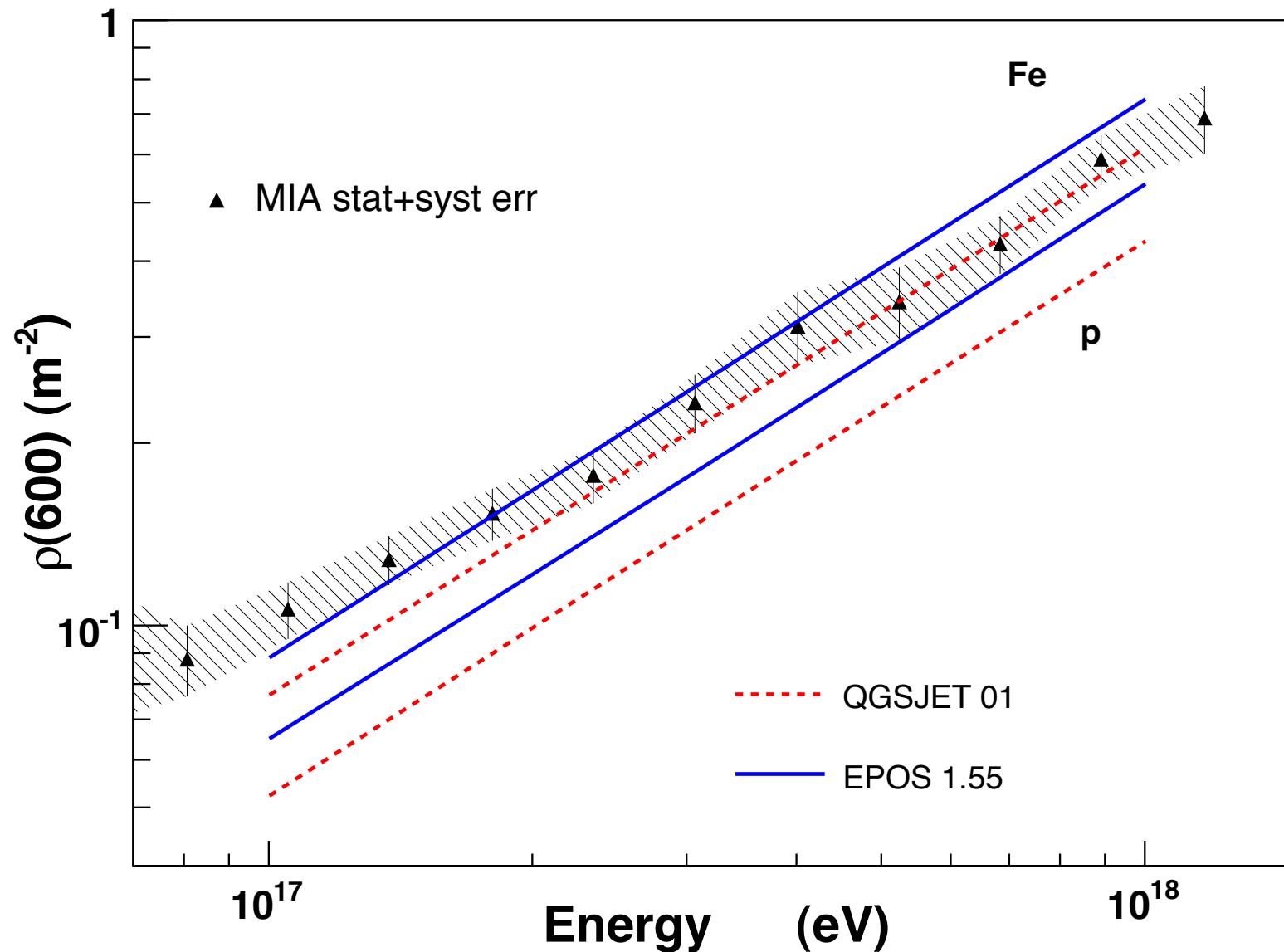
Not obvious how to fix this problem without creating others

Starting to use EPOS as interaction model, is
was found :

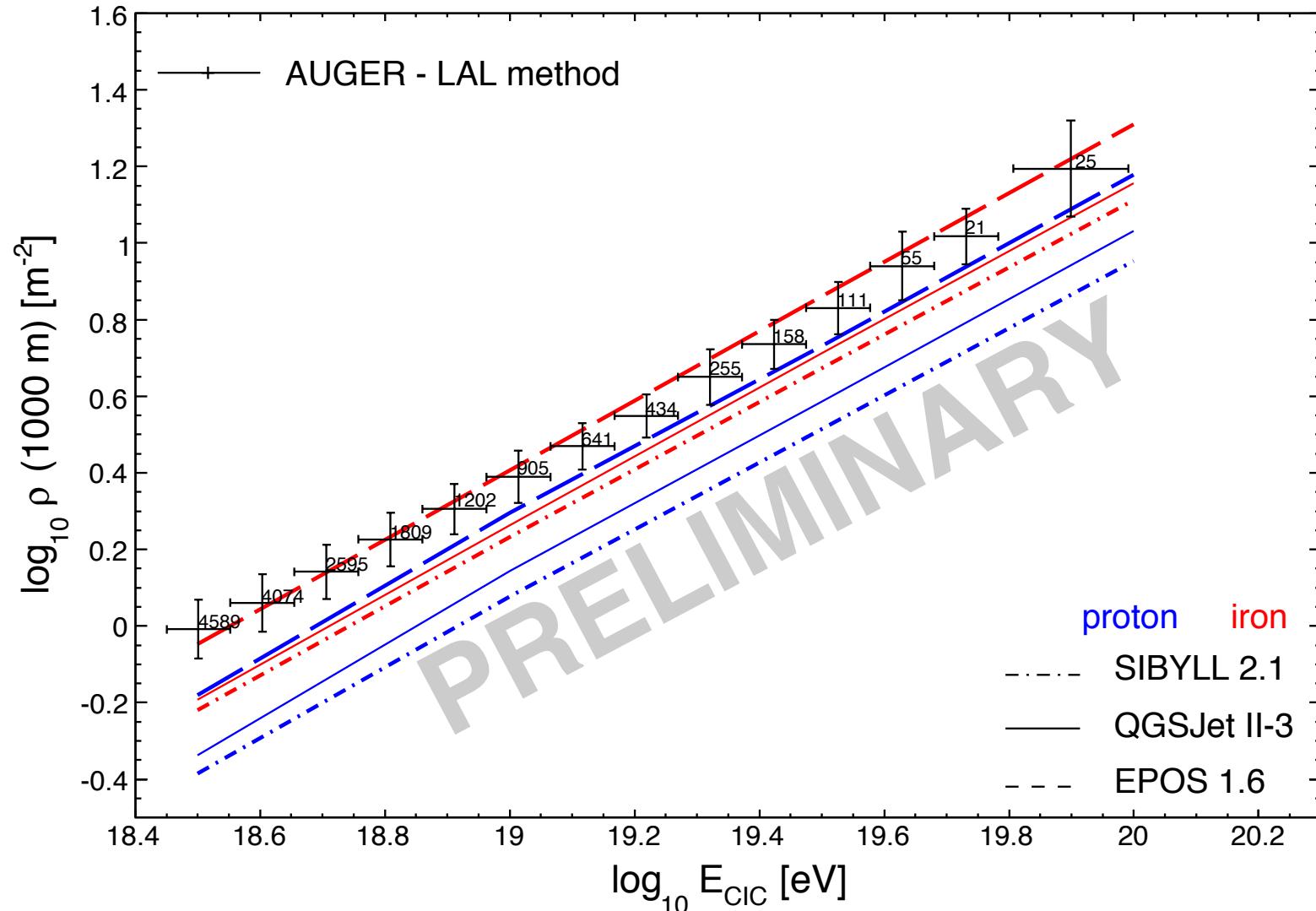
- one gets significantly more muons,
- without changing observables like X_{\max} too much

MUON PRODUCTION IN EXTENDED AIR SHOWER SIMULATIONS.
Tanguy Pierog, Klaus Werner. Phys. Rev. Lett. 101, 171101
(2008).

Muon density MIA

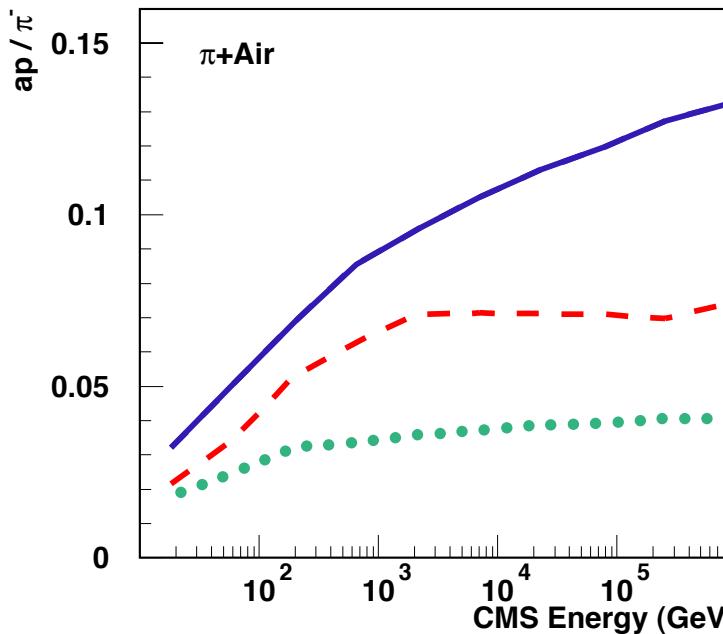
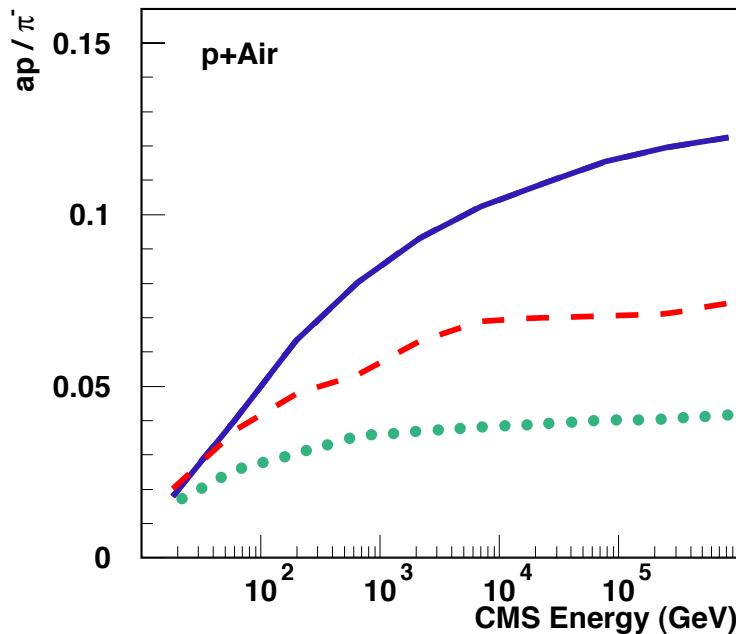


Muon density AUGER



Why more muons in EPOS ?

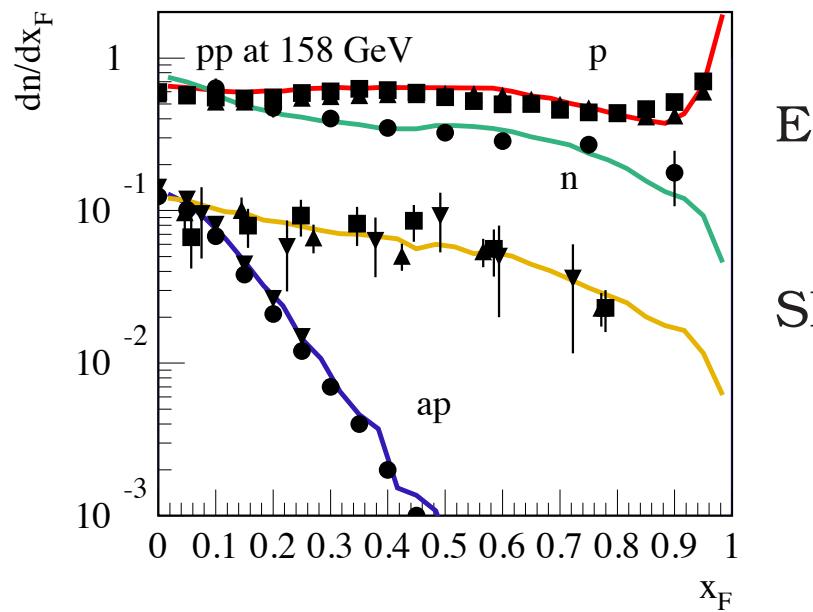
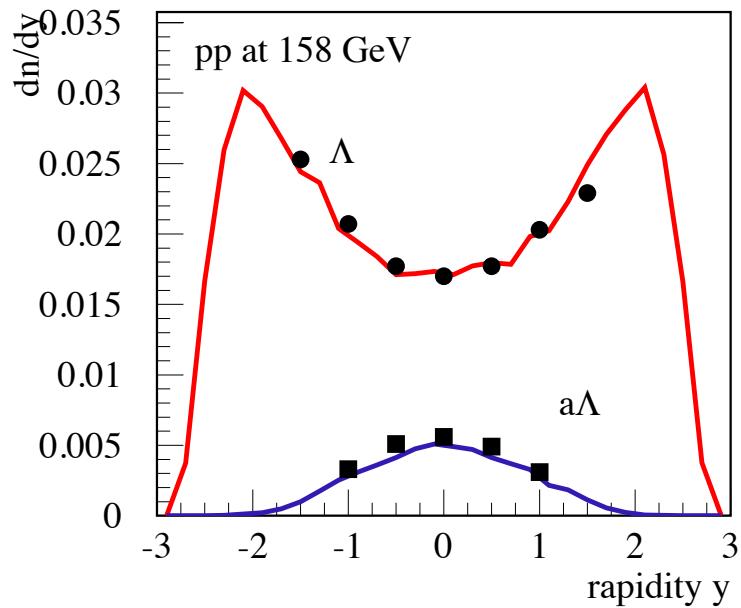
... because EPOS produces more baryons



EPOS 1.99
QGSJET II
SIBYLL 2.1

Baryon = no $\pi^0 \rightarrow$ no EM cascade
 \rightarrow chance to make muons

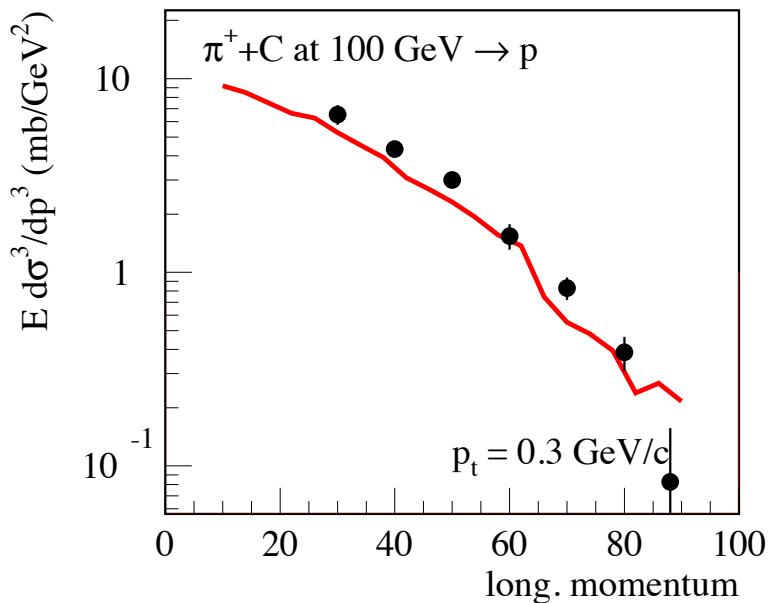
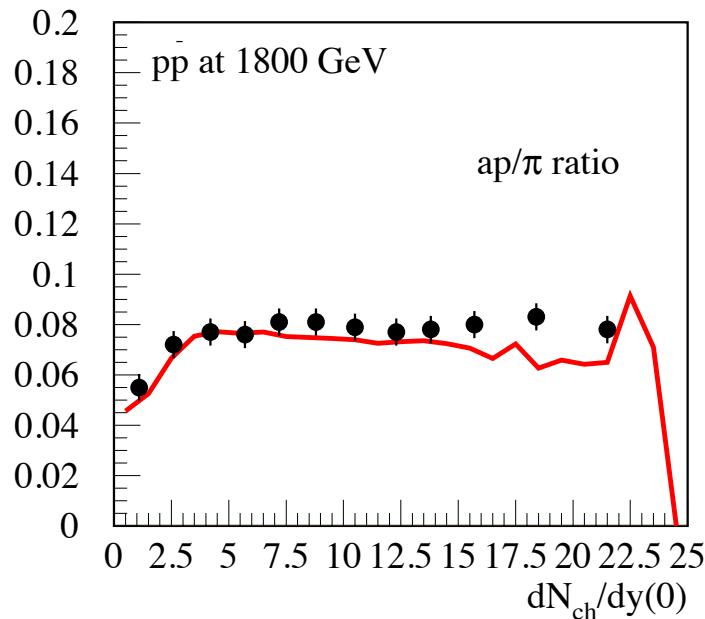
EPOS has been designed (and optimized)
to understand ALL types of hadrons
→ careful studies of baryon production *



* without thinking about CR applications

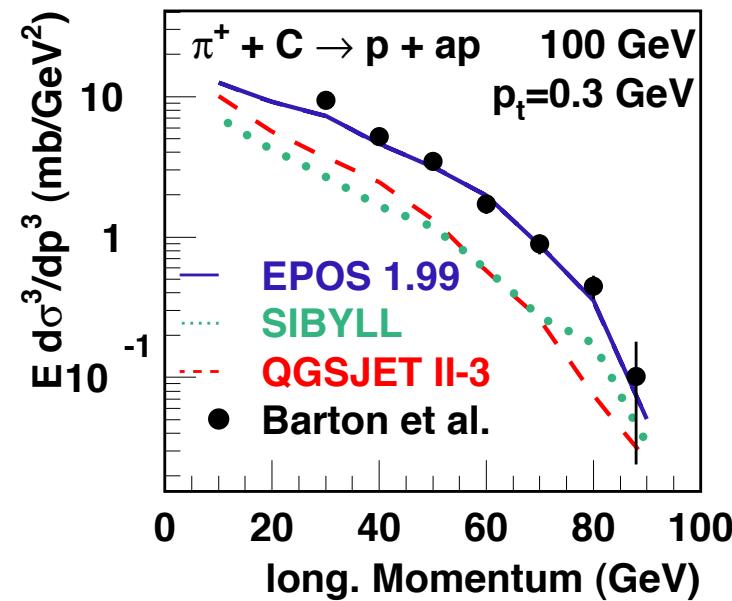
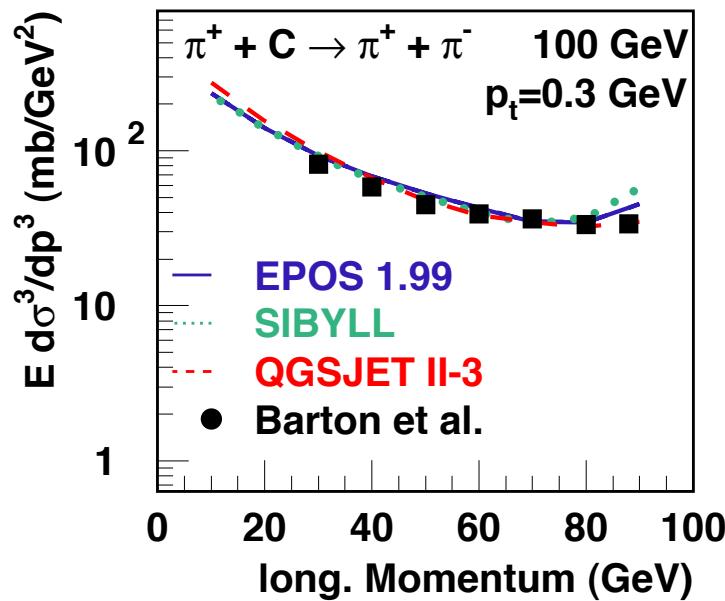
enormous amount of pp ($p\bar{p}$) data considered,
at SPS, ISR, RHIC, TEVATRON

also πp , pA and πA



EPOS compared to other models:

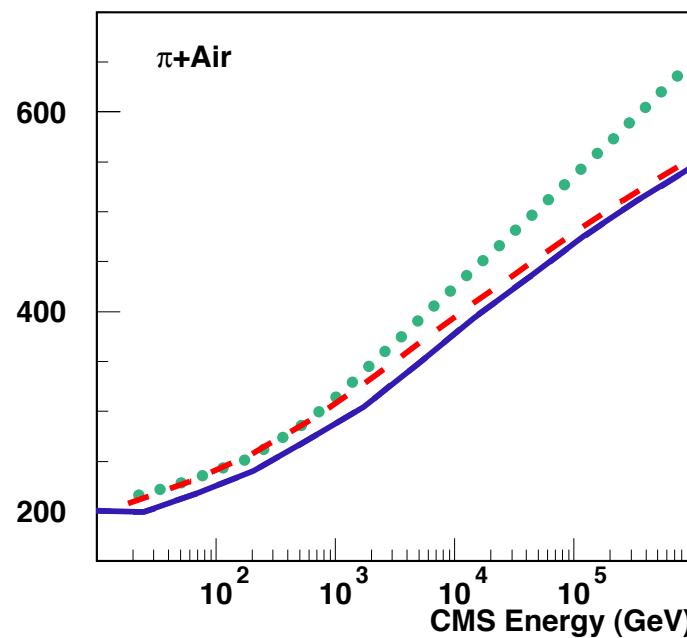
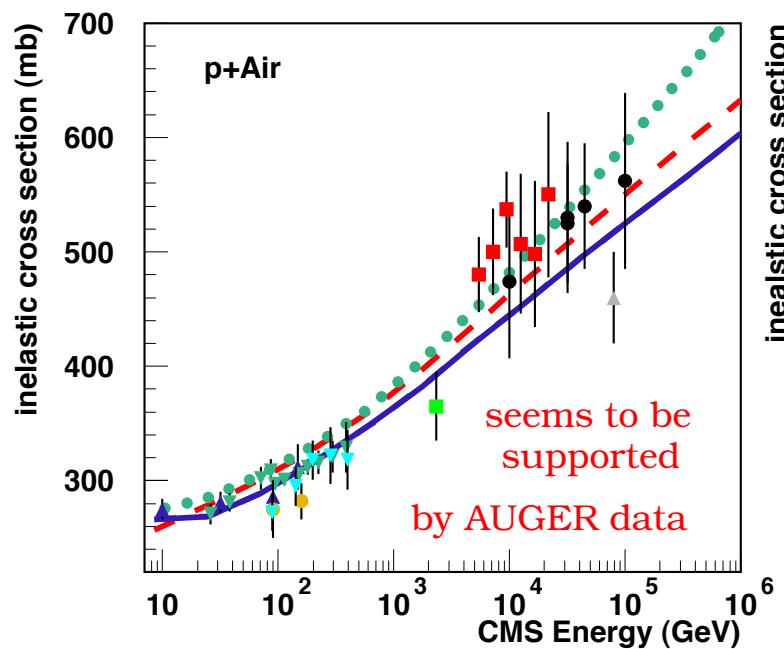
- similar concerning pions
- big differences concerning baryons



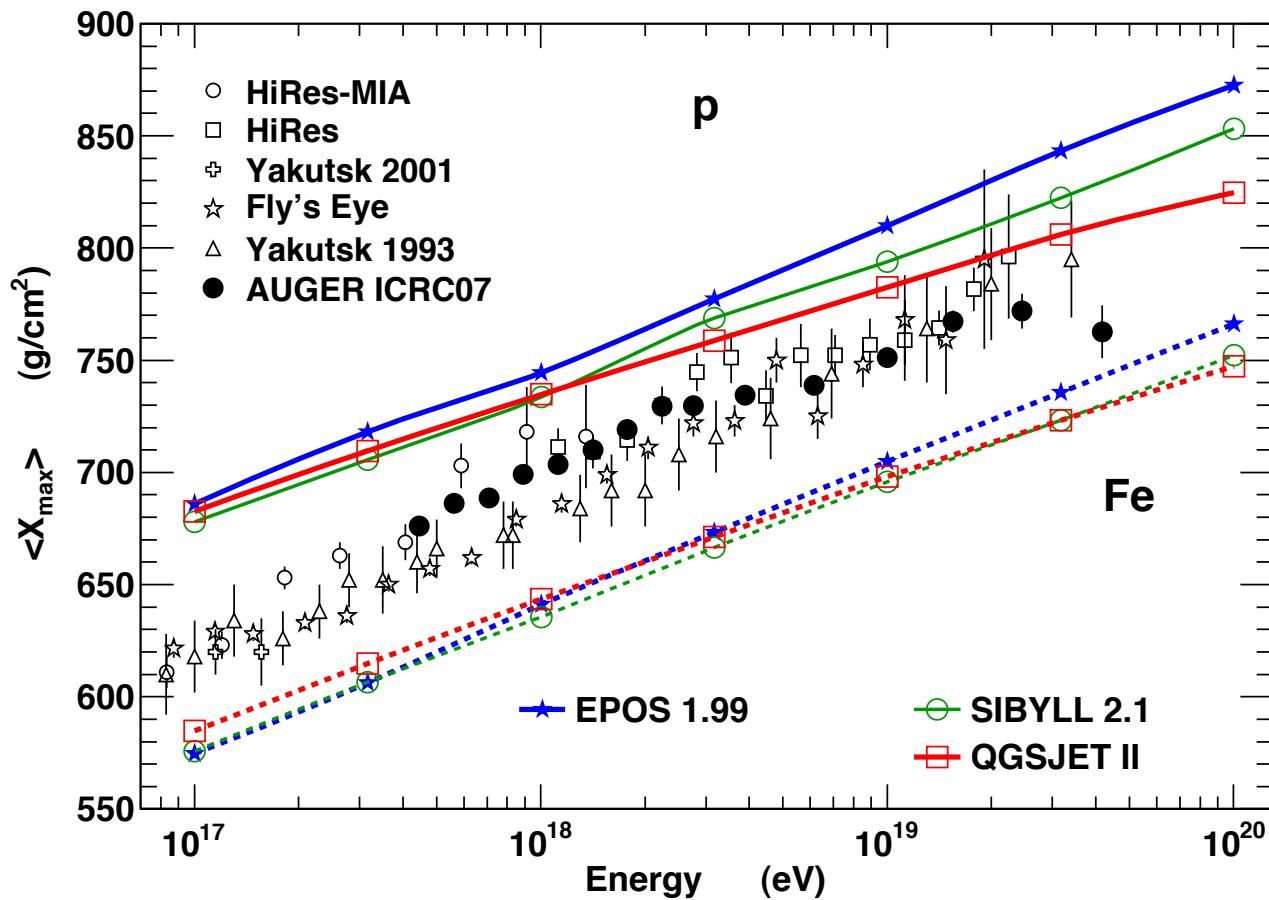
More muons require more electrons

Increase muon number (without changing the electrons)
→ contradiction with KASCADE ($N_{\text{muons}} - N_{\text{electron}}$ correlation)

Solution: non-linear effects (considered for particle production) also for cross section calculations



Consequences for Xmax



2 Multiple Scattering in p-p collisions

At high energies one has certainly multiple scattering even in pp ($\sigma_{\text{jet}} > \sigma_{\text{tot}}$).

Inclusive cross sections:

- quantum interference (“AGK cancellations”) may help to provide simple formulas referred to as “factorization”
(multiple scattering is “hidden”)

LHC: very interesting observables beyond inclusive
(multiplicity dependencies...):

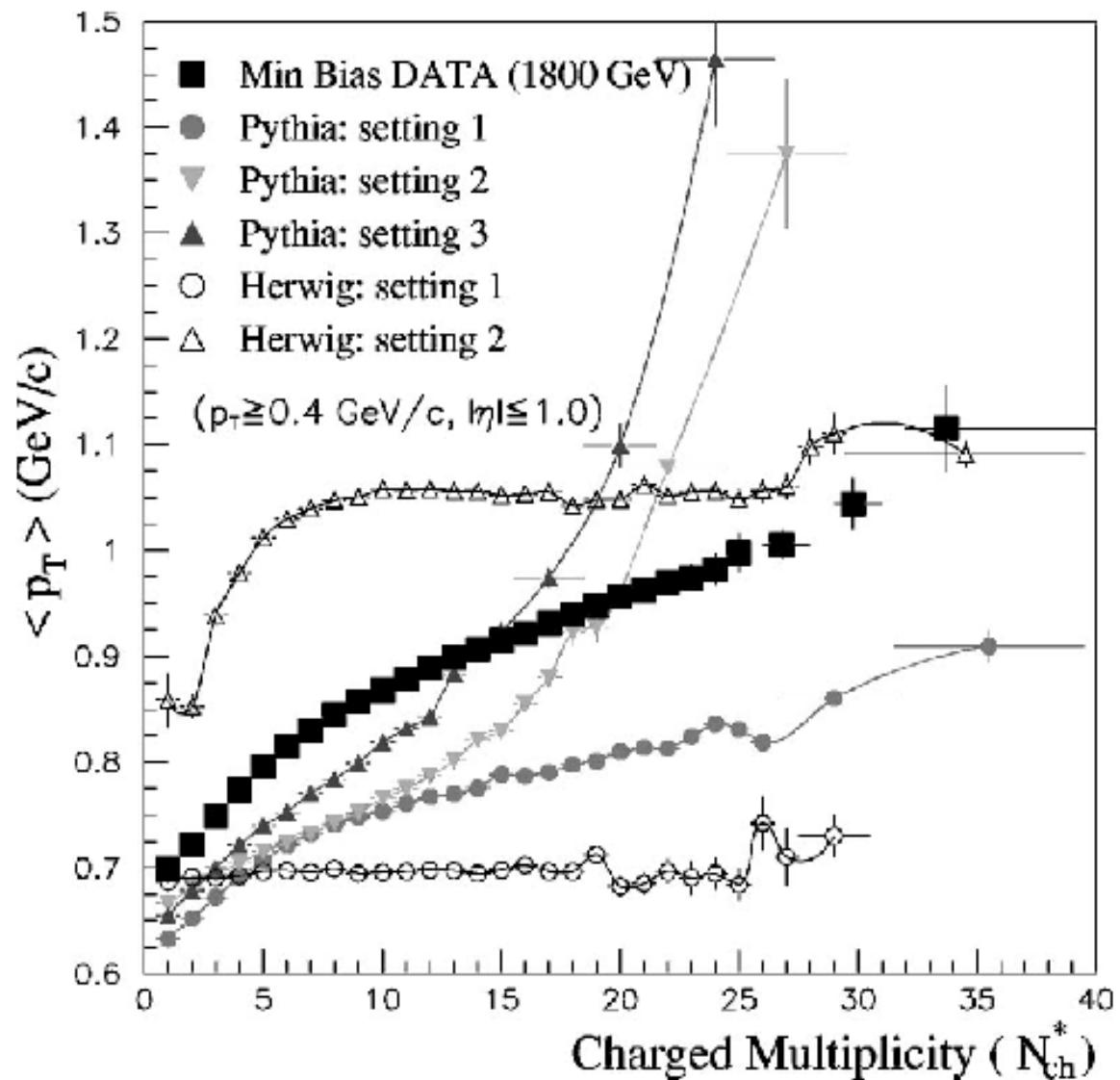
- one has to go beyond factorization and formulate a consistent multiple scattering theory

Interesting observations already at Tevatron ...

pp@1800GeV
data: CDF

Phys. Rev. D
Vol 65,
072005 (2002)

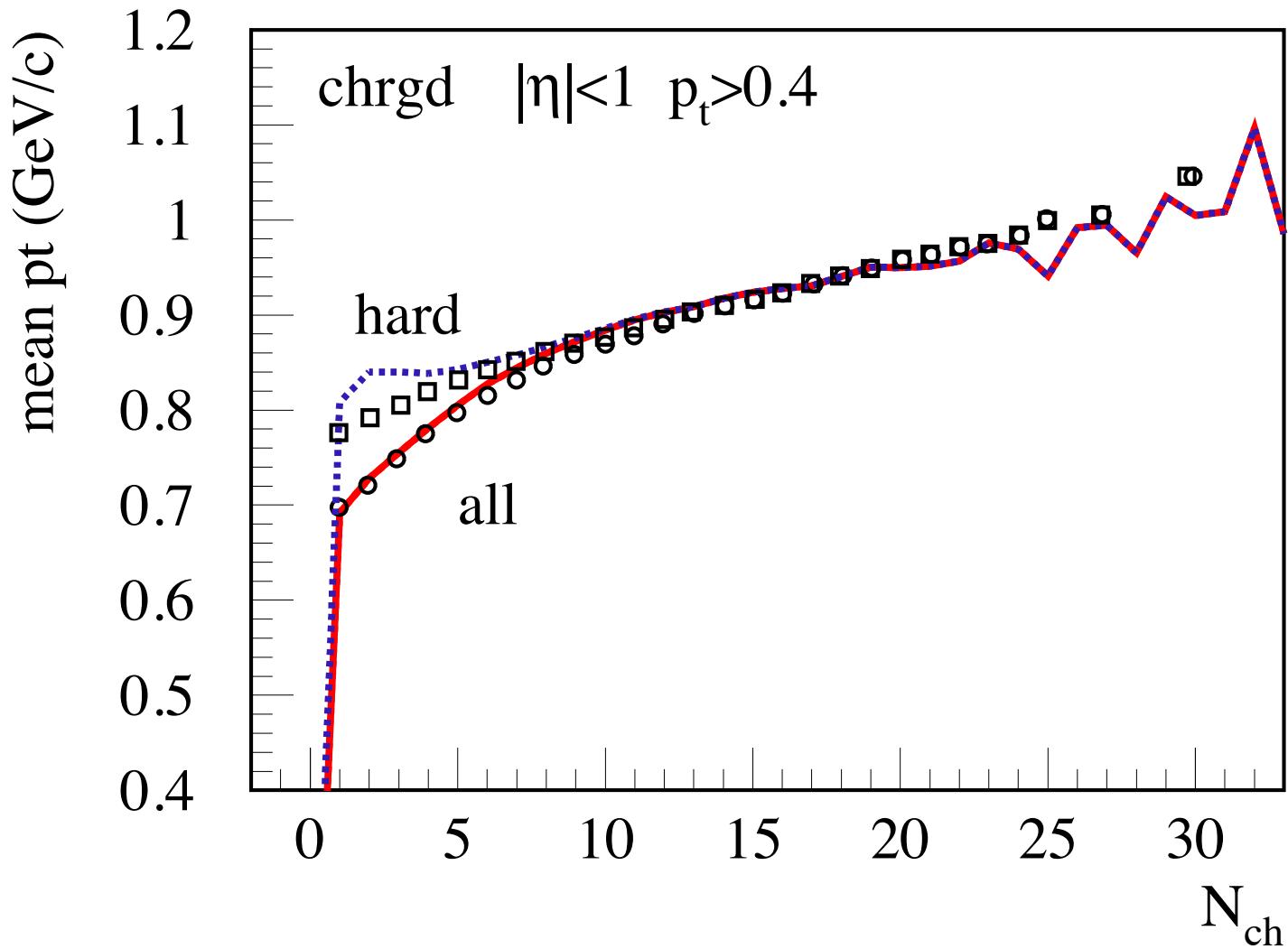
recent activities in
Pythia community
→ MPI@LHC
workshop



pp@1800GeV

points: CDF

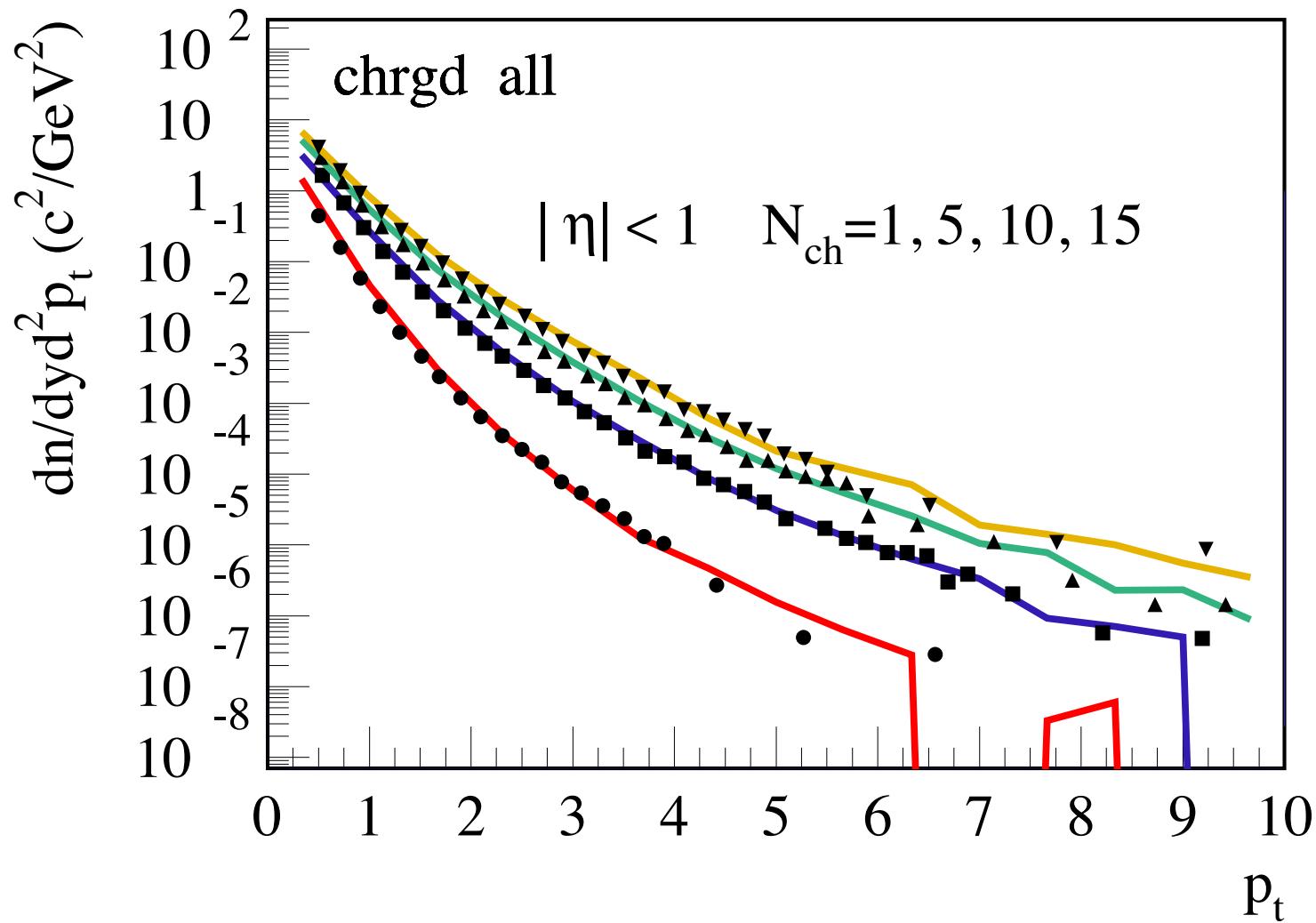
curves EPOS



pp@1800GeV

points: CDF

curves EPOS



In EPOS:

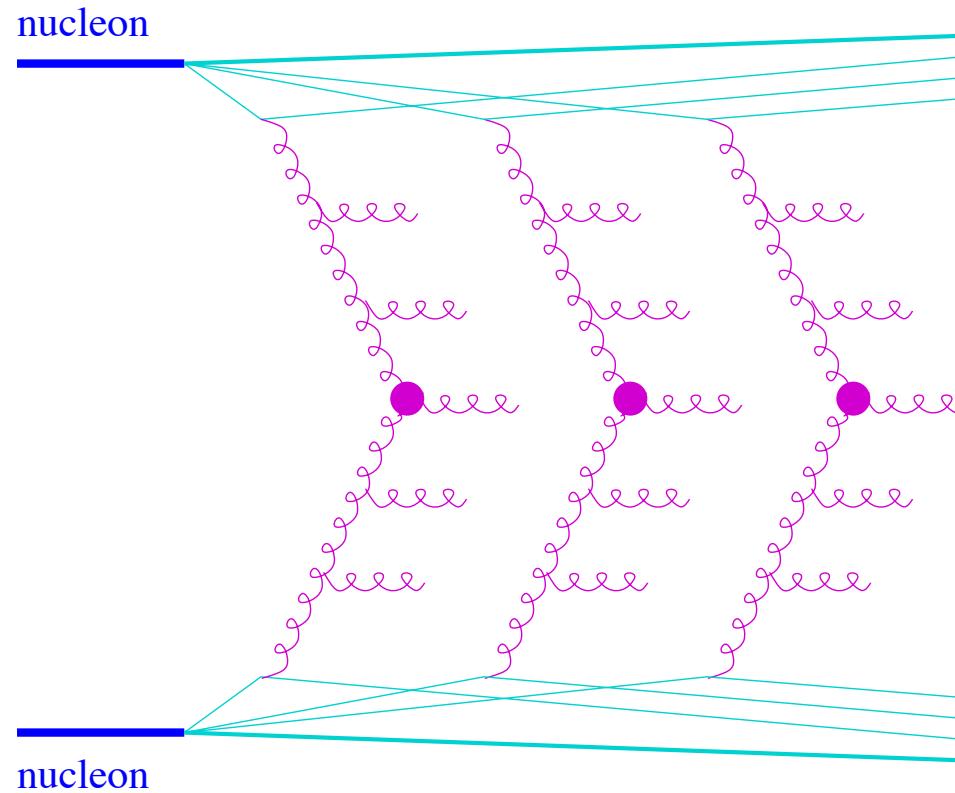
- high multiplicity is clearly related to multiple scattering
- However, multiple scattering also favours hard scatterings (just higher probability)

Multiple scattering approach

Possible solution:
Gribov's Pomeron calculus,

- several “Pomerons” are exchanged in parallel
- provides logarithmic increase of cross sections with energy

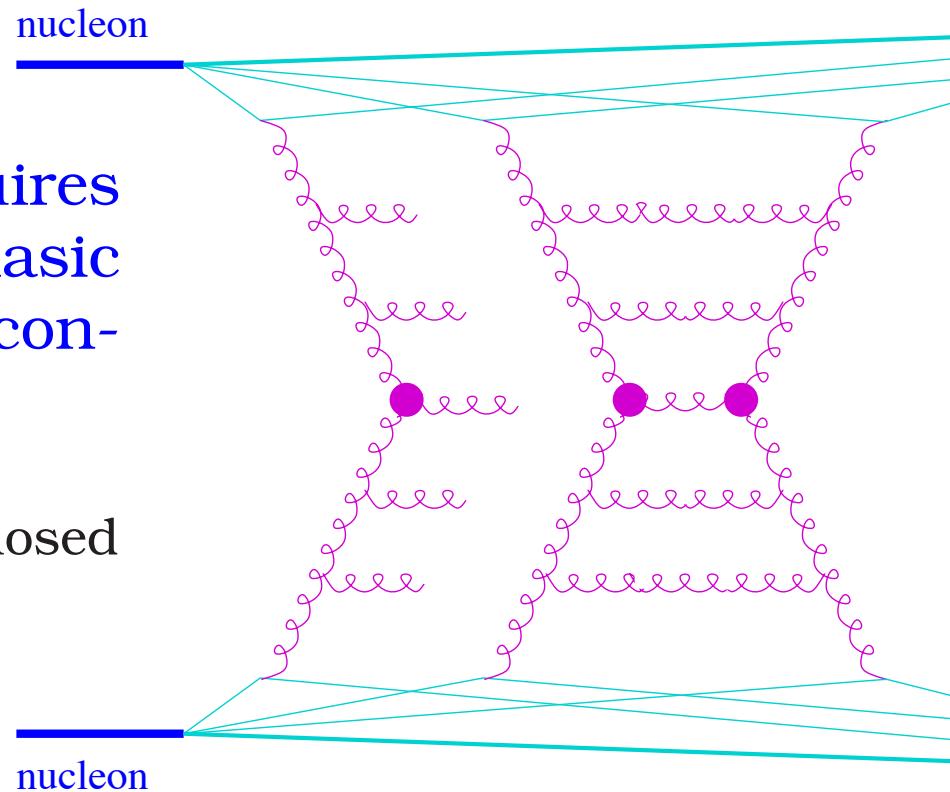
EPOS: Pomeron = parton ladder



important: multiple exchange of parton ladders, with energy sharing

Consistency requires
inelastic and elastic
processes to be con-
sidered

(here: open and closed
ladders)



Squaring such graphs leads to “cut diagrams”
→ handled by employing “cutting rule techniques”

Energy sharing requires Markov chain techniques

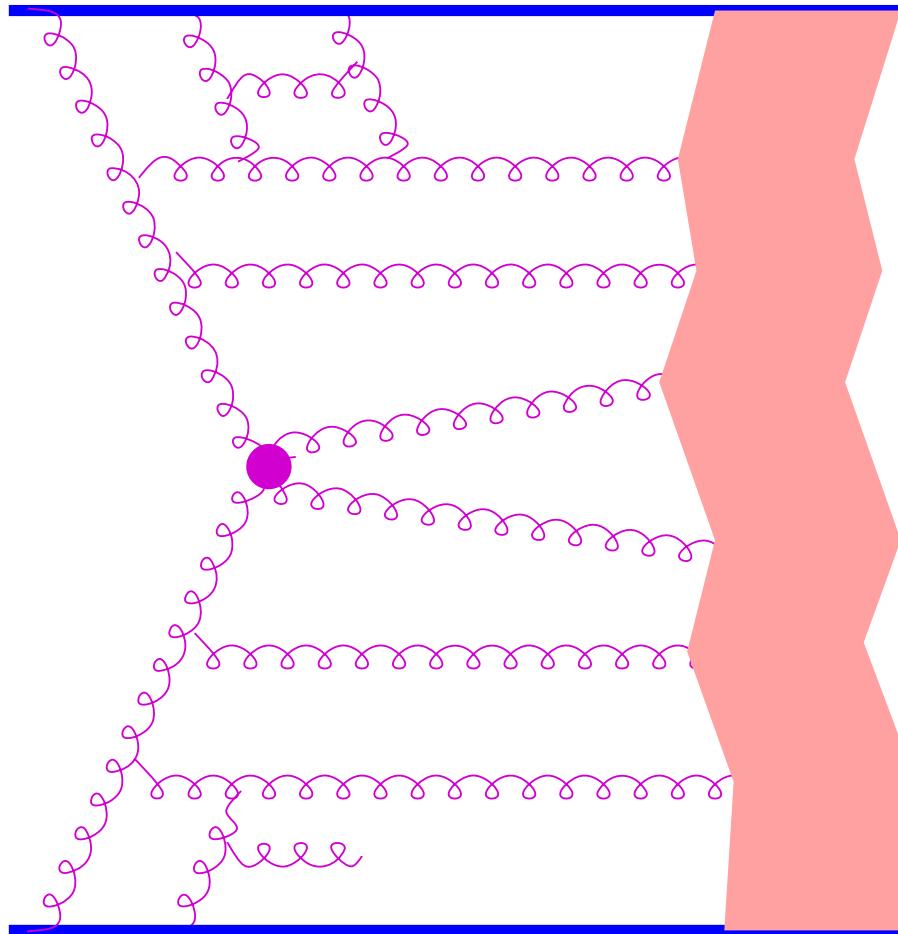
More details:

[Parton-based Gribov-Regge Theory](#), H. J. Drescher,
M. Hladik, S. Ostapchenko, T.Pierog, and K. Werner,
Phys. Rept. 350 (2001) 93-289

[Parton ladder splitting and the rapidity dependence of transverse momentum spectra in deuteron-gold collisions at RHIC](#), K. Werner, F.M. Liu, T. Pierog, hep-ph/0506232, Phys. Rev. C 74, 044902 (2006)

3 Space-time considerations

EPOS parton ladder



quasi longitudinal
color field
“flux tube”

gluons =
transverse
kinks

decay
via pair
production

Flux tube
stretches over wide
range in rapidity

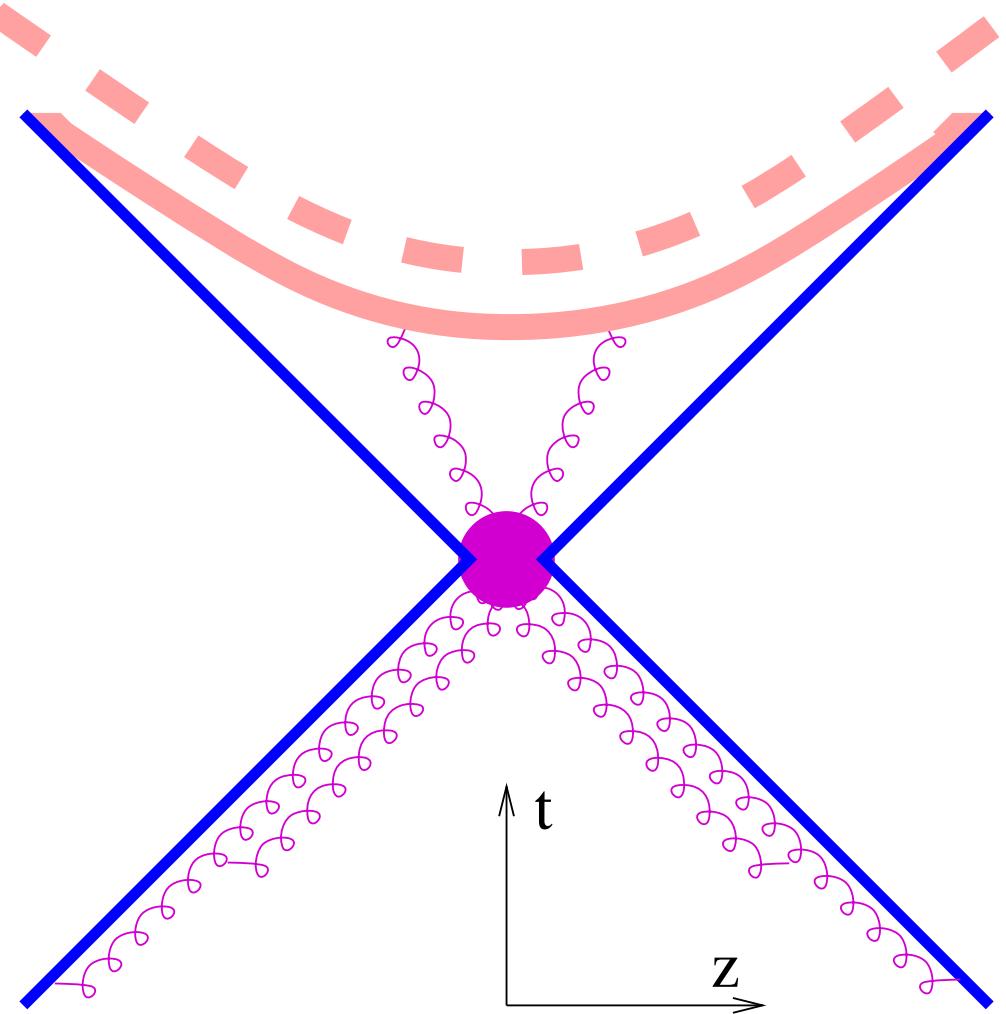
decays via pair pro-
duction

Hadrons are NOT as-
sociated to individual
partons!

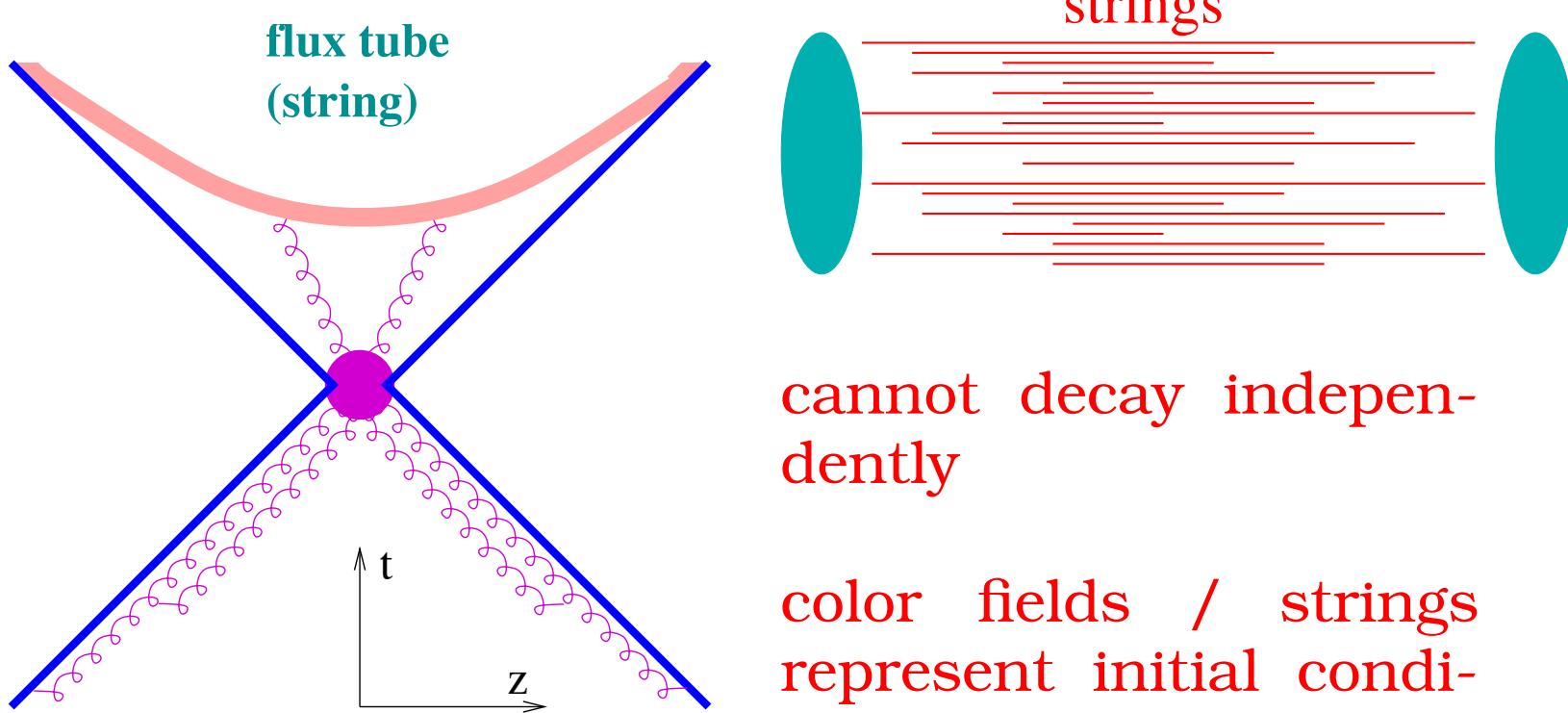
unless one considers
hard processes

flux tube
(string)

decays
into segments



in AA or central pp:
many overlapping flux
tubes



cannot decay indepen-
dently

color fields / strings
represent initial condi-
tion for hydro-evolution

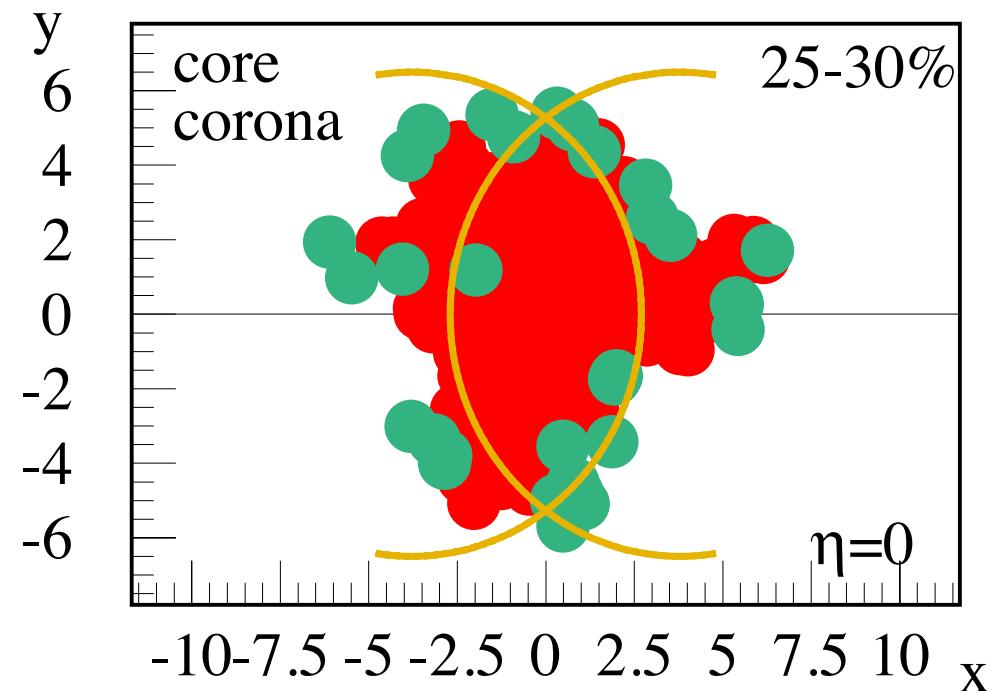
Core-corona separation (in AA)

Consider strings at some $\tau = \tau_0$

separate high density volume areas (which constitute the **core**)

from low density areas (**corona**)

high pt string pieces count as corona



core: we include inwards moving corona segments

Only core used to compute initial conditions for hydrodynamical evolution

at τ_0 : from space and momentum four-vectors of string segments, we get

- energy density $\varepsilon(\vec{x})$,
- flow velocity $\vec{v}(\vec{x})$
- net flavor densities $f(\vec{x})$

H.J. Drescher, S. Ostapchenko,
T. Pierog, and K.Werner,
hep-ph/0011219,
Phys.Rev.C65:054902,2002

$$T^{\mu\nu} = \frac{1}{\Delta V} \sum_{i \in \Delta V} \frac{p_i^\mu p_i^\nu}{p_i^0}$$

$$N_q^\mu = \frac{1}{\Delta V} \sum_{i \in \Delta V} \frac{p_i^\mu}{p_i^0} q_i$$

with

$$\begin{aligned} p &= \int_A^B \left\{ \frac{\partial X(r,t)}{\partial t} dr + \frac{\partial X(r,t)}{\partial r} dt \right\} \\ X(r,t) &= X_0 + \frac{1}{2} \left[\int_{r-t}^{r+t} g(\xi) d\xi \right] \end{aligned}$$

A, B : two neighboring points on X

$$g(r) = v_k \quad \text{for } r_{k-1} \leq r \leq r_k, \quad 1 \leq k \leq n$$

$$v_k = p_k/p_k^0, \quad r_k = p_k^0/\kappa$$

p_k = parton four-momentum

...back to pp

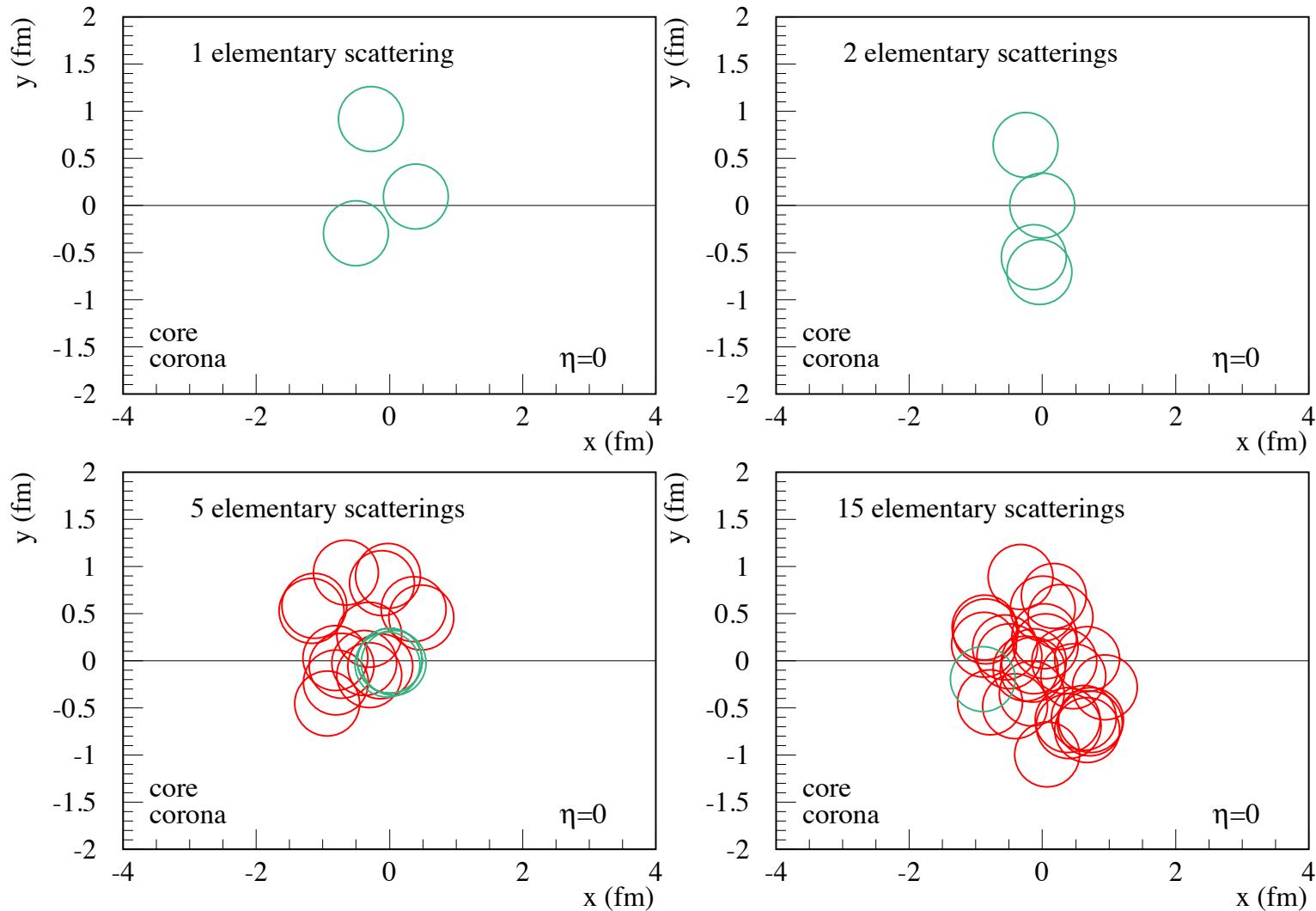
Be ν_{inel} the number of inelastic elementary scatterings.

The total charged multiplicity n_{ch} is certainly a monotonic (linear?) function of ν_{inel} .

Instead of centrality dependence as in AA ,

here we study the ν_{inel} or n_{ch} dependence of observables.

Core-corona approach in pp



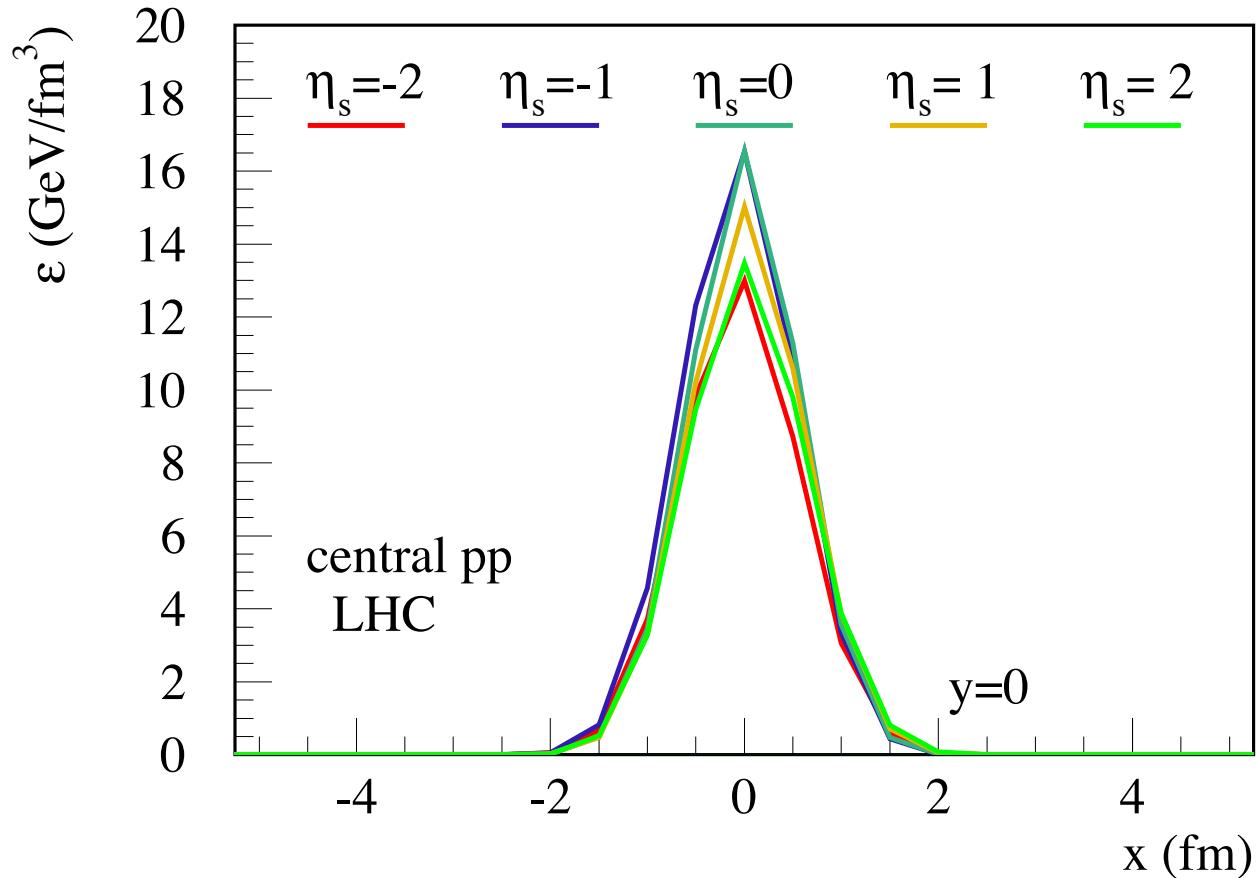
Core-corona in AA:

- separation of volume into (central) core and (peripheral) corona part

Completely different in pp:

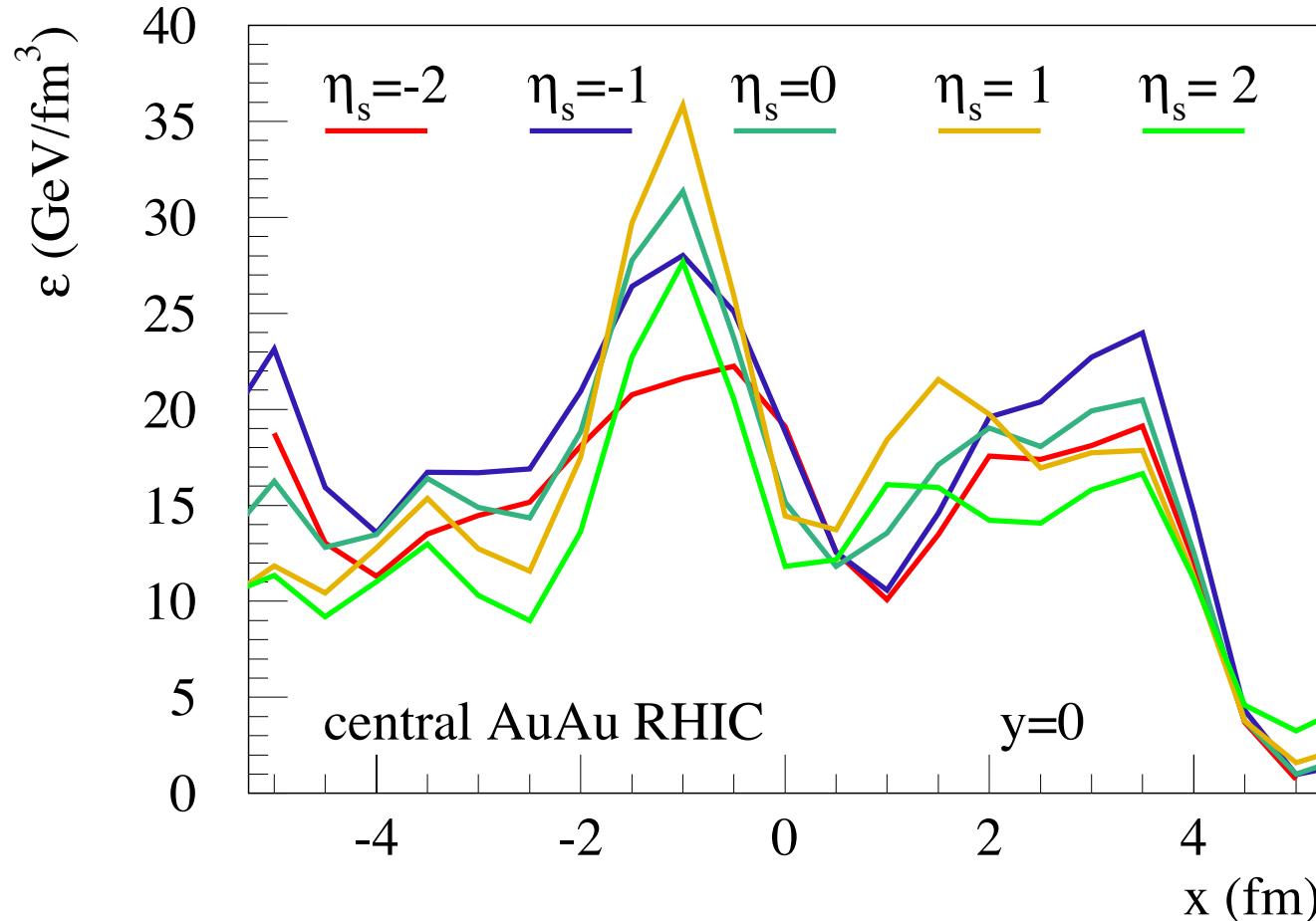
- separation of events into two classes: core and corona events

Energy density of central ($\nu_{\text{inel}} \geq 14$) pp at LHC



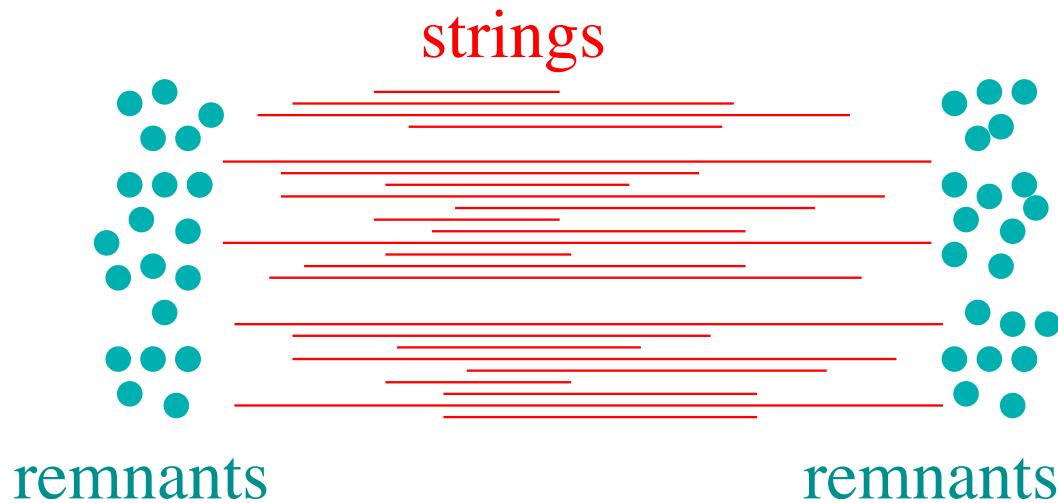
AuAu@RHIC

ridge structure in $\eta_s - \phi$ (coordinates)



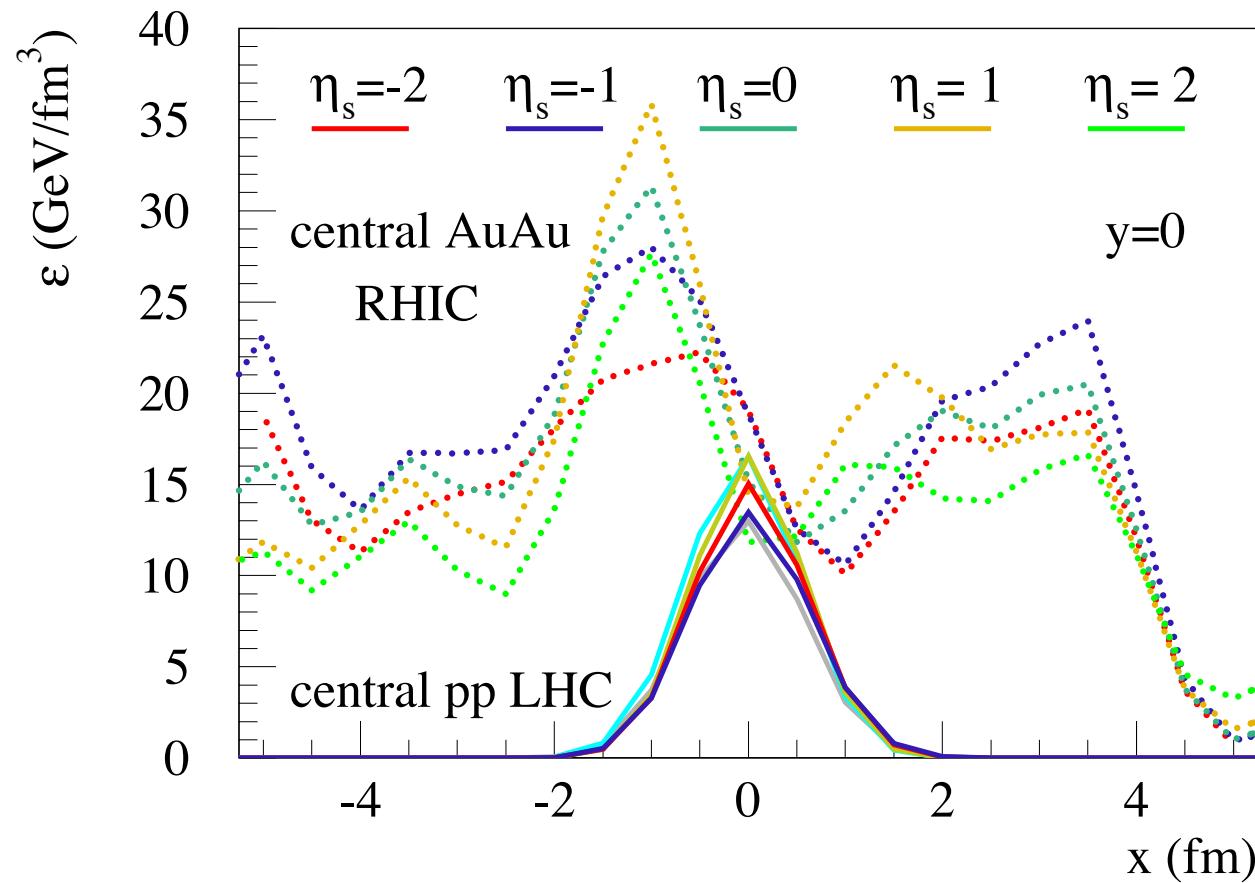
A single EPOS event is composed of several high density flux tubes (covering many η_s units)

The fluxtubes are due to random “clusterings” of nucleons in nuclei



One flux tube is the result of merging many individual strings

Epos: initial energy density obtained from strings, not partons



The widths of the sub-flux in AuAu tubes are
of the order of 2fm ... like the flux tubes for
“central” pp scatterings!

- Energy density comparable
to AuAu@RHIC

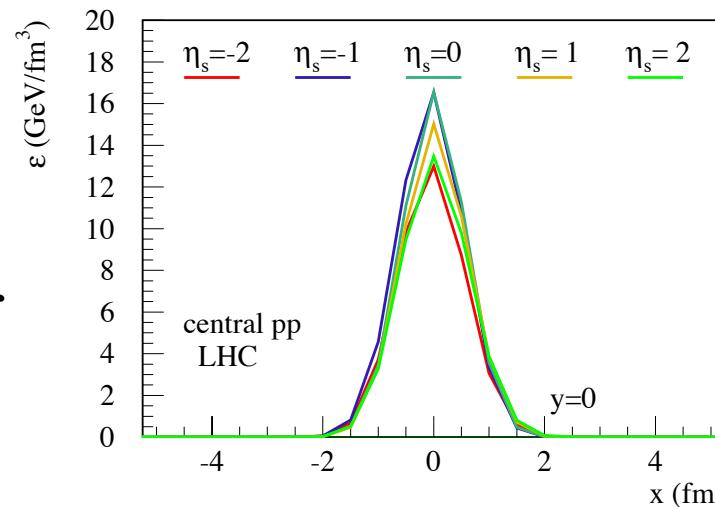
- So maybe as well hydrodynamical
expansion + statistical decay

- We will do the corresponding simulation

How to verify ?

- study “centrality dependence” of particle yields, spectra, ...
- multiple scattering events should exhibit long range y correlations

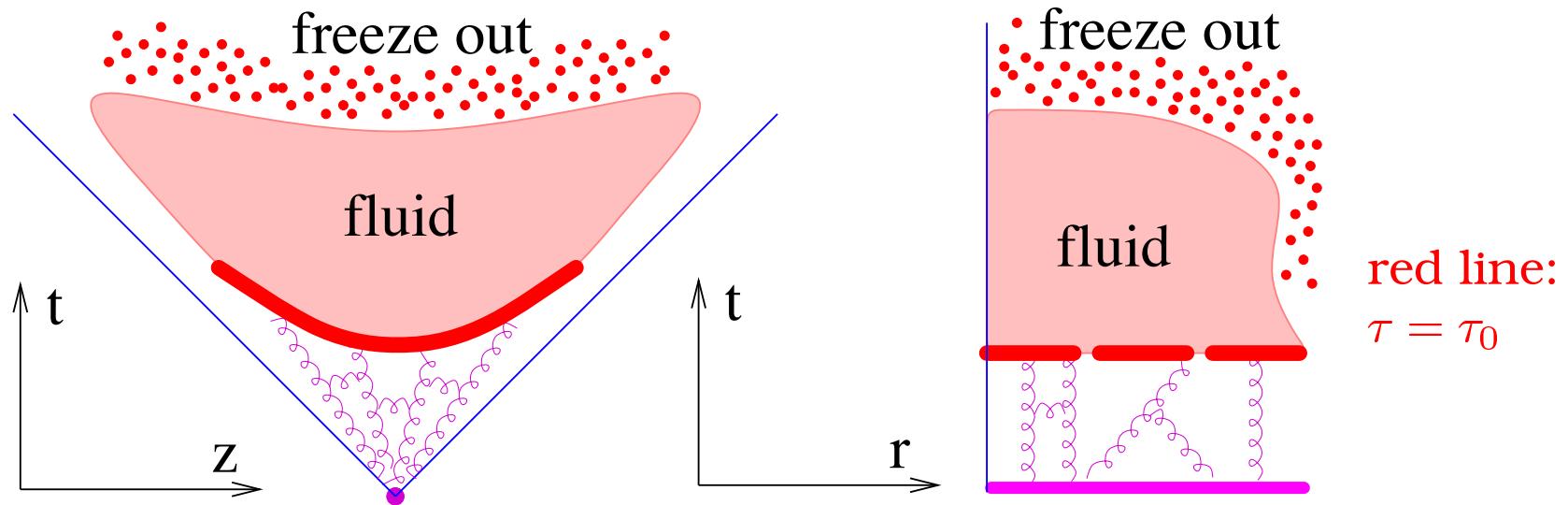
coming from the η_s correlation of the initial flux tubes



- study particle yields, spectra, ... at forward rapidity as a function of the backward multiplicity

- This should clearly exhibit the flux tube structure

4 Hydro evolution / freeze out



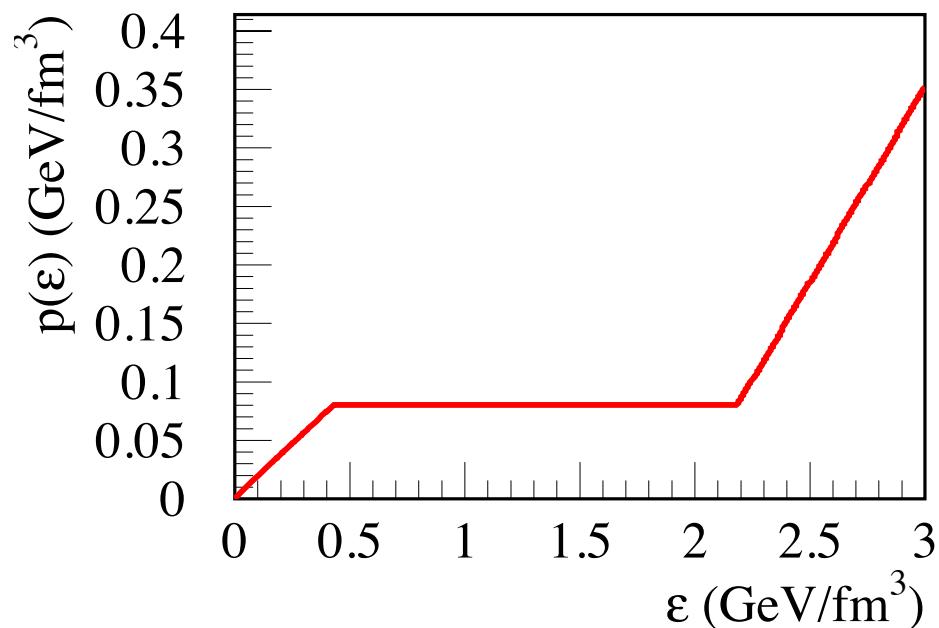
- For $\tau > \tau_0$: 3D hydrodynamic evolution
- determine freeze out hypersurface and collective velocities
- particle production via Cooper-Frye formula
- hadronic cascade

Hydro code (1) - T. Hirano

- T. Hirano, U. Heinz, D. Kharzeev, R. Lacey, Y. Nara, Phys.Rev.C77: 044909,2008, and T. Hirano, U.W.Heinz, D. Kharzeev, R. Lacey and Y. Nara, Phys. Lett. B 636 (2006) 299

- EoS: Massless quarks and gluons, $p = \frac{1}{3}(\varepsilon - 4B)$,
 $B^{1/4} = 247.19\text{MeV}$,
 $\mu_B = 0$

hadron resonance
gas, PCE
(chemical FO at
 $T=T_c=170$ MeV)



Hydro code (2) - Yuri Karpenko (unpublished)

- C++ code, coupled directly to EPOS
- Code based on Godunov method
 - introducing finite cells and computing fluxes between cells using the (approximate) Riemann problem solution for each cell boundary.
- Use relativistic HLLE solver to solve Riemann problems
- To achieve more accuracy in time : the predictor-corrector scheme is used for the second order of accuracy in time, i.e. the numerical error is $O(dt^3)$, instead of $O(dt^2)$
- To achieve more accuracy in space : to achieve the second order scheme, the linear distributions of quantities (conservative variables) inside cells are used. The conservative quantities are $(e + p * v^2)/(1 - v^2)$, $(e + p) * v/(1 - v^2)$.
- The code is written in hyperbolic coordinates

Hydro code (3) - SPHERIO 4, Wei-Liang Qian

- Wei-Liang Qian, Rone Andrade, Frederique Grassi, Otavio Socolowski Jr., Takeshi Kodama, Yojiro Hama, Int.J.Mod.Phys.E16:1877-1882,2007
coupled directly to EPOS
EbE possible

- SPH (Smoothed Particle Hydrodynamics) technique.
Physical quantities are written as

$$f(\vec{x}, t) = \sum_{i=1}^N f_i W(\vec{r} - \vec{r}_i(t))$$

$\partial_\mu T^{\mu\nu} = 0$ & conservations laws lead to eqs. for \vec{r}_i .

- EoS: Ideal gas of quarks and gluons,
 $m_u = m_d = 0$, $m_s = 120\text{MeV}$; $B^{1/4} = 232\text{MeV}$,
 $\mu_u = \frac{1}{3}\mu_B + \frac{1}{2}\mu_{I3}$, $\mu_d = \frac{1}{3}\mu_B - \frac{1}{2}\mu_{I3}$, $\mu_s = \frac{1}{3}\mu_B - \mu_S$;

hadron resonance gas,

$$\mu_h = B\mu_B + S\mu_S + I_3\mu_{I3}$$

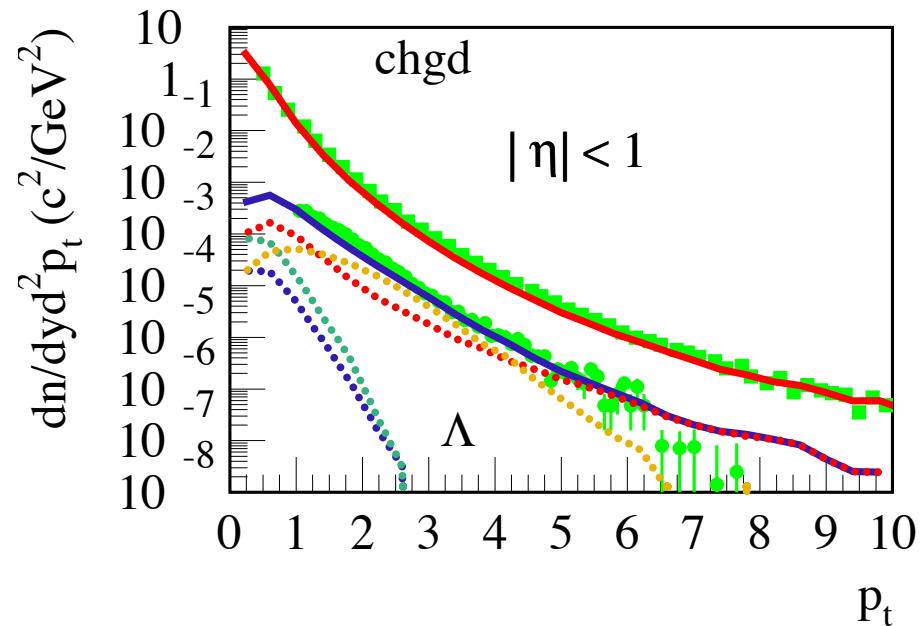
Final state hadronic rescatterings

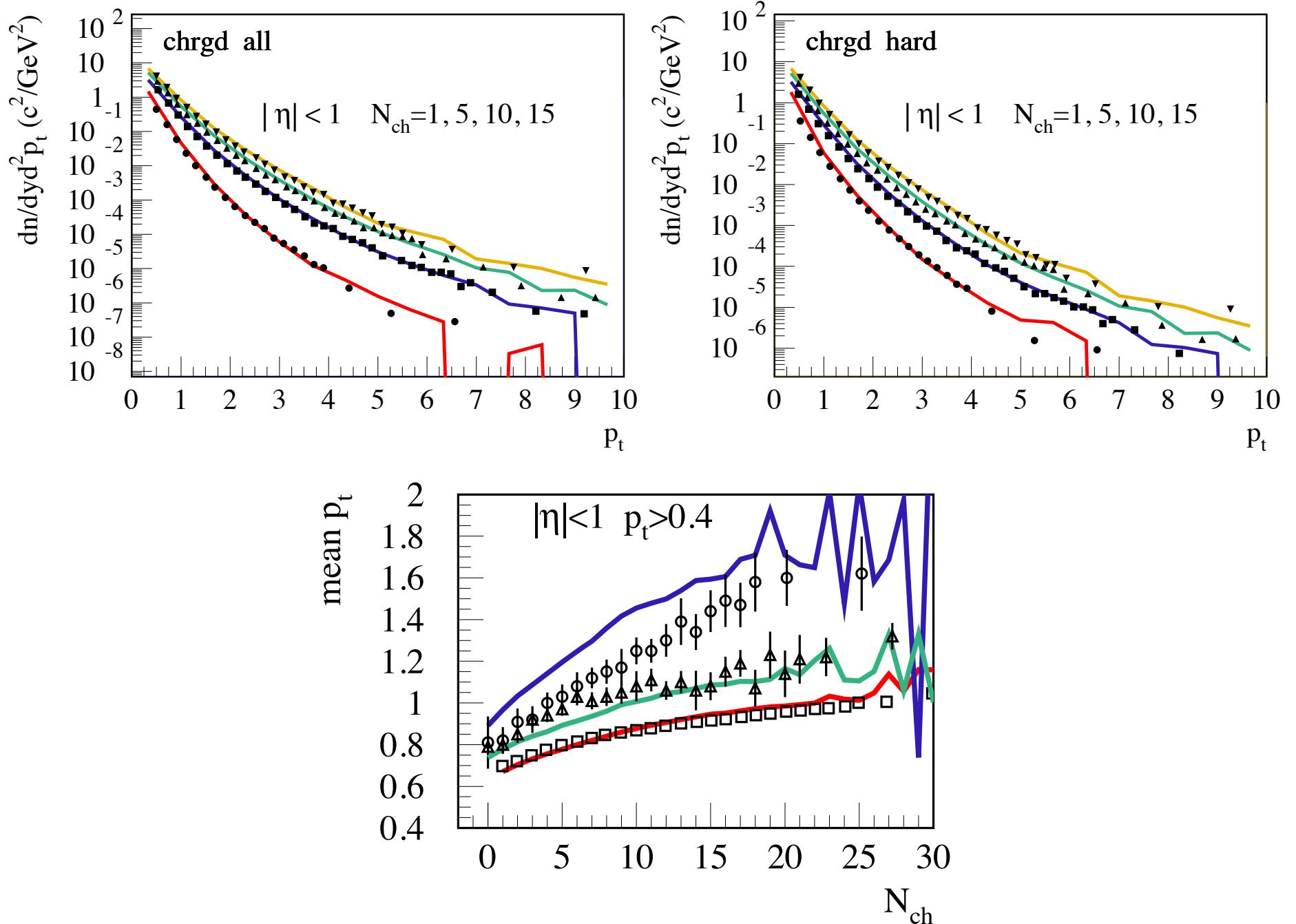
- UrQMD, M. Bleicher et al., J. Phys. G25 (1999) 1859, H. Petersen, J. Steinheimer, G. Burau, M. Bleicher and H. Stocker, Phys. Rev. C78 (2008) 044901,
- EPOS coupling in collaboration with S.Haussler, M.Bleicher, S. Porteboeuf
- FO at some temperature (in the hadronic phase),
FO hadrons & corona hadrons
= initial condition for hadronic cascade

5 Results for pp

- Real hydro calculation: work in progress...
- So far only "hydro-inspired"
(parameterization of FO-flow)

Charged particle and lambda pt spectra: different shapes
(as in AA)





to summarize

- Air shower simulations with EPOS: more muons, due to more baryon production, compared to conventional models. Smaller pA cross section (also necessary to be consistent with Kascade). Consequence: larger Xmax
- EPOS proton-proton collisions at LHC: Multiple scattering important → high energy density flux tubes
- Flux tubes in pp@LHC very similar to in size and density to sub-flux tubes in AuAu@RHIC → same collective behavior expected
- Flux tube picture also supported by “Ridge” phenomenon, and by $v_2 \eta$ dependence