



*The Abdus Salam  
International Centre for Theoretical Physics*



**2047-38**

**Workshop Towards Neutrino Technologies**

*13 - 17 July 2009*

**Stellar tomography with high energy neutrinos**

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# Stellar Tomography with High Energy Neutrinos

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*Workshop Towards Neutrino Technologies*

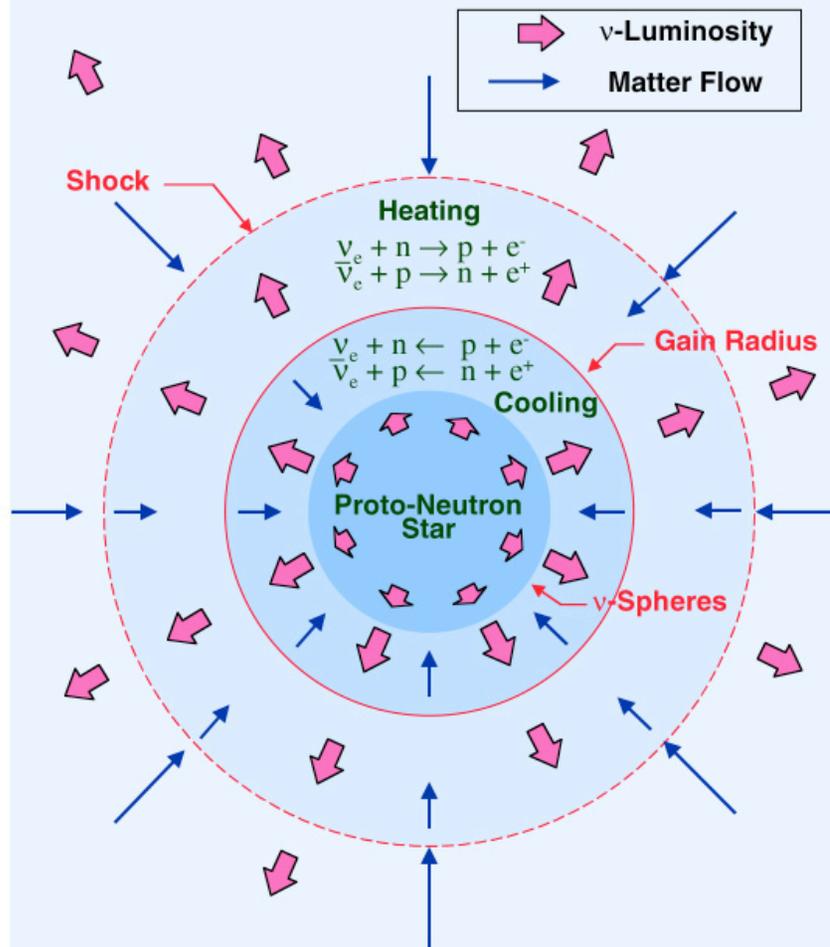
*The Abdus Salam International Centre for Theoretical Physics,*

*Trieste, Italy. 13-17 July, 2009*

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# Core Collapse Supernovae

## Standard Textbook picture



## ... and some details

- ❑ Fe core collapse of  $>8M_{\odot}$  stars
- ❑  $\sim 10^{54}$  erg of energy release in  $\nu$ 's
- ❑ Thermal  $\sim 10$  MeV  $\nu$ 's
- ❑ Detection from SN 1987A
- ❑ Rate: 1 Snu =  $10^{-2} \text{ yr}^{-1} 10^{-10}$  blue  $L_{\odot}$  or 1/yr within 20 Mpc (4000 galaxies)
- ❑ Can provide information on stellar collapse and on  $\nu$  properties

*No detection since 1987*

*Look for high energy  $\nu$  signature to probe stellar interior in the rarer cousin of SNe →*

# Gamma Ray Bursts

*Collapsar Model: Pioneered by Stan Woosley and collaborators*

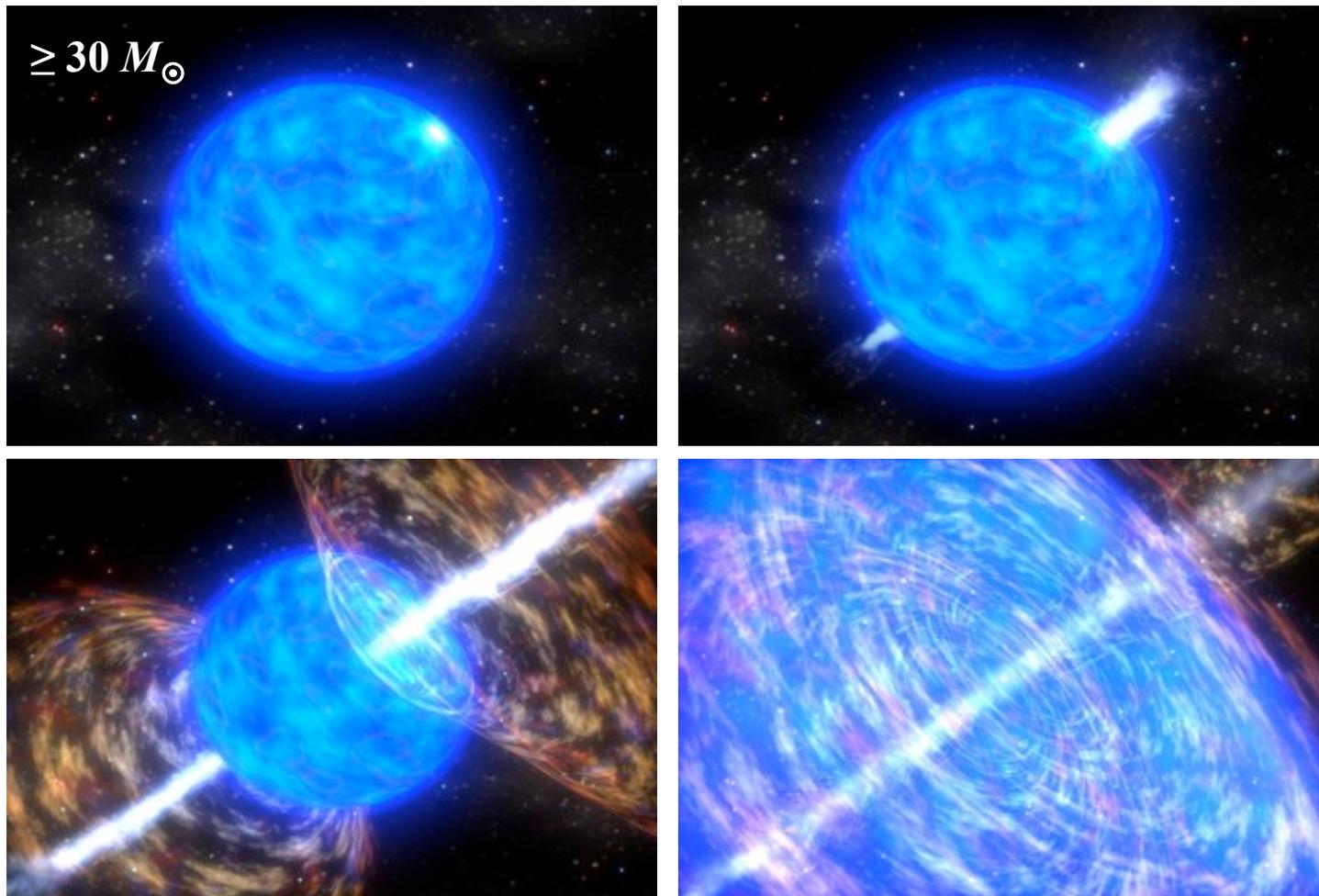


Illustration credits: NASA

# Relativistic Jet in Gamma Ray Bursts

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*Simulation by Zhang & Woosley*

Central  
Engine

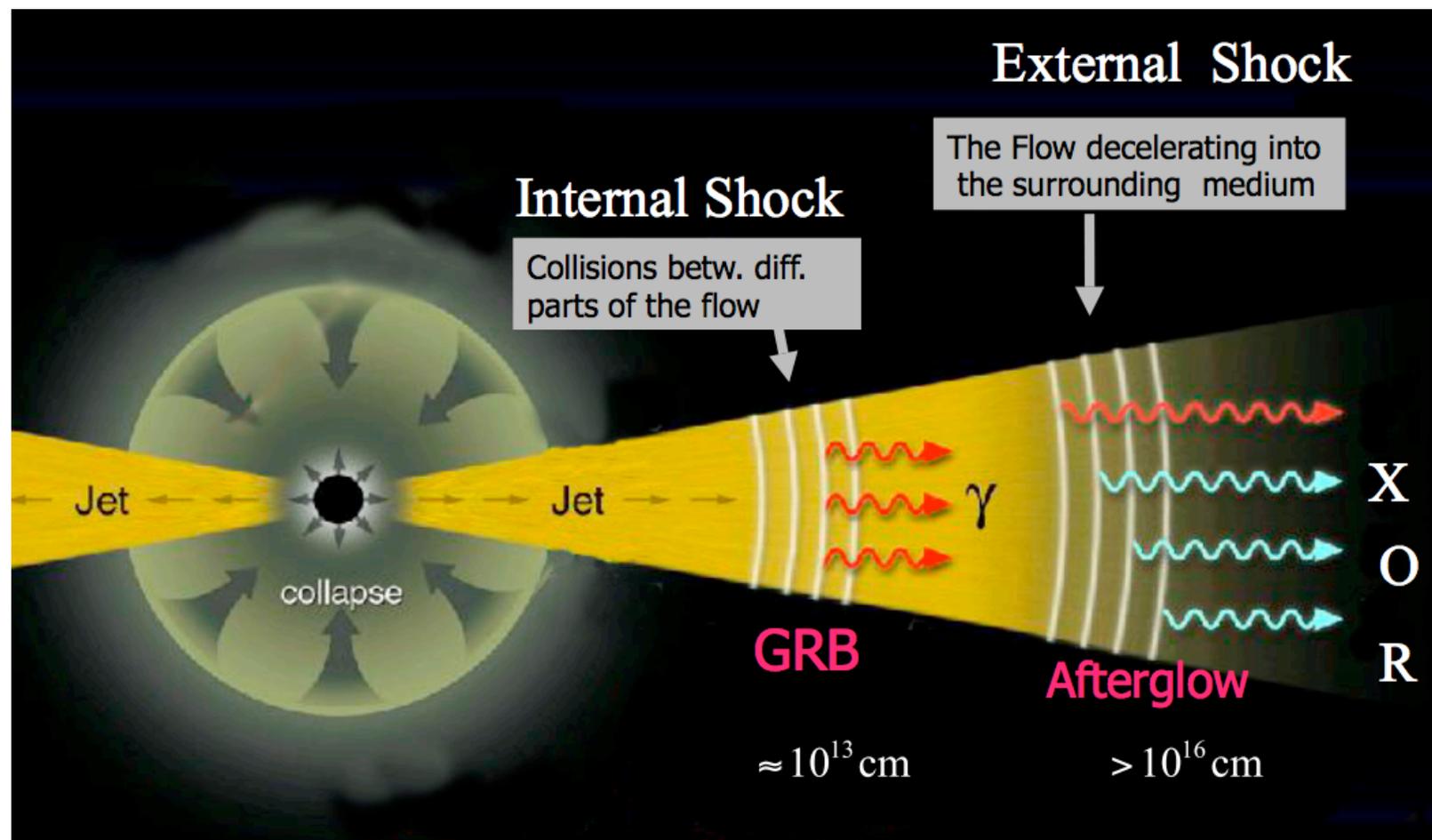


Black hole/  
Highly  
magnetized  
Neutron star



# GRB Fireball Shock Model

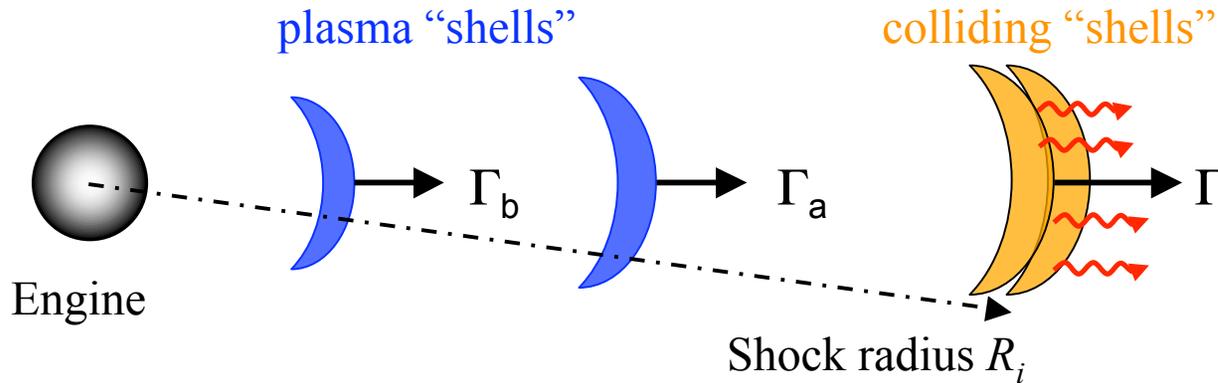
*Rees, Meszaros, Piran and others ...*



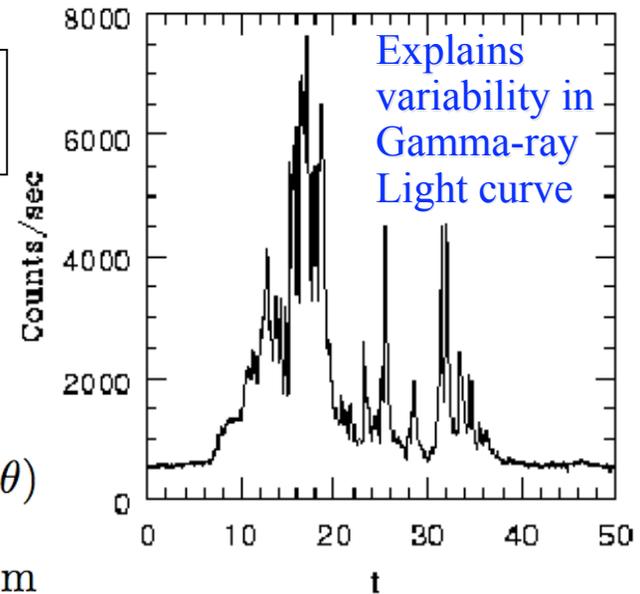
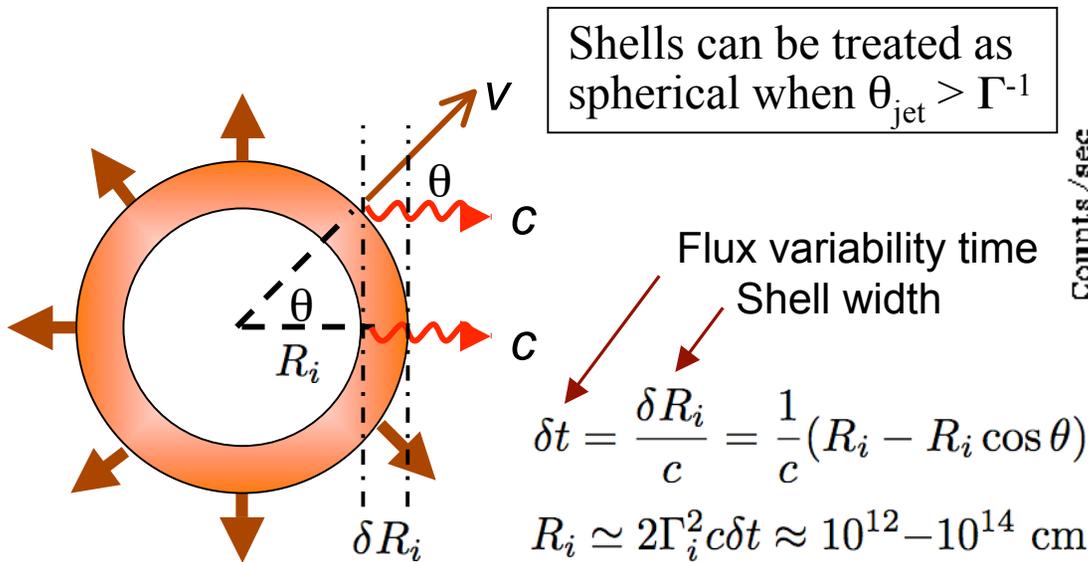
*Explains non-thermal prompt MeV data and afterglow X-ray, UV, ... data*

# Explanation of $\gamma$ -ray Lightcurve

*Simplest form ...* Discrete outflow or “shells” with variable speeds or  $\Gamma$



Synchrotron radiation by electrons that are accelerated in the induced electric field



# Baryons are Essential in GRB Jet

Generation of “shells” with variable  $\Gamma$

Entropy:  $\eta = L_0 / \dot{M} c^2 \geq 100$

$$\dot{M} = 4\pi R^2 n'_p m_p c$$

↑  
Density of protons

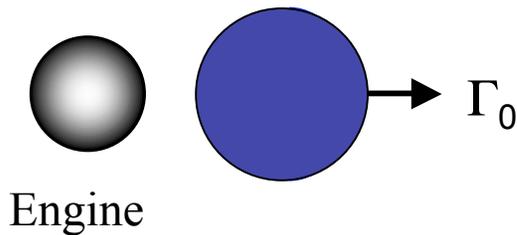
Impulsive injection of energy (fireball)

*Cavallo & Reese 1976*

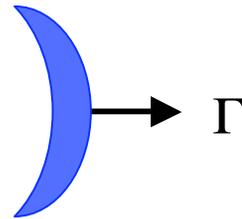
Expansion due to radiation pressure

Coasting fireball

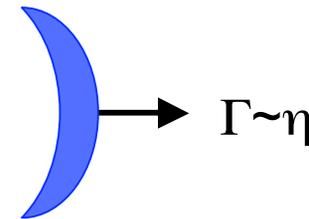
colliding “shells”



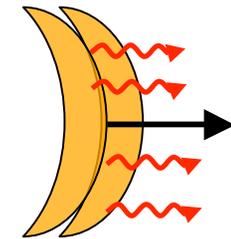
Base of the jet  
 $R_0 \sim 100$  km  
High temperature  
 $T_0 \sim 10$  MeV  
 $e, \gamma$  and few  $p$



Kinetic energy ( $L_k$ ) increases, temperature decreases  
 $(L_\gamma + L_k)R \sim L_0 R_0 \sim \text{const.}$   
 $TR \sim T_0 R_0 \sim \text{const.}$   
 $\Gamma \sim R/R_0$



No more radiation pressure, kinetic energy  
 $L_k \sim L_0$   
 $R_s \sim 10^9$  cm

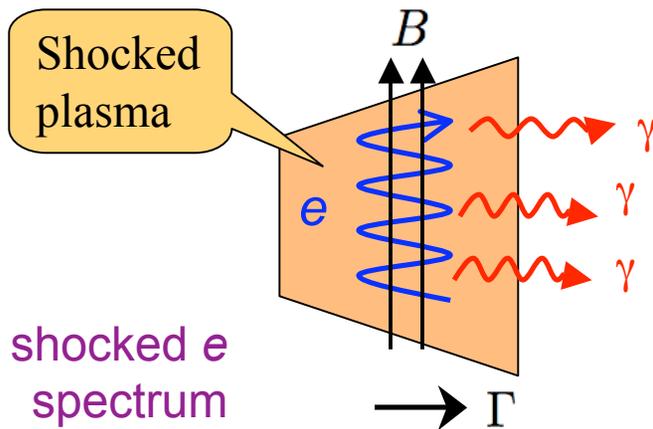


← Still inside the star ( $\sim 10^{11-12}$  cm)!

# Non-thermal $\gamma$ ray Emission Mechanism

Fitted by broken power-laws

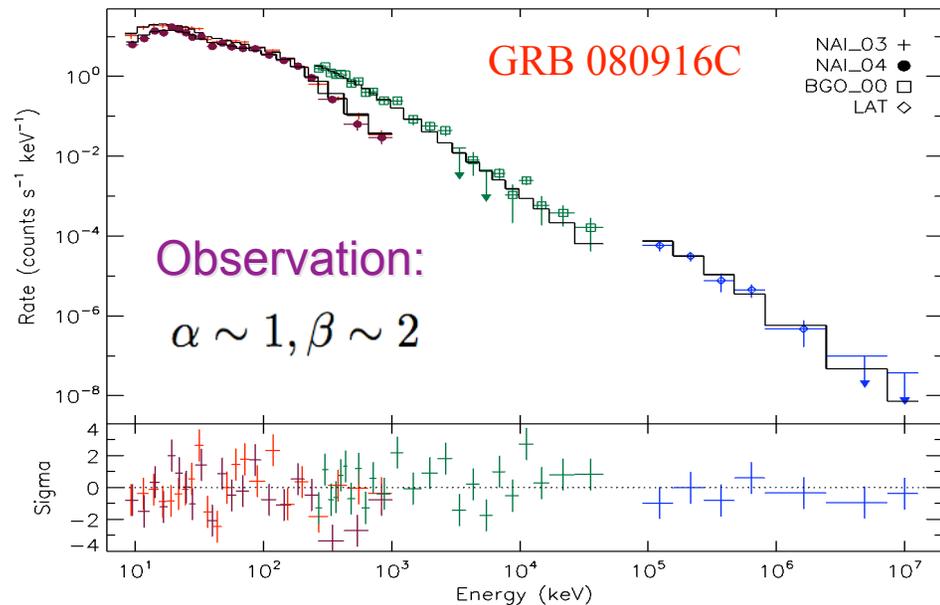
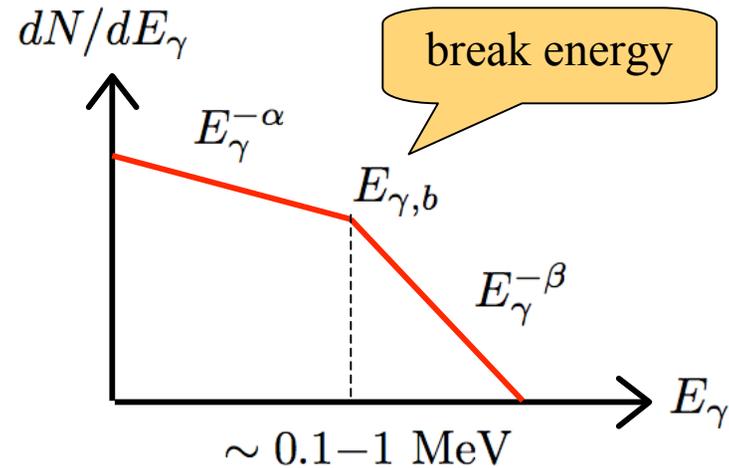
**Origin:** Synchrotron radiation by a population of shock-accelerated electrons



$$\frac{dN}{dE_e} \propto E_e^{-q} \quad \begin{array}{l} \text{All } e \text{ lose energy} \\ \text{Promptly fast cooling} \end{array}$$

Synchrotron radiation spectrum

$$\begin{aligned} \frac{dN}{dE_\gamma} &\propto E_\gamma^{-(q+2)/2} ; E_\gamma > E_{\gamma,b} \\ &\propto E_\gamma^{-2} ; q = 2 \end{aligned}$$



# Evidence of Relativistic Jet

Extreme relativistic motion of the  $\gamma$ -ray emitting region to avoid  $\gamma\gamma \rightarrow e^+e^-$  production (opacity  $\tau_{\gamma\gamma} < 1$ ) in-situ which will destroy non-thermal spectra

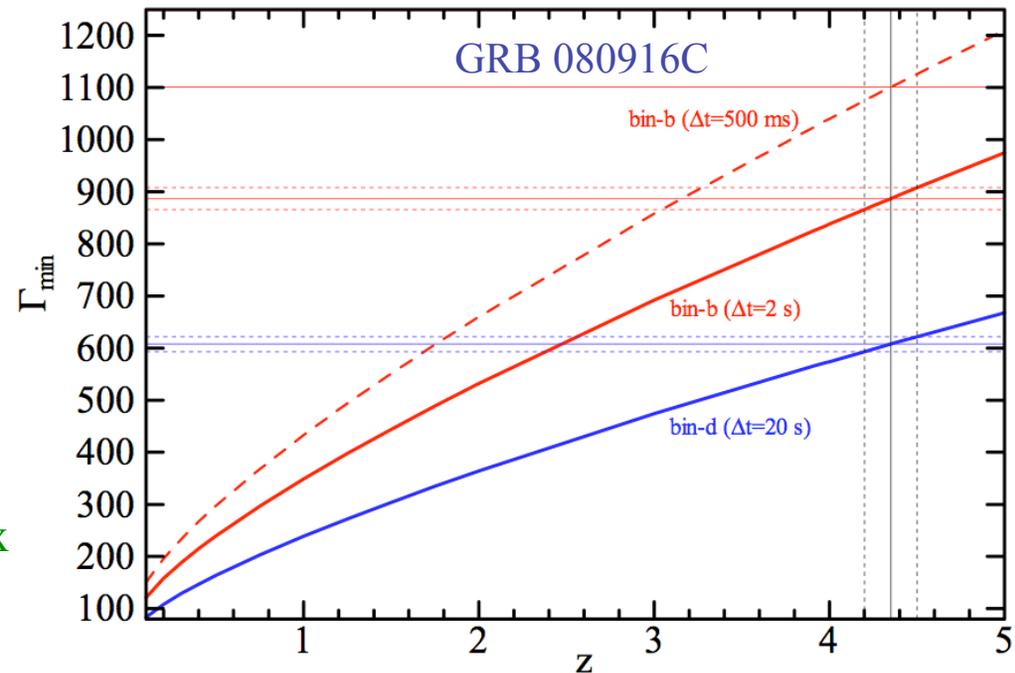
- Constraint on the bulk Lorentz factor:  $\Gamma > 887 \pm 21$  (time bin “b”,  $\Delta t \sim 2$  s) with observed variability time  $\Delta t$  from Fermi GBM or INTEGRAL
- $\Gamma > 1100$  (time bin “b”,  $\Delta t \sim 500$  ms)

- Size scale of prompt emission region is large

$$R \approx \frac{\Gamma^2 c \Delta t}{1+z}$$

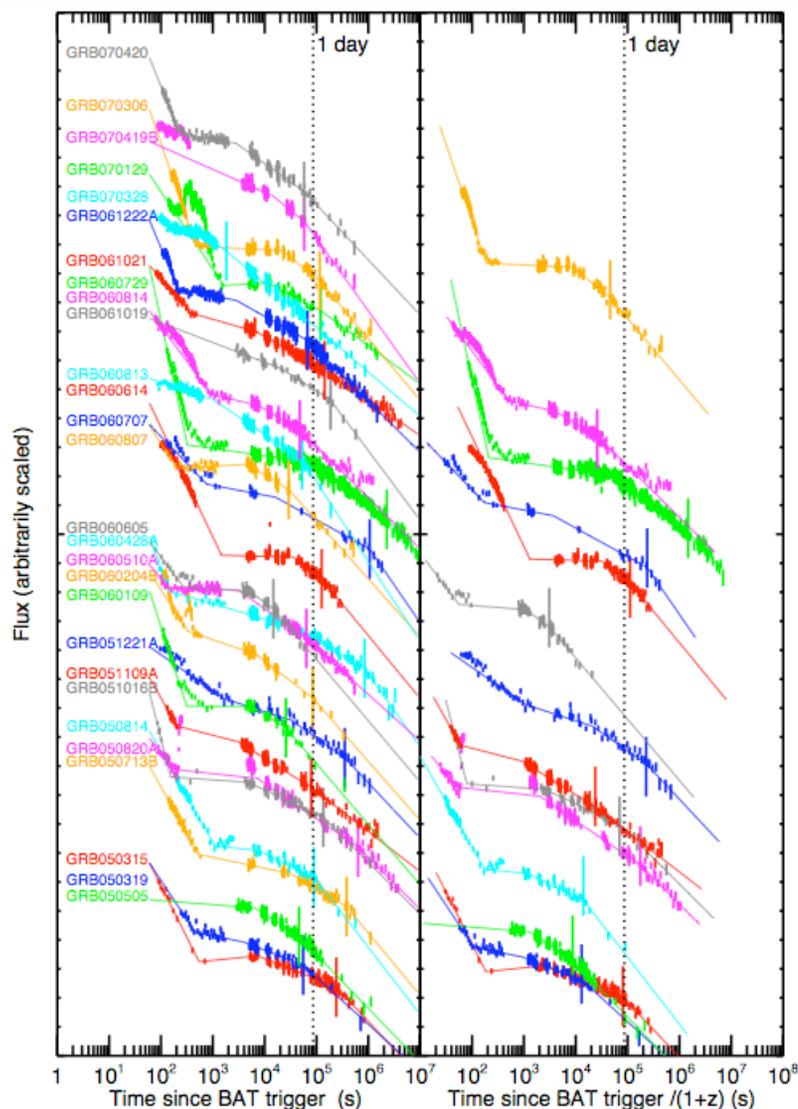
$$> 9 \times 10^{15} \left(\frac{\Gamma}{890}\right)^2 \left(\frac{\Delta t}{2s}\right) \left(\frac{5.35}{1+z}\right) \text{ cm}$$

High bulk Lorentz factor can relax the actual energy emission by up to  $1/\Gamma$  from the observed apparent isotropic  $8.8 \times 10^{54}$  erg



*Abdo et al. Science 2009*

# Further Evidence of Jetted Emission



## ← Afterglow lightcurves of Swift GRBs

*Racusin et al., ApJ 2009*

- ❑ GRB afterglow flux evolution  
 $F \sim t^\alpha \nu^{-\beta}$  initially with  $\alpha, \beta \sim 1$
- ❑ As the jet slows down by external medium the bulk Lorentz factor decreases
  - ➔ smooth light curve as long as  $1/\Gamma < \theta_{\text{jet}}$  or the edge of the jet is not visible
  - ➔ for  $1/\Gamma > \theta_{\text{jet}}$  the slope of the lightcurve changes  
“Jet break”
- ❑ Typically  $\theta_{\text{jet}} \sim 5\text{-}7$  degrees

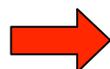
# The most powerful explosion in the universe

keV - MeV  $\gamma$ -ray flux of typical GRBs  $F \sim 10^{-6} - 10^{-5} \text{ erg cm}^{-2} \text{ s}^{-1}$

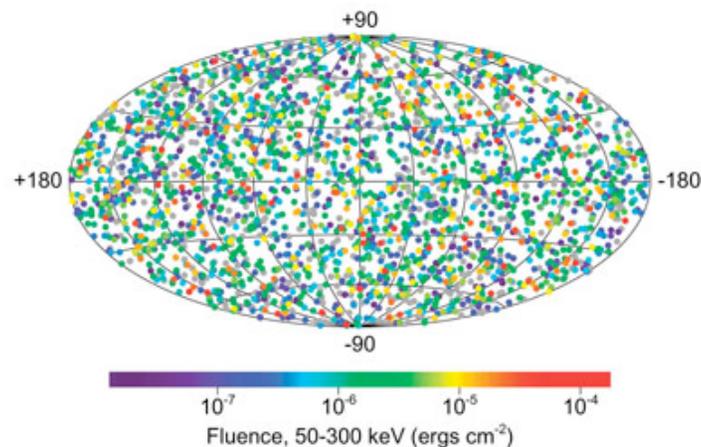
Isotropic distribution in sky

→ Typical redshift  $z \sim 1-2$

→ Huge energy release!



Sky map of 2512 GRBs



*Isotropic-equivalent  $\gamma$ -ray  
luminosity  $4\pi d^2 F \sim 10^{52} \text{ erg s}^{-1}$*

Sizable fraction of a solar rest mass energy release!

Outshines the entire  $\gamma$ -ray universe

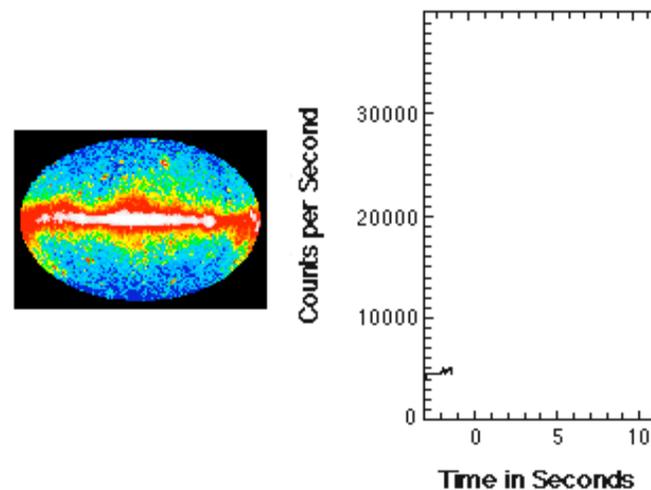


Observed rate: 600  $\text{yr}^{-1}$  over whole sky

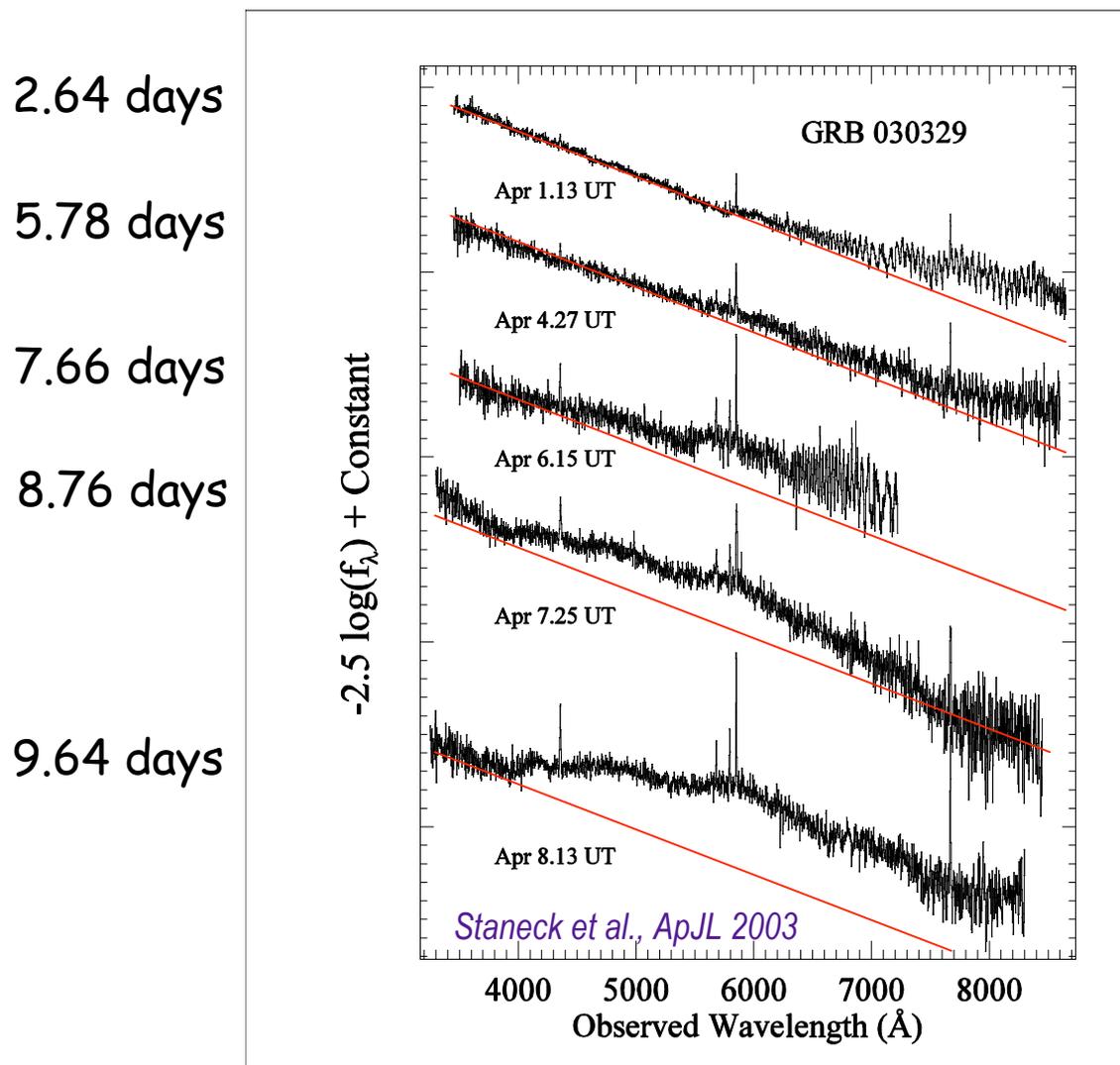
→ 2  $\text{Gpc}^{-3} \text{ yr}^{-1}$  (SN rate  $\sim 10^4 \text{ Gpc}^{-3} \text{ yr}^{-1}$ )

→ 200( $f_b/100$ )  $\text{Gpc}^{-3} \text{ yr}^{-1}$  beam-corrected

→ Follow star-formation rate



# Direct Evidence of SN-GRB Connection



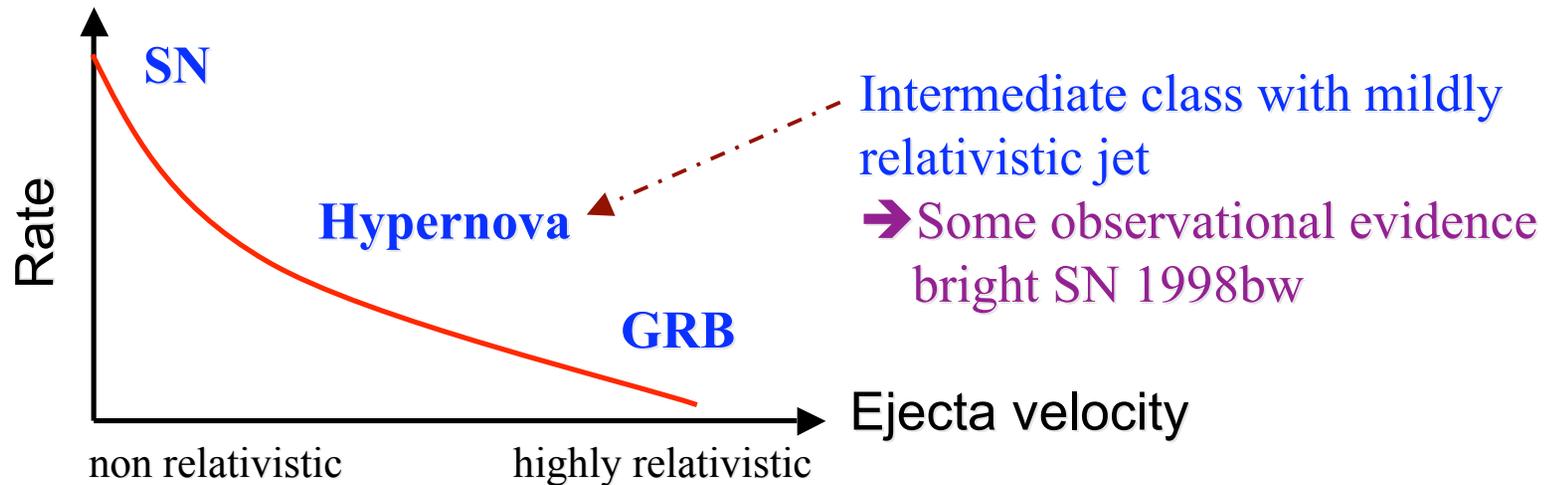
Low redshift ( $<0.2$ )  
GRBs have been  
observed as precursors  
to SNe: GRBs 980425,  
030329, etc.

Typical afterglow  
power-law spectrum

SN bump (SN 2003dh)  
due to radioactivity  
appears later when the  
envelope is optically  
thin to photons as it  
expands

# Core Collapse SN and GRB Relation

- ❖ GRBs and core-collapse SNe are related, both from collapse of massive stars
- ❖ GRBs are rare (few % of SN) → more massive stars are fewer in numbers
- ❖ SN explosions are spherical with sub-relativistic shock velocity
- ❖ GRB jets are highly relativistic → Highly asymmetric explosion



# Stellar Tomography with High Energy $\nu$ 's

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Concentrate on GRBs and jetted SN with jets buried inside stars

- ❖ Shocks in relativistic jets
- ❖ Jet energy estimate from observations
- ❖ Proton acceleration and interactions, neutrino production

Discuss three models

- ❖ **Supernova model** → SN explosion before the GRB event
- ❖ **Choked GRBs** → Relativistic GRB jet while still inside star
- ❖ **Hypernovae** → A fraction of SN which may have mildly relativistic buried jet  
→ Neutrino oscillation physics in play

# Calculation of Energetics in GRB Shocks

Basic calculation approach (*a la Astrophysicists*)

- Collision between two plasma “shells”
  - Relativistic forward & reverse shockwaves plough through the “shells”
  - Plasma instabilities, turbulent motion generate magnetic field
  - Charged particles (*test particle*) are accelerated in the induced electric field via a Fermi mechanism

Non-thermal  $\gamma$ -ray energy density in the jet frame

$$u'_\gamma = \frac{L_\gamma}{4\pi R^2 c \Gamma^2}$$

Observed  $\gamma$ -ray luminosity

Shock radius  $R=2\Gamma^2 ct_v$ ;  
 $\Gamma \sim 100-1000$ ,  $t_v \sim 0.001\text{s}-1\text{s}$

Particle energy density

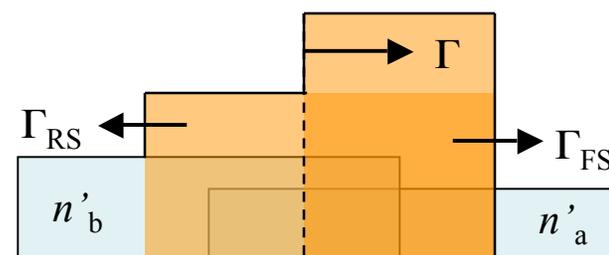
$$u'_p = \varepsilon_e^{-1} u'_e = \varepsilon_e^{-1} u'_\gamma$$

Fast cooling

$$u'_B = \varepsilon_B u'_p = (\varepsilon_B / \varepsilon_e) u'_\gamma$$

Energy density in magnetic field

$\varepsilon_e$  and  $\varepsilon_B$  are parameters to be fitted from data



Collision hydrodynamics

# Proton Acceleration and Cooling

Magnetic field

$$B' = \sqrt{8\pi u'_B} \approx 2 \times 10^6 R_{12}^{-1} \Gamma_{2.5}^{-1} L_{\gamma,52}^{-1/2} \sqrt{\epsilon_B / \epsilon_e} \text{ G}$$

$$R = 10^{12} R_{12} \text{ cm}; \Gamma = 10^{2.5} \Gamma_{2.5}$$

$$L_\gamma = 10^{52} L_{\gamma,52} \text{ erg/s (isotropic)}$$

• Acceleration time

$$t'_{acc} = \frac{\phi E'_p}{ecB'} \approx 1.1 \frac{\phi_1 E'_{p,9}}{B'_6} \text{ sec.}$$

$$E'_p = 10^9 E'_{p,9} \text{ GeV}; B' = 10^6 B'_6 \text{ G}$$

• Synchrotron cooling

$$t'_{acc} = \frac{3}{4} \left( \frac{m_p}{m_e} \right)^2 \frac{m_p^2 c^3}{\sigma_T u'_B E'_p} \approx \frac{0.0045}{B'^2_{p,9}} \text{ sec.}$$

• Compton cooling → may be important if  $u'_B \ll u'_\gamma$

• Photopion production → Dominant channel for high-energy neutrino production

$$p\gamma \rightarrow \Delta^+ \rightarrow n\pi^+ / p\pi^0 \quad \text{at resonance} \quad E_p E_\gamma \simeq 0.3 \text{ GeV}^2$$

• Hadronic interactions  $pp/pn \rightarrow \pi^\pm / K^\pm$

Neutrino production

$$\pi^+ / K^+ \rightarrow \mu^+ \nu_\mu \rightarrow e^+ \nu_e \bar{\nu}_\mu \nu_\mu$$

• Bethe-Heitler process

Similar to atmospheric  $\nu$ 's

Secondaries may suffer further losses

# Supranova GRB Model

Razzaque, Meszaros & Waxman, PRL 2003

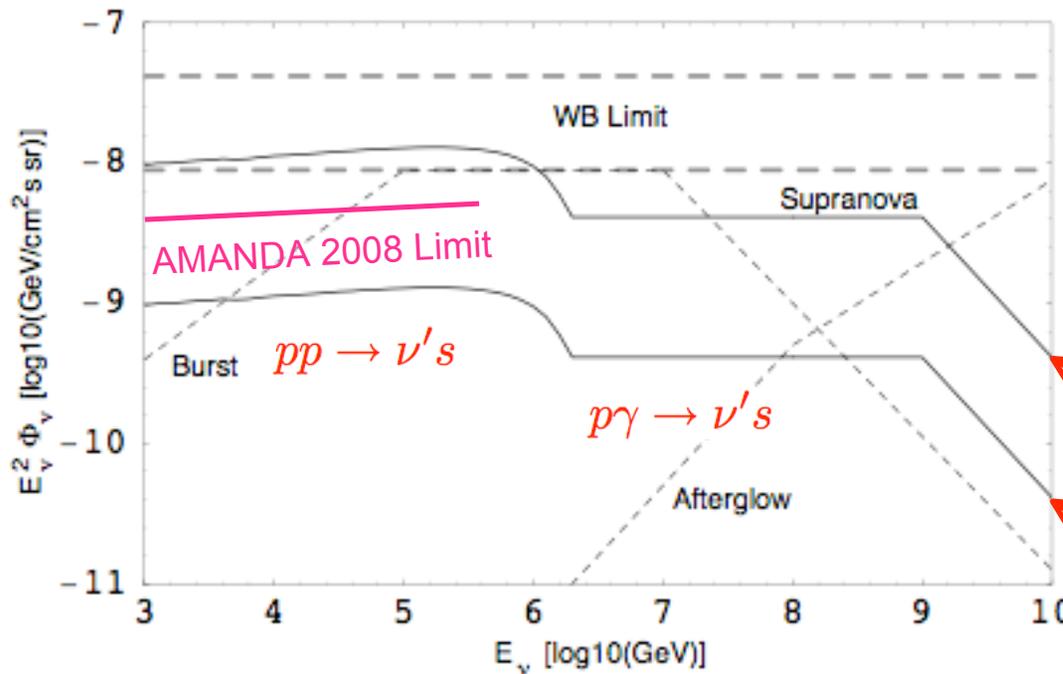
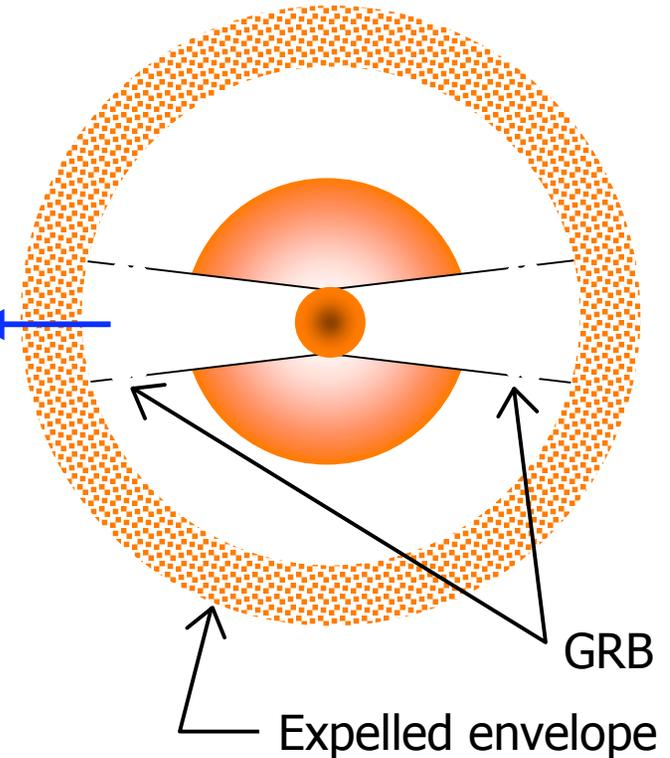
Two step stellar collapse model:

stellar collapse  $\rightarrow$  SN  $\rightarrow$  GRB

Time-delay between SN and GRB  $\sim$  hours-days

- Electromagnetic limit  $\sim$  days
- Neutrinos  $\sim$  hours

$$pp, p\gamma \rightarrow \nu's$$



All GRBs with supranova

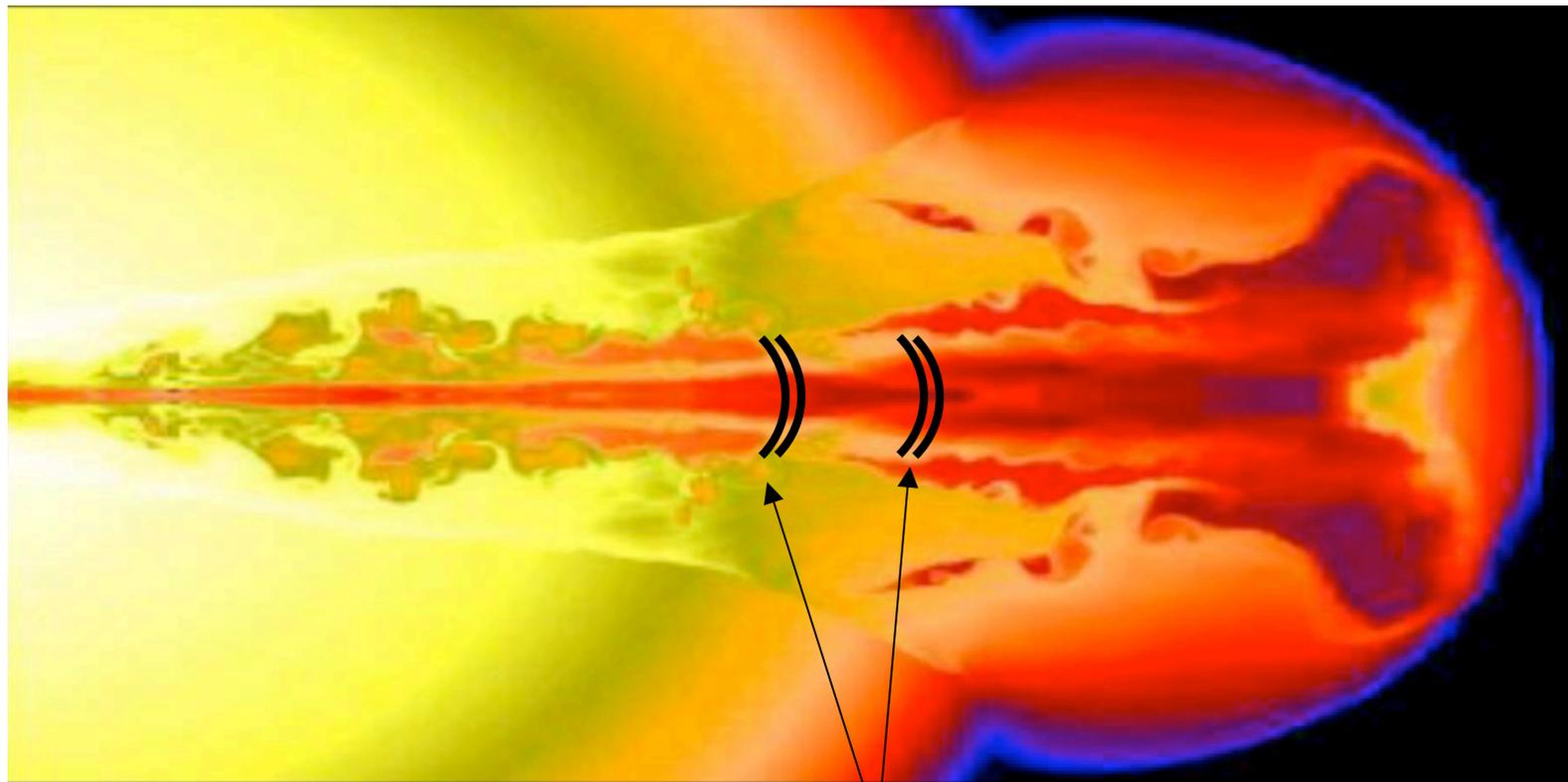
10% GRBs with supranova

# Buried Relativistic GRB Jet

Relativistic GRB-like jet inside star → Successful or *choked* GRB

→ Choked GRBs may be related to orphan afterglows

Shocks in the jet → particle acceleration → high-energy  $\nu$  production



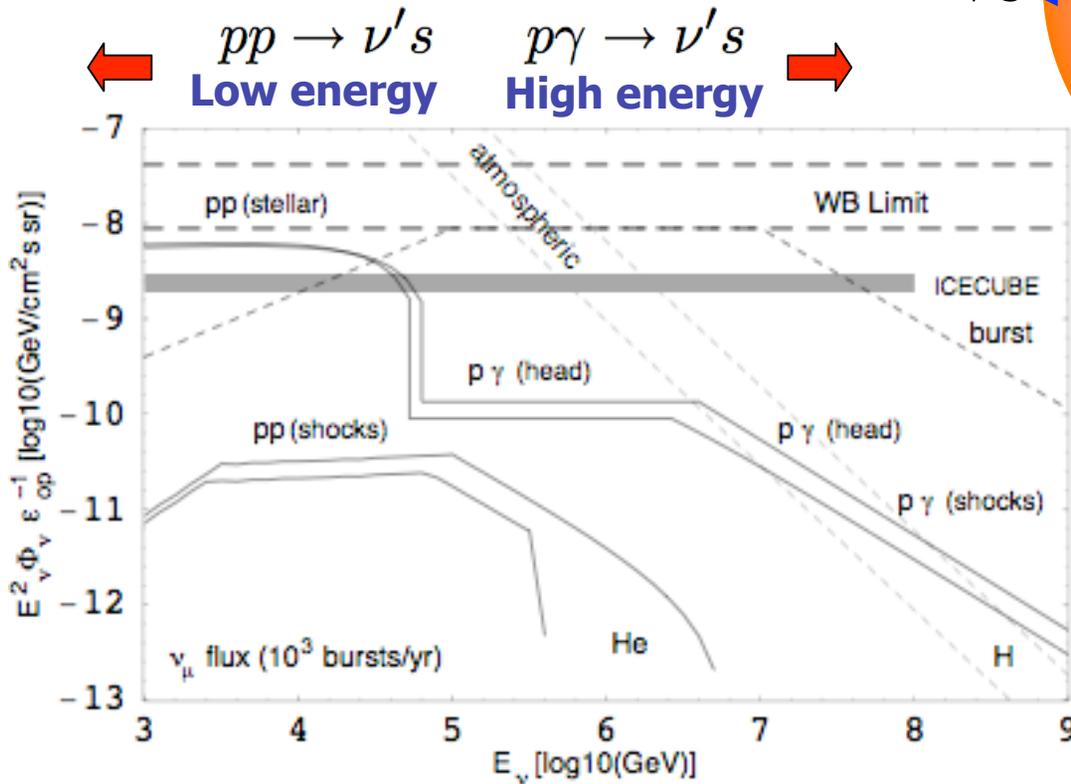
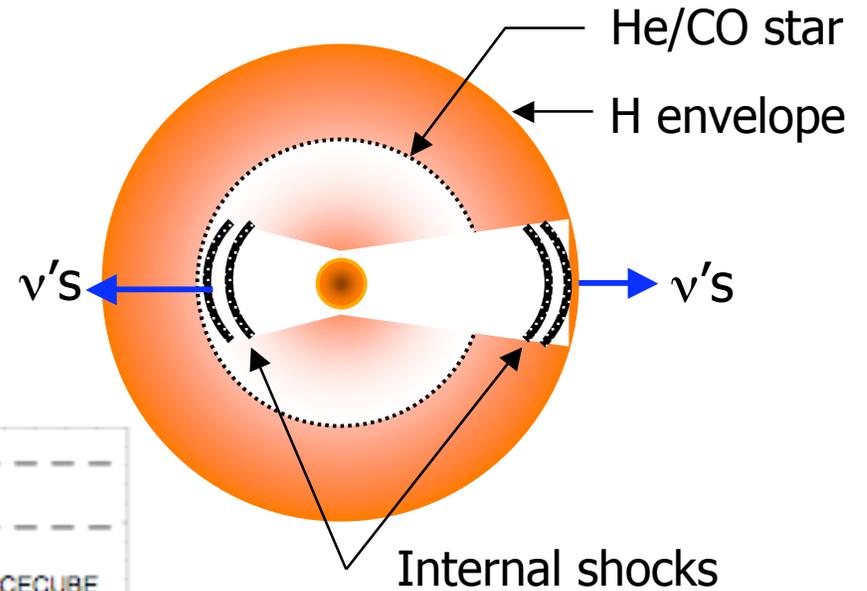
Credits: Zhang & Woosley

Shocks

# $\nu$ 's precursor to GRB or Orphan Afterglow

Razzaque, Meszaros & Waxman, PRD 2003

- Optically thick shocks
- High density of thermal  $\gamma$ -rays and target protons



$$R_i < R_\star \approx \begin{cases} 10^{11} \text{ cm (He)} \\ 10^{12.5} \text{ cm (H)} \end{cases}$$

← Diffuse flux

No. of choked jets can be Larger than the no. of GRBs

# High Energy GRB $\nu$ Detection Prospects

## Projected $\nu$ events for IceCube

Flux model	$\nu_\mu$	$\nu_e$
Precursor I (He)	-	-
Precursor II (H)	4.1	1.1
Burst/prompt	3.2	0.3
Afterglow (ISM)	-	-
Afterglow (wind)	0.1	-
Supranova (>0.1 d)	13	2.4

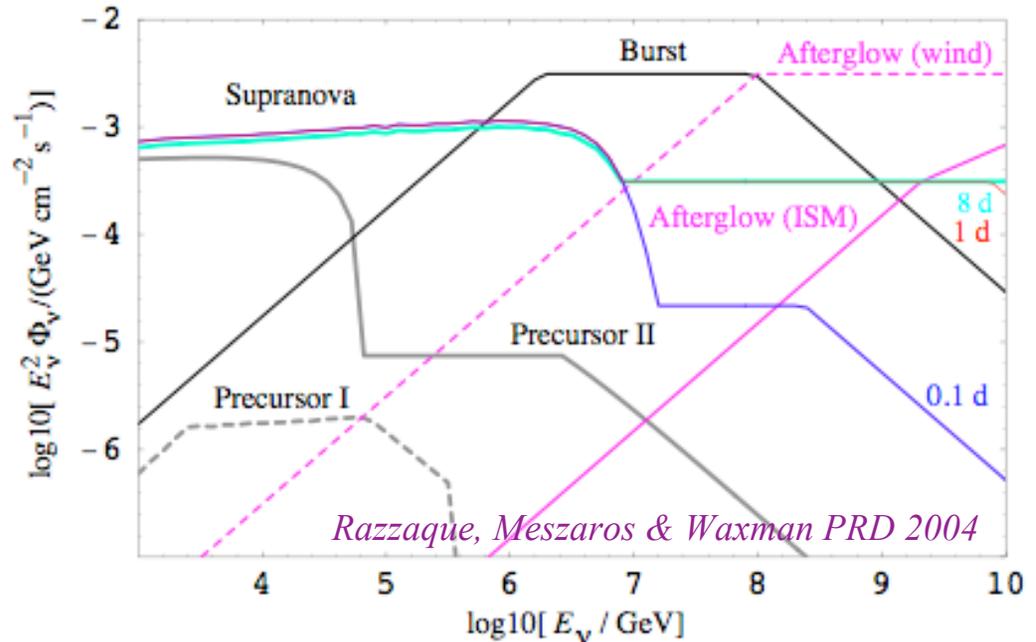
$E_\nu > \text{TeV}$ , no oscillation

## Conclusion

- Distinguish between H and He envelope
- Rule out >0.1 day delay between SN and GRB

## GRB 030329/SN 2003dh

Typical long duration GRB with bright SN  
 $\sim 10^{51}$  ergs/s luminosity at redshift  $z = 0.17$



Neutrino flux models:

*Dai & Lu 2000 (afterglow wind)*

*Razzaque, Meszaros & Waxman, PRL 2003 (supranova)*

*Razzaque, Meszaros & Waxman, PRD 2003 (precursor)*

*Waxman & Bahcall 2000 (afterglow ISM)*

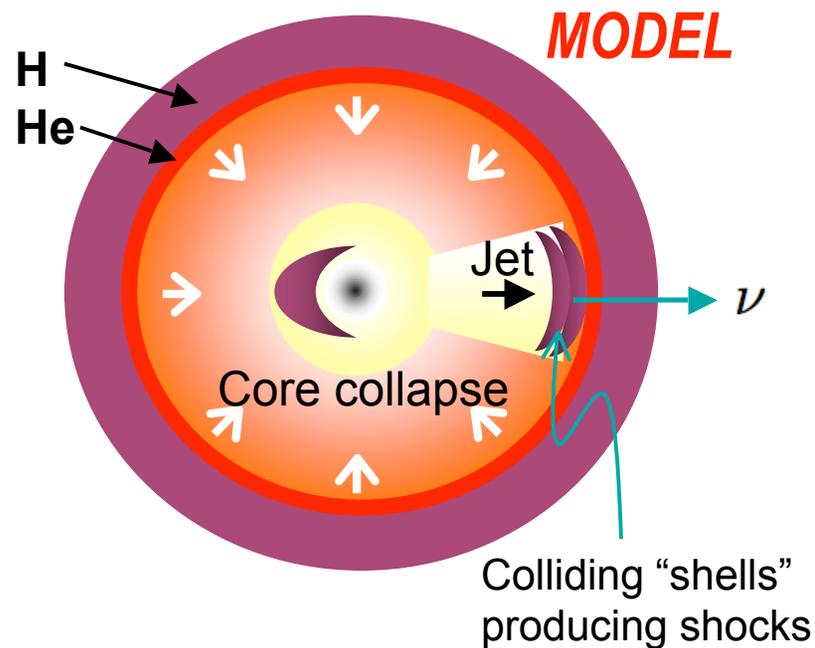
*Waxman & Bahcall 1997 (burst/prompt)*

# Jetted Supernova: Hypernova

*Razzaque, Meszaros & Waxman, PRL 2004*

A dirty fireball model of SN explosion

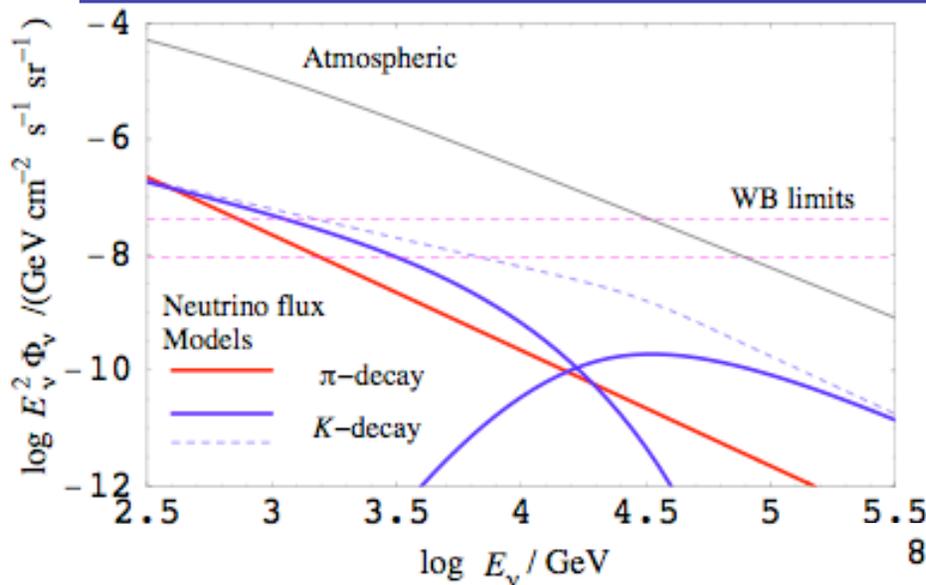
- A weak semi-relativistic jet ( $\Gamma \sim 3$ ) forms after core collapse
- Jet chokes inside



## Motivation

- High expansion velocity (30-40 x 1000 km/s) of SN remnant shell as seen in SN 1998bw
- Radio afterglow not associated with gamma-ray emission
- Asymmetric explosion inferred polarimetry observations of SN type Ib/c

# High Energy $\nu$ 's from Jetted SNe



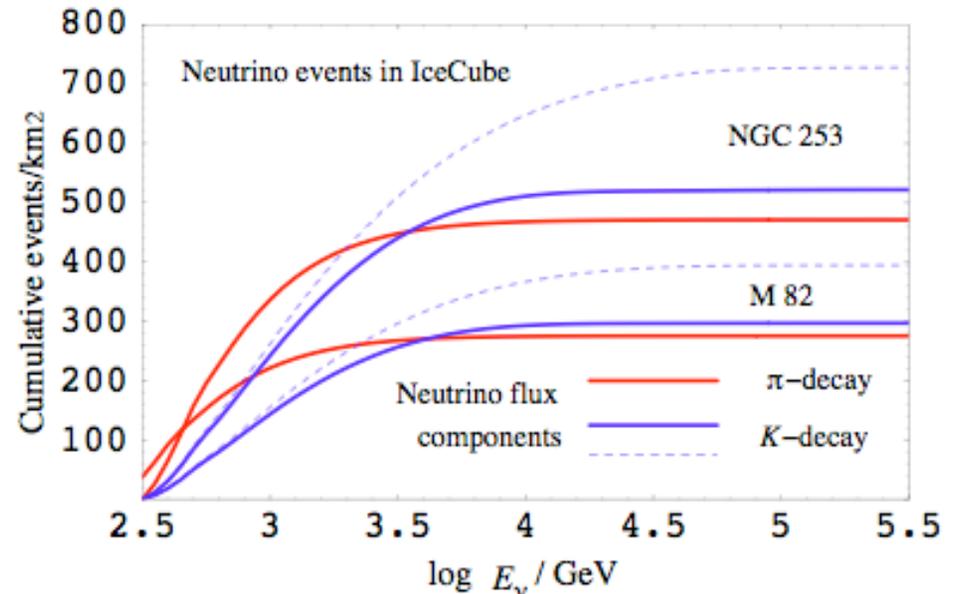
Diffuse Neutrino flux assuming all SNe with semi-relativistic jets

Prospects for individual source detection is much better from hypernovae within  $\sim 20$  Mpc and if their rate is a significant fraction of the SNe rate of 1/yr

*Razzaque, Meszaros & Waxman 2004; 2005*  
*Ando & Beacom 2005*

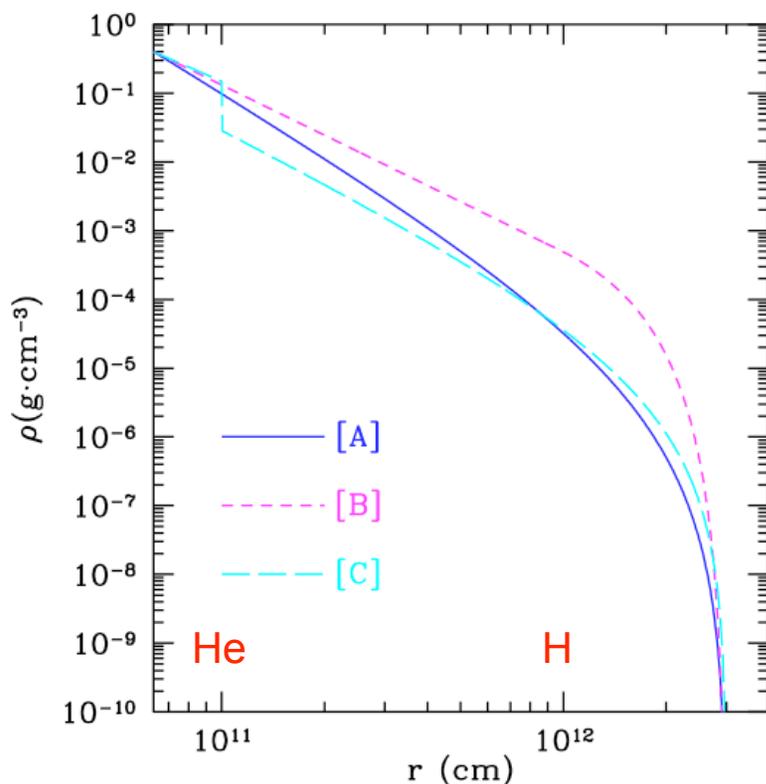
Recent progress by

*Farzan & Smirnov, 2008*  
*Enberg, Reno & Sarcevic, 2009*



# Oscillation Effects on Neutrino Fluxes

*Mena, Mocioiu & Razzaque, PRD 2007*



Density profiles of pre-SN stellar envelopes of a Blue Super Giant

High energy  $\nu$ 's are produced inside the He envelope and propagate through the He and H envelopes

$$N_e = 2.4 \times 10^{23} \text{ cm}^{-3} \text{ at } r = r_{\text{jet}} = 10^{10.8} \text{ cm}$$

Comprehensive study on MSW oscillation effects for thermal SN  $\nu$ 's by *Dighe & Smirnov 2000*

Resonant densities

$$N_e^L = \frac{\Delta m_{\text{sol}}^2 \cos 2\theta_{12}}{2\sqrt{2}G_F E} \simeq \frac{3 \times 10^{23}}{E[\text{GeV}]} \text{ cm}^{-3}$$

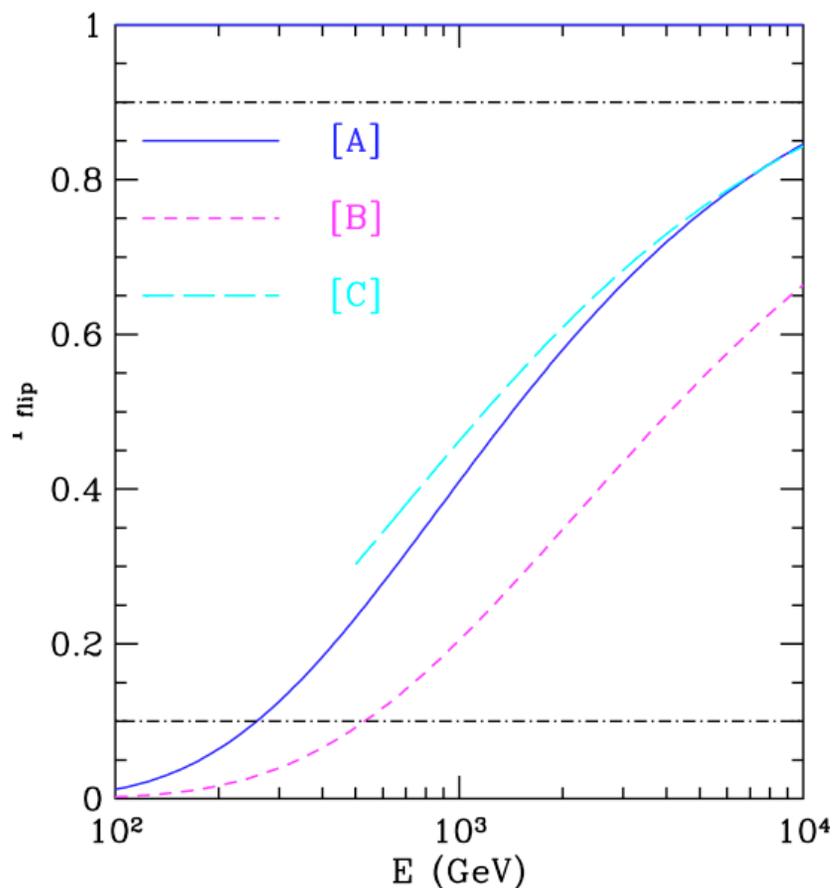
$$\sin^2 2\theta_{13} = 0.15$$

$$N_e^H = \frac{|\Delta m_{\text{atm}}^2| \cos 2\theta_{13}}{2\sqrt{2}G_F E} \simeq \frac{9 \times 10^{24}}{E[\text{GeV}]} \text{ cm}^{-3}$$

→ Expect MSW effect for  $\sim$ TeV  $\nu$ 's

# Numerical Calc. of Oscillation Probabilities

Flip probabilities due to atmospheric transition for  $\sin^2 2\theta_{13} = 0.15$



Transitions are mostly non-adiabatic at  $\sim$ TeV energy due to rapid change in density

- Analytic estimates are unreliable
- Numerically solve propagation equation

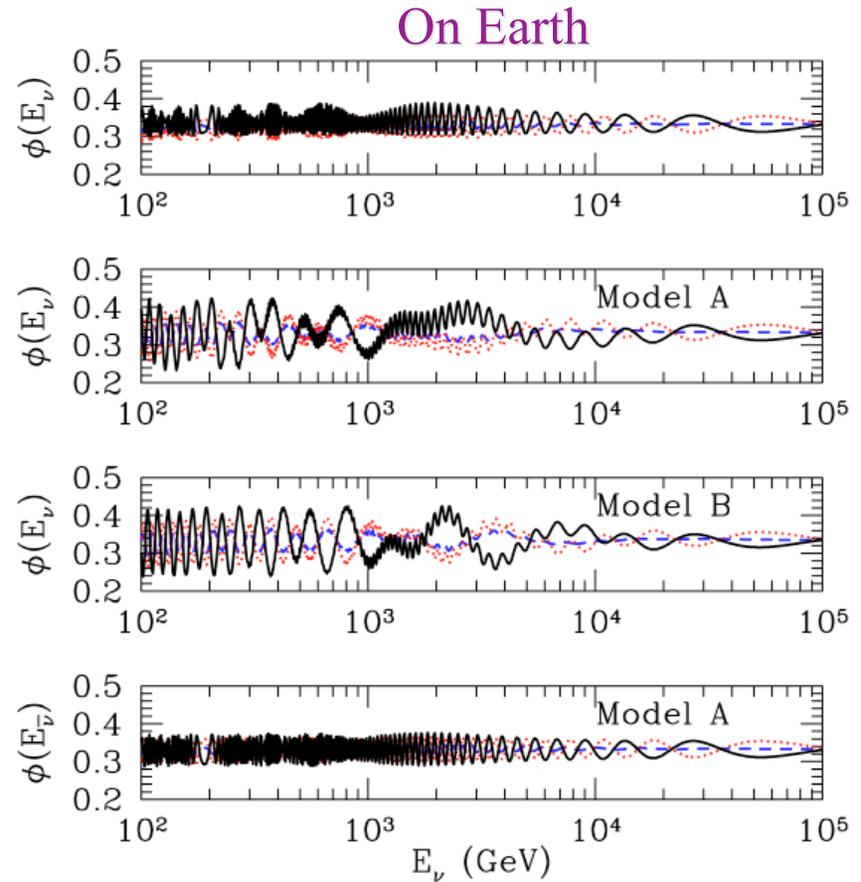
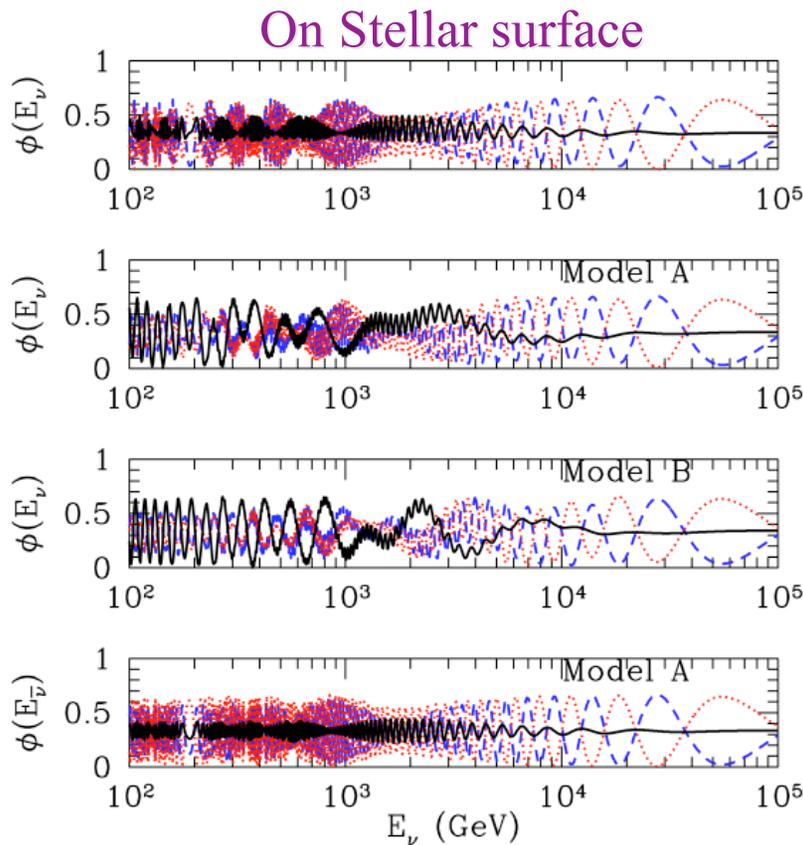
$$i \frac{d}{dr} |\nu_\alpha\rangle = U H_m U^\dagger |\nu_\alpha\rangle$$

With different matter potentials

$$V_{e,CC} = \sqrt{2} G_F N_e$$

# Fluxes at Production and on Earth

Production ratios in the jet for both neutrinos and anti-neutrinos in the 100 GeV - 100 TeV range:  $\Phi_{\nu\mu} = 2\Phi_{\nu e}$



Solid black:  $\nu_e$   
 Dashed blue:  $\nu_\mu$   
 Dotted red:  $\nu_\tau$

# Probing Oscillation Effects in $\nu$ Telescopes

Calculate neutrino events in a km-scale water/ice Cherenkov detector

→ Neutrino “telescopes” can not distinguish between  $\nu_e$  and  $\nu_\tau$  at these energies

Construct an Observable

$$R = \frac{N_{\nu_e} + N_{\nu_\tau}}{N_{\nu_\mu}}$$

No matter effect:  $R = 2$

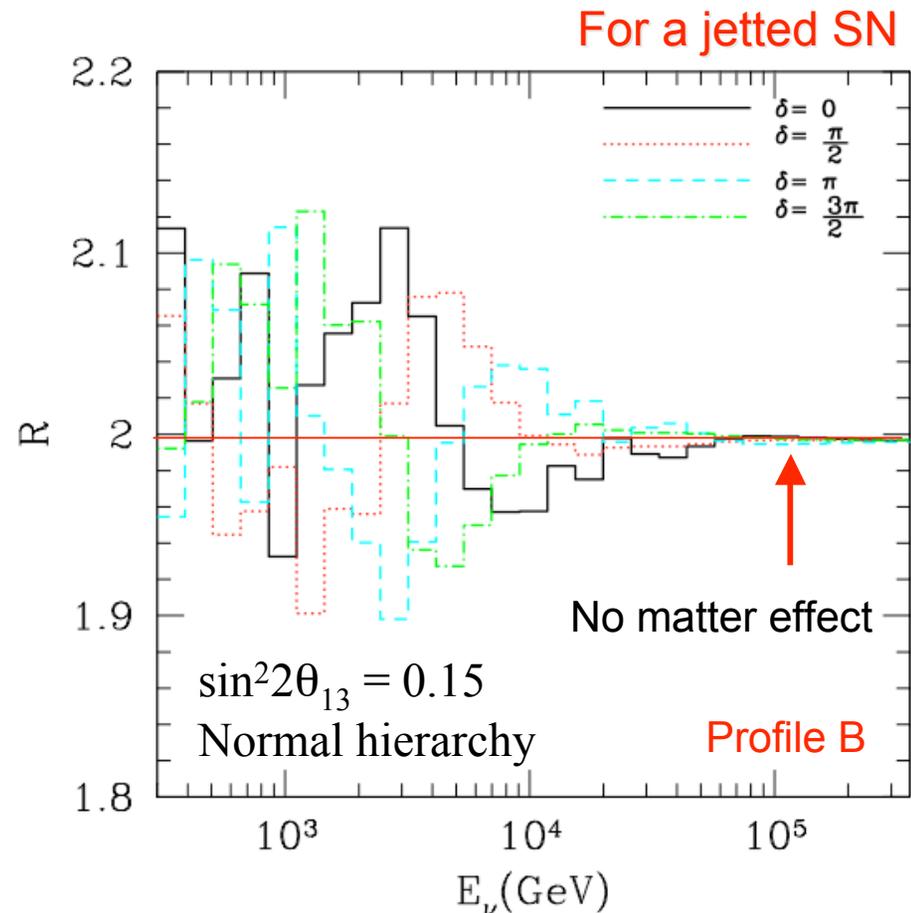
$R$  depends on the astrophysics

- Neutrino flux at production
- Density profile of the envelope

and on neutrino oscillation physics

- Mass hierarchy
- Oscillation parameters,  $\theta_{13}$

Small effect → high event rate from nearby jetted SN can help



# Summary

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Only neutrinos carry information from inside stars

High energy neutrinos can probe jetted SN/GRB models

- ❖ Observations of GRBs provide evidence of relativistic jet formation from massive stellar collapses, SN and GRBs are connected
- ❖ Supranova model can be constrained or ruled-out from neutrino telescope (such as IceCube) data
- ❖ Precursor neutrino from buried GRB jet can distinguish progenitor star model, better detection prospect than burst neutrinos
- ❖ Jetted SN or hypernova may constitute a new class of collapse
  - ➔ Can only be probed with high-energy neutrinos
  - ➔ Probe MSW effect for TeV neutrinos for the first time!

Not sure if SN/GRB science will lead to  $\nu$  technology though ...