



**2046-14**

**Summer College on Nonequilibrium Physics from Classical to  
Quantum Low Dimensional Systems**

*6 - 24 July 2009*

**Does a bad metal become good superinsulator?**

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# Does a bad metal become good “superinsulator”?

Giant jumps in  $I$ - $V$  characteristics in 2D films  
(near a superconductor-insulator transition)

Boris Altshuler, Vladimir Kravtsov, I.L., Igor Aleiner



Columbia U., NY

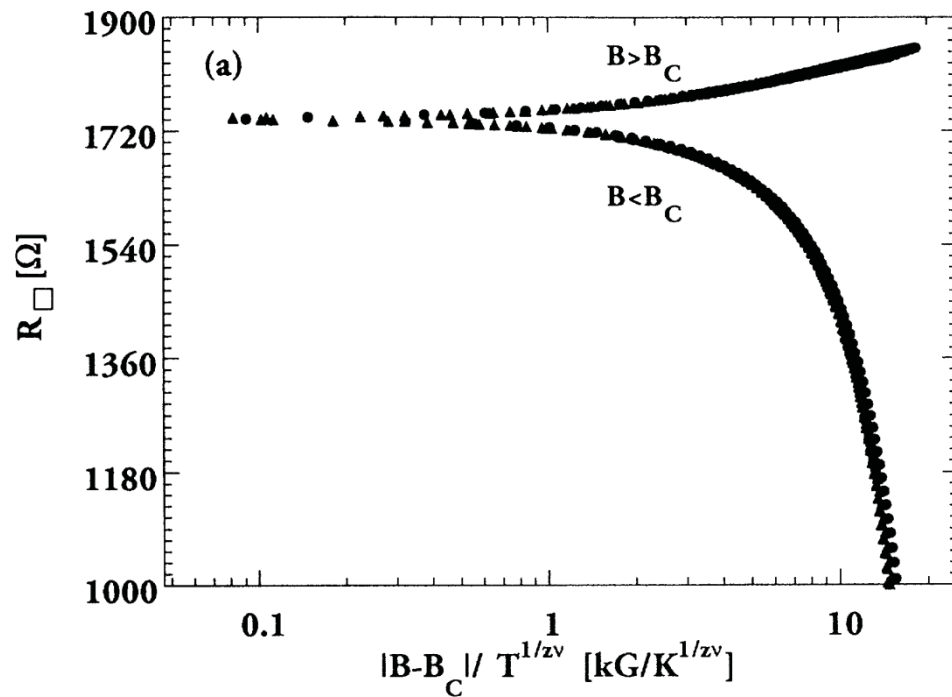


Columbia U., NY

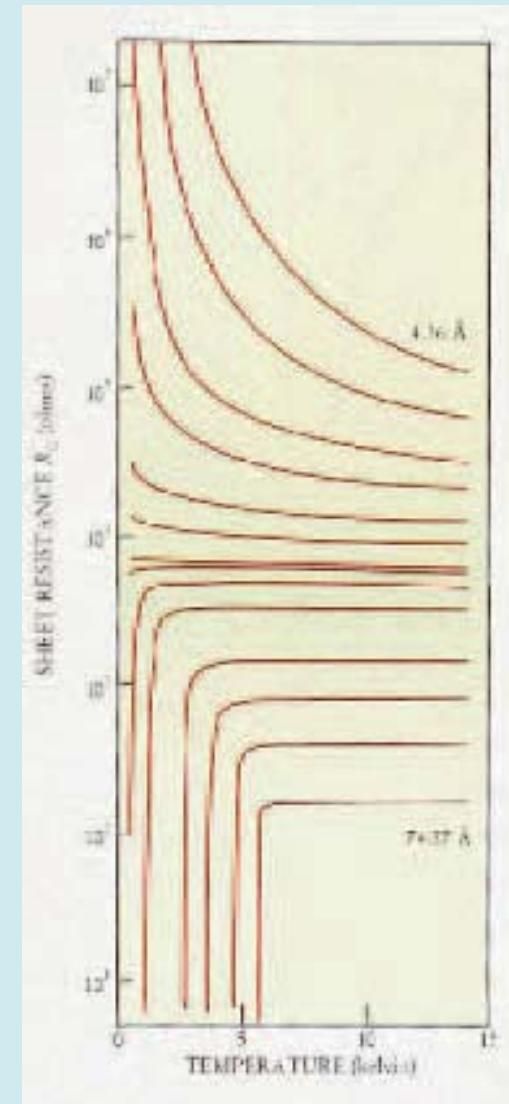
PRL, **102**, 176803 (2009)

(also Ovadia, Sacepe, Shahar, *ibid*, 176802)

# Superconductor-Insulator Transition



Goldman et al; Kapitulnik et al; Paalanen et al.,  
Hsu et al, Ovidiyahu et al, ..., 1989-till now

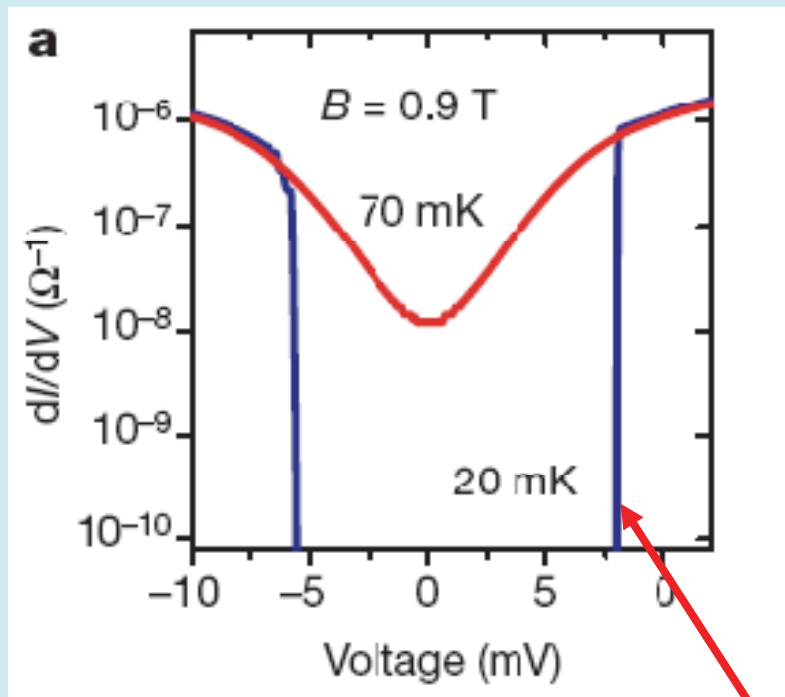


# Subject of the talk:

Highly unusual  
**nonlinear electronic transport**  
on the insulating side of SIT in  
disordered thin films of  
InO and TiN,  
and also in other materials

# Giant jumps in I-V characteristics

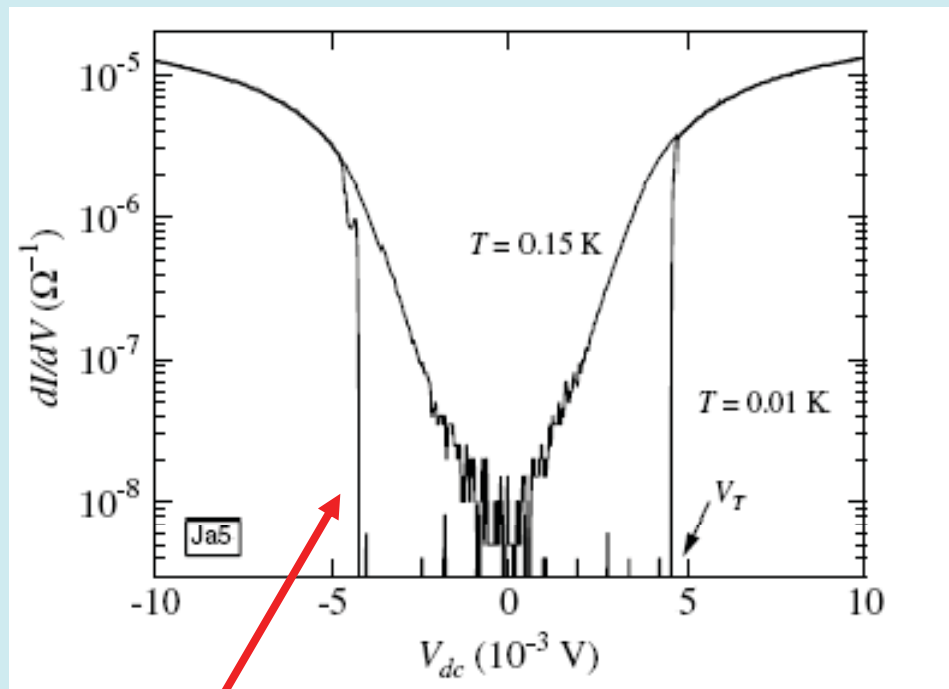
TiN films



Baturina, Mironov, Vinokur,  
Baklanov, Strunk, '07

Giant jumps in resistance  
from k $\Omega$  to G $\Omega$  regime

InO films



Sambandamurthy, Engel, Johansson,  
Peled, Shahar, '05

in systems tantalizingly  
close to superconductors

# From a superconductor to a **super**-insulator?

PRL 94, 017003 (2005)

PHYSICAL REVIEW LETTERS

week ending  
14 JANUARY 2005

## Experimental Evidence for a Collective Insulating State in Two-Dimensional Superconductors

G. Sambandamurthy,<sup>1</sup> L. W. Engel,<sup>2</sup> A. Johansson,<sup>1</sup> E. Peled,<sup>1</sup> and D. Shahar<sup>1</sup>

PRL 99, 257003 (2007)

PHYSICAL REVIEW LETTERS

week ending  
21 DECEMBER 2007

## Localized Superconductivity in the Quantum-Critical Region of the Disorder-Driven Superconductor-Insulator Transition in TiN Thin Films

T. I. Baturina,<sup>1,2</sup> A. Yu. Mironov,<sup>1,2</sup> V. M. Vinokur,<sup>3</sup> M. R. Baklanov,<sup>4</sup> and C. Strunk<sup>2</sup>

Vol 452 | 3 April 2008 | doi:10.1038/nature06837

nature

LETTERS

## Superinsulator and quantum synchronization

Valerii M. Vinokur<sup>1</sup>, Tatyana I. Baturina<sup>1,2,3</sup>, Mikhail V. Fistul<sup>4</sup>, Aleksey Yu. Mironov<sup>2,3</sup>, Mikhail R. Baklanov<sup>5</sup> & Christoph Strunk<sup>3</sup>

PRL 100, 086805 (2008)

PHYSICAL REVIEW LETTERS

week ending  
29 FEBRUARY 2008

## Collective Cooper-Pair Transport in the Insulating State of Josephson-Junction Arrays

M. V. Fistul,<sup>1</sup> V. M. Vinokur,<sup>2</sup> and T. I. Baturina<sup>3,2</sup>



# Is this resistance so **super** large?

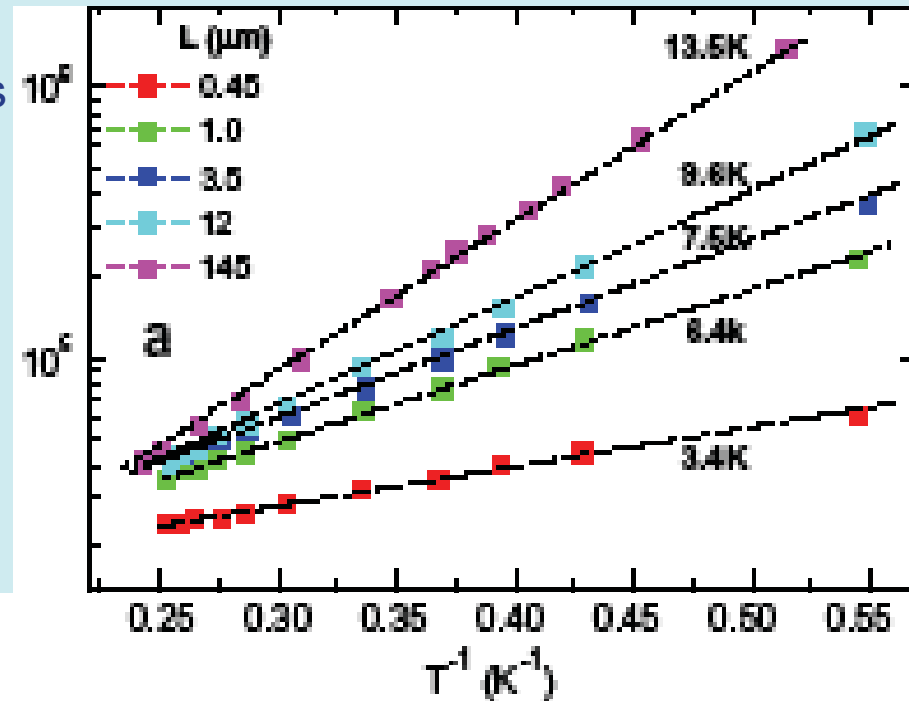
Linear regime: Arrhenius law at low  $T$  was observed in numerous experiments in InO amorphous films and elsewhere but is also **rather strange**

$$R(T) = R_0 e^{(\Delta/T)^\gamma}$$

$$\gamma \approx 1, \Delta \sim 1 \div 10 \text{ K}$$

One expects Mott's VRH,  $\gamma=1/(d+1)$ , or Efros-Shklovskii  $\gamma=1/2$

This was always considered as a puzzle and still doesn't have a fully satisfactory theoretical explanation



If we extrapolate this down to  $T \sim 100 \text{ mK}$ , then  $R \sim R_q e^{10} \sim 10^8 \Omega$ : one should **wonder why SMALL values of  $R$  were also observed in this range of  $T$ .**

# Is the closeness to superconducting transition so important?

PHYSICAL REVIEW B

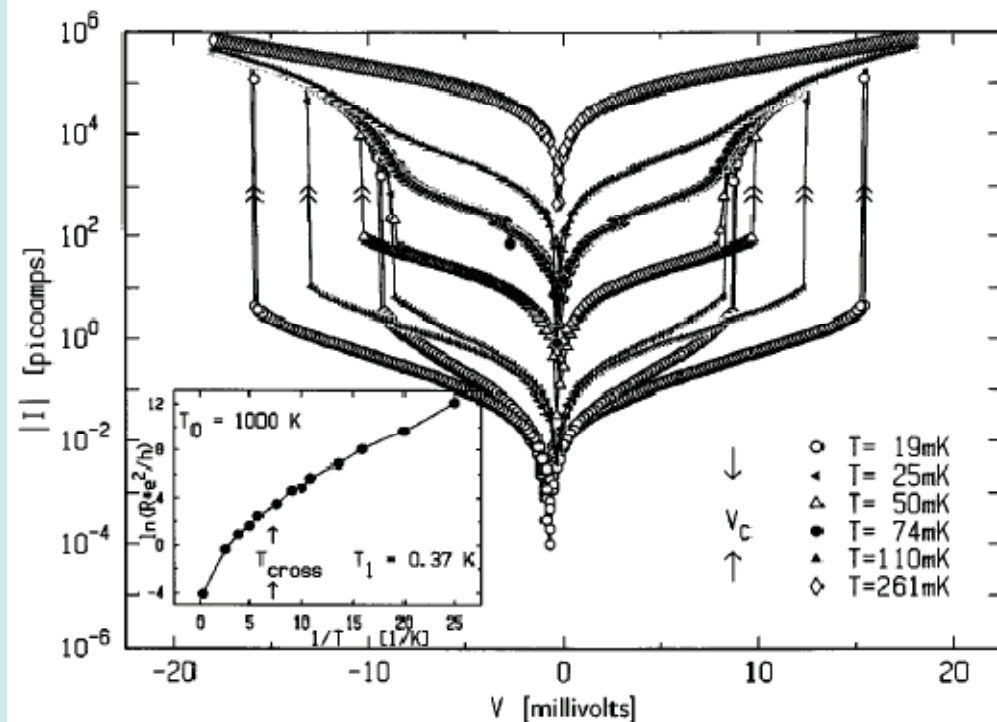
VOLUME 53, NUMBER 3

15 JANUARY 1996-I

## Depinning transition in Mott-Anderson insulators

F. Ladieu, M. Sanquer, and J. P. Bouchaud

A few orders in magnitude  
current jumps increasing  
with lowering temperature  
**not in the vicinity of the  
SIT transition**





# Something else?

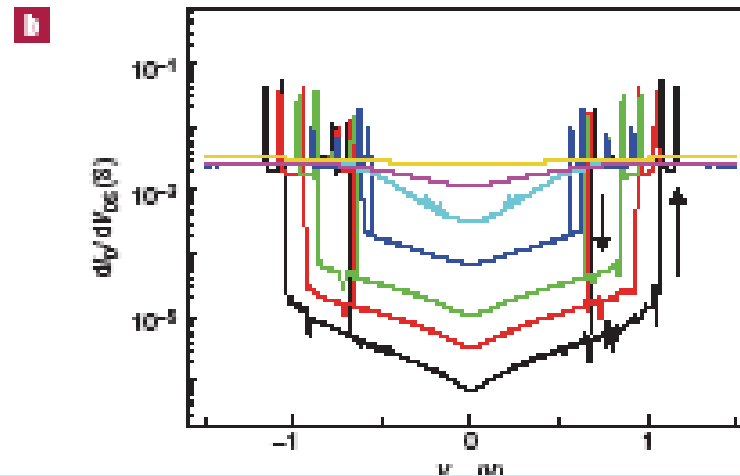
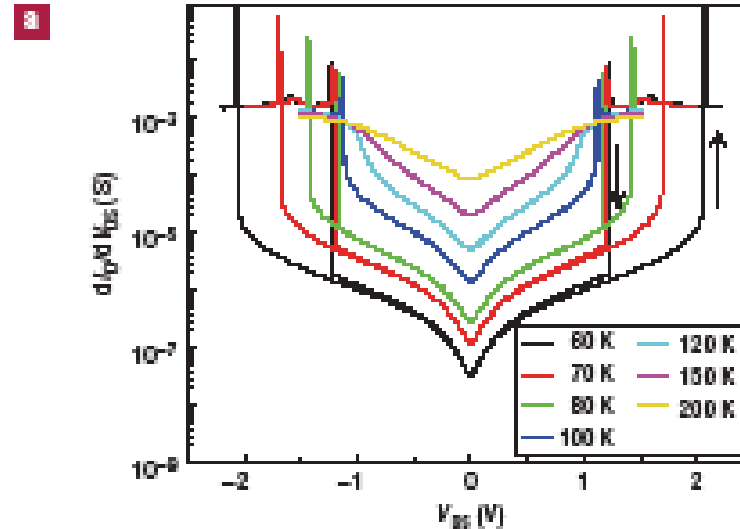
## LETTERS

### Electrically driven phase transition in magnetite nanostructures

SUNGBAE LEE<sup>1</sup>, ALEXANDRA FURSINA<sup>2</sup>, JOHN T. MAYO<sup>2</sup>, CAFER T. YAVUZ<sup>2</sup>, VICKI L. COLVIN<sup>2</sup>, R. G. SUMESH SOFIN<sup>3</sup>, IGOR V. SHVETS<sup>3</sup> AND DOUGLAS NATELSON<sup>1,4\*</sup>

**nature materials** | VOL 7 | FEBRUARY 2008 |

Magnetite ( $\text{Fe}_3\text{O}_4$ )  
nanostructures



# Common features

❑ Strong disorder:  $R_0 \sim R_q \equiv \frac{2h}{e^2} \sim 50\kappa\Omega$  in low- $R$  state

❑ Arrhenius law for linear ( $V \rightarrow 0$ ) resistance at low  $T$  - *pseudo-gap*

$$R(T) = R_0 e^{\Delta/T}$$

❑ VRH ( $\gamma \leq 1/2$ ) is not observed at low  $T$  – no electron-phonon thermalization?

~~$$R(T) \propto e^{(\Delta/T)^\gamma}$$~~

❑ Voltage threshold  $eV$  (at which jumps occurs) increases with increasing  $\Delta$  much faster than  $\Delta$  itself

# Phenomenological explanation?

No single microscopic approach can possibly explain so similar behaviour in so different systems...

**Our main idea: bi-stability due to (over)heating is the main cause of giant resistance jumps**

Not normally expected for hopping conductivity in the insulating regime – in contrast to the metallic one...

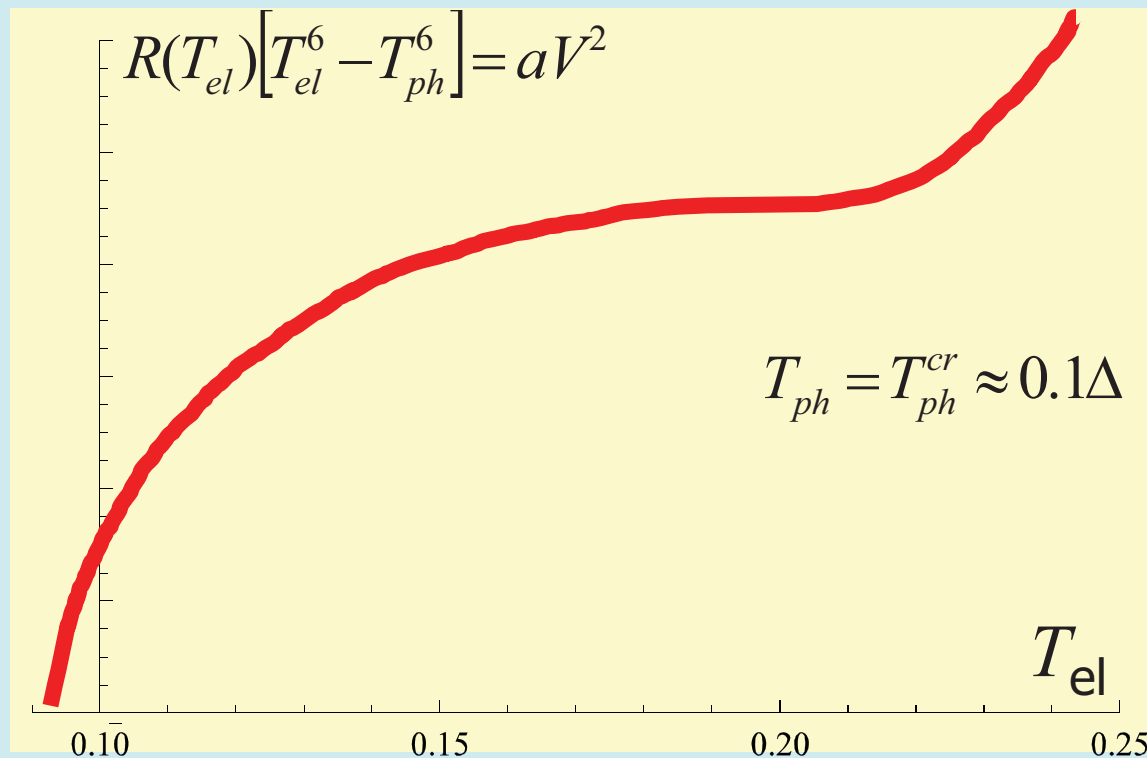
# Stepping Stones

- ❖ Electron-electron interaction is strong enough: electrons are mutually thermalized with  $T_{\text{el}}$
- ❖ Cooling is mainly due to electron-phonon interaction which is, however, inefficient: electrons can be joule-heated to temperature  $T_{\text{el}} > T_{\text{bath}} \equiv T_{\text{ph}}$
- ❖ Linear (Ohmic)  $R(T)$  has steep (Arrhenius-like)  $T$ -dependence which remains valid at a finite voltage with  $T \rightarrow T_{\text{el}}$
- ❖  $T_{\text{el}}$  should be found from the balance of Joule heating (by electric field) and phonon cooling

# Bi-stability in a nutshell

Heat balance:

$$\frac{V^2}{R(T_{\text{el}})} = \frac{\mathcal{E}(T_{\text{el}})}{\tau_{\text{e-ph}}(T_{\text{el}})} - \frac{\mathcal{E}(T_{\text{ph}})}{\tau_{\text{e-ph}}(T_{\text{ph}})} \propto T_{\text{el}}^\beta - T_{\text{ph}}^\beta$$

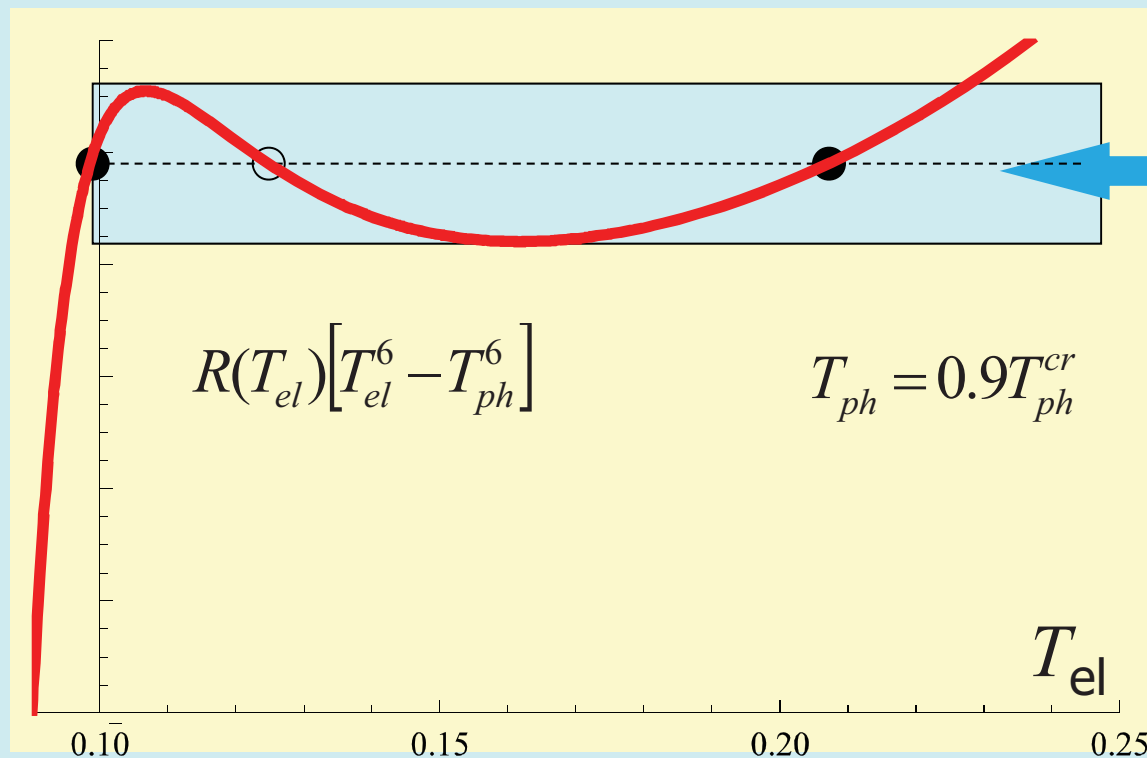


For each voltage there is a unique  $T_{\text{el}}$  provided that  $T_{\text{ph}} < T^{\text{cr}} \approx 0.1\Delta$

# Bi-stability in a nutshell

Heat balance:

$$\frac{V^2}{R(T_{\text{el}})} = \frac{\mathcal{E}(T_{\text{el}})}{\tau_{\text{e-ph}}(T_{\text{el}})} - \frac{\mathcal{E}(T_{\text{ph}})}{\tau_{\text{e-ph}}(T_{\text{ph}})} \propto T_{\text{el}}^\beta - T_{\text{ph}}^\beta$$



**Bi-  
stable  
region**

Two stable  
electron  
temperatures  
at the same  
voltage

# Suppression of cooling by disorder

$$\frac{\hbar}{\tau_{\text{e-ph}}} = \frac{T^3}{T_D^2}$$

electron-phonon scattering rate in a clean metal:

$T_D$  – Debye temperature;

assumed that  $p_F \sim \hbar/a$  (dense metal)

$$\frac{\hbar}{\tau_{\text{e-ph}}} = n^* \frac{T^3}{T_D^2}$$

in a clean semiconductor with  $p_F \ll \hbar/a$

$n^*$  = # of electrons per unit cell

Energy relaxation (cooling) from the kinetic equation:

$$\frac{\dot{\mathcal{E}}}{\mathcal{V}} = \nu_0 \int \varepsilon \dot{f}(\varepsilon, T_{\text{el}}) d\varepsilon \sim \frac{T_{\text{el}}^2}{\tau_{\text{e-ph}}(T_{\text{el}})} - \frac{T_{\text{ph}}^2}{\tau_{\text{e-ph}}(T_{\text{ph}})} \propto T_{\text{el}}^5 - T_{\text{ph}}^5$$

$$\frac{\hbar}{\tau_{\text{e-ph}}} \sim n^* \underbrace{\frac{q_T \ell}{\hbar}}_{\sim 10^{-4} \text{ in InO and TiN}} \frac{T^3}{T_D^2} \propto T^4$$

$\sim 10^{-4}$  in InO and TiN

Dirty-metal (or low T) limit:

$$q_T \ell / \hbar \ll 1 \quad \Leftrightarrow \quad T \ell \ll \hbar v_s$$

$\ell$  – electron mean free path

$v_s$  – transverse sound velocity

$q_T$  – thermal phonon momentum

# Disorder-independent heat balance

Substituting the exact solution of the kinetic equation in the model results in the disorder-independent equation for heat balance in proper dimensionless variables:

$$\frac{V^2}{R} = \frac{d\mathcal{E}}{dt} \quad \mapsto \quad v^2 e^{-1/t_{\text{el}}} = t_{\text{el}}^6 - t_{\text{ph}}^6,$$

$$t \equiv \frac{T}{\Delta}, \quad v \equiv \frac{V}{V_0},$$

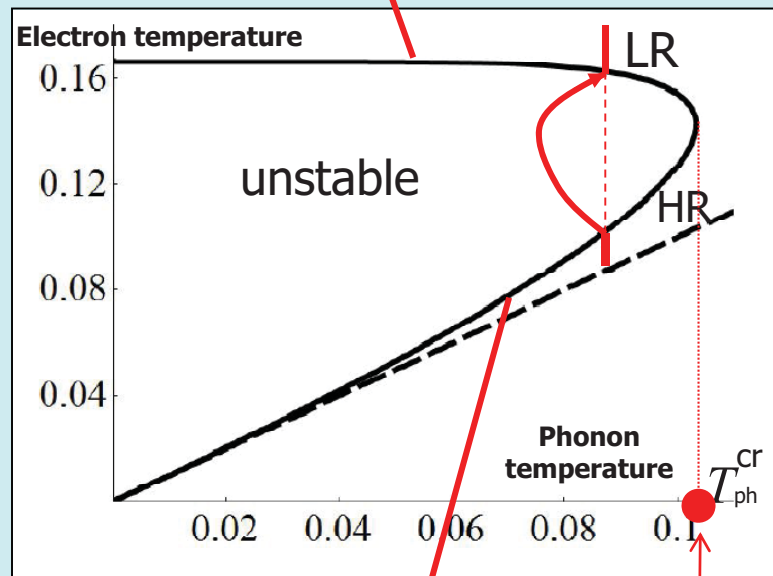
$$\frac{eV_0}{L} \equiv \frac{\alpha k_F \Delta^3}{\Delta_0^2}, \quad \Delta_0 \equiv (\rho v_s^5 \hbar^3)^{1/4}, \quad \alpha \equiv \frac{2\pi^2}{\sqrt{315}} \approx 1.1$$

Heat balance depends ONLY on electron density ( $k_F$ ), the Arrhenius pseudo-gap  $\Delta$  and the 'material' energy  $\Delta_0$



# Critical temperature and voltage

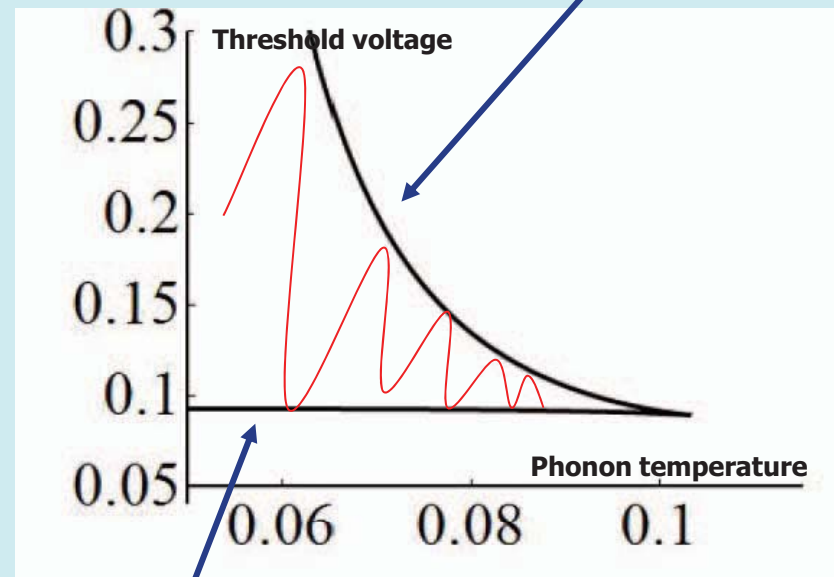
Minimal temperature of the hot (LR) state is  $0.14 \Delta$



Maximal temperature of the cold (HR) state is close to the bath temperature

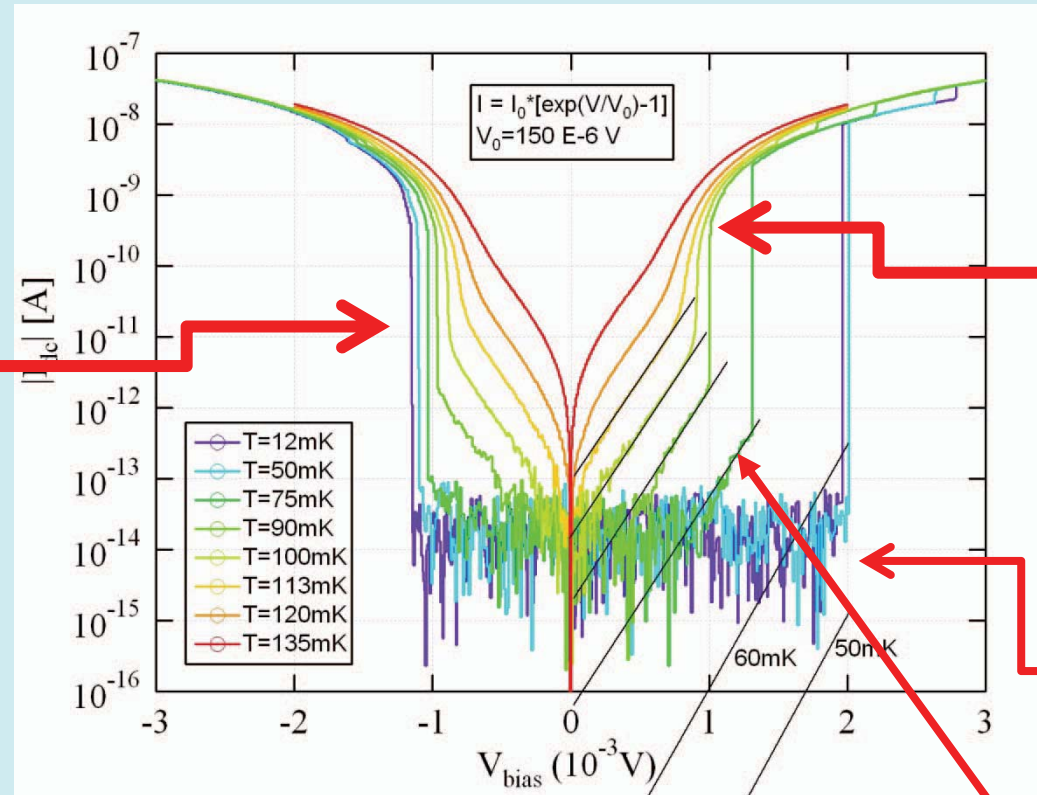
Critical bath temperature  $T_{ph}^{cr}$  depends only on  $\Delta$

Threshold voltage of the cold (HR) state is strongly  $T$ -dependent



Threshold voltage for the hot (LR) state is almost independent of  $T_{bath}$

# Compare to the newest data



Threshold voltage for the hot (LR) state is almost independent of  $T_{\text{bath}}$

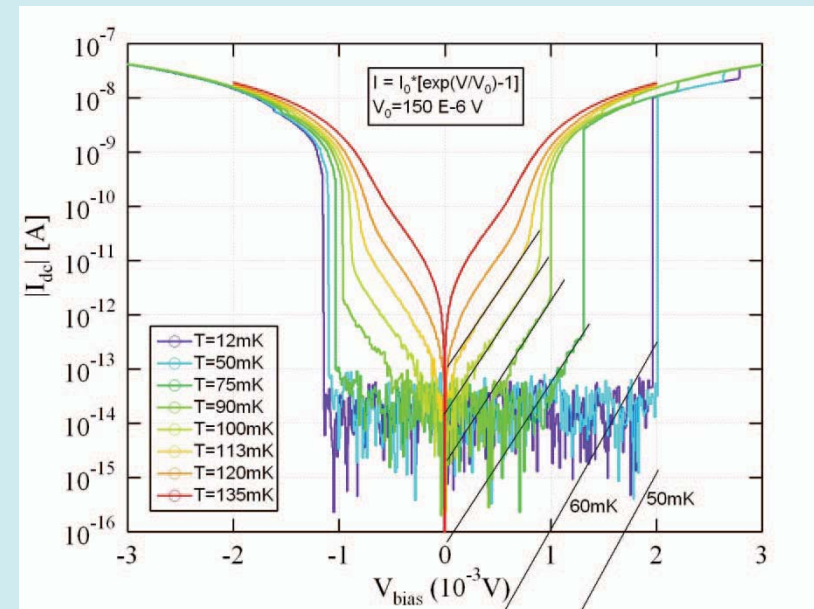
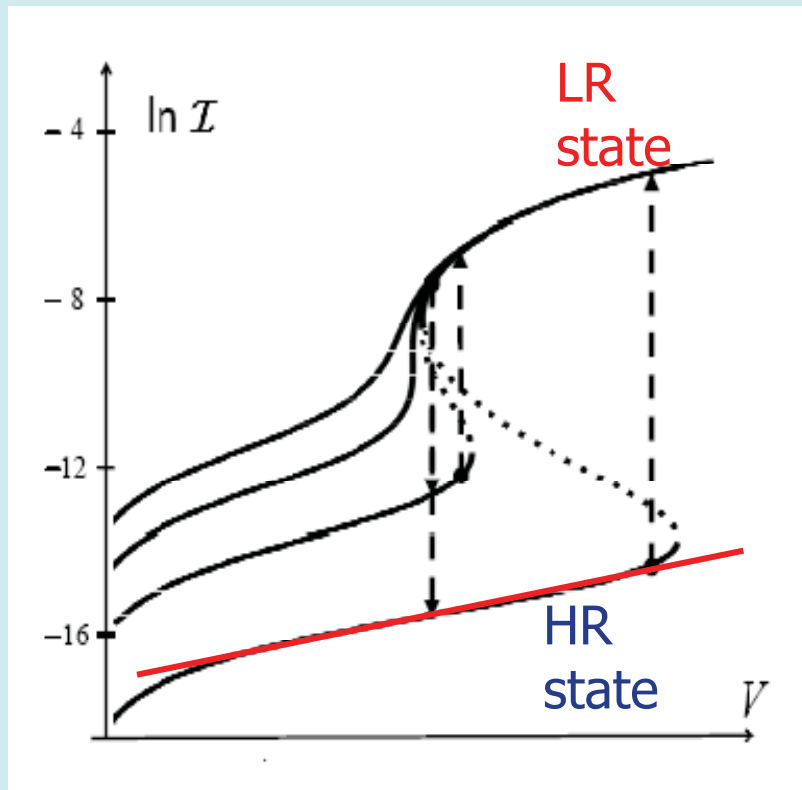
Threshold voltage of the cold (HR) state is strongly  $T$ -dependent

Higher  $R$  are unmeasurable due to noise

Non-zero almost exponential conductance: the insulator is not ideal

M.Ovadia, B.Sacepe,  
D.Shahar,  
InO film (PRL,'09)

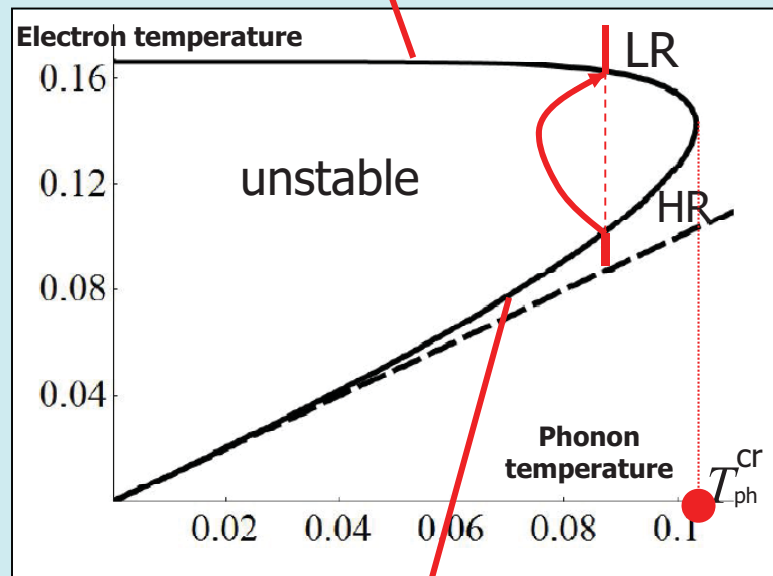
# Nonlinear I-V characteristics



- ❖ Current jumps of several orders of magnitude
- ❖ Wide range of almost exp behavior in the HR state

# Bistability temperature

Minimal temperature of the hot (LR) state is  $0.14 \Delta$



Maximal temperature of the cold (HR) state is close to the bath temperature

Experimental bistability diagram (Ovadia, Sasepe, Shahar, 2009)

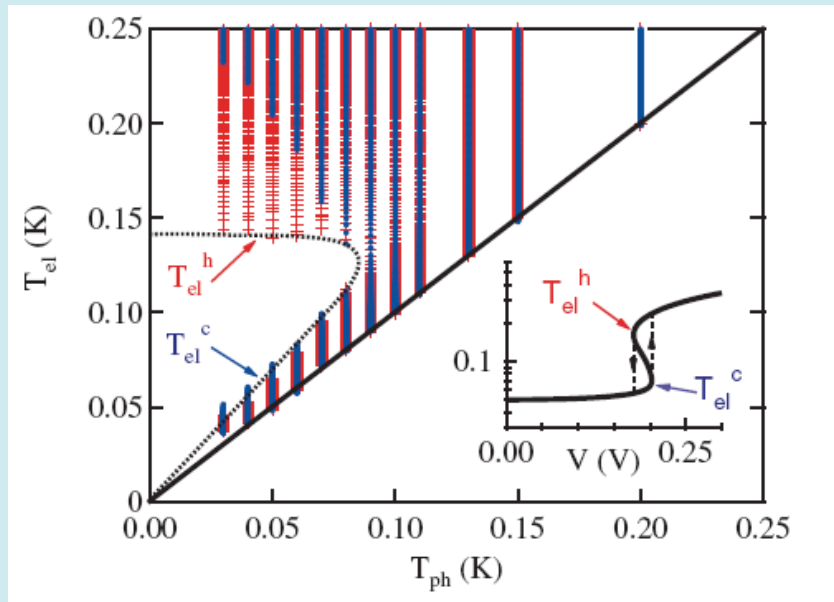


FIG. 3 (color online).  $T_{el}$  versus  $T_{ph}$ , showing the excluded region of temperatures which appears below  $T_{ph} = 0.1$  K, and the accompanying hysteresis. Blue (dark gray) circles correspond to data measured while increasing  $|V|$  and red (gray) crosses represent data taken while decreasing  $|V|$ . Inset:

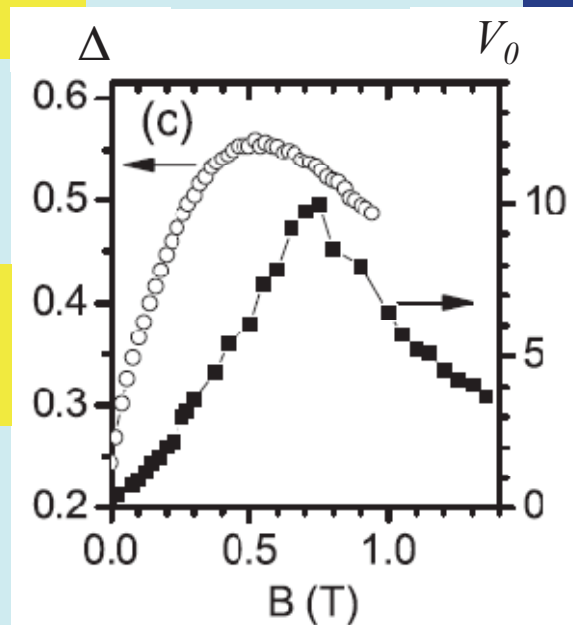
# Quantitative comparison

$$\frac{eV_{\text{hot}}^{\text{cr}}}{L} \equiv \frac{0.1k_{\text{F}}\Delta^3}{\Delta_0^2}, \quad T_{\text{ph}}^{\text{cr}} = 0.1\Delta, \quad \Delta_0 \equiv (\rho v_{\text{s}}^5 \hbar^3)^{1/4}$$

Theoretical estimates:  
 $V=0.8$  mV &  $T_{\text{ph}}^{\text{cr}}=190$ mK  
for  $\Delta=1.9$ K

Experimental data:  
 $V=1.0$  mV &  $T_{\text{ph}}^{\text{cr}}=120$ mK  
for  $\Delta=1.9$ K

Reasonable agreement in  
a wider range of  $\Delta$  for TiN



Baturina et al, 2007

# Beyond Arrhenius and $\tau_{\text{e-ph}}$

$$R(T) = R_0 \exp [(\Delta/T)^\gamma], \quad \frac{V^2}{R(T_{\text{el}})} \propto T_{\text{el}}^\beta - T_{\text{ph}}^\beta$$

Critical phonon temperature  $t_{\text{ph}}^{\text{cr}} = T_{\text{ph}}^{\text{cr}}/\Delta$

$$t_{\text{ph}}^{\text{cr}} = (1 + \beta/\gamma)^{-\frac{\beta+\gamma}{\gamma\beta}} = \begin{cases} 0.1 & \gamma = 1, \beta = 6 \\ 0.004 & \gamma = \frac{1}{2}, \beta = 6 \\ 1.5 \cdot 10^{-6} & \gamma = \frac{1}{4}, \beta = 6 \end{cases}$$

Scaling of the  
threshold voltage:

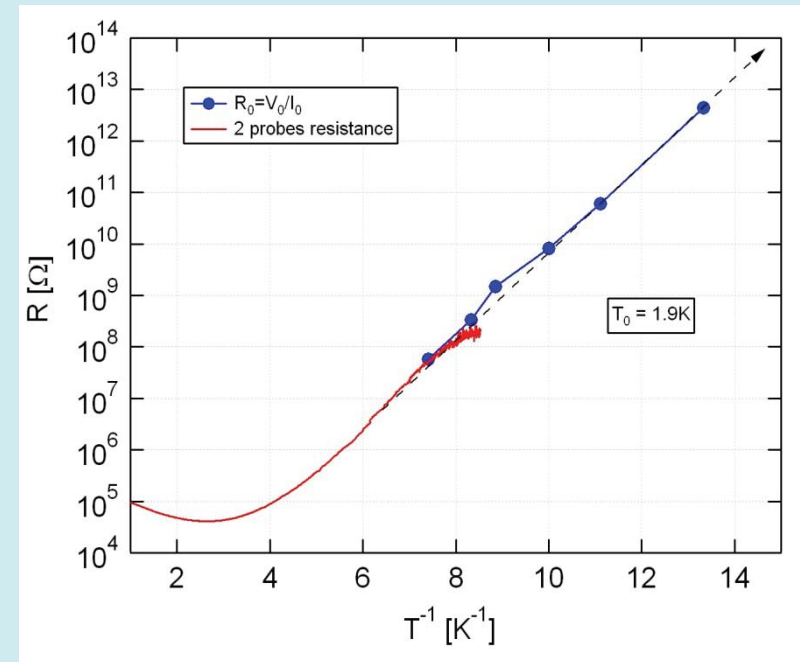
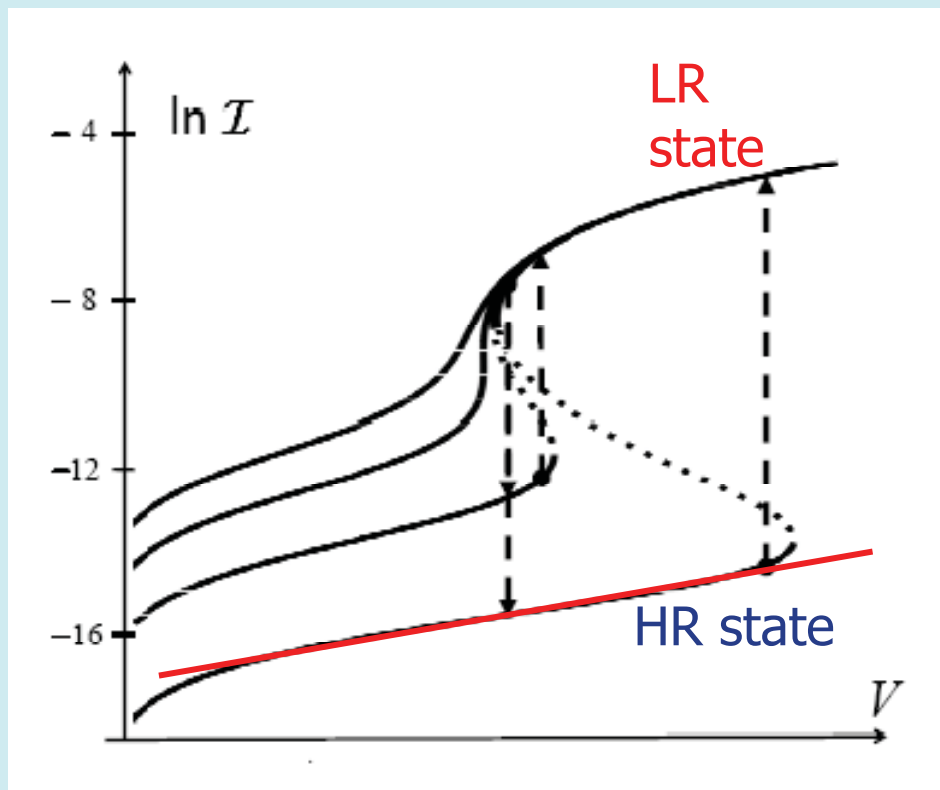
$$V_{\text{LH}}/\Delta^\beta = f(T_{\text{ph}}/\Delta).$$



# Not all experimental features captured

What is not quantitatively good:  $I_{\max}/I_{\min} < e$  in the HR state;

Experimentally this ratio is  $10 \div 20$ ; cannot be cured by any  $\gamma$  or  $\beta$



$$\ln \frac{I}{I_0} = \frac{V}{V_0}, \quad \frac{V_0}{I_0} \approx 2R_0$$

# Kapitza resistance?

- *A priori*, it is possible that a disordered film is overheated with respect to a substrate due to **Kapitza resistance** caused by acoustic or diffusive mismatch of phonons in the film and in the bulk

$$\frac{V^2}{R(T_{\text{el}})} = \frac{\Omega(T_{\text{el}}) - \Omega(T_{\text{ph}})}{\tau_K}, \quad \Omega \simeq \frac{\mathcal{V}T^3}{\hbar^3 v_s^3} \times \max\left(T, \frac{\hbar v_s}{d}\right), \quad \tau_K = \frac{d}{v_s D}$$

- However, this would give wrong (compared to experiment) T-dependence, no dependence on magnetic field, and requires the boundary transparency  $D$  to be unrealistically low:  $D < 10^{-5}$ , whereas

$$D = \frac{4Z_1 Z_2}{(Z_1 + Z_2)^2} > 10^{-2} \quad \text{even for artificially mismatched solids}$$

( $Z = v_s \rho$  is the acoustic impedance)



# Is e-ph overheating too mundane?

- ❑ Not usually happens on the insulating side, i.e. at  $R \ll h/e^2$
- ❑ Never was looked after as it is in contradiction to the picture of phonon-assisted hopping
- ❑ “Checked for” and vigorously denied in YSi and magnetite
- ❑ Signals new physics and requires a new approach to electron-assisted hopping at low  $T$

# Summary

- Electrons overheating due to inefficient cooling and the resulting current bistability leads to giant current jumps
- Good qualitative agreement with experiment without fitting parameters
- A microscopic description of hopping electron transport in the absence of thermalization with phonons is wanted
- Good super-insulator? – this particular hypothesis is not required for explaining experimental data...