



*The Abdus Salam
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2047-1

Workshop Towards the Neutrino Technologies

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Overview of neutrino masses and mixings

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Overview of ν masses and mixings (circa 2009)

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Mainly based on the following papers (+ comments on TAUP'2009 updates):
G.L. Fogli et al., 0805.2517, 0806.2649, 0808.0807, 0810.5733, 0905.3549

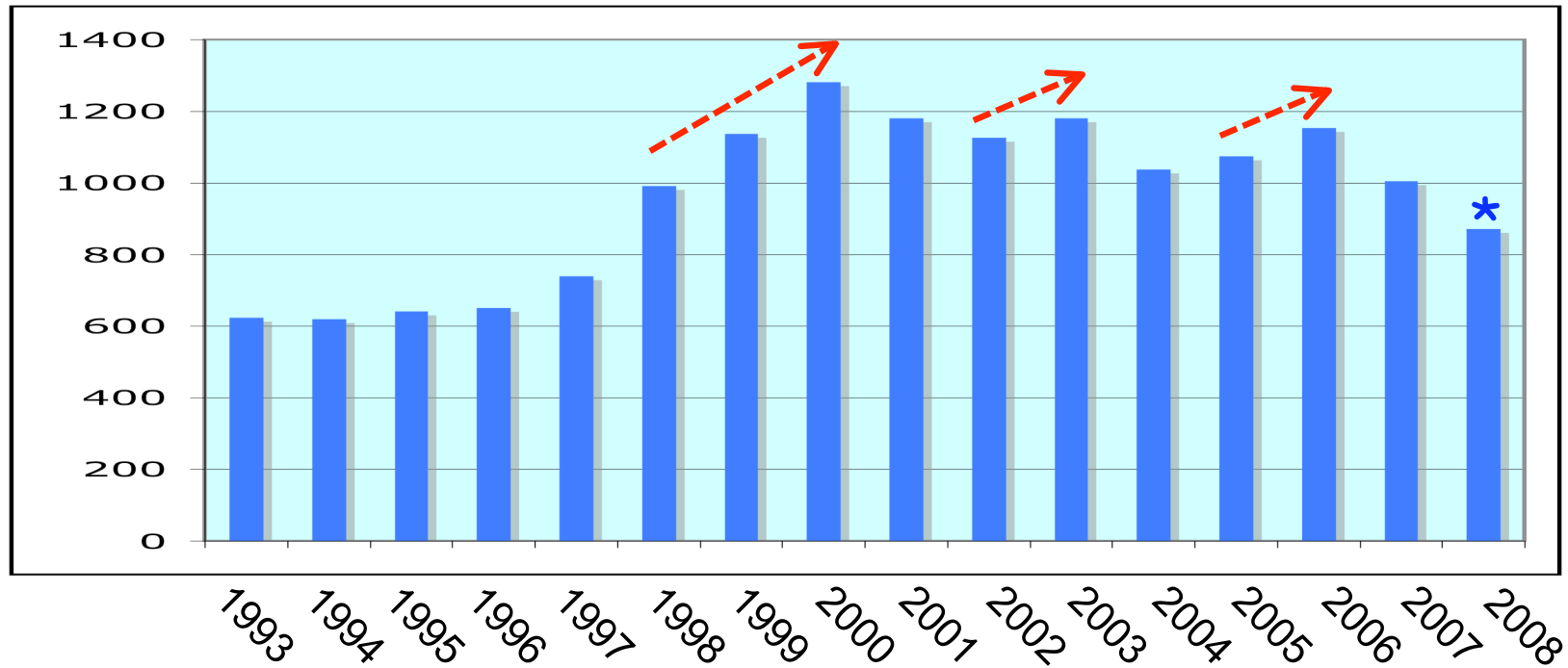
Interest in ν physics remains very high, with about 10^3 papers/year titled "...neutrino(s)..." on SPIRES

Peaks of interest:

Atmospheric ν oscillations,
Limit from
CHOOZ

Solar and reactor ν oscillations,
Nobel 2002 to
Davis & Koshiba

Accelerator ν oscillations,
Cosmological limits
on absolute masses



* Apparent drop in 2008 is not really a sign of decline (SPIRES counts saturate only after >1 year).

Unsuspected "technological interest" even in PIRELLI (the same of tires and calendars...)

I learned about a "PIRELLI \vee telecommunication project" from a 2004 article in PANORAMA (a weekly Italian magazine). Two PIRELLI researchers were trying to reproduce the old J.Weber's claim of solar \vee detection via coherent scattering on sapphire crystals, using his original equipment. I was asked to provide an opinion (negative!). No recent news about PIRELLI developments ...

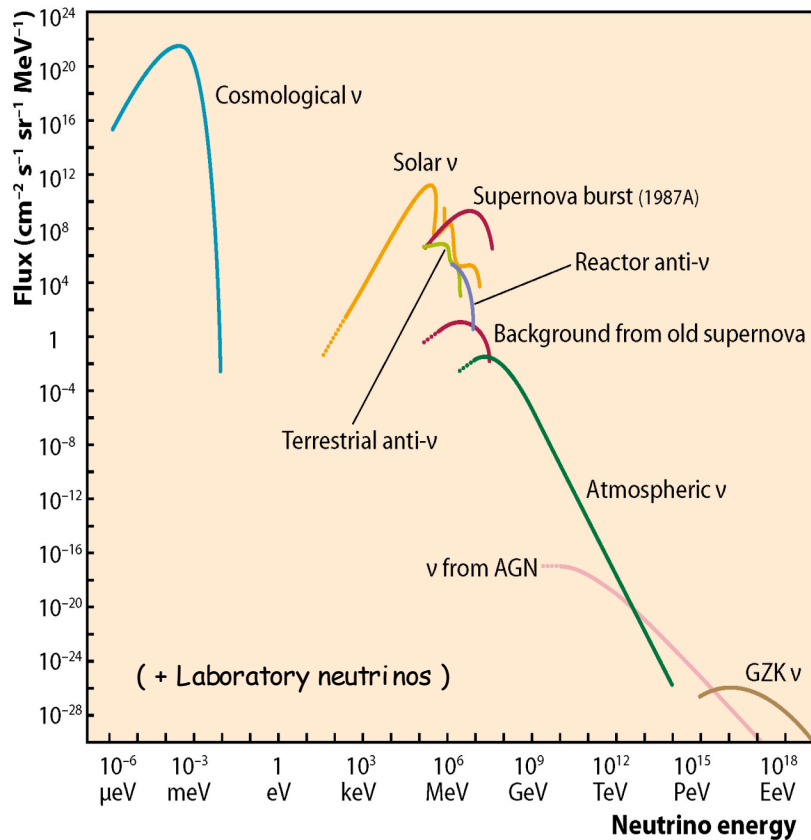


PANORAMA popular article, 2004



Neutrino researchers at
PIRELLI-lab (Milan, Italy)

But, of course, we all expect many exciting developments in neutrino science, and possibly, in neutrino technology



A synoptic view of neutrino fluxes. (from ASPERA roadmap)

Likely/possible “peaks of interest” in future years:

- Flavor appearance ($\nu_\mu \rightarrow \nu_\tau$, $\nu_\mu \rightarrow \nu_e$)
- Mixing between 1st-3rd family
- Mass spectrum hierarchy
- Absolute masses
- Spinorial nature (Majorana/Dirac)
- Leptonic CP violation
- Earth/Astro/Cosmo sources
- Possible new states/interactions
- Links with other LFV processes
- Theoretical “illumination”
- “Real” technological applications...

Solid starting point: the 3v mixing paradigm

3 eigenstates of mass, flavor: $(\nu_e, \nu_\mu, \nu_\tau)^T = U (\nu_1, \nu_2, \nu_3)^T$

Unitary matrix U_{PMNS} : 3 Euler rotation angles + 1 CP phase

Conventionally (and usefully), same rotation ordering as in U_{CKM} :

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$s_{23}^2 \sim 0.5$$

$$s_{13}^2 < \text{few } \%$$

$$s_{12}^2 \sim 0.3$$

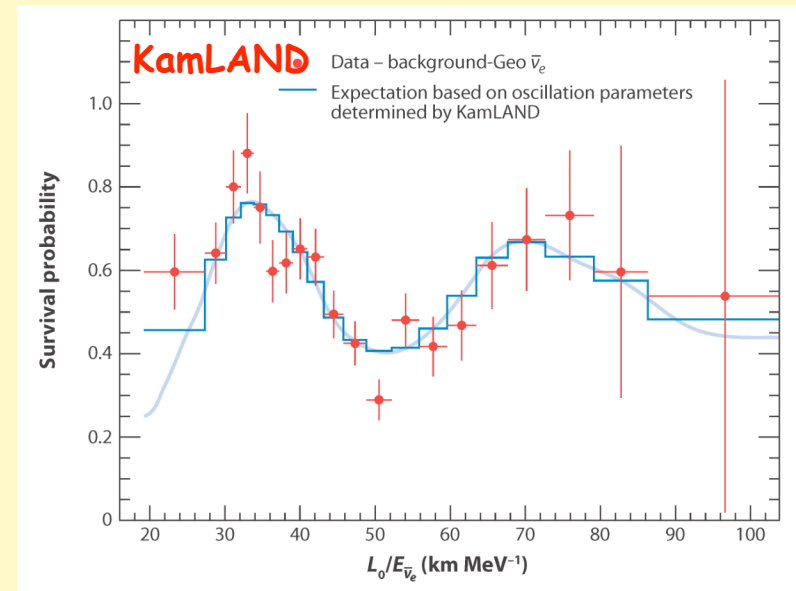
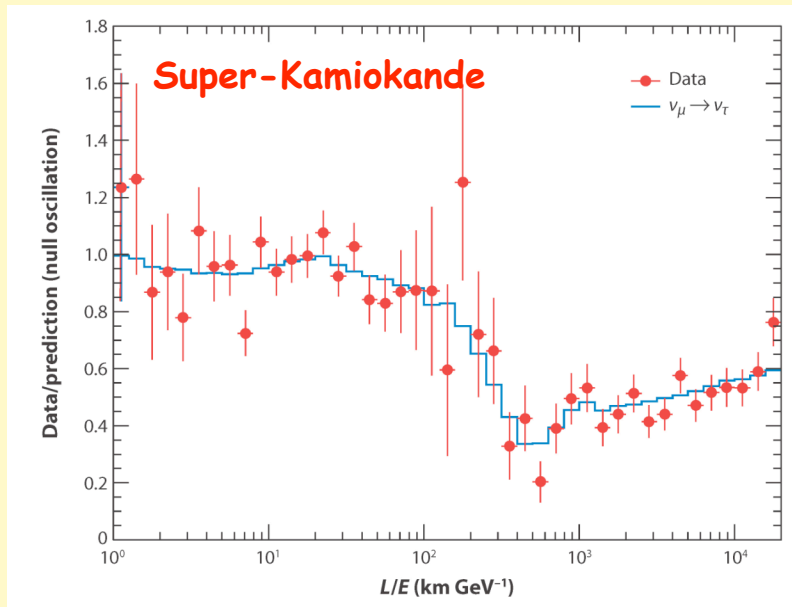
Measured by atmospheric
and accelerator
 ν experiments

Mainly constrained by
reactor experiments
(CHOOZ, PaloVerde)

Measured by
solar ν experiments
& by KamLAND

Two vacuum oscillation frequencies:

"Vacuum" phase $\sim (m_i^2 - m_j^2)L_{\text{length}}/E_{\text{energy}}$



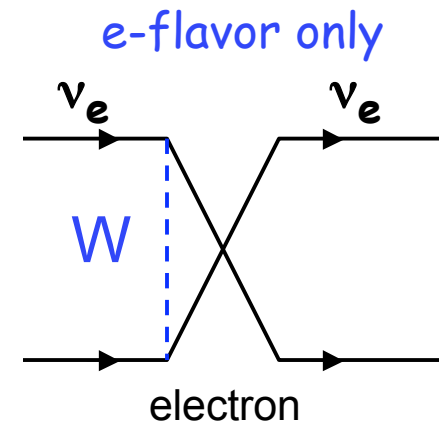
$$\Delta m^2 = m_3^2 - m_{1,2}^2 \gg$$

(ν from atmosphere, long-baseline accelerator, short-baseline reactors)

$$\delta m^2 = m_2^2 - m_1^2$$

(ν from long-baseline reactors, solar ν with corrections)

Evidence for matter effects :

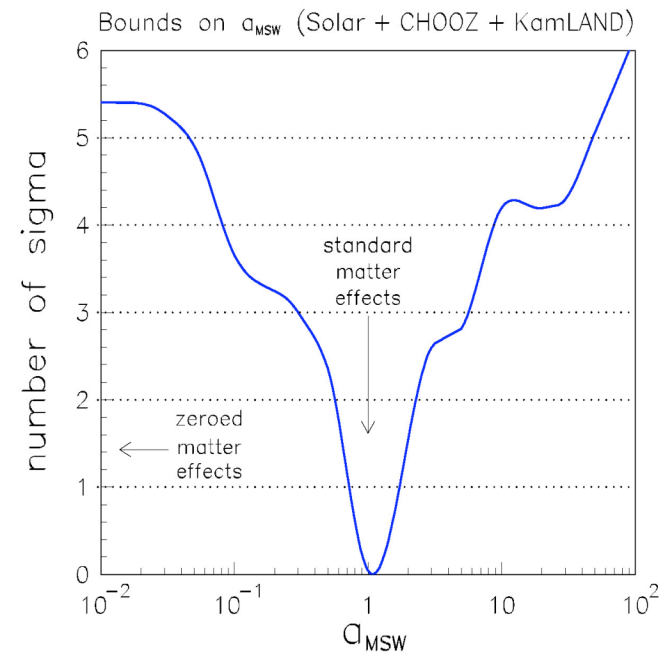
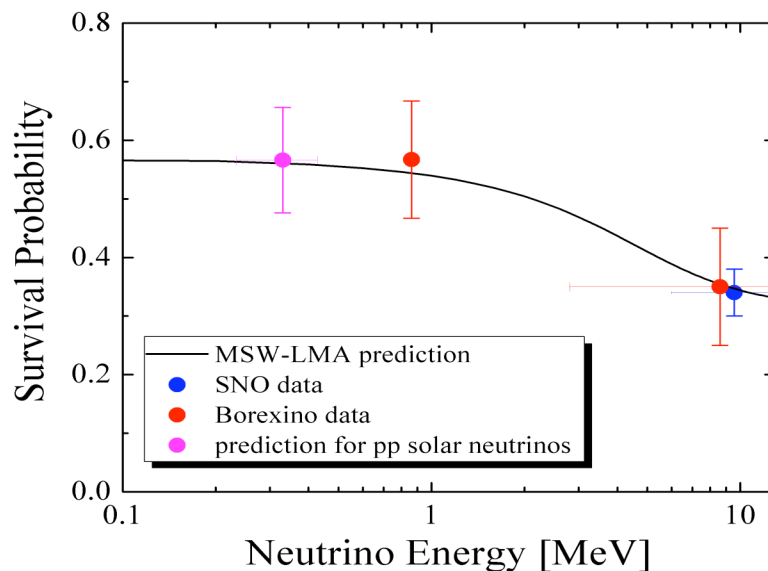


“Matter” contribution to phase (MSW effect):

$$\sim G_F \times \text{Solar electron density}$$

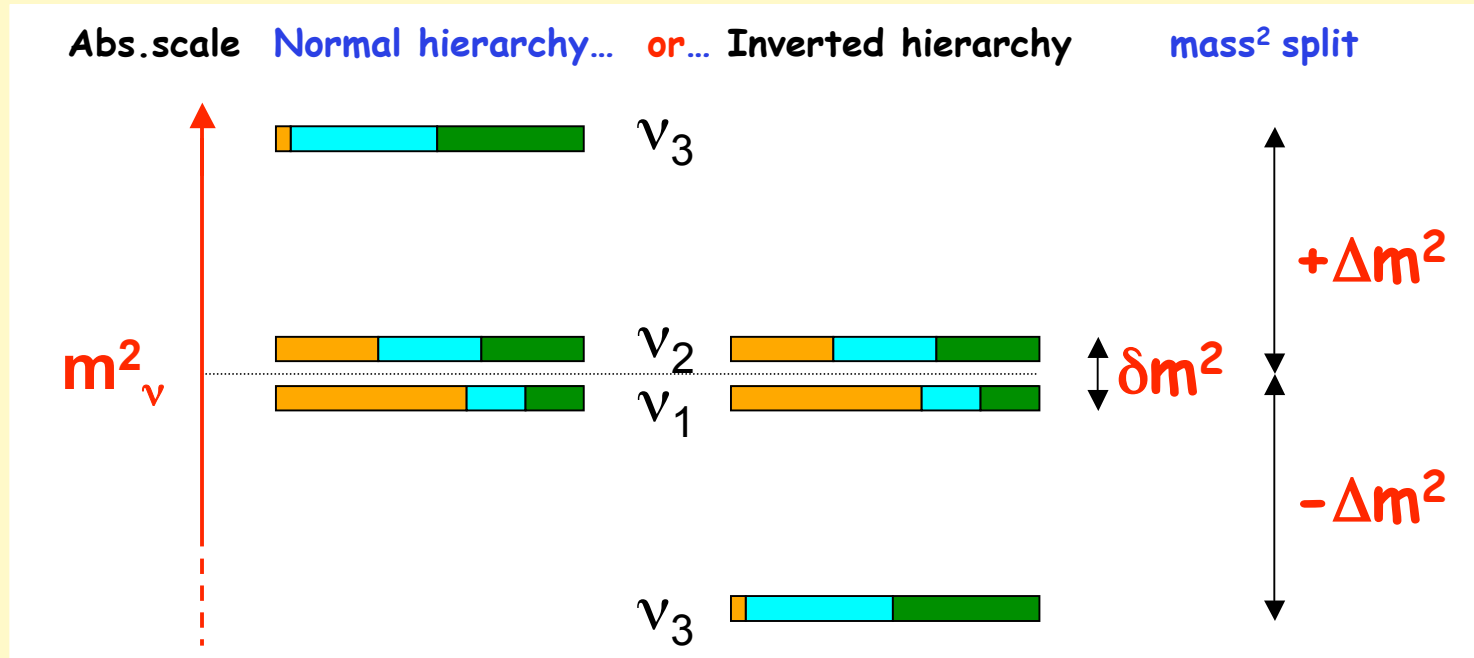
(but: averaged over many oscillation cycles)

Effect observed in a single expt., **Borexino**... ...in agreement with previous evidence



Current summary - if one needs just one significant digit...

(Useful for a global overview. Flavors = $e \mu \tau$)



$$\delta m^2 \sim 8 \times 10^{-5} \text{ eV}^2$$

$$\Delta m^2 \sim 3 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{12} \sim 0.3$$

$$\sin^2 \theta_{23} \sim 0.5$$

$$m_\nu < O(1) \text{ eV}$$

$$\sin^2 \theta_{13} < \text{few}\%$$

$$\text{sign}(\pm \Delta m^2) \text{ unknown}$$

$$\delta \text{ (CP) unknown}$$

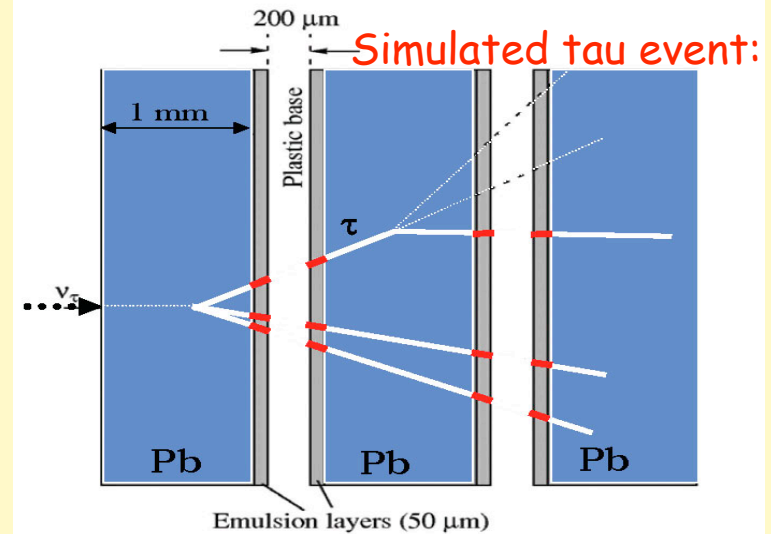
More significant digits ("precision physics"):

Always useful (fundamental parameters)
and needed for both experimental and theoretical reasons.

An experimental example: Δm^2 impact for CNGS physics



Two real tau events
might already be hidden
in the current statistics
collected by OPERA...



Expected tau production rate proport. to $(\Delta m^2)^2$.

Currently: Δm^2 uncertainty lower than 5-year statistical error

A theoretical example: accuracy of θ_{ij} for model building

Mixing angles seem to have some "special" values:

$$\sin^2\theta_{23} \approx 1/2$$

$$\sin^2\theta_{12} \approx 1/3 \quad \text{"tri-bimaximal mixing"}$$

$$\sin^2\theta_{13} \approx 0$$

A signal of discrete symmetries in the neutrino sector?

$$\theta_{12} + \theta_c \approx \pi/4 \quad \text{"quark-lepton complementarity"}$$

$$[\theta_{23} + \theta_{23,q} \approx \pi/4]$$

A possible link between neutrino and quark mixing?

Model diagnostic: dependent on the above " \approx "

Oscillation parameters: state of the art (overview)

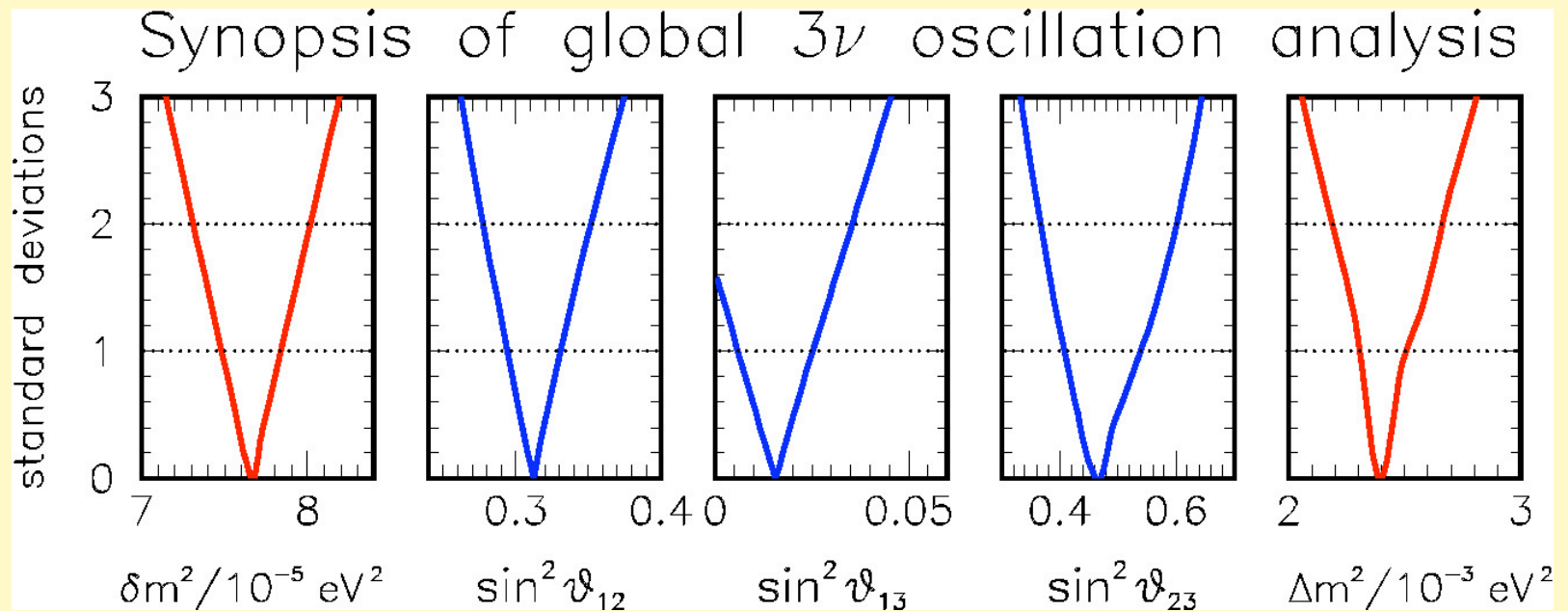


TABLE I: Global 3ν oscillation analysis (2008): best-fit values and allowed n_σ ranges for the mass-mixing parameters.

Parameter	$\delta m^2 / 10^{-5} \text{ eV}^2$	$\sin^2 \theta_{12}$	$\sin^2 \theta_{13}$	$\sin^2 \theta_{23}$	$\Delta m^2 / 10^{-3} \text{ eV}^2$
Best fit	7.67	0.312	0.016	0.466	2.39
1σ range	7.48 – 7.83	0.294 – 0.331	0.006 – 0.026	0.408 – 0.539	2.31 – 2.50
2σ range	7.31 – 8.01	0.278 – 0.352	< 0.036	0.366 – 0.602	2.19 – 2.66
3σ range	7.14 – 8.19	0.263 – 0.375	< 0.046	0.331 – 0.644	2.06 – 2.81

Oscillation parameters: state of the art, sector (1,2)

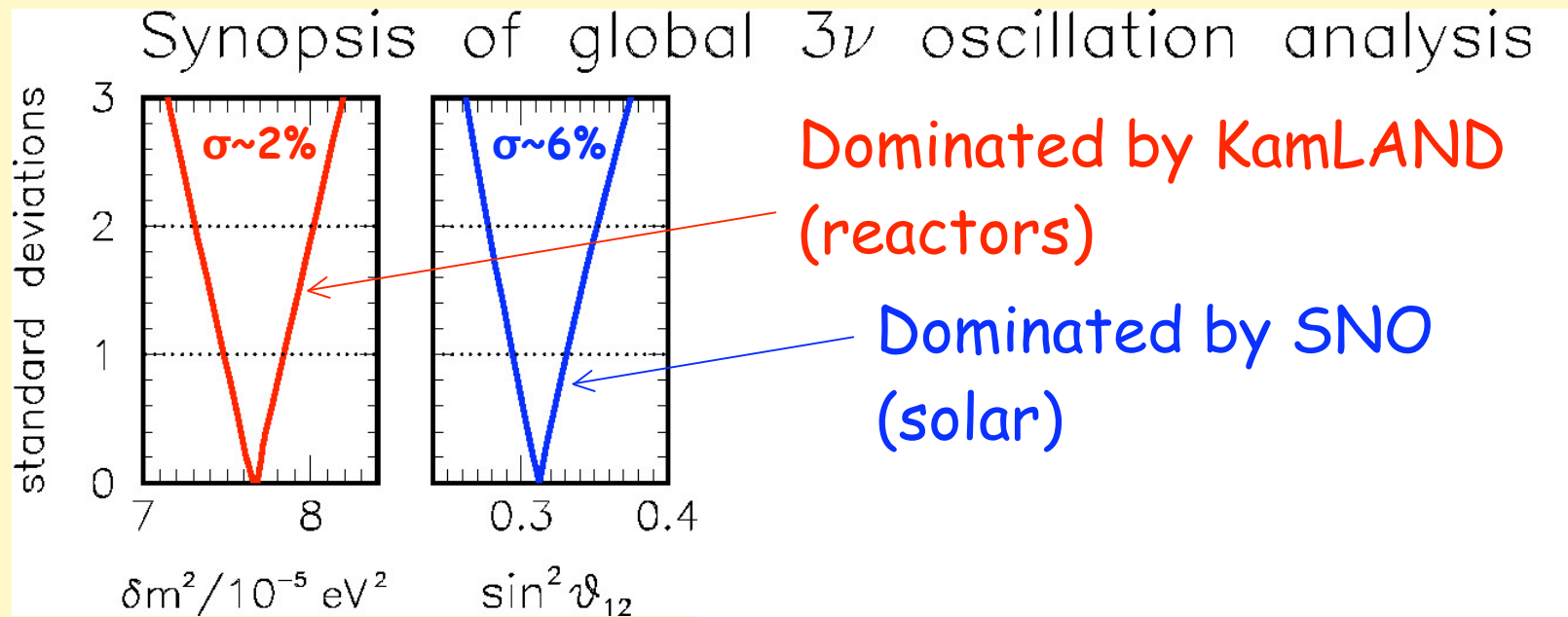


TABLE I: Global 3ν oscillation analysis (2008): best-fit values and allowed n_σ ranges for the mass-mixing parameters.

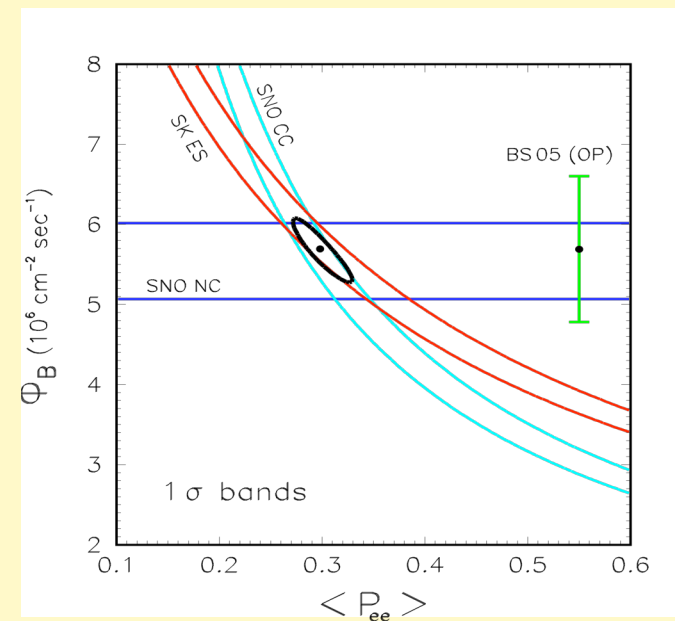
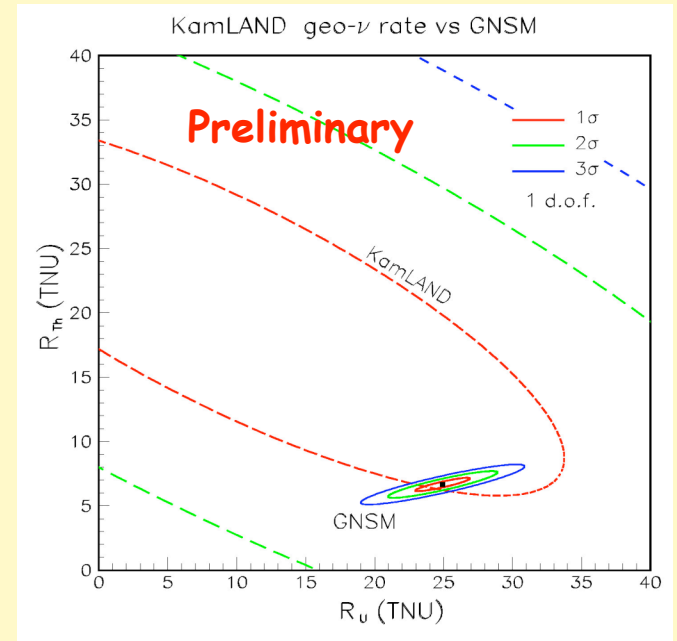
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ADDITIONAL RESULTS:

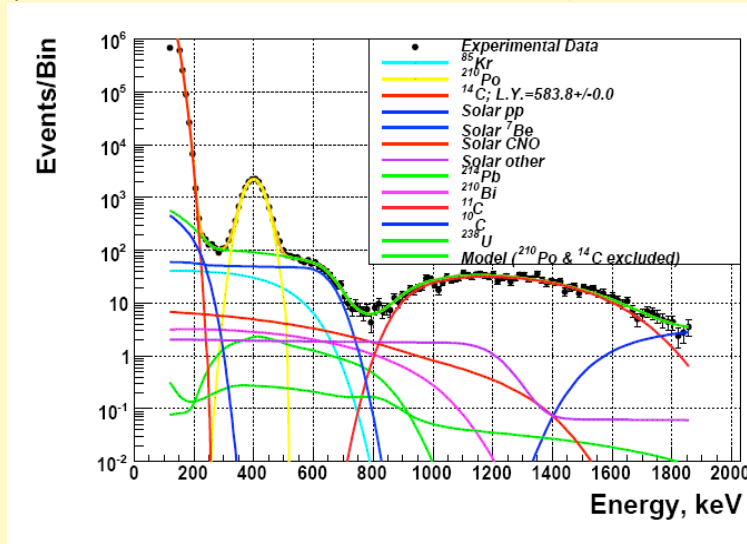
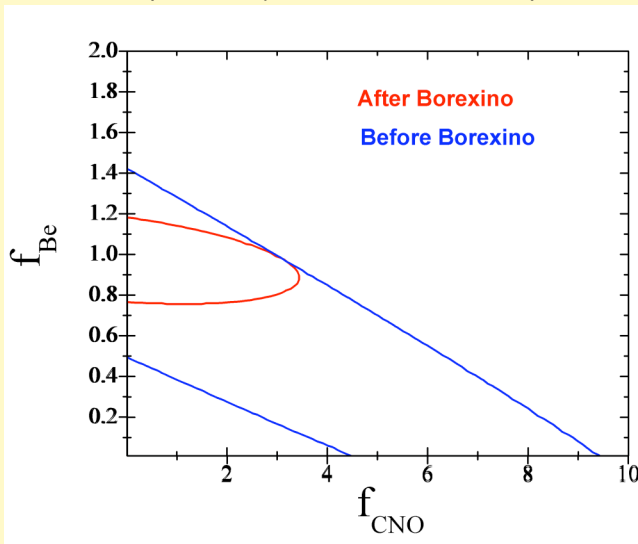
KamLAND results on geo- ν 's agree with geo-chemical/physical models for radiogenic heat production from U, Th decays inside the Earth (within large errors)...

... and SNO+SK data agree with the standard solar model expectations for neutrino production in Boron-8 decays (within comparable errors)

Future precision measurements in the (1,2) neutrino sector might lead to more significant tests of current models of the Earth and Sun interior.



Borexino can perform an independent measurement of the geoneutrino flux in a few years. A more challenging goal is to measure solar neutrino fluxes from the CNO cycle, which are relevant in the connection to the solar metallicity problem (discrepancy between photospheric & helioseismological data).

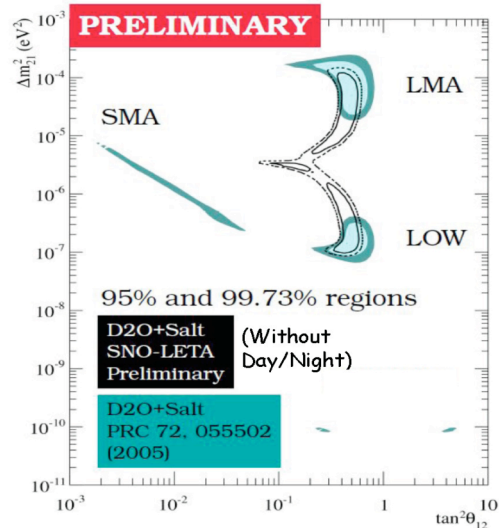


In general, CNO and low-energy fluxes are important goals for any future program of solar neutrino observations. New confirmations (or surprises) might then emerge in the context of solar & Earth model (as well as of neutrino physics)

Near future: Expected improvements on θ_{12}

Low Energy Threshold Analysis

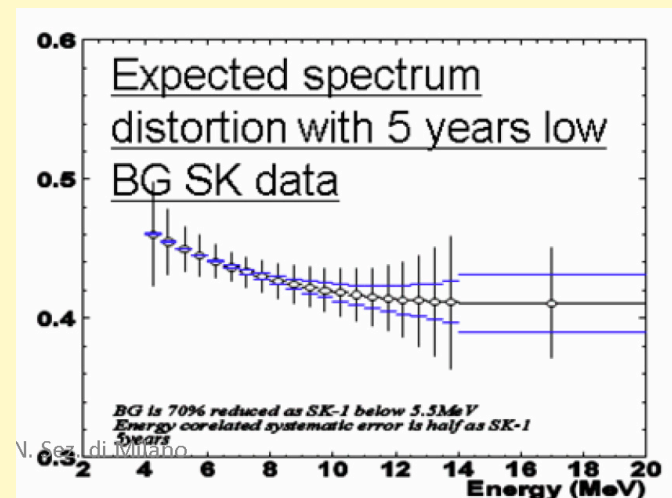
➤ SNO-Only Mixing Parameters



Final results from SNO low-energy threshold analysis (LETA) imminent.

Preliminary results shown by J. Klein at TAUP 2009 seem to suggest a preference for **relatively low values of θ_{12}** in the SNO-LETA.

Also: Low-threshold analysis in progress in SK (see talks by Smy, Ranucci at TAUP 2009).
SK & SNO expected to shed light on expected LMA spectrum upturn at low energy.



Oscillation parameters: state of the art, sectors (2,3)

Synopsis of global 3ν oscillation analysis

standard deviations

Dominated by MINOS
(accelerator)

Dominated by SuperK
(atmospheric)

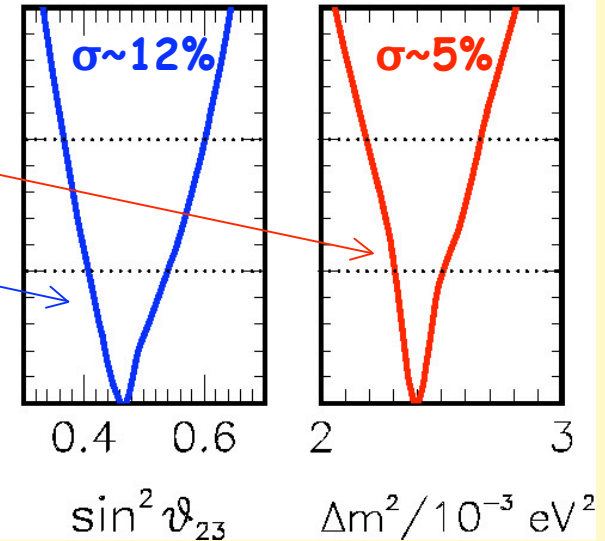
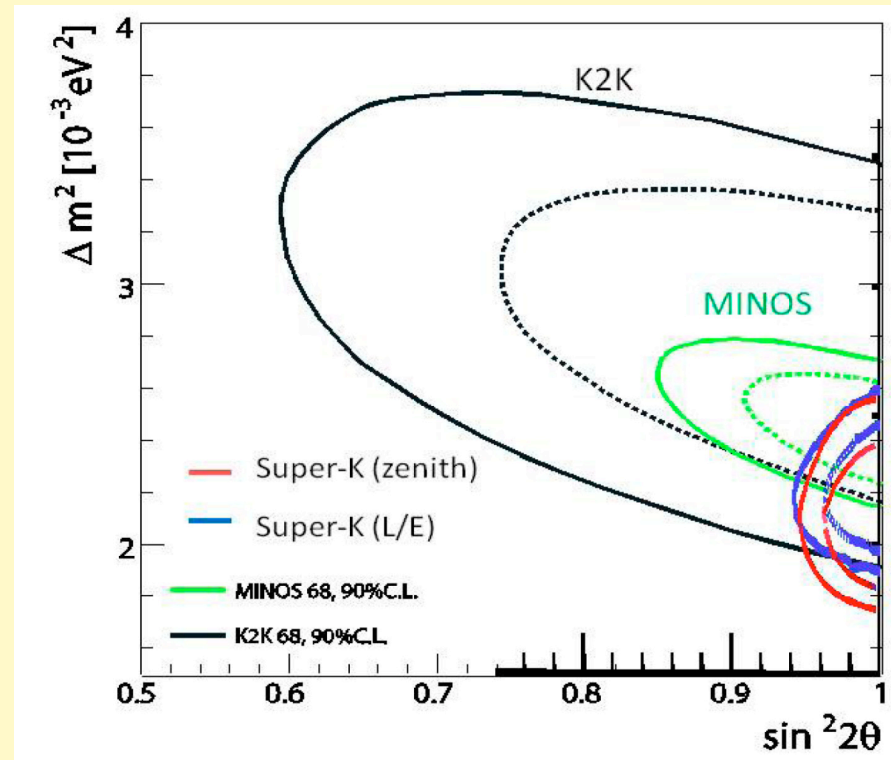


TABLE I: Global 3ν oscillation analysis (2008): best-fit values and allowed n_σ ranges for the mass-mixing parameters.

Parameter	$\sin^2 \theta_{23}$	$\Delta m^2 / 10^{-3} \text{ eV}^2$
Best fit	0.466	2.39
1σ range	0.408 – 0.539	2.31 – 2.50
2σ range	0.366 – 0.602	2.19 – 2.66
3σ range	0.331 – 0.644	2.06 – 2.81

note:
 $\delta m^2 / \Delta m^2 \sim 3\%$!

Latest MINOS
and SK-I+II+III
constraints in 2 ν
approximation
(as reviewed by
T. Kajita, TAUP'09):



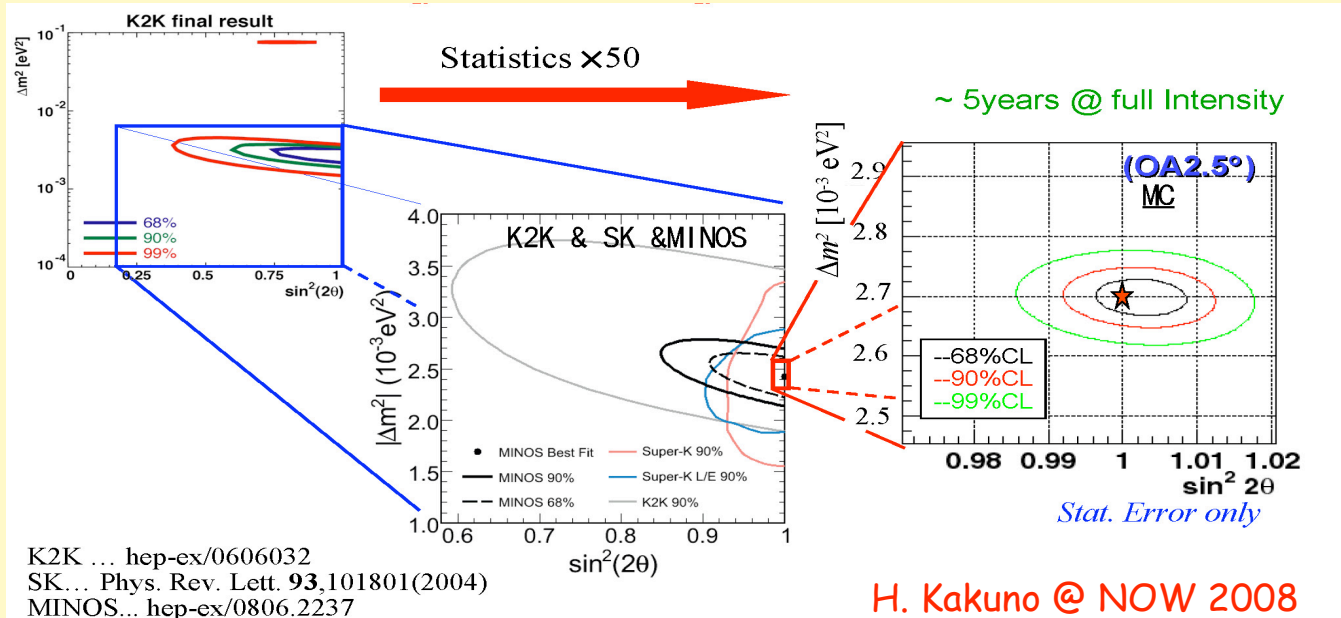
For the sake of precision, it would be better to perform future official analyses in a 3 ν framework, including “solar terms.”

Unambiguous definition of “atmospheric” Δm^2 is then mandatory.

Our convention:

$$\Delta m^2 = \left| \frac{\Delta m_{31}^2 + \Delta m_{32}^2}{2} \right| = \left| m_3^2 - \frac{m_1^2 + m_2^2}{2} \right|$$

Prospects: MINOS & SK may provide further fractional improvements in the disappearance channel $\nu_\mu \rightarrow \nu_\mu$.
T2K (starting this year, but with low-intensity beam) expected to reach percent accuracy:



From T2K onward: Multiple solutions may appear in the Parameter space $(\theta_{23}, \theta_{13}, \text{sign}(\Delta m^2), \delta)$ or in some subspaces

-> "degeneracy" or "clone" problem, relevant to optimize R&D

- Detour on hierarchy -

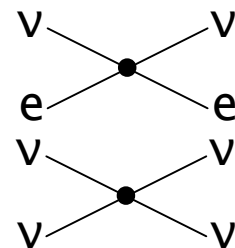
The ambiguity related to hierarchy, namely, $\text{sign}(\pm\Delta m^2)$, can be addressed (in principle), via interference of Δm^2 -driven oscillations with oscillations driven by some quantity Q having a known sign.

Barring new states/interactions, the only known options are:

Q = Electron density (MSW effect in Earth or SNe)

Q = Neutrino density (Collective effects in SNe)

$Q = \delta m^2$ (High-resolution oscill. patterns)



The first option seems more realistic (e.g., in NOvA or T2KK), provided that θ_{13} is not too small; but the other two are also being investigated as long-term (or last resort!) options.

- Also: keep in mind high-precision cosmology... -

Oscillation parameters: state of the art, angle (1,3)

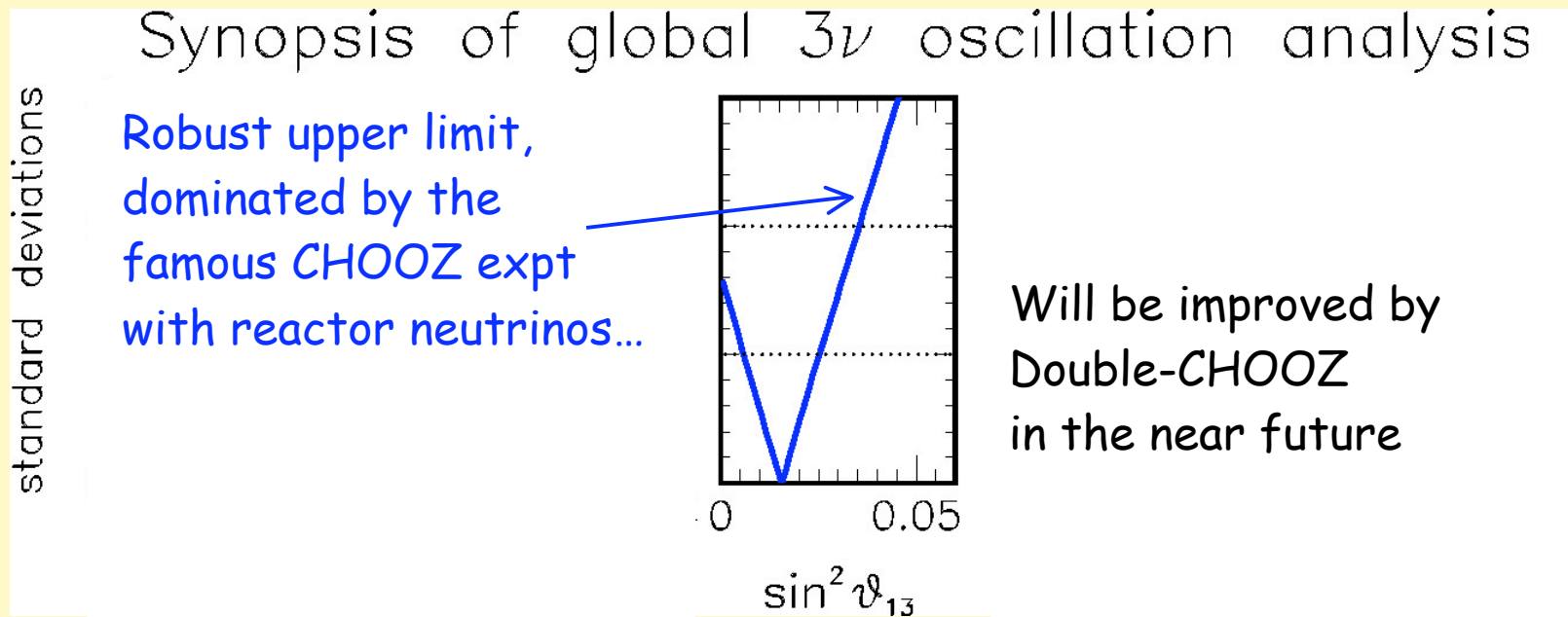
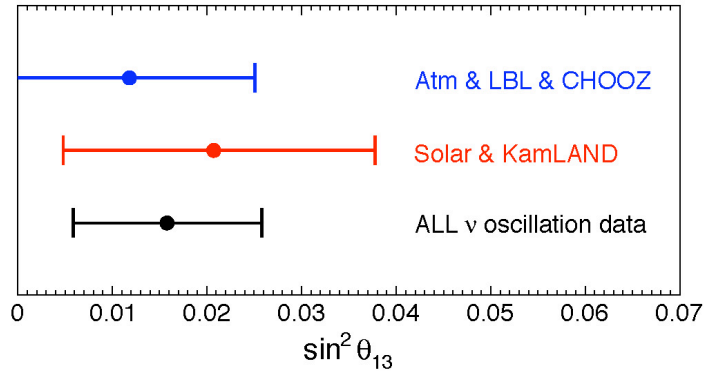


TABLE I: Global 3ν oscillation analysis (2008): best-fit values and allowed n_σ ranges for the mass-mixing parameters.

Parameter	$\sin^2 \theta_{13}$
Best fit	0.016
1σ range	0.006 – 0.026
2σ range	< 0.036
3σ range	< 0.046

However, some datasets seem to suggest also a weak lower limit...

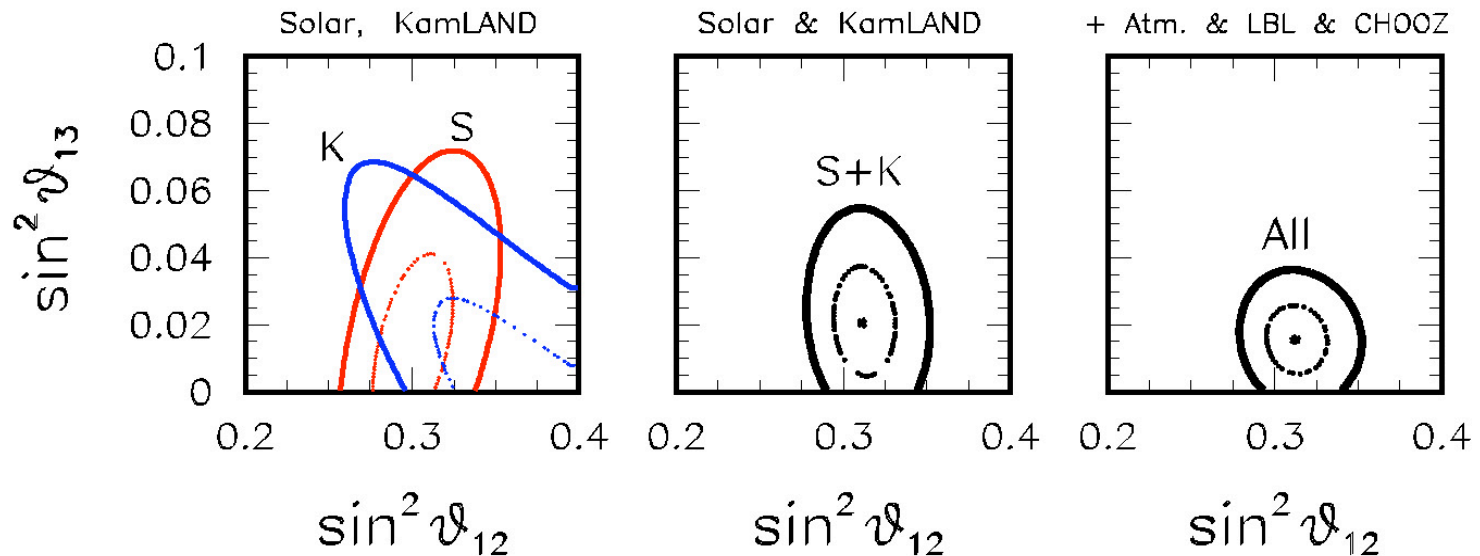


$\sim 1\sigma$ from sector (2,3)

$\sim 1\sigma$ from sector (1,2)

$\sim 90\%$ CL total:

$$\sin^2 \theta_{13} = 0.016 \pm 0.010$$



Well understood aspect: different correlation between mix. angles in KamLAND vs Solar, arising from different relative signs in P_{ee} (survival probability)

Solar, low energy (\sim vacuum):

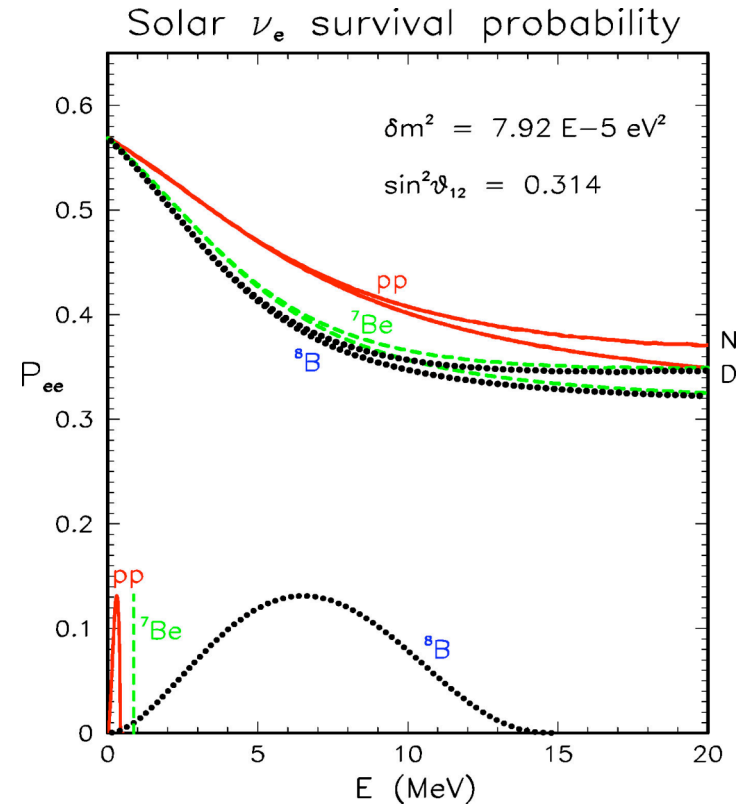
$$P_{ee} \simeq (1 - \underline{2s_{13}^2})(1 - \underline{2s_{12}^2 c_{12}^2})$$

Solar, high energy (\sim MSW):

$$P_{ee} \simeq (1 - \underline{2s_{13}^2})(\underline{+} s_{12}^2)$$

Reactor (\sim vacuum): KamLAND

$$P_{ee} \simeq (1 - \underline{2s_{13}^2})(1 - \underline{4s_{12}^2 c_{12}^2} \sin^2(\delta m^2 L/4E))$$



“Tension” on θ_{12} (solar vs KamLAND) can then be alleviated for $\theta_{13} > 0$

Atmospheric indication for $\theta_{13} > 0$ is less “direct” and more “fragile”

Some remarks on θ_{13} atmospheric hints

Weak hint for $\theta_{13} > 0$ in 3-neutrino analysis of atmospheric + LBL + Chooz data (Bari group, 2006), at the level of ~ 1 sigma.

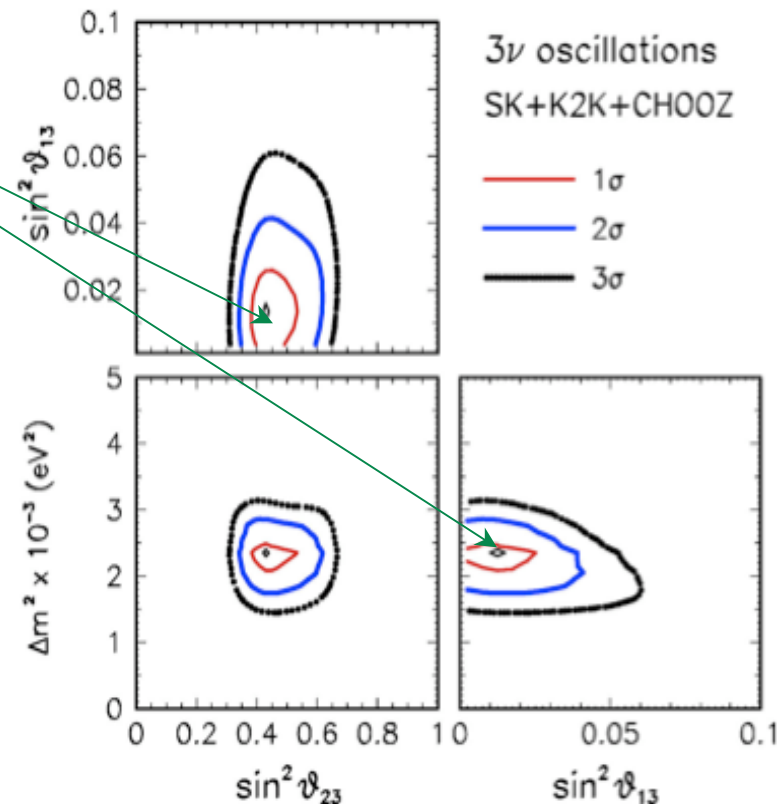
best fit ~ 1 sigma
away from zero

We attributed it to subleading “solar term” effects, which help to fit the atmospheric electron-like event data (especially sub-GeV) in Super-K phase I.

Hint is NOT killed by adding K2K and MINOS disappearance data.

But, other analyses found weaker or no hint (Note: not all of them include solar terms).

The “last word” is expected from the SK collaboration, since their data analysis is becoming too difficult to be reproduced at the needed level of accuracy.



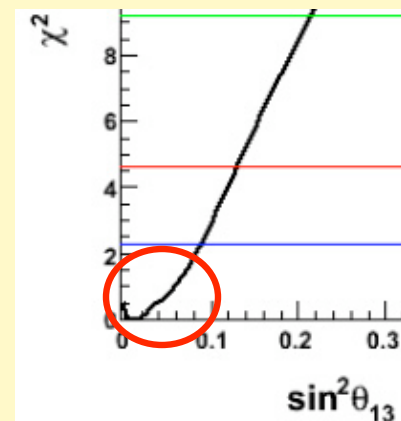
Status of official SK-I+II+III analysis: reported by T. Kajita at TAUP 2009. At present, SK analysis with solar terms is underway. Without solar terms, preliminary SK results were summarized as:

No evidence for non-zero θ_{13} with an analysis that **assumes $\Delta m_{12}^2 = 0$** .

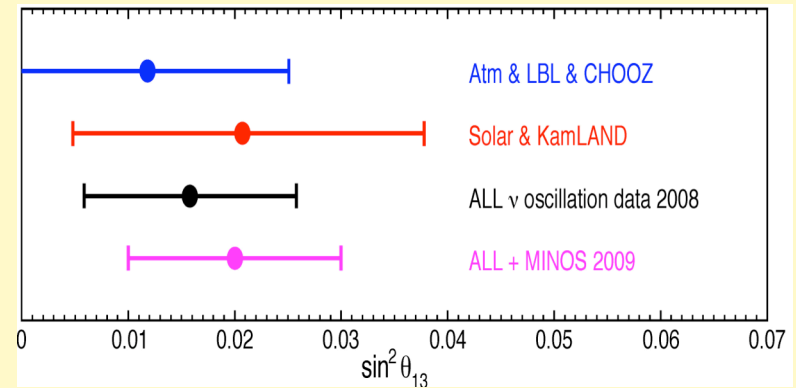
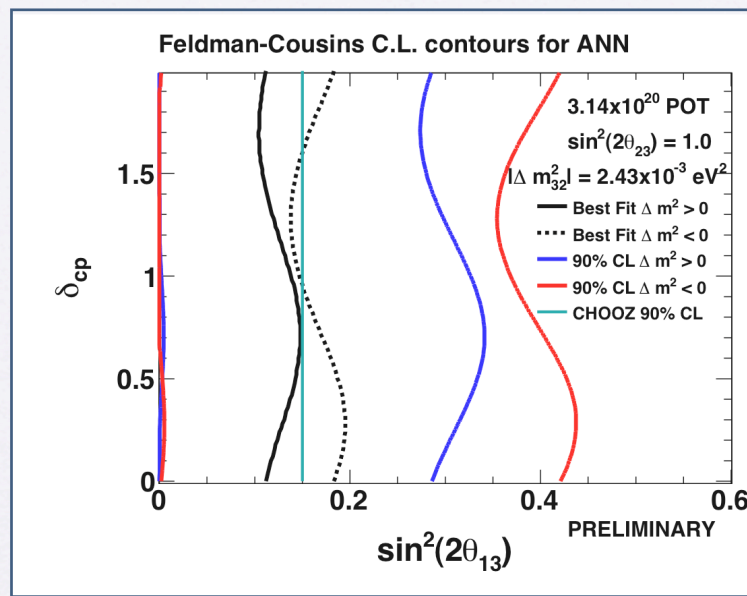
More details given by R. Wendell's at TAUP'09:

	χ^2 / dof	Δm^2	$\sin^2 \theta_{23}$	$\sin^2 \theta_{13}$
Normal	469 / 417	2.1×10^{-3}	0.50	0
Inverted	468 / 417	2.1×10^{-3}	0.55	0.01

Let me note the weak preference for inverted hierarchy and nonzero θ_{13} ... It remains to be seen how solar terms will affect these results in the final SK analysis.



A possible independent hint of $\theta_{13} > 0$ (at 90% C.L.) seems to come from the recent, preliminary **MINOS** results in appearance channel $\nu_\mu \rightarrow \nu_e$



Combining all data (with some optimism), the grand total is:

$$\sin^2 \theta_{13} \approx 0.02 \pm 0.01 \text{ (all data, circa 2009)}$$

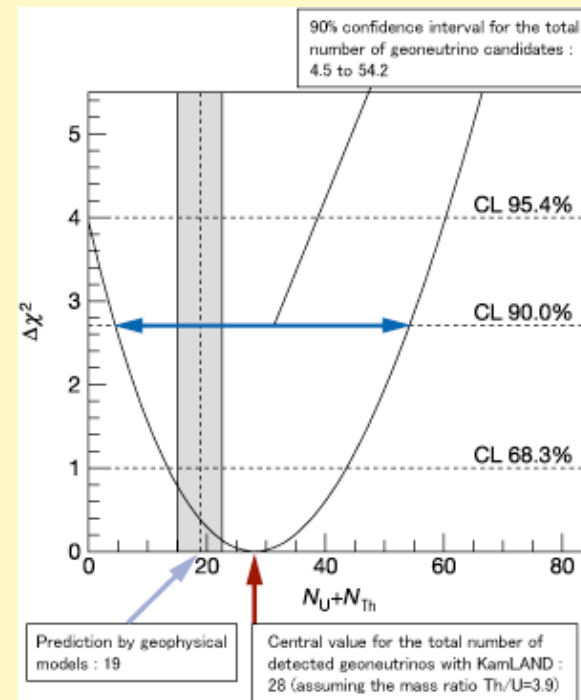
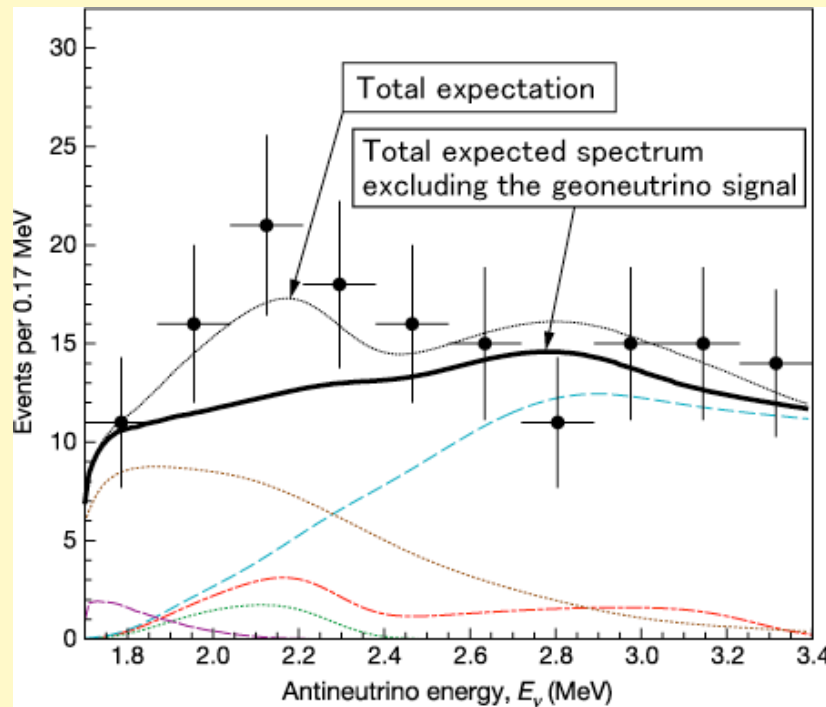
which is an encouraging 2σ hint, testable in the next few years.

(N.B.: MINOS, SK, SNO, KamLAND can still provide further improvements)

Is a “two-sigma hint” interesting or not? That's up to you...

[J. Bahcall's attitude: “Half of all three-sigma results are wrong”]

Note: the 2005 KamLAND geo- ν paper was based on a 2σ signal...



(latest published level of significance: $\sim 2.7\sigma$)

PDG quotes the θ_{13} hints in the 2009 update:

$\sin^2(2\theta_{13})$

At present time, limits of $\sin^2(2\theta_{13})$ are derived from the search for the reactor $\bar{\nu}_e$ disappearance at distances corresponding to the Δm_{23}^2 value, i.e. $L \sim 1\text{km}$. Alternatively, somewhat weaker limits can be obtained from the analysis of the solar neutrino data.

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<0.19	90	148 APOLLONIO	99 CHOZ	Reactor Experiment
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.06 ± 0.04		149 FOGLI	08 FIT	Global neutrino data
0.08 ± 0.07		150 FOGLI	08 FIT	Solar + KamLAND data
0.05 ± 0.05		151 FOGLI	08 FIT	Atmospheric + LBL + CHOOZ data
<0.48	90	152 HOSAKA	06A SKAM	3ν oscillation; normal mass hierarchy
<0.79	90	153 HOSAKA	06A SKAM	3ν oscillation; inverted mass hierarchy
<0.36		154 YAMAMOTO	06 K2K	Accelerator experiment
<0.48	90	155 AHN	04 K2K	Accelerator experiment
<0.36	90	156 BOEHM	01	Palo Verde react.
<0.45	90	157 BOEHM	00	Palo Verde react.

¹⁴⁸ The quoted limit is for $\Delta m_{32}^2 = 1.9 \times 10^{-3} \text{ eV}^2$. That value of Δm_{32}^2 is the 1-σ low value for ALIU 05. For the ALIU 05 best fit value of $2.8 \times 10^{-3} \text{ eV}^2$, the $\sin^2 2\theta_{13}$ limit is < 0.13. See also APOLLONIO 03 for a detailed description of the experiment.

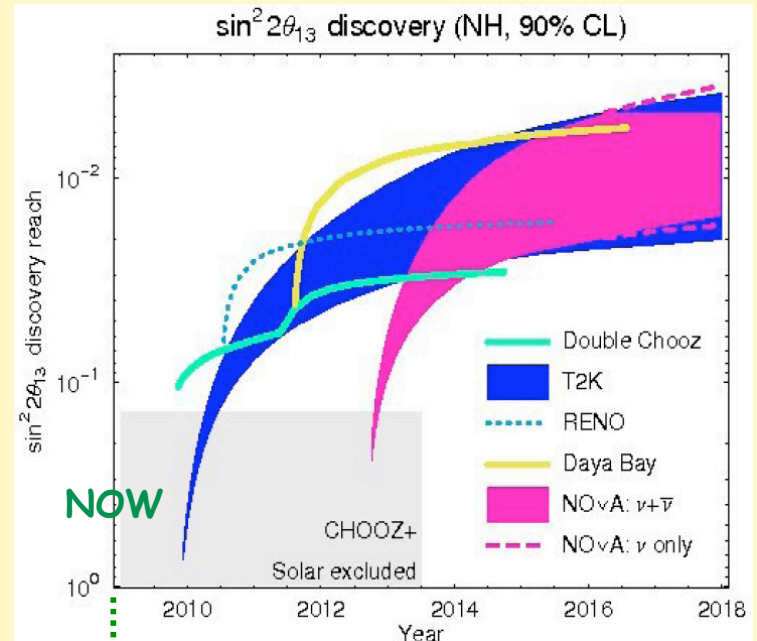
¹⁴⁹ FOGLI 08 obtained this result from a global analysis of all neutrino oscillation data, that is, solar + KamLAND + atmospheric + accelerator long baseline + CHOOZ.

¹⁵⁰ FOGLI 08 obtained this result from an analysis using the solar and KamLAND neutrino oscillation data.

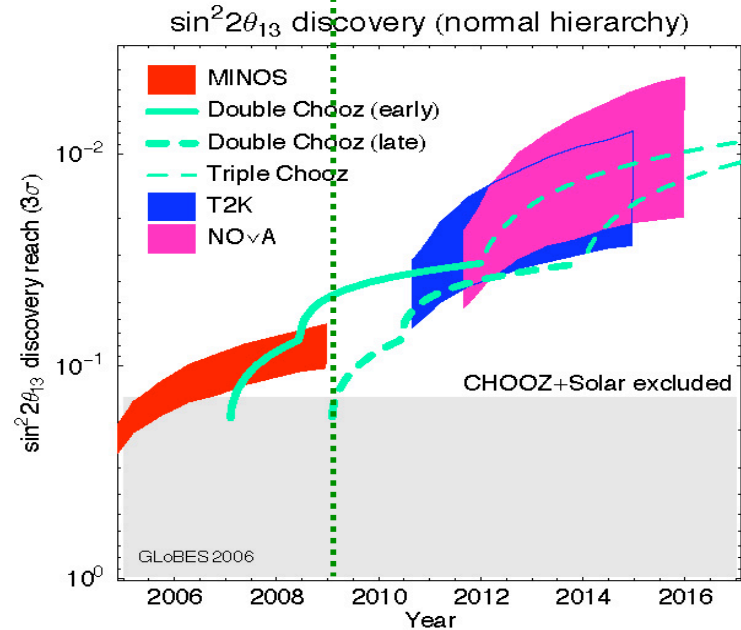
¹⁵¹ FOGLI 08 obtained this result from an analysis using the atmospheric, accelerator long baseline, and CHOOZ neutrino oscillation data.

The future:

θ_{13} prospects for the next decade
(as shown by J. Valle at TAUP'09,
courtesy of M. Lindner et al.):



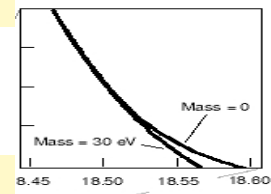
The same plot 3 years ago
(note time shift). Needless
to say, neutrino physics is
an exercise in patience...



Absolute neutrino masses. Threefold attack strategy: (m_β , $m_{\beta\beta}$, Σ)

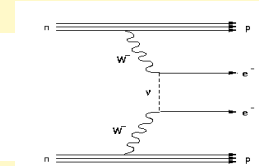
- 1) **Single β decay:** $m_i^2 \neq 0$ alters the spectrum tail. Sensitive to the so-called "effective mass of electron neutrino":

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$



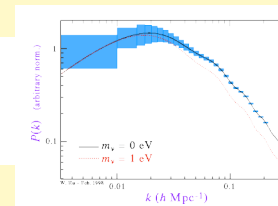
- 2) **Double $0\nu\beta\beta$ decay:** Iff $m_i^2 \neq 0$ and $\nu = \text{anti-}\nu$ (Majorana). Sensitive to the "effective Majorana mass" (and related phases):

$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

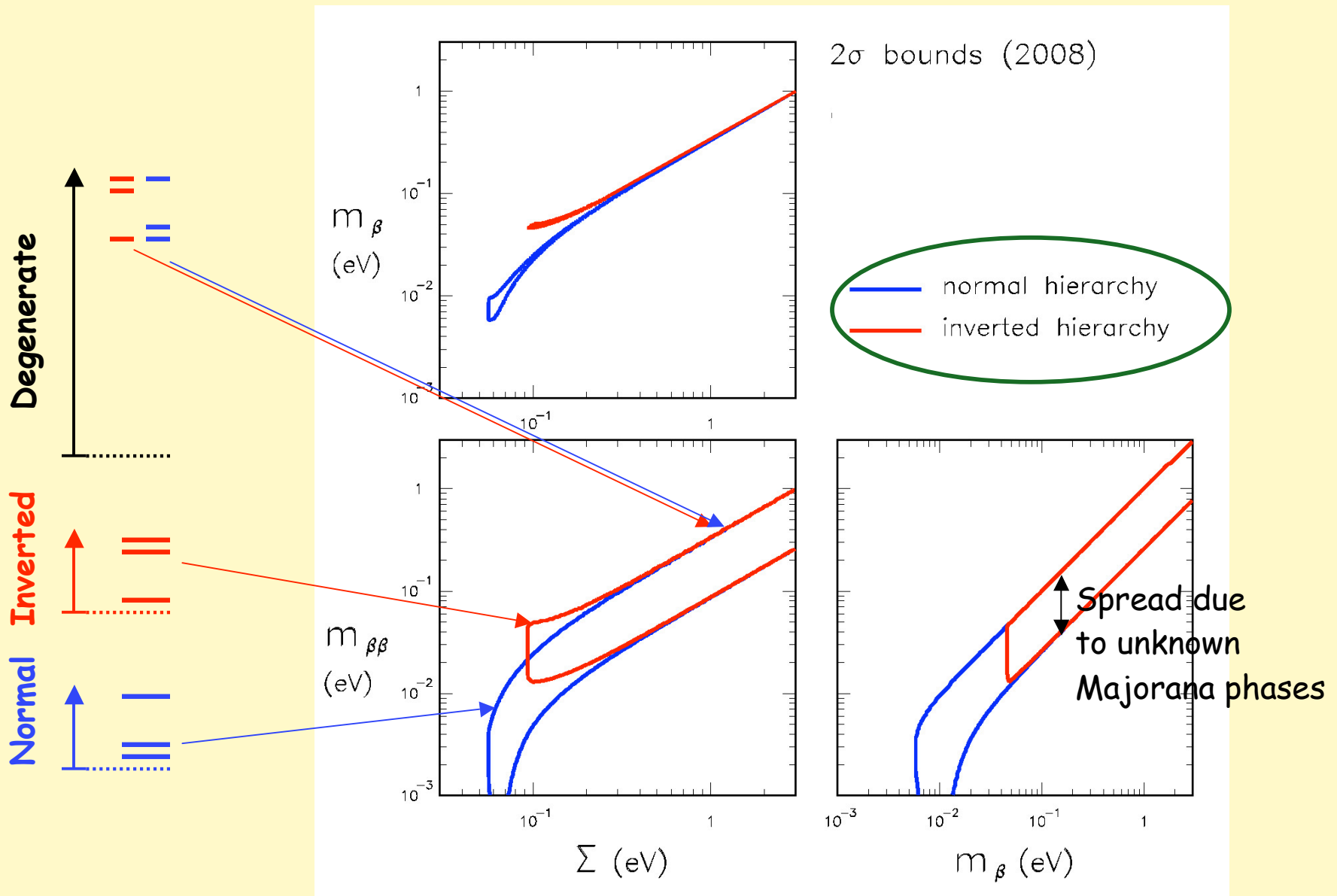


- 3) **Cosmology:** $m_i^2 \neq 0$ alters large scale structure formation within standard cosmology constrained by CMB + other data. Measures:

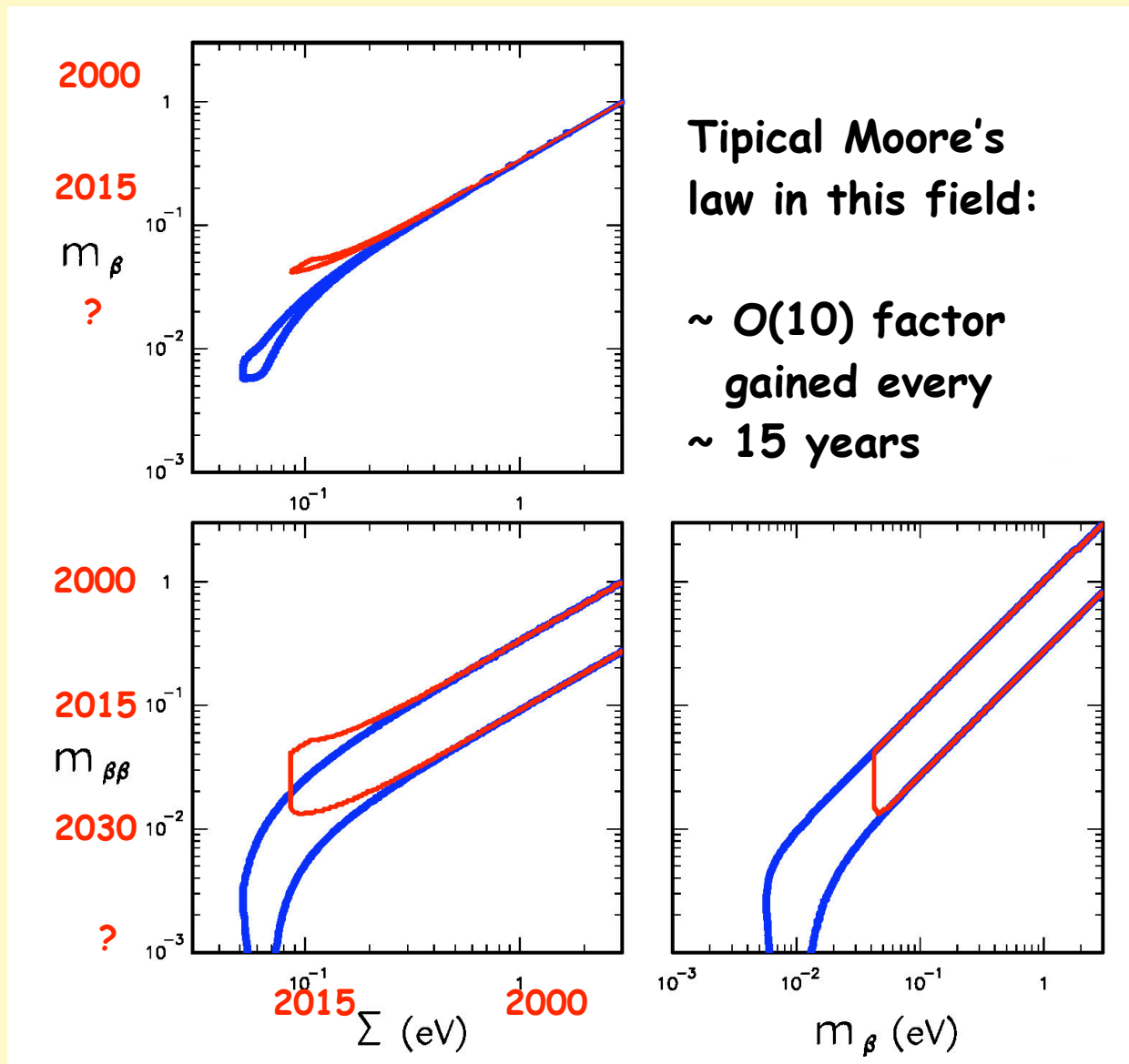
$$\Sigma = m_1 + m_2 + m_3$$



Oscillation data do constrain regions of the non-oscillation parameter space (m_β , $m_{\beta\beta}$, Σ) for both hierarchies (degenerate in the "large" mass limit)



... But, of course, we do need proper non-oscillation data on $(m_\beta, m_{\beta\beta}, \Sigma)$ to make real progress: another exercise in patience...



Single β decay

Tritium experiments:

Mainz + Troitsk: $m_\beta < 2 \text{ eV}$

KATRIN: improvement of $O(10)$

Some possible outcomes from
KATRIN ($\pm 1\sigma$, [eV]):

$$m_\beta = 0.35 \pm 0.07 \quad (5\sigma, \text{discovery})$$

$$m_\beta = 0.30 \pm 0.10 \quad (3\sigma, \text{evidence})$$

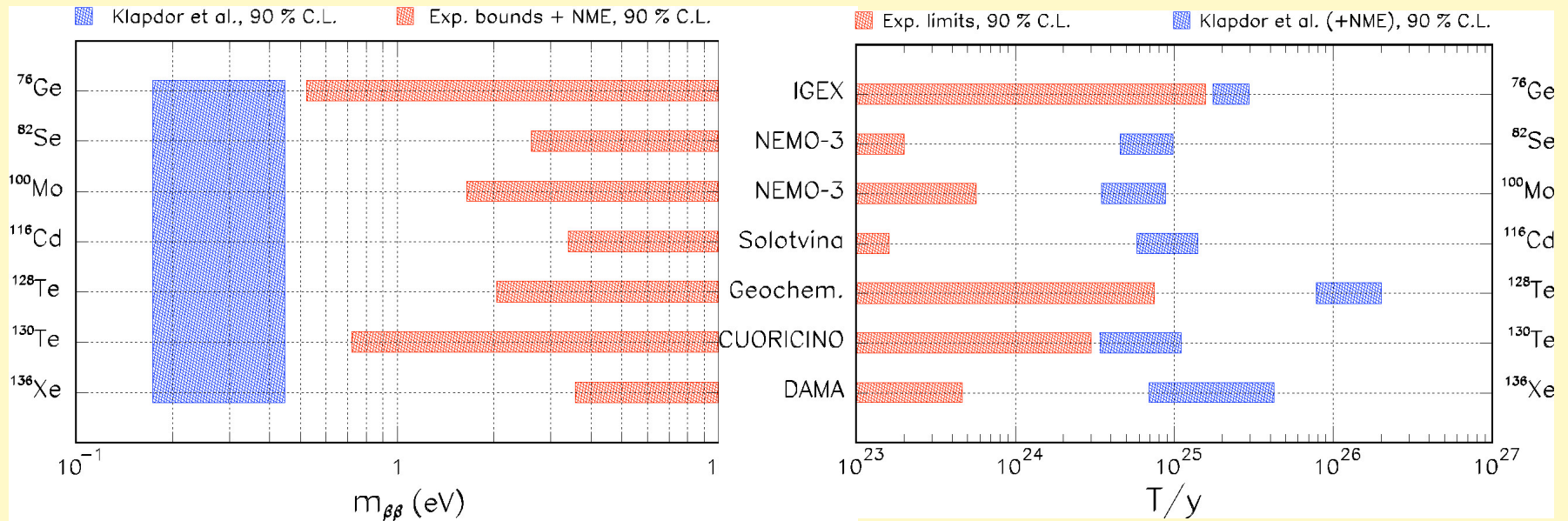
$$m_\beta = 0 \pm 0.12 \quad (<0.2 \text{ at } 90\% \text{ CL})$$



Clearly, new ideas are needed
to go below $\sim 0.2 \text{ eV}$. **MARE ?**

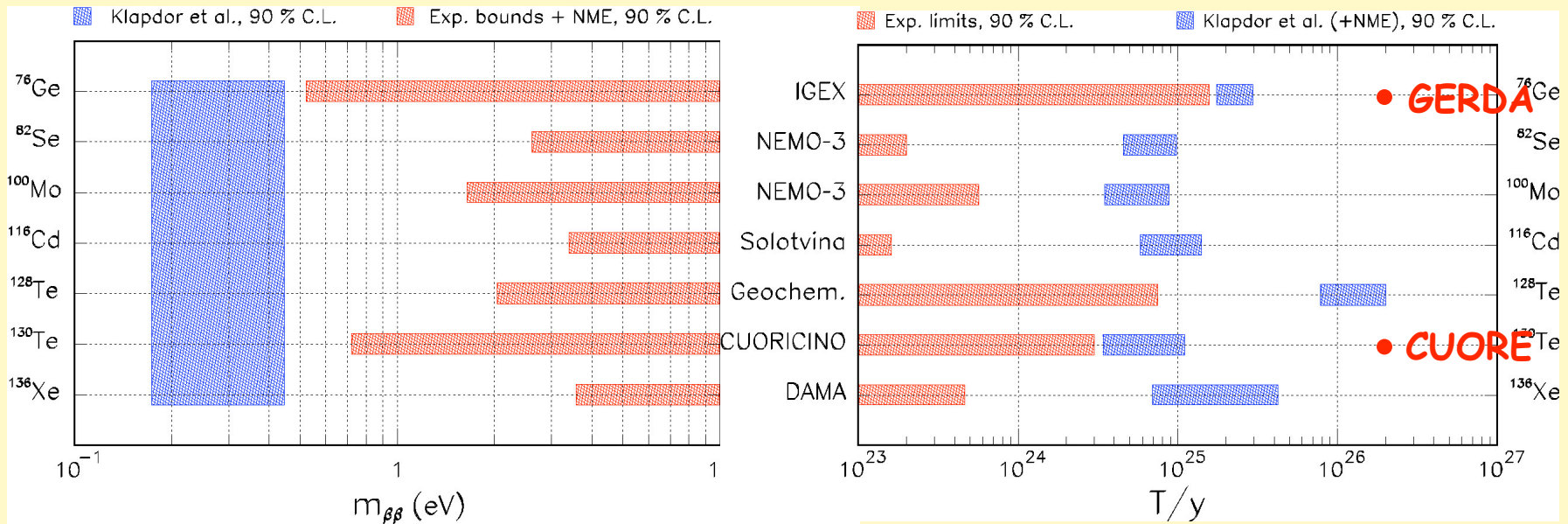
Neutrinoless double β decay

Only upper limits, except for a controversial signal in the most sensitive experiment to date (Klapdor et al.). By using recent estimates of nuclear matrix elements and their covariances:



Neutrinoless double β decay

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Expected sensitivities, e.g., for CUORE, GERDA @ LNGS
 [and best wishes to all our colleagues & their families at GS & L'Aquila]

Cosmology: Updated limits (2008) on the sum of ν masses from various data sets (assuming the “flat Λ CDM model”):

TABLE II: Representative cosmological data sets and corresponding 2σ (95% C.L.) constraints on the sum of ν masses Σ .

Case	Cosmological data set	Σ (at 2σ)
1	CMB	< 1.19 eV
2	CMB + LSS	< 0.71 eV
3	CMB + HST + SN-Ia	< 0.75 eV
4	CMB + HST + SN-Ia + BAO	< 0.60 eV
5	CMB + HST + SN-Ia + BAO + $\text{Ly}\alpha$	< 0.19 eV

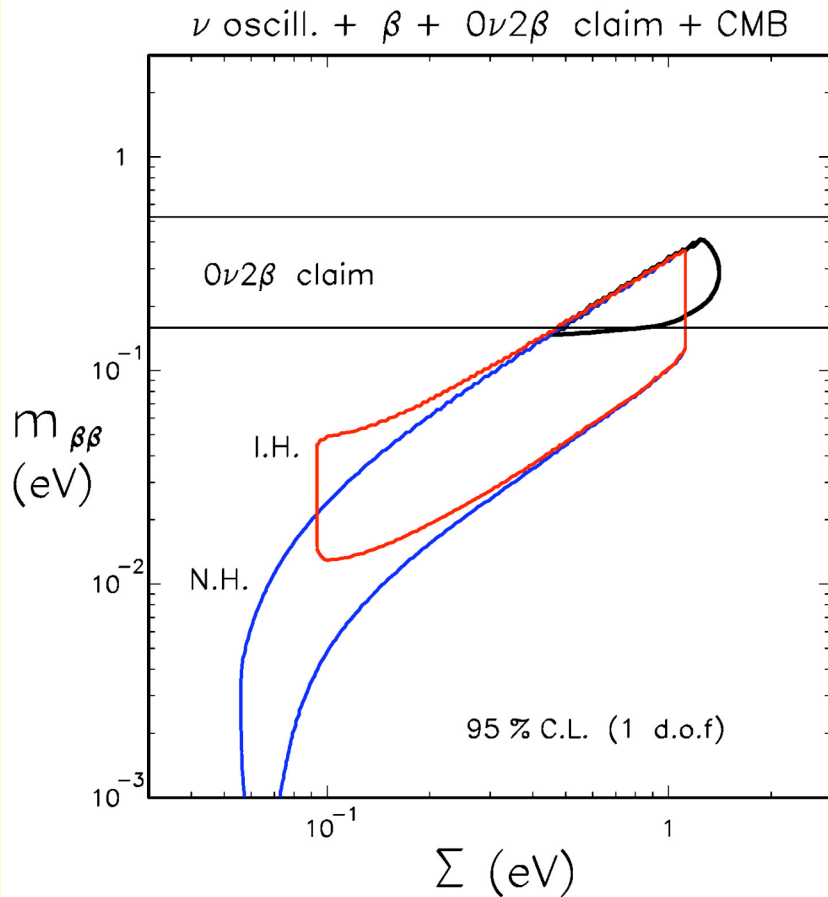
Case 1: “conservative” (only CMB data, dominated by WMAP 5y)

Case 5: “aggressive” (all relevant cosmological data)

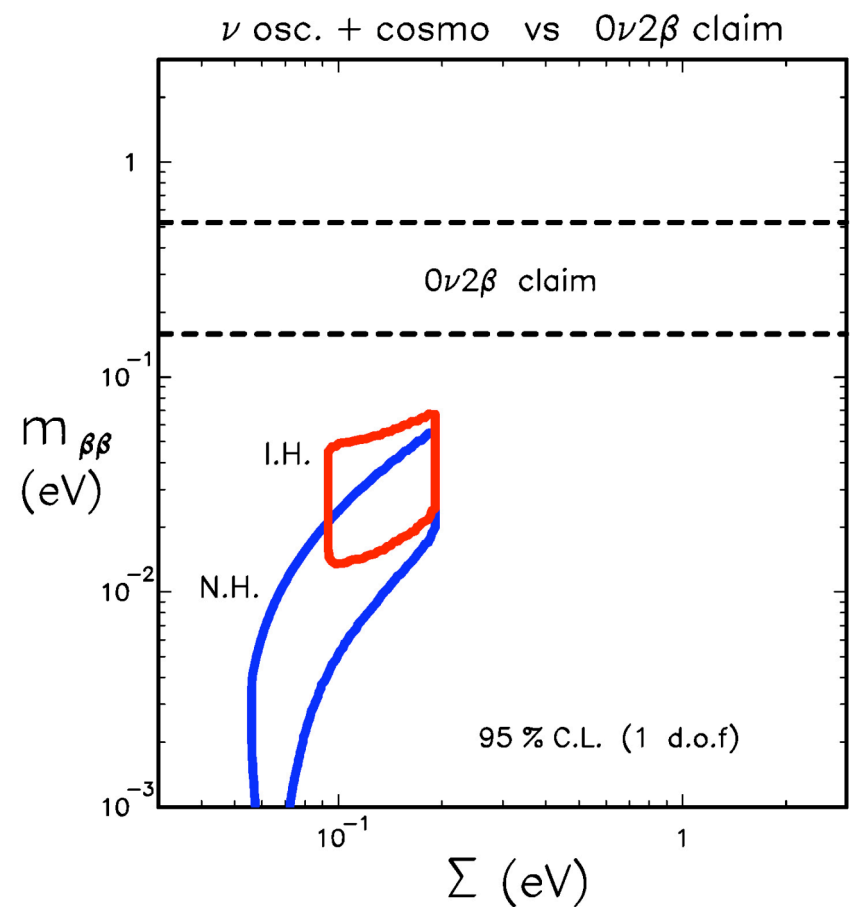
Upper limits in the range $\Sigma < 0.6\text{--}1.2$ eV have gained large consensus.

[Cosmologists envisage a brighter future, with sensitivities at the level of ~ 0.1 eV and, perhaps, to the hierarchy. But, will particle physicists be ready to accept a cosmological claim for $\Sigma > 0$?]

Cosmo-"conservative"



Cosmo-"aggressive"



Status of absolute neutrino masses inconclusive...

Let's entertain the possibility that the "true" masses are just around the corner... For instance, that neutrinos are Majorana, with nearly degenerate mass values as high as:

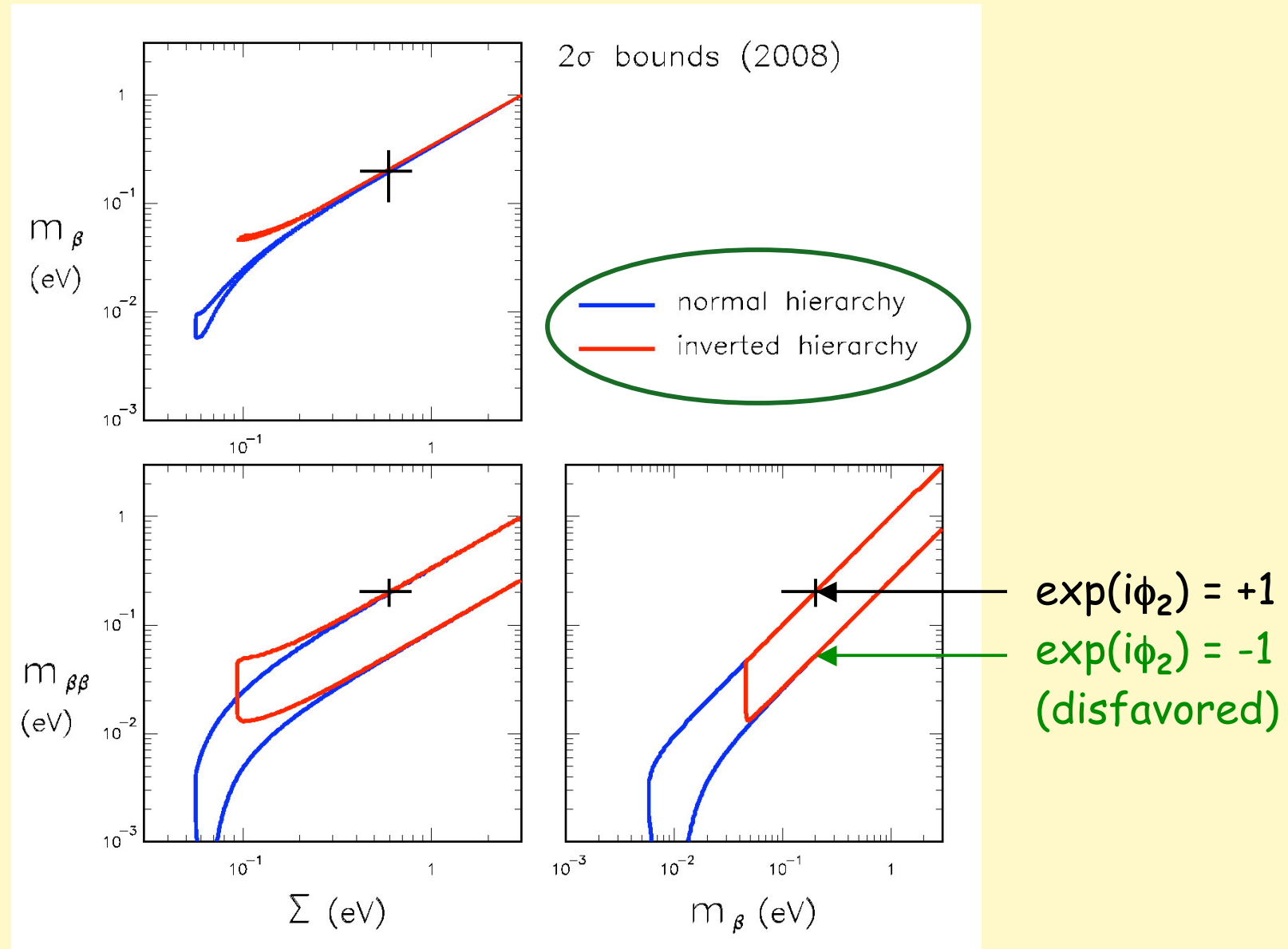
$$m_1 \sim m_2 \sim m_3 \sim 0.2 \text{ eV} .$$

Then we might reasonably hope to observe soon all three nonoscillation signals, e.g.,

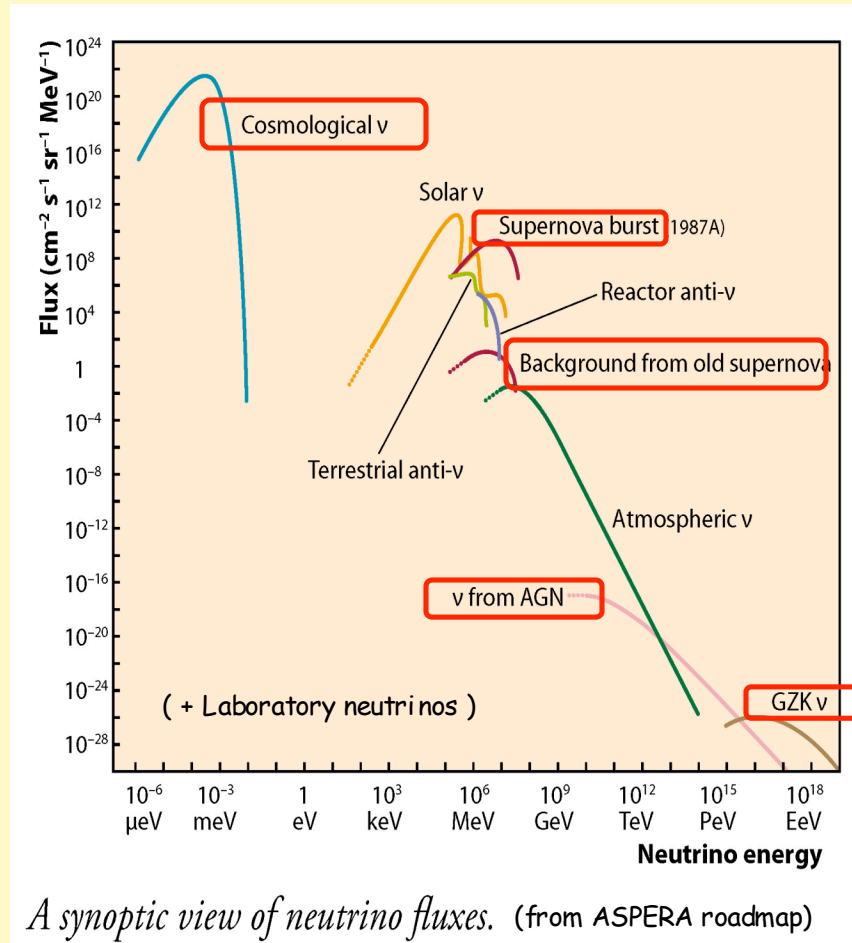
$$\begin{array}{lll} m_{\beta\beta} & \simeq & 0.2(1 \pm 0.3) \text{ eV} \\ \Sigma & \simeq & 0.6(1 \pm 0.3) \text{ eV} \\ m_{\beta} & \simeq & 0.2(1 \pm 0.5) \text{ eV} \end{array}$$

In which case...

...The absolute neutrino mass would be reconstructed within $\sim 25\%$ uncertainty, and one Majorana phase (ϕ_2) would be constrained...



Just a dream? Maybe. However, “dreaming” is essential to face and overcome the many challenges of neutrino science (and technology!), including those related to cosmo/astro neutrino sources...



... whose discussion would require another seminar.

Thank you for your attention.