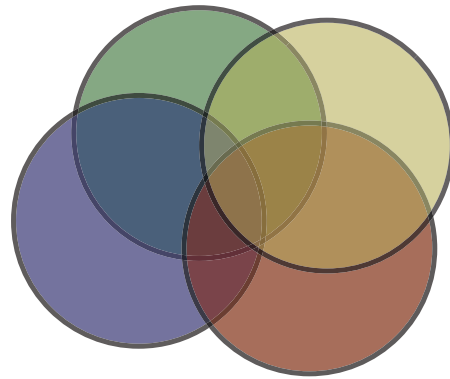**Workshop: Eternal Inflation**

8 - 12 June 2009

A CFT for Eternal Inflation

KLEBAN Matthew B.

New York University
Center for Cosmology and Particle Physics
Department of Physics 4 Washington Place
New York NY, 10003
U.S.A.

a conformal field theory for eternal inflation

Matthew Kleban
New York University

based on:

- "A Conformal Field Theory for Eternal Inflation", MK, B. Freivogel, arXiv:0903.2048

related work:

- MK, Freivogel, Nicolis, and Sigurdson; Bousso, Freivogel, and Yang; Garriga and Vilenkin; Guth, Garriga, and Vilenkin; Freivogel, Sekino, Susskind and Yeh; Chang, MK, and Levi; Susskind; Freivogel, Horowitz, and Shenker; Winitzki; Maldacena; Dyson, MK, and Susskind; Freivogel, MK, Rodriguez-Martinez, Susskind; Strominger; Guth and Weinberg; Hawking, Moss, and Stewart...

de Sitter space

- dS space is central in modern cosmology

- it approximates inflation, and the universe appears to be entering a future dS phase

- if they exist in the string landscape, one expects dS regions to dominate the global spacetime volume

- our observable universe would be a bubble immersed in an eternally inflating bath

- dS surrounds us in both space and time

but...

- dS is notoriously difficult to understand

- it expands exponentially, forever fragmenting into causally disconnected pieces

- every point is surrounded by a finite area event horizon, with a quantum temperature and horizon entropy

- it has no observable S-matrix or timelike boundary on which to define a holographic dual

- field at spacelike separation fluctuates independently at late times; correlations functions are unobservable
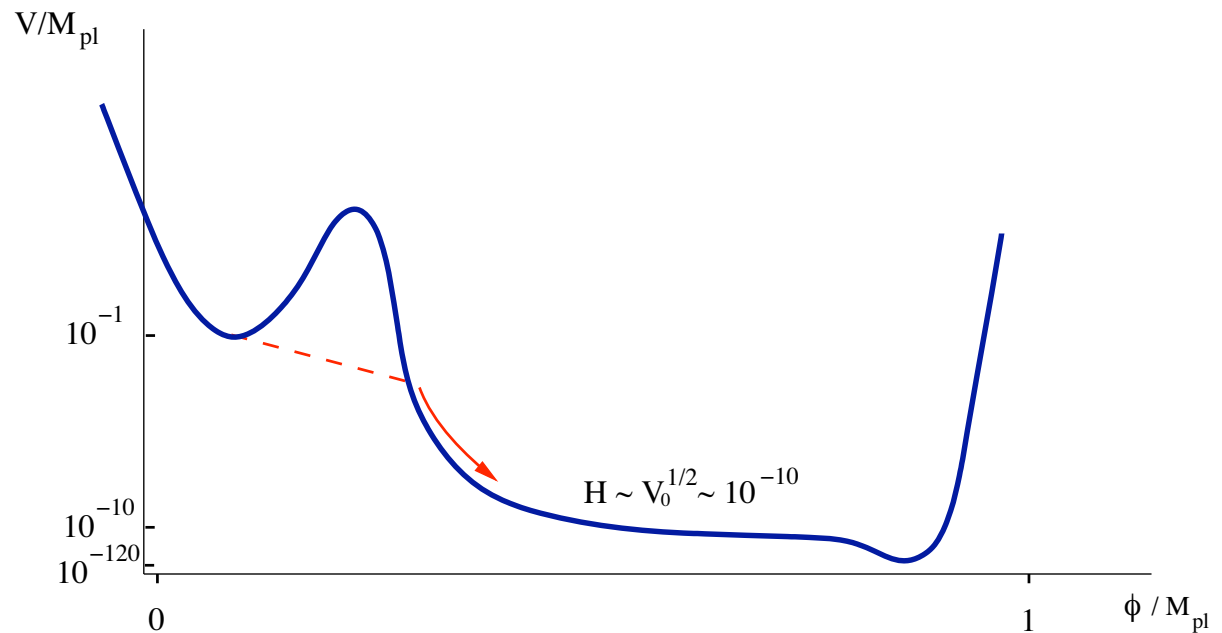
false vacuum eternal inflation

consider a scalar field with a potential like this

classically, it will inflate (i.e. dS) forever in either minimum

quantumly, it will tunnel via bubble nucleation from either into the other after finite time

V/M_{pl}

10^{-1}

10^{-10}
10^{-120}

$H \sim V_0^{1/2} \sim 10^{-10}$

0

0

1

ϕ / M_{pl}

(a potential like this makes a universe in a bubble, very much like the one we observe)

I'll call this dimensionless "decay rate" per unit Hubble time per unit Hubble volume γ

cosmology

- in the string theory landscape, our universe may be inside such a bubble

- every such bubble will eventually be struck by an infinite number of others

- these can have potentially observable effects now (for example on our CMB) if $\gamma\sqrt{\Omega_k}\,(V_f/V_i) > 1$

- in field theory, compute S-matrix elements because they are mathematically well-defined and closely related to real observables

- try to use real cosmological observables to define a set of asymptotic, well-defined quantities?
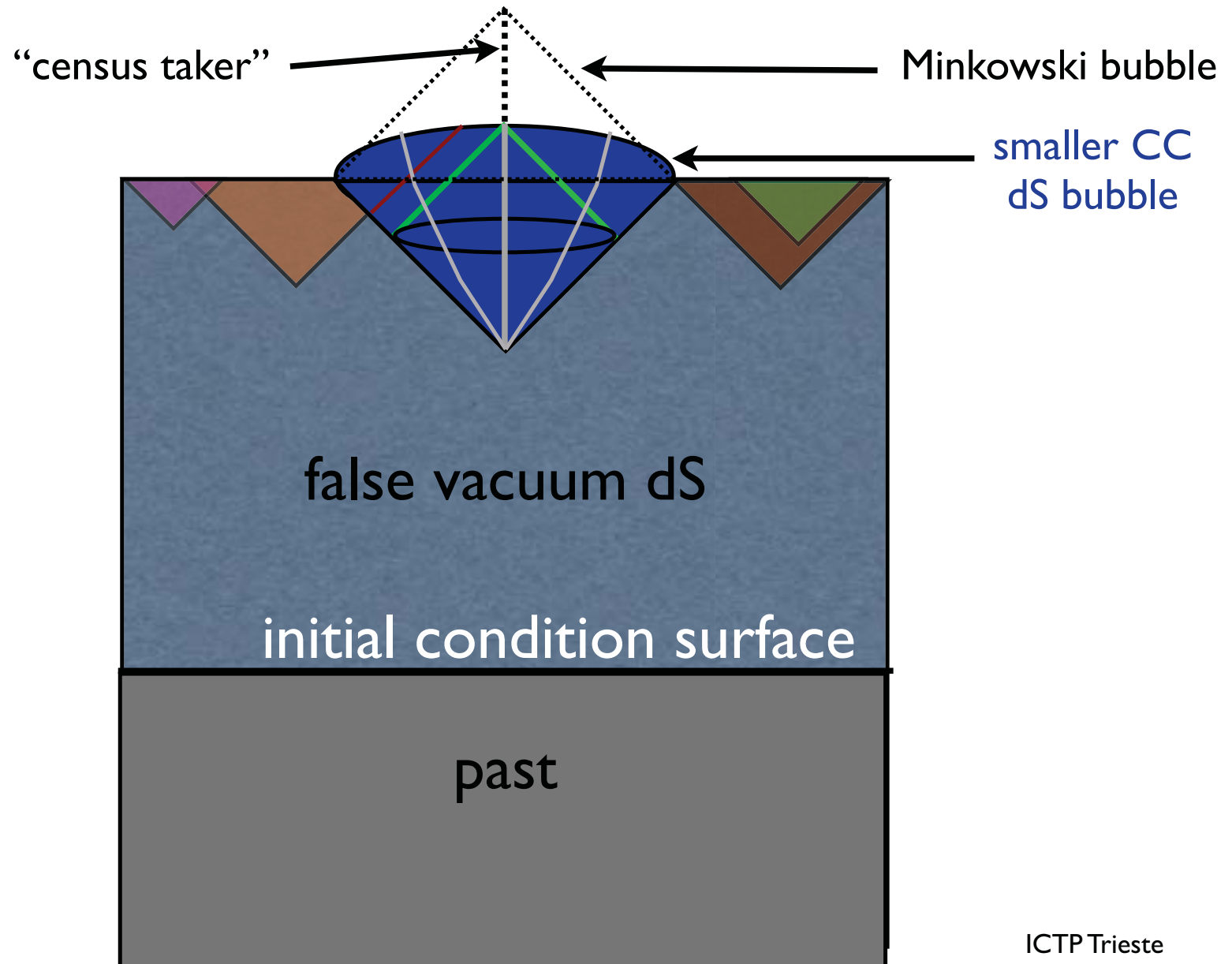
to begin...

...imagine starting in a region of the universe where the field is roughly homogeneous and in its false vacuum

any initial inhomgeneities or impurities will rapidly inflate away, leaving a state very close to empty de Sitter

but after about γ^{-1} efolds, a bubble of "true" vacuum will appear and begin to expand
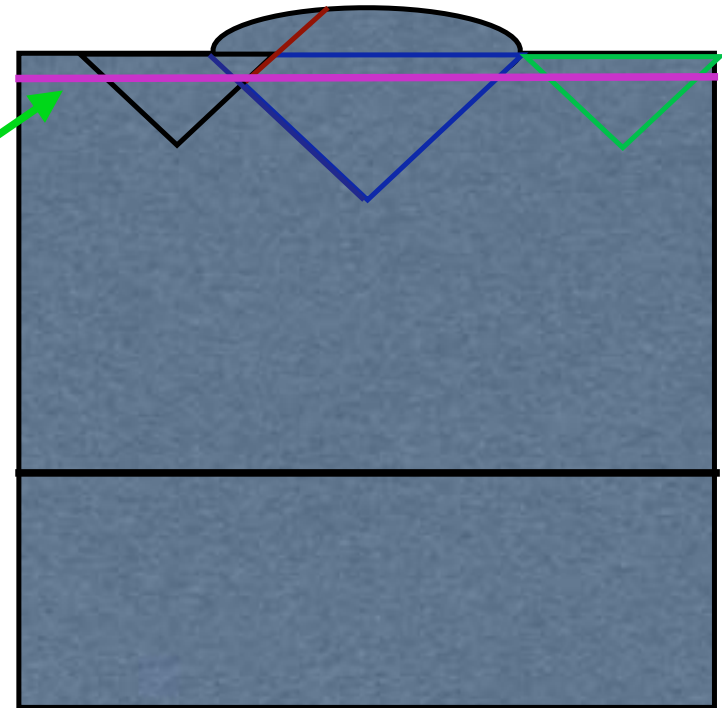
a conformal diagram

"census taker"

Minkowski bubble

smaller CC
dS bubble

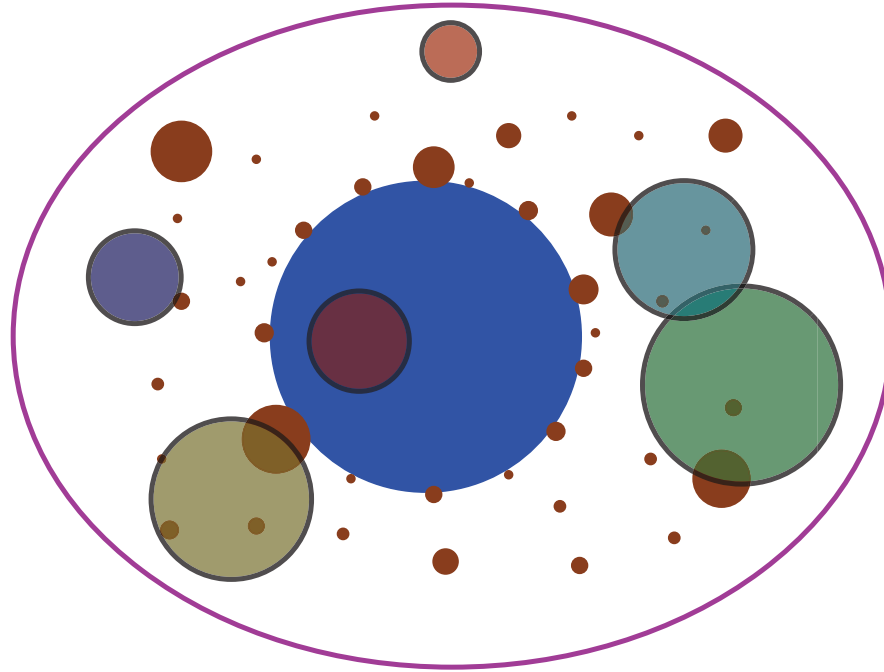false vacuum dS

initial condition surface

past

global slices

late global
time slice

a global time slice of dS in D
dimensions is a d=D-1 sphere

$$ds_D^2 = -dt^2 + H^{-2}\cosh^2(Ht)d\Omega_{D-1}^2$$

Matthew Kleban

ICTP Trieste

viewed from above (fixed t)

each bubble forms part of an infinite cluster, which may or may not connect to other clusters

for decay rate less than order one, the transition (if there is one) does not percolate or complete

observers in flat bubbles at arbitrarily late times ("census takers") can see an arbitrarily large number of bubbles - all others have a cutoff

the distribution...

...of bubble sizes and locations on these global slices follows immediately from metric

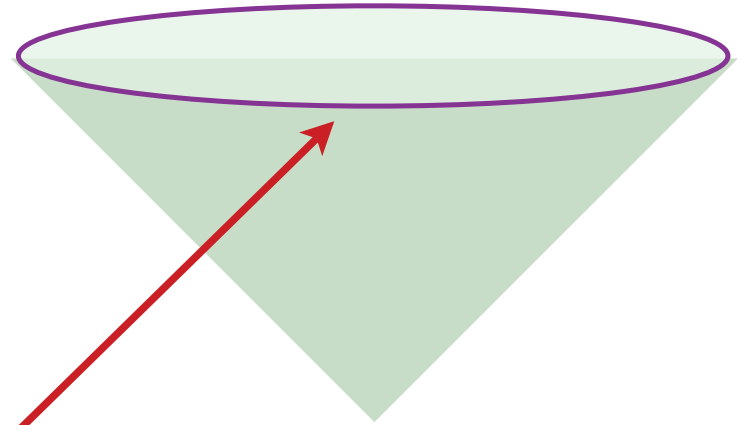the comoving size of the bubble is just the conformal time to infinity, and $dN = \gamma \, dV \, d\eta$

the metric in conformal coordinates is

$$ds^2 = \frac{1}{\sin^2 \eta}(-d\eta^2 + d\Omega_d^2)$$

and so one immediately obtains

$$dN = \gamma \sin(\psi)^{-(d+1)} d\psi \, d\Omega_d$$

observables?

- the full global slices are never observable

- it may be more interesting to consider the distribution on the wall of observer's bubble - which is the census takers asymptotic sky

- but it turns out that this distribution is **identical**, although now d=D-2

- this is all in the approximation of non-interacting bubbles

dS/dS?

- hence, one can define a d dimension theory either from d+1 dS using global slices, or d+2 dS using the census taker's sky

- finite CC/time for the census taker is a UV cutoff

- the two distributions (in this approximation) are identical, but the interpretation is very different
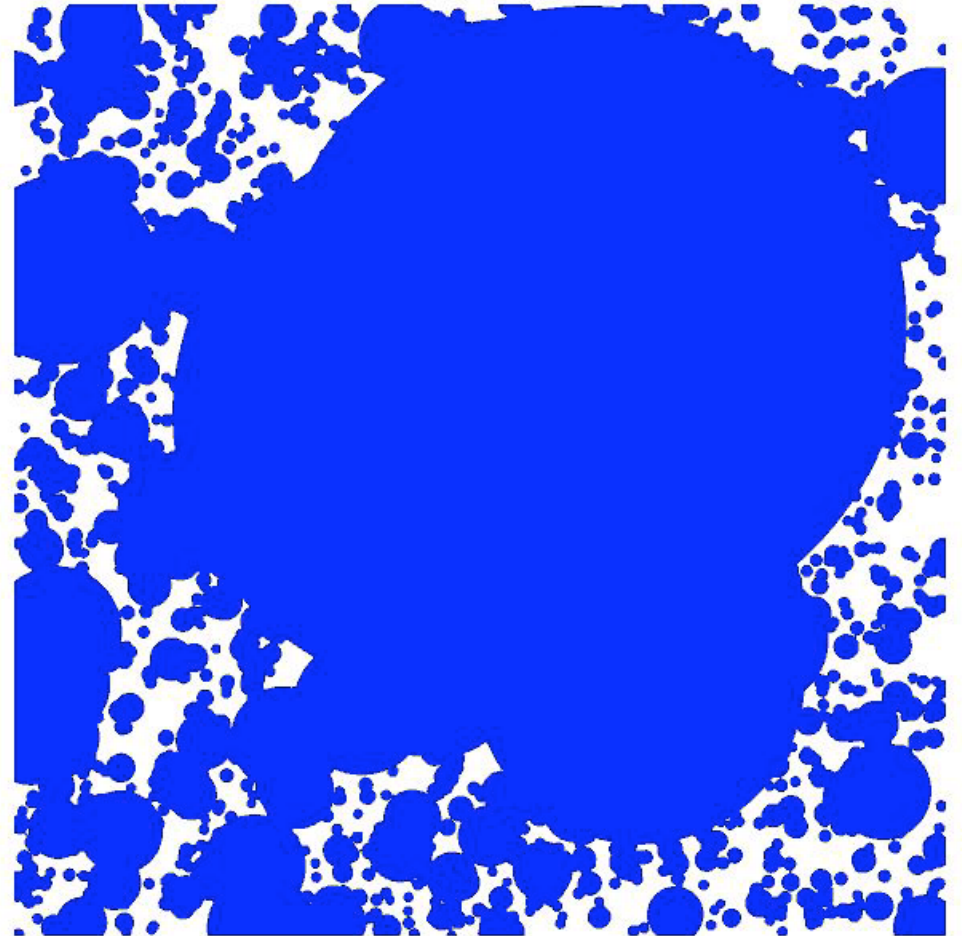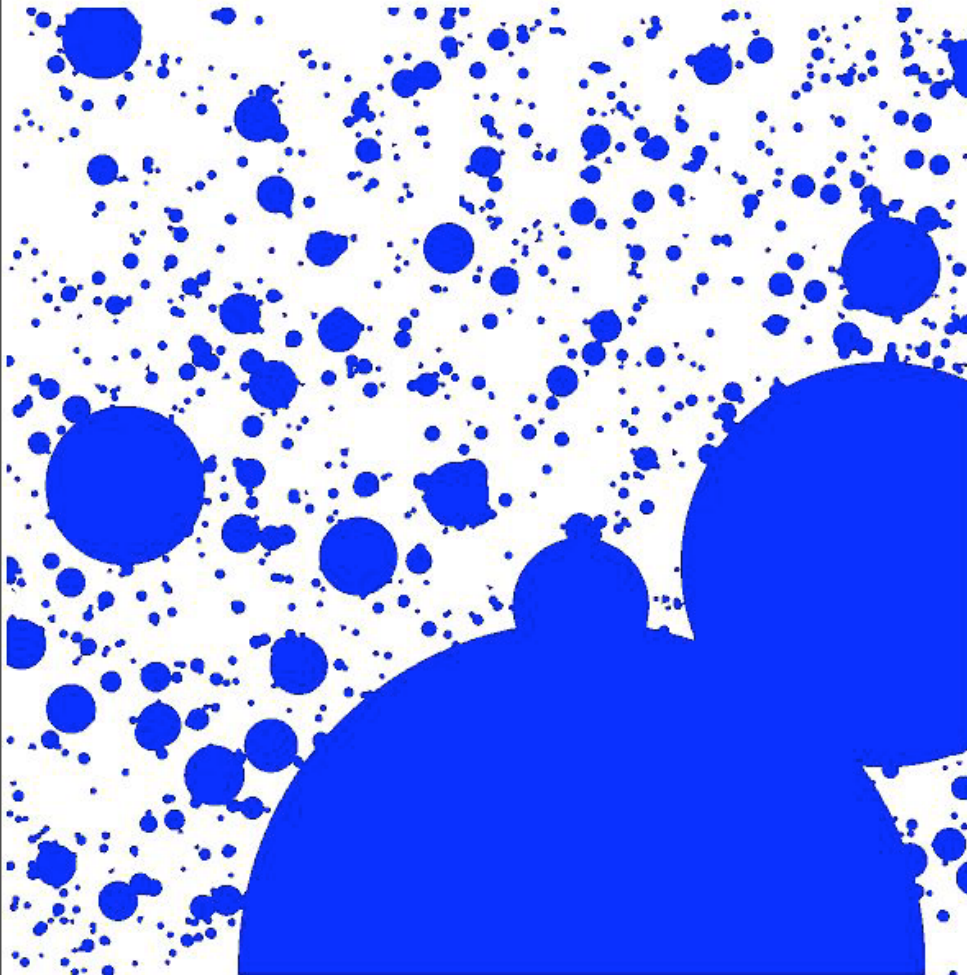
fractal dimension

one can compute the box counting fractal dimension of the set of points that are inside zero bubbles...

$$D_{BC} \equiv -d(\ln n(\epsilon))/d(\ln \epsilon) \qquad n(\epsilon) = V(\epsilon)\epsilon^{-d}$$

$$dV(\epsilon) = V r^d dN(r) = V\gamma(dr/r) \qquad n(\epsilon) = \epsilon^{\gamma-d}$$

$$\boxed{D_{BC} = d - \gamma}$$

Mandelbrot, Vilenkin

Numerical simulations of the model in d = 2. Only one disk type is shown. Left pane: γ = .1, δ/R = .01. Right pane: γ = .5, δ/R = .01.

percolation

- one expects percolation transitions in this set when fractal dimension is near integer

- but if the decay rate is very small, one is far from these transitions

- can there still be a conformal field theory description away from these special points?

- if so, quite unlike standard bond or site percolation

correlation functions

- let's try to define some correlation functions, focussing on the case d=2

- for now we can forget about the bulk dS and focus only on the statistical model

- the most natural quantity is N(z), the number of bubble disks that impinge on z

- so, try to compute <N(z)> using these distributions

- plainly this will diverge.... let's see how

d=2

- in d=(3+1)-2=(2+1)-1=2, stereographically project the 2-sphere distribution to the plane

$$dN = \gamma \sin(\psi)^{-(d+1)} d\psi d\Omega_d$$

- SP maps disks to disks, but both the radii and center locations change

- the distribution in the plane is simply

$$dN = \gamma (dr/r^3) dz d\bar{z}$$

- this is obviously scale invariant, and the stereographic mapping proves it is fully Mobius invariant

- Mobius transformations arise in a beautiful geometric way - they are the action of the 3+1 Lorentz group on the lightcone of the bubble's nucleation event

1-point function of N
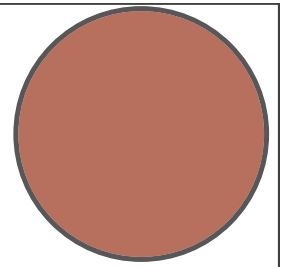
take the average of N(z) over the ensemble of all possible configurations, with weight given by the distribution

$$Z_+ = \sum_{n=0}^{\infty} \frac{\gamma^n}{n!} \prod_{k=1}^{n} \int_{\delta}^{R} \frac{dr_k}{r_k^3} \int dx_k d\bar{x}_k$$

$$N_n(z) = \sum_{k=1}^{n} \Theta\left(|x_k - z| - r_k\right)$$

$$\langle N(z) \rangle = Z_+^{-1} \sum_{n=0}^{\infty} \frac{\gamma^n}{n!} \prod_{k=1}^{n} \int_{\delta}^{R} N_n(z) \frac{dr_k}{r_k^3} dx_k d\bar{x}_k$$

$$\langle N(z) \rangle = Z_+^{-1} Z_+ \gamma \int_{\delta}^{R} \frac{dr}{r^3} \pi r^2 = \pi \gamma \ln\left(R/\delta\right)$$

disks and anti-disks

- the divergence occurs because N+>0

- but in dS, transitions will occur either way

- try allowing for "anti-bubbles" - up transitions - and count the difference

$$N(z) = N_+(z) - N_-(z)$$

bulk field theory

- simplest non-trivial possibility - bubbles can nucleate inside other bubbles, always with the same rate as the parent false vacuum

- such a rule would follow from a bulk field with a periodic potential

- will be interesting to extend this to non-periodic potentials, but will probably require approximation

Matthew Kleban
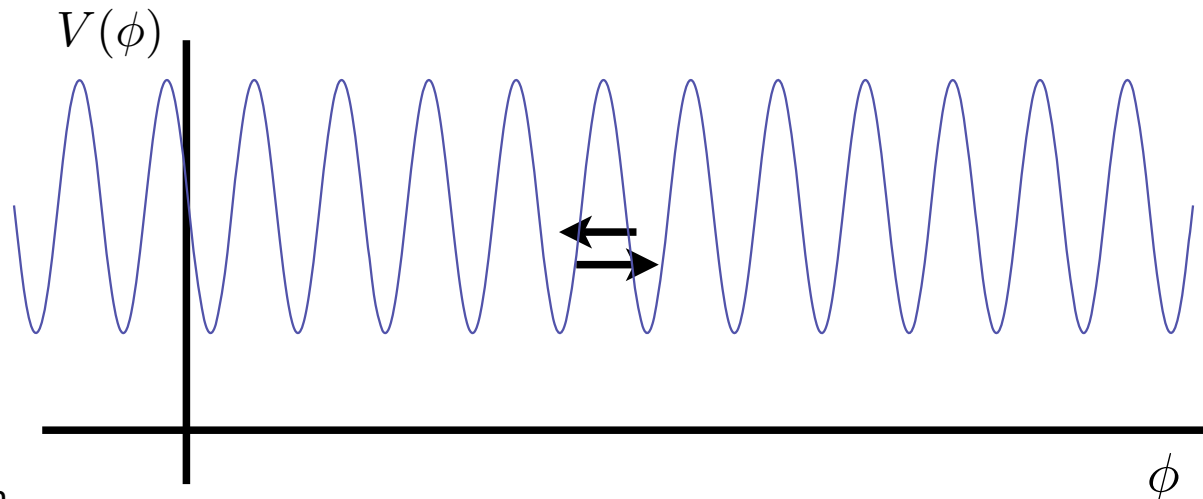
$$Z = Z_+ Z_- = \left(\sum_{n=0}^{\infty} \frac{\gamma^n}{n!} \prod_{k=1}^{n} \int_{\delta}^{R} \frac{dr_k}{r_k^3} \int dx_k d\bar{x}_k \right) \left(\sum_{n=0}^{\infty} \frac{\gamma^n}{n!} \prod_{k=1}^{n} \int_{\delta}^{R} \frac{dr_k}{r_k^3} \int dx_k d\bar{x}_k \right)$$
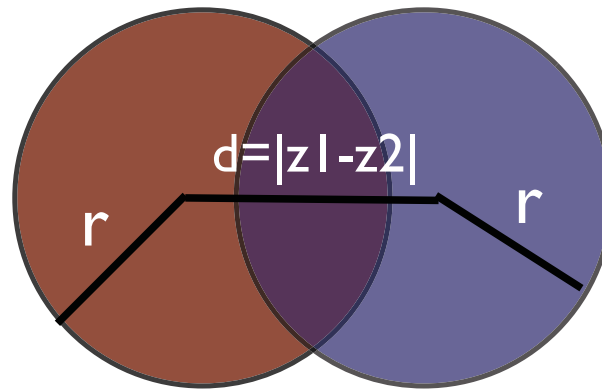
$$\langle N(z) \rangle = \langle N_+(z) - N_-(z) \rangle = (Z_- Z_-^{-1}) \langle N_+ \rangle - (Z_+ Z_+^{-1}) \langle N_- \rangle = 0$$

(note that the transition rates are equal)

what about 2-point functions?

$$\langle N(z_1) N(z_2) \rangle = \langle (N_+(z_1) - N_-(z_1))(N_+(z_2) - N_-(z_2)) \rangle = 2\langle N_+(z_1) N_+(z_2) \rangle - 2\langle N_+ \rangle^2$$

$$\langle N_+(z_1) N_+(z_2) \rangle = Z_+^{-1} \gamma Z_+ \int_{\delta}^{R} \frac{dr}{r^3} \int dz d\bar{z} \, \Theta\left(|z - z_1| - r \right) \Theta\left(|z - z_2| - r \right)$$

$$= \gamma \int_{\delta}^{R} \frac{dr}{r^3} A_{12}(d_{12}, r)$$

$$A_{12}(d_{12}, r) = 2r^2 \left(\cos^{-1}(d_{12}/2r) - (d_{12}/2r)\sqrt{1 - (d_{12}/2r)^2} \right) \Theta(2r - d_{12})$$

$$\int_\delta^R \frac{dr}{r^3} A_{12}(d_{12}, r) = \pi \ln(R/d_{12}) - \pi/2 + \mathcal{O}\left(R^{-1}\right)$$

$$\phi(z) \equiv (N_+(z) - N_-(z))/\sqrt{\pi\gamma},$$

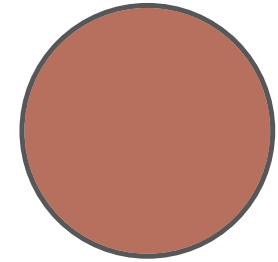$$\boxed{\langle \phi(z_1)\phi(z_2) \rangle = -\ln|z_1 - z_2|^2 + \ln R^2 - 1}$$

this result holds in ALL d: N is always a field with dimension 0

Matthew Kleban

massless scalars

- fields with log correlators are not particularly well-defined - and these fields have a (discrete) shift symmetry

- one usually either differentiates or exponentiates them

- let's try exponentials...

$$V_\beta(z) \equiv e^{i\alpha\phi(z)} = e^{i\beta(N_+(z)-N_-(z))}, \text{ where } \beta = \alpha/\sqrt{\pi\gamma}.$$
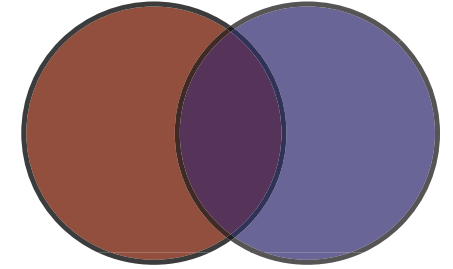
1-point function

$$\langle V_\beta(z_1) \rangle = Z_+^{-2} \left| \exp \left\{ \gamma \int_\delta^R \frac{dr}{r^3} \int dx d\bar{x} \left[e^{i\beta} \Theta(2r - |x - z_1|) + \Theta(-2r + |x - z_1|) \right] \right\} \right|^2$$

$$\langle V_\beta(z_1) \rangle = \exp \left[-2\gamma(1 - \cos\beta) \int_\delta^R \frac{dr}{r^3} A_1(r) \right]$$

$$\langle V_\beta(z) \rangle = \left(\frac{R}{\delta} \right)^{-2\pi\gamma(1-\cos\beta)} = \left\{ \begin{array}{ll} 1 & \text{if } \beta = 2\pi n, \ n \in \mathcal{Z} \\ 0 & \text{otherwise} \end{array} \right\}$$

periodic conservation of charge

2-point functions

$$\langle V_{\beta_1}(z_1)V_{\beta_2}(z_2)\rangle = |\langle \exp\left[i\beta_1 N(z_1) + i\beta_2 N(z_2)\right]\rangle|^2 =$$

$$\exp\left\{\gamma \int \frac{dr}{r^3}\int dxd\bar{x}\left(-2 + 2\cos\left[\beta_1\Theta(r-|x-z_1|) + \beta_2\Theta(r-|x-z_2|)\right]\right)\right\}$$

$$\langle V_{\beta_1}(z_1)V_{\beta_2}(z_2)\rangle = \exp\left\{-2\gamma\int \frac{dr}{r^3}\left[(1-\cos\beta_1)A_1^0 + (1-\cos\beta_2)A_2^0 + (1-\cos(\beta_1+\beta_2))A_{12}^0\right]\right\}$$

$$= \exp\left\{-2\pi\gamma\left[(1-\cos\beta_1)I_1^0 + (1-\cos\beta_1)I_1^0 + (1-\cos\beta_2)I_2^0 + (1-\cos(\beta_1+\beta_2))I_{12}^0\right]\right\}$$

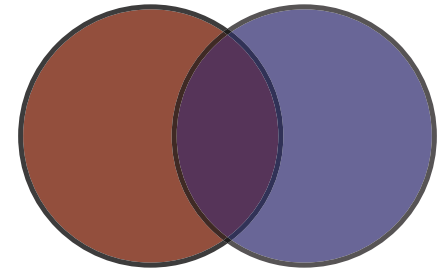$$I_1^0(z_1,z_2) \equiv \frac{1}{\pi}\int \frac{dr}{r^3}A_1^0(r,z_1,z_2)$$

$$I_1^0 = I_1 - I_{12}$$
$$I_2^0 = I_2 - I_{12}$$
$$I_{12}^0 = I_{12}$$

$$I_1^0 = I_2^0 = \ln \frac{|z_{12}|}{\delta}$$

$$I_{12}^0 = \ln \frac{R}{|z_{12}|}$$

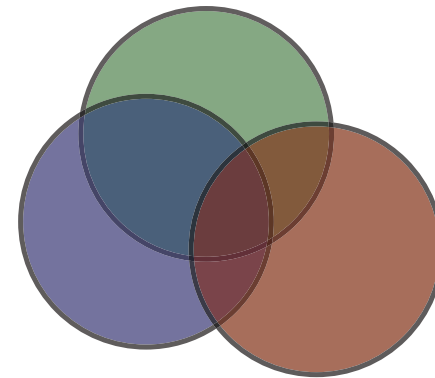Need the coeff of the overlap area =0, i.e. $\beta_1 + \beta_2 = 2\pi n$

$$\boxed{\langle V_{\beta_1}(z_1) V_{\beta_2}(z_2) \rangle = \left(\frac{\delta}{z_1 - z_2} \right)^{2\pi\gamma(1-\cos\beta_1)} \left(\frac{\delta}{\bar{z}_1 - \bar{z}_2} \right)^{2\pi\gamma(1-\cos\beta_1)}}$$

$$\Delta(\beta) = \bar{\Delta}(\beta) = \pi\gamma \left(1 - \cos\beta \right)$$

This is the correct behavior for a conformal field!

And reminiscent of bulk dispersion relation for a periodic potential...

3-point functions

$$\langle V_{\beta_1}(z_1)V_{\beta_2}(z_2)V_{\beta_3}(z_3)\rangle = \exp\left\{-2\pi\gamma\left[(1-\cos\beta_1)I_1^0 + (1-\cos\beta_2)I_2^0 + (1-\cos\beta_3)I_3^0 + (1-\cos(\beta_1+\beta_2))I_{12}^0 + (1-\cos(\beta_1+\beta_3))I_{13}^0 + (1-\cos(\beta_2+\beta_3))I_{23}^0 + (1-\cos(\beta_1+\beta_2+\beta_3))I_{123}^0\right]\right\}$$
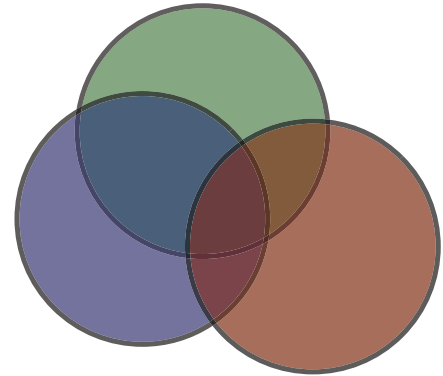
$$\beta_1 + \beta_2 + \beta_3 = 2\pi n$$

$$\langle V_{\beta_1}(z_1)V_{\beta_2}(z_2)V_{\beta_3}(z_3)\rangle =$$
$$\exp\left\{-2\pi\gamma\left[(1-\cos\beta_1)(I_1^0 + I_{23}^0) + (1-\cos\beta_2)(I_2^0 + I_{13}^0) + (1-\cos\beta_3)(I_3^0 + I_{12}^0)\right]\right\}$$

$$I_1^0 = I_1 - I_{12} - I_{13} + I_{123}$$
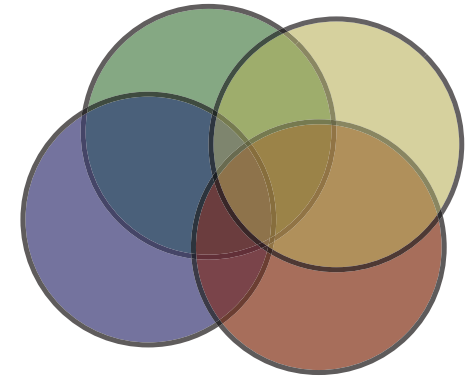$$I_{23}^0 = I_{23} - I_{123}$$

and the result is...

$$\langle V_{\beta_1}(z_1) V_{\beta_2}(z_2) V_{\beta_3}(z_3) \rangle = \left| \left(\frac{\delta}{z_1 - z_2} \right)^{\Delta_1 + \Delta_2 - \Delta_3} \left(\frac{\delta}{z_1 - z_3} \right)^{\Delta_1 + \Delta_3 - \Delta_2} \left(\frac{\delta}{z_2 - z_3} \right)^{\Delta_2 + \Delta_3 - \Delta_1} \right|^2$$

this is the correct conformally covariant 3-point function for a set of conformal primaries with dimensions as above

these quantities are IR finite and have consistent and positive dimensions, which is non-trivial

Mobius invariance fixes this form for operators of definite weight, because the lowest Mobius invariant is the cross ratio of four points
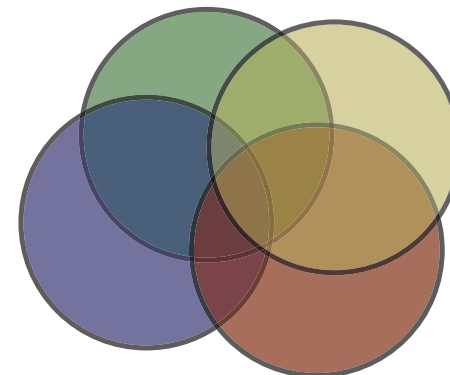
Matthew Kleban   ICTP Trieste

forging ahead...

$$\langle V_{\beta_1}(z_1) V_{\beta_2}(z_2) V_{\beta_3}(z_3) V_{\beta_4}(z_4) \rangle = \exp\{-2\pi\gamma[\sum_i (1 - \cos\beta_i) I_i^0 + \sum_{i<j} (1 - \cos(\beta_i + \beta_j)) I_{ij}^0 +$$

$$\sum_{i<j<k} (1 - \cos(\beta_i + \beta_j + \beta_k)) I_{ijk}^0 + (1 - \cos\sum_i \beta_i) I_{1234}^0]\}$$

$$= \left| \exp\left\{ -\Delta_1(I_1^0 + I_{234}^0) - \Delta_2(I_2^0 + I_{341}^0) - \Delta_3(I_3^0 + I_{412}^0) - \Delta_4(I_4^0 + I_{123}^0) - \sum_{i<j} \Delta_{ij} I_{ij}^0 \right\} \right|^2$$

$$
\begin{aligned}
I_1^0 &= I_1 - I_{12} - I_{13} - I_{14} + I_{123} + I_{124} + I_{134} - I_{1234} \\
I_{12}^0 &= I_{12} - I_{123} - I_{124} + I_{1234} \\
I_{123}^0 &= I_{123} - I_{1234} \\
I_{1234}^0 &= I_{1234}
\end{aligned}
$$

using Mobius, map

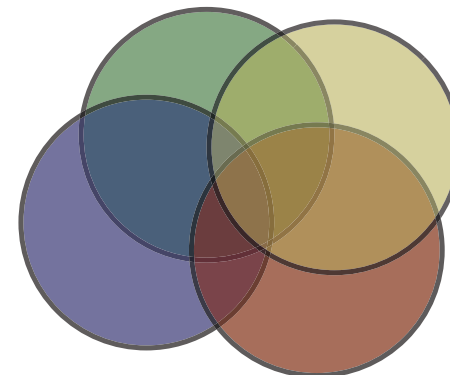$$z_1 = z$$
$$z_2 = 0$$
$$z_3 = 1$$
$$z_4 = \infty$$

$$\langle V_{\beta_1}(z) V_{\beta_2}(0) V_{\beta_3}(1) V_{\beta_4}(\infty) \rangle = C \left| z^{\Delta_1 + \Delta_2 - \Delta_{12}} (1-z)^{\Delta_1 + \Delta_3 - \Delta_{13}} \exp \left\{ - \left(\sum_i \Delta_i - \frac{1}{2} \sum_{i<j} \Delta_{ij} \right) I_{123} \right\} \right|^2$$

reduces 4-point function to 3 points, but now without 3-charge conservation

the cross ratio is z

4-point function

$$\pi I_{123} = -\frac{\pi}{2} + \pi \ln R - \mathrm{sgn}(\Im(z)) \left\{ \Im[\ln z \ln(1 - \bar{z})] + \mathrm{D}_2(z) \right\}$$

which gives

$$\langle V_{\beta_1}(z) V_{\beta_2}(0) V_{\beta_3}(1) V_{\beta_4}(\infty) \rangle = C \left| z^{-\Delta_1 - \Delta_2 + \Delta_{12}} (1 - z)^{-\Delta_1 - \Delta_3 + \Delta_{13}} \right|^2 \times$$

$$\exp \left\{ \left(\frac{2}{\pi} \sum_i \Delta_i - \frac{1}{\pi} \sum_{i<j} \Delta_{ij} \right) \mathrm{sgn}(\Im(z)) \left\{ \Im[\ln z \ln(1 - \bar{z})] + \mathrm{D}_2(z) \right\} \right\}$$

Here $\mathrm{D}_2(z)$ is the Bloch-Wigner function

$$\mathrm{D}_2(z) = \Im[\mathrm{Li}_2(z)] + \arg(1 - z) \ln |z|$$

This function is invariant under crossing symmetry:

$$z \to 1 - \frac{1}{z} \to \frac{1}{1-z} \to \frac{1}{z} \to 1 - z \to \frac{-z}{1-z}$$
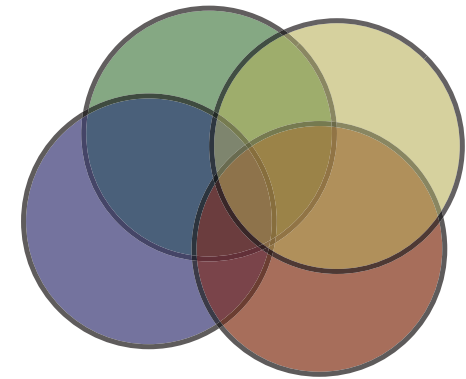
For example, using

$$\text{sgn}(\Im(z^{-1}))\Im[\ln z^{-1} \ln(1 - \bar{z}^{-1})] = \text{sgn}(\Im(z))\Im[\ln z \ln(1 - \bar{z})] - \pi \ln|z|$$

one can check that

$$\langle V_{\beta_1}(z)V_{\beta_2}(0)V_{\beta_3}(1)V_{\beta_4}(\infty)\rangle = z^{-2\Delta_1}\bar{z}^{-2\Delta_1}\langle V_{\beta_1}(1/z)V_{\beta_4}(0)V_{\beta_3}(1)V_{\beta_2}(\infty)\rangle$$

When z is real (i.e. when all four points are on some circle), it reduces to a simple product of powers

However...

$$\langle V_{\beta_1}(z)V_{\beta_2}(0)V_{\beta_3}(1)V_{\beta_4}(\infty)\rangle = C\left|z^{-\Delta_1-\Delta_2+\Delta_{12}}(1-z)^{-\Delta_1-\Delta_3+\Delta_{13}}\right|^2 \times$$

$$\exp\left\{\left(\frac{2}{\pi}\sum_i\Delta_i - \frac{1}{\pi}\sum_{i<j}\Delta_{ij}\right)\mathrm{sgn}(\Im(z))\left\{\Im[\ln z\ln(1-\bar{z})] + \mathrm{D}_2(z)\right\}\right\}$$

there is a problem. Without the sgn, the functions in the exponent are real and analytic for real z between 0 and 1. Therefore, the exponent is non-analytic (its fifth derivative diverges as z crosses the real axis).

This indicates a problem - this is not yet a true CFT

Arbitrary Dimension

- One can generalize this theory to any d in the obvious way

- the N-point functions can be computed using the same techniques.

- The number operator always has logarithmic correlators

- The 2- and 3-point functions are as before, but with

$$\Delta = \bar{\Delta} = \frac{C_d}{2}\gamma(1 - \cos\beta)$$

- We have not computed the 4-pt function

free field limit

$$\langle e^{i\beta_1 N(z_1)} e^{i\beta_2 N(z_2)} ... e^{i\beta_n N(z_n)} \rangle = \exp(-2C_d\gamma[\sum_{i=1}^{n}(1 - \cos\beta_i)I_i^0 + \sum_{i<j}(1 - \cos(\beta_i + \beta_j))I_{ij}^0 +$$

$$\sum_{i<j<k}(1 - \cos(\beta_i + \beta_j + \beta_k))I_{ijk}^0 + ...]$$

- Consider taking $\gamma \to \infty$ with α fixed $\quad (\alpha = \beta/\sqrt{\pi\gamma})$

- One can re-write the exponent as

$$\sum_{k=1}^{n}\frac{\Delta_{i_1...i_k}}{k!}\sum_{l=0}^{n}\frac{(-1)^l}{l!}\sum_{j_1,j_2,...,j_l}I_{i_1 i_2...i_k j_1...j_l}$$

- using $\quad \Delta_{i_1...i_k} = \pi\gamma(1 - \cos(\beta_{i_1} + ... + \beta_{i_k})) = (\alpha_{i_1} + ... + \alpha_{i_k})^2 + \mathcal{O}(\alpha^4/\gamma)$

- one can write the correlator as

$$\langle e^{i\beta_1 N(z_1)} e^{i\beta_2 N(z_2)} ... e^{i\beta_n N(z_n)} \rangle = \left| \exp\left\{ -\sum_{i,j}\alpha_i\alpha_j\left(\ln\frac{R}{\delta} + \ln\frac{\delta}{|z_{ij}|}(1 - \delta_{ij})\right)\right\}\right|^2$$

free fields

- the correlator is zero unless charge conservation holds:

$$\sum_i \alpha_i = \sum_{i,j} \alpha_i \alpha_j = 0 \qquad \left(\alpha = \beta/\sqrt{\pi\gamma} \right)$$

- If it does, the correlator becomes simply

$$\langle e^{i\sqrt{2}\alpha_1\phi(z_1)} e^{i\sqrt{2}\alpha_2\phi(z_2)} ... e^{i\sqrt{2}\alpha_n\phi(z_n)} \rangle = \prod_{i<j} \left| \frac{z_i - z_j}{\delta} \right|^{4\alpha_i\alpha_j}$$

This is the correlator of vertex operators of a free field with kinetic term $\phi\Box^{d/2}\phi$

central charge

given the partition function Z(R) of a 2-sphere of radius R, one can compute the central charge:
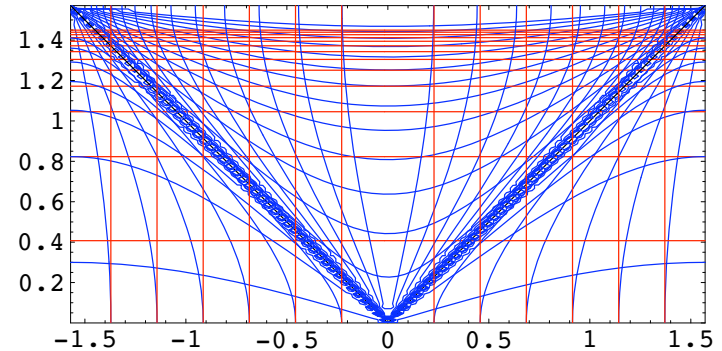
$$Z(R) = R^{c/3} Z_0$$

$$Z = \sum_{n=1}^{\infty} \frac{\gamma^n}{n!} \int d\Omega_2 \left(\int_{\epsilon}^{\pi-\epsilon} \frac{d\psi}{\sin^3 \psi} - \Lambda \right)$$

$$\ln Z = 4\pi\gamma \left(\frac{R^2}{\epsilon^2} - \ln \frac{\epsilon}{R} + \ln 2 - \frac{1}{6} - \Lambda R^2 + \mathcal{O}(\epsilon^2) \right)$$

$$\boxed{c = 12\pi\gamma}$$

eternal inflation?

- recall that the inside of a bubble is an open universe, and slices of constant density are hyperbolic 3-space

- Lorentz transformations around the point of nucleation are isometries, and an infinite boost moves a point to the boundary (which contains all the volume)

- It is often argued that inflation cannot be past eternal. Let's see what the effects of an initial condition surface are here
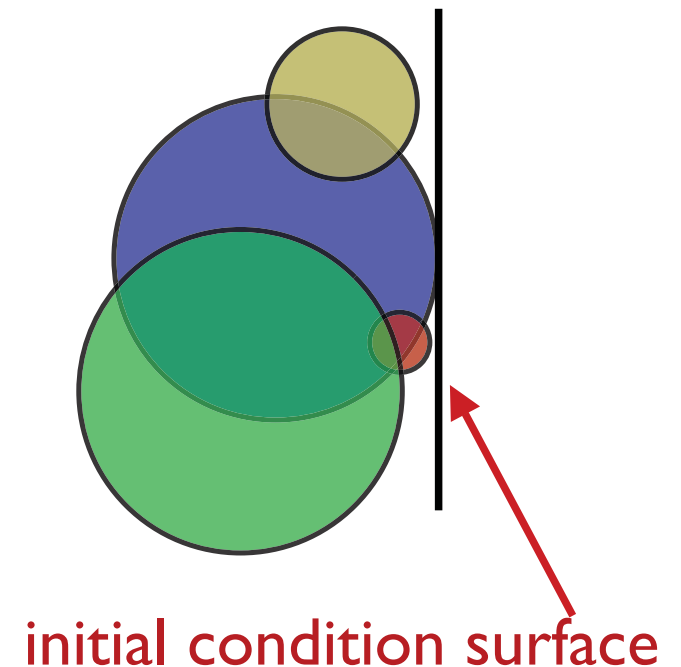
infinite boost

all initial conditions look the same after an infinite boost:

viewed from the side...   viewed from above...

false vacuum dS

initial condition surface
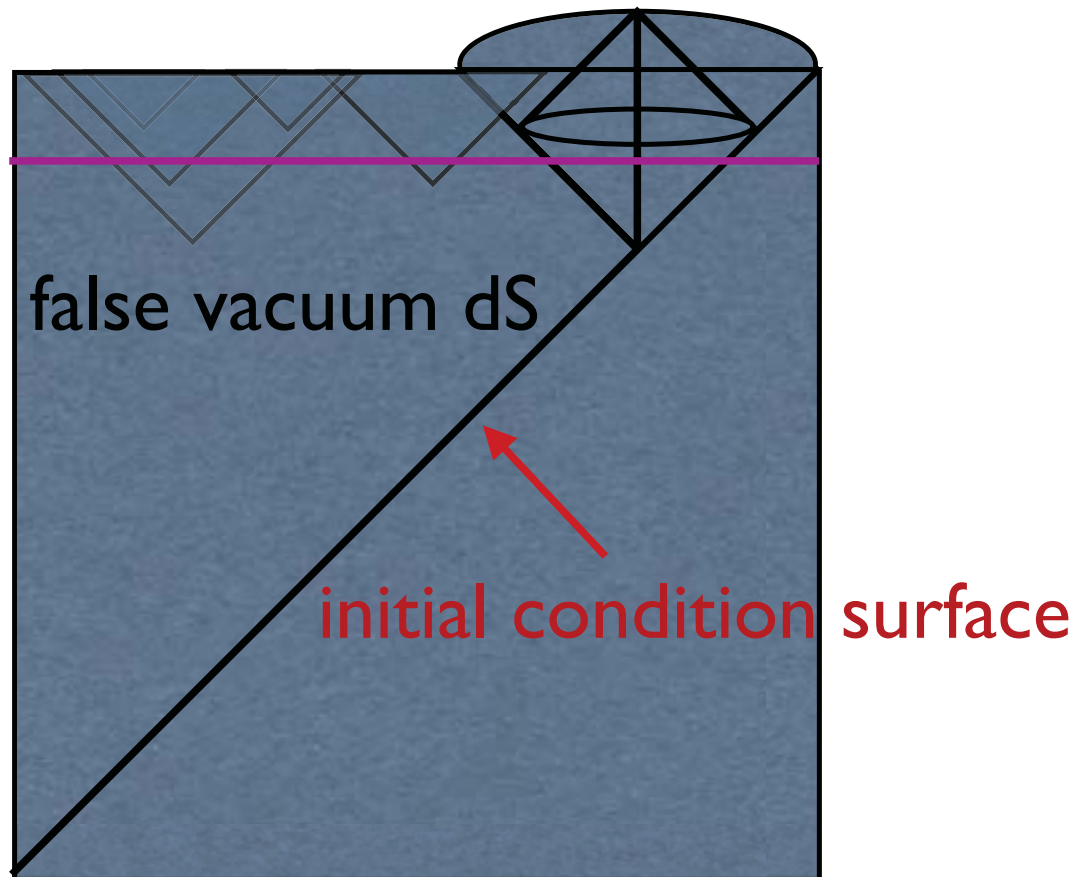
initial condition surface

preferred point

- in either sky or global slicing, the effect of an infinitely boosted initial condition surface is to pick a special point on the sphere which no disk can cover - the "persistence of memory"

- choosing this point to be Riemann infinity gives the distribution on the plane with no "inside out" disks

- no initial condition would mean there *can* be disks which cover infinity - but this has almost no effect on IR safe quantities such as these correlators

- therefore, it seems there is a true dS invariant (but fractal) equilibrium distribution which describes truly eternal (past and future) false-vacuum inflation

our world, today?

- can we actually see these collisions?

- first, there must be at least one collision in our past lightcone

- second, the collision's lightcone should bisect the part of the reheating/last scattering surface accessible to us to be easier to detect

- turns out the number of such collisions is

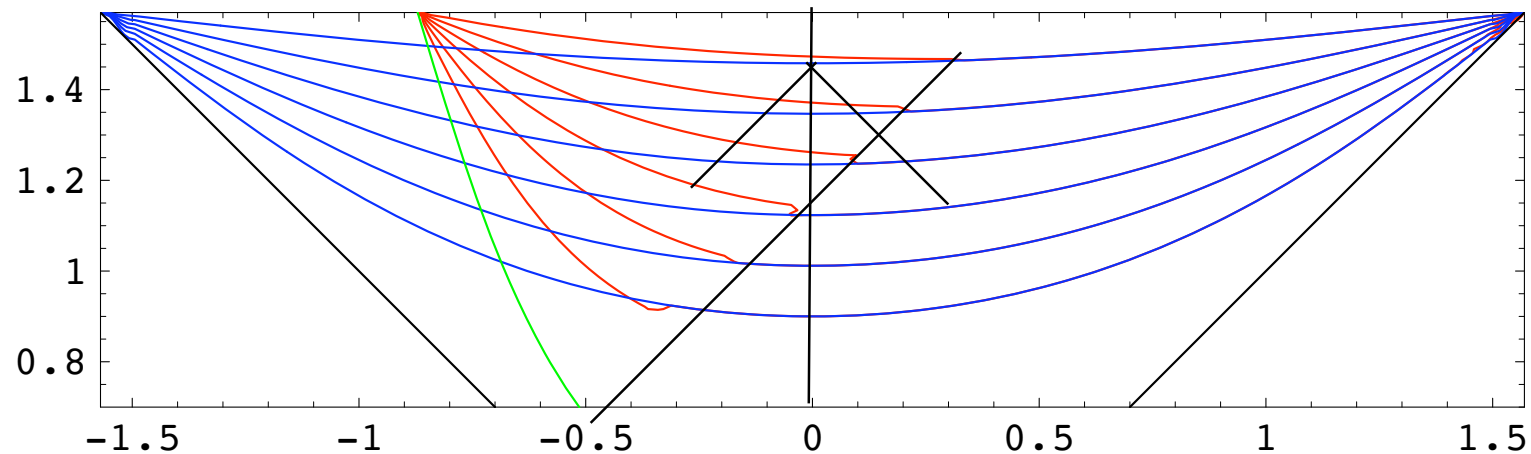$$N \sim \gamma \sqrt{\Omega_k(t)} (H_f^2 / H_i^2)$$

effects of one collision

- Observer C is oblivious to the collision

- Observer B will detect anisotropic redshifts in the CMB

- Observer A will detect the anisotropic redshifts and "see" the domain wall directly

- Might see radiation from collision itself, or from the other bubble.
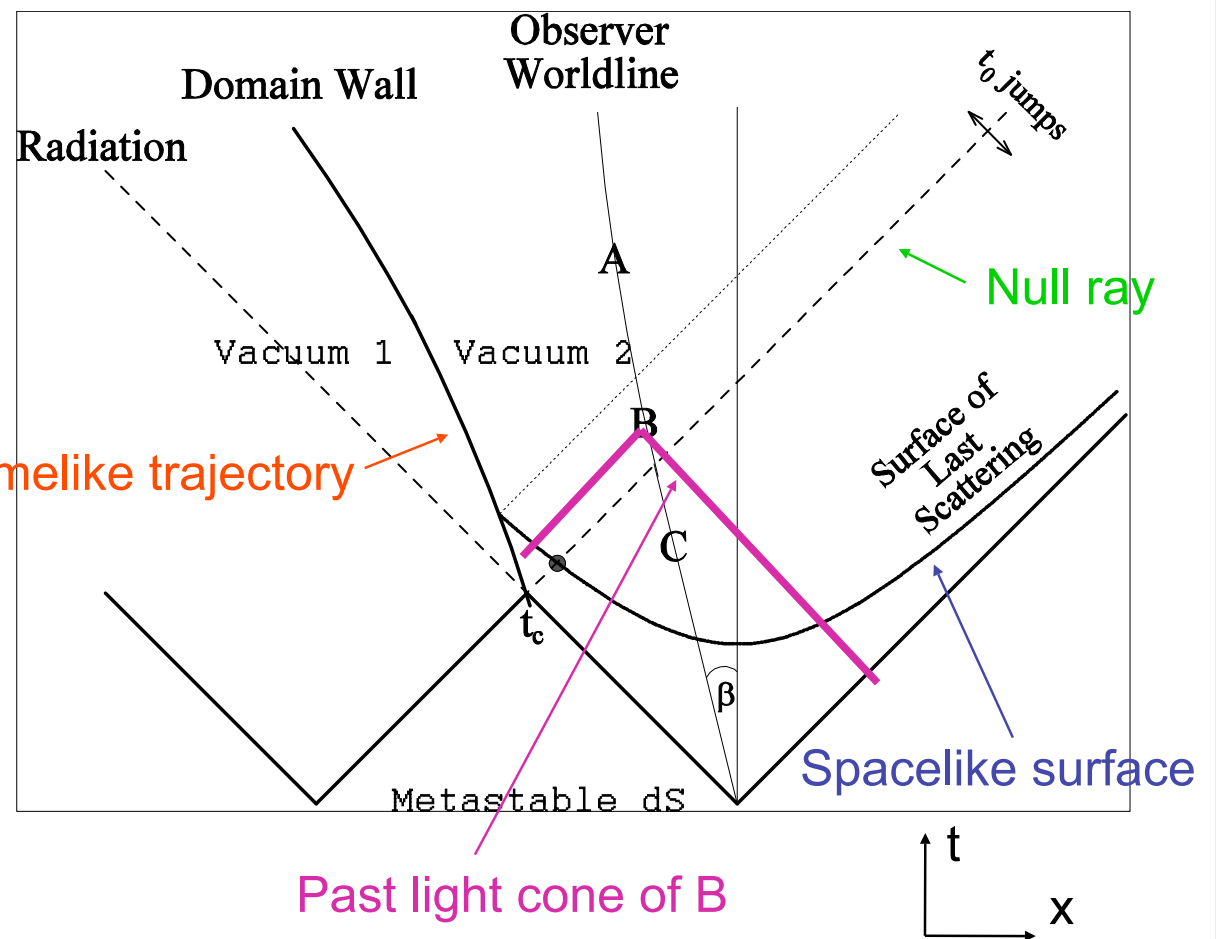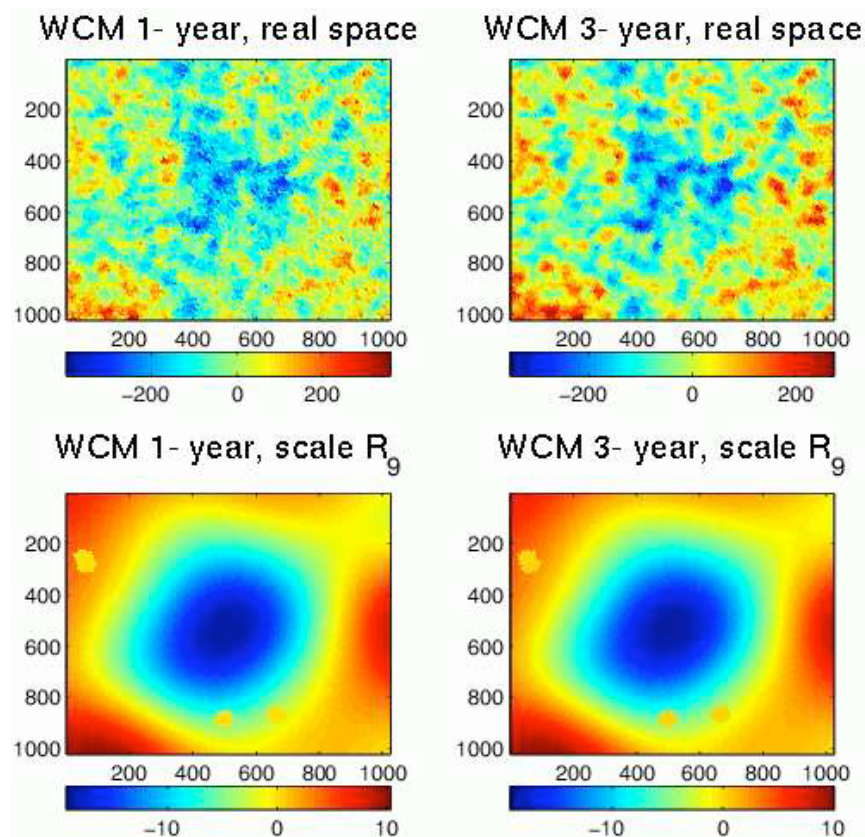

S. Chang, MK, T. Levi

Asymmetric redshifts

- Photons from different directions travel through different metrics, and originate from a perturbed reheating surface

- This leads to a differential redshift as a function of angle. Photons that last scatter inside the lightcone versus those outside divides the sky into two discs

- There is a preferred direction and dependence only on the angle towards it

  S. Chang, MK, T. Levi

- One can learn something about the physics of the other bubble from the sign and radial dependence of the temperature shift
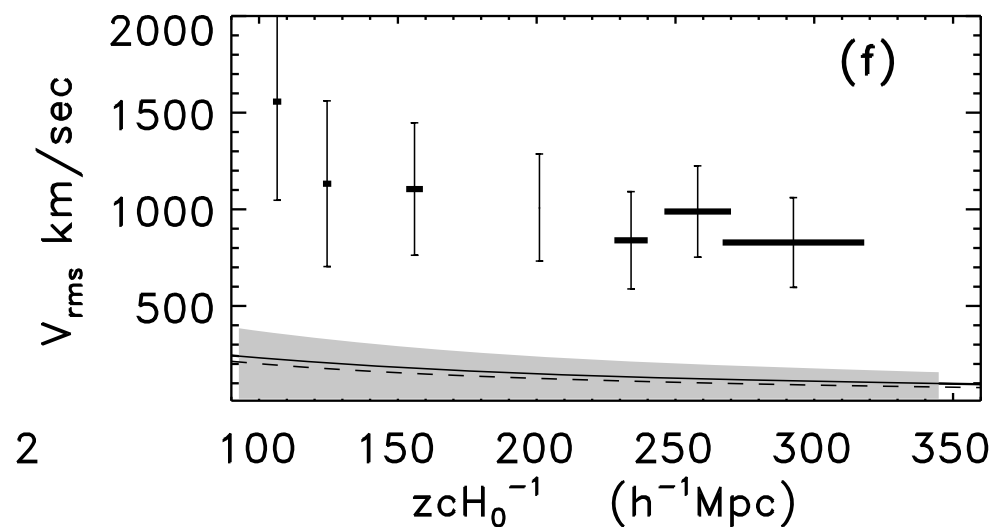
44

Some interesting anomalies...

WCM 1- year, real space

WCM 3- year, real space

WCM 1- year, scale R_9

WCM 3- year, scale R_9

(f)

V_{rms} km/sec

zcH_0^{-1} $(h^{-1}Mpc)$

From *The non-gaussian cold spot in the 3-year wmap data.*

M. Cruz, L. Cayon , E. Martinez-Gonzalez, P. Vielva, J. Jin

From *A measurement of large-scale peculiar velocities of clusters of galaxies: results and cosmological implications.*

A. Kashlinsky, F. Atrio-Barandela, D. Kocevski, H. Ebeling

Data search

- using the WMAP 5-year data set, we are currently writing code to search for the disk pattern in the CMB temperature map (with J. Bovy and O. Dore)

- results later...

- other possibilities in this line include polarization, "dark flow" type effects, and other variations in LSS (21 cm?)

end

- many of the conceptual difficulties with dS seem to be ameliorated by this formalism, which...

- defines (globally) conformally invariant correlation functions with positive definite conformal weights

- but the 4-pt function is bad - fixed by integrating over shape, interactions, gravity?

- has a Gaussian limit when the bulk decay rate is large

- central charge is proportional to the decay rate

- standard FT UV cutoff behavior, dual to bulk

- observable at least to census taker, maybe to us

- applications to percolation/condensed matter?