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Workshop Towards Neutrino Technologies

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Towards neutrino mass spectroscopy and relic detection using atomic targets; theoretical aspects

Motohiko YOSHIMURA

Okayama University Department of Physics Tsushima-naka 3-1-1 Okayama 700-8530, JAPAN Towards neutrino mass spectroscopy and relic detection

using atomic targets: theoretical aspects

Introduction:

merits and demerits using atoms

- SPAN (Spectroscopy of atomic neutrino) new systematic experimental method for resolving remaining important questions
- Macro-coherence; N^2 enhancement in macro region
- Photon spectrum, angular asymmetry, circular polarization in RNPE
- Future towards relic detection





Radiative neutrino pair emission (RNPE)

 2<sup>nd</sup> order electroweak process, 1<sup>st</sup> orders in weak and QED. No question about existence of process, but yet to be discovered.



 $|1\rangle \rightarrow |3\rangle + \gamma + \nu \nu$ 

Initial state metastable > 100 msec Prepared by > 2 lasers



# Merits and demerits of atomic process

• Infinitely many small energies are available

$$\Delta E_{n_1,n_2} \sim 13.6 eV \times (\frac{1}{n_2^2} - \frac{1}{n_1^2})$$

- Small rate of neutrino pair emission
- How to verify neutrino pair emission: 1 photon energy spectrum having 6 thresholds

$$\omega_{ij} = \Delta/2 - (m_i + m_j)^2/(2\Delta)$$

 How to enhance the rate is crucial target coherence: O[10^4] N^2 expected Xe

4.1996 4.19

Significance of discovering Majorana neutrino

- Neutral fermions follow economic Majorana eq or the same Dirac eq as charged fermions ?
- Leading to lepton number violation and lepto-genesis particle = anti-particle missing partner for leptogenesis



Figure 10: Leptogenesis bound on neutrino masses. The plot shows the measured baryon asymmetry (horizontal line) compared with the maximal leptogenesis value as function of the heaviest neutrino mass  $m_3$ , renormalized at low energy. Error bars are at  $3\sigma$ .

Contributing to better understanding of seesaw mechanism and GUT

# M vs D in 2-component equations



In terms of 2-spinor of Lorentz group

$$(i\partial_t - i\vec{\sigma} \cdot \vec{\nabla})\varphi = im\sigma_2\varphi^* \quad \begin{array}{l} (i\partial_t - i\vec{\sigma} \cdot \vec{\nabla})\varphi = m\chi \\ (i\partial_t + i\vec{\sigma} \cdot \vec{\nabla})\chi = m\varphi \end{array}$$

## Majorana vs Dirac equations: chirally projected solutions

$$(i\partial_t - i\vec{\sigma}\cdot\vec{\nabla})\varphi = im\sigma_2\varphi^*$$

 $\varphi_{\vec{p},h}(x) = c(\vec{p},h)e^{-ip\cdot x}u(\vec{p},h) + c^{\dagger}(\vec{p},-h)e^{ip\cdot x}\sqrt{\frac{E_p + hp}{E_p - hp}}(-i\sigma_2)u^*(\vec{p},h)$ 

$$u(\vec{p},h) = \frac{1}{2} \sqrt{\frac{E_p - hp}{pE_p(p+hp_3)}} \begin{pmatrix} p+hp_3 \\ h(p_1+ip_2) \end{pmatrix}$$

$$(i\partial_t - i\vec{\sigma}\cdot\vec{\nabla})\varphi = m\chi, \quad (i\partial_t + i\vec{\sigma}\cdot\vec{\nabla})\chi = m\varphi$$

$$\psi_D = \frac{1}{2}(1 - \gamma_5)\psi$$

$$\psi_D = b(\vec{p}, h)e^{-ip \cdot x}u(\vec{p}, h) + d^{\dagger}(\vec{p}, -h)e^{ip \cdot x}\sqrt{\frac{E_p + hp}{E_p - hp}}(-i\sigma_2)u^*(\vec{p}, h)$$

### Unique signature of Majorana = interference of identical fermions

$$\sum_{h_1h_2} |j_M \cdot j^e|^2 = \sum_{h_1h_2} |j_D \cdot j^e|^2 + \delta_{ij} \frac{m_i m_j}{2E_1E_2} \left( j_0^e (j_0^e)^\dagger - \vec{j}^e \cdot (\vec{j}^e)^\dagger \right)$$

- Effective only for pair emission
- Appear only (ii) threshold; proportional to m\_i^2  $(\nu_i \nu_j) \ i \neq j$  pair
- Can be positive or negative
- Direct test of Majorana nature cf LV in  $(0\nu)\beta\beta$

### Dependence and sensitivity on Majorana phases

Matrix element for two neutrino emission of definite mass species  $\nu_i \nu_j$ , momentum  $p_1, p_2$  and helicity  $h_1, h_2$ ,

$$\begin{aligned} \langle (ip_1h_1, jp_2h_2) | j_{\nu} | 0 \rangle &= \xi_i^* \xi_j e^{i(p_1 + p_2) \cdot x} v_1^{\dagger} \sigma u_2 - \xi_i \xi_j^* e^{i(p_1 + p_2) \cdot x} v_2^{\dagger} \sigma u_1 \\ &= e^{i(p_1 + p_2) \cdot x} \left( i \Im \xi_i^* \xi_j (v_1^{\dagger} \sigma u_2 + v_2^{\dagger} \sigma u_1) + \Re \xi_i^* \xi_j (v_1^{\dagger} \sigma u_2 - v_2^{\dagger} \sigma u_1) \right) \\ \xi_i^* \xi_j &= U_{ei}^* U_{ej} = c_{ij}^{(0)} , \quad U_{e1} = c_{12} c_{13} , \ U_{e2} = s_{12} c_{13} e^{i\alpha} , \ U_{e3} = s_{13} e^{i\beta} \end{aligned}$$

using the standard mass matrix parametrization.

The neutrino current product becomes

$$\langle (ip_1h_2, jp_2h_2) | j_{\nu}^{\alpha} | 0 \rangle \langle 0 | j_{\nu}^{\beta} | (ip_1h_2, jp_2h_2) \rangle$$
  
=  $2 |\Im c_{ij}^{(0)}|^2 (v_1^{\dagger} \sigma^{\alpha} u_2 + v_2^{\dagger} \sigma^{\alpha} u_1) u_2^{\dagger} \sigma^{\beta} v_1 + 2 |\Re c_{ij}^{(0)}|^2 (v_1^{\dagger} \sigma^{\alpha} u_2 - v_2^{\dagger} \sigma^{\alpha} u_1) u_2^{\dagger} \sigma^{\beta} v_1$   
 $- \Im c_{ij}^{(0)} \Re c_{ij}^{(0)} \Im \left( (v_1^{\dagger} \sigma^{\alpha} u_2 + v_2^{\dagger} \sigma^{\alpha} u_1) u_2^{\dagger} \sigma^{\beta} v_1 - (1 \leftrightarrow 2) \right) + (\text{c.c})$ 

(symmetry property under  $1 \leftrightarrow 2$  is used)

Dropping CP-odd terms, 1st term is common in Dirac and Majorana cases, while 2nd ia Majorana interference term;

$$\begin{aligned} |c_{ij}^{(0)}|^2 (v_1^{\dagger} \sigma^{\alpha} u_2 u_2^{\dagger} \sigma^{\beta} v_1 + (1 \leftrightarrow 2)), \quad (\text{common}) \\ + (|\Im c_{ij}^{(0)}|^2 - |\Re c_{ij}^{(0)}|^2) (v_2^{\dagger} \sigma^{\alpha} u_1 u_2^{\dagger} \sigma^{\beta} v_1 + (1 \leftrightarrow 2)), \quad (\text{Majorana interference}) \end{aligned}$$

### Cancellation of leading CP-odd terms

The most important term for CP-odd quantities comes from GT terms squared, the last term. When multiplied by the coupling factor  $2i\Im c_{ij}^{(0)}\Re c_{ij}^{(0)}$  which contains odd terms of Majorana phases,

$$\begin{aligned} \Im c_{ij}^{(0)} \Re c_{ij}^{(0)} &= \\ c_{12}^2 s_{12}^2 c_{13}^4 \sin \alpha \cos \alpha \,, \text{ for } (ij) = (12) \\ c_{12}^2 s_{13}^2 c_{13}^2 \sin \beta \cos \beta \,, \text{ for } (ij) = (13) \\ s_{12}^2 s_{13}^2 c_{13}^2 \sin (\alpha - \beta) \cos (\alpha - \beta) \,, \text{ for } (ij) = (23) \end{aligned}$$

at three thresholds, it gives rise to T-reversal non-invariant pieces. Other terms such as  $|\Im c_{ij}^{(0)}|^2$  are even in Majorana phases.

With neutrino helicity summation,

$$\begin{split} &\sum_{h} v_{1}^{\dagger} \sigma^{k} u_{2} u_{2}^{\dagger} \sigma^{l} v_{1} = \\ &- \delta_{kl} \frac{1}{2} (1 - \frac{\vec{p_{1}} \cdot \vec{p_{2}}}{E_{1} E_{2}}) - \frac{p_{1k} p_{2l} + p_{1l} p_{2k}}{2E_{1} E_{2}} - \frac{i}{2} \epsilon_{klm} (\frac{\vec{p_{1}}}{E_{1}} - \frac{\vec{p_{2}}}{E_{2}})_{m} \\ &\sum_{h} v_{2}^{\dagger} \sigma^{k} u_{1} u_{2}^{\dagger} \sigma^{l} v_{1} = -\frac{m_{i} m_{j}}{2E_{1} E_{2}} \delta_{kl} \\ &\sum_{h} v_{1}^{\dagger} \sigma^{0} u_{2} u_{2}^{\dagger} \sigma^{k} v_{1} = \frac{1}{2} \left( i (\frac{(\vec{p_{1}} \times \vec{p_{2}})_{k}}{E_{1} E_{2}} + (\frac{\vec{p_{1}}}{E_{1}} + \frac{\vec{p_{2}}}{E_{2}})_{k} \right) \\ &\sum_{h} v_{1}^{\dagger} \sigma^{k} u_{2} u_{2}^{\dagger} \sigma^{0} v_{1} = \frac{1}{2} \left( i (\frac{(\vec{p_{1}} \times \vec{p_{2}})_{k}}{E_{1} E_{2}} - (\frac{\vec{p_{1}}}{E_{1}} + \frac{\vec{p_{2}}}{E_{2}})_{k} \right) \end{split}$$

Cancellation of leading CP-odd quantity due to

$$\int dP_{\nu}(\frac{\vec{p}_{1}}{E_{1}} - \frac{\vec{p}_{2}}{E_{2}}) = -\frac{\vec{k}}{2} \int dP_{\nu} \left(\frac{E_{1} - E_{2}}{E_{1}E_{2}} \frac{\Delta(\Delta - 2\omega)}{\omega^{2}} - \frac{m_{1}^{2} - m_{2}^{2}}{\omega^{2}} \frac{\Delta - \omega}{E_{1}E_{2}}\right) = 0$$
$$dP_{\nu} = d^{3}p_{1}d^{3}p_{2}\delta(\vec{k} + \vec{p}_{1} + \vec{p}_{2})\delta(\Delta - \omega - E_{1} - E_{2})$$

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## Enhanced RNPE by macro-coherence

- Single photon SR: coherence region limited by wavelength^2 x linear size of excited region
- When many photons or photon+neutrino pair are involved, coherence region may become macroscopic, due to  $\left\|\sum_{k=1}^{N} \exp\{i(\vec{k_1}+\vec{k_2})\vec{r_i}\}\right\|^2 \Rightarrow N^2 \text{ if } \vec{k_1}+\vec{k_2}=0$
- 1. Xe etc implanted in nano-space such as solid matrix
- 2. N encapsulated in fullerene
- 3. Pair annihilation in p-n junction

Energy, momentum both conserved, giving 6 pair threshold of photon energy

Rate ~ volume



### Superradiance: 2 level and 1 photon case



1916-1997







Figure 2.2. Oscilloscope trace of the super-radiance pulse observed by Skribanowitz *et al* [SHMP73] in HF gas at 84  $\mu$ m ( $J = 3 \rightarrow 2$ ), pumped by the  $R_1(2)$  laser line, and the theoretical fit. The parameters are; pump intensity I = 1 kW cm<sup>-2</sup>, p = 1.3 mTorr, L = 100 cm. The small peak on the oscilloscope trace at t = 0 is the 3  $\mu$ m pump pulse, highly attenuated.



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# Theoretical understanding



Maxwell-Bloch equation

 $\frac{\partial \rho_{ee}}{\partial t} = \frac{id}{\hbar} \mathcal{E}(\rho_{ge} - \rho_{eg})$  $\frac{\partial \rho_{gg}}{\partial t} = -\frac{id}{\hbar} \mathcal{E}(\rho_{ge} - \rho_{eg})$  $\frac{\partial \rho_{eg}}{\partial t} = -i\omega_0 \rho_{eg} + \frac{id}{\hbar} \mathcal{E}(\rho_{gg} - \rho_{ee})$  $\frac{\partial^2 \mathcal{E}}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \mathcal{E}}{\partial t^2} = \frac{4\pi}{c^2} \frac{\partial^2 \mathcal{P}}{\partial t^2}$ 

## Numerical solution of MB equations: 1+1 dim.

#### Field intensity at each location



#### State occupancy and coherence



## Our observation of SR in Rb gas





# Target atom for RNPE of large rate



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### Rates and energy spectrum

With soliton formation,

$$\Gamma = \frac{13\alpha G_F^2 \langle x \rangle^2 \Delta^4}{54\pi^2} nN \times O[10^4] \sim 6 \times 10^{-4} \,\mathrm{Hz} \, (\frac{\Delta}{10 \mathrm{eV}})^4 (\frac{\langle x \rangle}{10^{-8} \mathrm{cm}})^2 (\frac{n}{10^{22} \mathrm{cm}^{-3}})^2 \frac{V}{\mathrm{cm}^3}$$

Xe implanted with a fraction  $10^{-3}$  in 100 gr para-H<sub>2</sub> (lattice constant  $3.8 \times 10^{-8}$  cm) gives  $nN = 1.1 \times 10^{45}$  cm<sup>-3</sup>, which then implies rate of 0.15 Hz.

10^-4-1 Hz for Xe including CG's



The closer of level energy to the neutrino mass sum, the better

# Normal vs inverted hierarchy



Figure 1: Assumed neutrino masses are 50, 10, 1 meV for the normal hierarchy, and 51, 50, 10 meV for the inverted hierarchy, with mixing angles,  $\sin^2 \theta_{12} = 0.3$ ,  $\sin^2 \theta_{13} = 0.039$ , and  $\eta = \pi/4$ .

We can equally well investigate both.

## Angle dependence



Figure 2: Xe spectral rate;  $\theta_{13}$  dependence. Figure 1 expanded. Assumed neutrino masses are 1meV, 10 meV, 50meV, with mixing angles,  $\sin^2 \theta_{12} = 0.3$ .

## • (33) threshold insensitive to ¥theta\_13

# M/D distinction



5% effect for atomic energy difference < 1 eV

Parity non-conservation: evidence for weak process

observables:

- 1. photon energy (with good resolution)
- 2.photon circular polarization



E-direction to be tilted from perpendicular direction

### Angular asymmetry and circular polarization for Xe



1 meV, 10 meV, 50 meV, with mixing angles,  $\sin^2 \theta_{12} = 0.3$ ,  $\sin^2 \theta_{13} = 0.039$  in the normal hierarchy case

PV > 0.1 effect

### Further enhancement and background rejection; Photonic soliton formation

- Topological objects classified by winding number, condensed field + atomic polarization
- Macro-coherence by 10<sup>4</sup> x N<sup>2</sup>
- Suppress 2 gamma mode, but may lead to RNPE







### Summary: small scale particle physics experiments using atoms; new principles involved

Decay from metastable atoms emitting neutrino pair

 $\theta_{13}$ 

 $|e\rangle \rightarrow |g\rangle + \gamma + \nu_i \nu_j$ Measurable quantities 1. Photon energy spectrum 6 threholds; mass and angle dependent

$$\omega_{ij} = \frac{\Delta}{2} - \frac{(m_i + m_j)^2}{2\Delta}$$

2. Parity violation: angular asymmetry from oriented atoms circular polarization



 $|n\rangle$ 

 $|e\rangle \rightarrow |g\rangle + \gamma + \gamma \gamma$  $|e\rangle \rightarrow |g\rangle + \gamma + \gamma$ 

Observability of relic neutrino w. T. Takahashi hep-ph/0703019

## • Pauli blocking effect

$$\Gamma^{M}(\omega; T_{\nu}) = \frac{4G_{F}^{2}F_{0}}{\pi\omega^{2}\Delta\omega} \frac{\gamma_{r}}{\gamma} \sum_{ij} \theta(\omega - \Delta_{fi} - m_{i} - m_{j}) \times \int_{m_{i}}^{\omega - \Delta_{fi} - m_{j}} dE_{1}I(E_{1}) (1 - f_{i}(E_{1})) \left(1 - f_{j}(\omega - \Delta_{fi} - E_{1})\right) \\ I(E_{1}) = k_{0}^{ij}E_{1}(\omega - \Delta_{fi} - E_{1})\sqrt{(E_{1}^{2} - m_{i}^{2})\{(\omega - \Delta_{fi} - E_{1})^{2} - m_{j}^{2}\}} \\ + k_{M}^{ij}\delta_{ij}m_{i}m_{j}\sqrt{(E_{1}^{2} - m_{i}^{2})\{(\omega - \Delta_{fi} - E_{1})^{2} - m_{j}^{2}\}}$$



## Distribution function near p=0

#### • Relic neutrino distribution

After the freeze-out at  $\approx 1 MeV,$  neutrinos obey shifted thermal distribution with finite masses;

$$\begin{pmatrix} \frac{\partial}{\partial t} - \frac{\dot{a}}{a}p\frac{\partial}{\partial p} \end{pmatrix} f(\vec{p}) = 0$$

$$f(\vec{p}) = \frac{1}{e^{\sqrt{\vec{p}^2 + (m/(z+1))^2/T_0} + 1}}, \quad z+1 = \frac{T_d}{T_0}$$

$$k_B T_{\nu} \approx (\frac{11}{4})^{1/3} T_{\gamma} \approx 1.9K \approx 0.17 meV$$

$$(1-f_i)(1-f_j) = \frac{1}{(1+e^{-m_i/T_d})(1+e^{-m_j/T_d})} \sim \frac{1}{4} + \frac{m_i + m_j}{8T_d}.$$

Here

$$\frac{m_i}{T_d} \approx 5 \times 10^{-10} \frac{m_i}{1 meV} \frac{2 MeV}{T_d} \,,$$

 $p = \sqrt{E^2 - m^2}$  to be used Essentially m/T\_0 is sensitivity on mass

Threshold reduction 1/2x1/2 = 1/4Temperature measurement possible ? Case of laser irradiated pair emission



Photon energy

For m\_1 < 1meV, temperature measurement is not difficult

## Experimental strategy

- Verification of superradiance enhancement in 2 gamma EM transition
- Discovery of neutrino pair emission far away from threshold region, with large rates
- Approach to threshold region for neutrino spectroscopy
- Detection of relic neutrino at lightest threshold



SPAN collaboration



### Present status of experiments

- Detection of SR
- @okayama Ar-matrix
  - @ kinki Ne/ Ar-matrix Xe implanted





Para-H\_2 matrix @UBC

## Evidence for Xe implantation in para-H\_2

In literature

Our result



Fig. 2. Infrared absorption spectra in the 4480–4490 cm<sup>-1</sup> region recorded at 2.0 K for as-deposited samples. Trace  $(pH_2)$  is for a 2.8(1) mm thick neat  $pH_2$  solid containing 100 ppm of  $oH_2$ . The other spectra are Rg atom doped samples with thicknesses and Rg atom concentrations as follows (Ne) 2.8(1) mm, 1000 ppm, (Ar) 1.8(1) mm, 1300 ppm, (Kr) 1.6(1) mm, 440 ppm, and (Xe) 2.5(1) mm, 260 ppm.



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Different impurity can be detected by different satelite sturucture 2009.07.17@ICTP M. Yoshimura

# Summary

- Discussed a new possibility of using macro-coherent atomic targets of large density
- Excellent for neutrino mass spectroscopy giving 3 masses and 3 angles, along with M/D distinction
- Soliton formation gives extra enhancement
- PV quantity measurable
- If works ideally, a long path towards relic detection Our result



# Back up

## Backgrounds (in case of Xe in p-H2)

### • Spontaneous emission (1)

- The excited level would emit 8.4eV photons.
- Then they might be converted to 4.2eV photons via inelastic scattering with detector materials.
- > Detector's angular acceptance  $(10^{-3})$ , and spectrometer band pass  $(\Delta\lambda=0.1$ nm)

### Spontaneous emission (2)

Severe ssion of 4.2eV photons due to Breit-Physics BG ner tail.

Detector's angular acceptance (10<sup>-3</sup>) BG rate would be similar to signal rate for 300cc p-H2 target.



### Spontaneous Emission



## Concrete ^131 Xe calculation

Xe: F = 7/2, M = -1/2

$$\begin{pmatrix} \cos \eta | F, M \rangle \\ \\ \\ + \sin \eta | F - 1, M + 1 \rangle \end{pmatrix} \xrightarrow{\rightarrow} \begin{cases} |F - 1, M - 1 \rangle \\ |F - 1, M \rangle \\ |F - 1, M + 1 \rangle \\ |F - 1, M + 2 \rangle \end{cases} \xrightarrow{\rightarrow} \begin{cases} |F - 2, M - 1 \rangle \\ |F - 2, M \rangle \\ |F - 2, M + 1 \rangle \\ |F - 2, M + 2 \rangle \end{cases}$$

#### 131Xe 5p6(2P3/2)6s 2[3/2]2



⊠ 1: Xe energy level for radiative neutrino pair emission

### Odd Xe for PV <sup>131</sup>Xe 5p<sup>6</sup>(<sup>2</sup>P<sub>3/2</sub>)6s <sup>2</sup>[3/2]<sub>2</sub> level hyperfine structure in an external magnetic field



State mixture at 1.5 kG

### Angular distribution of specific circular polarization



$$A(\theta) = \frac{s(a_3c^3 + a_1c)}{b_4c^4 + b_2c^2 + b_0}$$

Circular polarization

$$P(\theta) = \frac{s(f_2c^2 + f_0)}{b_4c^4 + b_2c^2 + b_0}$$
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#### Numbers to memorize

$$\begin{split} &\frac{G_F^2(10\text{eV})^4}{3\pi^3}\frac{d^2nN}{10^8cm^{-1}10^{22}}\sim 6.45\times 10^{-4}\text{sec}^{-1}\\ &\text{Xe atomic states} \\ &|i\rangle=5p^5(^2P_{3/2})6s^2[3/2]_2\,,\quad\text{metastable with lifetime }O[40]\,\text{sec}\\ &|n\rangle=5p^5(^2P_{3/2})6s^2[3/2]_1\,,\quad\frac{1}{\tau}\sim 2.8\times 10^8\text{sec}^{-1}\,,\quad|f\rangle=5p^{6\,1}S_0\\ &\Delta_{ni}\sim 0.12\text{eV}\,,\quad\Delta_{nf}\sim 8.4\text{eV}\,,\quad\text{Ionization energy}\sim 13.4\text{eV} \end{split}$$