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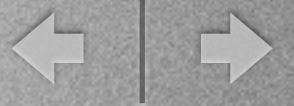
2040-5

Workshop: Eternal Inflation

8 - 12 June 2009

A bit about de Sitter

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A bit about de Sitter

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Eternal Inflation workshop, June 10 2009, ICTP



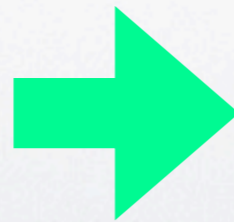
Introduction

QG/EFT in (quasi-) de Sitter is key to understanding eternal inflation

- No global timelike Killing vector
- Horizon, gravitational entropy
- Breakdown of EFT in de Sitter

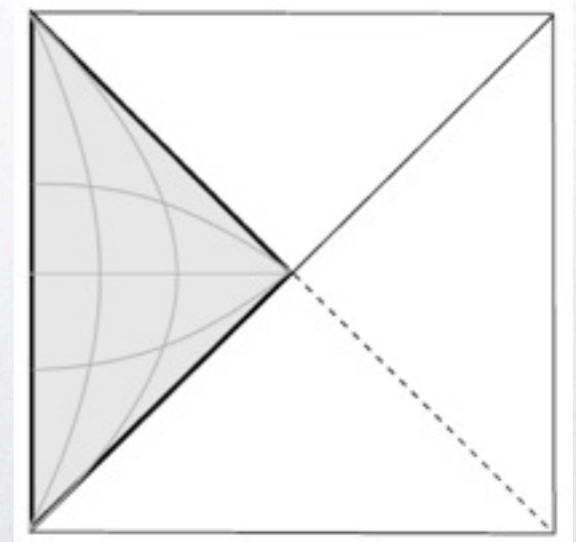
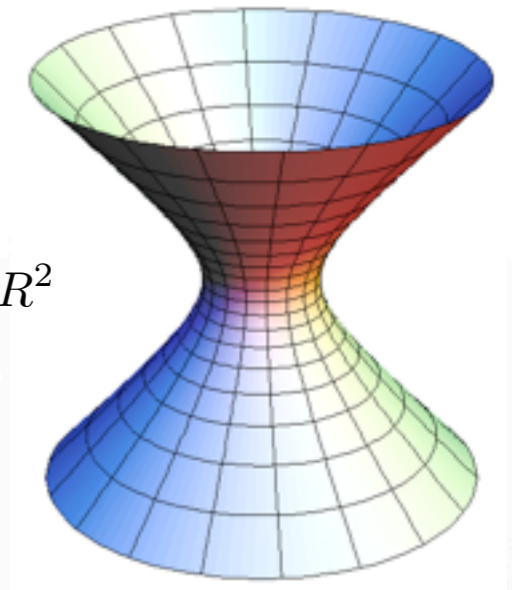
N. Arkani-Hamed, S. Dubovsky, A. Nicolis, E. Trincherini and G. Villadoro, 0704.1814 [hep-th]

**Free-falling observers:
static coordinates**



$$ds^2 = -(1 - H^2 r^2) dt^2 + (1 - H^2 r^2)^{-1} dr^2 + r^2 d\Omega^2$$

$$-X_0^2 + X_1^2 + X_2^2 + X_3^2 + X_4^2 = R^2$$

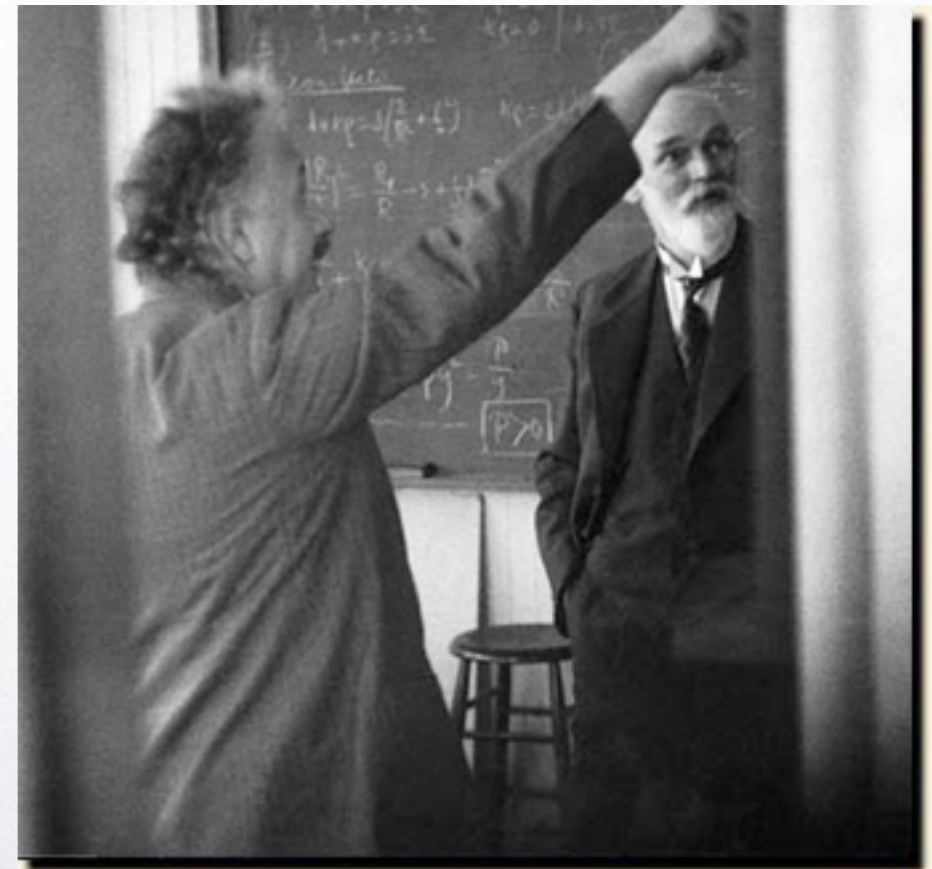


$$T_{GH} = \frac{H}{2\pi}$$
$$S = \frac{A}{4G} \propto \frac{M_{Pl}^2}{H^2}$$



Outline

- De Sitter and black holes
- Tunneling and backreaction
- Complementarity in de Sitter
- Concluding remarks



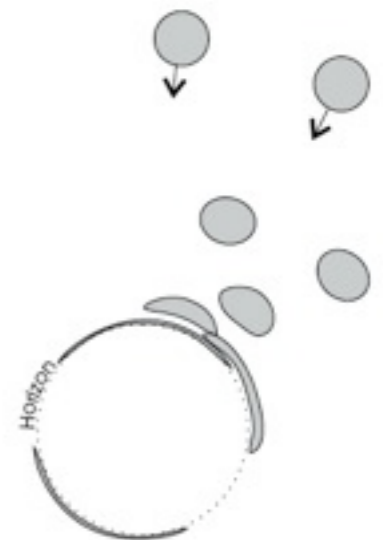
de Sitter and Einstein, 1932



De Sitter and black holes

Similarities and differences: horizon physics

- Locally, near horizon: Rindler space
- Black hole: distinction infalling and external observers
- De Sitter: horizon is observer dependent (dS symmetry)
- Black holes evaporate: sharpens information paradox
- No S-matrix in de Sitter (observables?)
- Black hole singularity



However: horizon properties seem universal

$$T_H = \frac{\hbar \kappa}{2\pi}$$
$$S_{BH} = \frac{A}{4G\hbar}$$



De Sitter vacua

Relation between the static and BD state:

$$ds^2 = -(1 - H^2 r^2) dt^2 + (1 - H^2 r^2)^{-1} dr^2 + r^2 d\Omega^2$$

$$b_k |S\rangle = 0 \quad \longrightarrow \quad T_{GH} = \frac{H}{2\pi} \quad \text{thermal to all other (outgoing) observers}$$

Formal 'lightlike observer' limit of static vacuum state : BD vacuum

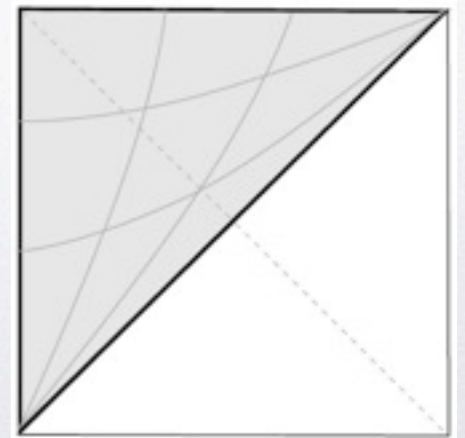
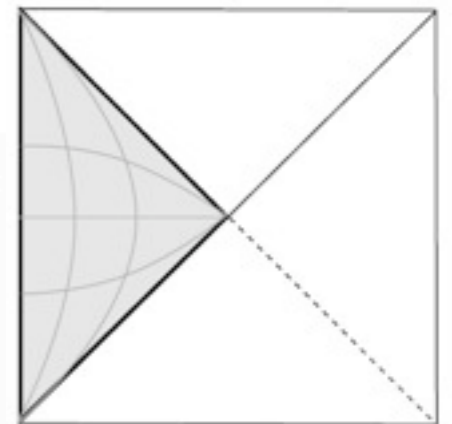
$$ds^2 = -dt^2 + e^{2Ht} dx^2 = \frac{1}{(H\eta)^2} (-d\eta^2 + d\rho^2 + \rho^2 d\Omega^2)$$

$$u_k(\eta, \vec{x}) = N_k (1 + ik\eta) e^{-ik\eta + i\vec{k} \cdot \vec{x}}$$

$$\frac{\partial}{\partial \eta} u_k(\eta, \vec{x}) = -ik u_k(\eta, \vec{x})$$

$$\eta \rightarrow -\infty$$

De Sitter invariant





Tunneling and backreaction

Applies universally (BH's and dS)

Painleve coordinates:

$$ds^2 = -(1 - H^2 r^2) dt^2 - 2Hr dr dt + dr^2 + r^2 d\Omega^2$$

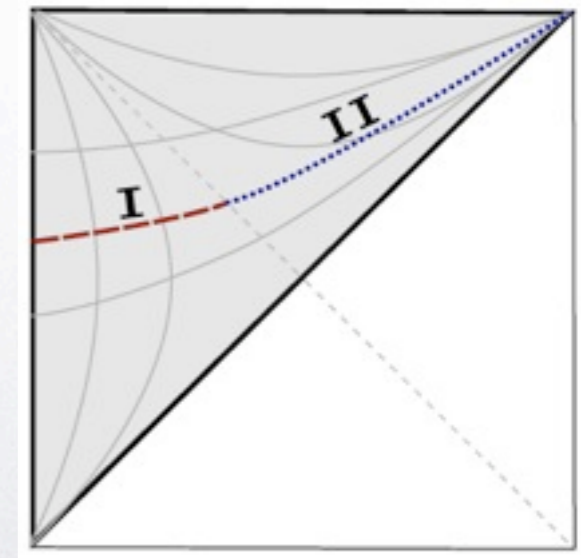
- Finite at horizon
- Planar flat slicing
- Stationary

$$\Gamma \sim \exp(-2 \operatorname{Im} I / \hbar) \sim \exp(\Delta S) = \exp \left[\frac{\pi}{G} (r_f^2 - r_i^2) \right]$$

$$r_i = H^{-1}$$

$$\frac{e^{S_{\text{final}}}}{e^{S_{\text{initial}}}} = \exp(\Delta S)$$

s-waves only



After emission of the spherical shell: SdS spacetime

$$ds^2 = -(1 - H^2 r^2 - 2G\omega/r) dt^2 + (1 - H^2 r^2 - 2G\omega/r)^{-1} dr^2 + r^2 d\Omega^2$$

$$G\omega H \ll 1$$



$$\Gamma \approx \exp \left[-\frac{2\pi}{H} \omega \left(1 + \frac{\omega H}{8\pi M_p^2} \right) \right]$$

$$\left| \frac{\langle \text{out} | b_k b_{-k} | \text{BD}' \rangle}{\langle \text{out} | \text{BD}' \rangle} \right|^2 = e^{\Delta S(\omega_k)}$$

Universal correction to BD

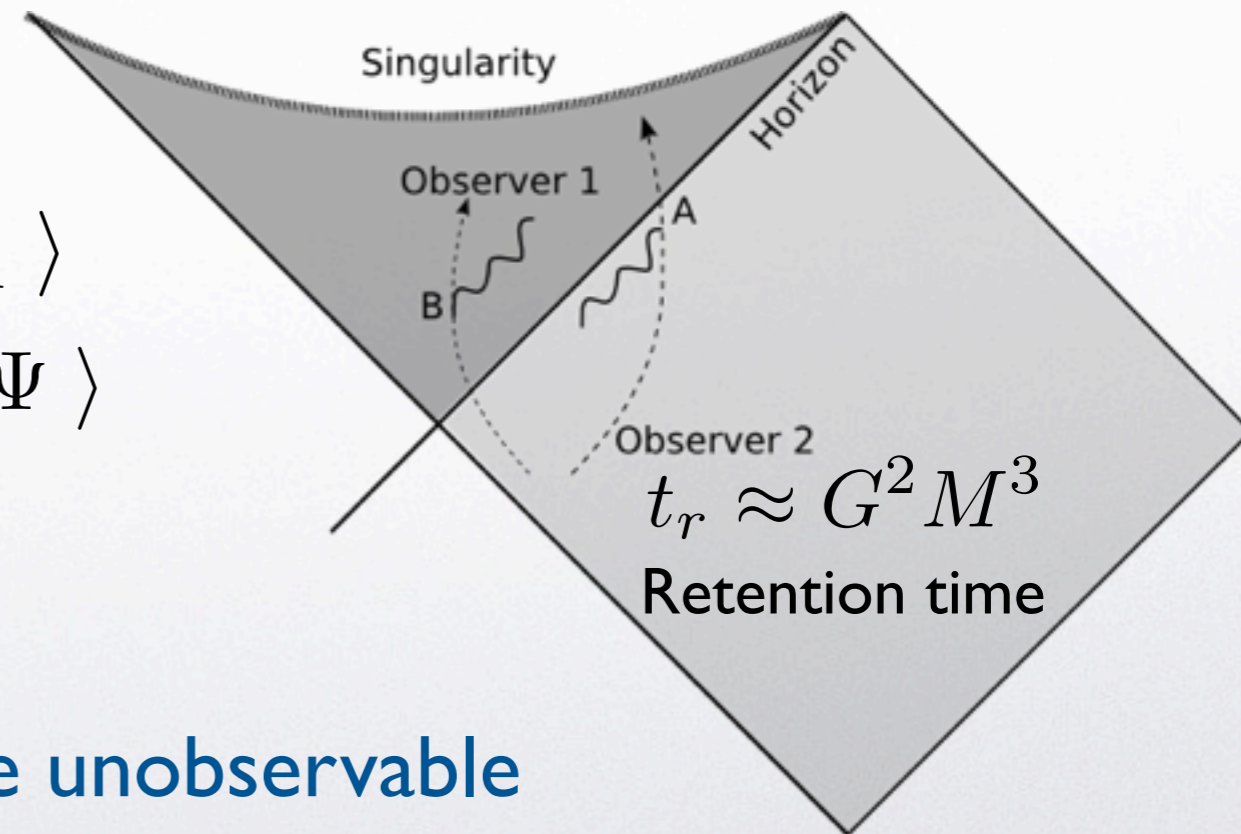
M. Parikh, hep-th/0204107
B. Greene, M. Parikh and JPvdS, hep-th/0512243



Black hole complementarity

1. Observer 1 jumps in carrying a single bit (spin)
2. At point A observer 2 reads the bit in the Hawking radiation
3. Observer 2 then jumps in to see same bit twice
4. At point B observer 1 sends the bit to observer 2

- **Unitarity** $|\Psi_{\text{out}}\rangle = S|\Psi_{\text{in}}\rangle$
- **Linearity** $|\Psi\rangle \not\rightarrow |\Psi\rangle \otimes |\Psi\rangle$
- **Equivalence principle**



Complementarity: violations should be unobservable



Entanglement and information

Information: $I = S_{\text{maximal}} - S_{\text{actual}}$

Consider two subsystems of a total system in a pure state and let the smaller subsystem have a Hilbert space of dimension $m < n$, where n is the Hilbert space dimension of the other subsystem

$$S = -\text{Tr } \rho \log \rho$$

The entanglement entropy, averaged over all pure states, reads

$$\langle S \rangle = \sum_{k=n+1}^{k=mn} \frac{1}{k} - \frac{m-1}{2n} \quad \rightarrow \quad \langle I_{m,n} \rangle = \ln m - \langle S \rangle \approx \frac{m}{2n}$$

Typically the subsystem contains no information (thermal) until it reaches at least half the size of the whole system

$$t_r \approx G^2 M^3$$

Page, gr-qc/9305007



Complementarity in de Sitter

1. Observer 1 jumps in carrying a single bit (spin)
2. At point A observer 2 reads the bit in the Hawking radiation
3. Observer 2 then jumps in to see same bit twice
4. At point B observer 1 sends the bit to observer 2

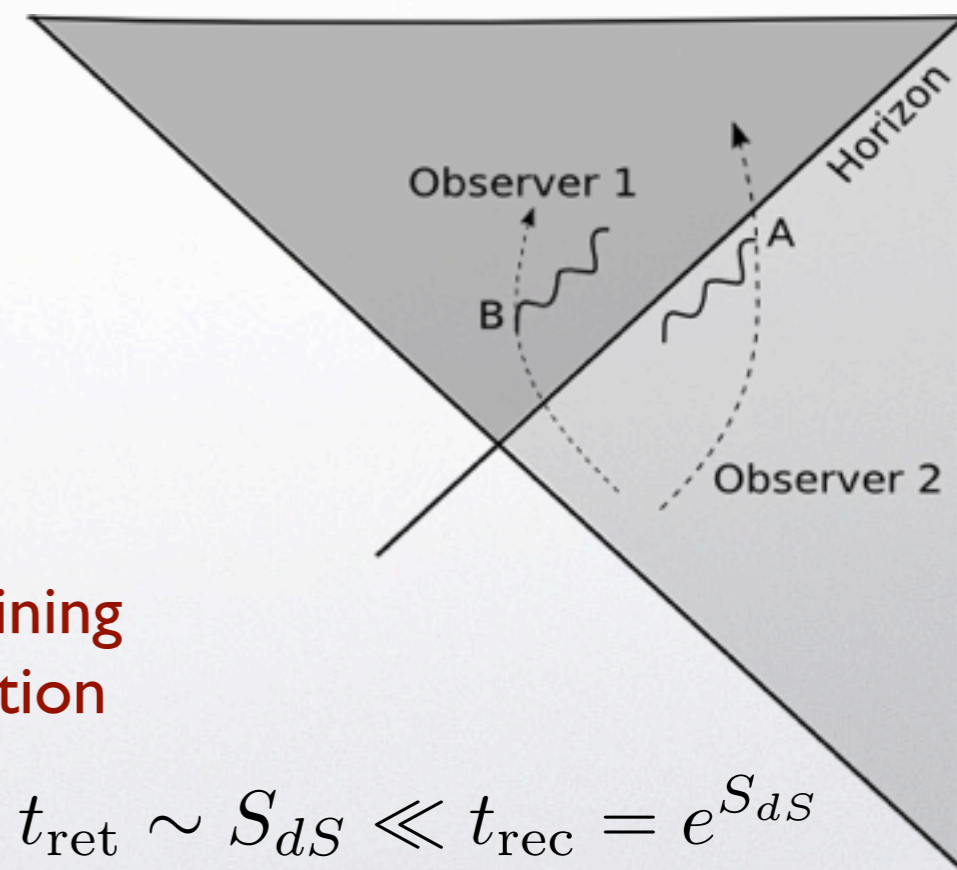
Observer 2:

$$S = \frac{A}{4G} \propto \frac{M_{Pl}^2}{H^2}$$

- **Unitarity** $|\Psi_{out}\rangle = S|\Psi_{in}\rangle$
- **Linearity** $|\Psi\rangle \not\rightarrow |\Psi\rangle \otimes |\Psi\rangle$
- **Equivalence principle**

Observer 2 collects Hawking radiation, but before obtaining a single bit the (maximal) entropy of the collected radiation should at least be 1/2 the dS entropy [Page]

$$t_{ret} \sim S_{dS} \ll t_{rec} = e^{S_{dS}}$$





Maximal information storage

In de Sitter, the most entropic subsystem consists of the largest black hole that will fit, the Nariai solution.

In D dimensions this reads $\frac{A_{D-2} r_H^{D-2}}{4G}$ with $H r_H = \left(\frac{D-3}{D-1} \right)^{1/2}$

$$\frac{S_{\text{subsystem}}}{S_{\text{dS}}} \leq \left(\frac{D-3}{D-1} \right)^{(D-2)/2} < \frac{1}{e} = \frac{1}{3} \text{ in } D=4$$

R. Bousso, hep-th/0205177

No observer will ever be able to register a single bit, because backreaction will have interfered. Saves complementarity, but applies more generally

M. Parikh and J. P. v. d. S., 0804.0231[hep-th]



Causal patch holography?

No observer in de Sitter can register even a single bit of information in the Hawking radiation

- Holography: all information stored in dS causal region
- Information might be there, but cannot be accessed
- Localized detectors have a finite number of states
- No information about the landscape can be retrieved through Hawking radiation (assuming asymptotic dS)



Final remarks

Be careful using EFT in an eternal inflation context

- Many black hole results/puzzles generalize to dS
- Crucial role played by backreaction
- Could imply breakdown of EFT, possibly at macroscopically large distance scales
- Fundamental obstruction to recover information
- Practical meaning of holography in causal region?